

Q: standard POS Expression :-

$$(A+B)(\bar{A}+C)(B+D)$$

Sol: $(A+B)(\bar{A}+C)(B+D)$

~~$(A+B)$~~

$$= (A+B+C\bar{C})(\bar{A}+B\bar{B}+C)(A\bar{A}+B+D)$$

$$= (A+B+C)(A+B+\bar{C})(\bar{A}+B+C)(\bar{A}+\bar{B}+C)(A+B+D) \quad \downarrow$$

$$(\bar{A}+B+D)$$

$$\Rightarrow (A+\bar{B}+C+D\bar{D})(A+B+\bar{C}+D\bar{D})(\bar{A}+B+C+D\bar{D})$$

$$(\bar{A}+\bar{B}+C+D\bar{D})(\bar{A}+B+C\bar{C}+D)$$

$$(A+B+C\bar{C}+D)$$

$$\Rightarrow (A+B+C+D)(A+B+C+\bar{D})(A+B+\bar{C}+D)$$

$$(A+B+\bar{C}+\bar{D})(\bar{A}+B+C+D)(\bar{A}+\bar{B}+C+\bar{D})$$

$$(\bar{A}+\bar{B}+C+D)(\bar{A}+\bar{B}+C+\bar{D})(A+B+C+D)$$

$$(A+B+\bar{C}+D)(\bar{A}+B+C+D)(\bar{A}+B+\bar{C}+D)$$

$A+B$ is missing variable D or D'
and (C) or (C')

$$\begin{aligned} A+B &= A+B + DD' + CC' \\ &= (A+B+D)(A+B+D) \end{aligned}$$

2) Second Term:

$$(A+B) \cdot (\bar{A}+C) \cdot (B+D)$$

$$((A \cdot \bar{A}) + B + C) \cdot (B+D)$$

$$\because A \cdot \bar{A} = 0$$

$$(0 + B + C) \cdot (B+D)$$

$$\underline{(B+C)(B+D)}$$

C:

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standard sop expression
from standard pos

Truth table

A	B	C	D
0	0	0	0
0	0	0	1
0	0	1	0
0	0	1	1
0	1	0	0
0	1	0	1
0	1	1	0
0	1	1	1
1	0	0	1
1	0	1	0
1	0	1	1
1	1	0	0
1	1	0	1
1	1	1	0
1	1	1	1

A	B	C	D
1	1	1	1

from truth table

$$\begin{aligned} & \bar{A}\bar{B}\bar{C}\bar{D} + \bar{A}\bar{B}\bar{C}D + \bar{A}\bar{B}C\bar{D} \\ & + \bar{A}\bar{B}CD + \bar{A}B\bar{C}\bar{D} + \bar{A}B\bar{C}D \\ & + A\bar{B}\bar{C}\bar{D} + AB\bar{C}\bar{D} \end{aligned}$$

40.

A minimum SOP:

AB	CD			
	$\bar{C}\bar{D}$	$\bar{C}D$	CD	$C\bar{D}$
$\bar{A}\bar{B}$				
$\bar{A}B$	1	1	1	1
$A\bar{B}$			1	1
AB			1	

$$S = ACD + \bar{A}B + BC$$

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