

## Quest for Internet

In Part C of the first installment of our weekly series at [emeagwali.com](http://emeagwali.com), we focus on the difference discovery and invention. In 1989, Philip Emeagwali used 65,536 computers to perform a world record 3.1 billion calculations per second. He solved a six-part problem that spanned 41 discoveries and inventions.

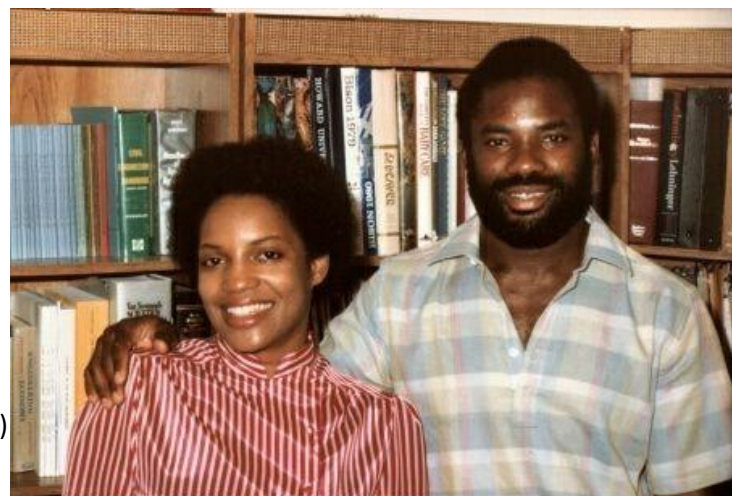
### The Discoverer is the First Teacher

Transcribed and edited from a lecture delivered by [Philip Emeagwali](http://Philip Emeagwali). The lecture [video](#) is posted at [emeagwali.com](http://emeagwali.com) and [youtube.com/emeagwali](http://youtube.com/emeagwali)



Emeagwali stopped pursuing his patent claims because the United States Patent and Trademark Office told him that his 36 algorithms were discoveries, not inventions. He argued that they were inventions, not discoveries, explaining that although the Second Law of Motion encoded within his algorithms was not patentable, his algorithmic techniques that embodied that Second Law within supercomputers should be, because they are the discrete analogue of the 36 partial derivative inertial terms that

he had discovered. In other words, they were functions with input and output.



I heard voices in three dimensions  
and saw visions in sixteen dimensions  
I programmed the sixteen dimensional  
internet email communication to  
be congruent with the three  
dimensional supercomputer computation.

And I visualized <sup>sixteen times</sup> ~~my~~ two-to-power  
~~the~~ sixteen <sup>(one million forty eight thousand</sup>  
~~20~~, or <sup>five hundred and seventy six</sup> 1,048,576, bi-directional  
communication channels as my  
connective tissues between my  
two-to-power <sup>sixteen</sup> ~~16~~, or 65,536,  
sub-computers. Those tissues

111010-06

Patenting algorithms was a gray area in 1989. You cannot patent a mathematical technique but you can patent a computer technology. The algorithm lies between mathematics and computer. Today, it is possible to patent algorithms; however, because he publicly disclosed his inventions in 1989, the one year filing deadline passed.

Importantly, scientific progress is only measured by discoveries, not patents. To discover means to see something that is previously unseen or unknown. Philip Emeagwali discovered that petroleum reservoir engineers summed only three forces, instead of summing all four forces within their oilfields. The word “invent” means the contrivance of that which did not

To discover means to see something that is previously unseen or unknown.

before exists. He invented 36 algorithms for summing all four forces.

To invent means to originate or create as a product of the inventor’s ingenuity. It does not mean to patent. In supercomputing, it means to correctly formulate and solve one of the “Twenty Grand Challenges” at a world-record speed. Philip Emeagwali simulated the flow of oil, water, and gas—with the forces correctly summed—at the then unheard of speed of 3.1 billion calculations per second. It was a Grand Challenge that was of interest to Mobil Corporation, but completed by one man in 1989.

In summary, Philip Emeagwali received a standing ovation at the International Congress for telling the field’s foremost experts that: Exxon was falsifying its petroleum reservoir equations and that the equations taught in universities are not equating to what’s happening inside a petroleum reservoir. It is an unpatented invention just as the Atomic Bomb and internet are unpatented inventions. If you submit a patent related to the Atomic Bomb, the USPTO will inform you that your invention has been stamped “secret.”

The internet is a planet-sized infrastructure comprising of billions of cables and computers. To patent it require that you build a prototype of the internet, which is impossible because:

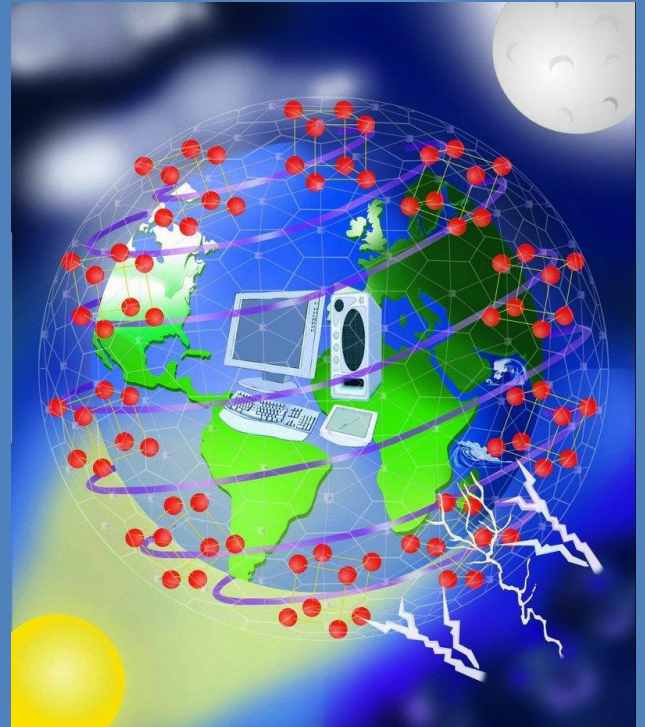
- The Act of Congress of July 4, 1836, section 6, requires an inventor who is desirous to take out a patent for his invention, to furnish a model of his invention, in all cases which admit of representation by model, of a convenient size to exhibit advantageously its several parts.

When reduced to its skeletal bones, the supercomputer Philip Emeagwali programmed was a superinternet outlined by two-to-power sixteen, or 65,536, computers that were interconnected by sixteen times two-to-power sixteen, or 1,048,576 bi-directional communication wires, each akin to a short telegraph wire.

What he discovered and invented was how to push it's frontier by extending the limits of supercomputer computation and superinternet communication. It was newsworthy in 1989.

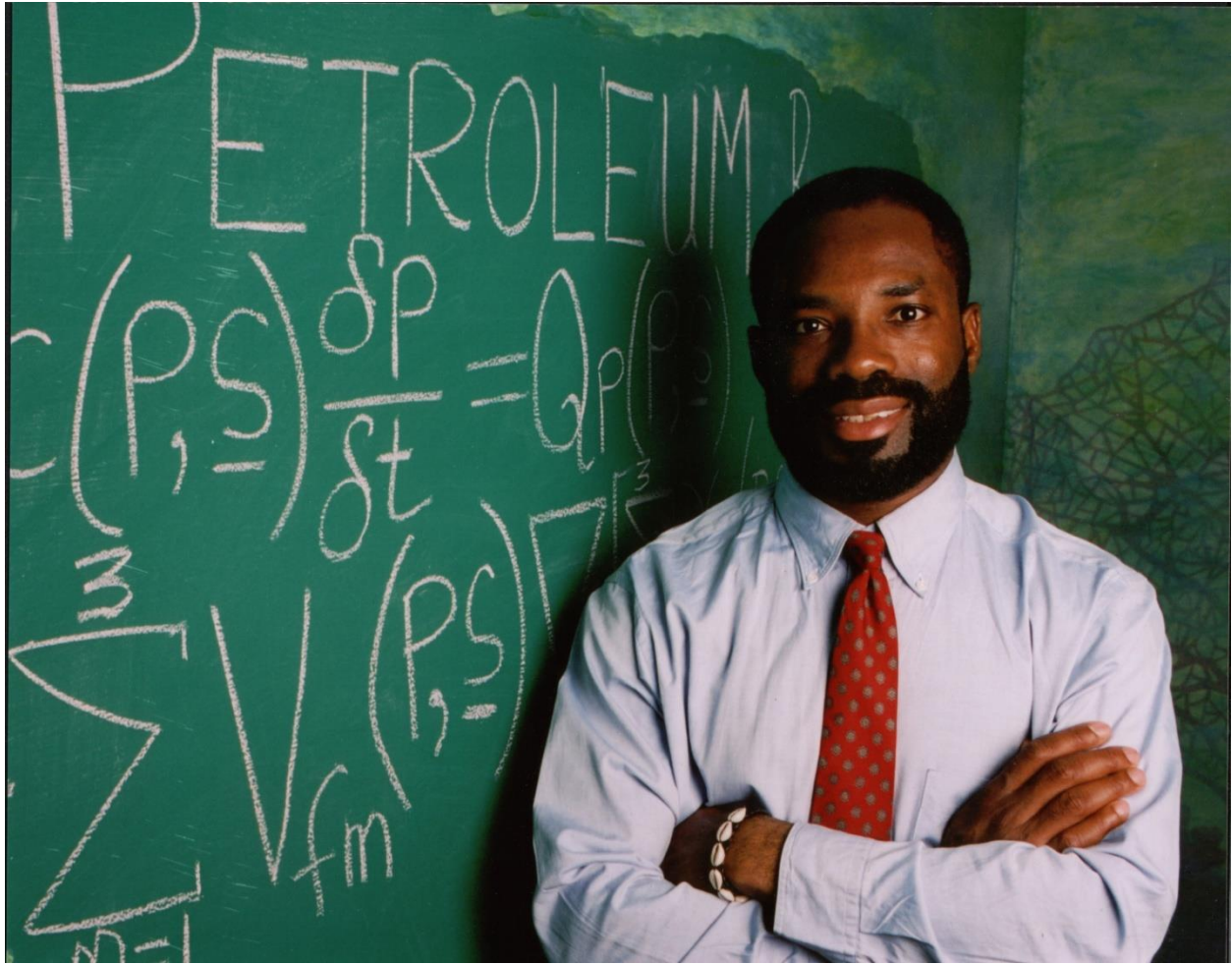
Your dictionary defines the word "invention" without using the word "patent" and groundbreaking inventions, such as the automobile, the airplane, and the Internet, cannot be patented because each has many fathers, mothers, aunts, and uncles. Most importantly, the discoverer is the first teacher of his discovery to humanity, present and future.

Groundbreaking inventions, such as the automobile, the airplane, and the Internet, cannot be patented because each has many fathers, mothers, aunts, and uncles.



An artist's rendition of Emeagwali's theorized Internet described in the book "History of the Internet."





Philip Emeagwali writes on the board the actual equations used by the oil company Exxon (now Exxon Mobil) to simulate the flow of oil, water, and gas inside its petroleum reservoirs. Emeagwali pointed out that four forces exist inside every petroleum reservoir; he discovered that the Exxon Mobil equation had summed only three forces. Emeagwali correctly summed all four forces, namely: pressure, viscosity, gravity, and inertia.



Scanned from our archives of Philip Emeagwali's Notebooks

## STABILITY ANALYSIS

Consider

$$u_t = u_{xx}$$

$$t > 0, 0 < x < 1$$

$$u = 0, x = 0, t > 0$$

$$u = 0, x = 1, t > 0$$

$$u = 2x, 0 \leq x \leq 1/2$$

$$= 2(1-x), 1/2 \leq x \leq 1 \quad \left. \vphantom{\frac{8}{\pi^2}} \right\} t=0$$

Solution:  $u(x,t) = \frac{8}{\pi^2} \sum_{k=1}^{\infty} \left( \sin \frac{k\pi}{2} \right) (\sin k\pi x) e^{-k^2 \pi^2 t}$

We approximate above as

$$u_{i-1}^n - 2u_i^n + u_{i+1}^n$$

$$\frac{u_i^{n+1} - u_i^n}{\Delta t} = \frac{u_{i-1}^n - 2u_i^n + u_{i+1}^n}{(\Delta x)^2}$$

Rearranging yields:

$$u_i^{n+1} = \gamma u_{i-1}^n + (1 - 2\gamma) u_i^n + \gamma u_{i+1}^n$$

$$\text{where } \gamma = \Delta t / (\Delta x)^2$$

$$u(x,t) = \frac{8}{\pi^2} \sum_{k=1}^{\infty} \left( \sin \frac{k\pi}{2} \right) (\sin k\pi x) \frac{e^{-k^2 \pi^2 t}}{k^2}$$



Expanding preceding approx. yields

$$u_1^{n+1} = (1-2\gamma)u_1^n + \gamma u_2^n$$

$$u_2^{n+1} = \gamma u_1^n + (1-2\gamma)u_2^n + \gamma u_3^n$$

$$u_3^{n+1} = \gamma u_2^n + (1-2\gamma)u_3^n + \gamma u_4^n$$

$$\vdots$$

$$u_{N-1}^{n+1} = \gamma u_{N-2}^n + (1-2\gamma)u_{N-1}^n$$

Rearranging yields

$$\begin{bmatrix} (1-2\gamma)\gamma & & & \\ & \gamma(1-2\gamma)\gamma & & \\ & & \ddots & \\ & & & \gamma(1-2\gamma) \end{bmatrix} \begin{bmatrix} u_1^n \\ u_2^n \\ \vdots \\ u_{N-1}^n \end{bmatrix} =$$

$$\begin{bmatrix} u_1^{n+1} \\ u_2^{n+1} \\ \vdots \\ u_{N-1}^{n+1} \end{bmatrix}$$



$$\begin{aligned}
 \bar{u}^{n+1} &= \bar{A} \bar{u}^n \\
 &= \bar{A} (\bar{A} \bar{u}^{n-1}) \\
 &= \bar{A} \cdot \bar{A} (\bar{A} \bar{u}^{n-2}) \\
 &= \bar{A} \cdot \bar{A} \cdot \bar{A} \dots \bar{A} \bar{u}^0, (n+1) \text{ times} \\
 &= \bar{A}^{n+1} \bar{u}^0
 \end{aligned}$$

Suppose

$$u^0 = \text{exact I.C.}$$

$$u_x^0 = \text{erroneous I.C.}$$

Then

$$\begin{aligned}
 \bar{e}^n &= \bar{u}^n - \bar{u}_x^n \\
 &= \bar{A}^n \bar{u}^0 - \bar{A}^n \bar{u}_x^0 \\
 &= \bar{A}^n (\bar{u}^0 - \bar{u}_x^0) \\
 &= \bar{A}^n \bar{e}^0
 \end{aligned}$$

$$\bar{e}^0 = \sum_{i=1}^{N-1} \alpha_i \bar{v}_i$$

$$\begin{aligned}
 \bar{e}^n &= \sum_{i=1}^{N-1} \alpha_i \bar{A}^n \bar{v}_i \\
 &= \sum_{i=1}^{N-1} \alpha_i \lambda_i^n \bar{v}_i
 \end{aligned}$$

$\lambda$  = eigenvalue of  $\bar{A}$



## Gerschgorin's Theorem

If  $\tilde{A}$  is  $n \times n$ ,  $\{S_i\}_{i=1}^n$  is sum of moduli of elements along col. or rows of  $\tilde{A}$ , where  $S_m = \max_i \{S_i\}$

Then  $\rho(\tilde{A}) \leq S_m$

In other words, spectral radius of  $\tilde{A} \leq S_m$

From Gerschgorin's thm, the error vector  $\tilde{e}^n$  is bounded when  $\rho(A) \leq 1$

For our approximation,  $\tilde{A} = \tilde{I} + \gamma \tilde{B}$   
where

$$B = \begin{bmatrix} -2 & 1 & & & \\ & 1 & -2 & 1 & \\ & & 1 & -2 & 1 \\ & & & \ddots & \ddots & \ddots \\ & & & & 1 & -2 \end{bmatrix}$$

The eigenvalues of  $\bar{B}$  are

$$-4 \sin^2 \frac{k\pi}{2N}, \quad k=1, 2, 3, \dots, N-1$$

Corresponding eigenvectors are

$$V_k = \left( \sin \frac{k\pi}{N}, \sin \frac{2k\pi}{N}, \dots, \sin \frac{(N-1)k\pi}{N} \right)$$

$\hat{A} = \hat{I} + \gamma \bar{B} \equiv f(\bar{B}) \Rightarrow$  eigenvalues  
of  $\hat{A}$ :

$$1 - 4\gamma \sin^2 \frac{k\pi}{2N}, \quad k=1, 2, 3, \dots, N-1$$

Convergence  $\Rightarrow \phi(\hat{A}) \leq 1$ , or

$$-1 < 1 - 4\gamma \sin^2 \frac{\pi k}{2N} < 1$$

$$\Rightarrow \gamma \leq \frac{1}{2}$$



Ref.

Gerschgorin, S.: "Über die Abgrenzung der Eigenwerte einer Matrix," Izv. Akad. Nauk SSSR (Ser. Mat. 7, 1931) Vol. 16, page 749

Price, H. S., Varga, R. S., and Warren, J. E.: "Application of Oscillation Matrices to Diffusion-Convection Equations," J. Math. & Physics (Sept. 1966) Vol. 45, No. 3, p. 301-311

O'Brien, G. G., Hyman, M. A., and Kaplan, S.: "A Study of the Numerical Solution of Partial Differential Equations," J. Math. Phys. (Jan. 1951) Vol. 29, No. 70, 223

Richtmeyer, R. D. and Morton, K. W.: "Difference Methods for Initial-Value Problems," 2nd ed., New York, 1967

Handwriting of Philip Emeagwali (1983, Library of Congress)



## STABILITY ANALYSIS

Assume: slight compressibility, constant viscosity, isotropic and homogeneous flow. The governing equation is

$$\frac{1}{\alpha} \frac{\partial P}{\partial \gamma} = \frac{\partial^2 P}{\partial x^2}, \quad \gamma > 0, \quad 0 < x < L$$

Define

$$t = \alpha \gamma / L^2, \quad x = X/L, \quad u = \frac{P - P_i}{P_i}$$

$P_i$  = pressure when  $\gamma = 0$

Substituting yields

$$u_t = u_{xx} \quad t > 0, \quad 0 < x < 1$$

Consider

Boundary Conditions:  $u = 0, x = 0, t > 0$   
 $u = 0, x = 1, t > 0$

Initial Condition:  $u = 2x, 0 \leq x \leq 1/2$   
 $u = 2(1-x), 1/2 \leq x \leq 1$  }  $t = 0$

The solution  $u(x, t)$  is

$$\frac{8}{\pi^2} \sum_{k=1}^{\infty} \left( \sin \frac{k\pi}{2} \right) \left( \sin k\pi x \right) \frac{e^{-k^2 \pi^2 t}}{k^2}$$

An approximation is

$$\frac{u_i^{n+1} - u_i^n}{\Delta t} = \frac{u_{i-1}^n - 2u_i^n + u_{i+1}^n}{(\Delta x)^2}$$

Rearranging yields

$$u_i^{n+1} = \gamma u_{i-1}^n + (1 - 2\gamma) u_i^n + \gamma u_{i+1}^n$$

where

$$\gamma = \frac{\Delta t}{(\Delta x)^2}$$



“Stability analysis is the technique that I used to invent my nine differential equations and nine difference algorithms.” Philip Emeagwali

IMPLICIT APPROXIMATION

$$\Delta_t u = \gamma \Delta^2 u^n$$

where

$$\Delta_t u \equiv u_i^{n+1} - u_i^n$$

$$\Delta^2 u \equiv u_{i-1} - 2u_i + u_{i+1}$$

$$\gamma = \Delta t / (\Delta x)^2$$

Rearranging yields

$$-\gamma u_{i-1}^{n+1} + 2(1+\gamma)u_i^{n+1} - \gamma u_{i+1}^{n+1} = \gamma u_{i-1}^n + 2(1-\gamma)u_i^n + \gamma u_{i+1}^n$$

Yielding global equations

$$\tilde{A} \tilde{u} = \tilde{d}$$

$$\tilde{A} = \begin{bmatrix} b_1 & -c_1 & & & \\ -a_2 & b_2 & -c_2 & & \\ & -a_3 & b_3 & -c_3 & \\ & & \ddots & \ddots & \ddots \\ & & & -a_{N-1} & b_{N-1} \end{bmatrix}$$

$$\tilde{u} = \begin{bmatrix} u_1 \\ u_2 \\ \vdots \\ u_{N-1} \end{bmatrix} \quad \tilde{d} = \begin{bmatrix} d_1 \\ d_2 \\ \vdots \\ d_{N-1} \end{bmatrix}$$

$$a_i = c_i = \gamma, \quad b_i = 2(1+\gamma), \quad i = 1, 2, 3, \dots, N-1$$

Thomas algorithm is most efficient method for solving the above tridiagonal equations



# STABILITY OF IMPLICIT APPROXIMATION

$$\begin{bmatrix} 2(1+\gamma) & -\gamma & & & \\ -\gamma & 2(1+\gamma) & -\gamma & & \\ & \ddots & \ddots & \ddots & \\ & & \ddots & \ddots & -\gamma & 2(1+\gamma) \end{bmatrix} \begin{bmatrix} u_1^{n+1} \\ u_2^{n+1} \\ \vdots \\ u_N^{n+1} \end{bmatrix} = \begin{bmatrix} 2(1-\gamma) & \gamma & & & \\ \gamma & 2(1-\gamma) & \gamma & & \\ & \ddots & \ddots & \ddots & \\ & & \ddots & \ddots & \gamma & 2(1-\gamma) \end{bmatrix} \begin{bmatrix} u_1^n \\ u_2^n \\ \vdots \\ u_N^n \end{bmatrix}$$

Reduces to

$$(2\tilde{I} - \gamma\tilde{B})\tilde{u}^{n+1} = (2\tilde{I} + \gamma\tilde{B})\tilde{u}^n$$

where

$\tilde{B}$  is tri diagonal matrix with "-2" on diagonals and "1" at other entries.

$\gamma > 0 \Rightarrow |2\tilde{I} - \gamma\tilde{B}| \neq 0, \Rightarrow (2\tilde{I} - \gamma\tilde{B})$  is nonsingular.  $\therefore$  inverse  $\exists$

$$u^{n+1} = (2\tilde{I} - \gamma\tilde{B})^{-1} (2\tilde{I} + \gamma\tilde{B}) \tilde{u}^n$$

$$u^{n+1} = \tilde{A} \tilde{u}^n$$

$$\tilde{A} = (2\tilde{I} - \gamma\tilde{B})^{-1} (2\tilde{I} + \gamma\tilde{B}) = f(\tilde{B})$$

Eigen values of  $\tilde{B}$ :

$$\begin{aligned} & -4 \sin^2 \frac{k\pi}{2N}, \quad k = 1, 2, \dots, N-1 \\ \text{Eigen vectors of } \tilde{B}: & \tilde{V}_k = \left( \sin \frac{k\pi}{N}, \sin 2 \frac{k\pi}{N}, \dots, \sin \frac{(N-1)k\pi}{N} \right) \end{aligned}$$



Emeagwali pointed out that four forces exist inside every petroleum reservoir; he discovered that the Exxon Mobil equation had summed only three forces. Emeagwali correctly summed all four forces, namely: pressure, viscosity, gravity, and inertia.

Follows that e-vectors of A are

$$\lambda_k = \frac{2 - 4\gamma \sin^2\left(\frac{k\pi}{2N}\right)}{2 + 4\gamma \sin^2\left(\frac{k\pi}{2N}\right)}, \quad k = 1, 2, \dots, N-1.$$

$\forall \gamma > 0, |\lambda_k| < 1, k = 1, 2, \dots, N-1.$

$\Rightarrow$  unconditional stability

Philip Emeagwali's research notes on a typical day at the Library of Congress in Washington, D.C. in 1983. He performed such mathematical analyses almost daily during the 1980s. (Handwriting of Philip Emeagwali)

Date: 10/13/2007, 4:19 pm, GMT +6

Name: Clinton Anokam <208.78.62.81>

Location: Nigeria,kaduna

Number: 215

With your achievement on Earth and of importance to Humanity .What have been your challenges

Date: 10/10/2007, 3:28 pm, GMT +6

Name: Philip NG.  
Ifechukwude <88.202.35.150>

Location: Ibusa, Nigeria

Number: 214

Philip Emegwalim is one of the best thing to happen to Nigeria of this generation.

Date: 10/10/2007, 3:20 am, GMT +6

Name: Henry Omoregie <196.3.61.4>

Location: Port Harcourt

Number: 213



OUR DEAR PHILLIP,  
IT IS WITH PROUD TAPS ON MY  
KEYBOARD THAT I MAKE THESE  
ASSERTIONS: THAT NIGERIA, NAY  
AFRICA OWES YOU APLENTY FOR  
YOUR SINGULAR MILLENIAL  
ACHIEVEMENTS. YOU DID NOT  
CARVE A NICHE FOR JUST NIGERIA  
BUT THE ENTIRE THIRD WORLD. THE  
ALMIGHTY HAS GIVEN YOU THE  
TALENT TO ENHANCE THE  
ENDEAVORS OF MANKIND

**Date:** 10/9/2007, 12:44 am, GMT +6

**Name:** Hon. Kelechi Ansel-  
Oliaku <91.152.183.208>

**Location:** Finland

**Number:** 212

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Dearest Prof. You are in no doubt one of  
the worlds prominent

inventors, innovator, accomplisher and to say the least, a moving scientific encyclopadia. You have however carved a place for yourself in the annals of world history, but remember to whom much is given much is expected, whether you like it or not, you owe it as a duty to the society that gave you life to create more Emeagwalis. My brother, for a person of your calibre to remain in another man's country for more than two centuries is not a credit. Come home and help develop the Igbo land, on that posterity will write your name in gold "Obu aku lue uno, oburu ezigbo aku"

**Date:** 10/7/2007, 7:50 am, GMT +6

**Name:** Baba Ajose <74.7.92.158>

**Location:** Los Angeles, California

**Number:** 211

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Philip,

I'm proud of you on your great



achievements. However effort needs to be organized privately to share and spread these intellectual knowledge that comes easy to you. There are hundreds perhaps thousands of minds that can and should be molded toward productive activities in Nigeria and on the Continent as a whole. Keep the faith but more importantly, do something.

Regards,  
Baba

**Date:** 10/6/2007, 8:49 pm, GMT +6

**Name:** Thayi K. <87.244.157.39>

**Location:** Douala, Cameroon

**Number:** 210

Cher aîné,

Votre cheminement émet de longues ondes de réflexion à la surface de la conscience. Vos réalisations et votre façon d'être sont plus qu'un exemple pour l'homo africanus disséminé à travers différentes régions du

globe terrestre.

Merci d'avoir fait progresser l'humanité  
par le biais de la science. Merci de  
redonner espoir ...

Emeagwali, you are more than wonderful  
and your name is a blessing.

May Chineke, the Gods and our great  
Ancestors continue to bless you !

Thanks.

**Date:** 10/4/2007, 4:19 pm, GMT +6

**Name:** Sheyin RBG <62.56.224.242>

**Location:** Abuja - Nigeria

**Number:** 209

YOU ARE GREAT!!!!!!!!!!!!!! From your photo  
albums, I observed that you have not  
forgotten your root; You dress like them  
and identify yourself with them. I also  
believe that you are sponsoring Africans  
that will take over from you. Once again be  
aware that it is only through this effort



that the spirit of Prof. Philip Emeagwali  
will not die. MAY YOUR SPIRIT LIVE  
FOREVER.

Date: 9/25/2007, 6:14 pm, GMT +6

Name: Jean <71.242.163.236>

Location: phila.

Number: 208

once again a very profound  
African it is proof Africa  
has a Stellar History

Date: 9/22/2007, 5:08 pm, GMT +6

Name: notonlybridges.blogspot.com <83.165.3.50>

Location: Spain

Number: 207

The entire story of your life and achievements is  
inspirational. Your role as a science and technology

promoter in developing countries is even more motivating. Regards and good luck.

**Date:** 9/18/2007, 8:35 pm, GMT +6

**Name:** alatta kingsley .o <208.78.59.42>

**Location:** abuja

**Number:** 206

may you keep up inspiring the youth of our generation.nigerian's in particular.God blees you sir,  
we will surely get there some day

**Date:** 9/17/2007, 4:23 pm, GMT +6

**Name:** Martin Udogie <80.89.176.36>

**Location:** Lagos

**Number:** 205

Dear Philip Emeagwali,

As a parent, a publisher, and an inspiration



speaker, I have followed your progress and have even used one or two of your materials in my presentations.

But I have a short question. We all have your father to thank for his foresight in getting you to solve 100 mathematical questions everyday. As a father yourself, are you applying your father's strategy to your son? Why or why not?

Date: 9/10/2007, 8:33 pm, GMT +6

Name: uche uzo <172.189.246.43>

Location: uk

Number: 204

I shudder to think how many brains, destinies, inventions, ideas etc like Emeagwali's that have been lost because of lack of funds to pursue education. FREE EDUCATION AS A RIGHT AT ALL LEVELS MUST BE SERIOUSLY CANVASSED. Can you pause and think what the world would have lost if

Emeagwali had ended up at alaba because of funds.

Date: 9/8/2007, 1:15 am, GMT +6

Name: Ajibola Oluwaseyi <82.206.131.126>

Location: Lagos state University

Number: 203

i saw this article about a great man & it suddenly occurred to me that civilization actually started for africa and it really sparked a hope in me that africa is destined for GREATNESS



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