

Q) color display - 8 bits of each primary color per pixel.
frame size - 1280×1024 .

(a) minimum size in bytes of the frame buffer to store a frame

Ans → 1 byte = 8 bits

∴ 3 colors, each using 8 bits = 1 byte.

∴ one pixel uses 3×1 bytes = 3 bytes.

∴ 3 colors and each color uses 1 byte. Also, the frame consists of

$$1280 \times 1024 = 1310720 \text{ pixels}$$

∴ (memory) size of the frame is

$$3 \times 1310720 = 3,932,160 \cancel{\text{pixels}} \text{ bytes.}$$

Finally, this means precisely that the minimum size of the frame buffer is $3,932,160$ bytes

Assn 18

3 colors, each using 10 bits

$$3 \times 10 \text{ bits} = 30 \text{ bits}$$

$$\text{frame } 3440 \times 1440 = 4,953,600 \text{ pixels}$$

∴ minimum size of frame is

$$30 \times 4,953,600 = 148,608,000 \text{ bits}$$

$$= [18,576,000 \text{ bytes}]$$

(b) how long would it take, at a minimum, for the frame to be sent over a 100Mbit/s?

$$1 \text{ Mbit/s} = 10^6 \text{ bit/s}, \text{ so speed is}$$

$$100 \text{ Mbit/s} = 100 \times 10^6 \text{ bit/s} = 10^8 \text{ bit/s}$$

(memory) size of the frame in bits is

$$3932160 \times 8 = 31457280 \text{ bit}$$

∴ speed = $\frac{\text{size}}{\text{time}}$ where size is the memory size of the object being sent

we have time = $\frac{\text{size}}{\text{speed}}$

$$= 31457280$$

10^8 bit/s

$$= [0.3145728]$$

Assn 1

(b) 400 Mbit/s

speed : $400 \times 10^6 \text{ bit/s} = 4 \times 10^8 \text{ bit/s}$

(assuming) size = 148608000 bits

$$\text{time} = \frac{148608000}{10^8 \times 4}$$

$$= \frac{3715200}{10^8 \times 10^5}$$

$$= [0.37152]$$

Assn 1

| | clock rate | CPI |
|----------------|------------|-----|
| P ₁ | : 4.4 GHz | 1.5 |
| P ₂ | : 3.3 GHz | 1.0 |
| P ₃ | : 4.1 GHz | 2.2 |

(a)

$$P_1 : 4.4 \text{ GHz} / 1.5 \Rightarrow = 2.93 \times 10^9 \text{ instruction per sec}$$

$$P_2 : 3.3 \text{ GHz} / 1 = 3.3 \times 10^9$$

$$P_3 : 4.1 \text{ GHz} / 2.2 = 1.86 \times 10^9$$

∴ P₂ has highest performance

(b) Cycles

P1: $4.4 \text{ GHz} \times 10 = 4.4 \times 10^9 \text{ cycles}$

P2: $3.3 \times 10 = 3.3 \times 10^9 \text{ cycles}$

P3: $4.1 \times 10 = 4.1 \times 10^9 \text{ cycles}$

Number of Instructions

P1: $4.4 \text{ GHz} * 10 / 1.5 = 2.93 \times 10^{10} \text{ instructions}$

P2: $3.3 \text{ GHz} * 10 / 1.0 = 3.3 \times 10^{10} \text{ instructions}$

P3: $4.1 \times 10 / 2.2 = 1.86 \times 10^{10} \text{ instructions}$

(c) Execution time = (num of instructions \times CPI) / clock rate

So, if we want to reduce execution time by 30%,

CPI increases by 20%, we have

$$\text{execution time} \times 0.7 = (\text{no. of ins} \times \text{CPI} \times 1.2) / \text{new clock rate}$$

$$\text{new clock rate} = \text{clock rate} \times \frac{1.2}{0.7}$$

$$4.4 \quad \text{new clock rate} = 1.7 \times \text{clock rate}$$

P1: ~~4.4 GHz \times 1.7~~ = ~~7.52 GHz~~ 7.524 GHz

P2: ~~3.3 GHz \times 1.7~~ = ~~5.643 GHz~~ 5.643 GHz

P3: ~~4.1 GHz \times 1.7~~ = ~~7.011 GHz~~ 7.011 GHz

Assn 1

| | clock rate | CPI | executing instruction |
|----|-------------|------|-------------------------------|
| QC | P1 4 GHz | 0.9 | 5×10^9 |
| | P2 3 GHz | 0.75 | $1.0 \times 10^9 \times 10^9$ |

$$\frac{P_{P1}}{P_{P2}} = \frac{ET_{P2}}{ET_{P1}} = \frac{(1 \times 10^9 \text{ instructions}) \times 0.75}{3 \times 10^9 \text{ cycles/instruction}}$$

$$= \frac{5 \times 10^9 \times 0.9}{4 \times 10^9} = \frac{0.75 \times 1}{5 \times 0.9} \times \frac{4}{3} = \frac{3}{13.5}$$

$\therefore P_1$ has less performance than P_2 hence it's not true for P_1 .

(b) $E_{TP1} = \frac{(IC_{P1} \times CPI_{P1})}{CR_{P1}}$
 $= 1.5 \times 10^9 \text{ instructions} \times 0.9 \text{ cycles/instruction}$
 $\quad \quad \quad 4 \times 10^9 \text{ cycles/sec}$

$= 0.225 \text{ s}$

$IC_{P2} = \frac{ET_{P2} \times CR_{P2}}{CPI_{P2}} = \frac{0.225 \times 3 \times 10^9}{0.75}$

$\Rightarrow 0.9 \times 10^9 \text{ instructions}$

need no. of instructions needed by P2 to execute in same time as P1

(c) MIPS = clock rate $\times 10^{-6}$ / CPI

$MIPS(P1) = 4 \times 10^9 \times 10^{-6} / 0.9 = 4.44 \times 10^3$

$P2 = 3 \times 10^9 \times 10^{-6} / 0.75 = 4 \times 10^3$

$MIPS(P1) > MIPS(P2)$ hence

\Rightarrow performance (P1) < performance (P2)

\therefore not true for P1 & P2

(d) MFLOPS = no. FP operations $\times 10^{-6}$ / ET

$MFLOPS(P1) = 0.4 \times 5 \times 10^9 \times 10^{-6} / 1.125 = 1.78 \times 10^3$

$(P2) = 0.4 \times 10^9 \times 10^{-6} / 0.25 = 1.6 \times 10^3$

$MFLOPS(P1) > MFLOPS(P2)$, Performance (P1) < performance (P2)

Hence not true for P1 and P2.

100 / time with overhead

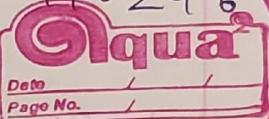
| Processors | Execution time / processors | Time with overhead | Speed up | Actual / ideal Speed up |
|------------|-----------------------------|--------------------|----------|-------------------------|
| 1 | 100s | (+4s) | 1.85 | 0.925 |
| 2 | 50s | 29 | 3.45 | 1.725 |
| 4 | 25s | 29 | 4.84 | 2.42 |
| 6 | 16.67 | 20.67 | 6.06 | 3.03 |
| 8 | 12.5 | 16.5 | 8.11 | 4.055 |
| 12 | 8.33 | 12.33 | 9.76 | 4.88 |
| 16 | 6.25 | 10.25 | 12.24 | 6.12 |
| 24 | 4.167 | 8.167 | 13.21 | 6.605 |
| 28 | 3.57 | 7.57 | 14.036 | 7.018 |
| 32 | 3.125 | 7.125 | 17.283 | 8.6415 |
| 56 | 1.786 | 5.786 | | |

QE //

Byteaddr

hex

| | | | | |
|-----|--------|--------|--------|--------|
| 64 | 1.5625 | 5.5625 | 17.978 | 8.989 |
| 224 | 0.446 | 4.446 | 22.492 | 11.246 |
| 448 | 0.223 | 4.223 | 23.68 | 11.84 |



~~QE~~

~~0x134433C~~ 0x-15EFBA4

Byteaddres

| | 0 | 1 | 2 | 3 - big |
|-----|-----------------------|---|---|---------|
| hex | 1 3 4 4 3 C | | | |
| | 2 | 1 | 0 | - low |

~~0x134433C~~ 0x-15EFBA4

| 3 | 0 | R | 1 | 2 | 3 | 0 - low |
|-------|-------|---------------|---|---|---|---------|
| - 1 | 5 E | F B A Y | | | | |
| 0 1 | 2 | 3 | | | | - big |

$$[E0F0] = (Ex08) + (01 \times 002) + (1 \times 2^2)$$

→ Linear Systems

Translate $0x134433C$ into decimal.

$$\begin{aligned}
 & \text{QF} \quad 134433C \\
 & \quad (4 \times 16^4) + (4 \times 16^3) + (3 \times 16^2) + (3 \times 16^1) + (C \times 16^0) \\
 & \quad + (3 \times 16^5) + (1 \times 16^6) \\
 & \Rightarrow [C = 12] \quad \Rightarrow \boxed{20,202,300}
 \end{aligned}$$

Q6) CPI = 0.1

- Arithmetic Instructions
- Load/Store
- Branch Instructions

| CPI | Instruction Breakdown |
|-----|-----------------------|
| 1 | 700 million |
| 10 | 200 million |
| 3 | 80 million |

$$\begin{aligned}
 & \cancel{(700)(1) + (200 \times 10) + (80 \times 3)} \times 10^6 \times (1.1 \times \text{clock cycle}) = \text{execute time} \\
 & \cancel{\text{It's not a good design choice because it increases the total execution time.}} \\
 & \cancel{(2672.72 \times 10^6) / \text{clock cycle}} = \text{execution time}
 \end{aligned}$$

i.e. increase means $100x + x = 101x$

* CPU time = clock cycles \times clock cycle time
new, no. of clock cycles in the beginning is (in millions);

$$\sum_{i=1}^3 \text{no. of instructions}_i \times \text{CPI}_i = 700 \times 1 + 200 \times 10 + 80 \times 3 \\
 = 2940$$

Therefore, the CPU time in the beginning is

$$\text{CPU time}_A = 2940 \times 10^6 \times \text{clock cycle time}_A$$

After decreasing the number of arithmetic instructions by 25%, we have $0.75 \times 700 = 525$ million arithmetic instructions.

The no. of clock cycles is now (in millions)

$$(525 \times 1) + (200 \times 10) + (80 \times 3) = \boxed{2765}$$

So, CPU time now is

$$\begin{aligned}
 \text{CPU time}_B &= 2765 \times 10^6 \times \text{clock cycle time}_B \\
 &= 2765 \times 10^6 \times 1.1 \times \text{clock cycle time}_A \\
 &= 3041.5 \times \text{clock cycle time}_A \times 10^6
 \end{aligned}$$

So CPU time

increase which is not good so not good design choice.

So CPU time now is,

$$CPU\ time_c = 2590 \times 10^6 \times \text{clock cycle time}$$

Since we do not change clock cycle time. Since

$$\frac{CPU\ time_c}{CPU\ time_{ref}} = \frac{2590}{2940} = 0.88095$$

this is an increase of only 6.58%.

now CPI of arithmetic instructions become 0.1. Thus the number of clock cycles is

$$(700 \times 0.1) + (200 \times 10) + (180 \times 3) = \underline{\underline{2310}}$$

So, CPU time now is

$$CPU\ time_p = 2590 \times 10^6 \times \text{clock cycle times}$$

$$\frac{CPU\ time_p}{CPU\ time_{ref}} = \frac{2590}{2940} \frac{2310}{2940} = 0.78571$$

Ass 1

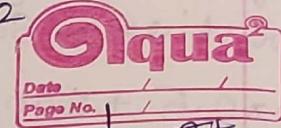
c) 10 bits for each color per pixel
• 3440x1440 frame size

transmit data at 144 frames per second.

$$\Rightarrow 10 \times 3440 \times 1440 \times 144 = 7133184000 \\ \text{bits frame} \quad \text{frame/seconds} \quad \text{bits/second}$$

= 7133.184 MB/s

Module 2 Unit 2 ASSN-02



Q1. $5ED4 - 07A4$

$$\begin{array}{r} 0101 \ 1110 \ 1101 \ 0100 \\ - 0000 \ 0111 \ 1010 \ 0100 \\ \hline 0101 \ 0111 \ 001 \ 10000 \end{array}$$

$$\begin{array}{r} 5 \quad 7 \quad 3 \quad 0 \\ \hline \end{array}$$

$$5ED4 - 07A4 = 5730$$

$$1 + 4 + 8 + 16$$

$$+ 2^2 + 2^4$$

$$2^3 + 2^5$$

=

$$8 + 4 + 8 + 32$$

$$+ 2^8 + 2^{10} + 2^4$$

$$2^{12} + 2^{14}$$

=

~~$$\begin{array}{r} A81F - 5D2E \\ 1010 \ 1000 \ 0001 \\ - 0101 \ 1101 \ 0010 \\ \hline 00 \ 0011 \ 0001 \end{array}$$~~

A81F - 5D2E

$$\begin{array}{r} 1010 \ 1000 \ 0001 \\ 0101 \ 1101 \ 0010 \\ \hline 1110 \end{array}$$

~~5D2E > A81F~~

so, the answer is going to be negative.

~~$$\begin{array}{r} 0101 \ 1101 \ 0010 \ 0001 \\ - 1010 \ 1000 \ 0001 \ 1111 \\ \hline 011 \ 0101 \ 0001 \ 1111 \end{array}$$~~

~~$$\begin{array}{r} 1010 \ 1000 \ 0001 \ 1111 \\ 0101 \ 1101 \ 0010 \ 1110 \\ \hline \end{array}$$~~

~~$$\begin{array}{r} 0 \ 2 \ 2 \ 2 \ 2 \ 2 \ 2 \\ 1010 \ 1000 \ 0001 \ 1111 \\ 0101 \ 1101 \ 0010 \ 1110 \\ \hline 0100 \ 1010 \ 1111 \ 0001 \\ 4 \quad 10=A \quad 15=F \quad 1 \end{array}$$~~

-0.75

-753

1004

$$3 \times \frac{1}{4}$$

$$\frac{3}{2} \times \left(\frac{1}{2}\right)$$

Subtract
to subtract
later or
the first

Subtraction of 2 signed binary numbers is similar to subtraction of 2 unsigned binary numbers but later on adding 2's complement of the first number.

Qlqua

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$$\frac{3}{2} \times \frac{1}{2} = \frac{3}{4}$$

$$\frac{2}{4}$$

$$\frac{13}{4}$$

$$\frac{25}{100}$$

$$\frac{3}{2} \times \frac{1}{2}$$

$$2^2 + 2^1 \\ 2^2 + \frac{1}{4} + \frac{1}{2} \\ \frac{1}{8} + \frac{1}{4} + \frac{1}{2}$$

$$1 + 2 + 4 = \frac{7}{8}$$

$$\frac{101}{100} - \frac{25}{100} = \frac{75}{100} = 0.75$$

$$1 +$$

$$0.75$$

$$1 \cdot 0101 \cdot 101$$

(5-7)

$$(-1) \times (1 + 101) \times 2 \\ = -1 \times (1 \cdot 25) \times 2^{\frac{1}{4}}$$

$$-1 \times \frac{5}{4} \times \frac{1}{4}$$

$$\frac{8}{16}$$

$$-0.75$$

$$-\frac{25}{100}$$

$$\left(-\frac{3}{4} \right)$$

$$(-1) \times (1 \cdot 1) \times 2^{\frac{-1}{2}}$$

$$3 \times \frac{1}{4} \times \frac{1}{2}$$

$$3 \times \frac{1}{4}$$

$$\frac{1}{2}$$

$$\frac{3}{2} \rightarrow 1.5$$

$$\frac{3}{2} \times \left(\frac{1}{2} \right)$$

$$x+y \quad x = 0 \begin{array}{l} 1001 \\ 0111 \end{array} \quad 010 \\ y = 0 \begin{array}{l} 0111 \\ 1110 \end{array} \quad A10$$

$$\boxed{x = 1 \cdot 010 \times 2} = 10 \quad (7-7)$$

$$y = (-1)^0 \times (1 \cdot 110) \times 2 \\ = 1 \times 1 \cdot 110 \times 1$$

$$\boxed{y = 1 \cdot 110}$$

$$x+y = 1 \cdot 010 \times 2 + 1 \cdot 110$$

~~10100
+110~~

~~= 101 + 1 \cdot 110~~

~~= +110110~~

~~101~~

~~1 \cdot 110~~

~~111 \cdot 110~~

~~= 1 \cdot 010 \times 2 + 0 \cdot 01110 \times 2^e~~

~~= 2^2 \times (1 \cdot 010 + 0 \cdot 0111)~~

~~1 \cdot 010
+0 \cdot 011
1 \cdot 101~~

~~= 1 \cdot 101 \times 2^2~~

~~Ex. 110 = 6~~

$$101 \cdot 000$$

$$-1 \cdot 110$$

$$\underline{110 \cdot 1 \cdot 10}$$

$$-4+2+0 \cdot 0 \cdot 5+0 \cdot 25$$

$$A = a \ b c d e \ f g h$$

$$(-1)^a \times 1 \cdot f g h \times 2^b$$

$$6 \cdot 75$$

(c-1)

$$A = 1 \begin{array}{l} 0101 \\ 01 \end{array} \quad 101$$

$$B = 0 \begin{array}{l} 0011 \\ 01 \end{array} \quad 001$$

$$B = (-1)^0 \times 1 \cdot 001 \times 2^{(3-7)}$$

$$= \boxed{1 \cdot 001 \times 2^{-4}} = 0 \cdot 0001001$$

$$A = (-1)^1 \times 1 \cdot 101 \times 2^{(5-7)}$$

$$= \boxed{-1 \cdot 101 \times 2^{-2}} - (-0 \cdot 01101)$$

$A + B$

$$\begin{array}{r} 0.000 \times 2^2 \\ + (-0.0110101) \\ \hline 0101 \end{array}$$

~~-1 4 ADSP~~~~-A~~

$$\begin{array}{r} 0.202 \times 2^1 \\ - 0.01 \times 2^0 \\ + 0.0001001 \end{array}$$

$$A + B = -0.010101011$$

$$1.011 \times 2^2$$

$$1,01010101$$

$$\frac{1}{7} + \frac{1}{8} + \frac{1}{16} + \frac{1}{32} + \frac{1}{64} = \frac{1}{128}$$

$$0.00010101$$

$$0.000101 \times 2$$

$$0.00010101$$

$$0.00010101$$

$$0.00010101$$

$$0.00010101$$

 $A - B$

$$- 0.0110100$$

$$- 0.0001001$$

$$1.111 = (-0.00011101)$$

$$1.0101111$$

$$A^*B = 1.001 \times 2^{-4} \times -1.101 \times 2^{-2}$$

$$= 1.001 \times -1.101 \times 2^{-6}$$

$$1.001 \times -1.101 \times 2^{-6}$$

$$1.0001110$$

$$\begin{array}{r} 1.001 \\ + 1.01 \\ \hline 1.0101 \end{array}$$

$$\begin{array}{r} 0001001 \\ 000000 \\ 110011 \\ 1001xx \\ \hline 101010101 \end{array}$$

$$A/B = \frac{1.001}{1.101} \times 2^{2-4}$$

$$\begin{array}{r} 1.001 \\ - 1.001 \\ \hline 010000 \end{array}$$

$$\begin{array}{r} 1.101 \times 2^{-2+4} \\ - 1.001 \times 2^{-4} \\ \hline 1.101 \times 2^2 \\ - 1.001 \end{array}$$

$$\begin{array}{r}
 1.0111001 \times 2^5 \\
 1001 \quad 1101 \\
 1001 \\
 \hline
 100000 \\
 -1001 \\
 \hline
 10010
 \end{array}$$

01110

1001

1010

1001

01000

$$\frac{A}{B} = 1.0111001 \times 2^2$$

$$\boxed{1 \ 001 \ 0100 \ 011} \quad \begin{matrix} 2+7 \\ = 9 \end{matrix}$$

$$5ED4 = 0101 \ 1110 \ 1101 \ 0100$$

$$07A4 = 0000 \ 0111 \ 1010 \ 0100$$

$$\begin{array}{cccc}
 0 & 101 & 0111 & 0011 \ 0000 \\
 & 5 & 7 & 3 & 0
 \end{array}$$

for signed, the first digit is 0, thus +ve,
and so the answer for signed will also be
5730.

bit pattern ~~0.11000000~~ then

0000 0 C=12 000000

0000 1100 0000 0000 0000 0000 0000 00

↓
0001100000 sign 0

exponent 0001100000-021

mantissa 00000000000000000000000000000000

0 1100 000

(-1)⁰ x 1.000 x 2²⁺⁷

1.000 x 2⁵

1.000 00.0

~~→ 0 0001 1000 0000 0000 0000 0000 0000~~

positive
sign

~~$00011000 = 24$~~

 ~~$00000000000000000000000000 = 0$~~

~~$(-1) \times 1.0 \times 2$~~

Assn 2

~~$\rightarrow 0 \times 0000000$~~

~~0000 1100 0000 0000 00000000 0000 0000~~
~~~ 1111 0011 1111 1111 1111 1111 1111 1111~~

adding 1

~~3) 0 11110100000000000000000000000000~~
~~2 29 + 2<sup>28</sup> + 2<sup>26</sup> = 4,093,640,960~~
 ~~$\ominus = [+201326592]$~~ 

2's complement

268B300C

0010 0100 001000 1001 0011 0000 0000 1100  
 1101 1011 0111 0100 1100 1111 1111 0011  
 r 101 1011 0111 0100 1100 1111 1111 0100

|     |           |
|-----|-----------|
| 000 | 11111001  |
| =   | 11111010  |
|     | 00000000  |
| 0 0 | 11001X XX |
| 1 1 | 11001X XX |
| 1 1 | 1001XX XX |
| 1 1 | 001XXX XX |
| 1 1 | 01XXXX XX |
| 1 1 | 1X**X* X* |
| 1 1 | 00101010  |

# Q Assn 2 F

31.625 to binary

31 to binary 11111

0.625 to binary

$$0.625 \times 2 = 1.25 \quad 1 + 0.25$$

$$0.25 \times 2 = 0.5 \quad 0 + 0.5$$

$$0.5 \times 2 = 1.0 \quad 1$$

$$\underline{0.101}$$

$$(31.25)_{10} = (11111.101)_2$$
$$= 11111.101 \times 2^0$$
$$= 1.111101 \times 2^4$$

Sign = 0 (positive no.)

Exponent = 4 (unadjusted).

Mantissa = .1.111101

$$\text{Exponent (adjusted)} = 4 + 2 - 1$$

$$= 4 + 127$$

$$= (131)_{10}$$

$$= (10000011)_2$$

Mantissa = 11111010000000000000000000000000

(normalized)

28 bits

$\Rightarrow [0 \boxed{10000011}]11111010000000000000000000$

$\$a_0 \rightarrow \text{matrix } A$   
 $\$a_1 \rightarrow \text{matrix } B$   
 $\$a_2 \rightarrow \text{size} = 4$   
 $\$a_2 \rightarrow \text{matrix } C$

$\$t0 = i$

$\$t1 = j$

~~$\$t2 = \text{size} * 4$~~   
 $= \$a2 * 4$

~~$\$t3 = 4 \times 16$~~

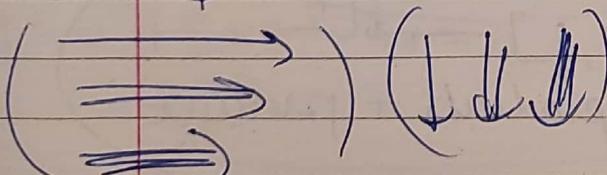
~~$\$t4 = 4 \times 4$~~

~~address  $\$t5 = \$tB + \$t4$~~

~~$\$t5 = \$t5 + \$a0$~~

~~$\$t6 = (\$t5 * 4) + \$a1$~~

~~$\$t7 = (\$a0, (\$t5) + (\$a1, (\$t6))$~~

 ~~$\$t2$~~ 


$(a_{11} \times a_{11}) + (a_{12} \times a_{21})$

$+ (a_{13} \times a_{31})$

$i=1$

while ( ~~$j \neq 3$~~   $j \leq 3$ )

$\text{addition} = i * (4 \times 4) + j \times 4$

~~$\$t0 = [ (i \times 4) + j ] \times 4$~~

~~+ base address~~

$\text{Sum} = A[i, j] + B[i, j]$

$\$t5 = \$t0 \times \$a2$

$\$t5 = \$t5 + \$t1$

$\$t5 = \$t5 \times 4$

$\$t6 = \$t5 + \$a0$

$\$t7 = \$t5 + \$a1$

$\$t8 = \$t5 + \$a2$

~~$\$t9 = \$t5 + \$a2$~~

~~sum~~

matrix multiplication

~~white~~ { int product = 0;

for( i=0; i<4; i++)

for( j=0; j<4; j++)

{ A[i,j] \* B[j,i] = product;

product = product +  
product += ; → \$VI

\$t0 = i

\$t1 = j

\$a0 → matrix A

\$a1 → matrix B

\$AB → size

$$A[i,j] = [(i * \text{size}) + j] * 4$$

$$B[j,i] = [(j * \text{size}) + i] * 4$$

loop:

j < 4 ←

i = 0

A[i,j] → \$t6

B[i,j] → \$t7

$$\text{product} = A[i,j] * B[i,j] → \$t2$$

sum of products = sum of products + product

j++

i++

$$\begin{pmatrix} 2 & 1 & 9 & 2 \\ 7 & 9 & 10 & 10 \\ 3 & 4 & 3 & 4 \\ 2 & 5 & 4 & 6 \end{pmatrix} \begin{pmatrix} 8 & 7 & 1 & 2 \\ 2 & 7 & 3 & 6 \\ 7 & 5 & 6 & 8 \\ 9 & 4 & 8 & 9 \end{pmatrix}$$

Transpose

$$A[i,j] = A'[j,i].$$

$$\begin{bmatrix} 1 & 4 & 7 \\ 2 & 5 & 8 \\ 3 & 6 & 9 \end{bmatrix}$$

A

$$\begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{bmatrix}$$

A'

1 2 3 4  
 ↴ 5 6 7 8  
 ↴ n n n n

\$t9 → index  
 through  
 matrix C.

columncount → \$t2  
 rowcount → \$t3

t

(t3, t1)

↓  
t0

$$\left( \begin{array}{cccc} 1 & 2 & 3 & 4 \\ 5 & 6 & 7 & 8 \\ 1 & 1 & 1 & 1 \\ \dots & \dots & \dots & \dots \end{array} \right)$$

$$\left( \begin{array}{cccc} 1 & 2 & 3 & 4 \\ 5 & 6 & 7 & 8 \\ 1 & 1 & 1 & 1 \\ \dots & \dots & \dots & \dots \end{array} \right)$$

(t0, t1)

(t3, t1)

t0=0 → t0=1

t3=0 t1=0, 1, 2, 3, 4 (t0, t1) x (t3, t1)

t0=0

t3=1

t1=0

t=0, 1, 2, 3, 4

t0=0

t3=2

1

;

:

t3=4

$$\begin{array}{c|c|c}
 16+2+63+18 & 14+7+4+8 & 2+3+54+16 \\
 56+18+70+90 & 49+63+50+40 & 7+27+60 \\
 24+8+21+36 & 21+28+15+16 & +80 \\
 16+10+28+54 & 14+35+20+24 & 3+12+18+32 \\
 \hline
 4+6+72+18 & & 2+15+24+48 \\
 14+54+80+90 & & \\
 6+24+24+36 & & \\
 \hline
 4+30+32+54 & &
 \end{array}$$

→ Linear Systems

| Address | Cache Block | (A/32) % 32 | (A/32) / 32 | address to tag | Aqua Data Page No. |
|---------|-------------|-------------|-------------|----------------|--------------------|
| 0       | 00000       | 00000       | 00000       | 0              | 0-31 min           |
| 4       | 00000       | 00000       | 00000       | 0              | 0-31 hit           |
| 16      | 00000       | 00000       | 00000       | 0              | 0-31 hit           |
| 132     | 00100       | 00000       | 00000       | 4              | 128-159            |
| 232     | 00011       | 00000       | 00000       | 7              | 200-255            |
| 160     | 00101       | 00000       | 00001       | 5              | 160-191            |
| 1024    | 00000       | 00000       | 00000       | 32             | 1024-1055          |
| 30      | 00000       | 00000       | B/32        | 0              | 0-31               |
| 140     | 00100       | 00000       | 00000       | 4              | 128-159 hit        |
| A[3100] | 00000       | 00000       | 0011        | 96             | 3072-3103          |
| +808    | 00101       | 00000       | 00000       | 5              | 160-191            |
| B[2180] | 00100       | 00000       | 0010        | 68             | 2176-2207          |

Cache Block



$$\begin{array}{r} 32 \\ | \\ 32 \end{array} \begin{array}{r} 132 \\ | \\ 128 \\ | \\ 9 \end{array} \boxed{\begin{array}{r} 4 \\ | \\ 4 \end{array} 32}$$

$$\begin{array}{r} 32 \\ | \\ 32 \end{array} \begin{array}{r} 232 \\ | \\ 224 \\ | \\ 8 \end{array} \boxed{7} 32$$

$$\begin{array}{r} 32 \\ | \\ 32 \end{array} \begin{array}{r} 160 \\ | \\ 16 \\ | \\ 0 \end{array} \boxed{5} 32$$

$$\begin{array}{r} 32 \\ | \\ 32 \end{array} \begin{array}{r} 1024 \\ | \\ 96 \\ | \\ 64 \\ | \\ 64 \end{array} \boxed{4} 32$$

$$\begin{array}{r} 32 \\ | \\ 32 \end{array} \begin{array}{r} 140 \\ | \\ 128 \end{array} \boxed{7} 32$$

$$\begin{array}{r} 32 \\ | \\ 32 \end{array} \begin{array}{r} 3100 \\ | \\ 288 \\ | \\ 220 \\ | \\ 20 \end{array} \boxed{96} 32$$

$$\begin{array}{r} 32 \\ | \\ 32 \end{array} \begin{array}{r} 96 \\ | \\ 32 \\ | \\ 0 \end{array} \boxed{3} 32$$

$$\begin{array}{r} 32 \\ | \\ 32 \end{array} \begin{array}{r} 180 \\ | \\ 160 \\ | \\ 20 \end{array} \boxed{6} 32$$

$$\begin{array}{r} 32 \\ | \\ 32 \end{array} \begin{array}{r} 2180 \\ | \\ 192 \\ | \\ 260 \\ | \\ 256 \\ | \\ 4 \end{array} \boxed{68} 32$$

$$\begin{array}{r} 32 \\ | \\ 32 \end{array} \begin{array}{r} 68 \\ | \\ 64 \\ | \\ 4 \end{array} \boxed{2} 32$$

$$\begin{array}{r} 32 \\ | \\ 32 \end{array} \begin{array}{r} 96 \\ | \\ 32 \\ | \\ 0 \end{array} \boxed{48} 32$$

$$\begin{array}{r} 32 \\ | \\ 32 \end{array} \begin{array}{r} 128 \\ | \\ 64 \\ | \\ 32 \\ | \\ 16 \\ | \\ 8 \\ | \\ 4 \end{array} \boxed{128} 32$$

Address

Index

3505

01101

0011

109

miss

32

185

00101

0000

5

not hit

64

869

11011

0000

27

miss

96

7041

11100

0110

220

miss

32

$$\begin{array}{r} 109 \\ 32 \overline{) 3505} \\ 32 \\ \hline 305 \\ 288 \\ \hline 13 \end{array}$$

$$\begin{array}{r} 93 \\ 32 \overline{) 109} \\ 96 \\ \hline 13 \end{array}$$

$$\begin{array}{r} 185 \quad 5 \\ 32 \overline{) 160} \\ 160 \\ \hline 25 \end{array}$$

$$\begin{array}{r} 869 \quad 27 \\ 32 \overline{) 229} \\ 229 \\ \hline 3 \end{array}$$

$$\begin{array}{r} 220 \\ 32 \overline{) 7041} \\ 64 \\ 64 \\ \hline 01 \end{array}$$

$$\begin{array}{r} 92 \\ 32 \overline{) 192} \\ 192 \\ \hline 28 \end{array}$$

$$\begin{array}{r} 288 \\ 32 \overline{) 256} \\ 256 \\ \hline 288 \end{array}$$

$$\begin{array}{r} 320 \\ 352 \end{array}$$

|     | Index | Offset |          |
|-----|-------|--------|----------|
| 22  | 0     | 00000  | 32 miss  |
| 128 | 4     | 00000  | hit      |
| 84  | 16    | 168432 | hit      |
| 132 | 00100 | 00100  | miss     |
| 128 | 232   | 00111  | hit miss |
| 64  |       |        |          |
| 32  |       |        |          |
| 84  |       |        |          |
| 132 |       |        |          |
| 232 |       |        |          |

$$\begin{array}{r} 128 \\ 32 \\ 160 \end{array}$$

$$\begin{array}{r} 136 \\ 4 \\ 140 \end{array}$$

1029

1029

2048

256

1028

2432

2432

2464

128

118

256

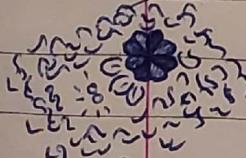
214

16

2480

1624

2464



(6) (b) A

$$1 \ 1100 \ 010 - 1 \ 1001 \ 011$$

$$A = 1 \underset{842}{\cancel{1100}} \underset{12}{\cancel{0102}}$$

$$\begin{aligned} &= (-1)^1 \times 1 \cdot 010 \times 2^5 \\ &= -1 \cdot 010 \times 2^5 \\ &= -101000 \end{aligned}$$

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Date \_\_\_\_\_  
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$$B = 1 \ 1001 \ 011 \ 9-7$$

$$\begin{aligned} &= (-1)^1 \times 1 \cdot 011 \times 2^2 \\ &= -1 \cdot 011 \times 2^2 \\ &= -101 \cdot 1 \end{aligned}$$

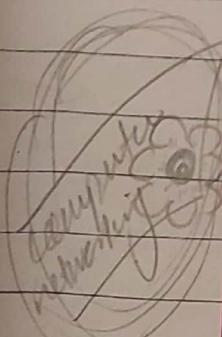
A - B

$$\begin{aligned} &-101000 \cdot 0 - (-101 \cdot 1) \\ &-101000 \cdot 0 + 101 \cdot 1 \\ &-101000 \cdot 0 + 101 \cdot 1 \\ &\underline{-100000 \cdot 1} \end{aligned}$$

$$\begin{array}{r} \textcircled{\text{b}} \ 100000 \cdot 1 \\ \hline 1 \quad +5 \quad +9 \quad = 12 \end{array}$$



$$\boxed{1 \ 1100 \ 001}$$



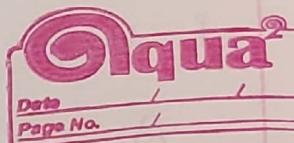
C#, Java, SQL,  
Python,

4400  
1400

→ Linear Systems

$$@ \text{a} \quad 0 \cdot 1100 \ 001 + 0 \begin{smallmatrix} 1 & 0 & 1 & 1 \\ 8 & 2 & 1 & 1 \end{smallmatrix}$$

$$\begin{aligned} A &= 0 \begin{smallmatrix} 1 & 1 & 0 & 0 & 0 & 0 & 1 \end{smallmatrix} \\ &= (-1) \times 1 \cdot 001 \times 2^{12-7} \\ &= 1 \cdot 001 \times 2^5 \\ &= 100100 \end{aligned}$$



$$\begin{aligned} B &= (-1) \begin{smallmatrix} 0 \\ \times 1 \cdot 010 \times 2 \end{smallmatrix} \\ &= 1 \cdot 010 \times 2^4 \\ &= 10100 \end{aligned}$$

$$\begin{array}{r} 100100 \\ 10100 \\ \hline + 10000 \\ \hline + 5 + 7 = 12 \end{array}$$

$$= 1 \cdot 110$$

$$\boxed{D \ 1100 \ 110}$$

$$@ \text{c} \quad 1 \ 0011 \ 100 * 0 \ 1100 \ 010$$

$$\begin{aligned} A &= 1 \begin{smallmatrix} 0 & 0 & 1 & 1 \\ 1 & 0 & 0 \end{smallmatrix} 100 \\ &= (-1) \times 1 \cdot 100 \times 2^{3-7} \\ &= -1 \cdot 100 \times 2^{-4} \\ &= -0.00011 \end{aligned}$$

$$\begin{aligned} B &= 0 \begin{smallmatrix} 8 & 4 \\ 1 & 1 & 0 & 0 \end{smallmatrix} 010 \oplus \begin{smallmatrix} 1 & 2 & -7 \end{smallmatrix} \\ &= (-1) \times 1 \cdot 010 \times 2^{12-7} \\ &= 1 \cdot 010 \times 2^5 \end{aligned}$$

$$\begin{aligned} &-1 \cdot 100 \times 2^{-4} \times 1 \cdot 010 \times 2^5 \\ &= -1 \cdot 100 \times 1 \cdot 010 \times 2^{-4+5} \end{aligned}$$

$$= -1.100 \times 1.01 \otimes \times 2$$

**Supco**

1.100  
+ 1.010

$$\begin{array}{r}
 0000000000 \\
 0011000000 \\
 0000000000 \\
 1100000000 \\
 \hline
 1.11110000
 \end{array}$$

8-7

**Oqua**  
Date / /  
Page No. / /

$$1.1111 \times 2^{\circ}$$

$$1+7 = 8$$

~~0000000~~

$$\boxed{0 \ 1000 \ 111}$$

(d)  $01011011 / 00111011$

$$\begin{array}{c|c}
 A = 0 \overset{8-2}{\cancel{1}} 0111011 & B = H \times 1.0111 \times 2^{\circ} \\
 = (-1) \times 1.0111 \times 2^{\circ} & = 1.0111 \times 2^{\circ} \\
 = 1.0111 \times 2^{\circ} & \\
 \hline
 1.0111 \times 2^{\circ} & 2^{\circ} \times 1.000 \\
 \hline
 1.0111 \times 2^{\circ} & 4+7 = 11
 \end{array}$$

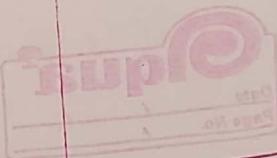
$$\boxed{010111000}$$

(e)  $01100001 \quad 12-7$   
 $(-1) \times 1.001 \times 2$

$$\begin{aligned}
 &= 1.001 \times 2^5 \\
 &= 100100
 \end{aligned}$$

Ans: 36

-0.25  
↑  
binary point  
floating point  
number



Q6 (a)  $0 \ 1100 \ 001 + 0 \ 1011 \ 010$

$$A = 0 \ \overbrace{1100}^{12} \ 001 \quad (12-7)$$

$$= (-1)^0 \times 1 \cdot 001 \times 2$$

$$= 1 \cdot 001 \times 2^5$$

$$= 100100$$

$$B = 0 \ \overbrace{1011}^{11} \ 010 \quad (11-7)$$

$$= (-1)^1 \times 1 \cdot 010 \times 2$$

$$= 1 \cdot 010 \times 2^4$$

$$= 10100$$

$$\begin{array}{r} A+B = 100100 \cdot 0 \\ \quad 10100 \cdot 0 \\ \hline 11000 \cdot 0 \\ \quad \quad \quad +5 \end{array}$$

$$+5 + 7 = 12$$

$$11000 \cdot 0 \times 2^5 = 1 \cdot 1100$$

$A+B = 0 \ 1100 \ 110$

$$(b) \quad (1 \ 1100 \ 010) - (1 \ 1001 \ 011)$$

$$\begin{aligned} A &= 1 \ 1100 \ 010 \quad (1,2-7) \\ &= (-1)^1 \times 1 \cdot 010 \times 2^2 \\ &= -1 \cdot 010 \times 2^5 \\ &= -101000 \cdot 0 \end{aligned}$$

$$\begin{aligned} B &= 1 \ 1001 \ 011 \quad (9-7) \\ &= (-1)^1 \times 1 \cdot 011 \times 2^2 \\ &= -1 \cdot 011 \times 2^5 \\ &= -101 \cdot 1 \end{aligned}$$

$$\begin{aligned} A-B &= -101000 \cdot 0 - (-101 \cdot 1) \\ &= -101000 + 101 \cdot 10 \end{aligned}$$

$$\begin{array}{r} 0 \ x \ 1 \ x \ 1 \\ - 10 \ x \ 0 \ x \ 0 \ x \ 0 \cdot 0 \\ \hline + 101 \cdot 1 \\ \hline - 1000 \ 10 \cdot 1 \end{array} \quad \text{+5}$$

$$+5+7=12 \quad A-B = -1 \cdot 001 \times \frac{+5}{2}$$

$$\boxed{A-B = 1 \ 1100 \ 001}$$

add \$50, \$10, \$7

sub \$12, \$50, \$13

beq \$12, \$3, LBL ~~three equal~~

add \$54, \$12, 1

LBL:

mul \$54 \$12 2

|       | IF | ID | EX | mem | WB |
|-------|----|----|----|-----|----|
| case1 | 20 | 15 | 20 | 20  | 15 |
| case2 | 25 | 5  | 30 | 10  | 20 |

(a) ET?

(b) barnds, MEny ET?

case1 | 1 2 3 4 5 6 7 8 9

add1 IF ID EX mem WB

sub IF ID EX mem WB

beq IF ID EX mem WB

add2 IF ID EX mem WB

20 20 20 20 20 20 20 15

total time = 155

case2 | 25 25 30 30 30 30 20 20 1210

50  
120  
220  
250  
280  
300

$$5.6105453 \cdot 10^{-6} = 12.375 \times 10^{-6}$$

$$0 \quad \begin{array}{r} 1000000 \\ \hline 1000000 \end{array} - (\epsilon - \text{bias})$$

$$(-1)^0 \times 1.0 \times 2 - (1.0 - 1.0)$$

$$(-1)^0 \times 1.0 \times 2^2 - (1.0 - 1.0)$$

~~0.001823~~

$$+ 1.523 \times 2^{-3}$$

~~+ 0.125~~

$$1. \begin{array}{r} 1000011 \\ - 123456 \\ \hline \end{array} \times 2^{-2}$$

$$1 + 2^1 \cdot \left( \frac{1}{2} + \frac{1}{2^6} + \frac{1}{2^7} \right)$$

~~2^7 / 2^6~~

~~2^7 / 2^6~~

$$2^1 + 2^6 + 2^{-2}$$

$$+ 12.375$$

$S=0 \rightarrow 12 \text{ to binary}$

$$\begin{array}{r} 12/2 = 6 \quad |0 \\ 6/2 = 3 \quad |0 \uparrow \\ 3/2 = 1 \quad |1 \\ 1/2 = 0 \quad ||1 \end{array}$$

~~2^7 / 2^6~~

$$12 \rightarrow 00011 (1100)_2$$

0.375 to binary

$$0.375 \times 2 = 0.750$$

$$0.75 \times 2 = 1.50$$

$$0.5 \times 2 = 1.00$$

$$0 \quad 1 \quad 0 \quad 1 \quad 0 \quad 0 \quad 1 \quad 1 \quad - (0.011)_2$$

$$(12.375)_0 = (1100.011)_2$$

make 1 non zero digit to left  
of decimal point

$$1.100011 \times 2^{(3) \text{ exp}}$$

S → 0

$$E \rightarrow 3 \rightarrow \text{add bias } 127 \quad 3 + 127 = 130 \quad \text{- convert to binary}$$

$E = (1000\ 0010)_2$

F → mantissa

remove  
the 1 before  
decimal pt

$100011 \rightarrow$  make it 23 bits by adding 0 to  
eight

$$F = 1000110000000000000000000$$

$$\textcircled{1} \quad (-1)^0 \times 1.100011 \times 2^{-(130 - 127)}$$

$$\boxed{(-1)^0 \times 1.100011 \times 2^{-3}} \\ + 1.100011 \times 2^{-3}$$