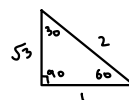


→ Compound Interest → Amount =  $P \left(1 + \frac{R}{100}\right)^t$

→ 5% annually compounded quarterly, now  $R = R/4$   
 $t = t \times 4$

→ 30, 60, 90 Triangle

1:√3:2



→ Multiples, difference between 2 multiples is also a multiple.

Eg → If  $K, K+200, K+350$  are multiples of  $P$ , what is  $P$

$P \rightarrow K \rightarrow K+200 \rightarrow K+350$



These both should be multiples of  $P$

→ Trapezoid area =  $\frac{b_1 + b_2}{2} \cdot h$

→ Prime number trick, to test if any no. less than 100 is a prime, check if it is divisible by any prime numbers less than 10

→ Factors of large numbers trick

- ① Prime factorization
- ② List all exponents of prime factors
- ③ add 1 to each
- ④ Multiply them

Eg →  $8400 \rightarrow 2^4 \times 3^1 \times 5^2 \times 7^1$   
 $\rightarrow \{4, 1, 2, 1\}$   
 $\rightarrow \{5, 2, 3, 2\}$   
 $\rightarrow 5 \times 2 \times 3 \times 2 \rightarrow \underline{60}$

Eg →  $21600 \rightarrow 216 \times 100$   
 $\rightarrow 6^3 \times 10^2$   
 $\rightarrow (2 \times 3)^3 \times (5 \times 2)^2$   
 $\rightarrow 2^3 \times 3^3 \times 5^2 \times 2^2$   
 $\rightarrow 2^5 \times 3^3 \times 5^2$   
 $\rightarrow (5, 3, 2) \rightarrow (6, 4, 3)$   
 $\rightarrow 6 \times 4 \times 3 \rightarrow \underline{72}$

→ Inequality as absolute value

→ Express  $-3 \leq x \leq 11$  as absolute inequality

→ Take midpoint  $\frac{-3+11}{2} = 4$

→  $|x-4| \leq (11-4)$  {right value}

→  $|x-4| \leq 7$

→  $|-K+4| > 2$   $\begin{cases} -K+4 > 2 \\ -K+4 < -2 \end{cases}$

$|x| \geq 6$

$\begin{cases} -x \geq 6 & -x \leq -6 \\ x \leq -6 & x \geq 6 \end{cases}$

→ Sum of angles in  $n$  sided polygon

$$(n-2) \times 180$$

→ Diagonals of an  $n$  sided polygon

$$\frac{n(n-3)}{2}$$

→ Double matrix

	Type A	Type B	
Type 1	a	b	a+b
Type 2	c	d	c+d
	a+c	b+d	a+b+c+d

→ Sum of integers in a range →  $\frac{n}{2}(a_1 + a_n)$

$n \rightarrow$  no. of terms →  $a_n - (a_1 + 1)$

Example → b/w 45 & 155  
                  ↓            ↓  
                   $a_1$         $a_n$

$$n = 155 - (45 + 1)$$

→ Sum of multiples in a range → No. of terms =  $N$

$a_1 \rightarrow$  beginning of range

$a_n \rightarrow$  last number in range

$$\rightarrow (a_1 + a_n) \times \frac{N}{2}$$

Examples → Sum of multiples of 5 bigger than 100 & less than 200.

$$\begin{aligned} \rightarrow \text{So } a_1 &= 105 \\ a_n &= 195 \\ N &= \frac{195 - 105}{5} + 1 \rightarrow 19 \end{aligned} \quad \left. \vphantom{\begin{aligned} \rightarrow \text{So } a_1 &= 105 \\ a_n &= 195 \\ N &= \frac{195 - 105}{5} + 1 \rightarrow 19 \end{aligned}} \right\} \begin{aligned} &(195 + 105) \times \frac{19}{2} \\ &= 2850 \end{aligned}$$

→ Unit digit of  $57^{123}$

→ only see  $\left. \begin{array}{l} 7^1 \rightarrow 7 \\ 7^2 \rightarrow \dots 9 \\ 7^3 \rightarrow \dots 3 \\ 7^4 \rightarrow \dots 1 \\ 7^5 \rightarrow \dots 7 \\ 7^6 \rightarrow \dots 9 \\ 7^7 \rightarrow \dots 3 \\ 7^8 \rightarrow \dots 1 \end{array} \right\} \text{pattern}$

→ Repeats every 4,  $123 \div 4 \rightarrow 3$ ,  
check third no in pattern = 3

→ Triangle side property



Sum of either 2 sides must be greater than the third side

$$a + b > c$$

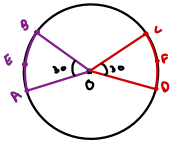
$$b + c > a$$

$$a + c > b$$

→ Set of  $n$  items with  $b$  identical items

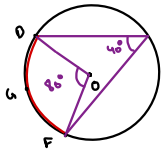
$$N = \frac{n!}{b!}$$

→ Equal arcs and chords



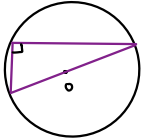
If  $\angle AOB = \angle COD$ , then arc AEB = arc CFD

→ Arc and inscribed angle (angle which doesn't fall on center  $\angle ABC$ )



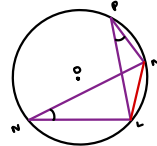
angle of arc will be  $80^\circ$ , double of inscribed angle

→ Right angle



This has to be  $90^\circ$

→ 2 inscribed angles and same arc / chord



These angles are equal

→ Arc length proportion

$$\frac{\text{arc length}}{2\pi r} = \frac{\text{angle}}{360}$$

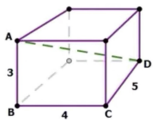
→ Area of a sector proportion

$$\frac{\text{area of sector}}{\pi r^2} = \frac{\text{angle}}{360}$$

→ Cylinder

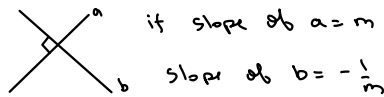
$$\text{Volume} = \pi r^2 h$$

$$\text{Area} = 2\pi r^2 + 2\pi rh$$



$$AD^2 = AB^2 + BC^2 + CD^2$$

→ Slope of  $\perp$  lines



if slope of  $a = m$

slope of  $b = -\frac{1}{m}$

Inter Quartile Range

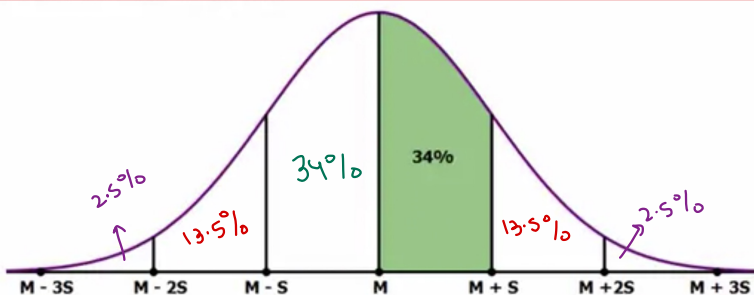
$$IQR \rightarrow Q_3 - Q_1$$

→ Distance b/w points  $(x, y)$  &  $(a, b)$

$$\sqrt{(x-a)^2 + (y-b)^2}$$

→ Standard deviation →

- ① Calc mean
- ② Subtract all values from mean
- ③ Square all values
- ④ Find mean of this new set → Variance
- ⑤ Square root variance → SD



→ Divisors = Factors

→ Parallelogram Area  
= base  $\times$  height

Surface area of box  
=  $2(wl + hl + hw)$

→ 92.645  
9 → tens  
2 → ones  
6 → tenths  
4 → hundredths  
5 → thousandths }ths

→ 1 percentile of  $x$   
=  
1% of  $x$

→ Proportionality  
→ Directly  $a = kb$   
→ Inversely  $a = \frac{k}{b}$

→ For how many integer values is  
 $f(x) = \frac{\sqrt{x-2}}{x}$  undefined

when  $x = 0$   
 $x = 1$   
 $x = -1, -2, -3, \dots, -\infty$   
INFINITE VALUES

→ if  $\frac{a}{b} > \frac{c}{d}$

then  $\frac{a}{b} - \frac{c}{d} > 0$  is true

but  $ad > cb$  is not always true  
since any of these could be  
negative and require sign change

→ 5 is how many fifths of 10  
• fifth of  $\rightarrow \frac{x}{5}$

$$\frac{x}{5} \times 10 = 5$$
$$x = 2.5$$

→  $7.5\bar{3}$  in fraction  
→  $7.5\bar{3} + 0.00\bar{3}$   
→  $\frac{75\bar{3}}{100} + 0.\bar{3} \times 0.01$   
→  $\frac{75\bar{3}}{100} + \left(\frac{1}{3}\right)\left(\frac{1}{100}\right)$   
→  $\frac{75\bar{3}}{100} + \frac{1}{300} \rightarrow \frac{2275}{300}$   
→  $\frac{91}{12}$

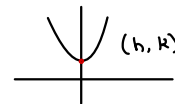
→ Standard Deviation

- Set of all positive numbers
- multiply all numbers with  $\frac{1}{2}$  ↓ SD
- Smallest no. increased to be median ↓ SD
- Smallest no. increased to become largest ↓ SD ↑ SD
- Largest number is doubled ↑ SD

→ Probability question  
"at least" →  $1 - x$

- $P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$  {not mutually exclusive}
- $P(A \text{ or } B) = P(A) + P(B)$  {for disjoint / mutually exclusive}
- $P(A \text{ and } B) = P(A) \cdot P(B)$  {for independent}

→ Equation of Parabola  
 $y = a(x-h)^2 + k$



$$y = x^2 + 1 \quad \vee$$
$$y = -x^2 + 1 \quad \wedge$$

→ Rhombus = 11<sup>th</sup> polygon with 4 equal sides  
→ Square = Largest rhombus of a given size

→ Standard deviation

A: 10, 20, 30, 40, 50 } Dis of 10  
B: 10, 30, 50, 70, 90 } Dis of 20

B has a higher SD

→ Legs of a right triangle

