CS339: Abstractions and Paradigms for Programming

Data Abstraction: Pairs and Lists

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Quiz 1

- > Wednesday, August 20, 8:30-9:15 AM
- > Syllabus: Everything until Tuesday, August 19th
- ➤ Last year's QP would be uploaded, but no guarantee that the pattern would be similar (except that it would be a short exam to test progress)
- ➤ Closed book, closed smart devices (bring ID cards)
- > Seating arrangement to be informed a day before
- ➤ Quiz 2 date also available on the course webpage



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Let's work with "rational" numbers

- > Say we have the following procedures available (wishful thinking):
 - ➤ (make-rat n d), which gives a rational number with numerator n and denominator d
 - > (numer x), which gives the numerator of a rational number x
 - ➤ (denom x), which gives the denominator of a rational number x

- ➤ Now we can play with rational numbers!
- > PC: What would be the problem if we didn't make an explicit rat?



Operations with rational numbers

➤ How do we add two rational numbers x and y?

➤ Print them nicely:

```
(define (print-rat x)
  (newline)
  (display (numer x))
  (display "/")
  (display (denom x)))
```

➤ Multiply them?

Interestingly, we don't yet know how to represent them!



One way to represent rational numbers

➤ Let's check if this works:





But pairing data is quite a popular operation!

> Scheme provides the following special forms to work with *pairs*:

> (cons x y) puts x and y together and returns a pair

> (car x) returns the first element of a pair x

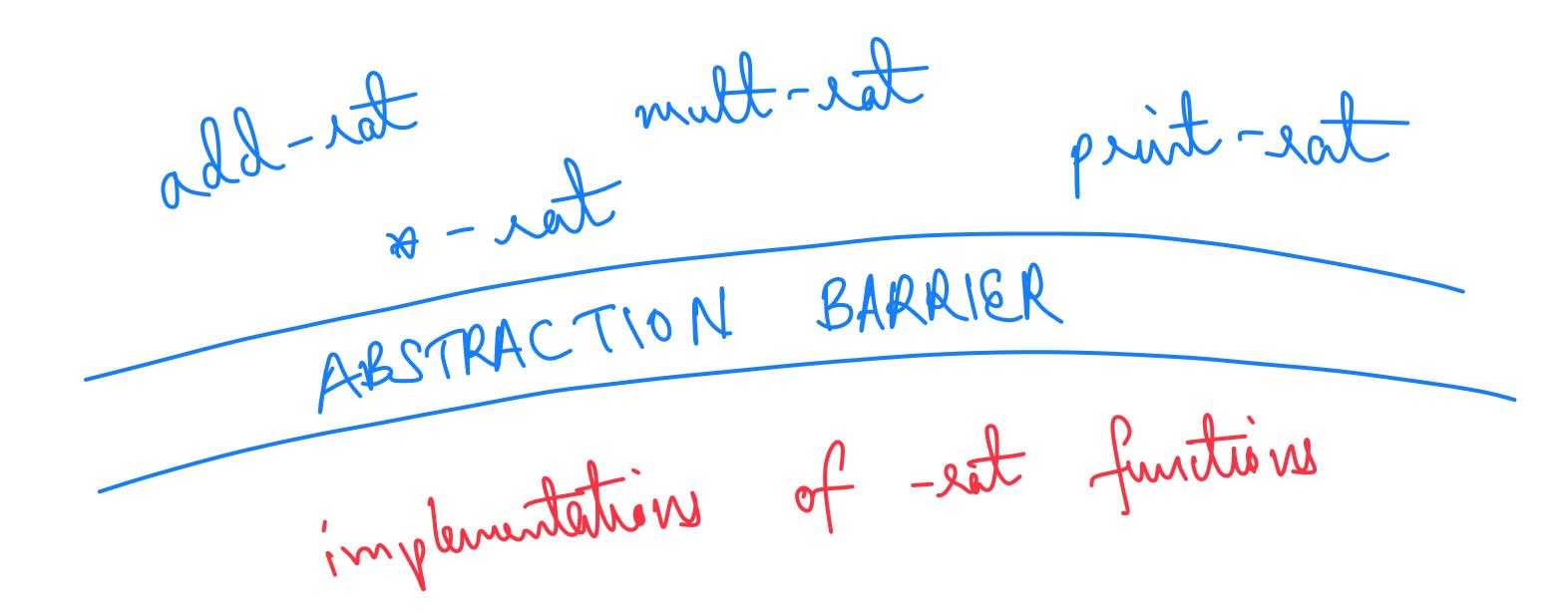
> (cdr x) returns the second element of a pair x





Data Abstraction

➤ Representation is separate from usage; designing/changing the former should not affect the latter.





Updated rational-number implementation

```
(define (make-rat n d)
  (cons n d))
(define (numer x)
  (car x))
(define (denom x)
  (cdr x))
```

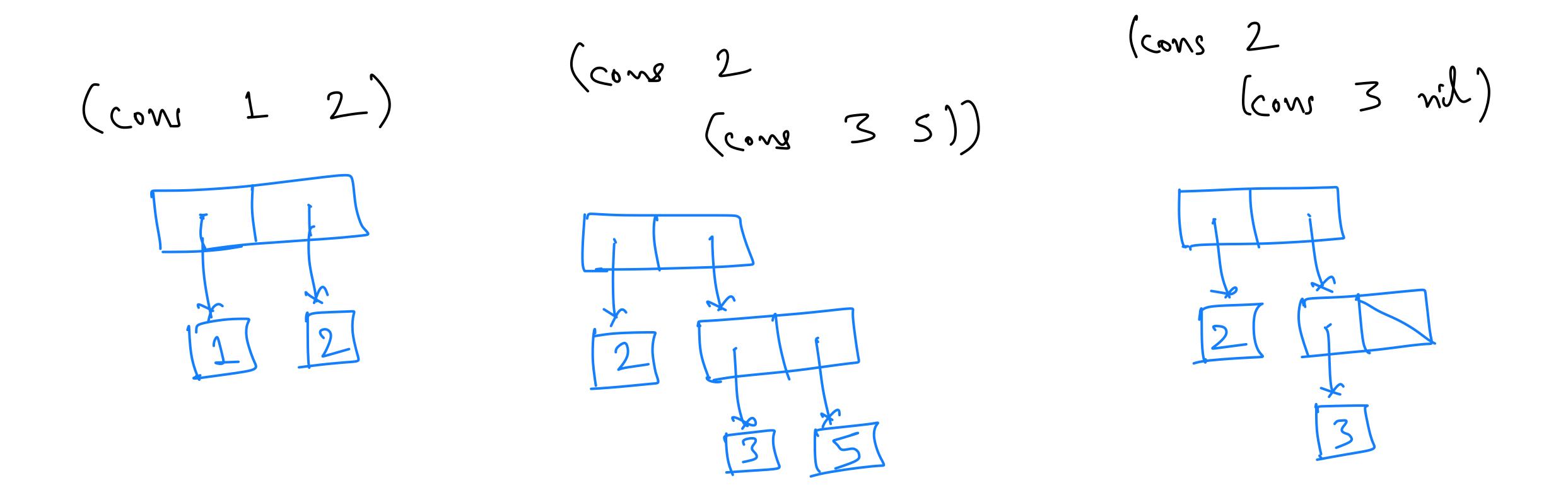


➤ Notice that the usage need not change:

```
(define (add-rat x y)
  (make-rat (+ (* (numer x) (denom y))
               (* (numer y) (denom x)))
            (* (denom x) (denom y))))
(define (mult-rat x y)
  (make-rat (* (numer x) (numer y))
            (* (denom x) (denom y))))
(define (print-rat x)
  (newline)
  (display (numer x))
  (display "/")
  (display (denom x)))
```



Box-Pointer Notation of Pairs



➤ Advantage: Implicit that pairs can have pairs as elements!



But chaining pairs to form a list is quite a popular operation!

> Scheme provides the following special forms to work with *lists*:

```
➤ (list e1 e2 e3) is a syntactic sugar for (cons (e1 (cons e2 (cons e3 nil))))
```

> nil represents an empty list

➤ (null? 1) checks whether a list l is empty and returns a boolean



And we often overdo stuff:D



