

EE6310: Image and Video Processing Spring 2023

Binary Morphology

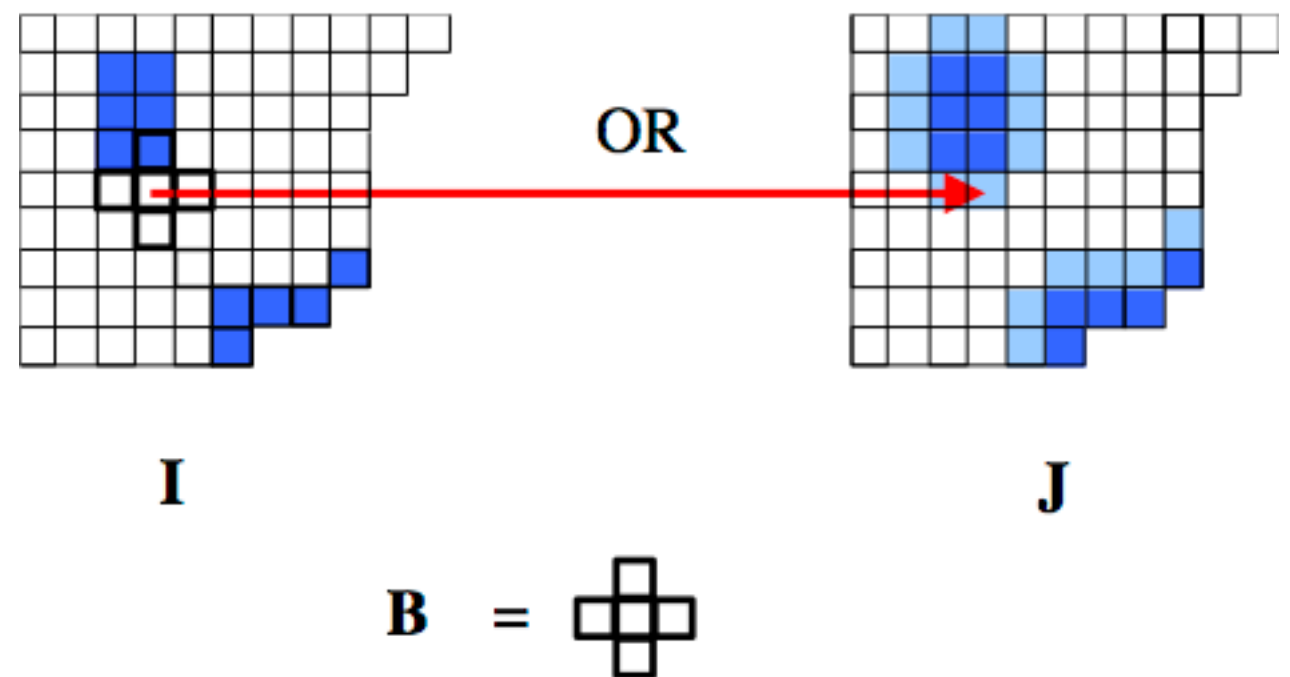


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Binary Morphology

Definition

- Morphology: the study of form and structure
- Mathematical morphology: tool for extracting image components for describing shapes like boundaries, skeletons, convex hulls
- Binary morphology: a class of binary image operators



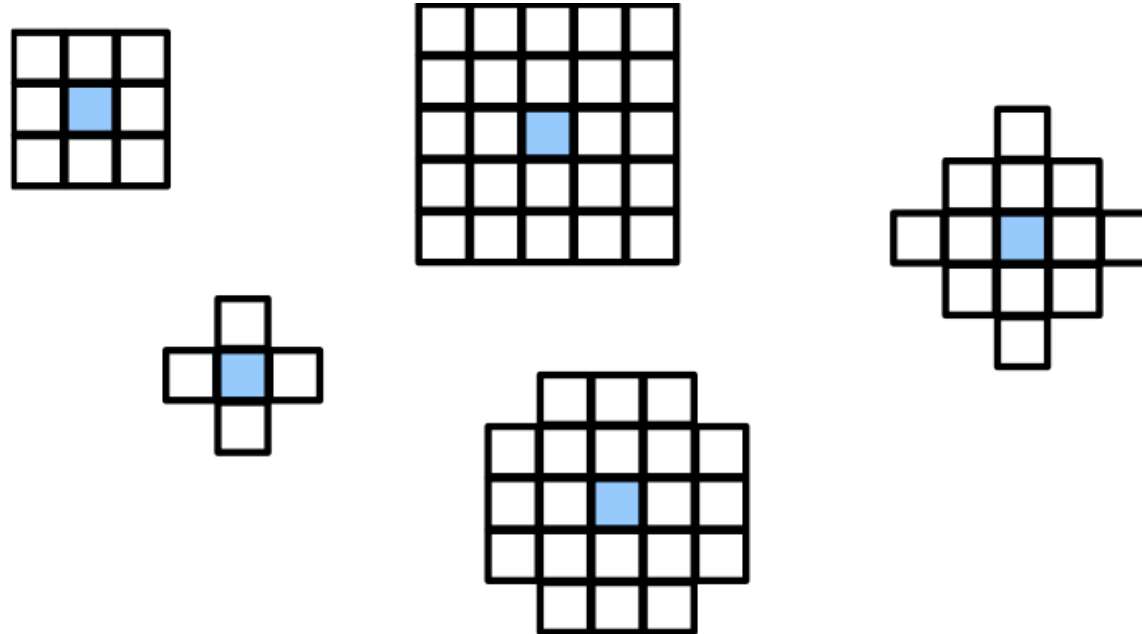
Binary Morphology

Morphological Operations

- Morphological operations:
 - **affect the shape** of objects and regions of binary images
 - operate on a local basis i.e., on **local neighbourhoods**
- Morphological operators:
 - expand or **dilate** objects
 - shrink or **erode** objects
 - smooth object boundaries
 - eliminate holes
 - fill gaps and eliminate convex hulls
 - are logical operations

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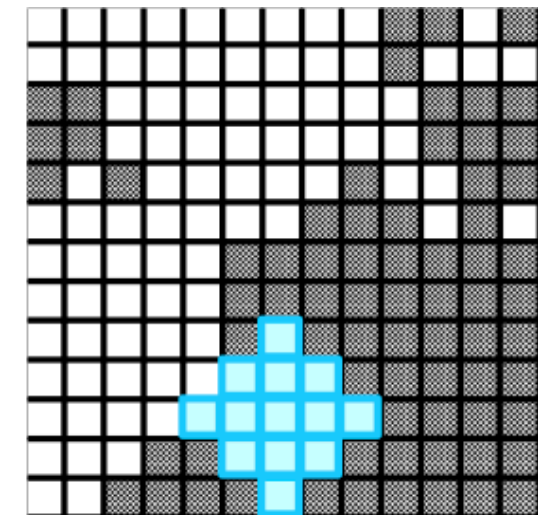
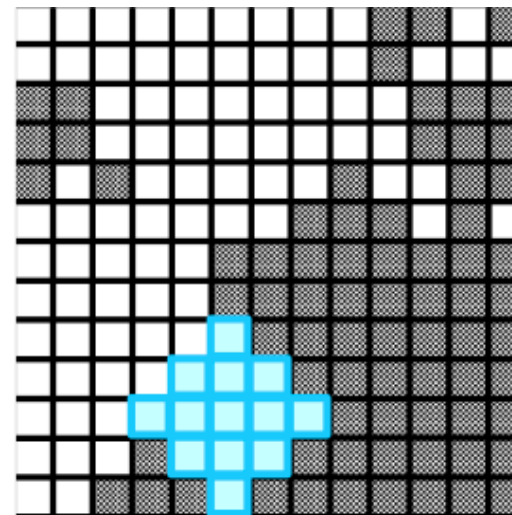
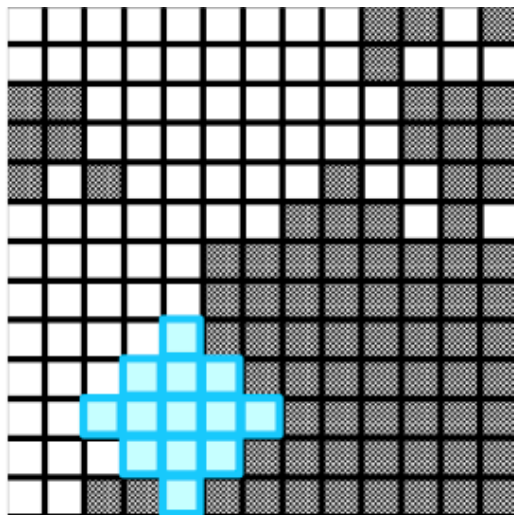
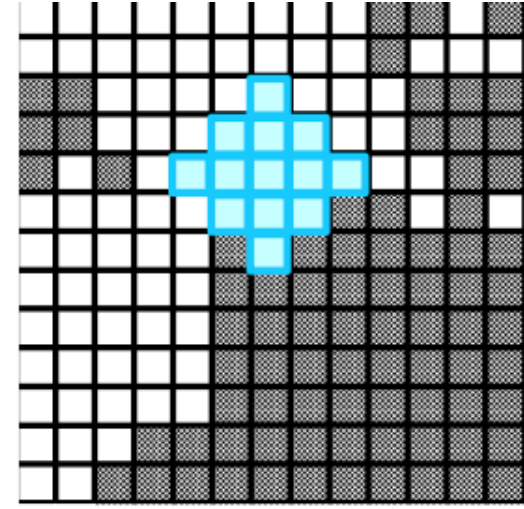
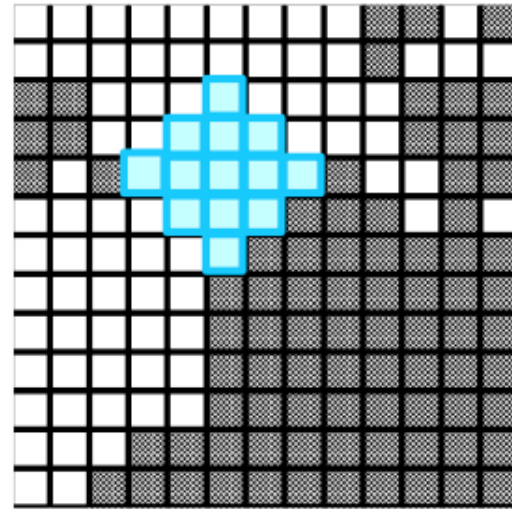
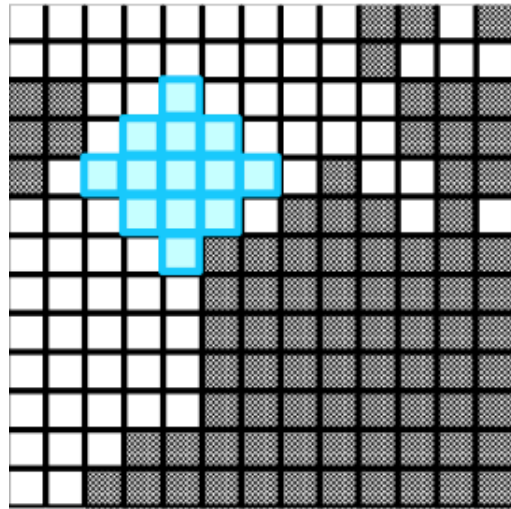
Structuring Element



- Definition: A structuring element defines a relationship between a pixel and its neighbours
- Window:
 - is a method of collecting pixels according to a geometric rule
 - is a structuring element
 - almost always contains an odd number of elements along each dimension - why?

Binary Morphology

Windows



- Using a window to perform local operations over an image

Binary Morphology

Windows

- Definition: A window \mathbf{B} is a set of coordinate shifts $\mathbf{B}_i = (p_i, q_i)$ centred around $(0,0)$ i.e.,
$$\mathbf{B} = \{\mathbf{B}_1, \mathbf{B}_2, \dots, \mathbf{B}_{2P+1}\} = \{(p_1, q_1), (p_2, q_2), \dots, (p_{2P+1}, q_{2P+1})\}$$
- Examples:
 - $\mathbf{B} = \text{ROW}(2P + 1) = \{(0, -P), \dots, (0, P)\}$
 - $\mathbf{B} = \text{COL}(2P + 1) = \{(-P, 0), \dots, (P, 0)\}$
 - $\mathbf{B} = \text{CROSS}(2P + 1) = \text{ROW}(2P + 1) \cup \text{COL}(2P + 1)$

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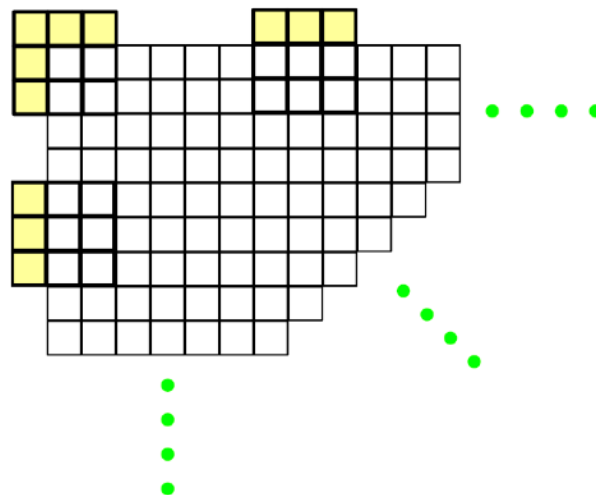
The Windowed Set

- Definition: For a binary image \mathbf{I} and window \mathbf{B} , the **windowed set** at location (i, j) is given defined as
$$\mathbf{B} \diamond \mathbf{I}(i, j) = \{ \mathbf{I}(i - p, j - q); (p, q) \in \mathbf{B} \}$$
- Interpreted as the set of pixels covered by \mathbf{B} centred at (i, j)
- Helps make simple and flexible design of binary filters
- Examples:
 - $\mathbf{B} = \text{ROW}(3); \mathbf{B} \diamond \mathbf{I}(i, j) = \{ \mathbf{I}(i, j - 1), \mathbf{I}(i, j), \mathbf{I}(i, j + 1) \}$
 - $\mathbf{B} = \text{COL}(3); \mathbf{B} \diamond \mathbf{I}(i, j) = \{ \mathbf{I}(i - 1, j), \mathbf{I}(i, j), \mathbf{I}(i + 1, j) \}$

Binary Morphology

General Binary Filter

- Notation: A binary operator \mathbf{G} on a windowed set $\mathbf{B} \diamond \mathbf{I}(i, j)$ is denoted as
$$\mathbf{J}(i, j) = \mathbf{G}\{\mathbf{B} \diamond \mathbf{I}(i, j)\} = \mathbf{G}\{\{\mathbf{I}(i - p, j - q); (p, q) \in \mathbf{B}\}\}$$
- Performing the operation at every pixel gives us the filtered image $\mathbf{J} = \mathbf{G}[\mathbf{I}, \mathbf{B}] = [\mathbf{J}(i, j); 0 \leq i \leq N - 1, 0 \leq j \leq M - 1]$
- How about image boundary?
 - Replication: use nearest neighbors to fill empty slots

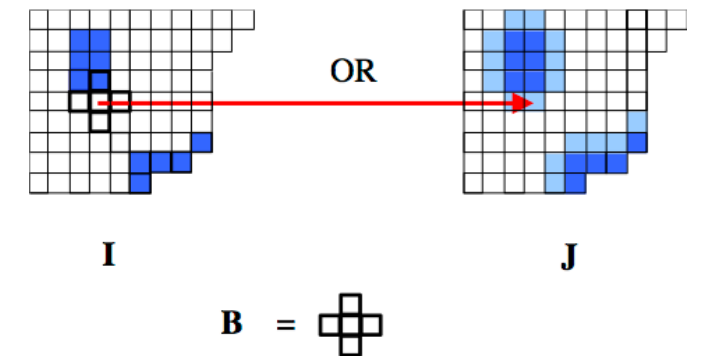


Binary Morphology

Dilation, Erosion and Median Filters

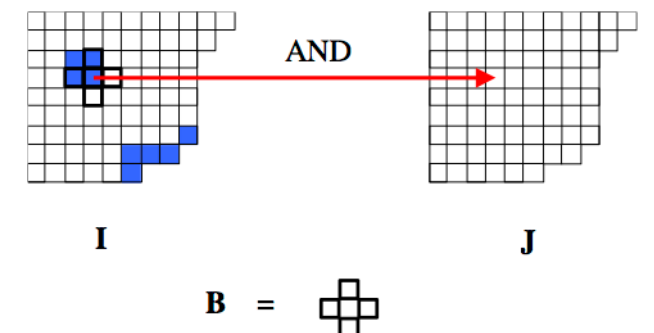
- **Dilation:** Given a window **B** and a binary image **I**,
 $\mathbf{J} = \text{DILATE}(\mathbf{I}, \mathbf{B})$ if

$$\mathbf{J}(i, j) = \text{OR}\{\mathbf{B} \diamond \mathbf{I}(i, j)\} = \text{OR}\{\{\mathbf{I}(i - p, j - q); (p, q) \in \mathbf{B}\}\}$$



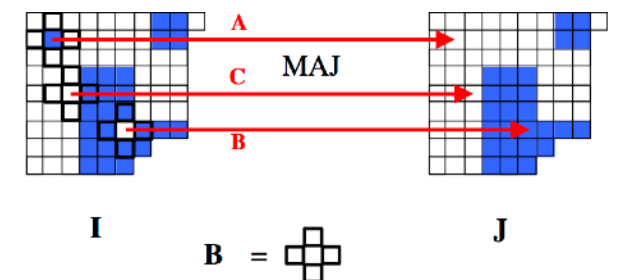
- **Erosion:** Given a window **B** and a binary image **I**,
 $\mathbf{J} = \text{ERODE}(\mathbf{I}, \mathbf{B})$ if

$$\mathbf{J}(i, j) = \text{AND}\{\mathbf{B} \diamond \mathbf{I}(i, j)\} = \text{AND}\{\{\mathbf{I}(i - p, j - q); (p, q) \in \mathbf{B}\}\}$$



- **Median:** Given a window **B** and a binary image **I**,
 $\mathbf{J} = \text{MEDIAN}(\mathbf{I}, \mathbf{B})$ if

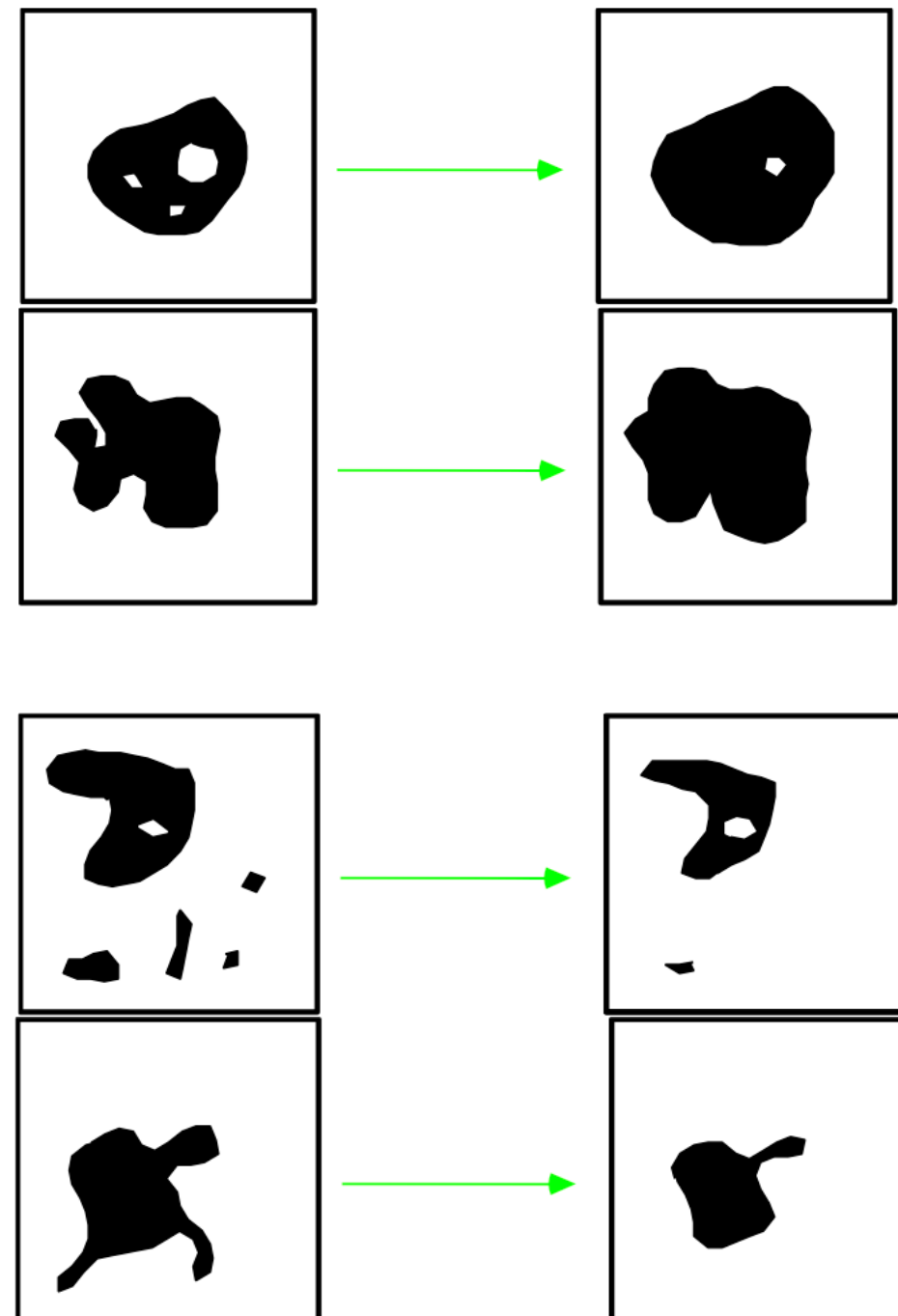
$$\mathbf{J}(i, j) = \text{MAJ}\{\mathbf{B} \diamond \mathbf{I}(i, j)\} = \text{MAJ}\{\{\mathbf{I}(i - p, j - q); (p, q) \in \mathbf{B}\}\}$$



Binary Morphology

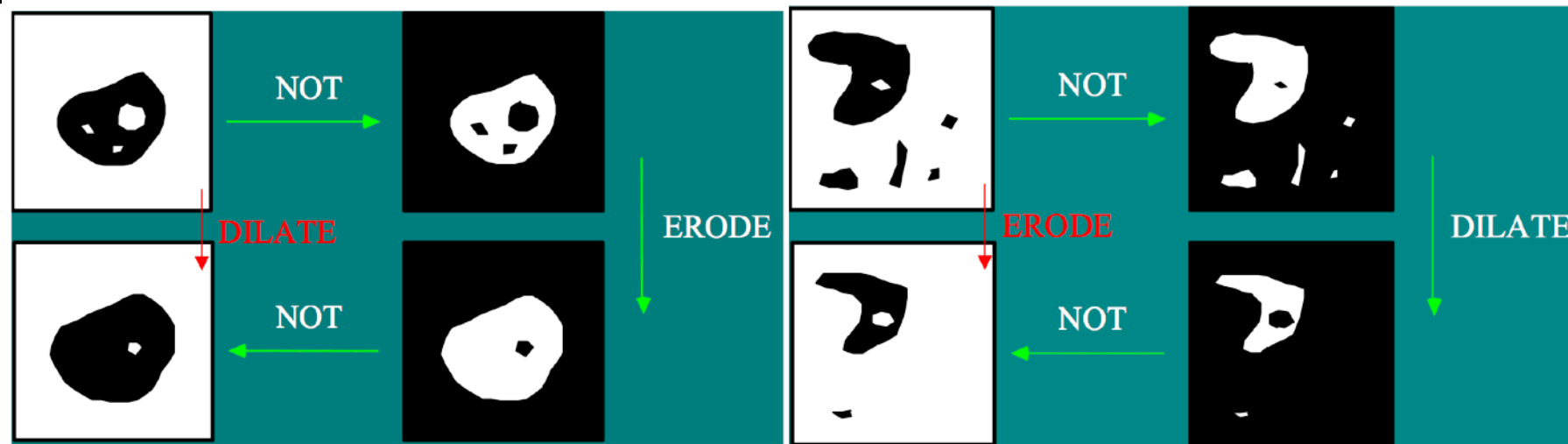
Dilation and Erosion Properties

- Dilation
 - Fills small gaps or holes
 - Fills bays
- Erosion
 - Eliminates small objects
 - Eliminates peninsulas



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Duality Property



- Dilation and Erosion are **duals** with respect to complementation
- Median is its **own dual** with respect to complementation
- Dilation and Erosion are *approximate inverses* of one another
 - Peninsulas *eliminated* by erosion cannot be recreated
 - Small object *eliminated* by erosion cannot be recreated
 - Holes *filled* by dilation cannot be recreated
 - Gaps or bays *filled* by dilation cannot be recreated
- Median filter generally does not change object size (boundary) but alters them

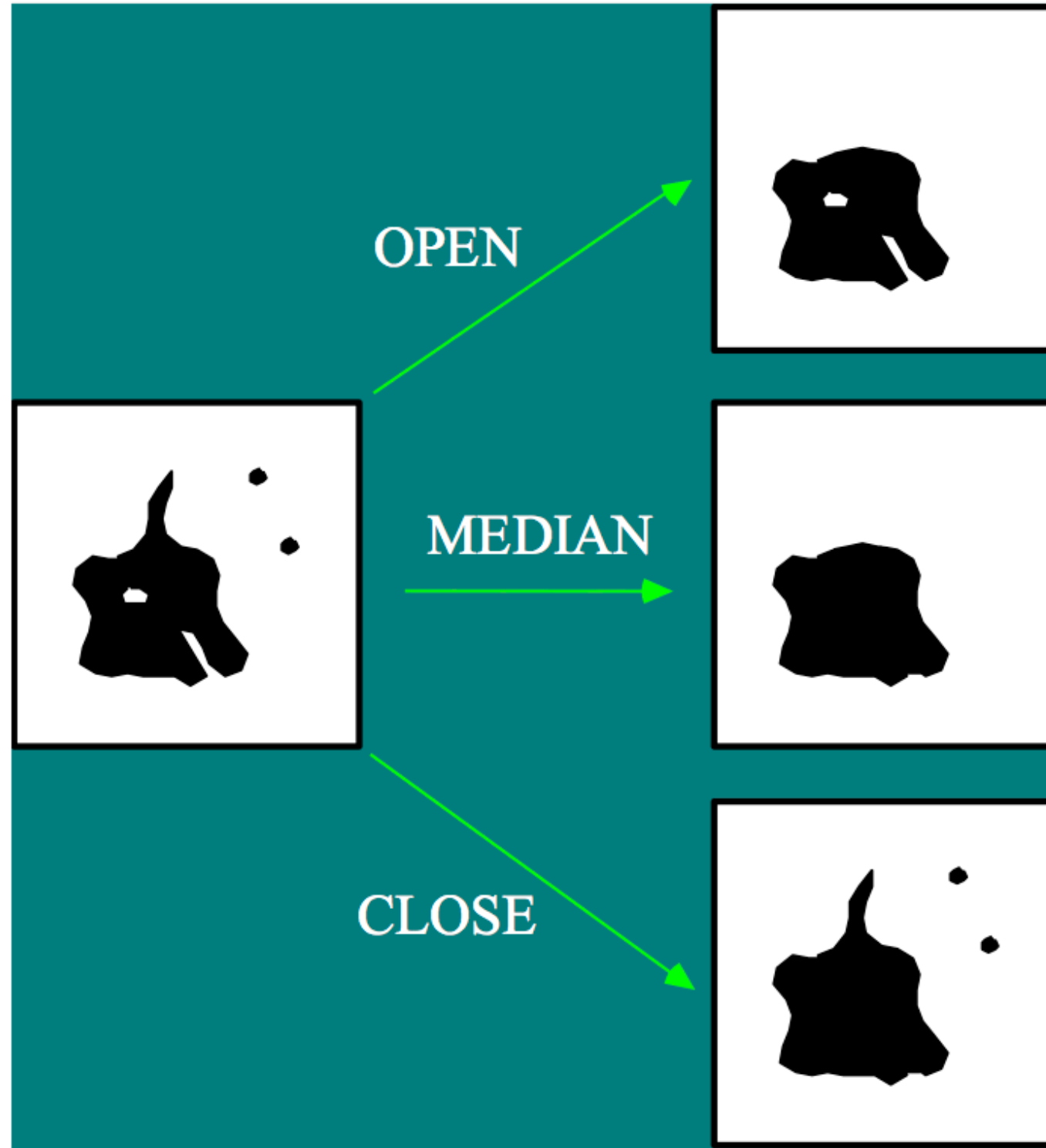
Binary Morphology

OPEN and CLOSE operators

- Definition of new operators by applying basic operators in sequence
- Given a binary image **I** and a window **B**,
 - $\text{OPEN}(\mathbf{I}, \mathbf{B}) = \text{DILATE}[\text{ERODE}(\mathbf{I}, \mathbf{B}), \mathbf{B}]]$
 - $\text{CLOSE}(\mathbf{I}, \mathbf{B}) = \text{ERODE}[\text{DILATE}(\mathbf{I}, \mathbf{B}), \mathbf{B}]]$
- Similar to MEDIAN filter
- OPEN removes small objects better than MEDIAN but not holes, gaps or bays
- CLOSE removes small holes and gaps better than MEDIAN but not small objects
- In general, OPEN and CLOSE do not affect object size

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Comparing OPEN, CLOSE and MEDIAN



Binary Morphology

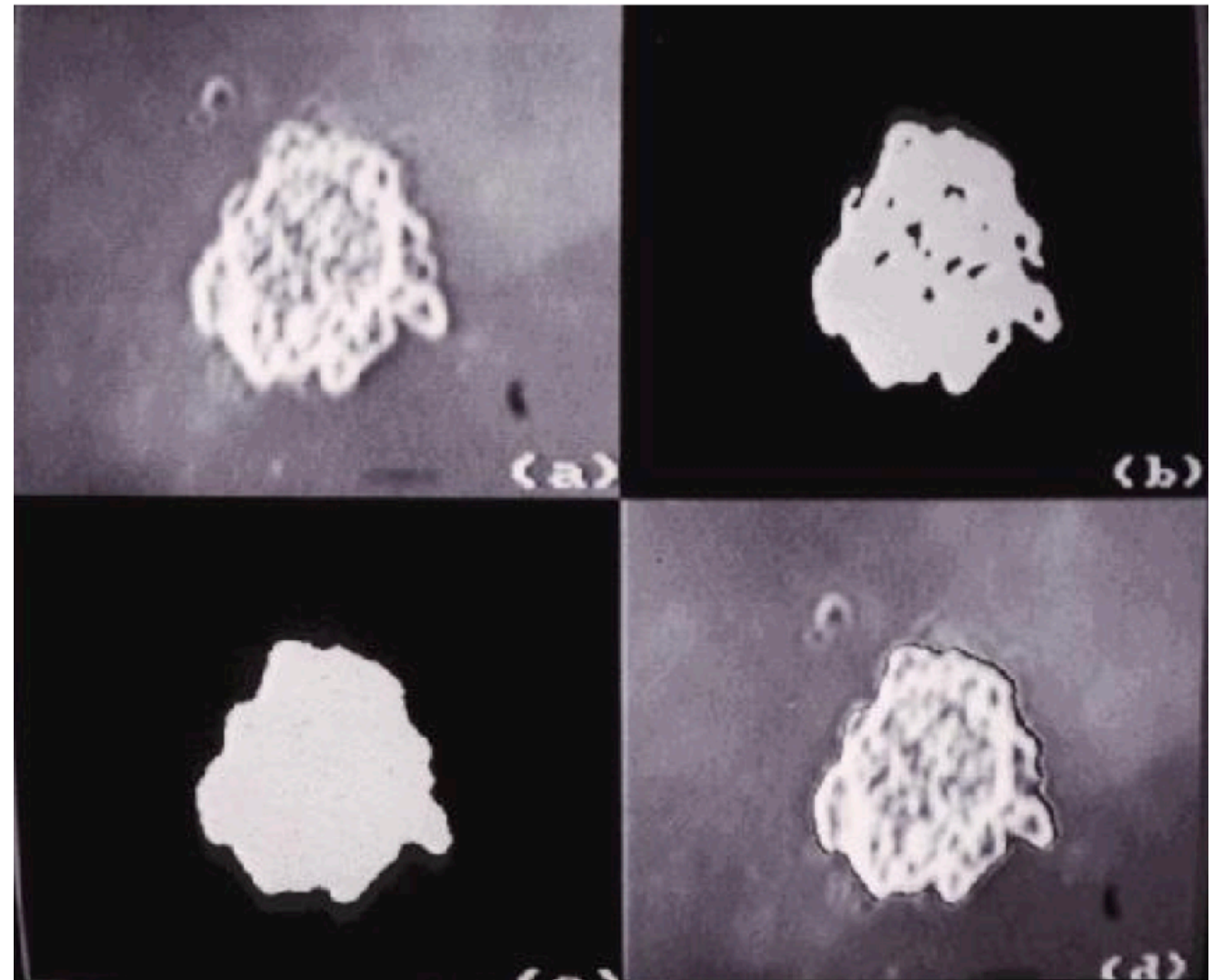
OPEN-CLOS and CLOS-OPEN operators

- Continue to cascade basic operators:
 - $\text{OPEN-CLOS}(\mathbf{I}, \mathbf{B}) = \text{OPEN}[\text{CLOSE}(\mathbf{I}, \mathbf{B}), \mathbf{B}]]$
 - $\text{CLOS-OPEN}(\mathbf{I}, \mathbf{B}) = \text{CLOSE}[\text{OPEN}(\mathbf{I}, \mathbf{B}), \mathbf{B}]]$
- Properties:
 - Good smoothing operators
 - Remove small objects without affecting size
 - Similar to MEDIAN filter but more smoothing
 - OPEN-CLOS tends to link neighboring objects together
 - CLOS-OPEN tends to link neighboring holes together

Binary Morphology

Application

- **Measuring cell area**
- Binarise image using thresholding
- Apply region correction
 - Blob colouring
 - Minor blob removal
 - CLOS-OPEN
- Display result for verifying operator
- Count pixels for cell area calculation
- True cell area computed using perspective projection



Binary Morphology

Summary

- Binary images are a very useful class of gray scale images
- Binary morphology provides techniques for accomplishing several useful tasks