Codebook- Team Far_Behind IIT Delhi, India

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| J | 5.1 BlockCut Tree | | 1. | .1 Template | |
| | 5.2 Bridges Online | | # i | <pre>include <bits stdc++.h=""></bits></pre> | |
| | 5.3 HLD | | # i | <pre>include <ext assoc_container.hpp="" pb_ds=""> sing namespacegnu_pbds;</ext></pre> | |
| | 5.5 TED | | us | sing namespacegnu_pods; sing namespace std; | |

```
template < class T > ostream & operator < < (ostream & os, ←
                                                                    while (!('0' \le c \&\& c \le '9')) c = \leftarrow
                                                                        getchar_unlocked();
   vector<T> V) {
                                                                    while ('0' <= c && c <= '9')
 os << "[ "; for(auto v : V) os << v << " "; return \leftrightarrow
    os << "]'";}
                                                                         n = n * 10 + c - '0', c = getchar_unlocked();
template < class L, class R> ostream& operator << (\leftarrow
                                                                    return n;
   ostream &os, pair < L, R > P) {
                                                               inline void write(ll a){
  return os << "¯(" << P.first << "," << P.second << "↔
                                                                    register char c; char snum[20]; 11 i=0;
)";}
#define TRACE
#ifdef TRACE
                                                                         snum[i++]=a%10+48;
#define trace(...) __f(#__VA_ARGS__, __VA_ARGS__)
                                                                         a=a/10;
template <typename Arg1>
void __f(const char* name, Arg1&& arg1){
                                                                    while(a!=0); i--;
  cout << name << " : " << arg1 << std::endl;</pre>
                                                                    while (i \ge 0)
                                                                         putchar_unlocked(snum[i--]);
template <typename Arg1, typename... Args>
                                                                    putchar_unlocked('\n');
void __f(const char* names, Arg1&& arg1, Args&&... ←
   args){
                                                                using getline, use cin.ignore()
  const char* comma = strchr(names + 1, ',');cout.←
  write(names, comma - names) << " : " << arg1<<" ←</pre>
                                                                // gp_hash_table
                                                                #include <ext/pb_ds/assoc_container.hpp>
     ";__f(comma+1, args...);
                                                                using namespace __gnu_pbds;
                                                                gp_hash_table < int, int > table; //cc_hash_table can \leftarrow
#else
#define trace(...) 1
                                                                also be used //custom hash function
#endif
#define 11 long long
                                                                const int RANDOM = chrono::high_resolution_clock::now←
                                                                   ().time_since_epoch().count();
#define ld long double
                                                                struct chash {
#define vll vector<11>
#define pll pair<11,11>
                                                                    int operator()(int x) { return hash<int>{}(x ^{\sim}
                                                                       RANDOM); }
#define vpll vector<pll>
#define I insert
#define pb push_back
                                                                gp_hash_table<int, int, chash> table;
#define F first
#define S second
#define all(x) x.begin(),x.end()
                                                                //custom hash function for pair
                                                                struct chash {
                                                                    int operator()(pair<int,int> x) const { return x.←
#define endl "\n"
                                                                       first* 31 + x.second; }
// const ll MAX=1e6+5;
                                                                };
// random
// int mod=1e9+7;
inline int mul(int a,int b){return (a*111*b)%mod;}
                                                                mt19937 rng(chrono::steady_clock::now().←
inline int add(int a,int b){a+=b;if(a>=mod)a-=mod; ←
                                                                   time_since_epoch().count());
   return a;}
                                                                uniform_int_distribution < int > uid(1,r);
inline int sub(int a,int b)\{a-b; if(a<0)a+mod; return \leftarrow a, int b\}
                                                                int x=uid(rng);
inline int power(int a, int b){int rt=1; while(b>0){if(\leftarrow
                                                                //mt19937_64 rng(chrono::steady_clock::now(). ←
   b&1)rt=mul(rt,a);a=mul(a,a);b>>=1;}return rt;}
                                                                   time_since_epoch().count());
                                                                 // - for 64 bit unsigned numbers
inline int inv(int a){return power(a,mod-2);}
inline void modadd(int &a,int b){a+=b;if(a>=mod)a-=←
                                                                vector<int> per(N);
   mod;}
                                                                for (int i = 0; i < N; i++)
int main(){
                                                                    per[i] = i;
  ios_base::sync_with_stdio(false);cin.tie(0);cout.←
                                                                shuffle(per.begin(), per.end(), rng);
     tie(0);cout<<setprecision(25);
                                                                // string splitting
                                                                // this splitting is better than custom function(w.r.\leftarrow
// clock
                                                                   t time)
clock_t clk = clock();
                                                                string line = "Ge";
clk = clock() - clk;
                                                                vector <string> tokens;
((ld)clk)/CLOCKS_PER_SEC
                                                                stringstream check1(line);
// fastio
                                                                string ele;
inline ll read() {
                                                                // Tokenizing w.r.t. space ' '
    11 n = 0; char c = getchar_unlocked();
```

```
while(getline(check1, ele, ''))
tokens.push_back(ele);
```

1.2 C++ Sublime Build

2 Data Structures

2.1 Fenwick

```
/*All indices are 1 indexed*/
/*Range update and point query: maintain BIT of \hookleftarrow
   prefix sum of updates
  to add val in range [a,b] add val at a and -val at \hookleftarrow
  value[a]=BITsum(a)+arr[a] where arr is constant*/
/***Range update and range query: maintain 2 BITs B1 \hookleftarrow
**to add val in [a,b] add val at a and -val at b+1 in\leftrightarrow
    B1. Add val*(a-1) at a and -val*b at b+1
**sum[1,b] = B1sum(1,b)*b-B2sum(1,b)
**sum[a,b]=sum[1,b]-sum[1,a-1]*/
ll n;
11 fen[MAX_N];
void update(ll p,ll val){
  for(11 i = p; i \le n; i += i \& -i)
    fen[i] += val;
ll sum(ll p){
  11 \text{ ans} = 0;
  for(ll i = p;i;i -= i & -i)
    ans += fen[i];
  return ans;
```

2.2 2D-BIT

```
//point updates and range sum in a ractangle
```

```
//all indices are 1 indices. to increment value of \hookleftarrow
   cell (i,j) by val call update(x,y,val)
//to find sum of rectangle [a,b]-[c,d] find sum of \leftarrow
   rectangles [1,1]-[c,d],[1,1]-[c,b],
//[1,1][a,d] and [1,1]-[a,b] and use inclusion \leftarrow
exclusion ll bit[MAX][MAX];
void update(ll x , ll y, ll val)
  while (x < MAX)
    11 y1 = y;
    while (y1 < MAX)
      bit[x][y1] += val, y1 += (y1 & -y1);
    x += (x \& -x);
ll sum(ll x , ll y)
  11 \text{ ans} = 0;
  while (x > 0)
    11 y1 = y;
    while (y1 > 0)
      ans += bit[x][y1], y1 -= ( y1 & -y1 );
    x = (x \& -x):
  return ans;
```

2.3 Segment Tree

```
Sum segment tree
All arrays are 0 indexed. How to use:
to build segtree for arr[n] build(0,n-1,1)
to increment all values in [x,y] by val: upd(0,n-1,1,\leftarrow
   x, y, val)
call ppgt before every recursive call
to get sum of range [x,y]: sum(0,n-1,1,x,y)
for an array of size N use segment tree of size 4*N
#define ll long long
const 11 N=1e5+10;
ll arr[N], st[N<<2], lazy[N<<2];
void ppgt(ll l, ll r,ll id)
  if(1 == r) return;
11 m = 1 + r >> 1;
  lazy[id << 1] += lazy[id]; lazy[id << 1 | 1] += \leftrightarrow
     lazy[id];
  st[id << 1] += (m - 1 + 1) * lazy[id];
  st[id << 1 | 1] += (r - m) * lazy[id];
  lazy[id] = 0;
```

```
void build(ll l,ll r,ll id)
  if(l==r) { st[id] = arr[l]; return; }
  build ( l, l+r >>1 , id << 1); build ( (l + r >> 1) +\leftarrow
      1, r, id << 1 | 1);
  st[id] = st[id << 1] + st[id << 1 | 1];
void upd(ll l,ll r,ll id,ll x,ll y,ll val)
  if (1 > y | | r < x ) return;
  ppgt(1, r, id);
  if (1 >= x \&\& r <= y) \{ lazy[id] += val; st[id] += \longleftrightarrow \}
      (r - l + 1)*val; return;}
  upd(l,l+r >> 1,id << 1, x, y, val); upd((l+r >> \leftarrow
     1) + 1,r ,id << 1 | 1,x, y, val);
  st[id] = st[id << 1] + st[ id << 1 | 1];
ll sum(ll l,ll r,ll id,ll x,ll y)
  if (1 > y \mid | r < x) return 0;
  ppgt(l, r, id);
  if (1 >= x && r <= y ) return st[id];</pre>
  return sum(1, 1 + r \Rightarrow 1, id \iff 1, x, y) + sum((1 + \iff
    r >> 1) + 1,r ,id << 1 | 1,x, y);
```

2.4 Persistent Segment Tree

```
/*Persistent Segment Tree for sum with point updates \leftarrow
   and range sum
Usage: See sample main for kth largest number in a \leftarrow
**id of first node is 0. call build(0,n-1) first. \leftarrow
   afterwards call upd(0,n-1,previous id,i,val) to \leftarrow
val in ith number. it returns root of new segment \leftarrow
   tree after modification
**sum(0,n-1,id of root,1,r) gives sum of values in \leftarrow
   whose index is between 1 and r in
tree rooted at id **size of st,lchild and rchild should be at least N\leftarrow
   *2+Q*logN
const 11 N=1e5+10;
ll arr[N],st[20*N];
ll lchild[20*N],rchild[20*N];
11 ids[N];
11 cnt=0;
void build(ll l,ll r)
  if (l==r) { lchild [cnt] = rchild [cnt] = -1; st [cnt] \leftrightarrow
     = arr[1]; ++cnt; return; }
  11 id = cnt++;
  lchild[id] = cnt;
  build (1, 1+r >>1);
  rchild[id] = cnt; build((1 + r >> 1) + 1, r);
```

```
st[id] = st[lchild[id]] + st[rchild[id]];
11 upd(11 1,11 r,11 id,11 x,11 val)
  if (1 == r) {lchild[cnt] = rchild[cnt] = -1; st[cnt] \leftrightarrow
      = st[id] + val; ++cnt; return cnt-1;}
  11 \text{ myid} = cnt++; 11 \text{ mid} = 1 + r >> 1;
  if(x \le mid)
    rchild[myid] = rchild[id], lchild[myid] = upd(1, \leftrightarrow 
       mid, lchild[id], x, val);
  else
    lchild[myid] = lchild[id],rchild[myid] = upd(mid↔
       +1, r, rchild[id], x, val);
  st[myid] = st[lchild[myid]] + st[rchild[myid]]; ←
     return myid;}
11 sum(11 1,11 r,11 id,11 x,11 y)
  if (1 > y || r < x) return 0;
  if (1 >= x && r <= y ) return st[id];</pre>
  return sum(1, 1 + r >> 1, lchild[id], x, y) + sum((1 \leftrightarrow
      + r >> 1 ) + 1,r ,rchild[id],x, y);
ll gkth(ll l,ll r,ll id1,ll id2,ll k)
  if(l==r) return 1;
  11 \text{ mid} = 1+r>>1;
  11 a = st[lchild[id2]] - (id1 >= 0 ? st[lchild[id1\leftrightarrow
     ]] : 0);
  if(a >= k)
    return gkth(1, mid ,(id1>=0?lchild[id1]:-1), ←
       lchild[id2], k);
    return gkth(mid+1, r,(id1>=0?rchild[id1]:-1), ←
       rchild[id2], k-a);
int main()
  ll n,m;cin>>n>m;vector<ll> finalid(n);vpll v;
  for(11 i=0; i< n; i++) cin>>arr[i], v.pb({arr[i],i}); \leftarrow
     sort(all(v));
  for (11 i=0; i<n; i++) finalid [v[i].second]=i; memset (\leftarrow
     arr, 0, sizeof(ll)*N);
  arr[finalid[0]]++;build(0,n-1);
  for(11 i=1; i < n; i++) ids[i]=upd(0, n-1, ids[i-1], \leftrightarrow
     finalid[i],1);
  while(m--)
    ll i,j,k;cin>>i>>j>>k;
    --i;--j;
    ll ans=gkth(0,n-1,(i==0?-1:ids[i-1]),ids[j],k);
    cout << v [ans]. F << endl;}
```

2.5 DP Optimization

```
/*You have an array of size L.You need to split it \hookleftarrow
   into G intervals,
minimizing the cost. (G<=L otherwise we can just \leftarrow
   split in 1-intervals).
There is a cost function C[i,j] of taking an interval\leftarrow
. The cost function satisfies : C[a,b]+C[c,d] \leftarrow C[a,d]+C[c,b] for all a \leftarrow C[a,b]+C[c,d]
   c \le b \le d.
This is the quadrangle inequality and intuitively you\leftarrow
    can think that
the cost function increases at a rate which is more \leftarrow than linear
at all intervals (may not be strictly true). So , if \leftarrow
   the cost function
satisfies this inequality, the following property \leftarrow
F(g,l): min cost of spliting first l elements into g \leftarrow
    intervals
Basic recurrence : F(g,1) = \min(F(g-1,k)+C(k+1,1)) \leftarrow
   over all valid k.
P(g,1): lowest position k s.t. it minimizes F(g,1).
P(g,0) \le P(g,1) \le \bar{P}(g,2) \dots \le P(g,1-1) \le P(g,1) . (\leftarrow
   DivConqOpti,O(G.L.log(L)))
Also, P(0,1) <= P(1,1) <= P(2,1) . . . . <= P(G-1,1) <= P(G,1) . This with previous inequality leads to Knuth Opti, \hookleftarrow
   complexity O(L.L).
For div&conq, we calculate P(g,1) for each g 1 by 1.\leftarrow
   In each g,
we calculate for mid-l and solve recursively using \leftarrow
   the obtained
upper and lower bounds. For knuth, we use P(g,1-1) \le P(\leftarrow)
   g,1) <= P(g+1,1),
and fill our table in increasing I and decreasing g.
In opt. BST type problems, use bk[i][j-1] \le bk[i][j] \leftrightarrow
    <=bk[i+1][j] . */
// Code for Divide and Conquer Opti O(G.L.log(L)): -
ll C[8111];
ll sums [8111]
ll F[811][8111];
                       // optimal value
                     // optimal position.
int P[811][8111];
// note first val. in arrays is for no. of groups
11 cost(int i, int j) { // cost function
    return i > j ? 0 : (sums[j] - sums[i-1]) * (j - i \leftrightarrow j)
         + 1);
// fill(g,11,12,p1,p2) calculates all P[g][l] and F[g\leftarrow
// for l1 <= l <= l2, with the knowledge that p1 <= P\downarrow \leftarrow
   g][1] <= p2
void fill(int g, int l1, int l2, int p1, int p2) {
     if (11 > 1\overline{2}) return;
     int lm = (l1 + l2) >> 1;
    11 \text{ nv} = INF, \text{nv}1 = -1;
    for (int k = p1; k \le min(lm-1, p2); k++) {
         ll\ new\_cost = F[g-1][k] + cost[k+1][lm];
          if (nv > new_cost) {
              nv = new_cost;
              nv1 = k;
```

```
P[g][lm] = nv1; F[g][lm] = nv;
    fill(g, l1, lm-1, p1, P[g][lm]);
    fill(g, lm+1, l2, P[g][lm], p2);
int main() { // example call
    for (i=0; i<=n; i++) F[0][i]=INF;
    for (i=0; i<=k; i++) F[i][0]=0;
    F[0][0]=0:
    for (i=1; i <= k; i++) fill (i,1,n,0,n);
// Code for Knuth Optimization O(L.L) :-
ll dp[8002][802];
int a[8002],s[8002][802];
    sum[8002];
   index strats from 1
ll run(int n, int m) {
    memset(dp,0xff,sizeof(dp));
    dp[0][0] = 0;
    for (int i = 1; i <= n; ++i) {
         sum[i] = sum[i - 1] + a[i];
         int maxj = min(i, m), mk;
         11 \text{ mn} = INF;
         for (int k = 0; k < i; ++k) {
             if (dp[k][maxj - 1] >= 0) {
                 ll tmp = dp[k][maxj - 1] +
                            (\operatorname{sum}[i] - \operatorname{sum}[k]) * (i - k); \leftarrow
                                //k + 1..i
                  if (tmp < mn) {
                       mn^- = tmp;
                       mk = k;
         dp[i][maxj] = mn;
    s[i][maxj] = mk;
         for (int j = \max_{j} - 1; j >= 1; --j) {
             11 \text{ mn} = INF;
             int mk;
             for (int k = s[i - 1][j]; k \leq s[i][j + \leftarrow
                 1]; ++k)
                  if (dp[k][j-1] >= 0) {
                       11 \text{ tmp} = \text{dp}[k][j - 1] +
                           (sum[i] - sum[k]) * (i - k);
                       if (tmp < mn) {
                           mn^- = tmp;
                           mk = k;
                  }
             dp[i][j] = mn;
             s[i][j] = mk;
    return dp[n][m];
```

```
}
// call -> run(n, min(n,m))
```

3 Flows and Matching

3.1 General Matching

```
/*Given any directed graph, finds maximal matching
  Vertices -> 0-indexed
Time Complexity:
  O(n^3) per call to edmonds()*/
const int MAXN = 100;
vector < int > adj[MAXN];
int p[MAXN], base[MAXN], match[MAXN];
int lca(int nodes, int u, int v){
 vector < bool > used (nodes);
  for (;;) {
    u = base[u]; used[u] = true;
    if (match[u] == -1) break;
    u = p[match[u]];
 for (;;) {
    v = base[v];
if (used[v]) return v;
    v = p[match[v]];
void mark_path(vector < bool > & blossom, int u, int b, ←
  int child) {
  for (; base[u] != b; u = p[match[u]]) {
    blossom[base[u]] = true;
    blossom[base[match[u]]] = true;
    p[u] = child;
    child = match[u];
int find_path(int nodes, int root) {
  vector < bool > used(nodes);
  for (int i = 0; i < nodes; ++i) {
    p[i] = -1;
    base[i] = i;
  used[root] = true;
  queue < int > q;
  q.push(root);
  while (!q.empty()) {
    int u = q.front();
    q.pop();
    for (int j = 0; j < (int)adj[u].size(); j++) {
      int v = adj[u][j];
      if (base[u] == base[v] || match[u] == v) {
```

```
if (v == root \mid | (match[v] \mid = -1 \&\& p[match[v]] \leftrightarrow
           ! = -1))
         int curr_base = lca(nodes, u, v);
         vector < bool > blossom(nodes);
         mark_path(blossom, u, curr_base, v);
         mark_path(blossom, v, curr_base, u);
         for (int i = 0; i < nodes; i++) {
           if (blossom[base[i]]) {
             base[i] = curr_base;
             if (!used[i]) {
                used[i] = true;
                q.push(i);
      \} else if (p[v] == -1) {
         p[v] = u;
         if (match[v] == -1) return v;
         v = match[v];
         used[v] = true;
         q.push(v);
  return -1;
int edmonds(int nodes) {
  for (int i = 0; i < nodes; i++) {
    match[i] = -1:
  for (int i = 0; i < nodes; i++) {</pre>
    if (match[i] == -1) {
       int u, pu, ppu;
      for (u = find_path(nodes, i); u != -1; u = ppu) \leftarrow
         pu = p[u]; ppu = match[pu];
         match[u] = pu; match[pu] = u;
  int matches = 0;
  for (int i = 0; i < nodes; i++) {
  if (match[i] != -1) {</pre>
       matches++;
  return matches/2;
u--; v--; adj[u].pb(v); adj[v].pb(u);
cout << edmonds(n) * 2 << endl;
for (int i = 0; i < n; i++) {
   if (match[i] != -1 && i < match[i]) {</pre>
         cout << i + 1 << " " << match[i] + 1 << endl;
```

3.2 Global Mincut

```
/*finds min weighted cut in undirected graph in
O(n^3), Adj Matrix, O-indexed vertices
output-(min cut value, nodes in half of min cut)*/
typedef vector <int > VI;
typedef vector < VI > VVI;
const int INF = 1000000000;
pair < int , VI > GetMinCut(VVI & weights) {
  int N = weights.size();
  VI used(N), cut, best_cut;
  int best_weight = -1;
  for (int phase = N-1; phase >= 0; phase--) {
    VI w = weights[0];
    VI added = used;
    int prev, last = 0;
    for (int i = 0; i < phase; i++) {</pre>
      prev = last;
      last = -1;
      for (int j = 1; j < N; j++)
  if (!added[j] \&\& (last == -1 || w[j] > w[last])) \leftrightarrow
      if (i == phase-1) {
  for (int j = \bar{0}; j < N; j++) weights[prev][j] += \leftarrow
     weights[last][j];
  for (int j = 0; j < N; j++) weights[j][prev] = \leftarrow
     weights[prev][j];
  used[last] = true;
  cut.push_back(last);
  if (best_weight == -1 || w[last] < best_weight) {</pre>
    best_cut = cut;
    best_weight = w[last];
      } else {
  for (int j = 0; j < N; j++)
    w[j] += weights[last][j];
  added[last] = true;
  return make_pair(best_weight, best_cut);
VVI weights(n, VI(n));
pair < int , VI > res = GetMinCut(weights);
```

3.3 Hopcroft Matching

```
// O(m * \sqrt{n})
struct graph {
  int L, R; // O-indexed vertices
  vector < vector < int >> adj;
  graph(int L, int R) : L(L), R(R), adj(L+R) { }
  void add_edge(int u, int v) {
```

```
adj[u].pb(v+L);
    adj[v+L].pb(u);
  int maximum_matching() {
    vector<int> level(L), mate(L+R, -1);
    function < bool (void) > levelize = [&]() { // BFS
queue < int > Q;
       for (int u = 0; u < L; ++u) {
         level[u] = -1;
         if (mate[u] < 0)
level[u] = 0, Q.push(u);</pre>
       while (!Q.empty()) {
         int u = Q.front(); Q.pop();
         for (int w: adj[u]) {
           int v = mate[w];
           if (v < 0) return true;
           if (level[v] < 0) {</pre>
             level[v] = level[u] + 1; Q.push(v);
      return false;
    function <bool(int) > augment = [&](int u) { // DFS
       for (int w: adj[u]) {
         int v = mate[w];
         if (v < 0 \mid | (level[v] > level[u] \&\& augment( \leftarrow
            v))) {
           mate[u] = w;
           mate[w] = u;
           return true;
      return false;
    int match = 0;
    while (levelize())
      for (int u = 0; u < L; ++u)
         if (mate[u] < 0 && augment(u))</pre>
           ++match;
    return match;
int main() {
  int L, R, m;
  scanf("%d %d %d", &L, &R, &m);
  graph g(L, R);
  for (int i = 0; i < m; ++i) {
    int u, v;
    scanf("%d %d", &u, &v); u--;v--;
    g.add_edge(u, v);
  printf("%d\n", g.maximum_matching());
```

```
/*Time: O(m*n^2) and for any unit capacity network O(\leftarrow
   m * n^1/2
TIme: O(min(fm,mn^2)) (f: flow routed)
(so for bipartite matching as well)
In practice it is pretty fast for any bipartite \hookleftarrow
   network
I/O:
         n -> vertice; DinicFlow net(n);
         for(z : edges) net.addEdge(z.F,z.S,cap);
         max flow = maxFlow(s,t);
e=(u,v), e.flow represents the effective flow from u \leftarrow
(i.e f(u->v) - f(v->u)), vertices are 1-indexed
*** use int if possible(ll could be slow in dinic) \leftrightarrow
   *** */
struct edge {ll x, y, cap, flow;};
struct DinicFlow {
    // *** change inf accordingly *****
    const ll inf = (1e18);
    vector <edge> e;
    vector <1l> cur, d;
vector < vector <1l> > adj;
    ll n, source, sink;
    DinicFlow() {}
    DinicFlow(11 v) {
        cur = vector < 11 > (n + 1);
        d = vector < 11 > (n + 1);
        adj = vector < vector < 11 > (n + 1);
    void addEdge(ll from, ll to, ll cap) {
        edge e1 = \{from, to, cap, 0\};
        edge e2 = \{to, from, 0, 0\};
        adj[from].push_back(e.size()); e.push_back(e1 \leftarrow
        adj[to].push_back(e.size()); e.push_back(e2);
    }
ll bfs() {
        queue <11> q;
        for (11 i = 0; i \le n; ++i) d[i] = -1;
        q.push(source); d[source] = 0;
        while(!q.empty() and d[sink] < 0) {</pre>
             ll x = q.front(); q.pop();
             for (ll i = 0; i < (ll)adj[x].size(); ++i) \leftarrow
                 ll id = adj[x][i], y = e[id].y;
                 if(d[y] < 0 \text{ and } e[id].flow < e[id]. \leftarrow
                    cap) {
                      q.push(y); d[y] = d[x] + 1;
        return d[sink] >= 0;
    11 dfs(ll x, ll flow) {
        if(!flow) return 0;
        if(x == sink) return flow;
```

```
for(; cur[x] < (11)adj[x].size(); ++cur[x]) {</pre>
            ll id = adj[x][cur[x]], y = e[id].y;
             if(d[y] != d[x] + 1) continue;
            ll pushed = dfs(y, min(flow, e[id].cap - \leftarrow
                e[id].flow));
             if(pushed) {
                 e[id].flow += pushed;
                 e[id ^ 1].flow -= pushed;
                 return pushed;
        return 0;
    11 maxFlow(ll src, ll snk) {
        this->source = src; this->sink = snk;
        11 flow = 0;
        while(bfs()) {
             for(11 i = 0; i \le n; ++i) cur[i] = 0;
             while(ll pushed = dfs(source, inf)) {
                 flow += pushed;
        return flow;
};
```

3.5 Ford Fulkerson

```
// running time - O(f*m) (f -> flow routed)
const 11 \text{ N} = 3e3;
ll n; // number of vertices
11 capacity[N][N]; // adj matrix for capacity
vll adj[N]; // adj list of the corresponding \leftarrow
   undirected graph(***imp***)
// E = {1-2,2->3,3->2}, adj list should be => \leftarrow
   \{1->2,2->1,2->3,3->2\}
// *** vertices are 0-indexed ***
11 \text{ INF} = (1e18);
ll \mathtt{snk}, \mathtt{cnt}; // \mathtt{cnt} for \mathtt{vis}, no \mathtt{need} to \mathtt{initialize} \leftarrow
vector<ll> par, vis;
ll dfs(ll u,ll curr_flow){
  vis[u] = cnt; if(u == snk) return curr_flow;
  if(adj[u].size() == 0) return 0;
  for (11 j=0; j<5; j++) { // random for good \leftarrow
     augmentation(**sometimes take time**)
         11 a = rand()%(adj[u].size());
         ll v = adj[u][a];
         if (vis[v] = cnt \mid capacity[u][v] = 0) \leftrightarrow
             continue;
         par[v] = u;
         ll f = dfs(v,min(curr_flow, capacity[u][v])); \leftarrow
              if(vis[snk] == cnt) return f;
```

```
for(auto v : adj[u]){
      if (vis[v] == cnt || capacity[u][v] == 0) \leftarrow
          continue;
      par[v] = u;
      ll f = dfs(v,min(curr_flow, capacity[u][v])); \leftarrow
          if(vis[snk] == cnt) return f;
    return 0;
il maxflow(ll s, ll t) {
    snk = t; ll flow = 0; cnt++;
    par = vll(n,-1); vis = vll(n,0);
    while(ll new_flow = dfs(s, INF)){
       flow += new_flow; cnt++;
       11 cur = t;
       while(cur != s){
         ll prev = par[cur];
         capacity[prev][cur] -= new_flow;
         capacity[cur][prev] += new_flow;
         cur = prev;
    return flow;
```

3.6 MCMF

```
// MCMF Theory:
// 1. If a network with negative costs had no \hookleftarrow
   negative cycle it is possible to transform it into↔
   one with nonnegative
        costs. Using Cij_new(pi) = Cij_old + pi(i) - ←
   pi(j), where pi(x) is shortest path from s to x in\leftarrow
   network with an
       added vertex s. The objective value remains \leftarrow
   the same (z_{new} = z + constant). z(x) = sum(cij*\leftarrow
  xij)
       (x-)flow, c-)cost, u-)cap, r-)residual cap).
// 2. Residual Network: cji = -cij, rij = uij-xij, ↔
   rji = xij.
// 3. Note: If edge (i,j),(j,i) both are there then \leftarrow
   residual graph will have four edges b/w i, j (pairs↔
   of parellel edges).
// 4. let x* be a feasible soln, its optimal iff \leftarrow
   residual network Gx* contains no negative cost \hookleftarrow
   cycle.
// 5. Cycle Cancelling algo => Complexity O(n*m^2*U*\leftarrow
   C) (C->max abs value of cost, U->max cap) (m*U*C \leftarrow
   iterations).
// 6. Succesive shortest path algo => Complexity O(n \leftarrow
   ^3 * B) / O(nmBlogn)(using heap in Dijkstra)(B \rightarrow \leftarrow
   largest supply node).
//Works for negative costs, but does not work for \leftarrow
   negative cycles
//Complexity: O(min(E^2 *V log V, E logV * flow))
```

```
// to use -> graph G(n), G.add_edge(u,v,cap,cost), G. \leftarrow
   min_cost_max_flow(s,t)
// ********* INF is used in both flow_type and \leftarrow
   cost_type so change accordingly
const 1\bar{1} TNF = 99999999;
// vertices are 0-indexed
struct graph {
  typedef ll flow_type; // **** flow type ****
  typedef 11 cost_type; // **** cost type ****
  struct edge {
    int src, dst;
    flow_type capacity, flow;
    cost_type cost;
    size_t rev;
  vector < edge > edges;
  void add_edge(int src, int dst, flow_type cap, \leftarrow
     cost_type cost) {
    adj[src].push_back(\{src, dst, cap, 0, cost, adj[ \leftarrow
       dst].size()});
    adj[dst].push_back({dst, src, 0, 0, -cost, adj}[\leftarrow
       src].size()-1});
  int n;
  vector < vector < edge >> adj;
  graph(int n) : n(n), adj(n) { }
  pair <flow_type, cost_type > min_cost_max_flow(int s, ←)
      int t) {
    flow_type flow = 0;
    cost_type cost = 0;
    for (int u = 0; u < n; ++u) // initialize
      for (auto &e: adj[u]) e.flow = 0;
    vector < cost_type > p(n, 0);
    auto rcost = [\&] (edge e) { return e.cost + p[e.\leftrightarrow
       src] - p[e.dst]; };
    for (int iter = 0; ; ++iter) {
      vector<int> prev(n, -1); prev[s] = 0;
      vector < cost_type > dist(n, INF); dist[s] = 0;
      if (iter == 0) { // use Bellman-Ford to remove \leftarrow
         negative cost edges
        vector < int > count(n); count[s] = 1;
        queue < int > que;
        for (que.push(s); !que.empty(); ) {
           int u = que.front(); que.pop();
           count[u] = -count[u];
           for (auto &e: adj[u]) {
             if (e.capacity > e.flow && dist[e.dst] > \leftarrow
                dist[e.src] + rcost(e)) {
               dist[e.dst] = dist[e.src] + rcost(e);
               prev[e.dst] = e.rev;
               if (count[e.dst] <= 0) {</pre>
                 count[e.dst] = -count[e.dst] + 1;
                 que.push(e.dst);
```

```
for (int i=0; i<n; i++) p[i] = dist[i]; // added \leftarrow
    continue;
  } else { // use Dijkstra
    typedef pair < cost_type, int > node;
    priority_queue < node, vector < node >, greater < ←
       node >> que;
    que.push(\{0, s\});
    while (!que.empty()) {
      node a = que.top(); que.pop();
      if (a.S == t) break;
      if (dist[a.S] > a.F) continue;
      for (auto e: adj[a.S]) {
         if (e.capacity > e.flow && dist[e.dst] > \leftarrow
            a.F + rcost(e) {
           dist[e.dst] = dist[e.src] + rcost(e);
           prev[e.dst] = e.rev;
           que.push({dist[e.dst], e.dst});
  if (prev[t] == -1) break;
  for (int u = 0; u < n; ++u)
    if (dist[u] < dist[t]) p[u] += dist[u] - dist \leftrightarrow
        [t];
  function <flow_type(int,flow_type) > augment = ←
     [&](int u, flow_type cur) {
    if (u == s) return cur;
    edge &r = adj[u][prev[u]], &e = adj[r.dst][r.\leftrightarrow
    flow_type f = augment(e.src, min(e.capacity -\leftarrow
    e.flow, cur));
e.flow += f; r.flow -= f;
    return f;
  flow_type f = augment(t, INF);
  flow += f;
  cost += f * (p[t] - p[s]);
return {flow, cost};
```

3.7 MinCost Matching

```
// Min cost bipartite matching via shortest 
   augmenting paths
//
// This is an O(n^3) implementation of a shortest 
   augmenting path
// algorithm for finding min cost perfect matchings 
   in dense
```

```
// graphs. In practice, it solves 1000 \times 1000 problems\leftarrow
    in around 1
// second.
     cost[i][j] = cost for pairing left node i with <math>\leftarrow
   right node j
// Lmate[i] = index of right node that left node i \leftarrow
   pairs with
     Rmate[j] = index of left node that right node j \leftarrow
   pairs with
^{\prime\prime}/ The values in cost[i][j] may be positive or \hookleftarrow
   negative. To perform
// maximization, simply negate the cost[][] matrix.
typedef ll cost_type;
typedef vector < cost_type > VD;
typedef vector < VD > VVD;
typedef vector <int> VI;
cost_type MinCostMatching(const VVD &cost, VI &Lmate, ←
    VI &Rmate) {
  int n = int(cost.size());
  // construct dual feasible solution
  VD u(n);
  VD v(n);
  for (int i = 0; i < n; i++) {
    u[i] = cost[i][0];
    for (int j = 1; j < n; j++) u[i] = min(u[i], cost <math>\leftarrow
       [i][j]);
  for (int j = 0; j < n; j++) {
    v[j] = cost[0][j] - u[0];
    for (int i = 1; i < n; i++) v[j] = min(v[j], cost \leftrightarrow
       [i][i] - u[i]);
  // construct primal solution satisfying \leftarrow
     complementary slackness
  Lmate = VI(n, -1);
  Rmate = VI(n, -1);
  int mated = 0;
  for (int i = 0; i < n; i++) {
    for (int j = 0; j < n; j++) {
      if (Rmate[j] != -1) continue;
      if (fabs(cost[i][j] - u[i] - v[j]) < 1e-10) {</pre>
      //**** change this comparision if double cost \leftarrow
         ****
         Lmate[i] = j;
         Rmate[j] = i;
         mated++;
         break;
  VD dist(n); VI dad(n); VI seen(n);
  // repeat until primal solution is feasible
  while (mated < n) {
    // find an unmatched left node
    int s = 0;
```

```
while (Lmate[s] != -1) s++;
  // initialize Dijkstra
  fill(dad.begin(), dad.end(), -1);
  fill(seen.begin(), seen.end(), 0);
  for (int k = 0; k < n; k++)
    dist[k] = cost[s][k] - u[s] - v[k];
  int j = 0;
  while (true) {
    // find closest
    j = -1;
    for (int k = 0; k < n; k++) {
      if (seen[k]) continue;
      if (j == -1 || dist[k] < dist[j]) j = k;</pre>
    seen[i] = 1;
    // termination condition
    if (Rmate[j] == -1) break;
    // relax neighbors
    const int i = Rmate[j];
    for (int k = 0; k < n; k++) {
      if (seen[k]) continue;
      const cost_type new_dist = dist[j] + cost[i][ \leftrightarrow struct pt \{
         k] - u[i] - v[k];
      if (dist[k] > new_dist) {
        dist[k] = new_dist;
        dad[k] = j;
  // update dual variables
  for (int k = 0; k < n; k++) {
    if (k == j | | !seen[k]) continue;
    const int i = Rmate[k];
    v[k] += dist[k] - dist[j];
    u[i] -= dist[k] - dist[i];
  u[s] += dist[j];
  // augment along path
  while (dad[j] > = 0) {
    const int d = dad[j];
    Rmate[j] = Rmate[d];
    Lmate[Rmate[j]] = j;
    j = d;
  Rmate[j] = s;
  Lmate[s] = j;
  mated++;
cost_type value = 0;
for (int i = 0; i < n; i++)
  value += cost[i][Lmate[i]];
return value;
```

Geometry

4.1 Geometry

```
//small non recursive functions should me made inline
//do not read input in double format if they are \hookleftarrow
integer points
#define ld double
#define PI acos(-1)
//atan2(y,x) slope of line (0,0) \rightarrow (x,y) in radian (\leftarrow
// to convert to degree multiply by 180/PI
ld\ INF = 1e100;
1d EPS = 1e-9;
inline bool eq(ld a,ld b) {return fabs(a-b) < EPS;}</pre>
inline bool lt(ld a,ld b) {return a+EPS<b;}</pre>
inline bool gt(ld a,ld b) {return a>b+EPS;}
inline bool Te(ld a,ld b) {return lt(a,b)||eq(a,b);}
inline bool ge(ld a,ld b) {return gt(a,b)||eq(a,b);}
  ld x, y;
  pt() {}
  pt(1d x, 1d y) : x(x), y(y) {}
  pt(const pt \&p) : x(p.x), y(p.y)
  pt operator + (const pt &p) const { return pt(x+p.↔
     x, y+p.y); }
  pt operator - (const pt &p) const { return pt(x-p. ←
     x, y-p.y); }
  pt operator * (ld c)
                              const { return pt(x*c,
                                                          y \leftarrow
     *c ); }
  pt operator / (ld c)
                              const { return pt(x/c,
     /c ); }
  bool operator < (const pt &p) const{ return lt(y,p. \leftarrow)
     y) | | (eq(y,p.y) && lt(x,p.x)); }
  bool operator > (const pt &p) const{ return p<pt(x,\leftarrow)
  bool operator \leq (const pt &p) const{ return !(pt(x\leftrightarrow
  bool operator \geq (const pt &p) const{ return !(pt(x\leftrightarrow
     ,y) < p);
  bool operator == (const pt &p) const{ return (pt(x,\leftarrow
     y) <= p) && (pt(x,y) >= p);
ld dot(pt p,pt q) {return p.x*q.x+p.y*q.y;}
ld dist2(pt p, pt q) {return dot(p-q,p-q);}
ld dist(pt p,pt q) {return sqrt(dist2(p,q));}
ld norm2(pt p) {return dot(p,p);}
ld norm(pt p) {return sqrt(norm2(p));}
ld cross(pt p, pt q) { return p.x*q.y-p.y*q.x;}
ostream & operator << (ostream & os, const pt & p) {
  return os << "(" << p.x << "," << p.y << ")";}
istream& operator >> (istream &is, pt &p){
  return is >> p.x >> p.y;}
```

```
//returns 0 if a,b,c are collinear,1 if a->b->c is cw\leftrightarrow // compute intersection of line passing through a and\leftrightarrow
    and -1 if ccw
int orient(pt a,pt b,pt c)
  pt p=b-a,q=c-b;double cr=cross(p,q);
  if (eq(cr, 0)) return 0; if (lt(cr, 0)) return 1; return \leftrightarrow
// rotate a point CCW or CW around the origin
pt RotateCCW90(pt p) { return pt(-p.y,p.x); }
pt RotateCW90(pt p) { return pt(p.y,-p.x); }
pt RotateCCW(pt p, ld t) { //rotate by angle t \leftarrow
   degree ccw
  return pt(p.x*cos(t)-p.y*sin(t), p.x*sin(t)+p.y*cos \leftarrow
     (t)); }
// project point c onto line (not segment) through a \leftarrow
   and b assuming a != b
pt ProjectPointLine(pt a, pt b, pt c) {
  return a + (b-a)*dot(c-a, b-a)/dot(b-a, b-a);}
// project point c onto line segment through a and b \leftarrow
   (closest point on line segment)
pt ProjectPointSegment(pt a, pt b, pt c) {
  ld r = dot(b-a,b-a); if (eq(r,0)) return a; //a and \leftarrow
  r = dot(c-a, b-a)/r; if (lt(r,0)) return a; //c on \leftrightarrow
     left of
  if (gt(r,1)) return b; return a + (b-a)*r;}
// compute distance from c to segment between a and b
ld DistancePointSegment(pt a, pt b, pt c) {
  return sqrt(dist\tilde{2}(c, ProjectPointSegment(a, b, c)))\leftarrow
// compute distance from c to line between a and b
ld DistancePointLine(pt a, pt b, pt c) {
  return sqrt(dist2(c, ProjectPointLine(a, b, c)));}
// determine if lines from a to b and c to d are \leftarrow
   parallel or collinear
bool LinesParallel(pt a, pt b, pt c, pt d) {
  return eq(cross(b-a, c-d),0); }
bool LinesCollinear(pt a, pt b, pt c, pt d) {
  return LinesParallel(a, b, c, d) && eq(cross(a-b, a\leftrightarrow
     -c),0) && eq(cross(c-d, c-a),0);}
// determine if line segment from a to b intersects \leftarrow
   with line segment from c to d
bool SegmentsIntersect(pt a, pt b, pt c, pt d) {
  if (LinesCollinear(a, b, c, d)) {
    //a->b and c->d are collinear and have one point \hookleftarrow
    if (eq(dist2(a,c),0)||eq(dist2(a,d),0)||eq(dist2(b\leftarrow
        if (gt(dot(c-a,c-b),0) \&\&gt(dot(d-a,d-b),0) \&\&gt(dot \leftrightarrow a,d-b))
       (c-b,d-b),0)) return false;
    return true;}
  if (gt(cross(d-a,b-a)*cross(c-a,b-a),0)) return \leftarrow
     false; //c, d on same side of a, b
  if (gt(cross(a-c,d-c)*cross(b-c,d-c),0)) return \leftarrow
     false; //a, b on same side of c, d
  return true;}
```

```
// with line passing through c and d, assuming that **\leftarrow
   unique** intersection exists;
//*for segment intersection, check if segments \leftarrow
   intersect first
pt ComputeLineIntersection(pt a,pt b,pt c,pt d){
  b=b-a;d=c-d;c=c-a;//lines must not be collinear
  assert(gt(dot(b, b),0)&&gt(dot(d, d),0));
  return a + b*cross(c, d)/cross(b, d);}
//returns true if point a,b,c are collinear and b \leftarrow
   lies between a and c
bool between(pt a,pt b,pt c){
  if(!eq(cross(b-a,c-b),0))return 0;//not collinear
  return le(dot(b-a,b-c),0);
//compute intersection of line segment a-b and c-d
pt ComputeSegmentIntersection(pt a,pt b,pt c,pt d){
  if (! SegmentsIntersect(a,b,c,d)) return \{INF,INF\}; //\leftarrow
     don't intersect
  //if collinear then infinite intersection points, \leftarrow
     this returns any one
  if (LinesCollinear (a,b,c,d)) {if (between(a,c,b)) \leftarrow
     return c;if(between(c,a,d))return a;return b;}
  return ComputeLineIntersection(a,b,c,d);
^{\prime\prime}/ compute center of circle given three points - *a,b \leftarrow
    c shouldn't be collinear
pt ComputeCircleCenter(pt a,pt b,pt c){
  b=(a+b)/2; c=(a+c)/2;
  return ComputeLineIntersection(b,b+RotateCW90(a-b), ←
     c,c+RotateCW90(a-c));}
//point in polygon using winding number -> returns 0 \leftrightarrow
   if point is outside
//winding number>0 if point is inside and equal to 0 \leftarrow
   if outside
//draw a ray to the right and add 1 if side goes from\leftarrow
    up to down and -1 otherwise
bool PointInPolygon(const vector < pt > &p,pt q){
  int n=p.size(), windingNumber=0;
  for(int i=0;i<n;++i){
    if(eq(dist2(q,p[i]),0)) return 1;//q is a vertex
    int j = (i+1) \%n;
    if (eq(p[i].y,q.y) \& eq(p[j].y,q.y)) \{//i,i+1 \leftarrow
      vertex is vertical if (le(min(p[i].x,p[j].x),q.x) \&\&le(q.x,max(p[i]. \leftrightarrow a))
         x, p[j].x))) return 1;}//q lies on boundary
    else {
      bool below=lt(p[i].y,q.y);
      if(below!=lt(p[j].y,q.y)) {
         auto orientation=orient(q,p[j],p[i]);
         if(orientation==0) return 1;//q lies on \leftarrow
            boundary i->j
         if (below == (orientation > 0)) winding Number += \leftarrow
            below?1:-1:}}
  return windingNumber == 0?0:1;
```

```
// determine if point is on the boundary of a polygon
bool PointOnPolygon(const vector < pt > &p, pt q) {
  for (int i = 0; i < p.size(); i++)</pre>
    if (eq(dist2(ProjectPointSegment(p[i],p[(i+1)%p.←)
       size()],q),q),0)) return true;
  return false:}
// Compute area or centroid of any polygon (\leftarrow
   coordinates must be listed in cw/ccw
//fashion.The centroid is often known as center of \hookleftarrow
   gravity/mass
ld ComputeSignedArea(const vector<pt> &p) {
  ld ans=0;
  for(int i = 0; i < p.size(); i++) {</pre>
    int j = (i+1) % p.size();
    ans+=cross(p[i],p[j]);
  } return ans / 2.0;}
ld ComputeArea(const vector<pt> &p) {
  return fabs(ComputeSignedArea(p));
^{\prime\prime} compute intersection of line through points a and \hookleftarrow
// circle centered at c with radius r > 0
vector<pt> CircleLineIntersection(pt a, pt b, pt c, \leftarrow
  ld r)
  vector<pt> ret;
  b = b-a; a = a-c;
  ld A = dot(b, b), B = dot(a, b), C = dot(a, a) - r*r, \leftarrow D = B*B - A*C;
  if (lt(D,0)) return ret; //don't intersect
  ret.push_back(c+a+b*(-B+sqrt(D+EPS))/A);
  if (gt(D,0)) ret.push_back(c+a+b*(-B-sqrt(D))/A);
  return ret;}
// compute intersection of circle centered at a with \hookleftarrow
// with circle centered at b with radius R
vector<pt> CircleCircleIntersection(pt a, pt b, ld r, \leftarrow
    1d R) {
  vector <pt> ret;
  1d d = sqrt(dist2(a, b)), d1=dist2(a,b);
  pt inf(INF,INF);
  if (eq(d1,0)\&eq(r,R)){ret.pb(inf);return ret;}//\leftarrow
     circles are same return (INF, INF)
  if(gt(d,r+R) \mid | lt(d+min(r, R),max(r, R))) return \leftrightarrow
     ret;
  1d x = (d*d-R*R+r*r)/(2*d), y = sqrt(r*r-x*x);
  pt v = (b-a)/d;
  ret.push_back(a+v*x + RotateCCW90(v)*y);
  if (gt(y,0)) ret.push_back(a+v*x - RotateCCW90(v)*y\leftarrow
  return ret;}
//compute centroid of simple polygon by dividing it \leftarrow
   into disjoint triangles
//and taking weighted mean of their centroids (Jerome↔
pt ComputeCentroid(const vector<pt> &p) {
  pt c(0,0), inf(INF, INF);
```

```
ld scale = 6.0 * ComputeSignedArea(p);
  if(p.empty())return inf;//empty vector
  if (eq(scale, 0)) return inf; //all points on straight \leftarrow
  for (int i = 0; i < p.size(); i++){
    int j = (i+1) % p.size();
    c = c + (p[i]+p[j])*cross(p[i],p[j]);
  return c / scale;}
// tests whether or not a given polygon (in CW or CCW\leftrightarrow
    order) is simple
bool IsSimple(const vector<pt> &p) {
  for (int i = 0; i < p.size(); i++) {
    for (int k = i+1; k < p.size(); k++) {</pre>
      int j = (i+1) % p.size();
      int \tilde{1} = (k+1) \% p.size();
      if (i == 1 || j == k) continue;
      if (SegmentsIntersect(p[i], p[j], p[k], p[l]))
        return false;}}
  return true: }
/*point in convex polygon
****bottom left point must be at index 0 and top is \leftarrow
   the index of upper right vertex
****if not call make_hull once*/
bool pointinConvexPolygon(vector<pt> poly,pt point, \leftarrow
   int top) {
  if (point < poly[0] || point > poly[top]) return 0; \leftarrow
     //O for outside and 1 for on/inside
  auto orientation = orient(point, poly[top], poly↔
  if (orientation == 0)_{
    if (point == poly[0] | point == poly[top]) ←
       return 1;
    return top == 1 \mid \mid top + 1 == poly.size() ? 1 : \leftarrow
       1;//checks if point lies on boundary when
    //bottom and top points are adjacent
  } else if (orientation < 0) {</pre>
    auto itRight = lower_bound(poly.begin() + 1, poly\leftrightarrow
       .begin() + top, point);
    return orient(itRight[0], point, itRight[-1])<=0;</pre>
    auto itLeft = upper_bound(poly.rbegin(), poly.
       rend() - top-1, point);
    return (orient(itLeft == poly.rbegin() ? poly[0] ←
       : itLeft[-1], point, itLeft[0]))<=0;
/*maximum distance between two points in convexy \leftarrow
   polygon using rotating calipers
make sure that polygon is convex. if not call \leftarrow
   make_hull first
ld maxDist2(vector<pt> poly) {
  int n = poly.size();
  ld res=0:
  for (int i = 0, j = n < 2 ? 0 : 1; <math>i < j; ++i)
```

```
for(auto z:cons){
    if(hull.size() <=1) {hull.pb(z); continue;}
    pt pr,ppr; bool fl=true;
    while((m=hull.size())>=2) {
        pr=hull[m-1]; ppr=hull[m-2];
        ll ch=orient(ppr,pr,z);
        if(ch==-1) {break;}
        else if(ch==1) {hull.pop_back(); continue;}
        else {
        ld d1,d2;
        d1=dist2(ppr,pr); d2=dist2(ppr,z);
        if(gt(d1,d2)) {fl=false; break;} else {hull.}
            pop_back();}
    }
    if(fl) {hull.push_back(z);}
}
return;
```

4.2 Convex Hull

```
pt firstpoint;
//for sorting points in ccw(counter clockwise) \leftarrow
   direction w.r.t firstpoint (leftmost and \leftarrow
   bottommost)
bool compare(pt x,pt y){
  11 o=orient(firstpoint,x,y);
  if (o==0) return lt(x.x+x.y,y.x+y.y);
  return o<0;
/*takes as input a vector of points containing input \leftarrow
   points and an empty vector for making hull
the points forming convex hull are pushed in vector \leftarrow
returns hull containing minimum number of points in \leftarrow
ccw order
****remove EPS for making integer hull
void make_hull(vector<pt>& poi, vector<pt>& hull)
  pair < ld, ld > bl = { INF, INF };
  ll n=poi.size();ll ind;
  for(ll i=0;i<n;i++){</pre>
    pair < ld, ld > pp = { poi[i].y, poi[i].x};
    if (pp < bl) {</pre>
      ind=i;bl={poi[i].y,poi[i].x};
  swap(bl.F,bl.S);firstpoint=pt(bl.F,bl.S);
  vector<pt> cons;
  for(ll i=0;i<n;i++){
    if (i == ind) continue; cons.pb(poi[i]);
  sort(cons.begin(),cons.end(),compare);
  hull.pb(firstpoint); ll m;
```

4.3 Convex Hull Trick

```
maintains upper convex hull of lines ax+b and gives \leftarrow
  minimum value at a given x
to add line ax+b: sameoldcht.addline(a,b), to get min\leftrightarrow
    value at x: sameoldcht.getbest(x)
to get maximum value at x add -ax-b as lines instead \leftarrow
  of ax+b and use -sameoldcht.getbest(x)
const int N = 1e5 + 5;
int n;
int a[N];
int b[N];
long long dp[N];
struct line{
    long long a , b;
    double xleft;
    bool type;
    line(long_long _a , long long _b){
        b = _b;
        type = 0;
    bool operator < (const line &other) const{</pre>
        if (other.type){
             return xleft < other.xleft;</pre>
        return a > other.a;
double meet(line x , line y){
    return 1.0 * (y.b - x.b) / (x.a - y.a);
struct cht{
```

```
set < line > hull;
cht(){
    hull.clear();
typedef set < line > :: iterator ite;
bool hasleft(ite node){
    return node != hull.begin();
bool hasright(ite node){
    return node != prev(hull.end());
void updateborder(ite node){
    if(hasright(node)){
        line temp = *next(node);
        hull.erase(temp);
        temp.xleft = meet(*node , temp);
        hull.insert(temp);
    if(hasleft(node)){
        line temp = *node;
        temp.xleft = meet(*prev(node) , temp);
        hull.erase(node);
        hull.insert(temp);
    else{
    line temp = *node;
    rede):
        hull.erase(node);
        temp.xleft = -1e18;
        hull.insert(temp);
bool useless(line left , line middle , line right\leftrightarrow
    double x = meet(left , right);
    double y = x * middle.a + middle.b;
    double 'ly = left.a * x + left.b;
    return y > ly;
bool useless(ite node){
    if(hasleft(node) && hasright(node)){
        return useless(*prev(node) , *node , *←
           next(node));
    return 0;
void addline(long long a , long long b){
    line temp = line(a , b);
    auto it = hull.lower_bound(temp);
    if(it != hull.end() && it -> a == a){
   if(it -> b > b){
             hull.erase(it);
        else{
             return;
    hull.insert(temp);
    it = hull.find(temp);
```

```
if(useless(it)){
             hull.erase(it);
             return;
        while(hasleft(it) && useless(prev(it))){
             hull.erase(prev(it));
        while(hasright(it) && useless(next(it))){
             hull.erase(next(it));
         updateborder(it);
    long long getbest(long long x){
         if(hull.empty()){
             return 1e18;
         line query (0, 0);
         query.xleft = x;
        query.type = 1;
         auto it = hull.lower_bound(query);
         it = prev(it);
         return it -> a * x + it -> b;
cht sameoldcht;
int main()
    scanf("%d" , &n);
    for(int i = 1; i <= n; ++i){
    scanf("%d", a + i);</pre>
    for(int i = 1; i <= n; ++i){
    scanf("%d", b + i);
    sameoldcht.addline(b[1]
    for (int_i = 2; i <= n; ++i){
        dp[i] = sameoldcht.getbest(a[i]);
         sameoldcht.addline(b[i] , dp[i]);
    printf("%11d\n", dp[n]);
```

5 Trees

5.1 BlockCut Tree

```
// code credits - http://codeforces.com/contest/487/←
    submission/15921824
// Take care it is 0 indexed -_-
struct BiconnectedComponents {
    struct Edge {
        int from, to;
    };
```

```
struct To {
   int to; int edge;
    véctor < Edge > edges;
    vector < vector < To > > g;
    vector < int > low, ord, depth;
    vector < bool > isArtic;
    vector < int > edgeColor;
    vector < int > edgeStack;
    int colors;
    int dfsCounter;
    void init(int n) {
        edges.clear();
        g.assign(n, vector<To>());
    void addEdge(int u, int v) {
        if(u > v) swap(u, v);
        Edge e = \{ u, v \};
        int ei = edges.size();
        edges.push_back(e);
        To tu = { v, ei }, tv = { u, ei };
        g[u].push_back(tu);
        g[v].push_back(tv);
    void run() {
        int n = g.size(), m = edges.size();
        low.assign(n, -2);
        ord.assign(n, -1);
        depth.assign(n, -2);
        isArtic.assign(n, false);
        edgeColor.assign(m, -1);
        edgeStack.clear();
        colors = 0;
        for(int i = 0; i < n; ++ i) if(ord[i] == -1) \leftarrow
             dfsCounter = 0;
             dfs(i);
private:
    void dfs(int i) {
        low[i] = ord[i] = dfsCounter ++;
        for(int j = 0; j < (int)g[i].size(); ++ j) {</pre>
             int to = g[i][j].to, ei = g[i][j].edge;
             if (ord[to] == -1) {
                 depth[to] = depth[i] + 1;
                 edgeStack.push_back(ei);
                 dfs(to);
                 low[i] = min(low[i], low[to]);
                 if(low[to] >= ord[i]) {
    if(ord[i] != 0 || j >= 1)
                          isArtic[i] = true;
                      while(!edgeStack.empty()) {
                          int fi = edgeStack.back(); ←
                             edgeStack.pop_back();
                          edgeColor[fi] = colors;
                          if(fi == ei) break;
```

5.2 Bridges Online

```
vector<int> par, dsu_2ecc, dsu_cc, dsu_cc_size;
int bridges;
int lca_iteration;
vector < int > last_visit;
void init(int n) {
    par.resize(n);
    dsu_2ecc.resize(n);
    dsu_cc.resize(n);
    dsu_cc_size.resize(n);
    lca_iteration = 0;
    last_visit.assign(n, 0);
    for (int i=0; i < n; ++i) {
    dsu_2ecc[i] = i;</pre>
         dsu_cc[i] = i;
        dsu_cc_size[i] = 1;
        par[i] = -1;
    bridges = 0;
int find_2ecc(int v) { // 2-edge connected comp.
    if (v == -1)
        return -1;
    return dsu_2ecc[v] == v ? v : dsu_2ecc[v] = ←
       find_2ecc(dsu_2ecc[v]);
int find_cc(int v) { // connected comp.
    v = find_2ecc(v);
    return dsu_cc[v] == v ? v : dsu_cc[v] = find_cc( \leftrightarrow
       dsu_cc[v]);
void make_root(int v) {
    v = find_2ecc(v);
    int root = v;
    int child = -1;
    while (v != -1) {
        int p = find_2ecc(par[v]);
        par[v] = child;
        dsu_cc[v] = root;
         child = v;
        \vec{v} = \vec{p};
    dsu_cc_size[root] = dsu_cc_size[child];
}
```

```
void merge_path (int a, int b) {
    ++lca_iteration;
    vector < int > path_a, path_b;
    int lca = -1;
    while (lca == -1) {
   if (a != -1) {
            a = find_2ecc(a);
             path_a.push_back(a);
             if (last_visit[a] == lca_iteration)
                 lca = a;
            last_visit[a] = lca_iteration;
             a = par[a];
        }
if (b != -1) {
             path_b.push_back(b);
             b = find_2ecc(b);
             if (last_visit[b] == lca_iteration)
                 lca = b;
            last_visit[b] = lca_iteration;
             b = par[b];
        }
    for (int v : path_a) {
        dsu_2ecc[v] = lca;
        if (y == 1ca)
             break:
        --bridges;
    for (int v : path_b) {
        dsu_2ecc[v] = lca;
        if (y == lca)
             break;
        --bridges;
void add_edge(int a, int b) {
    a = find_2ecc(a);
    b = find_2ecc(b);
    if (a == b)
        return;
    int ca = find_cc(a);
    int cb = find_cc(b);
    if (ca != cb) {
        ++bridges;
        if (dsu_cc_size[ca] > dsu_cc_size[cb]) {
            swap(a, b);
             swap(ca, cb);
        make_root(a);
        par[a] = dsu_cc[a] = b;
        dsu_cc_size[cb] += dsu_cc_size[a];
        merge_path(a, b);
```

5.3 HLD

```
v is adjacency matrix of tree. clear v[i], hdc[i]=0,i\leftarrow
   =-1 before every run
clear ord and curc=0
const 11 MAX = 250005;
v11 v[MAX], ord;
ll par[MAX], noc[MAX], hdc[MAX], curc, posinch[MAX], len[←
   MAX], ti=-1;
11 sta[MAX], en[MAX], subs[MAX], level[MAX];
11 st[4*MAX], lazy[4*MAX];
11 n;
void dfs(ll x){
    subs[x]=1;
    for(auto z:v[x]){
   if(z!=par[x]){par[z]=x;level[z]=level[x]+1;
       dfs(z); subs[x] += subs[z];
         }}}
void makehld(ll x){
    if(hdc[curc]==0) {hdc[curc]=x;len[curc]=0;}
    noc[x] = curc; posinch[x] = ++len[curc];
    ll a,b,c;a=b=0;ord.pb(x);sta[x]=++ti;
    for(auto z:v[x]){    if(z==par[x])continue;
         if (subs[z]>b) {b=subs[z];a=z;}
    if(a!=0)makehld(a);
    for (auto z:v[x]) {if (z=par[x] | |z==a) continue; curc \leftarrow
        ++; makehld(z);}
    en[x]=ti;
inline void upd(11 x,11 y)//to update on path from a \leftarrow
   to b
  11 a,b,c,d;
  while (x!=y) {
    a=hdc[noc[x]], b=hdc[noc[y]];
    if(a==b)
       if (level [x] > level [y]) swap (x,y); c=sta[x], d=sta[y \leftarrow
       //lca=a:
       update(1,0,n-1,c+1,d); return;}
    if(level[a]>level[b])swap(a,b),swap(x,y);
    update (1,0,n-1,sta[b],sta[y]); y=par[b]; \} //update \leftarrow
         on segment tree
int main() {
    //v is adjacency matrix
    for(i=1;i<=n;i++) v[i].clear(),hdc[i]=0,ti=-1;
    ord.clear(),curc=0;
    level[1]=0; par[1]=0; curc=1; dfs(1); makehld(1);
    while (m--) {cin>>a>>b; upd (a,b); ll ans=sumq (1,0,n \leftarrow)
       -1,0,n-1);
```

5.4 LCA

```
const int N = int(1e5)+10;
const int LOGN = 20;
set < int > g[N];
int level[N];
int DP[LOGN][N];
int n,m;
/*----*/
/st Code Cridits : Tanuj Khattar codeforces submission\leftrightarrow
void dfs0(int u)
 for(auto it=g[u].begin();it!=g[u].end();it++)
    if (*it!=DP[0][u])
      DP[0][*it]=u;
      level[*it]=level[u]+1;
      dfs0(*it);
void preprocess()
  level [0] = 0;
 DP[0][0]=0;
  dfs0(0);
  for(int i=1;i<LOGN;i++)</pre>
    for(int j=0; j<n; j++)
      DP[i][j] = DP[i-1][DP[i-1][j]];
int lca(int a, int b)
  if(level[a]>level[b])swap(a,b);
  int d = level[b]-level[a];
  for(int i=0;i<LOGN;i++)</pre>
    if (d&(1<<i))
      b=DP[i][b];
  if(a==b)return a;
  for (int i=LOGN-1; i>=0; i--)
    if (DP[i][a]!=DP[i][b])
  a=DP[i][a], b=DP[i][b];
  return DP[0][a];
int dist(int u,int v)
  return level[u] + level[v] - 2*level[lca(u,v)];
```

5.5 Centroid Decompostion

```
/*
nx:maximum number of nodes
adj:adjacency list of tree,adj1: adjacency list of ←
centroid tree
par:parents of nodes in centroid tree,timstmp: ←
timestamps of nodes when they became centroids (←)
```

```
helpful in comparing which of the two nodes became\leftarrow
    centroid first)
ssize, vis:utility arrays for storing subtree size and←
    visit times in dfs
tim: utility for doing dfs (for deciding which nodes \hookleftarrow
   to visit)
cntrorder: centroids stored in order in which they \leftarrow
   were formed
dist[nx]: vector of vectors with dist[i][0][j]=number \leftrightarrow
   of nodes at distance of k in subtree of i in \leftarrow centroid tree and dist[i][j][k]=number of nodes at \leftarrow
    distance k in jth child of i in centroid tree \leftarrow
   ***(use adj while doing dfs instead of adj1)***
dfs: find subtree sizes visiting nodes starting from \leftarrow
   root without visiting already formed centroids
dfs1: root- starting node, n- subtree size remaining \leftarrow
   after removing centroids \rightarrow returns centroid in \leftarrow
subtree of root preprocess: stores all values in dist array
*/
const int nx=1e5;
vector<int> adj[nx],adj1[nx]; //adj is adjacency list←
    of tree and adj1 is adjacency list for centroid \leftarrow
int par[nx],timstmp[nx],ssize[nx],vis[nx];//par is ←
   parent of each node in centroid tree, ssize is \leftarrow
   subtree size of each node in centroid tree, vis and ←
    timstmp are auxillary arrays for visit times in \leftarrow
   dfs- timstmp contains nonzero values only for \leftarrow
centroids
int tim=1;
vector<int> cntrorder;//contains list of centroids \hookleftarrow
   generated (in order)
vector < vector < int > > dist[nx];
int dfs(int root)
  vis[root]=tim;
  int t=0;
  for(auto i:adj[root])
    if(!timstmp[i]&&vis[i]<tim)</pre>
       t += dfs(i);
  ssize[root]=t+1; return t+1;
int dfs1(int root,int n)
  vis[root]=tim;pair<int,int> mxc={0,-1};bool poss=←
     true:
  for(auto i:adj[root])
    if (!timstmp[i]&&vis[i]<tim)</pre>
       poss\&=(ssize[i] \le n/2), mxc=max(mxc, \{ssize[i], i\}) \leftarrow
  if (poss&&(n-ssize[root]) <= n/2) return root;
  return dfs1(mxc.second,n);
int findc(int root)
```

```
dfs(root);
  int n=ssize[root];tim++;
  return dfs1(root,n);
void cntrdecom(int root,int p)
  int cntr=findc(root);
  cntrorder.push_back(cntr);
  timstmp[cntr]=tim++;
  par[cntr]=p;
 if(p>=0)adj1[p].push_back(cntr);
  for(auto i:adj[cntr])
    if(!timstmp[i])
      cntrdecom(i,cntr);
void dfs2(int root, int nod, int j, int dst)
  if(dist[root][j].size() == dst) dist[root][j]. ←
     push_back(0);
  vis[nod] = tim;
  dist[root][j][dst]+=1;
  for(auto i:adj[nod])
    if((timstmp[i] \le timstmp[root]) | | (vis[i] == vis[nod \leftarrow)
       ]))continue;
    vis[i] = tim; dfs2(root, i, j, dst+1);
void preprocess()
  for(int i=0;i<cntrorder.size();i++)</pre>
    int root=cntrorder[i];
    vector < int > temp;
    dist[root].push_back(temp);
    temp.push_back(0);
    ++tim;
    dfs2(root,root,0,0);
    int cnt=0;
    for(int j=0;j<adj[root].size();j++)</pre>
      int nod=adj[root][j];
      if (timstmp[nod] < timstmp[root])</pre>
        continue;
      dist[root].push_back(temp);
      ++tim;
      dfs2(root, nod, ++cnt, 1);
```

6 Maths

6.1 Chinese Remainder Theorem

```
/*solves system of equations x=rem[i]%mods[i] for any←
    mod (need not be coprime)
intput: vector of remainders and moduli
output: pair of answer(x%lcm of modulo) and lcm of \leftarrow
   all the modulo (returns -1 if it is inconsistent)\leftarrow
11 GCD(11 a, 11 b) { return (b == 0) ? a : GCD(b, a \% \leftrightarrow
inline 11 LCM(11 a, 11 b) { return a / GCD(a, b) * b; \leftarrow
inline 11 normalize(11 x, 11 mod) { x \%= mod; if (x \iff
    0) x += mod; <u>return</u> x; }
struct GCD_type { ll x, y, d; };
GCD_type ex_GCD(ll a, ll b)
    if (b == 0) return {1, 0, a};
    GCD_type_pom = ex_GCD(b, a \% b);
    return {pom.y, pom.x - a / b * pom.y, pom.d};
pair<11,11> CRT(vector<11> &rem, vector<11> &mods)
    11 n=rem.size();
    ll ans=rem[0]
    11 1cm=mods[0];
    for(ll i=1;i<n;i++)
        auto pom=ex_GCD(lcm,mods[i]);
        11 x1=pom.x;
        11 d=pom.d;
        if ((rem[i]-ans)%d!=0) return {-1,0};
        ans=normalize(ans+x1*(rem[i]-ans)/d\%(mods[i]/\leftrightarrow
           d)*lcm,lcm*mods[i]/d);
        lcm=LCM(lcm,mods[i]); // you can save time by \leftarrow
            replacing above lcm * n[i] / d by lcm = \leftarrow
           lcm * n[i] / d
    return {ans,lcm};
```

6.2 Discrete Log

```
// Discrete Log , Baby-Step Giant-Step , e-maxx
// The idea is to make two functions,
// f1(p) , f2(q) and find p,q s.t.
// f1(p) = f2(q) by storing all possible values of f1
// and checking for q. In this case a^(x) = b (mod m)
is
// solved by substituting x by p.n-q , where
// is choosen optimally , usually sqrt(m).
```

```
// returns a soln. for a^(x) = b \pmod{m}
// for given a,b,m . -1 if no. soln.
// complexity : O(sqrt(m).log(m))
// use unordered_map to remove log factor.
// IMP : works only if a,m are co-prime. But can be \leftarrow
   modified.
int solve (int a, int b, int m) {
    int n = (int) sqrt (m + .0) + 1;
    int an = 1;
    for (int i=0; i<n; ++i)</pre>
        an = (an * a) % m;
    map < int , int > vals;
    for (int i=1, cur=an; i<=n; ++i) {
        if (!vals.count(cur))
            vals[cur] = i;
        cur = (cur * an) % m;
    for (int i=0, cur=b; i<=n; ++i) {</pre>
        if (vals.count(cur)) {
            int ans = vals[cur] * n - i;
            if (ans < m) return ans;
        cur = (cur * a) \% m;
    return -1;
```

6.3 NTT

```
Kevin's different Code: https://s3.amazonaws.com/←
   codechef_shared/download/Solutions/JUNE15/tester/<math>\leftarrow
   MOREFB.cpp
****There is no problem that FFT can solve while this\hookleftarrow
  NTT cannot Case1: If the answer would be small choose a small \leftarrow enough NTT prime modulus
  Case2: If the answer is large(> ~1e9) FFT would not←
       work anyway due to precision issues
  In Case2 use NTT. If max_answer_size=n*(\leftarrow
      largest_coefficient^2)
So use two or three modulus to solve it ****Compute a*b%mod if a%mod*b%mod would result in \hookleftarrow
   overflow in O(\log(a)) time:
  ll mulmod(ll a, ll b, ll mod) {
       11 \text{ res} = 0;
       while (a != 0) {
            if (a \& 1) res = (res + b) \% m;
            a >>= 1;
            b = (b << 1) \% m;
       return res;
Fastest NTT (can also do polynomial multiplication if \leftarrow
    max coefficients are upto 1e18 using 2 modulus ←
   and CRT)
How to use:
```

```
Polynomial1 = A[0]+A[1]*x^1+A[2]*x^2+..+A[n-1]*x^n-1
Polynomial2 = B[0]+B[1]*x^1+B[2]*x^2+..+B[n-1]*x^n-1
P=multiply(A,B)
A and B are not passed by reference because they are \leftarrow
   changed in multiply function
For CRT after obtaining answer modulo two primes p1 \leftarrow
   and p2:
x = a1 \mod p1, x = a2 \mod p2 = x = ((a1*(m2^-1)%m1)*m2 \leftrightarrow a2 \mod p2)
   +(a2*(m1^{-1})%m2)*m1)%m1m2
*** Before each call to multiply:
  set base=1, roots=\{0,1\}, rev=\{0,1\}, max_base=x (such \leftarrow
     that if mod=c*(2^k)+1 then x<=k and 2^x is \leftarrow
     greater than equal to nearest power of 2 of 2*n)
  root=primitive_root^((mod-1)/(2^max_base))
  For P=A*A use square function
Some useful modulo and examples
mod1 = 463470593 = 1768*2^18+1 primitive root = 3 => \leftrightarrow
   max_base=18, root=3^1768
mod2 = 469762049' = 1792 * 2^18 + 1 primitive root = 3 => \leftrightarrow
   max_base=18, root=3^1792
(mod1^-1)\%mod2=313174774 \quad (mod2^-1)\%mod1=154490124
Some prime modulus and primitive root
//x = a1 \mod m1, x = a2 \mod m2, invm2m1 = (m2^-1)\%m1, \leftarrow
    invm1m2 = (m1^-1) m2, gives x m1 * m2
#define chinese(a1,m1,invm2m1,a2,m2,invm1m2) ((a1 *1\leftarrow
   ll* invm2m1 % m1 * 1ll*m2 + a2 *1ll* invm1m2 % m2 \leftarrow * 1ll*m1) % (m1 *1ll* m2))
int mod;//reset mod everytime with required modulus
inline int mul(int a,int b){return (a*111*b)%mod;}
inline int add(int a, int b) \{a+=b; if(a>=mod)a-=mod; \leftarrow\}
   return a;}
inline int sub(int a,int b)\{a-b; if(a<0)a+mod; return \leftarrow a, int b\}
inline int power(int a, int b){int rt=1; while(b>0){if(\leftarrow
   b&1)rt=mul(rt,a);a=mul(a,a);b>>=1;}return rt;}
inline int inv(int a){return power(a, mod-2);}
```

```
inline void modadd(int &a,int &b){a+=b;if(a>=mod)a-=\leftrightarrow
   mod;}
int base = 1;
vector<int> roots = {0, 1};
vector < int > rev = \{0, 1\};
int max_base=18; //x such that 2^x|(mod-1) and 2^x>\longleftrightarrow
   max answer size(=2*n)
int root = 202376916;
                       //primitive root((mod-1)/(2^{\leftarrow}))
   max_base))
void ensure_base(int nbase) {
  if (nbase <= base) {</pre>
  assert(nbase <= max_base);
  rev.resize(1 << nbase);
  for (int i = 0; i < (1 << nbase); i++) {
    rev[i] = (rev[i \Rightarrow 1] \Rightarrow 1) + ((i & 1) << (nbase \leftarrow
       \bar{-1});
  roots.resize(1 << nbase);</pre>
  while (base < nbase) {
    int z = power(root, 1 << (max_base - 1 - base));</pre>
    roots[i << 1] = roots[i];
      roots[(i << 1) + 1] = mul(roots[i], z);
    base++;
void fft(vector<int> &a) {
  int n = (int) a.size();
  assert((n & (n - 1)) == 0);
  int zeros = __builtin_ctz(n);
  ensure_base(zeros);
  int shift = base - zeros;
  for (int i = 0; i < n; i++) {
    if (i < (rev[i] >> shift)) {
      swap(a[i], a[rev[i] >> shift]);
  for (int k = 1; k < n; k <<= 1) {
    for (int i = 0; i < n; i += 2 * k) {
      for (int j = 0; j < k; j++) {
        int x = a[i + j];
        int y = mul(a[i + j + k], roots[j + k]);
        a[i + j] = x + y - mod;
        if (a[i + j] < 0) a[i + j] += mod;
        a[i + j + k] = x - y + mod;
        if (a[i + j + k] > = mod) a[i + j + k] -= mod;
 }
vector\langle int \rangle multiply(vector\langle int \rangle a, vector\langle int \rangle b, \leftarrow
   int eq = 0) {
  int need = (int) (a.size() + b.size() - 1);
  int nbase = 0;
  while ((1 << nbase) < need) nbase++;</pre>
```

```
ensure_base(nbase);
int sz = 1 << nbase;
a.resize(sz);
b.resize(sz);
fft(a);
if (eq) b = a; else fft(b);
int inv_sz = inv(sz);
for (int i = 0; i < sz; i++) {
    a[i] = mul(mul(a[i], b[i]), inv_sz);
}
reverse(a.begin() + 1, a.end());
fft(a);
a.resize(need);
return a;
}
vector<int> square(vector<int> a) {
    return multiply(a, a, 1);
}
```

6.4 Online FFT

```
//f[i] = sum over j from 0 to i-1 f[j]*g[i-1-j]
//handle f[0] and g[0] separately
const int nx=131072; int f[nx], g[nx];
void onlinefft(int a, int b, int c, int d)
  vector < int > v1, v2;
  v1.pb(f+a,f+b+1); v2.pb(g+c,g+d+1); vector\langle int \rangle res=\langle int \rangle
     multiply(v1,v2);
  for(int i=0;i<res.size();i++)</pre>
    if (a+c+i+1<nx) f [a+c+i+1] = add(f [a+c+i+1], res[i]);</pre>
void precal()
  g[0]=1:
  for(int i=1;i<nx;i++)
    g[i]=power(i,i-1);
  f[\bar{1}]=1;
  for(int i=1;i<=100000;i++)
    f[i+1]=add(f[i+1],g[i]);f[i+1]=add(f[i+1],f[i]);
    f[i+2] = add(f[i+2], mul(f[i], g[1])); f[i+3] = add(f[i \leftarrow
        +3], mul(f[i],g[2]));
    for (int j=2; i\%j==0\&\&j<nx; j=j*2) on line fft (i-j, i \leftrightarrow j
        -1, i+1, 2*i);
```

6.5 Langrange Interpolation

```
/* Input :
```

```
Degree of polynomial: k
Polynomial values at x=0,1,2,3,...,k
Output:
Polynomial value at x
Complexity: O(degree of polynomial)
Works only if the points are equally spaced
ll lagrange(vll& v , int k, ll x,int mod){
    if(x \le k)
    return v[x];
ll inn = 1;
ll den = 1;
    for(int i = 1;i<=k;i++)
         inn = (inn*(x - i))%mod;
         den = (den*(mod - i))%mod;
    inn = (inn*inv(den % mod))%mod;
    11 \text{ ret} = 0;
    for (int i = 0; i <= k; i++) {
         ret = (ret + v[i]*inn)%mod;
         11 \text{ md} 1 = \text{mod} - ((x-i)*(k-i))\%\text{mod};
         11 \text{ md2} = ((i+1)*(x-i-1))\%\text{mod};
         if(i!=k)
              inn = (((inn*md1)\%mod)*inv(md2 \% mod))\% \leftarrow
    return ret;
```

6.6 Matrix Struct

```
struct matrix{
    ld B[N][N], n;
    matrix()\{\hat{n} = \hat{N}; memset(B,0,sizeof B);\}
    matrix(int _n){
        n = _n; memset(B, 0, sizeof B);
    void iden(){
      for(int i = 0; i < n; i++)
        B[i][i] = 1;
    void operator += (matrix M){
        for(int i = 0; i < n; i++)
          for (int j = 0; j < n; j++)
            B[i][j] = add(B[i][j], M.B[i][j]);
    void operator -= (matrix M){}
    void operator *= (ld b){}
    matrix operator - (matrix M){}
    matrix operator + (matrix M){
        matrix ret = (*this);
        ret += M; return ret;
    matrix operator * (matrix M){
```

```
matrix ret = matrix(n); memset(ret.B, 0, \leftarrow
           sizeof ret.B);
        for(int i = 0; i < n; i++)
            for (int j = 0; j < n; j++)
                 for (int k = 0; k < n; k++) {
                     ret.B[i][j] = add(ret.B[i][j], \leftarrow
                        mul(B[i][k], M.B[k][j]));
        return rét;
    matrix operator *= (matrix M){ *this = ((*this) *←
        M);
    matrix operator * (int b){
        matrix ret = (*this); ret *= b; return ret;
    vector <double > multiply (const vector <double > & v) ←
        const{
      vector < double > ret(n);
      for(int i = 0; i < n; i++)
        for (int j = 0; j < n; j++) {
          ret[i] += B[i][j] * v[j];
      return ret;
    }
};
```

6.7 nCr(Non Prime Modulo)

```
// sandwich, jtnydv25 video
// calculates nCr, for small
// non-prime modulo, and (very) big n,r.
ll phimod;
vll pr,prn;vll fact;
ll power(ll a, ll x, ll mod){
  ll ans=1;
  while(x){
    if ((1LL)&(x)) ans = (ans*a)%mod;
    a=(a*a)\%mod;x>>=1LL;
  return ans;
// prime factorization of x.
// pr-> prime ; prn -> it's exponent
void getprime(ll x){
    pr.clear();prn.clear();
    11 i,j,k;
    for(i=2;(i*i)<=x;i++){
      k=0; while ((x\%i)==0)\{k++; x/=i;\}
      if (k>0) {pr.pb(i);prn.pb(k);}
    if (x!=1) {pr.pb(x);prn.pb(1);}
    return;
// factorials are calculated ignoring
    multiples of p.
```

```
void primeproc(ll p,ll pe){    // p , p^e
    ll i,d;
    fact.clear(); fact.pb(1); d=1;
    for(i=1;i<pe;i++){
      if(i%p){fact.pb((fact[i-1]*i)%pe);}
      else {fact.pb(fact[i-1]);}
    return:
}
// again note this has ignored multiples of p
11 Bigfact(11 n,11 mod){
  ll ă,b,c,d,i,j,k;
  a=n/mod;a%=phimod;a=power(fact[mod-1],a,mod);
  b=n\%mod; a=(a*fact[b])\%mod;
  return a;
  Chinese Remainder Thm.
vll crtval, crtmod;
11 crt(vll &val, vil &mod){
  ll a,b,c,d,i,j,k;b=1;
  for(11 z:mod)b*=z;
  11 \text{ ans} = 0;
  for (i = 0; i < mod.size(); i++) {</pre>
    a=mod[i];c=b/a;
    d=power(c,(((a/pr[i])*(pr[i]-1))-1),a);
    c = (c*d)\%b; c = (c*val[i])\%b; ans = (ans+c)\%b;
  return ans;
// calculate for prime powers and
// take crt. For each prime power,
// first ignore multiples of p,
// and then do recursively, calculating
// the powers of p separately.
11 Bigncr(ll n,ll r,ll mod){
  ll ă,b,c,d,i,j,k;ll p,pe;
  getprime(mod); ll Fnum=1; ll Fden;
  crtval.clear(); crtmod.clear();
  for(i=0;i<pr.size();i++){</pre>
    Fnum=1; Fden=1;
    p=pr[i]; pe=power(p,prn[i],1e17);
    primeproc(p,pe);
    \bar{a} = 1; d = 0;
    phimod = (pe*(p-1LL))/p;
    11 n1=n,r1=r,nr=n-r;
    while (n1) {
      Fnum = (Fnum * (Bigfact(n1, pe)))%pe;
      Fden=(Fden*(Bigfact(r1,pe)))%pe;
      Fden=(Fden*(Bigfact(nr,pe)))%pe;
      d+=n1-(r1+nr);
      n1/=p;r1/=p;nr/=p;
    Fnum = (Fnum * (power (Fden, (phimod-1LL), pe)))%pe;
    if (d>=prn[i])Fnum=0;
    else Fnum=(Fnum*(power(p,d,pe)))%pe;
    crtmod.pb(pe); crtval.pb(Fnum);
```

```
// you can just iterate instead of crt
// for(i=0;i<mod;i++){
   // bool cg=true;
   // for(j=0;j<crtmod.size();j++){
      // if(i%crtmod[j]!=crtval[j])cg=false;
   // }
   // if(cg)return i;
   // }
   return crt(crtval,crtmod);
}</pre>
```

6.8 Primitive Root Generator

```
/*To find generator of U(p), we check for all
  g in [1,p]. But only for powers of the
  form phi(p)/p_j, where p_j is a prime factor of
  phi(p). Note that p is not prime here.
  Existence, if one of these: 1. p = 1,2,4
  2. p = q^k, where q \rightarrow odd prime.
  3. p = 2.(q^k), where q \rightarrow odd prime
  Note that a.g^(phi(p)) = 1 \pmod{p}
             b. there are phi(phi(p)) generators if \leftarrow
                exists.
// Finds "a" generator of U(p),
// multiplicative group of integers mod p.
// here calc_phi returns the toitent function for p
// Complexity : O(Ans.log(phi(p)).log(p)) + time for \leftarrow
   factorizing phi(p).
// By some theorem, Ans = O((\log(p))^6). Should be \leftarrow
   fast generally.
int generator (int p) {
    vector < int > fact;
    int phi = calc_phi(p), n = phi;
    for (int i=2; i*i<=n; ++i)
        if (n % i == 0) {
             fact.push_back (i);
             while (n \% i == 0)
                 n /= i:
    if (n > 1)
        fact.push_back (n);
    for (int res=2; res<=p; ++res) {</pre>
        if (gcd(res,p)!=1) continue;
        bool ok = true;
         for (size_t i=0; i<fact.size() && ok; ++i)</pre>
             ok &= powmod (res, phi / fact[i], p) != \leftarrow
        if (ok) return res;
    return -1;
```

7 Strings

7.1 Hashing Theory

```
If order not imp. and count/frequency imp. use this \hookleftarrow as hash fn:- ( (a_1+h)^k + (a_2+h)^k + (a_3+h)^k + (a_4+h)^k ) % p \hookleftarrow . Select : h,k,p Alternate: ((x)^(a_1)+(x)^(a_2)+...+(x)^(a_k))%mod where x and \hookleftarrow mod are fixed and a_1...a_k is an unordered set
```

7.2 Manacher

```
// Same idea as Z_algo, Time : O(n)
// [l,r] represents \dot{\cdot} boundaries of rightmost \leftrightarrow
   detected subpalindrom(with max r)
// takes string s and returns a vector of lengths of \leftarrow
   odd length palindrom
// centered around that char(e.g abac for 'b' returns←
    2(not 3))
vll manacher_odd(string s){
    ll n = s.length(); vll d1(n);
    for (ll i = 0, l = 0, r = -1; i < n; i++) {
         d1[i] = 1;
         if(i <= r){
              d1[i] = min(r-i+1,d1[1+r-i]); // use prev \leftarrow
         while (i+d1[i] < n && i-d1[i] >= 0 && s[i+d1[i\leftrightarrow]] == s[i-d1[i]]) d1[i]++; // trivial \leftrightarrow
         if (r < i+d1[i]-1) l=i-d1[i]+1, r=i+d1[i]-1; \leftrightarrow
            // update r
    return d1;
// takes string s and returns vector of lengths of \hookleftarrow
   even length ...
// (it's centered around the right middle char, bb is\hookleftarrow
    centered around the later 'b')
vll manacher_even(string s){
    ll n = s.length(); vll d2(n);
    for (11 i = 0, 1 = 0, r = -1; i < n; i++) {
         d2[i] = 0;
         if(i <= r){
              d2[i] = min(r-i+1, d2[1+r+1-i]);
         while(i+d2[i] < n_&& i_d2[i]-1 >= 0 && s[i+d2\leftarrow
             [i]] == s[i-d2[i]-1]) d2[i]++;
         if(d2[i] > 0 \&\& r < i+d2[i]-1) l=i-d2[i], r=i \leftrightarrow
            +d2[i]-1;
    return d2;
```

```
// Other mtd : To do both things in one pass, add \hookleftarrow special char e.g string "abc" => "$a$b$c$"
```

7.3 Suffix Array

```
//code credits - https://cp-algorithms.com/string/\leftarrow
   suffix-array.html
/*Theory :-
Sorted array of suffixes = sorted array of cyclic \leftarrow
   shifts of string+$.
We consider a prefix of len. 2^k of the cyclic, in \leftarrow
   the kth iteration.
And find the sorted order, using values for (k-1)th \leftarrow
   iteration and
kind of radix sort. Could be thought as some kind of \hookleftarrow
binary lifting. String of len. 2^k -> combination of 2 strings of len\leftrightarrow
     2^{(k-1)}, whose
order we know. Just radix sort on pair for next \hookleftarrow
   iteration.
Time :- O(nlog(n) + alphabet)
Applications :-
Finding the smallest cyclic shift; Finding a substring ↔
    in a string;
Comparing two substrings of a string; Longest common \leftarrow
   prefix of two substrings;
Number of different substrings.
// return list of indices(permutation of indices \leftrightarrow
   which are in sorted order)
vector<ll> sort_cyclic_shifts(string const& s) {
    ll n = s.size();
    const 11 alphabét = 256;
    //******** change the alphabet size accordingly \hookleftarrow
       and indexing *************
         vector<11> p(n), c(n), cnt(max(alphabet, n), <math>\leftarrow
            0);
    // p -> sorted order of 1-len prefix of each \hookleftarrow
        cyclic shift index.
    // c -> class of a index
    // pn -> same as p for kth iteration . ||ly cn.
    for (ll i = 0; i < n; i++)
         cnt[s[i]]++;
    for (ll i = 1; i < alphabet; i++)</pre>
         cnt[i] += cnt[i-1];
    for (11 i = 0; i < n; i++)
         p[--cnt[s[i]]] = i;
    c[p[0]] = 0;
    ll classes = 1;
    for (ll i = 1; i < n; i++) {
         if (s[p[i]] != s[p[i-1]])
             classes++;
         c[p[i]] = classes - 1;
         vector<ll> pn(n), cn(n);
```

```
for (ll h = 0; (1 << h) < n; ++h) {
        for (11 i = 0; i < n; i++) { // sorting w.r.\leftarrow
           t second part.
             pn[i] = p[i] - (1 << h);
             if (pn[i] < 0)
                 pn[i] += n:
        fill(cnt.begin(), cnt.begin() + classes, 0);
        for (ll i = 0; i < n; i++)
             cnt[c[pn[i]]]++;
        for (ll i = 1; i < classes; i++)</pre>
             cnt[i] += cnt[i-1];
        for (ll i = n-1; i >= 0; i--)
             p[--cnt[c[pn[i]]]] = pn[i];
                                             // sorting \leftarrow
                w.r.t first (more significant) part.
        cn[p[0]] = 0;
        classes = 1;
        for (ll i = 1; i < n; i++) { // determining \leftarrow
           new classes in sorted array.
             pair<11, 11> cur = {c[p[i]], c[(p[i] + (1 \leftrightarrow
                 << h)) % n]};
             pair<11, 11> prev = \{c[p[i-1]], c[(p[i-1] \leftrightarrow
                 + (1 << h)) % n]};
             if (cur != prev)
                 ++classes;
             cn[p[i]] = classes - 1;
        c.swap(cn);
    return p;
vector<ll> suffix_array_construction(string s) {
    vector<ll> sorted_shifts = sort_cyclic_shifts(s);
    sorted_shifts.erase(sorted_shifts.begin());
    return sorted_shifts;
// For comparing two substring of length 1 starting \leftarrow
// k - 2^k > 1/2. check the first 2^k part, if equal,
// check last 2^k part. c[k] is the c in kth iter of \leftarrow
   S.A construction.
int compare(int i, int j, int l, int k) {
    pair < int , int > a = \{c[k][i], c[k][(i+l-(1 << k))\} \leftarrow
    pair < int , int > b = {c[k][j], c[k][(j+1-(1 << k))%\leftarrow
    return a == b ? 0 : a < b ? -1 : 1;
Kasai's Algo for LCP construction :
Longest Common Prefix for consecutive suffixes in \leftarrow
   suffix array.
lcp[i] = length of lcp of ith and (i+1)th suffix in the <math>\leftarrow
    susffix array.
1. Consider suffixes in decreasing order of length.
```

```
2. Let p = s[i...n]. It will be somewhere in the S.A \leftarrow
   . We determine its lcp = k.
3. Then lcp of q=s[(i+1)...n] will be atleast k-1. \leftrightarrow
4. Remove the first char of p and its successor in \leftarrow
   the S.A. These are suffixes with lcp k-1.
5. But note that these 2 may not be consecutive in S. \leftarrow
   A. But however lcp of strings in
   b/w have to be also atleast k-1.
vector<11> lcp_construction(string const& s, vector<←
   11> const& p) {
    ll n = s.size();
    vector<ll> rank(n, 0);
    for (ll i = 0; i < n; i++)
        rank[p[i]] = i;
    11 k = 0;
    vector<ll> lcp(n-1, 0);
    for (ll i = 0; i < n; i++) {
        if (rank[i] == n - 1) {
             k = 0;
             continue;
        ll j = p[rank[i] + 1];
        while (i + k < n \&\& j + k < n \&\& s[i+k] == s[\leftarrow]
           j+k∫)
             k++;
        lcp[rank[i]] = k;
    return lcp;
```

7.4 Trie

```
const 11 AS = 26; // alphabet size
11 go[MAX][AS];
11 \text{ cnt}[MAX]; 11 \text{ cn}=0;
// cn -> index of next new node
// convert all strings to vll
11 newNode() {
  for(ll i=0; i < AS; i++)
     go[cn][i]=-1;
  return cn++;
// call newNode once ******
// before adding anything **
void addTrie(vll &x) {
  \overline{11} \overline{v} = \overline{0};
  cnt[v]++:
  for(ll i=0;i<x.size();i++){</pre>
    ll y=x[i];
    if(go[v][y] == -1)
       go[v][y] = newNode();
    v=go[v][y];
```

```
cnt[v]++;
}

// returns count of substrings with prefix x

ll getcount(vll &x){
    ll v=0;
    for(i=0;i<x.size();i++){
        ll y=x[i];
        if(go[v][y]==-1)
            go[v][y]=newNode();
        v=go[v][y];
    }
    return cnt[v];
}</pre>
```

7.5 Z-algorithm

```
// [1,r] -> indices of the rightmost segment match
// (the detected segment that ends rightmost(with max←
// 2 cases \overline{\phantom{a}} > 1st. i <= r : z[i] is atleast min(r-i\leftrightarrow
   +1,z[i-l]), then match trivially
// 2nd. o.w compute z[i] with trivial matching
// update l,r
// Time : O(n) (asy. behavior), Proof : each iteration\leftarrow
    of inner while loop make r pointer advance to \leftarrow
   right,
                    1) Search substring(text t,\leftarrow
// Applications:
   pattern p) s = p + '$' + t.
// 3) String compression(s = t+t+...+t, then find |t\leftarrow
// 2) Number of distinct substrings (in O(n^2))
// (useful when appending or deleting characters \leftarrow
   online from the end or beginning)
vector<ll> z_function(string s) {
    11 n = (11) s.length();
    vector<ll> z(n);
    for (ll i = 1, l = 0, r = 0; i < n; ++i) {
         if (i <= r)
             z[i] = min (r - i + 1, z[i - 1]); // use \leftrightarrow
                previous z val
         while (i + z[i] < n \&\& s[z[i]] == s[i + z[i]]
            ]]) // trivial matching
             ++z[i];
        if (i + z[i] - 1 > r)

l = i, r = i + z[i] - 1; // update \leftarrow
                rightmost segment matched
    return z;
```

```
const int K = 26;
// remember to set K
struct Vertex {
    int next[K]; bool leaf = false;
    int p = -1; char pch;
    int link = -1;
    int go[K];
    Vertex(int p=-1, char ch='\$') : p(p), pch(ch) {
        fill(begin(next), end(next), -1);
        fill(begin(go), end(go), -1);
};
vector < Vertex > aho(1);
void add_string(string const& s) {
    int v = 0;
    for (char ch : s),{
   int c = ch - 'a';
        if (aho[v].next[c] == -1) {
             aho[v].next[c] = aho.size();
             aho.emplace_back(v, ch);
        v = aho[v].next[c];
    aho[v].leaf = true;
int go(int v, char ch);
int get_link(int v) {
    if (aho[v].link == -1) {
        if (v'' == 0 | | aho[v].p == 0)
             aho[v].link = 0;
         else
             aho[v].link = go(get_link(aho[v].p), aho[ \leftarrow
                v].pch);
    return aho[v].link;
int go(int v, char ch) {
    int c = ch - a;
    if (aho[v].go[c] == -1) {
         if (aho[v].next[c] != -1)
             aho[v].go[c] = aho[v].next[c];
        else
             aho[v].go[c] = v == 0 ? 0 : go(get_link(v \leftarrow) )
                ), ch);
    return aho[v].go[c];
}
```

7.7 KMP

```
/*Time:O(n)(j increases n times(& j>=0) only so asy. \leftarrow O(n))
pi[i] = length of longset prefix of s ending at i
```

```
applications: search substring, # of different \leftarrow
   substrings(O(n^2)),
3) String compression(s = t+t+...+t, then find |t|, k\leftrightarrow
  =n-pi[n-1], if k|n
4) Building Automaton(Gray Code Example)*/
vector<ll> prefix_function(string s) {
    ll n = (ll)s.length();
    vector<ll> pi(n);
    for (ll i = 1; i < n; i++) {
    ll j = pi[i-1];
        while (\bar{j} > 0 \&\& s[i] != s[j])
        j = pi[j-1];
if (s[i] == s[j]) j++;
        pi[i] = i;
    return pi;
// searching s in t, returns all occurences(indices)
vector<ll> search(string s, string t){
    vll pi = prefix_function(s);
    ll m = s.length(); vll ans; ll j = 0;
    for(11 i=0;i<t.length();i++){</pre>
        while (j > 0 \&\& t[i] != s[j])
             j = pi[j-1];
        if(t[i] == s[j]) j++;
        if(j == m) ans.pb(i-m+1);
    return ans; // if ans empty then no occurence
```

```
++d;
while(true){
  a=i-1-len[cur];
  if (a>=0) {
  if (s[a]==s[i]) {
       if (child[cur][(ll)(s[i]-'a')]==-1) {
  par[d]=cur; child[cur][(ll)(s[i]-'a')]=d;
          len[d]=len[cur]+2; cur=d;
       else{
         par[d]=cur;len[d]=len[cur]+2;
         cur=child[cur][(ll)(s[i]-'a')];
       break;
  if (cur==0) break;
  cur=suli[cur];
if (cur!=d) continue;
if (len [d] == 1) suli [d] = 1;
else{
  c=suli[par[d]];
  while (child[c][(ll)(s[i]-'a')]==-1){
     if (c==0) break;
     c=suli[c];
  suli[d]=child[c][(l1)(s[i]-'a')];
```

7.8 Palindrome Tree

```
const ll MAX=1e5+15;
11 par[MAX]; // stores index of parent node
ll suli[MAX]; // stores index of suffix link
ll len[MAX]; // stores length of largest pallindrome↔
    ending at that node
ll child[MAX][30]; // stores the children of the \leftarrow
   node
index 0 - root "-1" index 1 - root "0"
therefore node of s[i] is i+2 initialize all child[i][j] to -1
void eer_tree(string s){
  ll a,b,c,d,i,j,k,e,f;
  suli[1]=0; suli[0]=0; len[1]=0; len[0]=-1;
  11 n=s.length();
  for(i=0;i<n+10;i++)
    for (j=0; j<30; j++) child [i][j]=-1;
  ll cur=1;d=1;
  for(i=0;i<s.size();i++){</pre>
```

7.9 Suffix Array

```
//code credits - https://cp-algorithms.com/string/←
   suffix-array.html
/*Theory :-
Sorted array of suffixes = sorted array of cyclic \leftarrow
   shifts of string+$.
We consider a prefix of len. 2^k of the cyclic, in \leftarrow
   the kth iteration.
And find the sorted order, using values for (k-1)th \leftrightarrow
Iteration and kind of radix sort. Could be thought as some kind of \hookleftarrow
   binary lifting.
String of len. 2^k -> combination of 2 strings of len\leftrightarrow
  \leftrightarrow 2^(k-1), whose
order we know. Just radix sort on pair for next \leftarrow
   iteration.
Time :- O(nlog(n) + alphabet)
Applications :-
Finding the smallest cyclic shift; Finding a substring ←
    in a string;
Comparing two substrings of a string; Longest common \leftarrow
   prefix of two substrings;
Number of different substrings.
```

```
}
return p;
// return list of indices(permutation of indices \leftarrow
   which are in sorted order)
                                                                 vector<ll> suffix_array_construction(string s) {
vector<ll> sort_cyclic_shifts(string const& s) {
                                                                     s += "$":
    ll n = s.size();
                                                                     vector<ll> sorted_shifts = sort_cyclic_shifts(s);
    const 11 alphabet = 256;
                                                                     sorted_shifts.erase(sorted_shifts.begin());
    //******* change the alphabet size accordingly \leftarrow
       and indexing ************
                                                                     return sorted_shifts;
                                                                 }// For comparing two substring of length 1 starting \hookleftarrow
        vector <11 > p(n), c(n), cnt(max(alphabet, n), \leftarrow
                                                                    at i,j.
    // p -> sorted order of 1-len prefix of each \hookleftarrow
                                                                 // k - 2<sup>\hat{}</sup>k > 1/2. check the first 2<sup>\hat{}</sup>k part, if equal,
       cyclic shift index.
                                                                 // check last 2^k part. c[k] is the c in kth iter of \leftarrow
    // c -> class of a index
// pn -> same as p for kth iteration . ||ly cn.
      / c -> class of a index
                                                                    S.A construction.
                                                                 int compare(int i, int j, int l, int k) {
    for (11 i = 0; i < n; i++)
                                                                     pair < int , int > a = \{c[k][i], c[k][(i+l-(1 << k))\} \leftarrow
         cnt[s[i]]++;
    for (ll i = 1; i < alphabet; i++)</pre>
                                                                     pair < int , int > b = {c[k][j], c[k][(j+1-(1 << k))%\leftarrow
         cnt[i] += cnt[i-1];
    for (ll i = 0; i < n; i++)
    p[--cnt[s[i]]] = i;</pre>
                                                                     return a == b ? 0 : a < b ? -1 : 1;
    c[p[0]] = 0;
    ll classes = 1;
                                                                 Kasai's Algo for LCP construction :
    for (ll i = 1; i < n; i++) {
    if (s[p[i]] != s[p[i-1]])
                                                                Longest Common Prefix for consecutive suffixes in \leftarrow
                                                                    suffix array.
             classes++;
                                                                 lcp[i]=length of lcp of ith and (i+1)th suffix in the \leftarrow
         c[p[i]] = classes - 1;
                                                                     susffix array.

    Consider suffixes in decreasing order of length.

         vector<ll> pn(n), cn(n);
                                                                 2. Let p = s[i...n]. It will be somewhere in the S.A \leftarrow
    for (11 h = 0; (1 << h) < n; ++h) {
                                                                    . We determine its lcp = k.
         for (11 i = 0; i < n; i++) { // sorting w.r.\leftarrow
                                                                 3. Then lcp of q=s[(i+1)...n] will be at least k-1. \leftrightarrow
            t second part.
             pn[i] = p[i] - (1 << h);
                                                                 4. Remove the first char of p and its successor in \hookleftarrow
             if (pn[i] < 0)
                                                                    the S.A. These are suffixes with lcp k-1.
                  pn[i] += n;
                                                                 5. But note that these 2 may not be consecutive in S. \leftarrow
                                                                    A. But however lcp of strings in
         fill(cnt.begin(), cnt.begin() + classes, 0);
                                                                    b/w have to be also atleast k-1.
         for (ll_i = 0; i < n; i++)
             cnt[c[pn[i]]]++;
                                                                 vector<11> lcp_construction(string const& s, vector <←
         for (ll i = 1; i < classes; i++)</pre>
                                                                    11 > const& p) {
              cnt[i] += cnt[i-1];
                                                                     ll n = s.size();
         for (ll i = n-1; i \ge 0; i--)
                                                                     vector<ll> rank(n, 0);
             p[--cnt[c[pn[i]]] = pn[i];
                                              // sorting \leftarrow
                                                                     for (ll i = 0; i < n; i++)
                                                                          rank[p[i]] = i;
                 w.r.t first (more significant) part.
                                                                     11 k = 0;
         cn[p[0]] = 0;
                                                                     vector<ll> lcp(n-1, 0);
         classes = 1;
                                                                     for (11 i = 0; i < n; i++) {
         for (11 i = 1; i < n; i++) { // determining \leftarrow
                                                                          if (rank[i] == n'-1) {
    k = 0;
            new classes in sorted array.
             pair<11, 11> cur = {c[p[i]], c[(p[i] + (1 \leftarrow
                                                                              continue;
                  << h)) % n]};
             pair<11, 11> prev = {c[p[i-1]], c[(p[i-1]\leftrightarrow
                                                                          ll j = p[rank[i] + 1];
                 + (1 << h)) % n]};
                                                                          while (i + k < n \&\& j + k < n \&\& s[i+k] == s[\leftarrow]
             if (cur != prev)
                                                                             j+k∫)
                  ++classes;
                                                                              k++;
             cn[p[i]] = classes - 1;
                                                                          lcp[rank[i]] = k;
                                                                          if (k)
         c.swap(cn);
```

```
k--;
} return lcp;
}
```

// add the text to the tree, letter by letter for (la=0; la<(int)str.size(); ++la) ukkadd (str[la]-'a');</pre>

7.10 Suffix Tree

```
const int N=1000000, // set it more than 2*(len. of \leftrightarrow
   string)
string str;
                   // input string for which the \leftarrow
   suffix tree is being built
int chi[N][26],
lef[N], // left...
rig[N], // ...and right boundaries of the substring\leftarrow
    of a which correspond to incoming edge
par[N],
         // parent of the node
sfli[N],
          // suffix link
tv,tp,la,
        // the number of nodes
void ukkadd(int c) {
    suff:;
    if (rig[tv]<tp) {</pre>
        if (chi[tv][c]==-1) {chi[tv][c]=ts;lef[ts]=la\leftarrow
           ; par [ts++]=tv; tv=sfli[tv]; tp=rig[tv]+1; \leftarrow
           goto suff;}
        tv=chi[tv][c];tp=lef[tv];
    }
if (tp==-1 || c==str[tp]-'a')
        tp++;
    else d
        lef[ts]=lef[tv]; rig[ts]=tp-1; par[ts]=par[tv↔
           ]; chi[ts][str[tp]-'a']=tv;
        chi[ts][c]=ts+1; lef[ts+1]=la; par[ts+1]=ts;
        lef[tv]=tp; par[tv]=ts; chi[par[ts]][str[lef[←
           ts]]-'a']=ts; ts+=2;
        tv=sfli[par[ts-2]]; tp=lef[ts-2];
        while (tp <= rig[ts-2]) {tv=chi[tv][str[tp]-'←
           a']; tp+=rig[tv]-lef[tv]+1;}
        if (tp == rig[ts-2]+1) sfli[ts-2]=tv; else \leftarrow
           sfli[ts-2]=ts;
        tp=rig[tv]-(tp-rig[ts-2])+2; goto suff;
    }
void build() {
    ts=2;
    tv=0:
    tp=0;
    11 ss = str.size(); ss*=2; ss+=15;
    fill(rig,rig+ss,(int)str.size()-1);
    // initialize data for the root of the tree
    sfli[0]=1; lef[0]=-1;
    rig[0]=-1; lef[1]=-1; rig[1]=-1;
    for(ll i=0;i<ss;i++)</pre>
        fill (chi[i], chi[i]+27, -1);
    fill(chi[1],chi[1]+26,0);
```