

## UNIT 2 STATISTICS

1.	The marks obtained by five students in a mathematics test are: 45, 50, 55, 60, and 65. Find the mean (average) marks.																		
2.	<b>Problem:</b> Find the median of the following numbers: 12, 18, 25, 30, and 40.																		
3.	Find the mode of the data set: 3, 7, 7, 9, 12, 7, 15, 18, 9.																		
4.	The ages of five students are: <b>12, 14, 10, 16, 13</b> . Find the <b>range</b> of ages.																		
5.	The marks of five students in a test are: <b>8, 10, 12, 14, 16</b> . Find the <b>variance</b> and <b>standard deviation</b> .																		
6.	<p>A company wants to test if customer satisfaction depends on the type of service received. A random sample of 100 customers is surveyed, and the results are:</p> <table><tr><td></td><td><b>Satisfied</b></td><td><b>Not Satisfied</b></td><td><b>Total</b></td></tr><tr><td><b>Online Service</b></td><td>40</td><td>20</td><td>60</td></tr><tr><td><b>In-Person Service</b></td><td>25</td><td>15</td><td>40</td></tr><tr><td><b>Total</b></td><td>65</td><td>35</td><td>100</td></tr></table> <p>Does customer satisfaction depend on the type of service at a <b>5% significance level</b>? (critical chi-square value = 3.84)</p>		<b>Satisfied</b>	<b>Not Satisfied</b>	<b>Total</b>	<b>Online Service</b>	40	20	60	<b>In-Person Service</b>	25	15	40	<b>Total</b>	65	35	100		
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<b>In-Person Service</b>	25	15	40																
<b>Total</b>	65	35	100																
7.	<p>A researcher wants to determine the correlation between <b>study hours</b> and <b>exam scores</b> of five students. The data is:</p> <table><tr><td><b>Student</b></td><td><b>Study Hours (X)</b></td><td><b>Exam Score (Y)</b></td></tr><tr><td>1</td><td>2</td><td>50</td></tr><tr><td>2</td><td>3</td><td>60</td></tr><tr><td>3</td><td>5</td><td>80</td></tr><tr><td>4</td><td>7</td><td>90</td></tr><tr><td>5</td><td>8</td><td>95</td></tr></table> <p>Calculate the <b>Pearson correlation coefficient (r)</b>.</p>	<b>Student</b>	<b>Study Hours (X)</b>	<b>Exam Score (Y)</b>	1	2	50	2	3	60	3	5	80	4	7	90	5	8	95
<b>Student</b>	<b>Study Hours (X)</b>	<b>Exam Score (Y)</b>																	
1	2	50																	
2	3	60																	
3	5	80																	
4	7	90																	
5	8	95																	
8.	<p>One sample T-test</p> <p>A university claims that the <b>average IQ</b> of its students is <b>110</b>. A researcher collects a sample of <b>10 students</b> and records their IQ scores: 105,108,112,115,107,109,111,113,106,110 105, 108, 112, 115, 107, 109, 111, 113, 106, 110 105,108,112,115,107,109,111,113,106,110</p> <p>Test at a <b>5% significance level</b> whether the university’s claim is valid.</p>																		

9.	<p><b>Independent T-test</b></p> <p>A company wants to test if there is a difference in productivity between employees working <b>remotely</b> and those working <b>in-office</b>. They collect data on <b>weekly tasks completed</b> for 8 employees in each group:</p> <table><tr><th>Remote Workers</th><th>In-Office Workers</th></tr><tr><td>15</td><td>12</td></tr><tr><td>18</td><td>14</td></tr><tr><td>16</td><td>13</td></tr><tr><td>20</td><td>15</td></tr><tr><td>22</td><td>17</td></tr><tr><td>19</td><td>14</td></tr><tr><td>21</td><td>16</td></tr><tr><td>17</td><td>13</td></tr></table> <p>At a <b>5% significance level</b>, determine if there is a significant difference in productivity.</p>	Remote Workers	In-Office Workers	15	12	18	14	16	13	20	15	22	17	19	14	21	16	17	13			
Remote Workers	In-Office Workers																					
15	12																					
18	14																					
16	13																					
20	15																					
22	17																					
19	14																					
21	16																					
17	13																					
10.	<p><b>Paired t-Test</b></p> <p>A fitness coach tests whether a <b>new workout plan</b> improves the <b>number of push-ups</b> a person can do in <b>1 minute</b>. He records the performance of 6 clients <b>before</b> and <b>after</b> training:</p> <table><tr><th>Client</th><th>Before</th><th>After</th></tr><tr><td>1</td><td>20</td><td>25</td></tr><tr><td>2</td><td>18</td><td>22</td></tr><tr><td>3</td><td>15</td><td>19</td></tr><tr><td>4</td><td>22</td><td>27</td></tr><tr><td>5</td><td>19</td><td>23</td></tr><tr><td>6</td><td>16</td><td>21</td></tr></table> <p>Does the workout plan <b>significantly improve push-ups</b> at a <b>5% significance level</b>?</p>	Client	Before	After	1	20	25	2	18	22	3	15	19	4	22	27	5	19	23	6	16	21
Client	Before	After																				
1	20	25																				
2	18	22																				
3	15	19																				
4	22	27																				
5	19	23																				
6	16	21																				
11.	Define Type I and Type II errors in hypothesis testing.																					
12.	How does sample size affect Type I and Type II errors?																					
13.	What is the main difference between a one-tailed and a two-tailed test?																					
14.	What is the need of statistics in data science																					
15.	<p><b>Bayes Theorem</b></p> <p>A certain disease affects <b>1%</b> of a population. A test for the disease is <b>90% accurate for sick people</b> (true positive) and <b>95% accurate for healthy people</b> (true negative). If a person tests positive, what is the probability that they actually have the disease?</p>																					
16.	A spam filter is <b>80% effective</b> in identifying spam emails and <b>99% effective</b> in																					

	identifying non-spam emails. Suppose <b>30%</b> of all received emails are spam. If an email is classified as spam, what is the probability that it actually is spam?
17.	What is hypothesis? Explain types of hypotheses.
18.	Explain five point number summary of box plot
19.	Define: Mean deviation, interquartile range, lower fence (bound), upper fence (bound)
20.	What is skewness? Explain the types of skewness of data.