

Design a Hebb net to implement logical AND function:-  
 → The training data for the AND function :-  
 Note: Inputs and target both are binary & addition of bias is done.

Inputs	<u>Target</u>
1 1 1	1
1 -1 1	-1
-1 1 1	-1
-1 -1 1	-1

→ Initially the weight & bias are set to zero, i.e.

$$\cancel{w_1 = w_2 = b = 0}$$

→ First input  $[x_1 \ x_2 \ b] = [1 \ 1 \ 1]$  and target = 1 [i.e.,  $y = 1$ ].

→ setting the initial weights as old weights and applying the Hebb rule, we get :-

$$w_i(\text{new}) = w_i(\text{old}) + \Delta w_i$$

→ Here  $\Delta w_i = x_i y$

$$\Delta w_1 = x_1 y = 1 \times 1 = 1$$

$$\Delta w_2 = x_2 y = 1 \times 1 = 1$$

$$\Delta b = y = 1$$

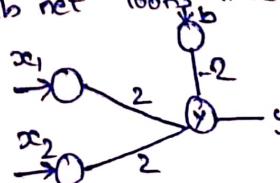
Inputs	weight changes			weights		
	$w_1$	$w_2$	$b$	$w_1$	$w_2$	$b$
$x_1 \ x_2 \ b$	$y \ \Delta w_1 \ \Delta w_2 \ \Delta b$			(0)	(0)	(0)
1 1 1	1 1 1 1			1	1	1
1 -1 1	-1 -1 1 -1			0	2	0
-1 1 1	-1 -1 1 -1			1	1	-1
-1 -1 1	-1 -1 1 -1			2	2	-2

$$\rightarrow \text{so, } w_1(\text{new}) = w_1(\text{old}) + \Delta w_1 \\ = 0 + 1 = 1$$

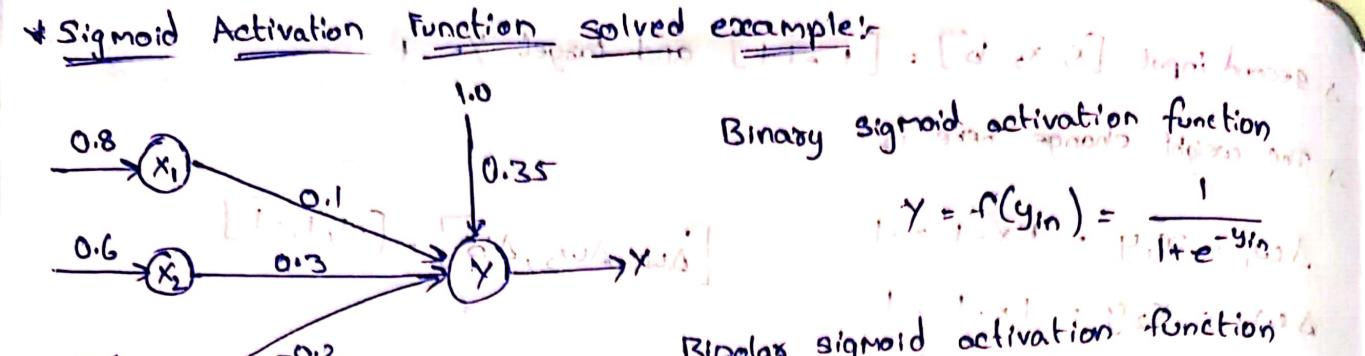
$$w_2(\text{new}) = w_2(\text{old}) + \Delta w_2 \\ = 0 + 1 = 1$$

$$b(\text{new}) = b(\text{old}) + \Delta b \\ = 0 + 1 = 1$$

∴ The Hebb net looks like



- second input  $[x_1, x_2, b] = [1, -1, 1]$  and target  $y = -1$
- The weight change here is :-
- $$\Delta w_1 = x_1 y = 1 \times -1 = -1$$
- $$\Delta w_2 = x_2 y = -1 \times -1 = 1$$
- $$\Delta b = b = -1$$
- so,  $w_1(\text{new}) = w_1(\text{old}) + \Delta w_1$ ,
- $$= 1 + (-1) = 0$$
- $$[w_1, w_2, b] = [0, 2, 0]$$
- $$w_2(\text{new}) = w_2(\text{old}) + \Delta w_2 \Rightarrow 1 + 1 = 2$$
- $$b(\text{new}) = b(\text{old}) + \Delta b \Rightarrow 1 + (-1) = 0$$
- third input  $[x_1, x_2, b] = [-1, 1, 1]$  and target i.e.,  $y = -1$ .
- The weight change here is :-
- $$\Delta w_1 = x_1 y = -1 \times 1 = -1$$
- $$\Delta w_2 = x_2 y = 1 \times 1 = 1$$
- $$\Delta b = b = -1$$
- so,  $w_1(\text{new}) = w_1(\text{old}) + \Delta w_1 \Rightarrow 0 + 1 = 1$
- $$w_2(\text{new}) = w_2(\text{old}) + \Delta w_2 \Rightarrow 2 + (-1) = 1$$
- $$b(\text{new}) = b(\text{old}) + \Delta b \Rightarrow 0 + (-1) = -1$$
- fourth input  $[x_1, x_2, b] = [-1, -1, 1]$  and target i.e.,  $y = -1$
- The weight change here is :-
- $$\Delta w_1 = x_1 y = (-1 \times -1) = 1$$
- $$\Delta w_2 = x_2 y = -1 \times -1 = 1$$
- $$\Delta b = b = -1$$
- so,  $w_1(\text{new}) = w_1(\text{old}) + \Delta w_1 \Rightarrow 1 + 1 = 2$
- $$w_2(\text{new}) = w_2(\text{old}) + \Delta w_2 \Rightarrow 1 + 1 = 2$$
- $$b(\text{new}) = b(\text{old}) + \Delta b \Rightarrow -1 + (-1) = -2$$



Binary sigmoid activation function

$$y = f(y_{in}) = \frac{1}{1+e^{-y_{in}}}$$

Bipolar sigmoid activation function

$$y = f(y_{in}) = \frac{2}{1+e^{-y_{in}}} - 1$$

$$0 \rightarrow (-1) + 1 = 0$$

$[0 \times 0] + [0 \times 0 \times 0]$

→ Here  $y_{in} = b + \sum_{i=1}^n w_i x_i$   $b = 0.35 + (0.1)(0.8) + (0.3)(0.6) + (-0.2)(0.4) = 0.53$

$$y_{in} = b + x_1 w_1 + x_2 w_2 + x_3 w_3 = 0.35 + (0.1)(0.8) + (0.3)(0.6) + (-0.2)(0.4)$$

$$= 0.35 + (0.8)(0.1) + (0.6)(0.3) + (0.4)(-0.2)$$

$$= 0.53.$$

→ Binary sigmoid activation function:  $y = f(y_{in}) = \frac{1}{1+e^{-y_{in}}} = \frac{1}{1+e^{-(0.53)}} = 0.625$

→ Bipolar sigmoid activation function:  $y = f(y_{in}) = \frac{2}{1+e^{-y_{in}}} - 1 = \frac{2}{1+e^{-(0.53)}} - 1 = 0.259$

→ Threshold Function:  $f(v) = \begin{cases} 0 & \text{if } v < 0 \\ 1 & \text{if } v \geq 0 \end{cases}$   $\text{Here: } v = y_{in}$

→ Linear Function:  $f(v) = \begin{cases} v & \forall v \\ 0 & v < 0 \end{cases}$

→ Piecewise Linear Function:  $f(v) = \begin{cases} 1, & v \geq 0.5 \\ v, & -0.5 \leq v < 0.5 \\ 0, & v \leq -0.5 \end{cases}$

→ Rectified Linear Unit (ReLU):  $f(v) = \max(0, v)$

→ leaky Rectified Linear unit (Leaky-ReLu):  $f(v) = \max(\alpha v, v)$  where  $0 < \alpha < 1$

(linear)  $= 0.4$   $\therefore$  Piecewise linear function  $= 0.4$

ReLU  $\Rightarrow f(v) = \max(0, v) \Rightarrow \max(0, 0.4) = 0.4$

$(\alpha=0.4)$  Leaky ReLU  $\Rightarrow f(v) = \max(\alpha v, v) = \max((0.4)(0.4), 0.4) = \max(0.16, 0.4) = 0.4$

Sigmoid ( $\alpha=1$ )  $\Rightarrow y = f(v) = \frac{1}{1+e^{-v}}$   $\frac{1}{1+e^{-0.4}} = 0.59$

softmax Activation function:  $f(v_i) = \frac{e^{v_i}}{\sum_{j=1}^n e^{v_j}} = \frac{e^{0.4}}{e^{0.16} + e^{0.2} + e^{0.4} + e^{0.7}} = \frac{1.49182}{4.431} = 0.336$

\* Implement AND function using perceptron networks for bipolar inputs and targets E.g.:-

In general, in a feed forward neural network, learning happens in 2 steps :-  
In case of perceptron learning rule, the learning signal is the difference between the calculated output and actual (target) output of a neuron.

The output "y" is obtained on the basis of the net input calculated and activation function being applied over the net input.

$$y_{in} = \text{bit } \sum_{i=1}^n w_i x_i + b \quad \text{or sum of products of weights (precsns) & bias}$$

$y = f(y_{in})$   $\begin{cases} 1 & \text{if } y_{in} > \theta \\ 0 & \text{if } -\theta \leq y_{in} \leq \theta \\ -1 & \text{if } y_{in} < -\theta \end{cases}$

Here  $\theta$  is threshold. If  $y_{in} > \theta$ , output is 1. If  $-\theta \leq y_{in} \leq \theta$ , output is 0. If  $y_{in} < -\theta$ , output is -1. This is called a step function or signum function.

Weights are updated using formula -  
if  $y \neq t$ , then  $w(\text{new}) = w(\text{old}) + \alpha t e_t$  (here  $\alpha$  is learning rate)

$$\text{else, we have: } w(\text{new}) = w(\text{old})$$

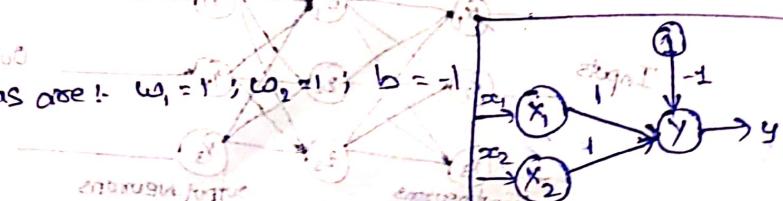
Input	Target	Netinput ( $y_{in}$ )	Output ( $y$ )	Weight changes		
				$\Delta w_1$	$\Delta w_2$	$b$
$x_1 = 1$	$t = 1$	0	0	0	0	0
-1	-1	1	1	0	0	0
1	-1	-1	-1	0	0	0
-1	1	-1	1	0	0	0
-1	-1	-1	-1	0	0	0

EPOCH-1		Measuring state lossage of						
1	1	0	0	0	0	0	0	0
-1	-1	1	1	0	0	0	0	0
1	-1	-1	-1	0	0	0	0	0
-1	1	-1	1	0	0	0	0	0
-1	-1	-1	-1	0	0	0	0	0

EPOCH-2 (or 2nd iteration)		Measuring state lossage of						
1	1	0	0	0	0	0	0	0
-1	-1	1	1	0	0	0	0	0
1	-1	-1	-1	0	0	0	0	0
-1	1	-1	1	0	0	0	0	0
-1	-1	-1	-1	0	0	0	0	0

EPOCH-3 (or 3rd iteration)		Measuring state lossage of						
1	1	0	0	0	0	0	0	0
-1	-1	1	1	0	0	0	0	0
1	-1	-1	-1	0	0	0	0	0
-1	1	-1	1	0	0	0	0	0
-1	-1	-1	-1	0	0	0	0	0

∴ for  $\alpha=1$ , the final weights & bias are:  $w_1 = 1, w_2 = 1, b = -1$



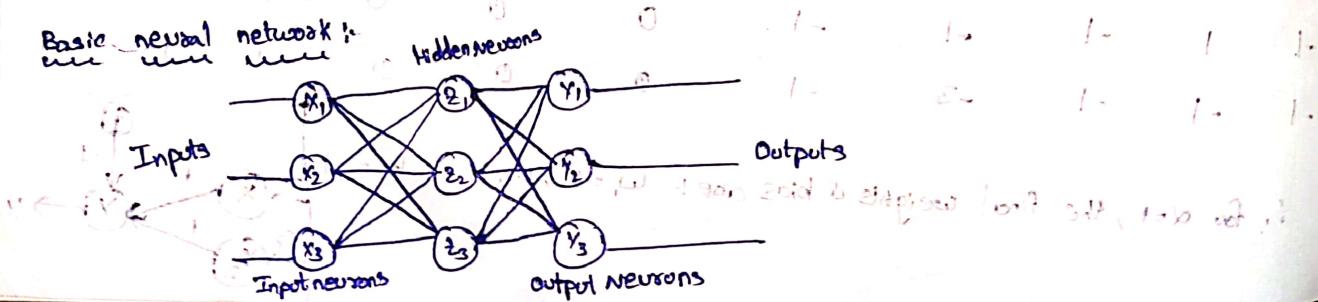
## \* Artificial Neural Network: Introduction

- An artificial neural network (ANN) may be defined as an information-processing model that is inspired by the way biological nervous systems, such as brain, process information.
- This model tries to replicate only the most basic functions of the brain.
- An ANN is composed of a large number of highly interconnected processing units (neurons) working in unison to solve specific problems.
- Like human being, the ANN learn by examples.
- An ANN is configured for a specific application, such as spam classification, Face Recognition, pattern recognition through a learning process.
- Each neuron is connected with the other by a connection/link.
- Each connection link is associated with weights, which contains the information about the input signal.
- This information is used to solve a particular problem by the neural network.
- ANN have the ability to learn, recall, identify & generalize training patterns or data similar to human brain.
- Thus, the ANN Processing elements are called neurons or artificial neurons.
- Each neuron has an internal state of its own.
- This internal state is called the activation level of neuron.
- The activation signal of a neuron is transmitted to other neurons.
- Remember, a neuron can send only one signal at a time, which can be transmitted to several other neurons.

### Neural Networks:

Huge distributed information-processing system, made up of simple inter-connected processing units, called as neurons (or) nodes which work together collectively.

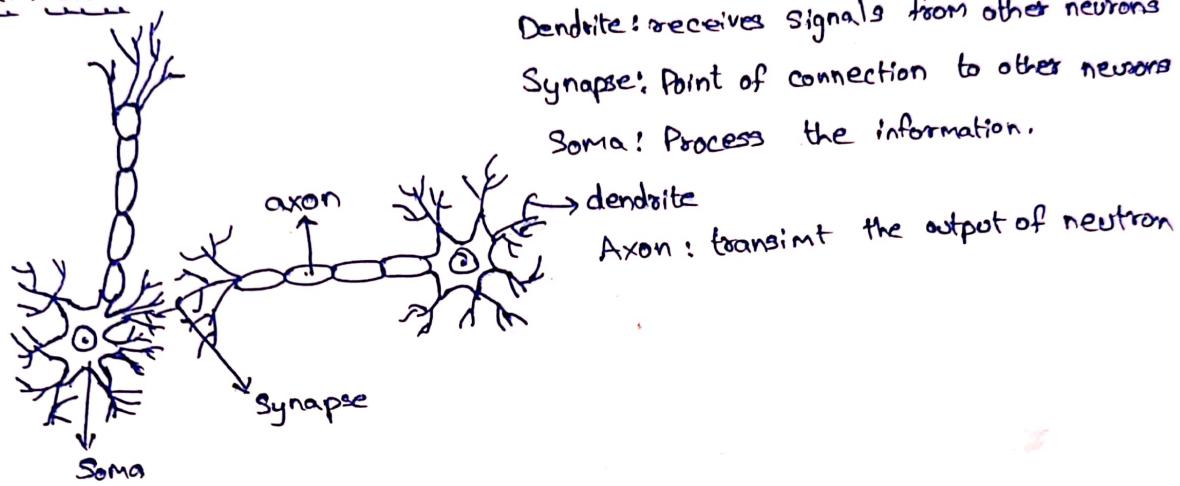
### Basic neural network:



## \* Application of Neural Networks :-

- Control systems → Signal processing
- Image, voice, Pattern recognition
- DBMS
- Data mining & processing
- medical Imaging & diagnosis
- Traffic control
- weather prediction & forecast.

## \* Biological Neuron :-



Dendrite: receives signals from other neurons

Synapse: Point of connection to other neurons

Soma: Process the information.

Axon: transmit the output of neuron

## BNN (Human)

- Cell
- Dendrites / synapse
- Soma
- Axon

→ Parallel processing i.e.,  
more than 1 at a time

→ Slow (Comparatively)

→ unreliable (can forget years ago  
topic)

→ Dynamic infrastructure

## ANN (Computer)

- Neuron / node
- weights
- Net input
- Output

→ Single time ~~single~~  
single processing

→ Fast

→ Reliable

→ Static infrastructure.

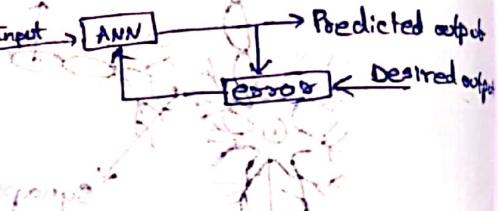
- A network is said to be feedforward network if no neuron in the output layer receives an input from a node in the same (or) preceding layer.
- The hidden layers are not in contact with external environment. With more help of hidden layers, the output response is more efficient. The nodes in the previous layers are connected to the nodes in the next layers.

- In a single layer recurrent network, the feedback forms a closed loop.

~~because each of different neurons has its own feedback path~~

\* Supervised learning :-

- The learning here is performed with the help of the teacher.
- Input vector along with target vector is known as the training pair.
- ex :- Classification problems, Regression problems



\* Unsupervised learning :-

- learning without teacher; Tadpole learn to swim.
- during training process, network receives input patterns and organize it to form clusters; eg: clustering.

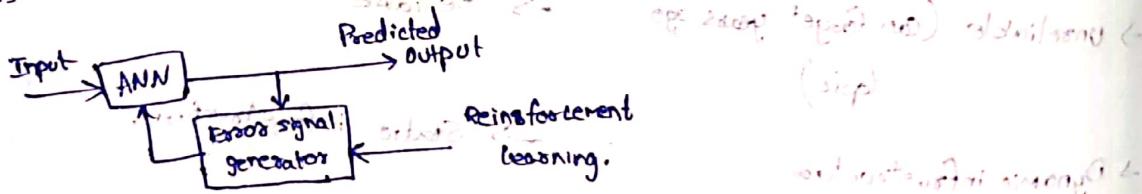


\* Semi-Supervised learning :-

- both labelled & unlabelled data is given. (sample of labelled data is small compare to unlabeled data)
- initial training is done using labelled and then it will be applied to greater no of unlabelled data.

\* Reinforcement learning :-

- learning is done by interaction with the environment. Similar to supervised learning.
- agent receives feedback in the form of rewards or penalties based on its actions, and its goal is to learn a policy that maximizes its cumulative reward over time.



Applications :-

- web search; Computational biology; Finance; E-commerce; space exploration; robotics; debugging
- Intelligent video surveillance; social networking,

## Learning Rules!:-

### i) Error correction:-

In this type of learning; The network adjusts its weights in response to the difference between its predicted output & desired output. This is done until the Predicted output equals to desired output.

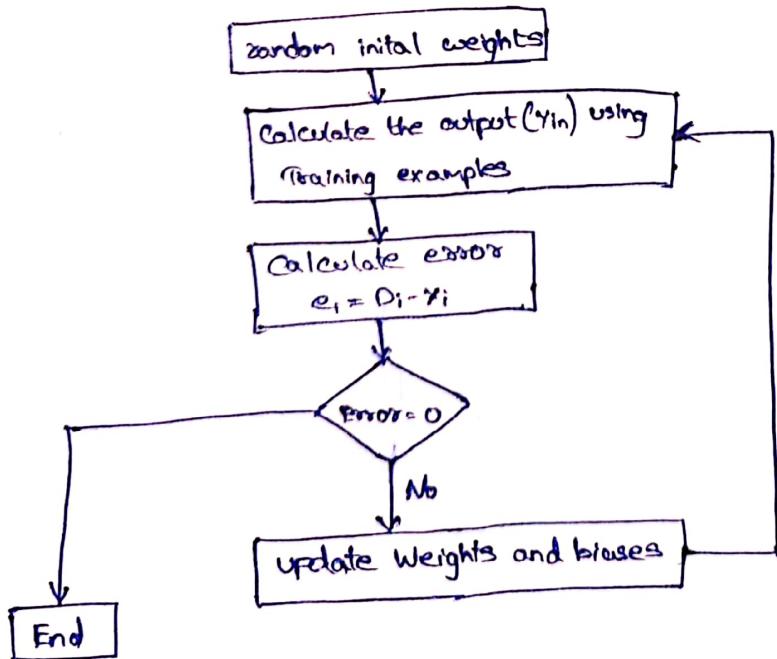
### ii) Memory-based learning:- This type of learning involves storing the training data examples in the network & using them on new data. (handwritten recog.)

### iii) Habbian learning:- "cell that fire together, wire together", in other words when two neurons are activated, the strength of the connection b/w them increases, and vice versa.

### iv) Competitive learning:- neurons in the network compete with each other to become activated in response to particular input. The winner then adjust its weight to better recognize the input.

### v) Boltzmann learning:- This type of learning is a unsupervised learning based on the Boltzmann distribution from statistical physics. learns by sampling from this distribution and adjusting the weights to maximize the probability of generating the correct outputs.

### \* Perception learning algorithm flow chart:



- To get the correct weights, many training 'epochs' are used with suitable learning rate  $\alpha$ .
- This can't be used to solve non-linearly separable like (XOR)

## 2 kinds of learning in ANN:-

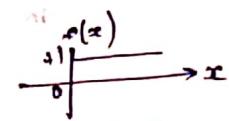
(gradient decent or back propagation)

- i) Parameter learning : It updates the connecting weight in a neural net.
- ii). Structure learning : It focuses on the change in network structure (which includes number of nodes in each layer & number of processing elements as well as their connecting types.)

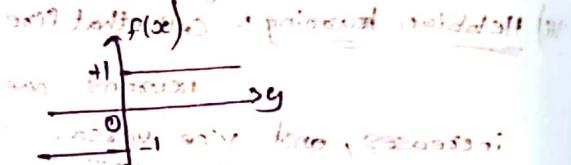
• simpler because of single input layer

Activation Functions :- (here  $\Theta$  represent some constant threshold value)

i) Identity function :  $f(x) = x$  for all  $x$

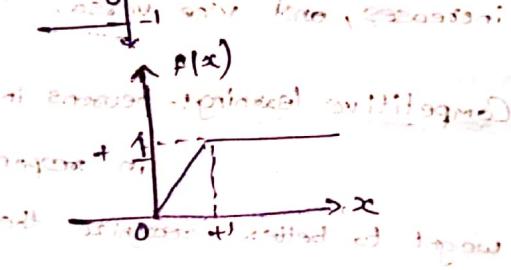


ii) binary step function :  $f(x) = \begin{cases} 1 & \text{if } x \geq \Theta \\ 0 & \text{if } x < \Theta \end{cases}$

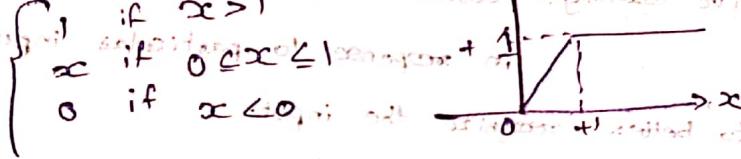


iii) bipolar step function :

$$f(x) = \begin{cases} 1 & \text{if } x \geq \Theta \\ 0 & \text{if } x = \Theta \\ -1 & \text{if } x < \Theta \end{cases}$$



iv) Ramp function :  $f(x) = \begin{cases} 1 & \text{if } x > 1 \\ x & \text{if } 0 \leq x \leq 1 \\ 0 & \text{if } x < 0 \end{cases}$



iii) no linear operation required in back-propagation nets. & of two types:

v) Sigmoidal functions; widely used in back-propagation nets. & of two types (0 to 1 range)

i) Binary sigmoid function :  $f(x) = \frac{1}{1+e^{-\lambda x}}$  { $\lambda$  is steepness parameter}

ii) Bipolar sigmoid function :  $f(x) = \frac{2}{1+e^{-\lambda x}} - 1$  (-1 to +1 range)

Has been in 'logistic' function

$$\text{so } y = f(x) = \frac{1}{1+e^{-\lambda x}} \quad \text{for Binary sigmoid activation function}$$

$$\text{and has } y = f(y_{in}) = \frac{2}{1+e^{-\lambda y_{in}}} - 1 \quad \text{for Bipolar sigmoid activation function}$$

(for eg, n=3 then,  $y_{in} = b + x_1 w_1 + x_2 w_2 + x_3 w_3$ )

$$\text{where: } y_{in} = b + \sum_{i=1}^n x_i w_i$$

local training  
weights  
outputs  
error

↓ forward pass  
↓ backward pass



[bias?]

## Mcculloch-Pitts Neuron:-

since the firing of the output neuron is based upon the threshold, the activation function here is defined as:-

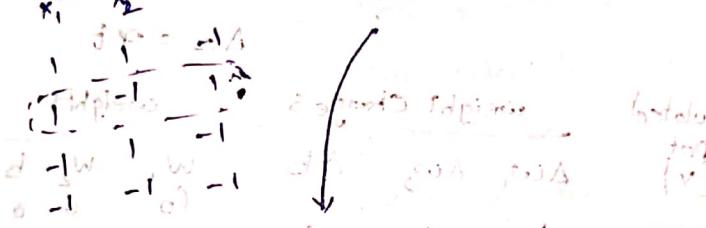
$$f(y_{in}) = \begin{cases} 1 & \text{if } y_{in} \geq 0 \\ 0 & \text{if } y_{in} < 0 \end{cases}$$

(Here, the threshold value should also satisfy :-  $\Theta > \sum w_i - p$   $\rightarrow$  negative weight  
+ve. weight)

## Implementing ANNOT function using Mcculloch-pitts Neuron:-

$x_1, x_2 \rightarrow y$

assume  $w_1=1$  &  $w_2=1$



$$\text{now, } y_{in} = x_1 w_1 + x_2 w_2$$

$$(1,1), y_{in} = 1(1) + 1(1) = 2$$

only this can be fixed in this

$$(1,-1), y_{in} = 1(1) + 1(-1) = 0$$

$$(-1,1), y_{in} = 1(-1) + 1(1) = 0$$

$$(-1,-1), y_{in} = 1(-1) + 1(-1) = -2$$

now by using  $w_1=1$  &  $w_2=-1$ ; we can

so the  $\Theta$  will be :  $\Theta \geq 2$  (threshold is 0)

## Implementing AND function using Mcculloch-pitts Neuron:-

$x_1, x_2 \rightarrow y$

assume  $w_1=1$  &  $w_2=1$

$$\text{now, } y_{in} = x_1 w_1 + x_2 w_2$$

$$(1,1), y_{in} = 1(1) + 1(1) = 2$$

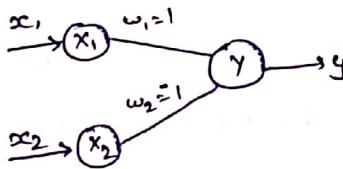
$$(1,-1), y_{in} = 1(1) + 1(-1) = 0$$

$$(-1,1), y_{in} = 1(-1) + 1(1) = 0$$

$$(-1,-1), y_{in} = 1(-1) + 1(-1) = -2$$

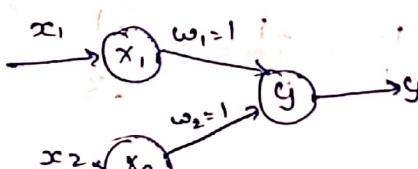
here in macculloch-pitts Neuron, we will change

the desired and required  $x_1, x_2$  should be fired.



$$\begin{aligned} (1,1), y_{in} &= 1(1) + 1(1) = 2 \\ (1,-1), y_{in} &= 1(1) + 1(-1) = 0 \\ (-1,1), y_{in} &= 1(-1) + 1(1) = 0 \\ (-1,-1), y_{in} &= 1(-1) + 1(-1) = -2 \end{aligned}$$

only fire for  $x_1=1$  &  $x_2=1$



here for  $\Theta \geq 2$  will fire only the required  $x_1$  &  $x_2$ .

$$\therefore y = f(y_{in}) = \begin{cases} 1 & \text{if } y_{in} \geq 2 \\ 0 & \text{if } y_{in} < 2 \end{cases}$$

the assume weights until only

AND using perception:-

Logistic function

$$x_1, x_2$$

$$\begin{matrix} 1 & 1 \\ 1 & -1 \\ -1 & 1 \\ -1 & -1 \end{matrix}$$

Target output T = 1 if sum of all neurons, just as 0 if sum is less than or equal to zero.

$$\text{OR } y = \begin{cases} 1 & \text{if } y > 0 \\ 0 & \text{if } y = 0 \\ -1 & \text{if } y < 0 \end{cases}$$

$$y_{in} = b + \sum_{i=1}^n x_i w_i \quad ; \quad y = f(y_{in}) = \begin{cases} 1 & \text{if } y_{in} > 0 \\ 0 & \text{if } y_{in} = 0 \\ -1 & \text{if } y_{in} < 0 \end{cases}$$

Initial weights

$$w_i(\text{new}) = w_i(\text{old}) + \Delta w_i$$

$$\Delta w_i = \alpha x_i t \cdot (y_{in})$$

$$\Delta w_1 = \alpha t x_1$$

$$\Delta w_2 = \alpha t x_2$$

$$\Delta b = \alpha t$$

Perceptron rule

Input vector

Output vector

Target output

Calculated output

Weight changes

Final weights

Inputs

Epoch-1

Inputs

Epoch-2

Inputs

Epoch-3

Inputs

Epoch-4

Inputs

Epoch-5

Inputs

Epoch-6

Inputs

Epoch-7

Inputs

Epoch-8

Inputs

Epoch-9

Inputs

Epoch-10

Inputs

Epoch-11

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Epoch-12

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Epoch-13

Inputs

Epoch-14

Inputs

Epoch-15

Inputs

Epoch-16

Inputs

Epoch-17

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Epoch-18

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Epoch-19

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Epoch-20

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Epoch-22

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Epoch-86

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Epoch-87

Inputs

Epoch-88

Inputs

Epoch-89

Inputs

Epoch-90

Inputs

Epoch-91

Inputs

Epoch-92

Inputs

Epoch-93

Inputs

Epoch-94

Inputs

Epoch-95

Inputs

Epoch-96

Inputs

Epoch-97

Inputs

Epoch-98

Inputs

Epoch-99

Inputs

Epoch-100

Inputs

Inputs

Epoch-1

Inputs

Epoch-2

Inputs

Epoch-3

Inputs

Epoch-4

Inputs

Epoch-5

Inputs

Epoch-6

Inputs

Epoch-7

Inputs

Epoch-8

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Epoch-9

Inputs

Epoch-10

Inputs

Epoch-11

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Epoch-12

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Epoch-13

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Epoch-14

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Epoch-15

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Epoch-16

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Epoch-17

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Epoch-29

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Epoch-30

Inputs

Epoch-31

Inputs

Epoch-32

Inputs

Epoch-33

Inputs

Epoch-34

Inputs

Epoch-35

Inputs

Epoch-36

Inputs

Epoch-37

Inputs

Epoch-38

Adaline for OR function's

antibiotic prices are astronomical

$x_1 \quad x_2 \quad t$  Initially, the weights are set to  $w_1 = w_2 = b = 0$ ,  
 and learning rate = 0.1 & 0.2 All for AND NOT

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→ Initially, the weights are set to  $w_1 = w_2 = b = 0.1$   
 and learning rate = 0.1 & 0.2 All for AND NOT

- 1 -

→ Calculate net input  $\Rightarrow Y_{in} = b + \sum_{i=1}^n \alpha_i w_i$

$$\begin{matrix} -1 & 1 & 1 \\ & -1 & - \end{matrix}$$

→ Then compute  $(t-y_{in})$

$\rightarrow$  Then calculate change in weights:  $\Delta w_i = \alpha (t - y_{in}) x_i$

$$\Delta\omega_2 = \alpha (\text{tryin})^{x_2}$$

$$\Delta b = \alpha(t - y_n)$$

-> Then update weights :  $w_i(\text{new}) = w_i(\text{old}) + \Delta w_i$

$\rightarrow$  Then calculate error :  $E = (\text{tryin})^2 - (\text{calcd})^2$

→ Then calculate errors:  $E = \text{Argin}$ ,  $\Sigma E$  in each epoch and  
 → Calculate the sum of errors i.e.  $\Sigma E$  in each epoch and  
 → If  $\Sigma E$  in each epoch is decreasing by calculating

for First 2 Epochs

$$y_{in} = b + \sum x_i w_i$$

$$(t - y_{in})^2 = \text{const.}$$

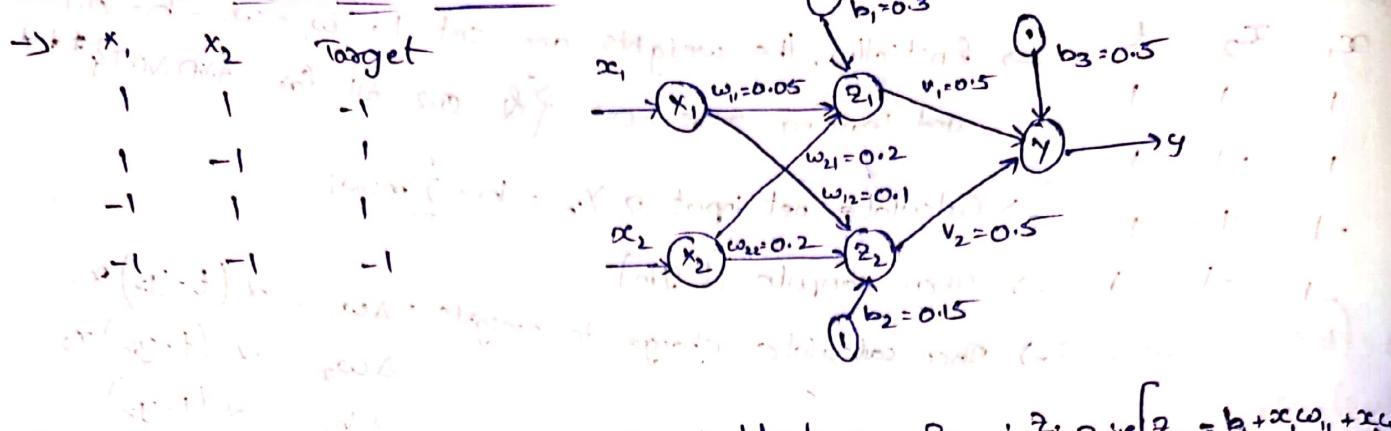
$$\Delta w_1 = \alpha (t - y_{in}) x_1$$

$$\Delta w_2 = \alpha (t - y_{in}) x_2$$

where  $\alpha = 0.1$

Inputs		Target	Net input	Error	Weight changes	Weights	Error
$x_1$	$x_2$	$t$	$(y_{in})$	$(t-y_{in})$	$\Delta w_1, \Delta w_2$	$\Delta b$	$b$
1	1	1	0.3	0.7	0.07	0.07	0.49
1	-1	1	0.17	0.83	0.083	-0.083	0.17
-1	1	1	0.087	0.913	-0.0913	0.0913	0.1617
-1	-1	1	0.0043	-1.0043	0.1004	0.1004	0.2787
-1	-1	-1					0.2439

## Implementing XOR using Madaline



→ First calculate the net input to the hidden layer  $z_{in1}, z_{in2}$  i.e.

$$\begin{cases} z_{in1} = b_1 + x_1 w_{11} + x_2 w_{21} \\ z_{in2} = b_2 + x_1 w_{12} + x_2 w_{22} \end{cases}$$

→ Output of the hidden layer can be calculated by applying ~~hidden~~ activation function :-

$$z_i = f(z_{in}) = \begin{cases} 1 & \text{if } z_{in} \geq 0.5 \\ -1 & \text{if } z_{in} < 0.5 \end{cases}$$

→ Now calculate the net input to the output :  $y_{in} = b_3 + z_1 v_1 + z_2 v_2$

→ ~~apply~~ activation function over net input  $y_{in}$  to calculate the output  $y$

→ if  $y \neq t$ , perform weight updation by updating ~~weights & bias of hidden layer~~

$$w_{ij}(\text{new}) = w_{ij}(\text{old}) + \alpha (t - z_{inj}) x_i$$

$$b_j(\text{new}) = b_j(\text{old}) + \alpha (t - z_{inj})$$

Inputs  
 $x_1, x_2$

Target

t

(t)

$z_{in1}$

$z_{in2}$

$z_1$

$z_2$

$y_{in}$

$y$

$w_{11}, w_{12}$

$w_{21}, w_{22}$

$b_1, b_2$

$b_3$

BAM :- is a supervised learning model.

→ This can be used for pattern recognition and associative recall task.

→ The network consists of two layers ; input layer and output layer with each layer containing equal number of neurons.

→ The connection b/w i/p & o/p is bidirectional, so the information can flow bidirectionally.

→ During the training process, the network adjusts its weights between neurons by presented i/p, o/p pairs.

→ Once the network is trained, it can be used to recall an output.

Partten from the given input pattern and vice versa.

→ BAM is mainly used to retrieve a pattern from the given, noisy or incomplete pattern.

Adaline (Adaptive linear neuron) :- Used for regression classification & pattern recognition.

→ It is a single layered neural network with a linear activation function.

→ used for handling linearly separable classes and adjust its weights iteratively to minimize the error between the predicted and desired.

using gradient descent algorithm.

Madaline (multiple Adaptive linear neuron) :-

→ multi-layer NN that consists of multiple Adalin units in layers.

→ used in pattern recognition where goal is to classify into multiple categories.

→ designed to handle non linear separable classes

→ desired to handle non linear separable classes

- Associative memory network :- is a type of ANN that is designed to store and retrieve data from memory.
- Auto-associative memory :- stores & retrieves patterns by comparing it with itself, and information all over → used for pattern completion.
- consists of single layered neurons that are fully connected.
  - present with set of inputs during training and weights b/w neurons adj. using Hebb's rule.
- Hebb-associative memory :- Comparing with other patterns
- used for pattern recognition.
  - consists of multiple layers of neurons
  - present with set of input & output during training and Hebb is used to adj. weight.
- Hopfield learning :- is a type of unsupervised learning which is also known as content addressable memory in which neurons are arranged in specific pattern to form recurrent neural network, and adjust the weights of the network to minimize the energy.
- Discrete Hopfield network :- is a fully interconnected single-layer feedback network.
- it is also a symmetric weighted network that takes two valued inputs: binary (0 or 1) / bipolar (-1 or +1)
  - uses discrete functions to minimize the energy of the network, used for discrete problems.
- Continuous Hopfield network :- A discrete H.f.n can be modified to C.H.N by assuming time as a continuous variable.
- This is a type of recurrent neural network used for pattern recognition & optimization problem.
  - uses continuous functions to minimize the energy of the network and update their values.
  - limitation - Can't store large no. of patterns & get stuck in local minima.

Hopfield, Boltzmann, Competitive  $\rightarrow$  unsupervised learning

### Delta learning rule :- (supervised)

- > is a gradient descent method that adjust the weights in order to minimize the diff b/w actual output and desired output.
  - > used in single layer perceptron, and can also used in backpropagation.
  - > find error b/w actual o/p and desired o/p and use this error to adjust weights
- credit assignment problem is a fundamental challenge in ANN, particularly in deep neural networks with multiple layers of interconnected neurons.  
uses backpropagation & reinforcement learning

Properties

### Properties of ANN:-

- i) Non linearity (Can model nonlinear relationship b/w input & output variables)
- ii) Adaptability (used for real time processing & continuous learning)
- iii) Distributed computation (simple processing units works in parallel)
- iv) Generalization (to predictions on new, unseen data)
- v) Robustness (can tolerate noise and errors in input data)
- vi) Scalability (can handle large amount of data / can increase complexity of model)