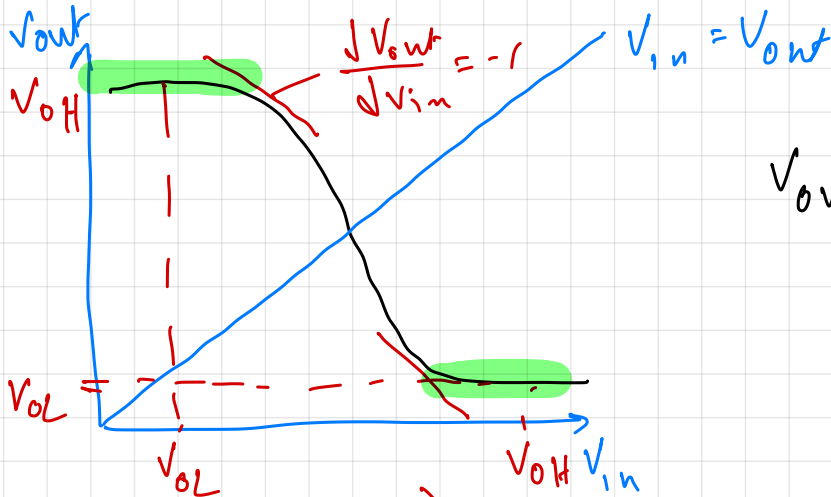


5th Aug 2022

Use the generic $0.25\text{ }\mu\text{m}$ CMOS model below for all your work unless otherwise specified. Assume $|2\phi_F| = 0.6\text{ V}$.

| | V_{T0} (V) | γ ($V^{0.5}$) | V_{DSAT} (V) | k' (A/V^2) | λ (V^{-1}) | R_{eq} ($k\Omega$)@ V_{DD} |
|------|--------------|------------------------|----------------|----------------------|------------------------|----------------------------------|
| NMOS | 0.43 | 0.4 | 0.63 | 115×10^{-6} | 0.06 | 13 |
| PMOS | -0.4 | -0.4 | -1 | -30×10^{-6} | -0.1 | 31 |



$$V_{out} = f(V_{in} + \Delta V)$$

$$= f(V_{in}) + \frac{df}{dV} \Delta V + \dots$$

↙
gain

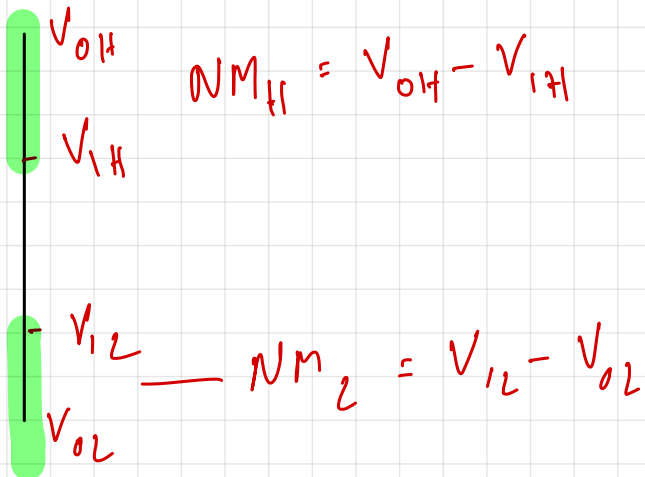
$$V_{out} = f(V_{in})$$

$$V_{OH} = f_{inv}(V_{OL})$$

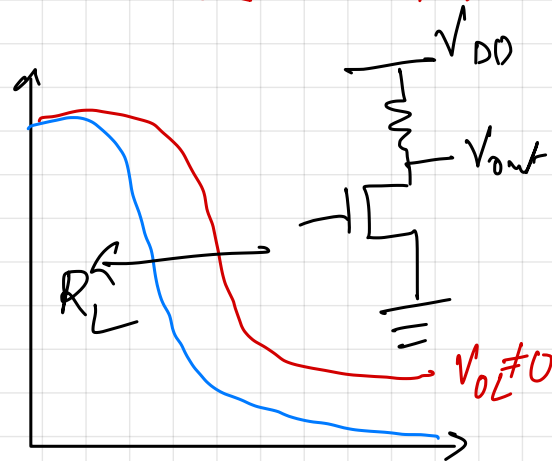
$$V_{OL} = f_{inv}(V_{OH})$$

If gain < -1
Noise is suppressed

gain > 1
Noise is amplified



$$NM_1 = V_{12} - V_{02}$$



$$V_{OL} = \frac{R_{ON}}{R_{ON} + R_L}$$

V_{OL} :
1/1

$$I_R = I_D$$

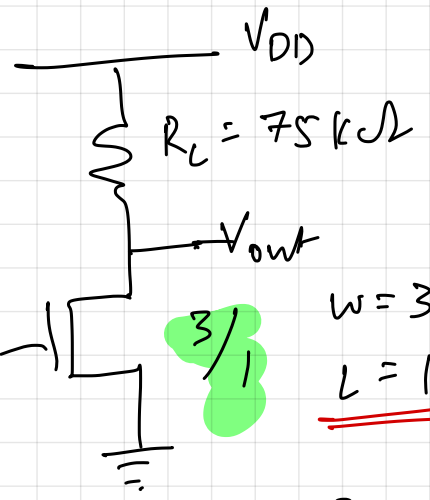
$$\frac{V_{DD} - V_{out}}{R_L} = k'_n \frac{W}{L} \left[\left((V_{GS} - V_T) V_{DS} - \frac{V_{DS}^2}{2} \right) \right]$$

$$V_{GS} - V_T = 2.5 - 0.43$$

$$V_{DS} \sim (V_{GS} - V_T)$$

$$I_D = \frac{1}{2} k'_n \frac{W}{L} (V_{GS} - V_T)^2 (1 + \lambda V_{DS})$$

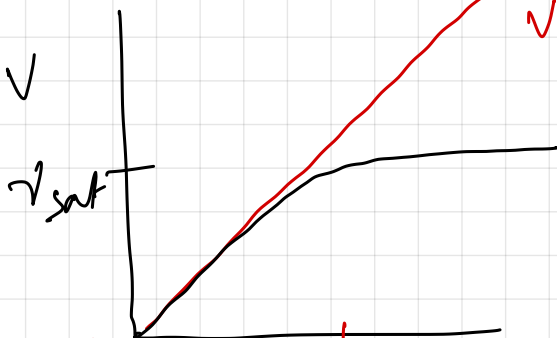
$$\frac{0.75}{0.25}$$



$$\frac{2.5 - V_{OL}}{75 \text{ k}\Omega} = 115 \times 10^{-6} \times 3 \times \left[(2.5 - 0.43) V_{OL} \right]$$

I_D for a short channel transistor

$v = \mu E$ - Electric field between S & D



$$E_c = 10^4 \frac{\text{V}}{\text{cm}}$$

$$I_D = k'_n \frac{W}{L} \left[(V_{GS} - V_T) V_{DSAT} - \frac{V_{DSAT}^2}{2} \right] (1 + \lambda V_{DS})$$

$V_{OL} \sim 50 \text{ mV}$ (Please check)

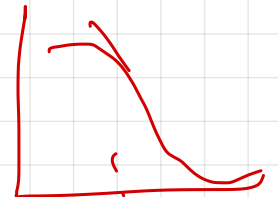
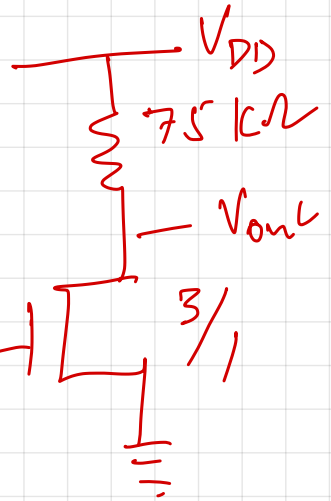
43.1 mV

$$V_M = I_R = I_D$$

$$\frac{V_{DD} - V_M}{R_L} = \frac{1}{2} K_n' \frac{W}{L} (V_{GS} - V_T)^2$$

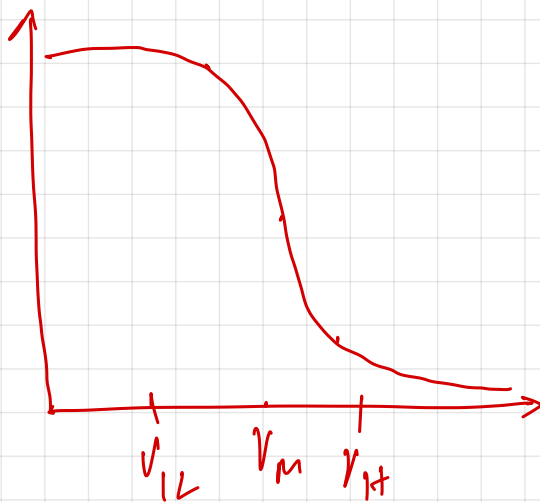
$$\therefore \frac{2.5 - V_M}{75 \text{ k}} = \frac{1}{2} \times 115 \times 10^{-6} \times 3 \times (V_M - 0.43)^2$$

$$= V_M \sim ?$$

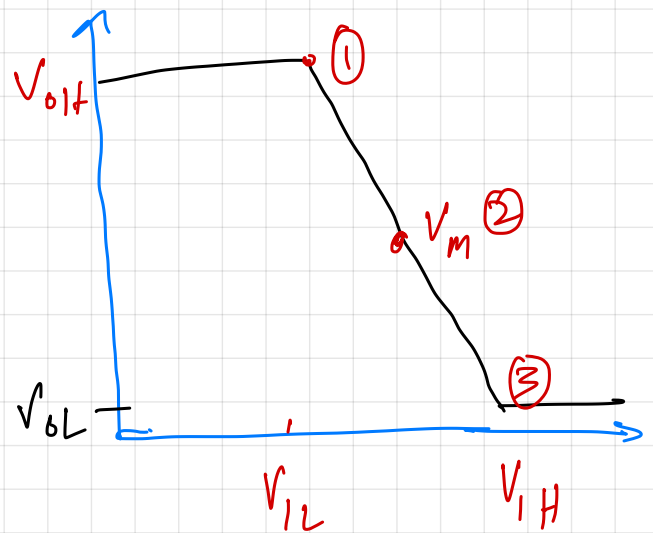


$$V_{IL}: \frac{V_{DD} - V_{out}}{R_L} = \frac{1}{2} K_n' \frac{W}{L} (V_{in} - V_T)^2$$

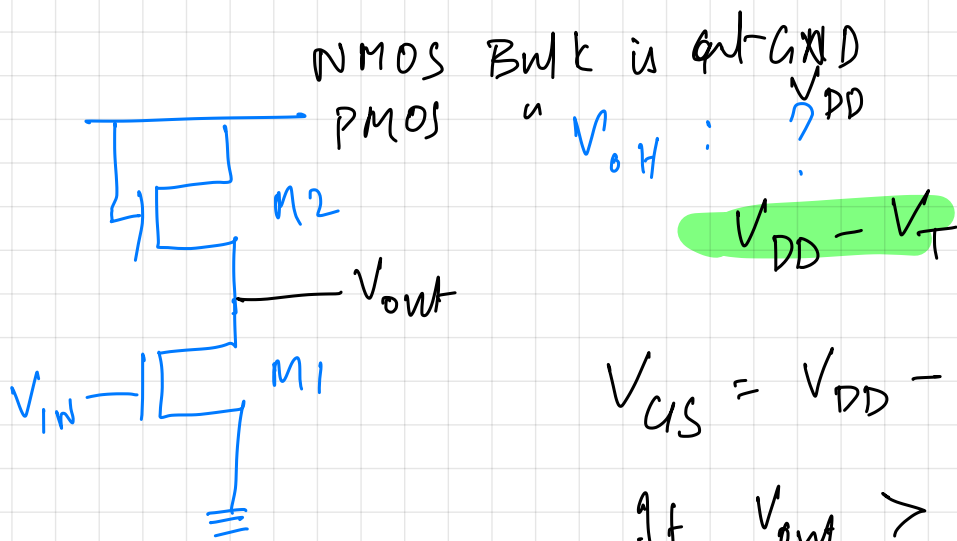
$$-\frac{1}{R_L} \frac{dV_{out}}{dV_{in}} = K_n' \frac{W}{L} (V_{in} - V_T)$$



$$g = \frac{V_{OH} - V_M}{V_{IL} - V_M}$$



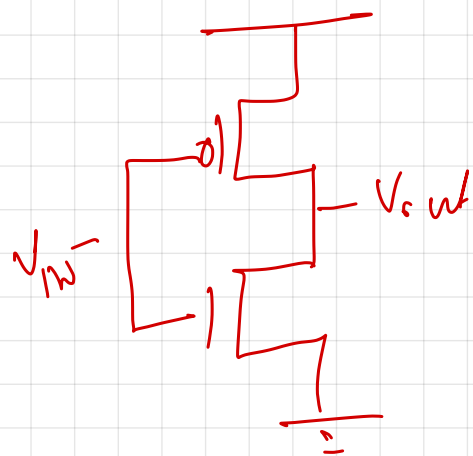
$$g = \frac{V_M - V_{OL}}{V_M - V_{IH}}$$



$$V_{GS} = V_{DD} - V_{out}$$

$$\text{If } V_{out} > V_{DD} - V_{out}$$

$$\text{then } V_{GS} < V_T$$

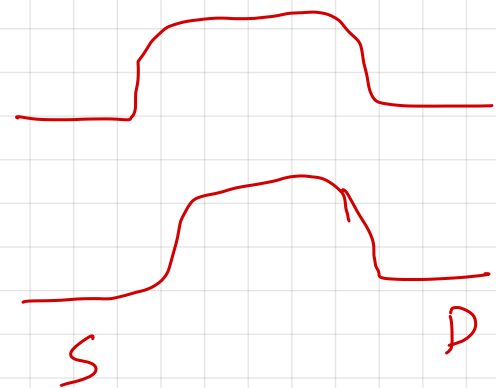
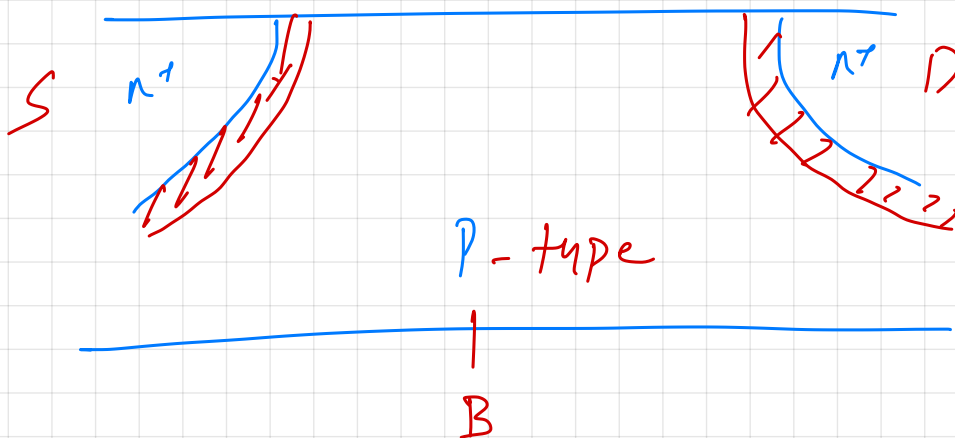


a) $V_T = 0.43V$

(b) $V_T = -0.4V$ X PMOS

(c) It depends

(d) I don't care X



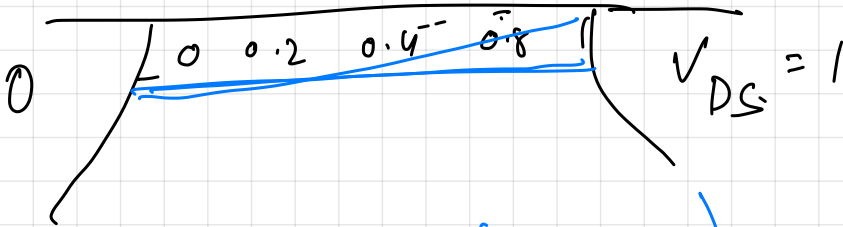
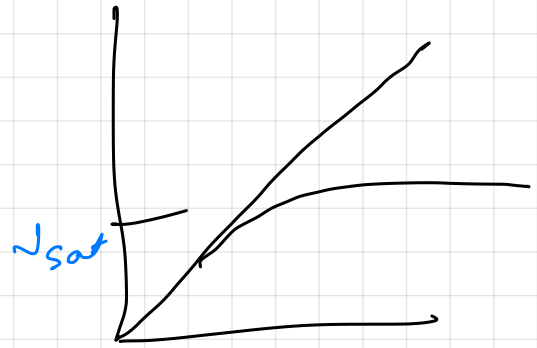
V_{SB} If V_{SB} is negative

$$V_T = V_{T0} + \gamma \left(\sqrt{2\phi_F + V_{SB}} - \sqrt{2\phi_F} \right)$$

$$I_{\text{drift}} = n e \mu \Sigma$$

V_G

$$\frac{V}{L}$$



$$Q_{\text{inv}} = C(V_G - V_C)$$

V_G

$$V_{DS} = 2.5 - 0.43$$

$$0.63 \text{ V}$$

