

$$\begin{aligned}
S(\mathbf{W}, \mathbf{c}) &= \lambda \sum_{j=1}^n \left( p - \frac{1}{m} \sum_{l=1}^m \mathbb{E}[h_j^{(l)} | v^{(l)}] \right)^2 \\
&= \lambda \sum_{j=1}^n \left( p - \frac{1}{m} \sum_{l=1}^m h_j^{(l)} \text{sigm}(c_l + \sum_i W_{li} x_j^{(i)}) \right)^2 \\
\frac{\delta S(\mathbf{W}, \mathbf{c})}{\delta c_k} &= \lambda \sum_{j=1}^n 2 \left( p - \frac{1}{m} \sum_{l=1}^m h_j^{(l)} \text{sigm}(c_l + \sum_i W_{li} x_j^{(i)}) \right) \\
&\quad \left( -\frac{1}{m} h_j^{(k)} (1 - \text{sigm}(c_k + \sum_i W_{ki} x_j^{(i)})) \text{sigm}(c_k + \sum_i W_{ki} x_j^{(i)}) \right) \\
&= 2\lambda \sum_{j=1}^n \left( -\frac{1}{m} h_j^{(k)} (1 - \text{sigm}(c_k + \sum_i W_{ki} x_j^{(i)})) \text{sigm}(c_k + \sum_i W_{ki} x_j^{(i)}) \right) \\
&\quad \left( p - \frac{1}{m} \sum_{l=1}^m h_j^{(l)} \text{sigm}(c_l + \sum_i W_{li} x_j^{(i)}) \right)
\end{aligned}$$