



ECONOMICS OF POWER GENERATION



-Dr. Pranjal Saxena

(Assistant Professor)

B.Tech, M.Tech, PhD

techinsight08@gmail.com



(The art of determining the per unit (1kWh) cost of production of electrical energy is known as Economics of power generation")



Determining the production cost is very complex



Cost of Land



Staff Salary

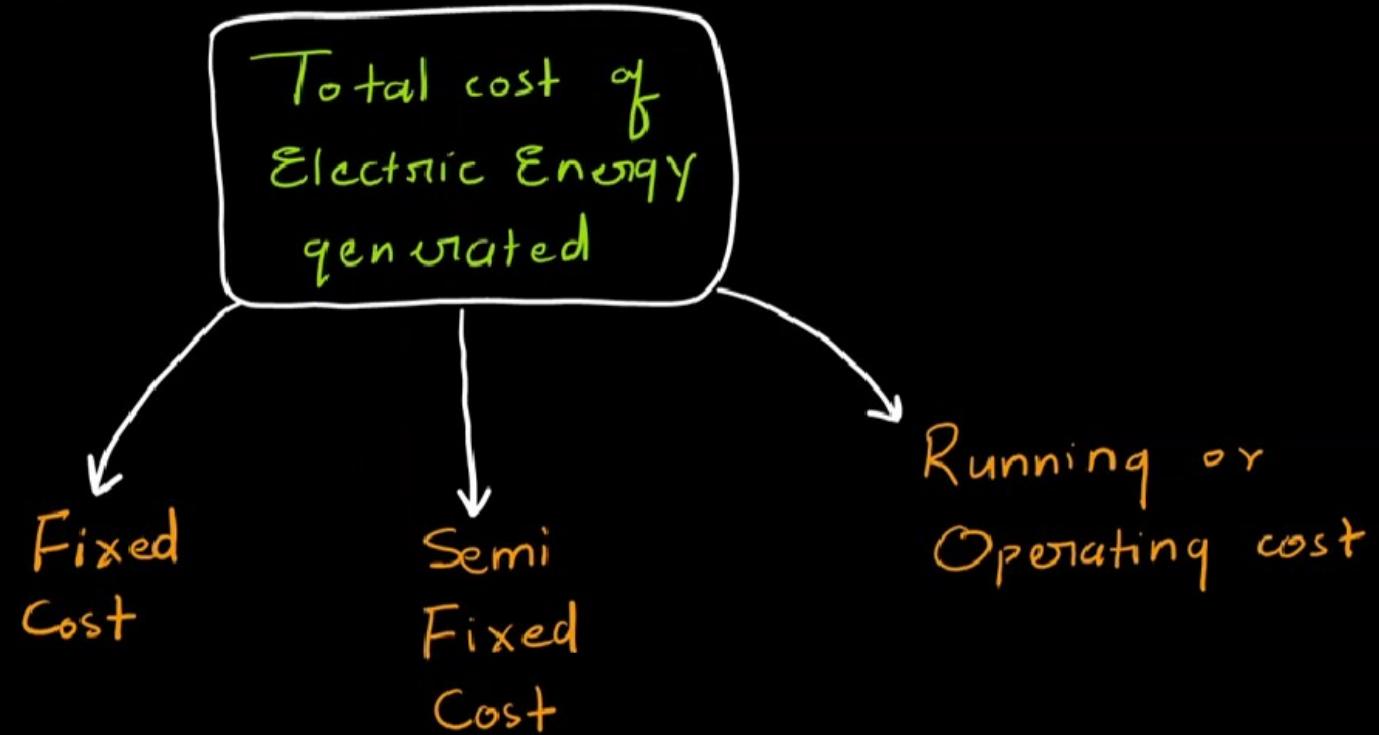


Depreciation Cost



Interest on Capital

Cost estimation



1. Fixed Cost

"Cost which is independent of max^m demand and Units generated"



Annual cost
of organization

Fixed Cost



Salary
vector illustration

High rank official
Salaries



Capital cost of
Land

* Fixed Cost = a \rightarrow constant



2. **Semi-Fixed** Cost

depends on
max^m demand

↳ Variable



Interest
on
Capital

independent of
units generated

* Semi fixed Cost \propto Max^m demand on
Power station

= b. kW



Depreciation
Cost



Management &
Clerical staff



* Higher the max^m demand \longrightarrow Higher the semi-fixed cost

Max demand
on Power
Station

staff \uparrow



Equipment \uparrow



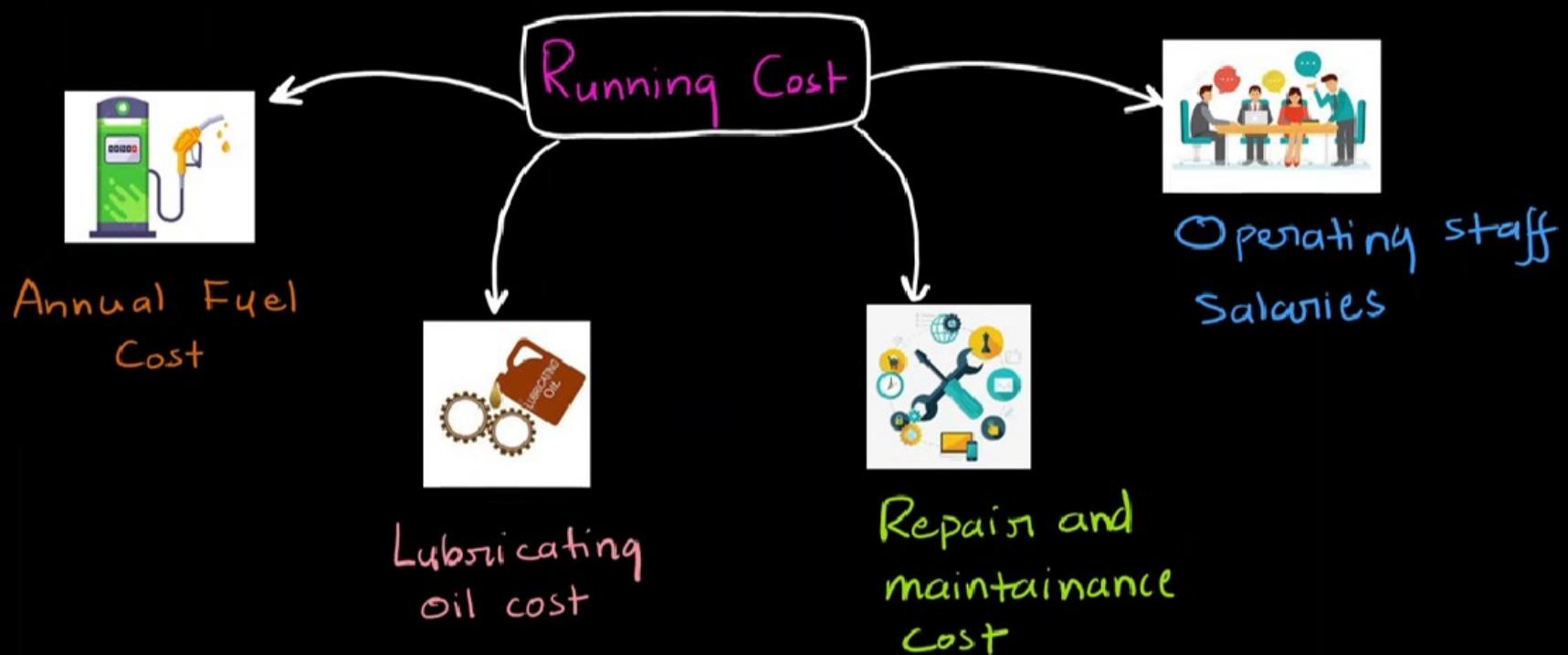
Interest
on
Capital \uparrow

Depreciation
Cost \uparrow



3. Running Cost

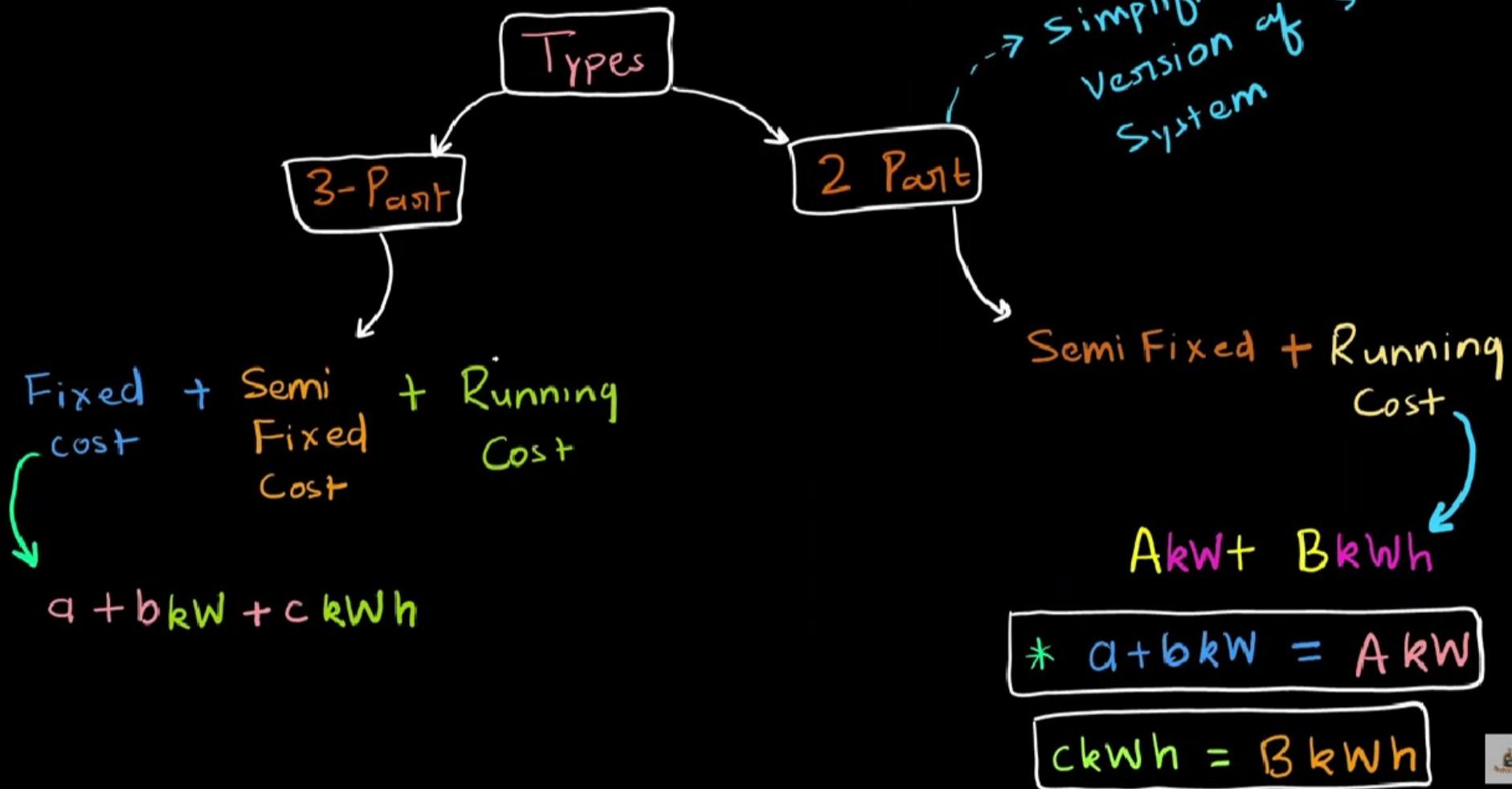
" Depends on number of units generated "

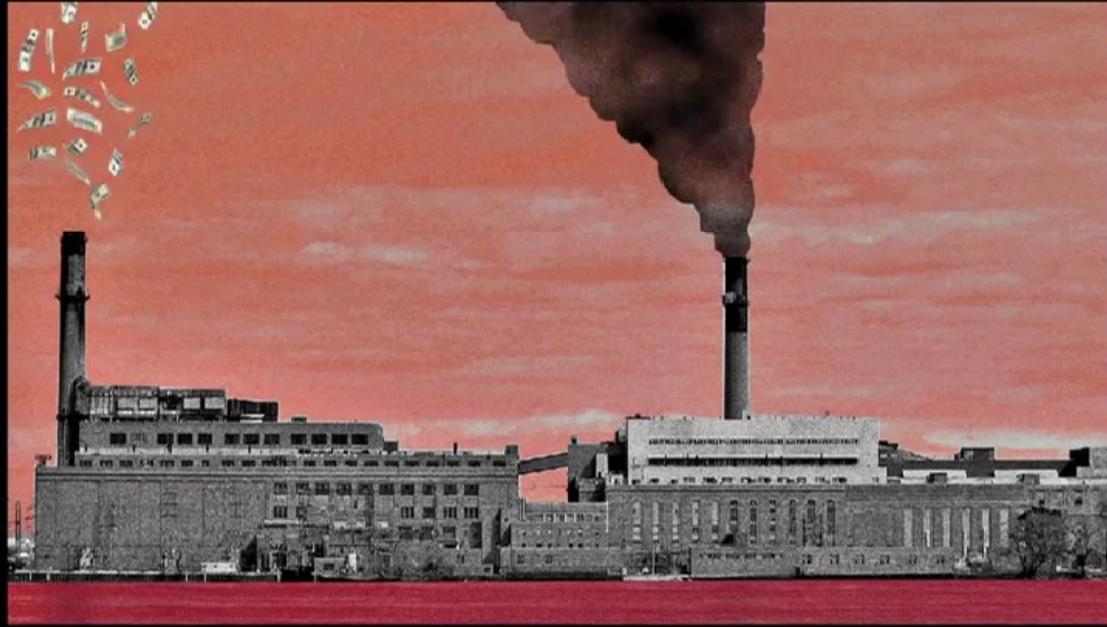
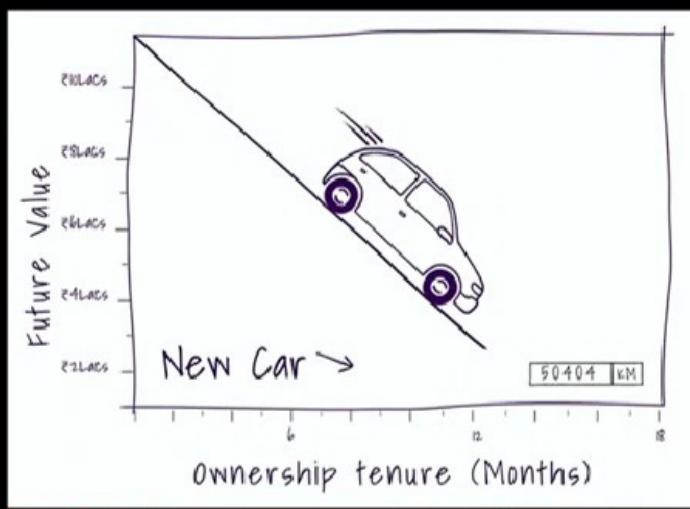


$$* \text{Running Cost} = C \cdot \text{kWh}$$



Expression for cost of Electrical Energy





decrement in value

Depreciation
Cost

DEPRICIATION COST



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10 Lakh → Buy Price

2 Years
useful life



Annual depreciation cost
4 Lakh/year

8 Lakh → Depreciation cost



Depreciation Cost

"The decrease in value of power plant equipment and building due to constant use is known as depreciation Cost"



useful
life

50 to 60
years

}
due to wear and tear,
the equipment of Power
System deteriorates

* Plant has to replace
the depreciated
equipments via new
one

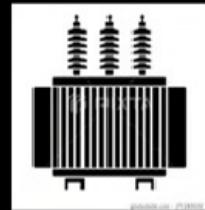


Old
equipment

Buy = 9 Lakh

↓
10 years

1 Lakh



New
equipment

= 9 lakh

↑
8 lakh
more



Depreciation
cost

.....> act as huge economic burden
on utility

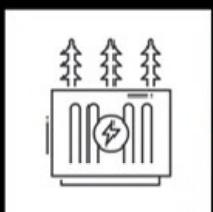


Annual Depreciation charges

"Depreciation charges to be set aside every year to counter the depreciation of equipment")

equals to the cost of replacement of equipment

annual depreciation
charges



Old
equipment

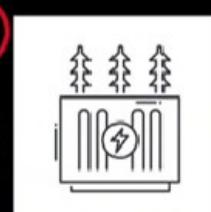
Buy = 9 Lakh

80K 80K 80K - - - - -

10 years

depreciation
charge
collected

80K

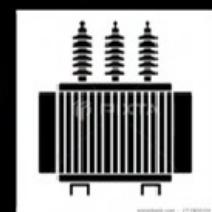


1 Lakh

+

= 8 Lakh

Replace



New
equipment
= 9 lakh

3 Methods

1. Straight line method
2. Diminishing value
3. Sinking fund

1. Straight Line method

constant depreciation
every year

$$* \text{Annual depreciation charge} = \frac{\text{Total depreciation}}{\text{Useful life}} = \frac{\text{Buy Price} - \text{Scrap value}}{\text{Useful life}}$$



Old equipment Annual depreciation charge

$$\text{Buy} = 9 \text{ Lakh}$$

$$= \frac{9 - 1}{10}$$

$$= 0.8 \text{ Lakh}$$

$$\text{or}$$

$$80k$$

Scrap cost
after useful life

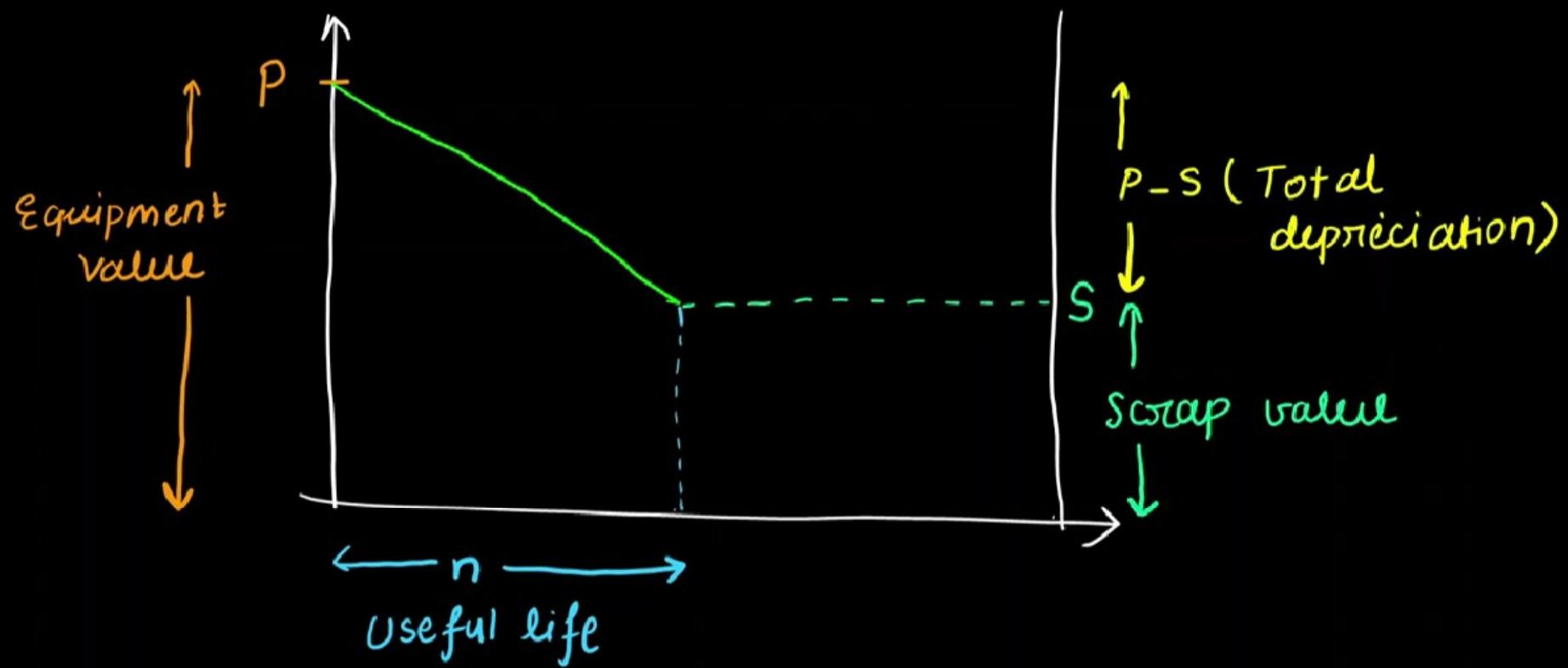
Scrap value

Useful life

equipment available for use

$$\boxed{ADC = \frac{P - S}{n}}$$

Curve



* Curve shows constant depreciation charges

Features

1. Extreme simple method
2. Defects → assumption of constant depreciation every year
 |
 | is not correct
 |
 | → not include interest accumulated



Diminishing Value Method

"Diminishing change is made at a fixed rate on the diminishing value."

e.g.



fixed rate = 10%.

assume that
equipment
depreciated at
fixed rate

Old
equipment

Buy = 9 Lakh	$\xrightarrow{10\%}$	90,000/-	Depreciation charges collected
after 1 year	$\xrightarrow{10\%}$	81,000/-	
8.1 lakh	$\xrightarrow{10\%}$	72,900/-	

Mathematical formulation

- Initial value = P
- useful life = n
- scrap value = S

Annual depreciation unit = x

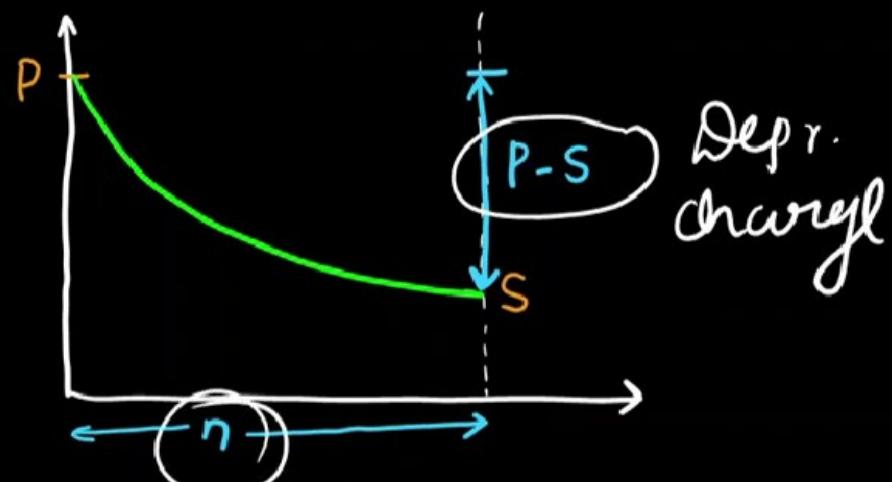
eg 10% depreciation, $x = 0.1$

\therefore value of equipment

after 1 year = $P(1-x)$

after 2 years = $P(1-x)^2$

after n years = $P(1-x)^n$



$$x = 1 - \left(\frac{S}{P}\right)^{1/n}$$

$$S = P(1-x)^n$$

Scrap value

Features

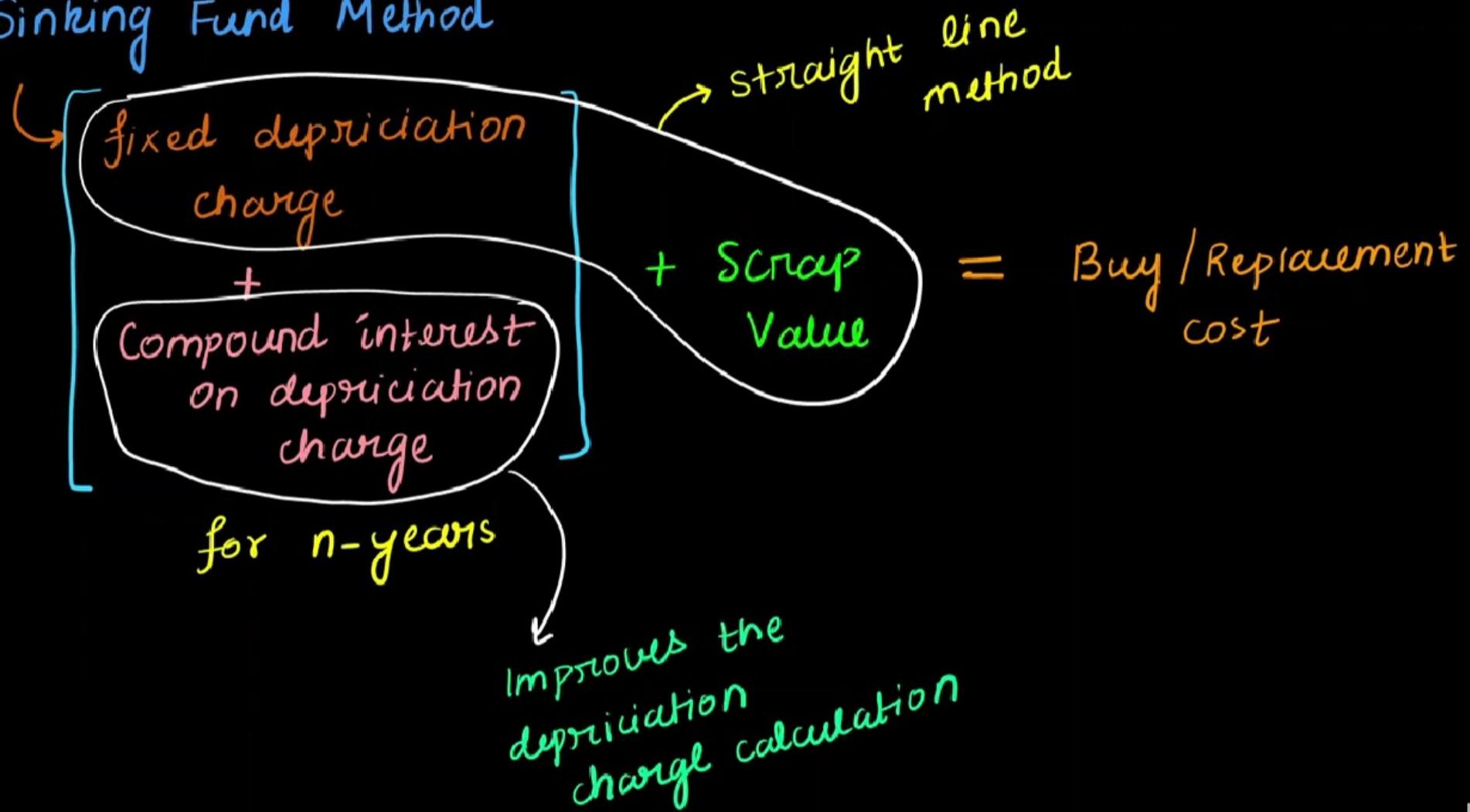
- more rational than straight line method
- curve shows heavy charges in initial years and diminishing charges in later years.

Drawback

- In later years, maintenance and repair ↑ while depreciation charges ↓
- Interest on depreciation charges not included

Sinking Fund Method

Sinking Fund Method



Formula

* Total fund collected
in n-years



$(P-S)$

$$= \frac{q((1+\gamma)^n - 1)}{\gamma}$$

fixed annual
depreciation
charge

γ

annual rate of
interest

Sinking
Fund
Factor

K_{FF}

$$\therefore P-S = \frac{q((1+\gamma)^n - 1)}{\gamma}$$

$$q = (P-S) \left[\frac{\gamma}{(1+\gamma)^n - 1} \right]$$

$$q = K_{FF} \cdot (P-S)$$

Important Formulas

1. Annual Depreciation Cost

$$\hookrightarrow \text{straight line method} = \frac{P-S}{n}$$

$$\hookrightarrow \text{Diminishing value} = X\%$$

$$\Rightarrow X = 1 - \left(\frac{S}{P}\right)^{\gamma n}$$

$$\hookrightarrow \text{sinking fund method} \Rightarrow q = (P-S) \left[\frac{\gamma}{(1+\gamma)^n - 1} \right]$$

2. Fund collected after N-years

↳ straight line method = $\frac{P-S}{n} \times N$

↳ Diminishing value = $P [1 - (1-x)^N]$

↳ Sinking fund method = $\frac{q(1+r)^N - 1}{r}$

3. Actual value of equipment after N -years

$$\hookrightarrow P - \underbrace{\{ \text{fund collected in } N \text{ years} \}}$$

$$\hookrightarrow \text{Straight line method} = P - \left[\frac{\text{annual depreciation}}{N} \times N \right]$$

$$\hookrightarrow \text{Diminishing value} = P(1-x)^N$$

$$\hookrightarrow \text{Sinking fund method} = P - \left[\frac{q(1+y)^N - 1}{y} \right]$$

a. Equipment has cost £ 15,60,000/- has a salvage value of 60,000/- at the end of 25 years. Determine annual depreciation cost / fund/unit in

(a) straight line

(b) Diminishing value

$\text{scr} + (\text{fixed}) = \text{Repldn.}$

$$\text{Am} \quad \text{(i) Annual depreciation} = \frac{P-S}{n} = \boxed{60,000}^-$$

$$\text{(ii) annual depreciation unit} \Rightarrow x = 1 - \left(\frac{s}{P}\right)^{\frac{1}{n}} \xrightarrow[15,60,000]{60,000}^{25}$$

$$\text{compound} \quad \text{fixed} + \text{scrapp} = \text{Repldn.} \xrightarrow[0.122 \text{ or } 12.2\%]{15,60,000}$$

$$\text{(iii) annual depreciation fund} \Rightarrow q = (P-S) \left[\frac{r}{(1+r)^n - 1} \right] = \boxed{31,433}^-$$



Design of Power Transmission

Cost Efficient

Economic conductor size

Economic transmission voltage



ECONOMIC CONDUCTOR SIZE



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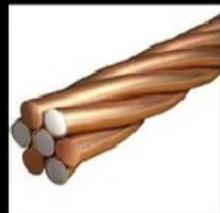
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techinsight08@gmail.com



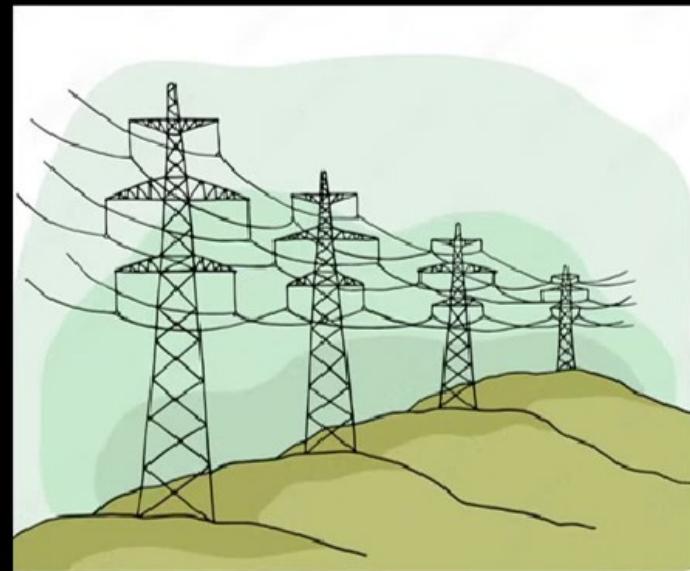
Economic Conductor Size



conductors
cost

→ considerable part
of total transmission
cost

Area should be
economical



Kelvin's Law: →

Most economical
area of
conductor

→ Total annual
cost of
Transmission line
is Minimum



Total annual cost of Transmission line

C_1

Annual charge
on capital cost of conductor

↳ Interest on capital

cost of conductor

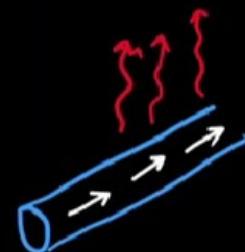
↳ Depreciation on
capital cost of conductor



C_2

cost of energy
wasted in the
conductor

↳ mainly energy lost
due to I^2R losses



$C_1 \propto$ area of conductor (a)

$$= P_1 a$$

$C_2 \propto \frac{1}{\text{area}} (a)$



* Total cost $C_T = C_1 + C_2 = P_1 a + \frac{P_2}{a}$

$$\therefore C_T = P_1 a + \frac{P_2}{a}$$

Most economical area (a) = $\sqrt{\frac{P_2}{P_1}}$

* Its min. value is obtained by ; $\frac{dC_T}{da} = 0 \Rightarrow P_1 - \frac{P_2}{a^2} = 0$

$$= P_1 = P_2/a^2$$

$$P_1 a = \frac{P_2}{a}$$

$$C_1 = C_2$$

"The Kelvin's law states that the most economical size of a conductor is that for which annual interest and depreciation on the capital cost of the conductor is equal to the annual cost of energy loss."

Kelvin's Law

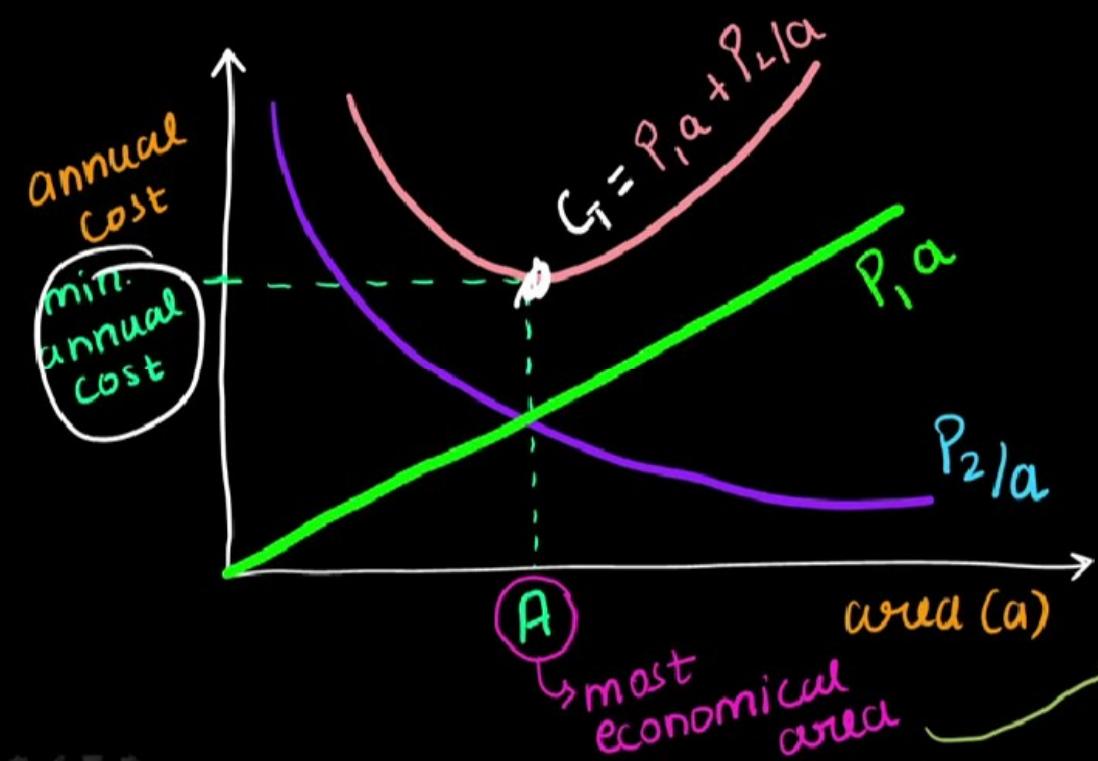
~~Most economical area of conductor~~



Annual interest and depreciation cost of conductor = annual cost of energy wasted

$P_1 a$

P_2/a

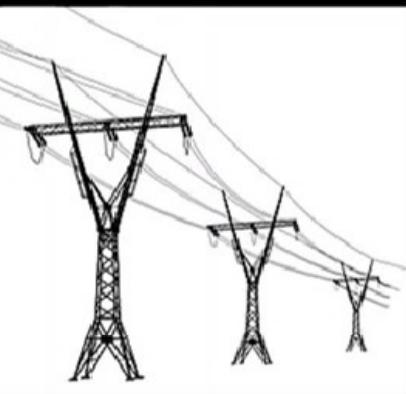


$$P_1 a = P_2/a$$

$$A = \sqrt{\frac{P_2}{P_1}}$$

Erosion

C_1 → Missing



Overhead
Transmission

annual interest and depreciation on capital
cost of conductor

- Insulator cost
- Labour cost
- Support structure cost



Underground
cable

Modified
KELVIN'S
LAW

Gr. Kapp



MODIFIED KELVIN'S LAW



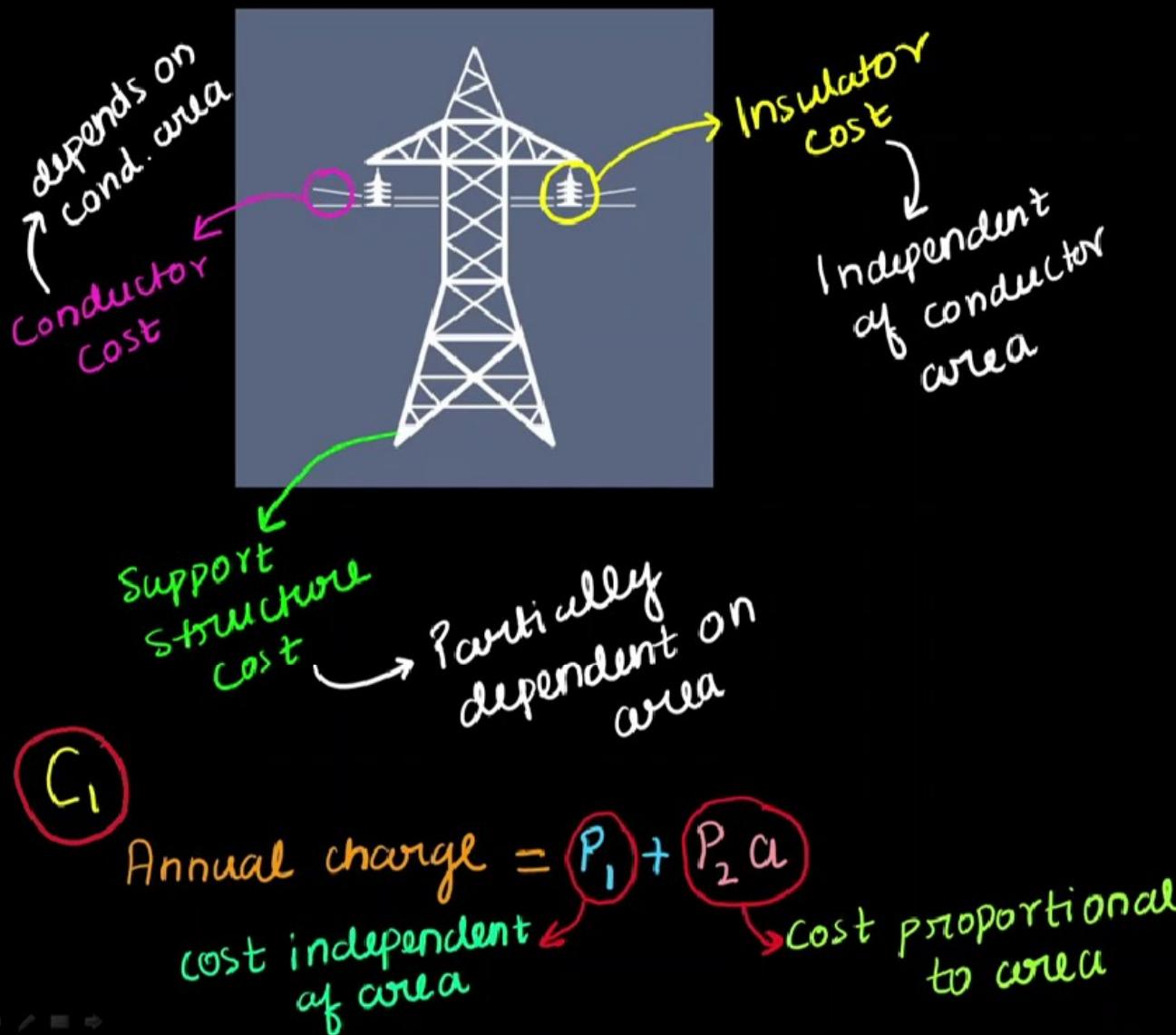
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C₂ Annual cost = $\frac{P_3}{a}$
 cost inversely proportional to area of conductor

Total annual cost

$$C = P_1 + P_2 a + \frac{P_3}{a} \quad \text{--- (1)}$$

* To obtain min. annual capital cost \rightarrow differentiate eq (1) w.r.t area (a)

$$P_2 a = \frac{P_3}{a}$$

variable
part of
annual capital
cost

Annual
cost of
energy wasted

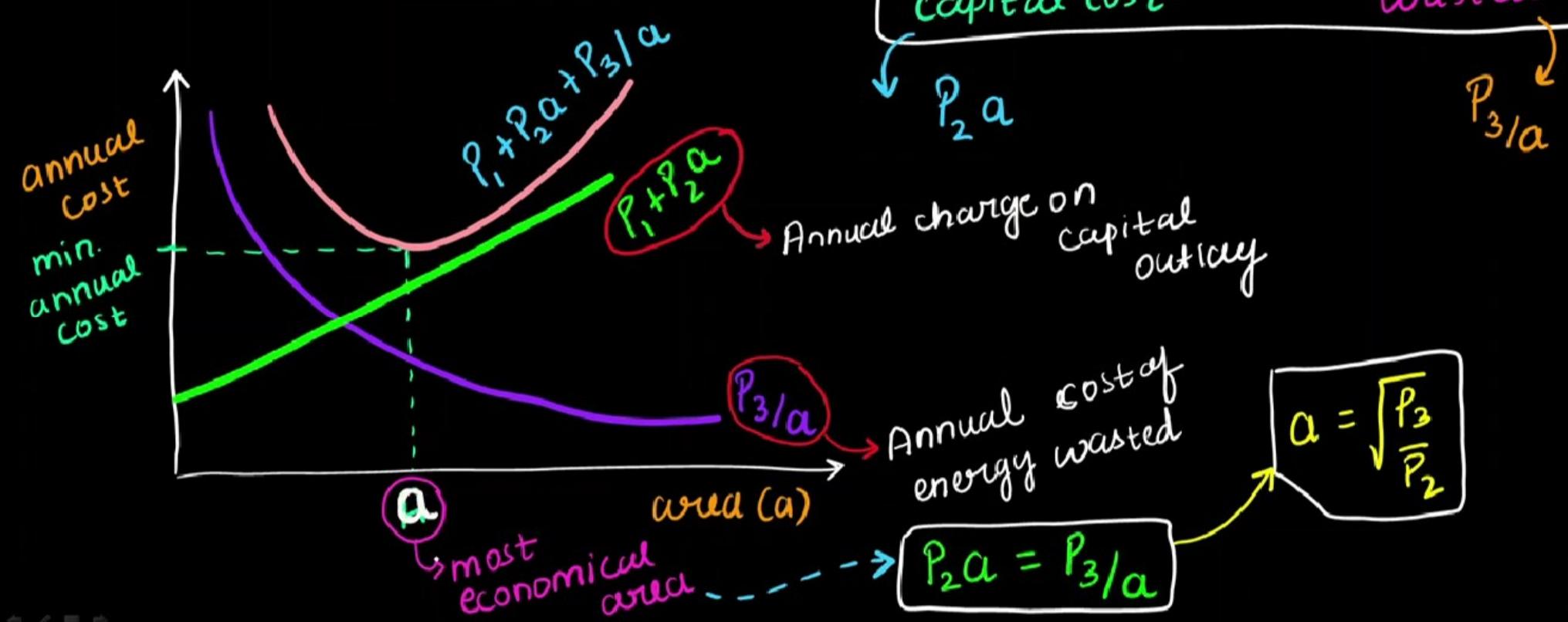
$$\frac{dC}{da}$$

Modified Kelvin's Law

Most economical area of conductor

Variable part
of annual capital cost

= annual cost
of energy wasted



Kelvin's Law

Most economical area of conductor

Annual interest
and depreciation = annual cost
cost of conductor of energy
wasted

Consider only
conductor cost

$$P_1 a = P_2 \frac{a}{\alpha}$$

Modified Kelvin's Law

Most economical area of conductor

Variable part of annual capital cost = annual cost of energy wasted

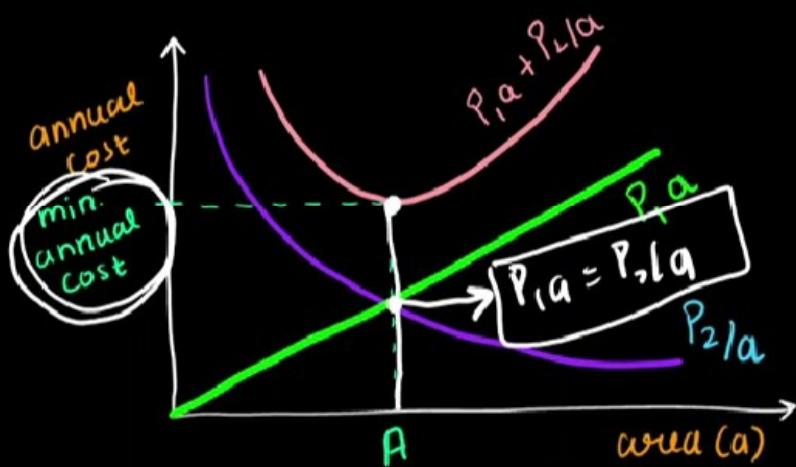
Consider cost of conductor, support, insulator, labour.

$$P_2 a = P_3 \frac{a}{\alpha}$$

Kelvin's Law

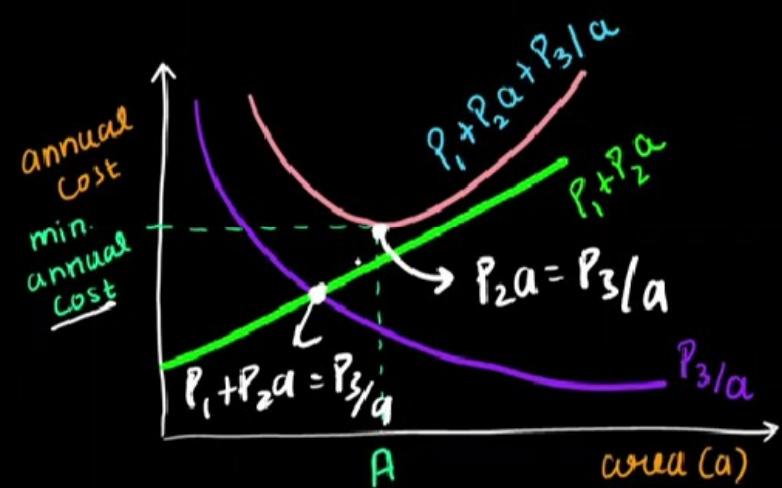
$$P_1 a = P_2/q$$

$$C_T = P_1 a + \frac{P_2}{a}$$



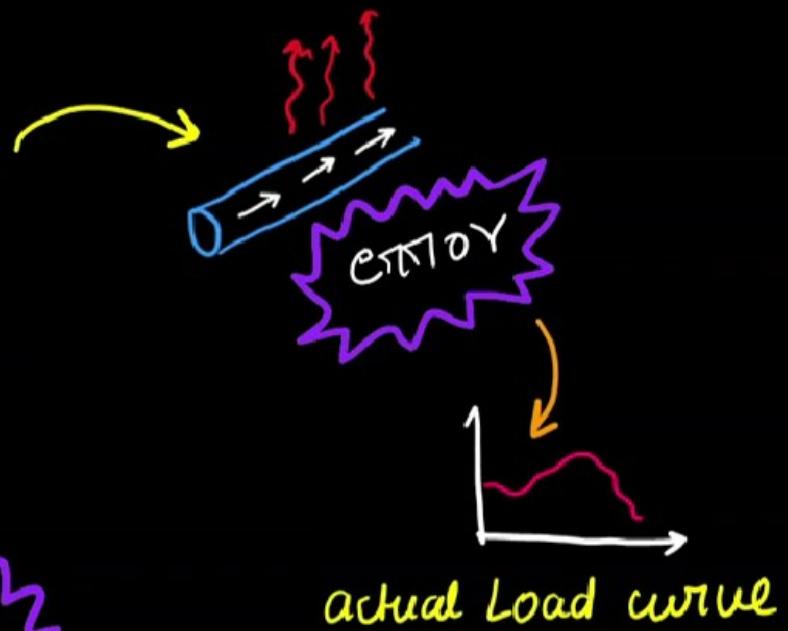
Modified Kelvin's Law

$$C = P_1 + P_2 a + \frac{P_3}{a}$$



Limitation

1. Variable part
of annual capital cost = annual cost
of energy wasted



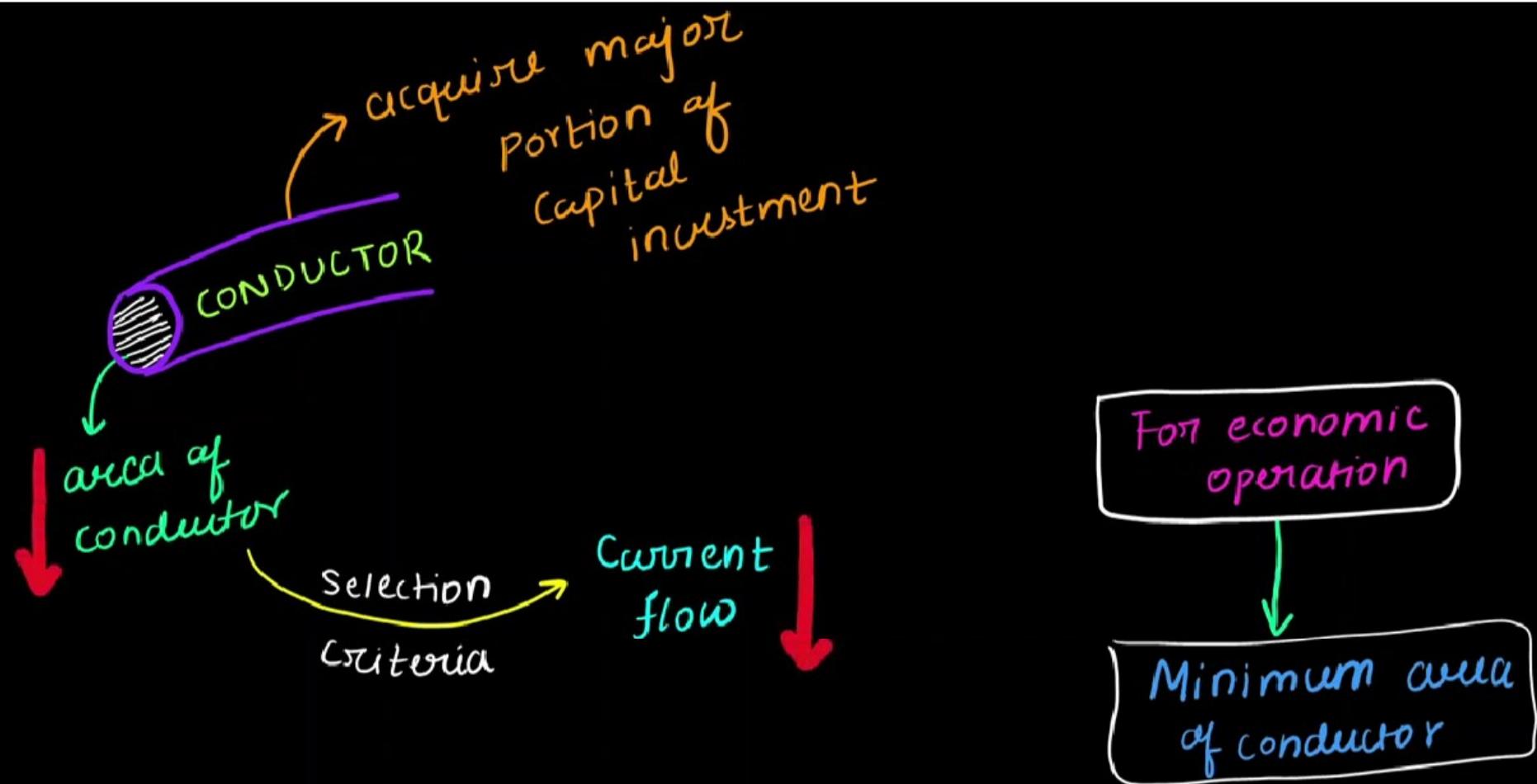
2. Annual capital cost = $P_1 + \alpha P_2$
inaccurate assumption



3. Law ignores: → Corona loss, safety factor

4. economical area of conductor
not practical

→ No mechanical strength

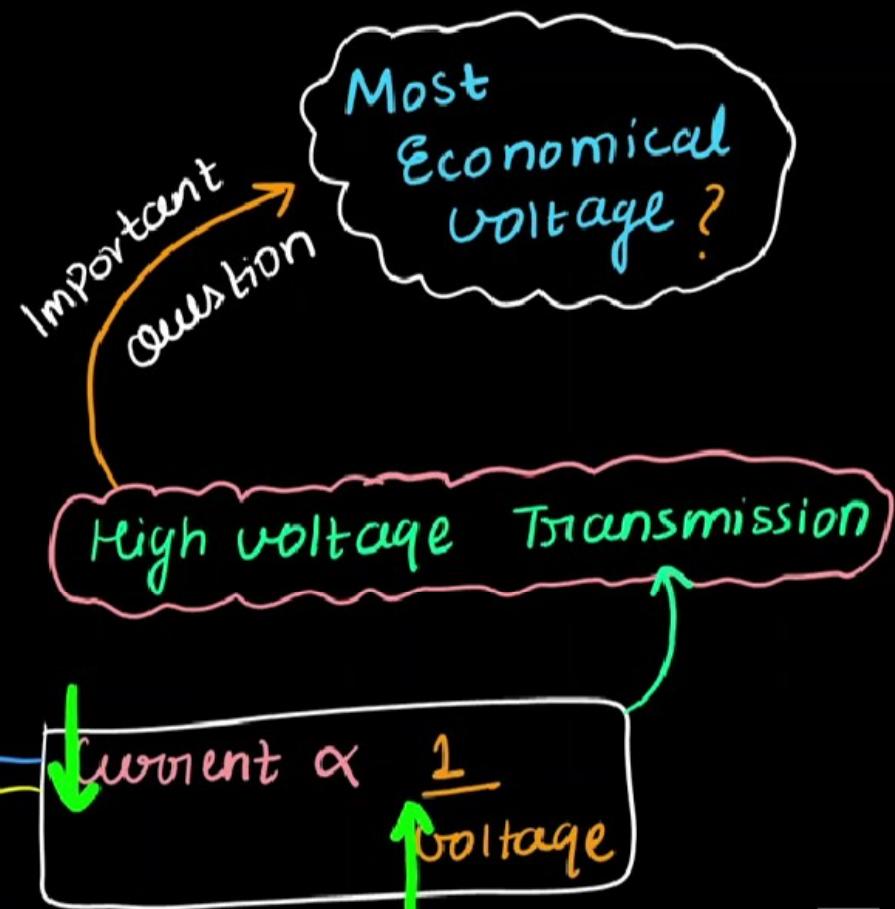




$$S = V I$$

for constant S ;

\downarrow Ohmic losses
 \downarrow conductor required



ECONOMIC TRANSMISSION VOLTAGE



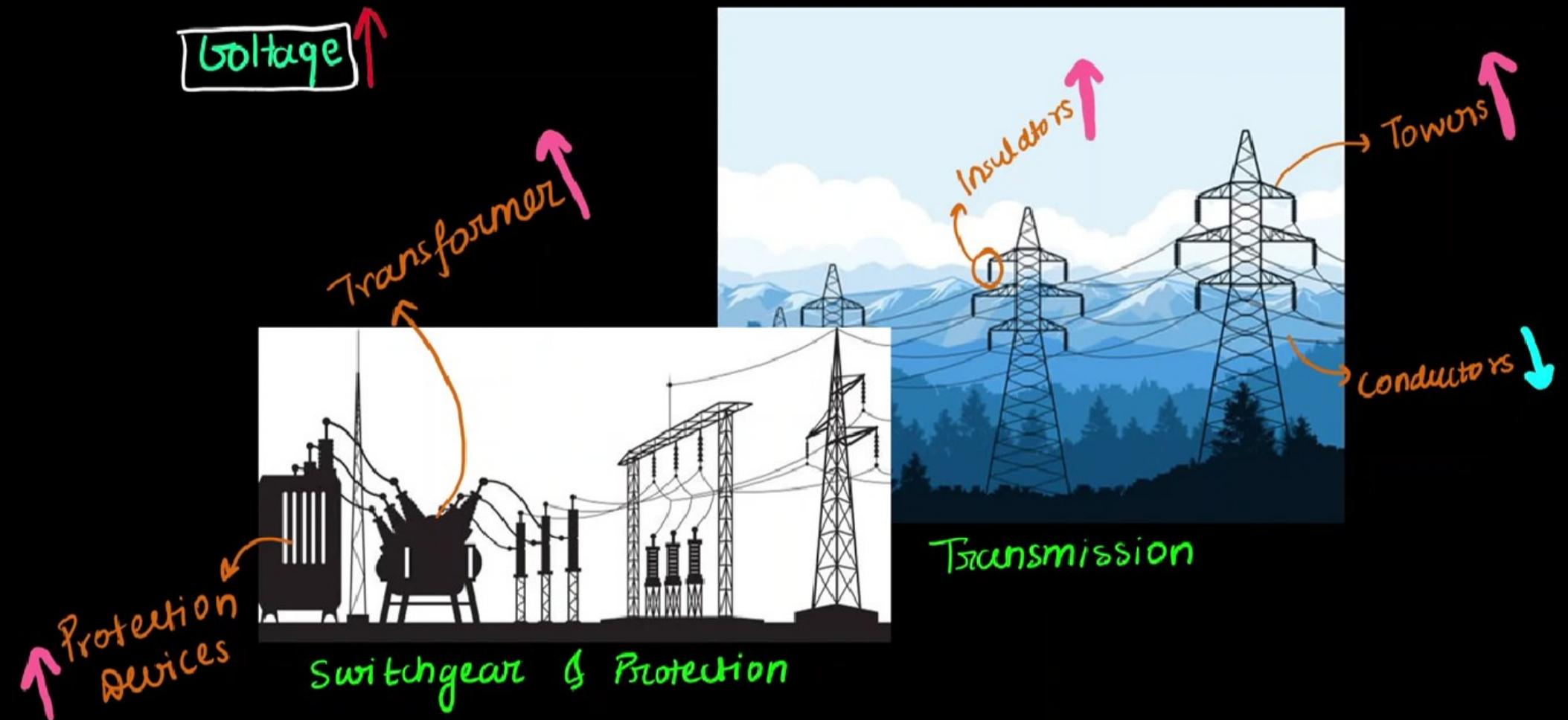
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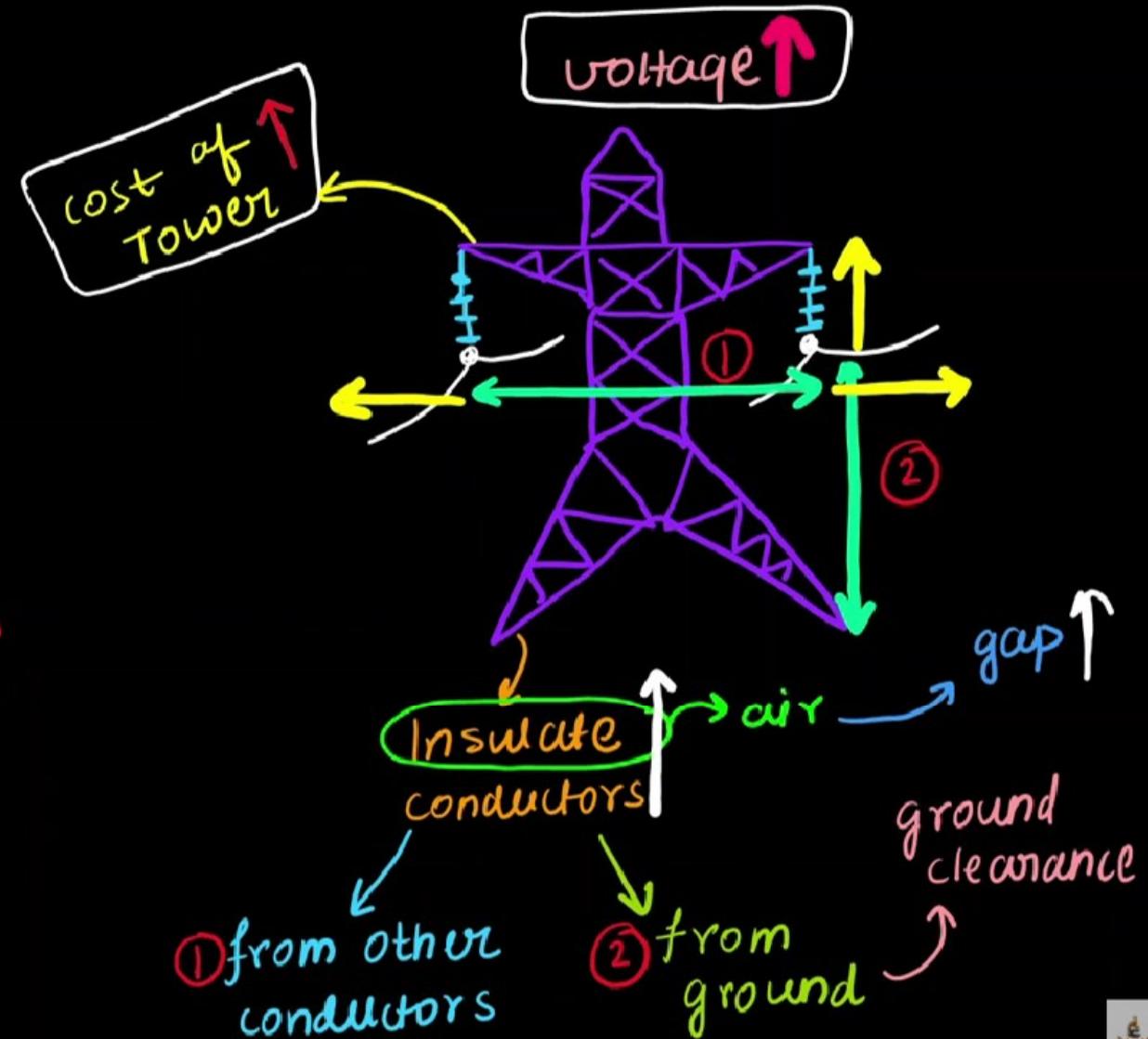




Effect of voltage

Insulators
No. of discs required \propto voltage \uparrow

cost of Insulator \uparrow

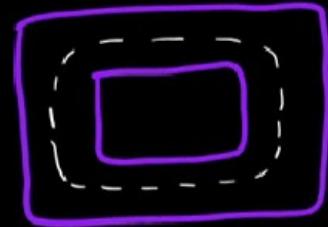




Circuit Breakers

↑ Rating of CB \propto Voltage ↑

(Cost of CB ↑)



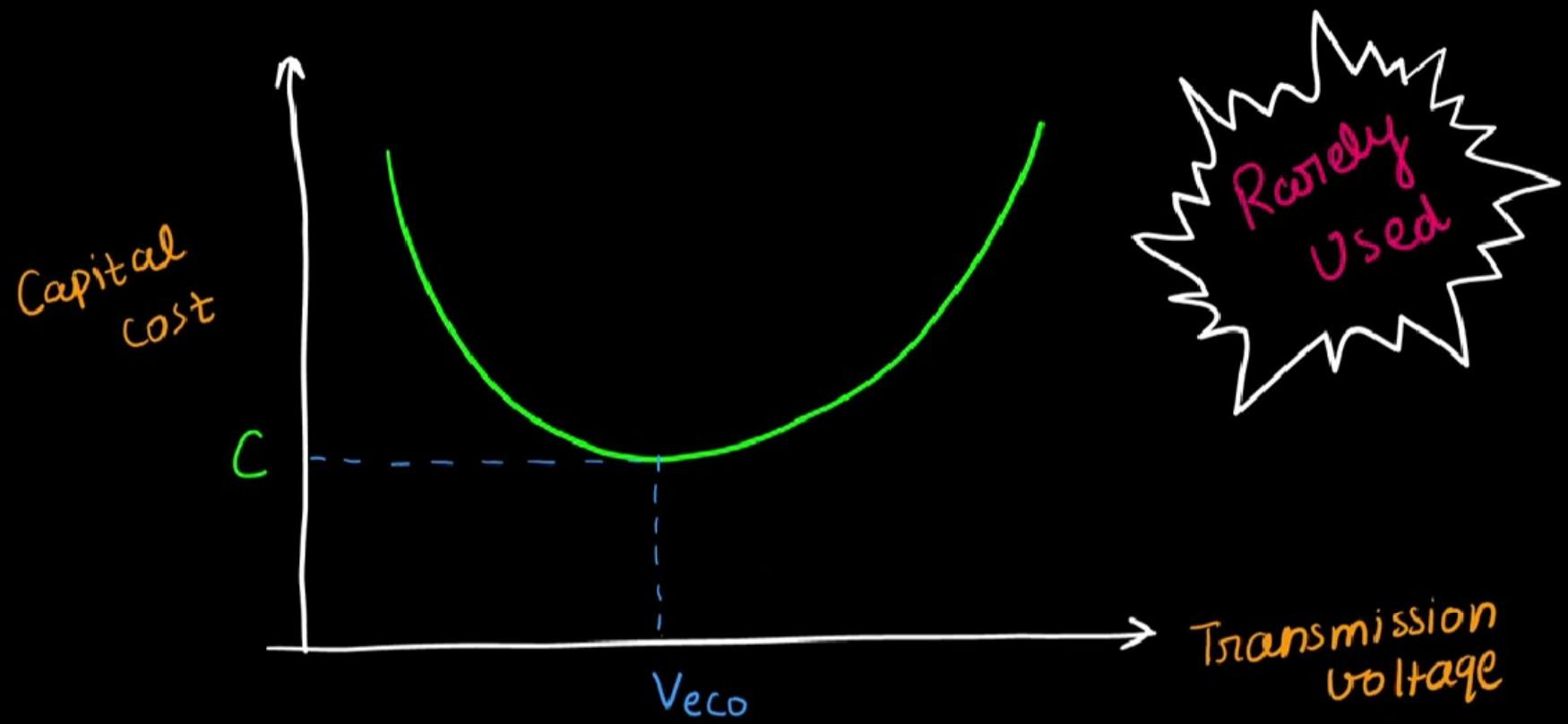
Transformers

flux density > Rated

Lose saturate

V_f ↑
constant
size of Transformer ↑

(Cost of Transformer ↑)



Empirical formula for Economical Voltage

$$V_{eo} = 5.5 \sqrt{0.62(l) + \frac{3P}{150}}$$

These 2 includes all factors

V_{eo} → line voltage
in kV

l → distance of
transmission
line in km

P → max^m kW/phase
to be delivered

