

# Examples

## Geostrophic Adjustment: 1D and 1L

In the directory `src` you will find an example entitled `example_1D_1L_spectral.py`

First, libraries are imported. Two standard ones are `numpy`, for calculations, and `matplotlib.pyplot` for plotting. Those are standard to `numpy`. Then, there are four other things that are imported:

- **Steppers** This contains different time-stepping functions. At the moment we have Euler, Adams-Bashforth 2 (AB2) and Runge-Kutta 4 (RK4). PyRsw uses adaptive time stepping to try and be more efficient in how the solution is marched forward.
- **Fluxes** This contains the fluxes for the RSW model. At the moment there is only the option for a pseudo-spectral model but this will be generalized to include a Finite Volume method as well.
- **PyRsw** This is the main library and importing `Simulation` imports the core of the library.
- **constants** This has some useful constants, more can be added if desired.

After the libraries are imported then a simulation object is created.

```
sim = Simulation()
```

Below specifies the geometry in  $x$  and  $y$ : [Options 'periodic', 'walls']

We use AB2, a spectral method: [Options: Euler, AB2, RK4]

We solve the nonlinear dynamics (can be Linear)

Use spectral sw model (no other choices). Maybe hide this.

```
sim.geomx      = 'walls'
sim.geomy      = 'periodic'
sim.stepper     = Step.AB2
sim.method     = 'Spectral'
sim.dynamics   = 'Nonlinear'
sim.flux_method = Flux.spectral_sw
```

We specify a lot of parameters. There are some default values that are specified in `PyRsw`.

```
sim.Lx = 4000e3      # Domain extent          (m)
sim.Ly = 4000e3      # Domain extent          (m)
sim.geomx = 'periodic' # Boundary Conditions
sim.geomy = 'periodic' # Boundary Conditions
sim.Nx = 128         # Grid points in x
sim.Ny = 1           # Grid points in y
sim.Nz = 1           # Number of layers
sim.g = 9.81         # Gravity                      (m/sec^2)
sim.f0 = 1.e-4       # Coriolis                      (1/sec)
sim.cfl = 0.05       # CFL coefficient              (m)
sim.Hs = [100.]      # Vector of mean layer depths (m)
sim.rho = [1025.]    # Vector of layer densities   (kg/m^3)
sim.end_time = 36.*hour # End Time                   (sec)
```

We can specify the periodicity of plotting and whether we want a life animation or make a video. More on this this later.

```
sim.output = False    # True or False
sim.savet   = 1.*hour  # Time between saves
```

Specify periodicity of diagnostics and whether to compute them. This is not tested.

```
sim.diagt   = 2.*minute # Time for output
sim.diagnose = False    # True or False
```

Initialize the simulation.

```
sim.initialize()
```

Specify the initial conditions. There is an option whether we want the domain in  $x$  or  $y$ . At the moment there is no difference because there is no  $\beta$ -plane but this will be added.

```
for ii in range(sim.Nz): # Set mean depths
    sim.soln.h[:, :, ii] = sim.Hs[ii]

# Gaussian initial conditions
x0 = 1.*sim.Lx/2.      # Centre
W = 200.e3             # Width
amp = 1.               # Amplitude
if sim.Ny==1:
    sim.soln.h[:, :, 0] += amp*np.exp(-(sim.x-x0)**2/(W**2)).reshape((sim.Nx,1))
elif sim.Nx==1:
    sim.soln.h[:, :, 0] += amp*np.exp(-(sim.y-x0)**2/(W**2)).reshape((1,sim.Ny))
```

Solve the problem.

```
sim.run()
```

Plot the Hovmöller diagram in time versus space.

```
if sim.Ny==1:
    plt.figure
    t = np.arange(0, sim.end_time+sim.plott, sim.plott)/86400.

    for L in range(sim.Nz):
        field = sim.hov_h[:, 0, :].T - np.sum(sim.Hs[L:])
        plt.subplot(sim.Nz, 1, L+1)
        plt.pcolormesh(sim.x/1e3, t, field,
                        cmap=sim.cmap, vmin = 0, vmax = amp)
        plt.xlim([sim.x[0]/1e3, sim.x[-1]/1e3])
        plt.ylim([t[0], t[-1]])
        plt.title(r"$Hovm{\text{o}}ller Plot\, , \{of\} \, , \, \eta$")
        plt.xlabel(r"$distance \, , \, (km)$")
        plt.ylabel(r"$Time \, , \, (days)$")
        plt.colorbar()
    plt.show()
```

There is a second example called `example_1D_geoadjust2.py` that begins with a hyperbolic tangent profile instead if a Gaussian initial condition.

## Geostrophic Adjustment: 2D and 1L

The basic script is almost identical to the 1D case. The changes are as follows:

1. Set  $Nx$  and  $Ny$  both equal to 128, and from this we build a 2D grid.
2. Define the initial conditions on a 2D grid.
3. The plotting is different. We plot a 2D field using `pcolormesh` and we don't do a Hovmöller plot.

## Bickley Jet: 2D and 1L

Following Poulin and Flierl (2003) and Irwin and Poulin (2014), we look at the instability of a jet.

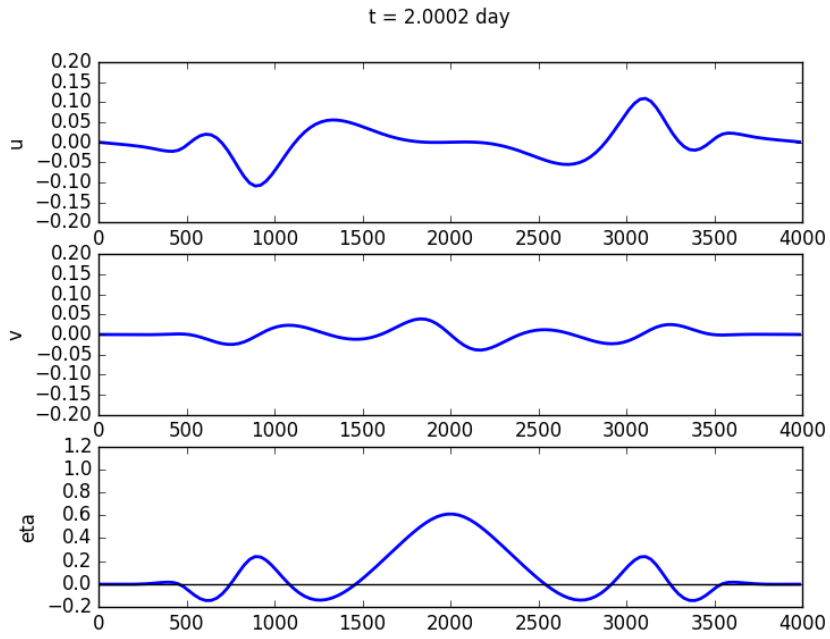


Figure 1: Final solution for the test case.

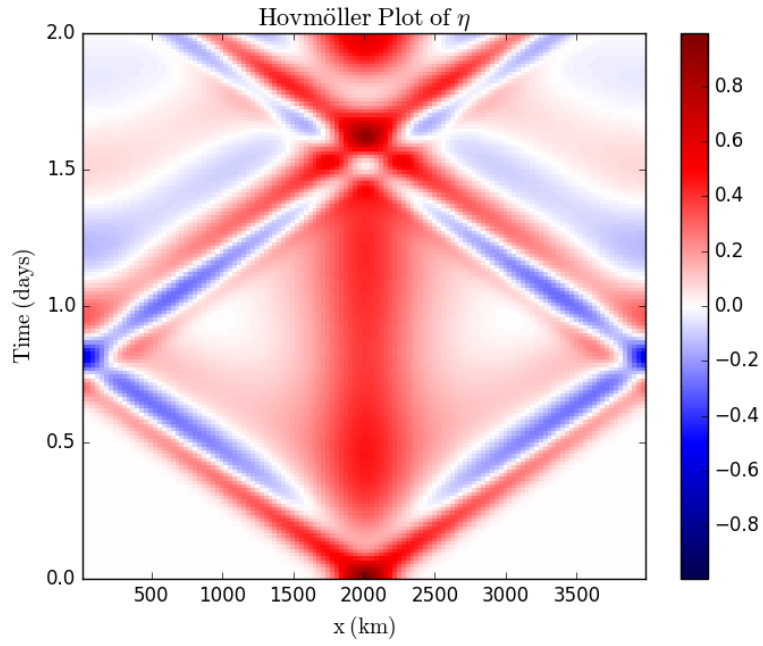


Figure 2: Hovmöller plot for the test case.