

Codebook- Team Far_Behind

IIT Delhi, India

Ayush Ranjan, Naman Jain, Manish Tanwar

Contents

1 Syntax	1	5.3 HLD	19
1.1 Template	1	5.4 LCA	19
1.2 C++ Sublime Build	3	5.5 Centroid Decompostion	19
2 Data Structures	3	6 Maths	21
2.1 Fenwick	3	6.1 Chinese Remainder Theorem	21
2.2 2D-BIT	3	6.2 Discrete Log	21
2.3 Segment Tree	3	6.3 NTT	21
2.4 Persistent Segment Tree	4	6.4 Online FFT	23
2.5 DP Optimization	5	6.5 Langrange Interpolation	23
3 Flows and Matching	6	6.6 Matrix Struct	23
3.1 General Matching	6	6.7 nCr(Non Prime Modulo)	24
3.2 Global Mincut	7	6.8 Primitive Root Generator	25
3.3 Hopcroft Matching	7	7 Strings	25
3.4 Dinic	8	7.1 Hashing Theory	25
3.5 Edmond Karp	8	7.2 Manacher	25
3.6 Ford Fulkerson	9	7.3 Suffix Array	26
3.7 Push Relabel	9	7.4 Trie	27
3.8 MCMF	10	7.5 Z-algorithm	27
3.9 MinCost Matching	11	7.6 Aho Corasick	28
4 Geometry	13	7.7 KMP	28
4.1 Geometry	13	7.8 Palindrome Tree	28
4.2 Convex Hull	15	7.9 Suffix Array	29
4.3 Convex Hull Trick	16	7.10 Suffix Tree	30
5 Trees	17	1 Syntax	
5.1 BlockCut Tree	17	1.1 Template	
5.2 Bridges Online	18	<code>#include <bits/stdc++.h></code>	
		<code>#include <ext/pb_ds/assoc_container.hpp></code>	

```

using namespace __gnu_pbds;
using namespace std;
template<class T> ostream& operator<<(ostream &os, ←
    vector<T> V) {
    os << "["; for(auto v : V) os << v << " "; return ←
    os << "];"}
template<class L, class R> ostream& operator<<(←
    ostream &os, pair<L,R> P) {
    return os << "(" << P.first << "," << P.second << "←
    )";}
#define TRACE
#ifdef TRACE
#define trace(...) _f(#__VA_ARGS__, __VA_ARGS__)
template <typename Arg1>
void _f(const char* name, Arg1&& arg1){
    cout << name << " : " << arg1 << std::endl;
}
template <typename Arg1, typename... Args>
void _f(const char* names, Arg1&& arg1, Args&&... ←
    args){
    const char* comma = strchr(names + 1, ',');cout.<<
    write(names, comma - names) << " : " << arg1<<" ←
    | ";_f(comma+1, args...);
}
#else
#define trace(...) 1
#endif
#define ll long long
#define ld long double
#define vll vector<ll>
#define pll pair<ll,ll>
#define vpll vector<pll>
#define I insert
#define pb push_back
#define F first
#define S second
#define all(x) x.begin(),x.end()
#define endl "\n"
// const ll MAX=1e6+5;
// int mod=1e9+7;
inline int mul(int a,int b){return (a*1ll*b)%mod;}
inline int add(int a,int b){a+=b;if(a>=mod)a-=mod;←
    return a;}
inline int sub(int a,int b){a-=b;if(a<0)a+=mod;return←
    a;}
inline int power(int a,int b){int rt=1;while(b>0){if(←
    b&1)rt=mul(rt,a);a=mul(a,a);b>>=1;}return rt;}
inline int inv(int a){return power(a,mod-2);}
inline void modadd(int &a,int b){a+=b;if(a>=mod)a-=←
    mod;}
int main(){
    ios_base::sync_with_stdio(false);cin.tie(0);cout.<<
    tie(0);cout<<setprecision(25);
}
// clock
clock_t clk = clock();
clk = clock() - clk;
((ld)clk)/CLOCKS_PER_SEC
// fastio

```

```

inline ll read() {
    ll n = 0; char c = getchar_unlocked();
    while (!('0' <= c && c <= '9')) c = ←
    getchar_unlocked();
    while ('0' <= c && c <= '9')
        n = n * 10 + c - '0', c = getchar_unlocked();
    return n;
}
inline void write(ll a){
    register char c; char snum[20]; ll i=0;
    do{
        snum[i++]=a%10+48;
        a=a/10;
    }
    while(a!=0); i--;
    while(i>=0)
        putchar_unlocked(snum[i--]);
    putchar_unlocked('\n');
}
using getline, use cin.ignore()
// gp_hash_table
#include <ext/pb_ds/assoc_container.hpp>
using namespace __gnu_pbds;
gp_hash_table<int, int> table; //cc_hash_table can ←
also be used
//custom hash function
const int RANDOM = chrono::high_resolution_clock::now←
().time_since_epoch().count();
struct chash {
    int operator()(int x) { return hash<int>{}(x ^ ←
    RANDOM); }
};
gp_hash_table<int, int, chash> table;
//custom hash function for pair
struct chash {
    int operator()(pair<int,int> x) const { return x.←
    first* 31 + x.second; }
};
// random
mt19937 rng(chrono::steady_clock::now().←
time_since_epoch().count());
uniform_int_distribution<int> uid(1,r);
int x=uid(rng);
//mt19937_64 rng(chrono::steady_clock::now().←
time_since_epoch().count());
// - for 64 bit unsigned numbers
vector<int> per(N);
for (int i = 0; i < N; i++)
    per[i] = i;
shuffle(per.begin(), per.end(), rng);
// string splitting
// this splitting is better than custom function(w.r.←
t time)
string line = "Ge";
vector <string> tokens;
stringstream check1(line);
string ele;

```

```
// Tokenizing w.r.t. space ' '
while(getline(check1, ele, ' '))
tokens.push_back(ele);
```

1.2 C++ Sublime Build

```
{
  "cmd": ["bash", "-c", "g++ -std=c++11 -O3 '${file}' -o '${file_path}/${file_base_name}' && gnome-terminal -- bash -c '\"${file_path}/${file_base_name}\" < input.txt > output.txt'"],
  "file_regex": "^(..[^:]*):([0-9]+):?([0-9]+)??:?(.*)$",
  "working_dir": "${file_path}",
  "selector": "source.c++, source.cpp",
}
```

2 Data Structures

2.1 Fenwick

```

/*All indices are 1 indexed*/
/*Range update and point query: maintain BIT of  $\leftarrow$ 
    prefix sum of updates
    to add val in range [a,b] add val at a and -val at  $\leftarrow$ 
        b
    value[a]=BITsum(a)+arr[a] where arr is constant*/
/***Range update and range query: maintain 2 BITs B1  $\leftarrow$ 
    and B2
    **to add val in [a,b] add val at a and -val at b+1 in $\leftarrow$ 
        B1. Add val*(a-1) at a and -val*b at b+1
    **sum[1,b]=B1sum(1,b)*b-B2sum(1,b)
    **sum[a,b]=sum[1,b]-sum[1,a-1]*/
ll n;
ll fen[MAX_N];
void update(ll p,ll val){
    for(ll i = p;i <= n;i += i & -i)
        fen[i] += val;
}
ll sum(ll p){
    ll ans = 0;
    for(ll i = p;i;i -= i & -i)
        ans += fen[i];
    return ans;
}

```

2.2 2D-BIT

```

//point updates and range sum in a ractangle
//all indices are 1 indices. to increment value of ←
cell (i,j) by val call update(x,y,val)
//to find sum of rectangle [a,b]-[c,d] find sum of ←
rectangles [1,1]-[c,d],[1,1]-[c,b],
//[1,1][a,d] and [1,1]-[a,b] and use inclusion ←
exclusion
ll bit[MAX][MAX];
void update(ll x , ll y, ll val)
{
    while( x < MAX )
    {
        ll y1 = y;
        while( y1 < MAX )
            bit[x][y1] += val , y1 += ( y1 & -y1 );
        x += ( x & -x );
    }
}
ll sum(ll x , ll y)
{
    ll ans = 0;
    while( x > 0 )
    {
        ll y1 = y;
        while( y1 > 0 )
            ans += bit[x][y1] , y1 -= ( y1 & -y1 );
        x -= ( x & -x );
    }
    return ans;
}

```

2.3 Segment Tree

```

/*
Sum segment tree
All arrays are 0 indexed. How to use:
to build segtree for arr[n] build(0,n-1,1)
to increment all values in [x,y] by val: upd(0,n-1,1,↵
    x,y,val)
call ppgt before every recursive call
to get sum of range [x,y]: sum(0,n-1,1,x,y)
for an array of size N use segment tree of size 4*N
*/
#define ll long long
const ll N=1e5+10;
ll arr[N],st[N<<2], lazy[N<<2];
void ppgt(ll l, ll r,ll id)
{
    if(l == r) return;
    ll m = l + r >> 1;
    lazy[id << 1] += lazy[id]; lazy[id << 1 | 1] += ↵
        lazy[id];
    st[id << 1] += (m - l + 1) * lazy[id];
    st[id << 1 | 1] += (r - m) * lazy[id];
}

```

```

    lazy[id] = 0;
}
void build(ll l,ll r,ll id)
{
    if(l==r) { st[id] = arr[l]; return; }
    build ( l, l+r >>1 , id<< 1); build( (1 + r >> 1) + <
        1, r , id<< 1 | 1);
    st[id] = st[ id << 1] + st[id << 1 | 1];
}
void upd(ll l,ll r,ll id,ll x,ll y,ll val)
{
    if (l > y || r < x ) return;
    ppgt(l, r, id);
    if (l >= x && r <= y ) { lazy[id] += val; st[id] += <
        (r - l + 1)*val; return;}
    upd(l,l + r >> 1,id << 1, x, y, val);upd((1 + r >> <
        1) + 1,r ,id << 1 | 1,x, y, val);
    st[id] = st[id << 1] + st[ id << 1 | 1];
}
ll sum(ll l,ll r,ll id,ll x,ll y)
{
    if (l > y || r < x ) return 0;
    ppgt(l, r, id);
    if (l >= x && r <= y ) return st[id];
    return sum(l, l + r >> 1,id << 1, x, y) + sum((1 + <
        r >> 1 ) + 1,r ,id << 1 | 1,x, y);
}

```

2.4 Persistent Segment Tree

```

/*Persistent Segment Tree for sum with point updates <
    and range sum
Usage: See sample main for kth largest number in a <
    range
**id of first node is 0. call build(0,n-1) first. <
    afterwards call upd(0,n-1,previous id,i,val) to <
    add
val in ith number. it returns root of new segment <
    tree after modification
**sum(0,n-1,id of root,l,r) gives sum of values in <
    whose index is between l and r in
tree rooted at id
**size of st,lchild and rchild should be at least N<
    *2+Q*logN
*/
const ll N=1e5+10;
ll arr[N],st[20*N];
ll lchild[20*N],rchild[20*N];
ll ids[N];
ll cnt=0;
void build(ll l,ll r)
{
    if(l==r) { lchild[cnt] = rchild[cnt] = -1; st[cnt] <
        = arr[l]; ++cnt; return; }
    ll id = cnt++;
    lchild[id] = cnt;

```

```

    build ( l, l+r >>1);
    rchild[id] = cnt; build( (1 + r >> 1) + 1, r);
    st[id] = st[lchild[id]] + st[rchild[id]];
}
ll upd(ll l,ll r,ll id,ll x,ll val)
{
    if(l == r) {lchild[cnt] = rchild[cnt] = -1; st[cnt]<
        = st[id] + val; ++cnt; return cnt-1;}
    ll myid = cnt++; ll mid = l + r >>1;
    if(x <= mid)
        rchild[myid] = rchild[id],lchild[myid] = upd(l, <
            mid, lchild[id], x, val);
    else
        lchild[myid] = lchild[id],rchild[myid] = upd(mid<
            +1, r, rchild[id], x, val);
    st[myid] = st[lchild[myid]] + st[rchild[myid]];<
        return myid;}
ll sum(ll l,ll r,ll id,ll x,ll y)
{
    if (l > y || r < x ) return 0;
    if (l >= x && r <= y ) return st[id];
    return sum(l, l + r >> 1,lchild[id], x, y) + sum((l<
        + r >> 1 ) + 1,r ,rchild[id],x, y);
}
ll gkth(ll l,ll r,ll id1,ll id2,ll k)
{
    if(l==r) return l;
    ll mid = l+r>>1;
    ll a = st[lchild[id2]] - (id1 >= 0 ? st[lchild[id1]<
        ] : 0);
    if(a >= k)
        return gkth(l, mid ,(id1>=0?lchild[id1]:-1), <
            lchild[id2], k);
    else
        return gkth(mid+1, r,(id1>=0?rchild[id1]:-1), <
            rchild[id2], k-a);
}
int main()
{
    ll n,m;cin>>n>>m;vector<ll> finalid(n);vll v;
    for(ll i=0;i<n;i++)cin>>arr[i],v.pb({arr[i],i});<
        sort(all(v));
    for(ll i=0;i<n;i++)finalid[v[i].second]=i;memset(<
        arr,0,sizeof(ll)*N);
    arr[finalid[0]]++;build(0,n-1);
    for(ll i=1;i<n;i++) ids[i]=upd(0,n-1,ids[i-1],<
        finalid[i],1);
    while(m--){
        ll i,j,k;cin>>i>>j>>k;
        --i;--j;
        ll ans=gkth(0,n-1,(i==0?-1:ids[i-1]),ids[j],k);
        cout<<v[ans].F<<endl;}
}

```

2.5 DP Optimization

```

/*You have an array of size L.You need to split it ←
into G intervals,
minimizing the cost. (G<=L otherwise we can just ←
split in 1-intervals).
There is a cost function C[i,j] of taking an interval←
. The cost function
satisfies : C[a,b]+C[c,d]<=C[a,d]+ C[c,b] for all a<=←
c<=b<=d.
This is the quadrangle inequality and intuitively you←
can think that
the cost function increases at a rate which is more ←
than linear
at all intervals (may not be strictly true). So , if ←
the cost function
satisfies this inequality, the following property ←
holds :
F(g,l) : min cost of splitting first l elements into g←
intervals
Basic recurrence : F(g,l) = min(F(g-1,k)+C(k+1,l)) ←
over all valid k.
P(g,l) : lowest position k s.t. it minimizes F(g,l).
P(g,0)<=P(g,1)<=P(g,2).....<=P(g,l-1)<=P(g,l). (←
DivConqOpti, O(G.L.log(L)))
Also, P(0,l)<=P(1,l)<=P(2,l)....<=P(G-1,l)<=P(G,l).
This with previous inequality leads to Knuth Opti, ←
complexity O(L.L).
For div&conq, we calculate P(g,l) for each g 1 by 1.←
In each g,
we calculate for mid-l and solve recursively using ←
the obtained
upper and lower bounds.For knuth, we use P(g,l-1)<=P(←
g,l)<=P(g+1,l),
and fill our table in increasing l and decreasing g.
In opt. BST type problems, use bk[i][j-1]<= bk[i][j]←
<=bk[i+1][j] . */
// Code for Divide and Conquer Opti O(G.L.log(L)): -
ll C[8111];
ll sums[8111];
ll F[811][8111]; // optimal value
int P[811][8111]; // optimal position.
// note first val. in arrays is for no. of groups
ll cost(int i, int j) { // cost function
    return i > j ? 0 : (sums[j] - sums[i-1]) * (j - i←
    + 1);
}
// fill(g,l1,l2,p1,p2) calculates all P[g][l] and F[g←
][l]
// for l1 <= l <= l2,with the knowledge that p1 <= P[←
g][l] <= p2
void fill(int g, int l1, int l2, int p1, int p2) {
    if (l1 > l2) return;
    int lm = (l1 + l2) >> 1;
    ll nv=INF,nv1=-1;
    for (int k = p1; k <= min(lm-1,p2); k++) {
        ll new_cost = F[g-1][k] + cost[k+1][lm];
        if (nv > new_cost) {

```

```

            nv = new_cost;
            nv1 = k;
        }
    }
    P[g][lm]=nv1; F[g][lm]=nv;
    fill(g, l1, lm-1, p1, P[g][lm]);
    fill(g, lm+1, l2, P[g][lm], p2);
}
int main() { // example call
    for(i=0;i<=n;i++) F[0][i]=INF;
    for(i=0;i<=k;i++) F[i][0]=0;
    F[0][0]=0;
    for(i=1;i<=k;i++) fill(i,1,n,0,n);
}
// Code for Knuth Optimization O(L.L) :-
ll dp[8002][802];
int a[8002],s[8002][802];
ll sum[8002];
// index strats from 1
ll run(int n,int m) {
    memset(dp,0xff,sizeof(dp));
    dp[0][0] = 0;
    for (int i = 1; i <= n; ++i) {
        sum[i] = sum[i - 1] + a[i];
        int maxj = min(i, m), mk;
        ll mn = INF;
        for (int k = 0; k < i; ++k) {
            if (dp[k][maxj - 1] >= 0) {
                ll tmp = dp[k][maxj - 1] +
                    (sum[i] - sum[k]) * (i - k); ←
                    //k + 1..i
                if (tmp < mn) {
                    mn = tmp;
                    mk = k;
                }
            }
        }
        dp[i][maxj] = mn;
        s[i][maxj] = mk;
        for (int j = maxj - 1; j >= 1; --j) {
            ll mn = INF;
            int mk;
            for (int k = s[i - 1][j]; k <= s[i][j + ←
            1]; ++k) {
                if (dp[k][j - 1] >= 0) {
                    ll tmp = dp[k][j - 1] +
                        (sum[i] - sum[k]) * (i - k);
                    if (tmp < mn) {
                        mn = tmp;
                        mk = k;
                    }
                }
            }
        }
        dp[i][j] = mn;
        s[i][j] = mk;
    }
}
}

```

```

    return dp[n][m];
}
// call -> run(n, min(n,m))

```

3 Flows and Matching

3.1 General Matching

```

/*Given any directed graph, finds maximal matching
Vertices-0-indexed, O(n^3) per call to edmonds*/
vll adj[MAXN]; int p[MAXN], base[MAXN], match[MAXN];
int lca(int n, int u, int v){
    vector<bool> used(n);
    for(;;) {
        u = base[u]; used[u] = true;
        if (match[u] == -1) break; u = p[match[u]];
    }
    for(;;) {
        v = base[v]; if (used[v]) return v;
        v = p[match[v]];
    }
}
void mark_path(vector<bool> &blo, int u, int b, int ←
child){
    for (; base[u] != b; u = p[match[u]]){
        blo[base[u]] = true; blo[base[match[u]]] = true;
        p[u] = child; child = match[u];
    }
}
int find_path(int n, int root) {
    vector<bool> used(n);
    for (int i = 0; i < n; ++i)
        p[i] = -1, base[i] = i;
    used[root] = true;
    queue<int> q; q.push(root);
    while(!q.empty()) {
        int u = q.front(); q.pop();
        for (int j = 0; j < (int)adj[u].size(); j++) {
            int v = adj[u][j];
            if(base[u]==base[v] || match[u]==v) continue;
            if(v==root || (match[v]!= -1 && p[match[v]]!= ←
-1)){
                int curr_base = lca(n, u, v);
                vector<bool> blossom(n);
                mark_path(blossom, u, curr_base, v);
                mark_path(blossom, v, curr_base, u);
                for(int i = 0; i < n; i++){
                    if(blossom[base[i]]){
                        base[i] = curr_base;
                        if(!used[i]) used[i] = true, q.push(i);
                    }
                }
            }
        }
    }
    else if (p[v] == -1){
        p[v] = u;
        if (match[v] == -1) return v;
        v=match[v]; used[v]=true; q.push(v);
    }
}

```

```

    }
    return -1;}
int edmonds(int n){
    for(int i=0;i<n;i++) match[i] = -1;
    for(int i = 0; i < n; i++){
        if (match[i] == -1) {
            int u, pu, ppu;
            for (u = find_path(n, i); u != -1; u = ppu) {
                pu = p[u]; ppu = match[pu];
                match[u] = pu; match[pu] = u;
            }
        }
    }
    int matches = 0;
    for (int i = 0; i < n; i++)
        if (match[i] != -1) matches++;
    return matches/2;
}
u--; v--; adj[u].pb(v); adj[v].pb(u);
cout << edmonds(n) * 2 << endl;
for (int i = 0; i < n; i++) {
    if (match[i] != -1 && i < match[i]) {
        cout << i + 1 << " " << match[i] + 1 << endl;
    }
}

```

3.2 Global Mincut

```

/*finds min weighted cut in undirected graph in
O(n^3), Adj Matrix, 0-indexed vertices
output-(min cut value, nodes in half of min cut)*/
typedef vector<int> VI;
typedef vector<VI> VVI;
const int INF = 1000000000;
pair<int, VI> GetMinCut(VVI &weights) {
    int N = weights.size();
    VI used(N), cut, best_cut;
    int best_weight = -1;
    for (int phase = N-1; phase >= 0; phase--) {
        VI w = weights[0];
        VI added = used;
        int prev, last = 0;
        for (int i = 0; i < phase; i++) {
            prev = last;
            last = -1;
            for (int j = 1; j < N; j++)
                if (!added[j] && (last == -1 || w[j] > w[last])) ←
last = j;
            if (i == phase-1) {
                for (int j = 0; j < N; j++) weights[prev][j] += ←
weights[last][j];
                for (int j = 0; j < N; j++) weights[j][prev] = ←
weights[prev][j];
                used[last] = true;
            }
        }
    }
}

```



```

cut.push_back(last);
if (best_weight == -1 || w[last] < best_weight) {
    best_cut = cut;
    best_weight = w[last];
}
} else {
for (int j = 0; j < N; j++)
    w[j] += weights[last][j];
added[last] = true;
}
}
return make_pair(best_weight, best_cut);
}
VVI weights(n, VI(n));
pair<int, VI> res = GetMinCut(weights);

```

3.3 Hopcroft Matching

```

// O(m * \sqrt{n})
struct graph {
    int L, R; // 0-indexed vertices
    vector<vector<int>> adj;
    graph(int L, int R) : L(L), R(R), adj(L+R) { }
    void add_edge(int u, int v) {
        adj[u].pb(v+L);
        adj[v+L].pb(u);
    }
    int maximum_matching() {
        vector<int> level(L), mate(L+R, -1);
        function<bool(void)> levelize = [&]() { // BFS
            queue<int> Q;
            for (int u = 0; u < L; ++u) {
                level[u] = -1;
                if (mate[u] < 0)
                    level[u] = 0, Q.push(u);
            }
            while (!Q.empty()) {
                int u = Q.front(); Q.pop();
                for (int w: adj[u]) {
                    int v = mate[w];
                    if (v < 0) return true;
                    if (level[v] < 0) {
                        level[v] = level[u] + 1; Q.push(v);
                    }
                }
            }
            return false;
        };
        function<bool(int)> augment = [&](int u) { // DFS
            for (int w: adj[u]) {
                int v = mate[w];
                if (v < 0 || (level[v] > level[u] && augment(
                    v))) {

```

```

                    mate[u] = w;
                    mate[w] = u;
                    return true;
                }
            }
            return false;
        };
        int match = 0;
        while (levelize())
            for (int u = 0; u < L; ++u)
                if (mate[u] < 0 && augment(u))
                    ++match;
        return match;
    }
};
int main() {
    int L, R, m;
    scanf("%d %d %d", &L, &R, &m);
    graph g(L, R);
    for (int i = 0; i < m; ++i) {
        int u, v;
        scanf("%d %d", &u, &v); u--;v--;
        g.add_edge(u, v);
    }
    printf("%d\n", g.maximum_matching());
}

```

3.4 Dinic

```

/*Time:  $O(m \cdot n^2)$  and for any unit capacity network  $O(\leftarrow m \cdot n^{1/2})$ 
Time:  $O(\min(fm, mn^2))$  (f: flow routed)
(so for bipartite matching as well)
In practice it is pretty fast for any bipartite  $\leftarrow$ 
network
I/O: n -> vertice; DinicFlow net(n);
for(z : edges) net.addEdge(z.F,z.S,cap);
max flow = maxFlow(s,t);
e=(u,v), e.flow represents the effective flow from u  $\leftarrow$ 
to v
(i.e f(u->v) - f(v->u)), vertices are 1-indexed
*** use int if possible(ll could be slow in dinic)  $\leftarrow$ 
*** */
struct edge {ll x, y, cap, flow;};
struct DinicFlow {
    // *** change inf accordingly *****
    const ll inf = (1e18);
    vector<edge> e;
    vector<ll> cur, d;
    vector<vector<ll>> > adj;
    ll n, source, sink;
    DinicFlow() {}
    DinicFlow(ll v) {
        n = v;
        cur = vector<ll>(n + 1);
        d = vector<ll>(n + 1);
        adj = vector<vector<ll>>(n + 1);
    }

```

```

}
void addEdge(ll from, ll to, ll cap) {
    edge e1 = {from, to, cap, 0};
    edge e2 = {to, from, 0, 0};
    adj[from].push_back(e1.size()); e.push_back(e1);
    adj[to].push_back(e2.size()); e.push_back(e2);
}
ll bfs() {
    queue<ll> q;
    for(ll i = 0; i <= n; ++i) d[i] = -1;
    q.push(source); d[source] = 0;
    while(!q.empty() and d[sink] < 0) {
        ll x = q.front(); q.pop();
        for(ll i = 0; i < (ll)adj[x].size(); ++i) {
            ll id = adj[x][i], y = e[id].y;
            if(d[y] < 0 and e[id].flow < e[id].cap) {
                q.push(y); d[y] = d[x] + 1;
            }
        }
    }
    return d[sink] >= 0;
}
ll dfs(ll x, ll flow) {
    if(!flow) return 0;
    if(x == sink) return flow;
    for(; cur[x] < (ll)adj[x].size(); ++cur[x]) {
        ll id = adj[x][cur[x]], y = e[id].y;
        if(d[y] != d[x] + 1) continue;
        ll pushed = dfs(y, min(flow, e[id].cap - e[id].flow));
        if(pushed) {
            e[id].flow += pushed;
            e[id ^ 1].flow -= pushed;
            return pushed;
        }
    }
    return 0;
}
ll maxFlow(ll src, ll snk) {
    this->source = src; this->sink = snk;
    ll flow = 0;
    while(bfs()) {
        for(ll i = 0; i <= n; ++i) cur[i] = 0;
        while(ll pushed = dfs(source, inf)) {
            flow += pushed;
        }
    }
    return flow;
}
};

```

3.5 Edmond Karp

```

// running time -  $O(n \cdot m^2)$ 
// The matrix capacity stores the capacity for every pair of vertices. adj
// is the adjacency list of the undirected graph, since we have also to use
// the reversed of directed edges when we are looking for augmenting paths.
// The function maxflow will return the value of the maximal flow. During
// the algorithm the matrix capacity will actually store the residual capacity
// of the network. The value of the flow in each edge will actually no stored,
// but it is easy to extent the implementation - by using an additional matrix
// - to also store the flow and return it.
const ll N = 3e3;
ll n; // number of vertices
ll capacity[N][N]; // adj matrix for capacity
vll adj[N]; // adj list of the corresponding undirected graph(***imp***)
// E = {1-2,2->3,3->2}, adj list should be => {1->2,2->1,2->3,3->2}
// *** vertices are 0-indexed ***
ll INF = (1e18);
ll bfs(ll s, ll t, vector<ll>& parent) {
    fill(parent.begin(), parent.end(), -1);
    parent[s] = -2;
    queue<pair<ll, ll>> q;
    q.push({s, INF});
    while (!q.empty()) {
        ll cur = q.front().first;
        ll flow = q.front().second;
        q.pop();
        for (ll next : adj[cur]) {
            if (parent[next] == -1 && capacity[cur][next]) {
                parent[next] = cur;
                ll new_flow = min(flow, capacity[cur][next]);
                if (next == t)
                    return new_flow;
                q.push({next, new_flow});
            }
        }
    }
    return 0;
}
ll maxflow(ll s, ll t) {
    ll flow = 0; ll new_flow;
    vector<ll> parent(n);
    while (new_flow = bfs(s, t, parent)) {
        flow += new_flow;
        ll cur = t;
    }
}

```



```

        while (cur != s) {
            ll prev = parent[cur];
            capacity[prev][cur] -= new_flow;
            capacity[cur][prev] += new_flow;
            cur = prev;
        }
    }
    return flow;
}

```

3.6 Ford Fulkerson

```

// running time - O(f*m) (f -> flow routed)
const ll N = 3e3;
ll n; // number of vertices
ll capacity[N][N]; // adj matrix for capacity
vll adj[N]; // adj list of the corresponding ←
undirected graph(**imp**)
// E = {1-2,2->3,3->2}, adj list should be => ←
{1->2,2->1,2->3,3->2}
// *** vertices are 0-indexed ***
ll INF = (1e18);
ll snk, cnt; // cnt for vis, no need to initialize ←
vector<ll> par, vis;
ll dfs(ll u, ll curr_flow) {
    vis[u] = cnt; if(u == snk) return curr_flow;
    if(adj[u].size() == 0) return 0;
    for(ll j=0; j<5; j++){ // random for good ←
        augmentation(**sometimes take time**)
        ll a = rand()%(adj[u].size());
        ll v = adj[u][a];
        if(vis[v] == cnt || capacity[u][v] == 0) ←
            continue;
        par[v] = u;
        ll f = dfs(v, min(curr_flow, capacity[u][v])); ←
        if(vis[snk] == cnt) return f;
    }
    for(auto v : adj[u]) {
        if(vis[v] == cnt || capacity[u][v] == 0) ←
            continue;
        par[v] = u;
        ll f = dfs(v, min(curr_flow, capacity[u][v])); ←
        if(vis[snk] == cnt) return f;
    }
    return 0;
}
ll maxflow(ll s, ll t) {
    snk = t; ll flow = 0; cnt++;
    par = vll(n, -1); vis = vll(n, 0);
    while(ll new_flow = dfs(s, INF)) {
        flow += new_flow; cnt++;
        ll cur = t;
        while(cur != s) {
            ll prev = par[cur];

```

```

            capacity[prev][cur] -= new_flow;
            capacity[cur][prev] += new_flow;
            cur = prev;
        }
    }
    return flow;
}

```

3.7 Push Relabel

```

// Adjacency list implementation of FIFO push relabel ←
// maximum flow
// with the gap relabeling heuristic. This ←
// implementation is
// significantly faster than straight Ford-Fulkerson. ←
// It solves
// random problems with 10000 vertices and 1000000 ←
// edges in a few
// seconds, though it is possible to construct test ←
// cases that
// achieve the worst-case.
// Time: O(V^3)
// I/O:- addEdge(), src, snk ** vertices are 0-indexed ←
// **
// - To obtain the actual flow values, look at ←
// all edges with
// capacity > 0 (zero capacity edges are ←
// residual edges).
struct edge {
    ll from, to, cap, flow, index;
    edge(ll from, ll to, ll cap, ll flow, ll index) :
        from(from), to(to), cap(cap), flow(flow), index(←
        index) {}
};
struct PushRelabel {
    ll n;
    vector<vector<edge> > G;
    vector<ll> excess;
    vector<ll> dist, active, count;
    queue<ll> Q;
    PushRelabel(ll n) : n(n), G(n), excess(n), dist(n), ←
        active(n), count(2*n) {}
    void addEdge(ll from, ll to, ll cap) {
        G[from].push_back(edge(from, to, cap, 0, G[to]. ←
        size()));
        if (from == to) G[from].back().index++;
        G[to].push_back(edge(to, from, 0, 0, (ll)G[from]. ←
        size() - 1));
    }
    void enqueue(ll v) {
        if (!active[v] && excess[v] > 0) { active[v] = ←
        true; Q.push(v); }
    }
    void push(edge &e) {
        ll amt = min(excess[e.from], e.cap - e.flow);

```

```

    if (dist[e.from] <= dist[e.to] || amt == 0) ←
        return;
    e.flow += amt;
    G[e.to][e.index].flow -= amt;
    excess[e.to] += amt;
    excess[e.from] -= amt;
    enqueue(e.to);
}
void gap(ll k) {
    for (ll v = 0; v < n; v++) {
        if (dist[v] < k) continue;
        count[dist[v]]--; dist[v] = max(dist[v], n+1);
        count[dist[v]]++; enqueue(v);
    }
}
void relabel(ll v) {
    count[dist[v]]--;
    dist[v] = 2*n;
    for (ll i = 0; i < G[v].size(); i++)
        if (G[v][i].cap - G[v][i].flow > 0)
            dist[v] = min(dist[v], dist[G[v][i].to] + 1);
    count[dist[v]]++;
    enqueue(v);
}
void discharge(ll v) {
    for (ll i = 0; excess[v] > 0 && i < G[v].size(); i++)
        push(G[v][i]);
    if (excess[v] > 0) {
        if (count[dist[v]] == 1) gap(dist[v]);
        else relabel(v);
    }
}
ll getMaxFlow(ll s, ll t) {
    count[0] = n-1;
    count[n] = 1;
    dist[s] = n;
    active[s] = active[t] = true;
    for (ll i = 0; i < G[s].size(); i++) {
        excess[s] += G[s][i].cap;
        push(G[s][i]);
    }
    while (!Q.empty()) {
        ll v = Q.front(); Q.pop();
        active[v] = false; discharge(v);
    }
    ll totflow = 0;
    for (ll i = 0; i < G[s].size(); i++) totflow += G[s][i].flow;
    return totflow;
}
};

```

```

// 1. If a network with negative costs had no ←
// negative cycle it is possible to transform it into ←
// one with nonnegative ←
// costs. Using  $C_{ij\_new}(pi) = C_{ij\_old} + pi(i) - pi(j)$ , where  $pi(x)$  is shortest path from s to x in ←
// network with an ←
// added vertex s. The objective value remains ←
// the same ( $z\_new = z + constant$ ).  $z(x) = \sum(c_{ij} * x_{ij})$  ←
// (x->flow, c->cost, u->cap, r->residual cap).
// 2. Residual Network:  $c_{ji} = -c_{ij}$ ,  $r_{ij} = u_{ij} - x_{ij}$ , ←
//  $r_{ji} = x_{ij}$ .
// 3. Note: If edge (i,j),(j,i) both are there then ←
// residual graph will have four edges b/w i,j (pairs ←
// of parallel edges).
// 4. let  $x^*$  be a feasible soln, its optimal iff ←
// residual network  $Gx^*$  contains no negative cost ←
// cycle.
// 5. Cycle Cancelling algo => Complexity  $O(n*m^2*U * C)$  (C->max abs value of cost, U->max cap) ( $m*U*C$  ←
// iterations).
// 6. Successive shortest path algo => Complexity  $O(n^3 * B)$  /  $O(nm \log n)$  (using heap in Dijkstra) (B -> ←
// largest supply node).
// Works for negative costs, but does not work for ←
// negative cycles
// Complexity:  $O(\min(E^2 * V \log V, E \log V * flow))$ 
// to use -> graph G(n), G.add_edge(u,v,cap,cost), G. ←
// min_cost_max_flow(s,t)
// ***** INF is used in both flow_type and ←
// cost_type so change accordingly
const ll INF = 999999999;
// vertices are 0-indexed
struct graph {
    typedef ll flow_type; // **** flow type ****
    typedef ll cost_type; // **** cost type ****
    struct edge {
        int src, dst;
        flow_type capacity, flow;
        cost_type cost;
        size_t rev;
    };
    vector<edge> edges;
    void add_edge(int src, int dst, flow_type cap, ←
        cost_type cost) {
        adj[src].push_back({src, dst, cap, 0, cost, adj[ ←
            dst].size()});
        adj[dst].push_back({dst, src, 0, 0, -cost, adj[ ←
            src].size()-1});
    }
    int n;
    vector<vector<edge>> adj;
    graph(int n) : n(n), adj(n) { }
    pair<flow_type, cost_type> min_cost_max_flow(int s, ←
        int t) {
        flow_type flow = 0;

```

3.8 MCMF

// MCMF Theory:

```

cost_type cost = 0;
for (int u = 0; u < n; ++u) // initialize
    for (auto &e: adj[u]) e.flow = 0;
vector<cost_type> p(n, 0);
auto rcost = [&](edge e) { return e.cost + p[e.src] - p[e.dst]; };
for (int iter = 0; ; ++iter) {
    vector<int> prev(n, -1); prev[s] = 0;
    vector<cost_type> dist(n, INF); dist[s] = 0;
    if (iter == 0) { // use Bellman-Ford to remove negative cost edges
        vector<int> count(n); count[s] = 1;
        queue<int> que;
        for (que.push(s); !que.empty(); ) {
            int u = que.front(); que.pop();
            count[u] = -count[u];
            for (auto &e: adj[u]) {
                if (e.capacity > e.flow && dist[e.dst] > dist[e.src] + rcost(e)) {
                    dist[e.dst] = dist[e.src] + rcost(e);
                    prev[e.dst] = e.rev;
                    if (count[e.dst] <= 0) {
                        count[e.dst] = -count[e.dst] + 1;
                        que.push(e.dst);
                    }
                }
            }
        }
    }
    for (int i=0; i<n; i++) p[i] = dist[i]; // added
    continue;
} else { // use Dijkstra
    typedef pair<cost_type, int> node;
    priority_queue<node, vector<node>, greater<node>> que;
    que.push({0, s});
    while (!que.empty()) {
        node a = que.top(); que.pop();
        if (a.S == t) break;
        if (dist[a.S] > a.F) continue;
        for (auto e: adj[a.S]) {
            if (e.capacity > e.flow && dist[e.dst] > a.F + rcost(e)) {
                dist[e.dst] = dist[e.src] + rcost(e);
                prev[e.dst] = e.rev;
                que.push({dist[e.dst], e.dst});
            }
        }
    }
}
if (prev[t] == -1) break;
for (int u = 0; u < n; ++u)
    if (dist[u] < dist[t]) p[u] += dist[u] - dist[t];
function<flow_type(int, flow_type)> augment = [&](int u, flow_type cur) {

```

```

    if (u == s) return cur;
    edge &r = adj[u][prev[u]], &e = adj[r.dst][r.rev];
    flow_type f = augment(e.src, min(e.capacity - e.flow, cur));
    e.flow += f; r.flow -= f;
    return f;
};
flow_type f = augment(t, INF);
flow += f;
cost += f * (p[t] - p[s]);
}
return {flow, cost};
};

```

3.9 MinCost Matching

```

// Min cost bipartite matching via shortest augmenting paths
// This is an  $O(n^3)$  implementation of a shortest augmenting path algorithm for finding min cost perfect matchings in dense graphs. In practice, it solves 1000x1000 problems in around 1 second.
// cost[i][j] = cost for pairing left node i with right node j
// Lmate[i] = index of right node that left node i pairs with
// Rmate[j] = index of left node that right node j pairs with
// The values in cost[i][j] may be positive or negative. To perform maximization, simply negate the cost[][] matrix.
typedef ll cost_type;
typedef vector<cost_type> VD;
typedef vector<VD> VVD;
typedef vector<int> VI;
cost_type MinCostMatching(const VVD &cost, VI &Lmate, VI &Rmate) {
    int n = int(cost.size());
    // construct dual feasible solution
    VD u(n);
    VD v(n);
    for (int i = 0; i < n; i++) {
        u[i] = cost[i][0];
        for (int j = 1; j < n; j++) u[i] = min(u[i], cost[i][j]);
    }
    for (int j = 0; j < n; j++) {

```

```

    v[j] = cost[0][j] - u[0];
    for (int i = 1; i < n; i++) v[j] = min(v[j], cost[
        [i][j] - u[i]);
}
// construct primal solution satisfying ←
// complementary slackness
Lmate = VI(n, -1);
Rmate = VI(n, -1);
int mated = 0;
for (int i = 0; i < n; i++) {
    for (int j = 0; j < n; j++) {
        if (Rmate[j] != -1) continue;
        if (fabs(cost[i][j] - u[i] - v[j]) < 1e-10) {
            //**** change this comparison if double cost ←
            ****
            Lmate[i] = j;
            Rmate[j] = i;
            mated++;
            break;
        }
    }
}
VD dist(n); VI dad(n); VI seen(n);
// repeat until primal solution is feasible
while (mated < n) {
    // find an unmatched left node
    int s = 0;
    while (Lmate[s] != -1) s++;
    // initialize Dijkstra
    fill(dad.begin(), dad.end(), -1);
    fill(seen.begin(), seen.end(), 0);
    for (int k = 0; k < n; k++)
        dist[k] = cost[s][k] - u[s] - v[k];
    int j = 0;
    while (true) {
        // find closest
        j = -1;
        for (int k = 0; k < n; k++) {
            if (seen[k]) continue;
            if (j == -1 || dist[k] < dist[j]) j = k;
        }
        seen[j] = 1;
        // termination condition
        if (Rmate[j] == -1) break;
        // relax neighbors
        const int i = Rmate[j];
        for (int k = 0; k < n; k++) {
            if (seen[k]) continue;
            const cost_type new_dist = dist[j] + cost[i][←
                k] - u[i] - v[k];
            if (dist[k] > new_dist) {
                dist[k] = new_dist;
                dad[k] = j;
            }
        }
    }
}
// update dual variables

```

```

for (int k = 0; k < n; k++) {
    if (k == j || !seen[k]) continue;
    const int i = Rmate[k];
    v[k] += dist[k] - dist[j];
    u[i] -= dist[k] - dist[j];
}
u[s] += dist[j];
// augment along path
while (dad[j] >= 0) {
    const int d = dad[j];
    Rmate[j] = Rmate[d];
    Lmate[Rmate[j]] = j;
    j = d;
}
Rmate[j] = s;
Lmate[s] = j;
mated++;
}
cost_type value = 0;
for (int i = 0; i < n; i++)
    value += cost[i][Lmate[i]];
return value;
}

```

4 Geometry

4.1 Geometry

```

//small non recursive functions should me made inline
//do not read input in double format if they are ←
//integer points
#define ld double
#define PI acos(-1)
//atan2(y,x) slope of line (0,0)->(x,y) in radian (←
//PI,PI]
// to convert to degree multiply by 180/PI
ld INF = 1e100;
ld EPS = 1e-9;
inline bool eq(ld a,ld b) {return fabs(a-b)<EPS;}
inline bool lt(ld a,ld b) {return a+EPS<b;}
inline bool gt(ld a,ld b) {return a>b+EPS;}
inline bool le(ld a,ld b) {return lt(a,b)||eq(a,b);}
inline bool ge(ld a,ld b) {return gt(a,b)||eq(a,b);}
struct pt {
    ld x, y;
    pt() {}
    pt(ld x, ld y) : x(x), y(y) {}
    pt(const pt &p) : x(p.x), y(p.y) {}
    pt operator + (const pt &p) const { return pt(x+p.←
        x, y+p.y); }
    pt operator - (const pt &p) const { return pt(x-p.←
        x, y-p.y); }
}

```

```

pt operator * (ld c)      const { return pt(x*c, y←
    *c ); }
pt operator / (ld c)      const { return pt(x/c, y←
    /c ); }
bool operator < (const pt &p) const{ return lt(y,p.←
    y)|| (eq(y,p.y)&&lt;(x,p.x));}
bool operator > (const pt &p) const{ return p<pt(x,←
    y);}
bool operator <= (const pt &p) const{ return !(pt(x←
    ,y)>p);}
bool operator >= (const pt &p) const{ return !(pt(x←
    ,y)<p);}
bool operator == (const pt &p) const{ return (pt(x,←
    y)<=p)&&(pt(x,y)>=p);}
};
ld dot(pt p,pt q) {return p.x*q.x+p.y*q.y;}
ld dist2(pt p, pt q) {return dot(p-q,p-q);}
ld dist(pt p,pt q) {return sqrt(dist2(p,q));}
ld norm2(pt p) {return dot(p,p);}
ld norm(pt p) {return sqrt(norm2(p));}
ld cross(pt p, pt q) { return p.x*q.y-p.y*q.x;}
ostream &operator<<(ostream &os, const pt &p) {
    return os << "(" << p.x << "," << p.y << ")";}
istream& operator >> (istream &is, pt &p){
    return is >> p.x >> p.y;}
//returns 0 if a,b,c are collinear,1 if a->b->c is cw←
//and -1 if ccw
int orient(pt a,pt b,pt c)
{
    pt p=b-a,q=c-b;double cr=cross(p,q);
    if(eq(cr,0))return 0;if(lt(cr,0))return 1;return ←
    -1;}
// rotate a point CCW or CW around the origin
pt RotateCCW90(pt p)      { return pt(-p.y,p.x); }
pt RotateCW90(pt p)       { return pt(p.y,-p.x); }
pt RotateCCW(pt p, ld t) { //rotate by angle t ←
    degree ccw
    return pt(p.x*cos(t)-p.y*sin(t), p.x*sin(t)+p.y*cos←
    (t)); }
// project point c onto line (not segment) through a ←
// and b assuming a != b
pt ProjectPointLine(pt a, pt b, pt c) {
    return a + (b-a)*dot(c-a, b-a)/dot(b-a, b-a);}
// project point c onto line segment through a and b ←
// (closest point on line segment)
pt ProjectPointSegment(pt a, pt b, pt c) {
    ld r = dot(b-a,b-a); if (eq(r,0)) return a;//a and ←
    b are same
    r = dot(c-a, b-a)/r;if (lt(r,0)) return a;//c on ←
    left of a
    if (gt(r,1)) return b; return a + (b-a)*r;}
// compute distance from c to segment between a and b
ld DistancePointSegment(pt a, pt b,pt c) {
    return sqrt(dist2(c, ProjectPointSegment(a, b, c))←
    );}
// compute distance from c to line between a and b
ld DistancePointLine(pt a, pt b, pt c) {
    return sqrt(dist2(c, ProjectPointLine(a, b, c)));}
// determine if lines from a to b and c to d are ←
// parallel or collinear
bool LinesParallel(pt a, pt b, pt c, pt d) {
    return eq(cross(b-a, c-d),0); }
bool LinesCollinear(pt a, pt b, pt c, pt d) {
    return LinesParallel(a, b, c, d) && eq(cross(a-b, a←
    -c),0) && eq(cross(c-d, c-a),0);}
// determine if line segment from a to b intersects ←
// with line segment from c to d
bool SegmentsIntersect(pt a, pt b, pt c, pt d) {
    if (LinesCollinear(a, b, c, d)) {
        //a->b and c->d are collinear and have one point ←
        common
        if(eq(dist2(a,c),0)||eq(dist2(a,d),0)||eq(dist2(b←
        ,c),0)||eq(dist2(b,d),0)) return true;
        if(gt(dot(c-a,c-b),0)&&gt;(dot(d-a,d-b),0)&&gt;(dot←
        (c-b,d-b),0)) return false;
        return true;}
    if(gt(cross(d-a,b-a)*cross(c-a,b-a),0)) return ←
    false;//c,d on same side of a,b
    if(gt(cross(a-c,d-c)*cross(b-c,d-c),0)) return ←
    false;//a,b on same side of c,d
    return true;}
// compute intersection of line passing through a and←
// b
// with line passing through c and d,assuming that **←
// unique** intersection exists;
//*for segment intersection,check if segments ←
// intersect first
pt ComputeLineIntersection(pt a,pt b,pt c,pt d){
    b=b-a;d=c-d;c=c-a;//lines must not be collinear
    assert(gt(dot(b, b),0)&&gt;(dot(d, d),0));
    return a + b*cross(c, d)/cross(b, d);}
//returns true if point a,b,c are collinear and b ←
// lies between a and c
bool between(pt a,pt b,pt c){
    if(!eq(cross(b-a,c-b),0))return 0;//not collinear
    return lt(dot(b-a,b-c),0);
}
//compute intersection of line segment a-b and c-d
pt ComputeSegmentIntersection(pt a,pt b,pt c,pt d){
    if(!SegmentsIntersect(a,b,c,d))return {INF,INF};//←
    don't intersect
    //if collinear then infinite intersection points, ←
    this returns any one
    if(LinesCollinear(a,b,c,d)){if(between(a,c,b))←
    return c;if(between(c,a,d))return a;return b;}
    return ComputeLineIntersection(a,b,c,d);
}
// compute center of circle given three points - *a,b←
// ,c shouldn't be collinear
pt ComputeCircleCenter(pt a,pt b,pt c){
    b=(a+b)/2;c=(a+c)/2;

```



```

return ComputeLineIntersection(b,b+RotateCW90(a-b),←
    c,c+RotateCW90(a-c));}
//point in polygon using winding number -> returns 0 ←
//if point is outside
//winding number>0 if point is inside and equal to 0 ←
//if outside
//draw a ray to the right and add 1 if side goes from←
//up to down and -1 otherwise
bool PointInPolygon(const vector<pt> &p,pt q){
    int n=p.size(),windingNumber=0;
    for(int i=0;i<n;++i){
        if(eq(dist2(q,p[i]),0)) return 1;//q is a vertex
        int j=(i+1)%n;
        if(eq(p[i].y,q.y)&&eq(p[j].y,q.y)) {//i,i+1 ←
            vertex is vertical
            if(le(min(p[i].x,p[j].x),q.x)&&le(q.x,max(p[i].←
                x, p[j].x))) return 1;}//q lies on boundary
        else {
            bool below=lt(p[i].y,q.y);
            if(below!=lt(p[j].y,q.y)) {
                auto orientation=orient(q,p[j],p[i]);
                if(orientation==0) return 1;//q lies on ←
                boundary i->j
                if(below==(orientation>0)) windingNumber+=←
                    below?1:-1;}}}
    return windingNumber==0?0:1;
}
// determine if point is on the boundary of a polygon
bool PointOnPolygon(const vector<pt> &p,pt q) {
    for (int i = 0; i < p.size(); i++)
        if (eq(dist2(ProjectPointSegment(p[i],p[(i+1)%p.←
            size()],q),q),0)) return true;
    return false;}
// Compute area or centroid of any polygon (←
// coordinates must be listed in cw/ccw
// fashion.The centroid is often known as center of ←
// gravity/mass
ld ComputeSignedArea(const vector<pt> &p) {
    ld ans=0;
    for(int i = 0; i < p.size(); i++) {
        int j = (i+1) % p.size();
        ans+=cross(p[i],p[j]);
    } return ans / 2.0;}
ld ComputeArea(const vector<pt> &p) {
    return fabs(ComputeSignedArea(p));
}
// compute intersection of line through points a and ←
// b with
// circle centered at c with radius r > 0
vector<pt> CircleLineIntersection(pt a, pt b, pt c, ←
    ld r) {
    vector<pt> ret;
    b = b-a;a = a-c;
    ld A = dot(b, b),B = dot(a, b),C = dot(a, a) - r*r,←
        D = B*B - A*C;
    if (lt(D,0)) return ret; //don't intersect

```

```

ret.push_back(c+a+b*(-B+sqrt(D+EPS))/A);
    if (gt(D,0)) ret.push_back(c+a+b*(-B-sqrt(D))/A);
    return ret;}
// compute intersection of circle centered at a with ←
// radius r
// with circle centered at b with radius R
vector<pt> CircleCircleIntersection(pt a, pt b, ld r,←
    ld R) {
    vector<pt> ret;
    ld d = sqrt(dist2(a, b)),d1=dist2(a,b);
    pt inf(INF,INF);
    if(eq(d1,0)&&eq(r,R)){ret.pb(inf);return ret;}//←
    circles are same return (INF,INF)
    if(gt(d,r+R) || lt(d+min(r, R),max(r, R)) ) return ←
    ret;
    ld x = (d*d-R*R+r*r)/(2*d),y = sqrt(r*r-x*x);
    pt v = (b-a)/d;
    ret.push_back(a+v*x + RotateCCW90(v)*y);
    if (gt(y,0)) ret.push_back(a+v*x - RotateCCW90(v)*y←
    );
    return ret;}
//compute centroid of simple polygon by dividing it ←
//into disjoint triangles
//and taking weighted mean of their centroids (Jerome←
//)
pt ComputeCentroid(const vector<pt> &p) {
    pt c(0,0),inf(INF,INF);
    ld scale = 6.0 * ComputeSignedArea(p);
    if(p.empty())return inf;//empty vector
    if(eq(scale,0))return inf;//all points on straight ←
    line
    for (int i = 0; i < p.size(); i++){
        int j = (i+1) % p.size();
        c = c + (p[i]+p[j])*cross(p[i],p[j]);}
    return c / scale;}
// tests whether or not a given polygon (in CW or CCW←
// order) is simple
bool IsSimple(const vector<pt> &p) {
    for (int i = 0; i < p.size(); i++) {
        for (int k = i+1; k < p.size(); k++) {
            int j = (i+1) % p.size();
            int l = (k+1) % p.size();
            if (i == 1 || j == k) continue;
            if (SegmentsIntersect(p[i], p[j], p[k], p[l]))
                return false;}}
    return true;}
/*point in convex polygon
****bottom left point must be at index 0 and top is ←
the index of upper right vertex
****if not call make_hull once*/
bool pointinConvexPolygon(vector<pt> poly,pt point, ←
    int top) {
    if (point < poly[0] || point > poly[top]) return 0;←
    //0 for outside and 1 for on/inside

```



```

auto orientation = orient(point, poly[top], poly[0]);
if (orientation == 0) {
    if (point == poly[0] || point == poly[top]) ←
        return 1;
    return top == 1 || top + 1 == poly.size() ? 1 : ←
        1; // checks if point lies on boundary when
        // bottom and top points are adjacent
} else if (orientation < 0) {
    auto itRight = lower_bound(poly.begin() + 1, poly.←
        .begin() + top, point);
    return orient(itRight[0], point, itRight[-1]) <= 0;
} else {
    auto itLeft = upper_bound(poly.rbegin(), poly.←
        rend() - top - 1, point);
    return (orient(itLeft == poly.rbegin() ? poly[0] ←
        : itLeft[-1], point, itLeft[0])) <= 0;
}
}
/* maximum distance between two points in convexy ←
   polygon using rotating calipers
make sure that polygon is convex. if not call ←
make_hull first
*/
ld maxDist2(vector<pt> poly) {
    int n = poly.size();
    ld res = 0;
    for (int i = 0, j = n < 2 ? 0 : 1; i < j; ++i)
        for (; j = j + 1 % n) {
            res = max(res, dist2(poly[i], poly[j]));
            if (gt(cross(poly[j + 1 % n] - poly[j], poly[i + 1] ←
                - poly[i]), 0)) break;
        }
    return res;
}
// Line polygon intersection: check if given line ←
// intersects any side of polygon
// if yes then line intersects. If no, then check if ←
// its midpoint is inside polygon
// if midpoint is inside then line is inside else ←
// outside
// compute distance between point (x,y,z) and plane ←
// ax+by+cz=d
ld DistancePointPlane(ld x, ld y, ld z, ld a, ld b, ld c, ←
    ld d)
{ return fabs(a*x+b*y+c*z-d)/sqrt(a*a+b*b+c*c); }

```

4.2 Convex Hull

```

pt firstpoint;
// for sorting points in ccw (counter clockwise) ←
// direction w.r.t firstpoint (leftmost and ←
// bottommost)
bool compare(pt x, pt y) {

```

```

    ll o = orient(firstpoint, x, y);
    if (o == 0) return lt(x.x + x.y, y.x + y.y);
    return o < 0;
}
/* takes as input a vector of points containing input ←
   points and an empty vector for making hull
the points forming convex hull are pushed in vector ←
hull
returns hull containing minimum number of points in ←
ccw order
**** remove EPS for making integer hull
*/
void make_hull(vector<pt> &poi, vector<pt> &hull)
{
    pair<ld, ld> bl = {INF, INF};
    ll n = poi.size(); ll ind;
    for (ll i = 0; i < n; i++) {
        pair<ld, ld> pp = {poi[i].y, poi[i].x};
        if (pp < bl) {
            ind = i; bl = {poi[i].y, poi[i].x};
        }
    }
    swap(bl.F, bl.S); firstpoint = pt(bl.F, bl.S);
    vector<pt> cons;
    for (ll i = 0; i < n; i++) {
        if (i == ind) continue; cons.pb(poi[i]);
    }
    sort(cons.begin(), cons.end(), compare);
    hull.pb(firstpoint); ll m;
    for (auto z : cons) {
        if (hull.size() <= 1) { hull.pb(z); continue; }
        pt pr, ppr; bool fl = true;
        while ((m = hull.size()) >= 2) {
            pr = hull[m - 1]; ppr = hull[m - 2];
            ll ch = orient(ppr, pr, z);
            if (ch == -1) { break; }
            else if (ch == 1) { hull.pop_back(); continue; }
            else {
                ld d1, d2;
                d1 = dist2(ppr, pr); d2 = dist2(ppr, z);
                if (gt(d1, d2)) { fl = false; break; } else { hull.←
                    pop_back(); }
            }
        }
        if (fl) { hull.push_back(z); }
    }
    return;
}

```

4.3 Convex Hull Trick

```

/*
maintains upper convex hull of lines ax+b and gives ←
minimum value at a given x

```

```

to add line ax+b: sameoldcht.addline(a,b), to get min←
value at x: sameoldcht.getbest(x)
to get maximum value at x add -ax-b as lines instead ←
of ax+b and use -sameoldcht.getbest(x)
*/
const int N = 1e5 + 5;
int n;
int a[N];
int b[N];
long long dp[N];
struct line{
    long long a , b;
    double xleft;
    bool type;
    line(long long _a , long long _b){
        a = _a;
        b = _b;
        type = 0;
    }
    bool operator < (const line &other) const{
        if(other.type){
            return xleft < other.xleft;
        }
        return a > other.a;
    }
};
double meet(line x , line y){
    return 1.0 * (y.b - x.b) / (x.a - y.a);
}
struct cht{
    set < line > hull;
    cht(){
        hull.clear();
    }
    typedef set < line > :: iterator ite;
    bool hasleft(ite node){
        return node != hull.begin();
    }
    bool hasright(ite node){
        return node != prev(hull.end());
    }
    void updateborder(ite node){
        if(hasright(node)){
            line temp = *next(node);
            hull.erase(temp);
            temp.xleft = meet(*node , temp);
            hull.insert(temp);
        }
        if(hasleft(node)){
            line temp = *node;
            temp.xleft = meet(*prev(node) , temp);
            hull.erase(node);
            hull.insert(temp);
        }
        else{
            line temp = *node;
            hull.erase(node);
            temp.xleft = -1e18;

```

```

            hull.insert(temp);
        }
    }
    bool useless(line left , line middle , line right←
    ){
        double x = meet(left , right);
        double y = x * middle.a + middle.b;
        double ly = left.a * x + left.b;
        return y > ly;
    }
    bool useless(ite node){
        if(hasleft(node) && hasright(node)){
            return useless(*prev(node) , *node , *←
            next(node));
        }
        return 0;
    }
    void addline(long long a , long long b){
        line temp = line(a , b);
        auto it = hull.lower_bound(temp);
        if(it != hull.end() && it -> a == a){
            if(it -> b > b){
                hull.erase(it);
            }
            else{
                return;
            }
        }
        hull.insert(temp);
        it = hull.find(temp);
        if(useless(it)){
            hull.erase(it);
            return;
        }
        while(hasleft(it) && useless(prev(it))){
            hull.erase(prev(it));
        }
        while(hasright(it) && useless(next(it))){
            hull.erase(next(it));
        }
        updateborder(it);
    }
    long long getbest(long long x){
        if(hull.empty()){
            return 1e18;
        }
        line query(0 , 0);
        query.xleft = x;
        query.type = 1;
        auto it = hull.lower_bound(query);
        it = prev(it);
        return it -> a * x + it -> b;
    }
};
cht sameoldcht;
int main()
{
    scanf("%d" , &n);

```

```

for(int i = 1 ; i <= n ; ++i){
    scanf("%d" , a + i);
}
for(int i = 1 ; i <= n ; ++i){
    scanf("%d" , b + i);
}
sameoldcht.addline(b[1] , 0);
for(int i = 2 ; i <= n ; ++i){
    dp[i] = sameoldcht.getbest(a[i]);
    sameoldcht.addline(b[i] , dp[i]);
}
printf("%lld\n" , dp[n]);
}

```

5 Trees

5.1 BlockCut Tree

```

// code credits - http://codeforces.com/contest/487/←
// submission/15921824
// Take care it is 0 indexed --
struct BiconnectedComponents {
    struct Edge {
        int from, to;
    };
    struct To {
        int to; int edge;
    };
    vector<Edge> edges;
    vector<vector<To> > g;
    vector<int> low, ord, depth;
    vector<bool> isArtic;
    vector<int> edgeColor;
    vector<int> edgeStack;
    int colors;
    int dfsCounter;
    void init(int n) {
        edges.clear();
        g.assign(n, vector<To>());
    }
    void addEdge(int u, int v) {
        if(u > v) swap(u, v);
        Edge e = { u, v };
        int ei = edges.size();
        edges.push_back(e);
        To tu = { v, ei }, tv = { u, ei };
        g[u].push_back(tu);
        g[v].push_back(tv);
    }
    void run() {
        int n = g.size(), m = edges.size();
        low.assign(n, -2);
        ord.assign(n, -1);

```

```

        depth.assign(n, -2);
        isArtic.assign(n, false);
        edgeColor.assign(m, -1);
        edgeStack.clear();
        colors = 0;
        for(int i = 0; i < n; ++ i) if(ord[i] == -1) ←
        {
            dfsCounter = 0;
            dfs(i);
        }
    private:
    void dfs(int i) {
        low[i] = ord[i] = dfsCounter ++;
        for(int j = 0; j < (int)g[i].size(); ++ j) {
            int to = g[i][j].to, ei = g[i][j].edge;
            if(ord[to] == -1) {
                depth[to] = depth[i] + 1;
                edgeStack.push_back(ei);
                dfs(to);
                low[i] = min(low[i], low[to]);
                if(low[to] >= ord[i]) {
                    if(ord[i] != 0 || j >= 1)
                        isArtic[i] = true;
                    while(!edgeStack.empty()) {
                        int fi = edgeStack.back(); ←
                        edgeStack.pop_back();
                        edgeColor[fi] = colors;
                        if(fi == ei) break;
                    }
                    ++ colors;
                }
            }
            else if(depth[to] < depth[i] - 1) {
                low[i] = min(low[i], ord[to]);
                edgeStack.push_back(ei);
            }
        }
    }
};

```

5.2 Bridges Online

```

vector<int> par, dsu_2ecc, dsu_cc, dsu_cc_size;
int bridges;
int lca_iteration;
vector<int> last_visit;
void init(int n){
    par.resize(n);
    dsu_2ecc.resize(n);
    dsu_cc.resize(n);
    dsu_cc_size.resize(n);
    lca_iteration = 0;
    last_visit.assign(n, 0);
    for (int i=0; i<n; ++i) {
        dsu_2ecc[i] = i;

```

```

        dsu_cc[i] = i;
        dsu_cc_size[i] = 1;
        par[i] = -1;
    }
    bridges = 0;
}

int find_2ecc(int v) { // 2-edge connected comp.
    if (v == -1)
        return -1;
    return dsu_2ecc[v] == v ? v : dsu_2ecc[v] = ←
        find_2ecc(dsu_2ecc[v]);
}

int find_cc(int v) { // connected comp.
    v = find_2ecc(v);
    return dsu_cc[v] == v ? v : dsu_cc[v] = find_cc(←
        dsu_cc[v]);
}

void make_root(int v) {
    v = find_2ecc(v);
    int root = v;
    int child = -1;
    while (v != -1) {
        int p = find_2ecc(par[v]);
        par[v] = child;
        dsu_cc[v] = root;
        child = v;
        v = p;
    }
    dsu_cc_size[root] = dsu_cc_size[child];
}

void merge_path (int a, int b) {
    ++lca_iteration;
    vector<int> path_a, path_b;
    int lca = -1;
    while (lca == -1) {
        if (a != -1) {
            a = find_2ecc(a);
            path_a.push_back(a);
            if (last_visit[a] == lca_iteration)
                lca = a;
            last_visit[a] = lca_iteration;
            a = par[a];
        }
        if (b != -1) {
            path_b.push_back(b);
            b = find_2ecc(b);
            if (last_visit[b] == lca_iteration)
                lca = b;
            last_visit[b] = lca_iteration;
            b = par[b];
        }
    }
    for (int v : path_a) {
        dsu_2ecc[v] = lca;
        if (v == lca)
            break;
        --bridges;
    }
    for (int v : path_b) {

```

```

        dsu_2ecc[v] = lca;
        if (v == lca)
            break;
        --bridges;
    }
}

void add_edge(int a, int b) {
    a = find_2ecc(a);
    b = find_2ecc(b);
    if (a == b)
        return;
    int ca = find_cc(a);
    int cb = find_cc(b);
    if (ca != cb) {
        ++bridges;
        if (dsu_cc_size[ca] > dsu_cc_size[cb]) {
            swap(a, b);
            swap(ca, cb);
        }
        make_root(a);
        par[a] = dsu_cc[a] = b;
        dsu_cc_size[cb] += dsu_cc_size[a];
    } else {
        merge_path(a, b);
    }
}

```

5.3 HLD

```

/*
v is adjacency matrix of tree. clear v[i],hdc[i]=0,i←
=-1 before every run
clear ord and curc=0
*/
const ll MAX=250005;
vll v[MAX],ord;
ll par[MAX],noc[MAX],hdc[MAX],curc,posinch[MAX],len[←
MAX],ti=-1;
ll sta[MAX],en[MAX],subs[MAX],level[MAX];
ll st[4*MAX],lazy[4*MAX];
ll n;
void dfs(ll x){
    subs[x]=1;
    for(auto z:v[x]){
        if(z!=par[x]){par[z]=x;level[z]=level[x]+1;
            dfs(z);subs[x]+=subs[z];
        }
    }
}
void makehld(ll x){
    if(hdc[curc]==0){hdc[curc]=x;len[curc]=0;}
    noc[x]=curc;posinch[x]=++len[curc];
    ll a,b,c;a=b=0;ord.pb(x);sta[x]=++ti;
    for(auto z:v[x]){
        if(z==par[x]) continue;
        if(subs[z]>b){b=subs[z];a=z;}
    }
    if(a!=0)makehld(a);

```

```

    for(auto z:v[x]){if(z==par[x]||z==a) continue; curc←
        ++;makehld(z);}
    en[x]=ti;
}
inline void upd(ll x,ll y)//to update on path from a ←
    to b
{
    ll a,b,c,d;
    while(x!=y){
        a=hdc[noc[x]],b=hdc[noc[y]];
        if(a==b){
            if(level[x]>level[y])swap(x,y);c=sta[x],d=sta[y]←
                ];
            //lca=a;
            update(1,0,n-1,c+1,d);return;}
        if(level[a]>level[b])swap(a,b),swap(x,y);
        update(1,0,n-1,sta[b],sta[y]);y=par[b];}}//update←
        on segment tree
int main() {
    //v is adjacency matrix
    for(i=1;i<=n;i++) v[i].clear(),hdc[i]=0,ti=-1;
    ord.clear(),curc=0;
    level[1]=0;par[1]=0;curc=1;dfs(1);makehld(1);
    cin>>m;
    while(m--){cin>>a>>b;upd(a,b);ll ans=sumq(1,0,n←
        -1,0,n-1);}
}

```

5.4 LCA

```

const int N = int(1e5)+10;
const int LOGN = 20;
set<int> g[N];
int level[N];
int DP[LOGN][N];
int n,m;
/*----- Pre-Processing -----*/
/* Code Cridits : Tanuj Khattar codeforces submission←
    */
void dfs0(int u)
{
    for(auto it=g[u].begin();it!=g[u].end();it++)
        if(*it!=DP[0][u])
            DP[0][*it]=u;
            level[*it]=level[u]+1;
            dfs0(*it);
}
void preprocess()
{
    level[0]=0;
    DP[0][0]=0;
    dfs0(0);
    for(int i=1;i<LOGN;i++)
        for(int j=0;j<n;j++)

```

```

        DP[i][j] = DP[i-1][DP[i-1][j]];
    }
    int lca(int a,int b)
    {
        if(level[a]>level[b])swap(a,b);
        int d = level[b]-level[a];
        for(int i=0;i<LOGN;i++)
            if(d&(1<<i))
                b=DP[i][b];
        if(a==b)return a;
        for(int i=LOGN-1;i>=0;i--)
            if(DP[i][a]!=DP[i][b])
                a=DP[i][a],b=DP[i][b];
        return DP[0][a];
    }
    int dist(int u,int v)
    {
        return level[u] + level[v] - 2*level[lca(u,v)];
    }
}

```

5.5 Centroid Decomposition

```

/*
nx:maximum number of nodes
adj:adjacency list of tree,adj1: adjacency list of ←
    centroid tree
par:parents of nodes in centroid tree,timstamp: ←
    timestamps of nodes when they became centroids (←
    helpful in comparing which of the two nodes became←
    centroid first)
ssize,vis:utility arrays for storing subtree size and←
    visit times in dfs
tim: utility for doing dfs (for deciding which nodes ←
    to visit)
cntnrorder: centroids stored in order in which they ←
    were formed
dist[nx]: vector of vectors with dist[i][0][j]=number←
    of nodes at distance of k in subtree of i in ←
    centroid tree and dist[i][j][k]=number of nodes at←
    distance k in jth child of i in centroid tree ←
    *(use adj while doing dfs instead of adj1)*
dfs: find subtree sizes visiting nodes starting from ←
    root without visiting already formed centroids
dfs1: root- starting node, n- subtree size remaining ←
    after removing centroids -> returns centroid in ←
    subtree of root
preprocess: stores all values in dist array
*/
const int nx=1e5;
vector<int> adj[nx],adj1[nx]; //adj is adjacency list←
    of tree and adj1 is adjacency list for centroid ←
    tree
int par[nx],timstamp[nx],ssize[nx],vis[nx]; //par is ←
    parent of each node in centroid tree,ssize is ←
    subtree size of each node in centroid tree,vis and←
    timstamp are auxillary arrays for visit times in ←

```

```

    dfs- timstamp contains nonzero values only for ←
    centroids
int tim=1;
vector<int> cntnorder;//contains list of centroids ←
    generated (in order)
vector<vector<int> > dist[nx];
int dfs(int root)
{
    vis[root]=tim;
    int t=0;
    for(auto i:adj[root])
    {
        if(!timstamp[i]&&vis[i]<tim)
            t+=dfs(i);
    }
    ssize[root]=t+1;return t+1;
}
int dfs1(int root,int n)
{
    vis[root]=tim;pair<int,int> mxc={0,-1};bool poss=←
    true;
    for(auto i:adj[root])
    {
        if(!timstamp[i]&&vis[i]<tim)
            poss&=(ssize[i]<=n/2),mx=max(mxc,{ssize[i],i})←
            ;
    }
    if(poss&&(n-ssize[root])<=n/2)return root;
    return dfs1(mxc.second,n);
}
int findc(int root)
{
    dfs(root);
    int n=ssize[root];tim++;
    return dfs1(root,n);
}
void cntnrecom(int root,int p)
{
    int cntr=findc(root);
    cntnorder.push_back(cntr);
    timstamp[cntr]=tim++;
    par[cntr]=p;
    if(p>=0)adj1[p].push_back(cntr);
    for(auto i:adj[cntr])
        if(!timstamp[i])
            cntnrecom(i,cntr);
}
void dfs2(int root,int nod,int j,int dst)
{
    if(dist[root][j].size()==dst)dist[root][j].←
    push_back(0);
    vis[nod]=tim;
    dist[root][j][dst]+=1;
    for(auto i:adj[nod])
    {
        if((timstamp[i]<=timstamp[root])||(vis[i]==vis[nod]←
        ))continue;
        vis[i]=tim;dfs2(root,i,j,dst+1);
    }
}

```

```

    }
}
void preprocess()
{
    for(int i=0;i<cntnorder.size();i++)
    {
        int root=cntnorder[i];
        vector<int> temp;
        dist[root].push_back(temp);
        temp.push_back(0);
        ++tim;
        dfs2(root,root,0,0);
        int cnt=0;
        for(int j=0;j<adj[root].size();j++)
        {
            int nod=adj[root][j];
            if(timstamp[nod]<timstamp[root])
                continue;
            dist[root].push_back(temp);
            ++tim;
            dfs2(root,nod,++cnt,1);
        }
    }
}

```

6 Maths

6.1 Chinese Remainder Theorem

```

/*solves system of equations x=rem[i]%mods[i] for any←
    mod (need not be coprime)
input:vector of remainders and moduli
output: pair of answer(x%lcm of modulo) and lcm of ←
    all the modulo (returns -1 if it is inconsistent)←
    */
ll GCD(ll a, ll b) { return (b == 0) ? a : GCD(b, a %←
    b); }
inline ll LCM(ll a, ll b) { return a / GCD(a, b) * b;←
    }
inline ll normalize(ll x, ll mod) { x %= mod; if (x <←
    0) x += mod; return x; }
struct GCD_type { ll x, y, d; };
GCD_type ex_GCD(ll a, ll b)
{
    if (b == 0) return {1, 0, a};
    GCD_type pom = ex_GCD(b, a % b);
    return {pom.y, pom.x - a / b * pom.y, pom.d};
}
pair<ll,ll> CRT(vector<ll> &rem,vector<ll> &mods)
{
    ll n=rem.size();
    ll ans=rem[0];
    ll lcm=mods[0];

```



```

for(ll i=1;i<n;i++)
{
    auto pom=ex_GCD(lcm,mods[i]);
    ll x1=pom.x;
    ll d=pom.d;
    if((rem[i]-ans)%d!=0) return {-1,0};
    ans=normalize(ans+x1*(rem[i]-ans)/d%(mods[i]/d)*lcm,lcm*mods[i]/d);
    lcm=LCM(lcm,mods[i]); // you can save time by replacing above lcm * n[i] /d by lcm = lcm * n[i] / d
}
return {ans,lcm};
}

```

6.2 Discrete Log

```

// Discrete Log , Baby-Step Giant-Step , e-maxx
// The idea is to make two functions,
// f1(p) , f2(q) and find p,q s.t.
// f1(p) = f2(q) by storing all possible values of f1
// and checking for q. In this case  $a^x = b \pmod m$ 
// is solved by substituting x by p.n-q , where
// n is choosen optimally , usually sqrt(m).
// returns a soln. for  $a^x = b \pmod m$ 
// for given a,b,m . -1 if no. soln.
// complexity :  $O(\sqrt{m} \cdot \log(m))$ 
// use unordered_map to remove log factor.
// IMP : works only if a,m are co-prime. But can be modified.
int solve(int a, int b, int m) {
    int n = (int) sqrt(m + .0) + 1;
    int an = 1;
    for (int i=0; i<n; ++i)
        an = (an * a) % m;
    map<int,int> vals;
    for (int i=1, cur=an; i<=n; ++i) {
        if (!vals.count(cur))
            vals[cur] = i;
        cur = (cur * an) % m;
    }
    for (int i=0, cur=b; i<=n; ++i) {
        if (vals.count(cur)) {
            int ans = vals[cur] * n - i;
            if (ans < m) return ans;
        }
        cur = (cur * a) % m;
    }
    return -1;
}

```

6.3 NTT

```

/*
Kevin's different Code: https://s3.amazonaws.com/codechef_shared/download/Solutions/JUNE15/tester/MOREFB.cpp
****There is no problem that FFT can solve while this NTT cannot
Case1: If the answer would be small choose a small enough NTT prime modulus
Case2: If the answer is large(> ~1e9) FFT would not work anyway due to precision issues
In Case2 use NTT. If max_answer_size=n*(largest_coefficient^2)
So use two or three modulus to solve it
****Compute a*b%mod if a%mod*b%mod would result in overflow in  $O(\log(a))$  time:
ll mulmod(ll a, ll b, ll mod) {
    ll res = 0;
    while (a != 0) {
        if (a & 1) res = (res + b) % m;
        a >>= 1;
        b = (b << 1) % m;
    }
    return res;
}

Fastest NTT (can also do polynomial multiplication if max coefficients are upto  $1e18$  using 2 modulus and CRT)
How to use:
P=A*B
Polynomial1 = A[0]+A[1]*x^1+A[2]*x^2+...+A[n-1]*x^n-1
Polynomial2 = B[0]+B[1]*x^1+B[2]*x^2+...+B[n-1]*x^n-1
P=multiply(A,B)
A and B are not passed by reference because they are changed in multiply function
For CRT after obtaining answer modulo two primes p1 and p2:
x = a1 mod p1, x = a2 mod p2 => x=((a1*(m2^-1)%m1)*m2+(a2*(m1^-1)%m2)*m1)%m1m2
*** Before each call to multiply:
set base=1,roots={0,1},rev={0,1},max_base=x (such that if mod=c*(2^k)+1 then x<=k and 2^x is greater than equal to nearest power of 2 of 2*n)
root=primitive_root^((mod-1)/(2^max_base))
For P=A*A use square function
Some useful modulo and examples
mod1=463470593 = 1768*2^18+1 primitive root = 3 => max_base=18,root=3^1768
mod2=469762049 = 1792*2^18+1 primitive root = 3 => max_base=18,root=3^1792
(mod1^-1)%mod2=313174774 (mod2^-1)%mod1=154490124
Some prime modulus and primitive root
635437057 11 6
833886331 13 6
645500198 17 3
648800198 17 3
666688943 37 3
680087415 37 3
700083415 37 3
715128833 37 3
740294657 37 3

```



```

v1.pb(f+a,f+b+1);v2.pb(g+c,g+d+1); vector<int> res=↵
    multiply(v1,v2);
for(int i=0;i<res.size();i++)
    if(a+c+i+1<nx) f[a+c+i+1]=add(f[a+c+i+1],res[i]);
}
void precal()
{
    g[0]=1;
    for(int i=1;i<nx;i++)
        g[i]=power(i,i-1);
    f[1]=1;
    for(int i=1;i<=100000;i++)
    {
        f[i+1]=add(f[i+1],g[i]);f[i+1]=add(f[i+1],f[i]);
        f[i+2]=add(f[i+2],mul(f[i],g[1]));f[i+3]=add(f[i↵
            +3],mul(f[i],g[2]));
        for(int j=2;i%j==0&&j<nx;j=j*2) onlinefft(i-j,i↵
            -1,j+1,2*j);
    }
}

```

6.5 Langrange Interpolation

```

/* Input :
Degree of polynomial: k
Polynomial values at x=0,1,2,3,...,k
Output :
Polynomial value at x
Complexity: O(degree of polynomial)
Works only if the points are equally spaced
*/
ll lagrange(vll& v , int k, ll x,int mod){
    if(x <= k)
        return v[x];
    ll inn = 1;
    ll den = 1;
    for(int i = 1;i<=k;i++)
    {
        inn = (inn*(x - i))%mod;
        den = (den*(mod - i))%mod;
    }
    inn = (inn*inv(den % mod))%mod;
    ll ret = 0;
    for(int i = 0;i<=k;i++){
        ret = (ret + v[i]*inn)%mod;
        ll md1 = mod - ((x-i)*(k-i))%mod;
        ll md2 = ((i+1)*(x-i-1))%mod;
        if(i!=k)
            inn = (((inn*md1)%mod)*inv(md2 % mod))%↵
                mod;
    }
    return ret;
}

```

6.6 Matrix Struct

```

struct matrix{
    ld B[N][N], n;
    matrix(){n = N; memset(B,0,sizeof B);}
    matrix(int _n){
        n = _n; memset(B, 0, sizeof B);
    }
    void iden(){
        for(int i = 0; i < n; i++)
            B[i][i] = 1;
    }
    void operator += (matrix M){
        for(int i = 0; i < n; i++)
            for(int j = 0; j < n; j++)
                B[i][j] = add(B[i][j], M.B[i][j]);
    }
    void operator -= (matrix M){}
    void operator *= (ld b){}
    matrix operator - (matrix M){}
    matrix operator + (matrix M){
        matrix ret = (*this);
        ret += M; return ret;
    }
    matrix operator * (matrix M){
        matrix ret = matrix(n); memset(ret.B, 0, ↵
            sizeof ret.B);
        for(int i = 0; i < n; i++)
            for(int j = 0; j < n;j++){
                for(int k = 0; k < n; k++){
                    ret.B[i][j] = add(ret.B[i][j], ↵
                        mul(B[i][k], M.B[k][j]));
                }
            }
        return ret;
    }
    matrix operator *= (matrix M){ *this = ((*this) *↵
        M);}
    matrix operator * (int b){
        matrix ret = (*this); ret *= b; return ret;
    }
    vector<double> multiply(const vector<double> & v)↵
        const{
        vector<double> ret(n);
        for(int i = 0; i < n; i++)
            for(int j = 0; j < n; j++){
                ret[i] += B[i][j] * v[j];
            }
        return ret;
    }
};

```

6.7 nCr(Non Prime Modulo)

```

// sandwich, jtnydv25 video
// calculates nCr, for small
// non-prime modulo, and (very) big n,r.
ll phimod;
vll pr,prn;vll fact;
ll power(ll a,ll x,ll mod){
    ll ans=1;
    while(x){
        if((1LL)&(x))ans=(ans*a)%mod;
        a=(a*a)%mod;x>>=1LL;
    }
    return ans;
}
// prime factorization of x.
// pr-> prime ; prn -> it's exponent
void getprime(ll x){
    pr.clear();prn.clear();
    ll i,j,k;
    for(i=2;(i*i)<=x;i++){
        k=0;while((x%i)==0){k++;x/=i;}
        if(k>0){pr.pb(i);prn.pb(k);}
    }
    if(x!=1){pr.pb(x);prn.pb(1);}
    return;
}
// factorials are calculated ignoring
// multiples of p.
void primeproc(ll p,ll pe){    // p , p^e
    ll i,d;
    fact.clear();fact.pb(1);d=1;
    for(i=1;i<pe;i++){
        if(i%p){fact.pb((fact[i-1]*i)%pe);}
        else {fact.pb(fact[i-1]);}
    }
    return;
}
// again note this has ignored multiples of p
ll Bigfact(ll n,ll mod){
    ll a,b,c,d,i,j,k;
    a=n/mod;a%=phimod;a=power(fact[mod-1],a,mod);
    b=n%mod;a=(a*fact[b])%mod;
    return a;
}
// Chinese Remainder Thm.
vll crtval,crtmod;
ll crt(vll &val,vll &mod){
    ll a,b,c,d,i,j,k;b=1;
    for(ll z:mod)b*=z;
    ll ans=0;
    for(i=0;i<mod.size();i++){
        a=mod[i];c=b/a;
        d=power(c,(((a/pr[i])*(pr[i]-1))-1),a);
        c=(c*d)%b;c=(c*val[i])%b;ans=(ans+c)%b;
    }
    return ans;
}
// calculate for prime powers and

```

```

// take crt. For each prime power,
// first ignore multiples of p,
// and then do recursively, calculating
// the powers of p separately.
ll Bigncr(ll n,ll r,ll mod){
    ll a,b,c,d,i,j,k;ll p,pe;
    getprime(mod);ll Fnum=1;ll Fden;
    crtval.clear();crtmod.clear();
    for(i=0;i<pr.size();i++){
        Fnum=1;Fden=1;
        p=pr[i];pe=power(p,prn[i],1e17);
        primeproc(p,pe);
        a=1;d=0;
        phimod=(pe*(p-1LL))/p;
        ll n1=n,r1=r,nr=n-r;
        while(n1){
            Fnum=(Fnum*(Bigfact(n1,pe)))%pe;
            Fden=(Fden*(Bigfact(r1,pe)))%pe;
            Fden=(Fden*(Bigfact(nr,pe)))%pe;
            d+=n1-(r1+nr);
            n1/=p;r1/=p;nr/=p;
        }
        Fnum=(Fnum*(power(Fden,(phimod-1LL),pe)))%pe;
        if(d>=prn[i])Fnum=0;
        else Fnum=(Fnum*(power(p,d,pe)))%pe;
        crtmod.pb(pe);crtval.pb(Fnum);
    }
    // you can just iterate instead of crt
    // for(i=0;i<mod;i++){
    //     bool cg=true;
    //     for(j=0;j<crtmod.size();j++){
    //         if(i%crtmod[j]!=crtval[j])cg=false;
    //     }
    //     if(cg)return i;
    // }
    return crt(crtval,crtmod);
}

```

6.8 Primitive Root Generator

```

/*To find generator of U(p),we check for all
g in [1,p]. But only for powers of the
form phi(p)/p_j, where p_j is a prime factor of
phi(p). Note that p is not prime here.
Existence , if one of these :
1. p = 1,2,4
2. p = q^k , where q -> odd prime.
3. p = 2.(q^k) , where q-> odd prime
Note that a.g^(phi(p)) = 1 (mod p)
        b.there are phi(phi(p)) generators if <-
        exists.
*/
// Finds "a" generator of U(p),

```

```

// multiplicative group of integers mod p.
// here calc_phi returns the totient function for p
// Complexity : O(Ans.log(phi(p)).log(p)) + time for ←
// factorizing phi(p).
// By some theorem, Ans = O((log(p))^6). Should be ←
// fast generally.
int generator (int p) {
    vector<int> fact;
    int phi = calc_phi(p), n = phi;
    for (int i=2; i*i<=n; ++i)
        if (n % i == 0) {
            fact.push_back (i);
            while (n % i == 0)
                n /= i;
        }
    if (n > 1)
        fact.push_back (n);
    for (int res=2; res<=p; ++res) {
        if(gcd(res,p)!=1) continue;
        bool ok = true;
        for (size_t i=0; i<fact.size() && ok; ++i)
            ok &= powmod (res, phi / fact[i], p) != ←
                1;
        if (ok) return res;
    }
    return -1;
}

```

7 Strings

7.1 Hashing Theory

If order not imp. and count/frequency imp. use this ←
as hash fn:-
 $(a_1+h)^k + (a_2+h)^k + (a_3+h)^k + (a_4+h)^k \pmod p$
. Select : h,k,p
Alternate:
 $((x)^{(a_1)}+(x)^{(a_2)}+...+(x)^{(a_k)})\%mod$ where x and ←
mod are fixed and $a_1...a_k$ is an unordered set

7.2 Manacher

```

// Same idea as Z_algo, Time : O(n)
// [l,r] represents : boundaries of rightmost ←
// detected subpalindrom(with max r)
// takes string s and returns a vector of lengths of ←
// odd length palindrom
// centered around that char(e.g abac for 'b' returns←
// 2(not 3))
vll manacher_odd(string s){
    ll n = s.length(); vll d1(n);

```

```

for(ll i = 0, l = 0, r = -1; i<n; i++){
    d1[i] = 1;
    if(i <= r){
        d1[i] = min(r-i+1, d1[l+r-i]); // use prev←
        val
    }
    while(i+d1[i] < n && i-d1[i] >= 0 && s[i+d1[i]←
        ] == s[i-d1[i]]) d1[i]++; // trivial ←
        matching
    if(r < i+d1[i]-1) l=i-d1[i]+1, r=i+d1[i]-1; ←
        // update r
    }
    return d1;
}
// takes string s and returns vector of lengths of ←
// even length ...
// (it's centered around the right middle char, bb is←
// centered around the later 'b')
vll manacher_even(string s){
    ll n = s.length(); vll d2(n);
    for(ll i = 0, l = 0, r = -1; i<n; i++){
        d2[i] = 0;
        if(i <= r){
            d2[i] = min(r-i+1, d2[l+r+1-i]);
        }
        while(i+d2[i] < n && i-d2[i]-1 >= 0 && s[i+d2[i]←
            [i]] == s[i-d2[i]-1]) d2[i]++;
        if(d2[i] > 0 && r < i+d2[i]-1) l=i-d2[i], r=i←
            +d2[i]-1;
        }
        return d2;
    }
}
// Other mtd : To do both things in one pass, add ←
// special char e.g string "abc" => "$a$b$c$"

```

7.3 Suffix Array

```

//code credits - https://cp-algorithms.com/string/←
//suffix-array.html
/*Theory :-
Sorted array of suffixes = sorted array of cyclic ←
shifts of string+$.
We consider a prefix of len.  $2^k$  of the cyclic, in ←
the kth iteration.
And find the sorted order, using values for (k-1)th ←
iteration and
kind of radix sort. Could be thought as some kind of ←
binary lifting.
String of len.  $2^k$  -> combination of 2 strings of len←
.  $2^{(k-1)}$ , whose
order we know. Just radix sort on pair for next ←
iteration.
Time :-  $O(n \log(n) + \text{alphabet})$ 
Applications :-
Finding the smallest cyclic shift; Finding a substring←
in a string;

```



```

Comparing two substrings of a string; Longest common ←
prefix of two substrings;
Number of different substrings.
*/
// return list of indices (permutation of indices ←
// which are in sorted order)
vector<ll> sort_cyclic_shifts(string const& s) {
    ll n = s.size();
    const ll alphabet = 256;
    //***** change the alphabet size accordingly ←
    // and indexing *****
    vector<ll> p(n), c(n), cnt(max(alphabet, n), ←
    0);
    // p -> sorted order of 1-len prefix of each ←
    // cyclic shift index.
    // c -> class of a index
    // pn -> same as p for kth iteration . ||ly cn.
    for (ll i = 0; i < n; i++)
        cnt[s[i]]++;
    for (ll i = 1; i < alphabet; i++)
        cnt[i] += cnt[i-1];
    for (ll i = 0; i < n; i++)
        p[--cnt[s[i]]] = i;
    c[p[0]] = 0;
    ll classes = 1;
    for (ll i = 1; i < n; i++) {
        if (s[p[i]] != s[p[i-1]])
            classes++;
        c[p[i]] = classes - 1;
    }
    vector<ll> pn(n), cn(n);
    for (ll h = 0; (1 << h) < n; ++h) {
        for (ll i = 0; i < n; i++) { // sorting w.r. ←
            // second part.
            pn[i] = p[i] - (1 << h);
            if (pn[i] < 0)
                pn[i] += n;
        }
        fill(cnt.begin(), cnt.begin() + classes, 0);
        for (ll i = 0; i < n; i++)
            cnt[c[pn[i]]]++;
        for (ll i = 1; i < classes; i++)
            cnt[i] += cnt[i-1];
        for (ll i = n-1; i >= 0; i--)
            p[--cnt[c[pn[i]]]] = pn[i]; // sorting ←
            // w.r.t first (more significant) part.
        cn[p[0]] = 0;
        classes = 1;
        for (ll i = 1; i < n; i++) { // determining ←
            // new classes in sorted array.
            pair<ll, ll> cur = {c[p[i]], c[(p[i] + (1 ←
            << h)) % n]};
            pair<ll, ll> prev = {c[p[i-1]], c[(p[i-1] ←
            + (1 << h)) % n]};
            if (cur != prev)
                ++classes;
        }
    }
}

```

```

        cn[p[i]] = classes - 1;
    }
    c.swap(cn);
}
return p;
}
vector<ll> suffix_array_construction(string s) {
    s += "$";
    vector<ll> sorted_shifts = sort_cyclic_shifts(s);
    sorted_shifts.erase(sorted_shifts.begin());
    return sorted_shifts;
}
// For comparing two substring of length l starting ←
// at i, j.
// k - 2^k > l/2. check the first 2^k part, if equal,
// check last 2^k part. c[k] is the c in kth iter of ←
// S.A construction.
int compare(int i, int j, int l, int k) {
    pair<int, int> a = {c[k][i], c[k][(i+1-(1 << k))% ←
    n]};
    pair<int, int> b = {c[k][j], c[k][(j+1-(1 << k))% ←
    n]};
    return a == b ? 0 : a < b ? -1 : 1;
}
/*
Kasai's Algo for LCP construction :
Longest Common Prefix for consecutive suffixes in ←
suffix array.
lcp[i] = length of lcp of ith and (i+1)th suffix in the ←
suffix array.
1. Consider suffixes in decreasing order of length.
2. Let p = s[i...n]. It will be somewhere in the S.A ←
. We determine its lcp = k.
3. Then lcp of q = s[(i+1)...n] will be at least k-1. ←
Why?
4. Remove the first char of p and its successor in ←
the S.A. These are suffixes with lcp k-1.
5. But note that these 2 may not be consecutive in S. ←
A. But however lcp of strings in
b/w have to be at least k-1.
*/
vector<ll> lcp_construction(string const& s, vector<ll> ←
const& p) {
    ll n = s.size();
    vector<ll> rank(n, 0);
    for (ll i = 0; i < n; i++)
        rank[p[i]] = i;
    ll k = 0;
    vector<ll> lcp(n-1, 0);
    for (ll i = 0; i < n; i++) {
        if (rank[i] == n - 1) {
            k = 0;
            continue;
        }
        ll j = p[rank[i] + 1];
        while (i + k < n && j + k < n && s[i+k] == s[ ←
        j+k])
            k++;
    }
}

```



```

        k++;
lcp[rank[i]] = k;
        if (k)
            k--;
    }
    return lcp;
}

```

7.4 Trie

```

const ll AS = 26; // alphabet size
ll go[MAX][AS];
ll cnt[MAX]; ll cn=0;
// cn -> index of next new node
// convert all strings to vll
ll newNode() {
    for(ll i=0; i<AS; i++)
        go[cn][i]=-1;
    return cn++;
}
// call newNode once *****
// before adding anything **
void addTrie(vll &x) {
    ll v = 0;
    cnt[v]++;
    for(ll i=0; i<x.size(); i++){
        ll y=x[i];
        if(go[v][y]==-1)
            go[v][y]=newNode();
        v=go[v][y];
        cnt[v]++;
    }
}
// returns count of substrings with prefix x
ll getcount(vll &x){
    ll v=0;
    for(i=0; i<x.size(); i++){
        ll y=x[i];
        if(go[v][y]==-1)
            go[v][y]=newNode();
        v=go[v][y];
    }
    return cnt[v];
}

```

7.5 Z-algorithm

```

// [l,r] -> indices of the rightmost segment match
// (the detected segment that ends rightmost (with max ←
// r))
// 2 cases -> 1st. i ≤ r : z[i] is atleast min(r-i ←
// +1, z[i-1]), then match trivially
// 2nd. o.w compute z[i] with trivial matching

```

```

// update l,r
// Time : O(n)(asy. behavior), Proof : each iteration ←
// of inner while loop make r pointer advance to ←
// right,
// Applications: 1) Search substring(text t, ←
// pattern p) s = p + '$' + t.
// 3) String compression(s = t+t+...+t, then find |t ←
// |)
// 2) Number of distinct substrings (in O(n^2))
// (useful when appending or deleting characters ←
// online from the end or beginning)
vector<ll> z_function(string s) {
    ll n = (ll) s.length();
    vector<ll> z(n);
    for (ll i = 1, l = 0, r = 0; i < n; ++i) {
        if (i ≤ r)
            z[i] = min(r - i + 1, z[i - 1]); // use ←
            previous z val
        while (i + z[i] < n && s[z[i]] == s[i + z[i] ←
            ]) // trivial matching
            ++z[i];
        if (i + z[i] - 1 > r)
            l = i, r = i + z[i] - 1; // update ←
            rightmost segment matched
    }
    return z;
}

```

7.6 Aho Corasick

```

const int K = 26;
// remember to set K
struct Vertex {
    int next[K]; bool leaf = false;
    int p = -1; char pch;
    int link = -1;
    int go[K];
    Vertex(int p=-1, char ch='$') : p(p), pch(ch) {
        fill(begin(next), end(next), -1);
        fill(begin(go), end(go), -1);
    }
};
vector<Vertex> aho(1);
void add_string(string const& s) {
    int v = 0;
    for (char ch : s) {
        int c = ch - 'a';
        if (aho[v].next[c] == -1) {
            aho[v].next[c] = aho.size();
            aho.emplace_back(v, ch);
        }
        v = aho[v].next[c];
    }
    aho[v].leaf = true;
}

```

```

}
int go(int v, char ch);
int get_link(int v) {
    if (aho[v].link == -1) {
        if (v == 0 || aho[v].p == 0)
            aho[v].link = 0;
        else
            aho[v].link = go(get_link(aho[v].p), aho[
                v].pch);
    }
    return aho[v].link;
}
int go(int v, char ch) {
    int c = ch - 'a';
    if (aho[v].go[c] == -1) {
        if (aho[v].next[c] != -1)
            aho[v].go[c] = aho[v].next[c];
        else
            aho[v].go[c] = v == 0 ? 0 : go(get_link(v), ch);
    }
    return aho[v].go[c];
}
}

```

7.7 KMP

```

/*Time:O(n)(j increases n times(& j>=0) only so asy. ←
0(n))
pi[i] = length of longest prefix of s ending at i
applications: search substring, # of different ←
substrings(O(n^2)),
3) String compression(s = t+t+...+t, then find |t|, k←
=n-pi[n-1],if k|n)
4) Building Automaton(Gray Code Example)*/
vector<ll> prefix_function(string s) {
    ll n = (ll)s.length();
    vector<ll> pi(n);
    for (ll i = 1; i < n; i++) {
        ll j = pi[i-1];
        while (j > 0 && s[i] != s[j])
            j = pi[j-1];
        if (s[i] == s[j]) j++;
        pi[i] = j;
    }
    return pi;
}
// searching s in t, returns all occurrences(indices)
vector<ll> search(string s, string t){
    vll pi = prefix_function(s);
    ll m = s.length(); vll ans; ll j = 0;
    for(ll i=0; i<t.length(); i++){
        while(j > 0 && t[i] != s[j])
            j = pi[j-1];
        if(t[i] == s[j]) j++;
    }
}

```

```

        if(j == m) ans.pb(i-m+1);
    }
    return ans; // if ans empty then no occurrence
}

```

7.8 Palindrome Tree

```

const ll MAX=1e5+15;
ll par[MAX]; // stores index of parent node
ll sul1[MAX]; // stores index of suffix link
ll len[MAX]; // stores length of largest pallindrome←
ending at that node
ll child[MAX][30]; // stores the children of the ←
node
/*←
-----
index 0 - root "-1"
index 1 - root "0"
therefore node of s[i] is i+2
initialize all child[i][j] to -1
-----
*/
void eer_tree(string s){
    ll a,b,c,d,i,j,k,e,f;
    sul1[1]=0;sul1[0]=0;len[1]=0;len[0]=-1;
    ll n=s.length();
    for(i=0;i<n+10;i++)
        for(j=0;j<30;j++) child[i][j]=-1;
    ll cur=1;d=1;
    for(i=0;i<s.size();i++){
        ++d;
        while(true){
            a=i-1-len[cur];
            if(a>=0){
                if(s[a]==s[i]){
                    if(child[cur][(ll)(s[i]-'a')]==-1){
                        par[d]=cur;child[cur][(ll)(s[i]-'a')]=d;
                        len[d]=len[cur]+2;cur=d;
                    }
                    else{
                        par[d]=cur;len[d]=len[cur]+2;
                        cur=child[cur][(ll)(s[i]-'a')];
                    }
                    break;
                }
            }
        }
        if(cur==0) break;
        cur=sul1[cur];
    }
    if(cur!=d) continue;
    if(len[d]==1) sul1[d]=1;
    else{
        c=sul1[par[d]];
        while(child[c][(ll)(s[i]-'a')]==-1){
            if(c==0) break;
            c=sul1[c];
        }
    }
}

```


1. Consider suffixes in decreasing order of length.
2. Let $p = s[i \dots n]$. It will be somewhere in the S.A. \leftarrow We determine its $\text{lcp} = k$.
3. Then lcp of $q = s[(i+1) \dots n]$ will be at least $k-1$. \leftarrow Why?
4. Remove the first char of p and its successor in \leftarrow the S.A. These are suffixes with $\text{lcp} k-1$.
5. But note that these 2 may not be consecutive in S. \leftarrow A. But however lcp of strings in \leftarrow b/w have to be also at least $k-1$.

```

*/
vector<ll> lcp_construction(string const& s, vector<ll>
ll> const& p) {
    ll n = s.size();
    vector<ll> rank(n, 0);
    for (ll i = 0; i < n; i++)
        rank[p[i]] = i;
    ll k = 0;
    vector<ll> lcp(n-1, 0);
    for (ll i = 0; i < n; i++) {
        if (rank[i] == n - 1) {
            k = 0;
            continue;
        }
        ll j = p[rank[i] + 1];
        while (i + k < n && j + k < n && s[i+k] == s[j+k])
            k++;
        lcp[rank[i]] = k;
        if (k)
            k--;
    }
    return lcp;
}

```

```

}
if (tp == -1 || c == str[tp] - 'a') tp++;
else {
    lef[ts] = lef[tv]; rig[ts] = tp - 1; par[ts] = par[tv];
    chi[ts][str[tp] - 'a'] = tv; chi[ts][c] = ts + 1;
    lef[ts + 1] = la; par[ts + 1] = ts; lef[tv] = tp; par[tv] = ts;
    chi[par[ts]][str[lef[ts]] - 'a'] = ts; ts += 2;
    tv = sfli[par[ts - 2]]; tp = lef[ts - 2];
    while (tp <= rig[ts - 2]) {
        tv = chi[tv][str[tp] - 'a']; tp += rig[tv] - lef[tv] + 1;
        if (tp == rig[ts - 2] + 1) sfli[ts - 2] = tv; else sfli[ts - 2] = ts;
        tp = rig[tv] - (tp - rig[ts - 2]) + 2; goto suff;
    }
}
void build() {
    ts = 2; tv = 0; tp = 0;
    ll ss = str.size(); ss *= 2; ss += 15;
    fill(rig, rig + ss, (int)str.size() - 1);
    // initialize data for the root of the tree
    sfli[0] = 1; lef[0] = -1; rig[0] = -1;
    lef[1] = -1; rig[1] = -1; for (ll i = 0; i < ss; i++)
        fill(chi[i], chi[i] + 27, -1);
    fill(chi[1], chi[1] + 26, 0);
    // add the text to the tree, letter by letter
    for (la = 0; la < (int)str.size(); ++la)
        ukkadd(str[la] - 'a');
}

```

7.10 Suffix Tree

```

const int N = 1000000, // set it more than 2*(len. of string)
string str; // input string for which the suffix tree is being built
int chi[N][26],
lef[N], // left...
rig[N], // ...and right boundaries of the substring of a which correspond to incoming edge
par[N], // parent of the node
sfli[N], // suffix link
tv, tp, la,
ts; // the number of nodes
void ukkadd(int c) {
    suff:;
    if (rig[tv] < tp) {
        if (chi[tv][c] == -1) { chi[tv][c] = ts; lef[ts] = la;
            par[ts++] = tv; tv = sfli[tv]; tp = rig[tv] + 1; goto suff; }
        tv = chi[tv][c]; tp = lef[tv];
    }
}

```