Total No. of Questions: 09]

[Total No. of Pages: 02

Paper ID [CS203]

(Please fill this Paper ID in OMR Sheet)

DE1-07

B.Tech. (Sem. - 3rd/4th) www.allnehectily ou.com.
MATHEMATICS - III (CS - 203)

Time: 03 Hours

Maximum Marks: 60

Instruction to Candidates:

- 1) Section A is Compulsory.
- 2) Attempt any Four questions from Section B.
- 3) Attempt any Two questions from Section C.

Section - A

Q1)

 $(10 \times 2 = 20)$

- a) State Taylor's Expansion.
- b) State and prove second shifting property of Laplace transforms.
- c) Find the inverse Laplace transform of $2s/4s^2 + 16$.
- d) State Cauchy's integral theorem.
- e) Show that function $|z|^2$ is not analytic at any point.
- f) Write down one dimensional, two dimensional heat flow equations.
- g) Show that if |z+1| < 1, $z^{-2} = 1 + \sum_{n=1}^{\infty} (n+1)(z+1)^n$.
- h) Find the length of the curve $y = \frac{4}{3} x^{3/2}$ for $0 \le x \le 20$.
- i) State and prove sufficient condition for a function to be analytic.
- j) Determine a,b,c,d so that function $f(z) = (x^2 + axy + by^2) + i(cx^2 + dxy + y^2)$ is analytic.

P.T.O.

R-60

Section - B

$$(4 \times 5 = 20)$$

- **Q2)** Expand $f(z) = \frac{1}{z^2(z-i)}$ as a Laurent's series about i and hence find the residue. There at.
- Q3) Evaluate $\oint_C \frac{z-23}{z^2-4z-5} dz$, where C is the circle |z-2|=4
- **Q4)** Find the image of circle |z-1| = 1 in the w-plane under the mapping $w = z^2$.
- **Q5**) Determine the analytic function whose real part is $e^x (\cos y y \sin y)$.
- **Q6**) Verify the Roll's theorem to the function $f(x) = e^{-x} \sin x$, $x \in [0, \pi]$.

Section - C

$$(2 \times 10 = 20)$$

- **Q7)** Evaluate $\int_{-\infty}^{\infty} \frac{\cos x}{x^2 + a^2} dx.$
- **Q8)** solve $\nabla^2 u = 0$, under the condition (h = k = 1), u(0,y) = 0, u(4,y) = 12 + y, for $0 \le y \le 4$; u(x,0) = 3x, $u(x,4) = x^2$ for $0 \le x \le 4$.
- **Q9)** A string of length ' ℓ ' is initially at rest in equilibrium position and each of its points is given the velocity $\left(\frac{\partial y}{\partial t}\right)_{t=0} = b \sin^3 \frac{\pi x}{\ell}$. Find the displacement y(x,t).

