## $1.\{1,5,9,10\}$

**Reminder:** Midterm 1 will take place on Thursday, 2/18, from 8:10 to 9:25 in our usual classroom. The exam will cover the first four chapters of Kleppner and Kolenkow. You will not need a calculator.

- **1 Center of mass of a non-uniform rod\* KK 4.1** The mass per unit length of a non-uniform rod of length l is given by  $\lambda = A\cos(\pi x/2l)$ , where x is the position along the rod,  $0 \le x \le l$ .
  - (a) What is the mass *M* of the rod?
  - (b) What is the coordinate *X* of the center of mass?

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**2 - Acrobat and monkey - KK 4.5** A circus acrobat of mass M leaps straight up with initial velocity  $v_0$  from a trampoline. As he rises up, he takes a trained monkey of mass m off a perch at a height h above the trampoline. What is the maximum height attained by the pair?

**3 - Rocket sled - KK 4.9** A rocket sled moves along a horizontal plane, and is retarded by a friction force  $f_{\text{friction}} = \mu W$ , where  $\mu$  is constant and W is the weight of the sled. The sled's initial mass is M, and its rocket engine expels mass at constant rate  $dM/dt \equiv \gamma$ ; the expelled mass has constant speed  $v_0$  relative to the rocket. The rocket starts from rest and the engine stops when half the sled's total mass is gone. Find an expression for the maximum speed.

**4 - Rolling freight car with sand - KK 4.10** A freight car of mass M contains a mass of sand m. At t=0 a constant horizontal force R is applied in the direction of rolling and at the same time a port in the bottom is opened to let the sand flow out at constant rate dm/dt. Find the speed of the freight car when all the sand is gone. Assume the freight car is at rest at t=0.