Chapter 4 - Writing Structured Programs

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- 1 Algorithm Design
 - Divide-and-Conquer
 - Recursion
 - Space-Time Tradeoffs
 - Dynamic Programming

Please refer to chapter 4 of *Natural Language Processing with Python* and related lectures in my programming basics course for the following topics:

- Back to the Basics
- Sequences
- Questions of Style
- Functions: The Foundation of Structured Programming
- Doing More with Functions
- Program Development

- 1 Algorithm Design
 - Divide-and-Conquer
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Divide-and-Conquer

The basic idea is dividing a problem of size n into two problems of size n/2, solving these problems, and combining their results into a solution of the original problem.

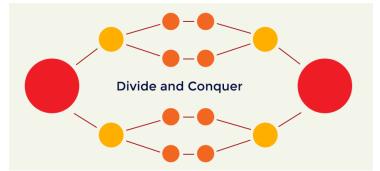


Figure 1: Divide-and-Conquer Paradiam

Merge sort algorithm a typical application of divide and conquer paradiam.

Merge Sort

Divide: 自顶向下,递归地二等分列表,直到不可分为止,即每个子列表只包含一个元素。

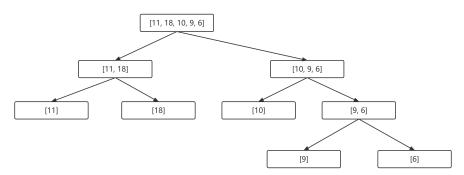


Figure 2: Dividing

```
def merge_sort(arr):
    # dividing
    if len(arr) == 1:
        return arr
    else:
        length = len(arr)
        left_arr = arr[:length//2]
        right_arr = arr[length//2:]
        print('split',arr,'--->',left_arr, right_arr)
        # sorting and merging
        return sort_list(merge_sort(left_arr), merge_sort(right_arr))
```

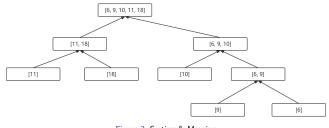


Figure 3: Sorting & Merging

- 对比第一个元素, 11 < 6, 6放入结果列表中,结果列表为 [6];
- ② 两个子列表变为 [11, 18] 和 [9, 10];
- ③ 对比第一个元素 11 > 9,9 放入结果列表中,结果列表为 [6,9];
- 两个子列表变为 [11, 18] 和 [10];
- 对比第一个元素 11 > 10, 10 放入结果列表中,结果列表为 [6, 9, 10];
- 两个子列表变为 [11, 18] 和 [];
- ◎ 第一个子列表有序,第二个子列表为空,将第一个子列表加入结果 列表,结果列表为 [6, 9, 10, 11, 18]。

已排序子列表 [11, 18] 和 [6, 9, 10] 的排序合并过程如前所述,实现 代码如下:

```
def sort_list(left, right):
 1, r = deepcopy(left), deepcopy(right)
  result = []
  while len(left) > 0 and len(right) > 0:
    if left[0] < right[0]:</pre>
      result.append(left.pop(0))
    else:
      result.append(right.pop(0))
  result += left
  result += right
  print('merge',1, r,'--->',result)
  return result
```

```
merge_sort([1,4,2])
111
split [1, 4, 2] ---> [1] [4, 2]
split [4, 2] ---> [4] [2]
merge [4] [2] ---> [2, 4]
merge [1] [2, 4] ---> [1, 2, 4]
111
merge_sort([11, 18, 10, 9, 6])
split [11, 18, 10, 9, 6] ---> [11, 18] [10, 9, 6]
split [11, 18] ---> [11] [18]
merge [11] [18] ---> [11, 18]
split [10, 9, 6] ---> [10] [9, 6]
split [9, 6] ---> [9] [6]
merge [9] [6] ---> [6, 9]
merge [10] [6, 9] ---> [6, 9, 10]
merge [11, 18] [6, 9, 10] ---> [6, 9, 10, 11, 18]
111
```

1. Algorithm Design Recursion

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Recursion

Example: count the size of a (sub)tree rooted at a given node.

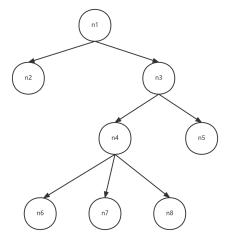


Figure 4: The size of the tree rooted at n1 is 8

```
# 采用字典结构存储上图中的树
n1 = {
       'n2':{},
        'n3':{
               'n4':{
                       'n6':{},
                       'n7':{},
                       'n8':{}
                     },
               'n5':{}
             }
     }
```

两种基本情况:

- 1. 叶子节点 (没有子节点), 如, 'n5':{}
- 2. 非叶子节点 (有子节点), 如, 'n4':{'n6':{},'n7':{},'n8':{}}

```
# 递归计数
def tree_nodes_count_recursive(tree_dict):
  return 1 + sum(tree_nodes_count(v) for v in tree_dict.values())
# 逐层遍历计数
def tree_nodes_count_loop(tree_dict):
  trees = [tree_dict]
 total = 0
  while trees:
    total += len(trees)
    trees = [value for tree in trees for value in tree.values()]
  return total
nn = \{'n1': \{'n2': \{'n3': \{\}\}\}\}\
tree_nodes_count_recursive(nn) # 4
tree_nodes_count_loop(nn) # 4
tree_nodes_count_recursive(n1) # 8
tree_nodes_count_loop(n1) # 8
```

将上述代码中的 values() 替换为 hyponyms() 即可用来计算wordNet中以同义词集 s 为根节点的子树节点数。

```
def recursive_size(s):
  return 1 + sum(size1(child) for child in s.hyponyms())
def loop_size(s):
  layer = [s] # The first layer is the synset itself
 total = 0
  # it computes the next layer by finding the hyponyms of
  → everything in the last layer
  while layer:
    total += len(layer)
    layer = [h for c in layer for h in c.hyponyms()]
  return total
from nltk.corpus import wordnet as wn
dog = wn.synset('dog.n.01')
recursive_size(dog), loop_size(dog) # 190
```

Example: a letter trie is a data structure that can be used for indexing a lexicon.

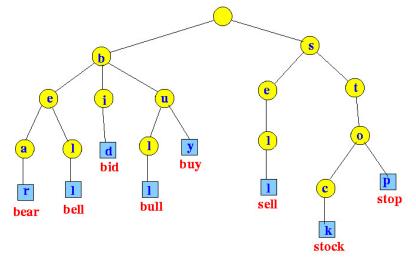


Figure 5: Letter Trie Example

Recursively build a letter trie with Python dictionaries.

```
def insert(trie, key, value):
  if key:
    first, rest = key[0], key[1:]
    if first not in trie:
      trie[first] = {}
    insert(trie[first], rest, value)
  else:
    trie['value'] = value
trie = {}
insert(trie, 'bear', '熊')
insert(trie, 'bell', '钟')
insert(trie, 'bid', '出价')
insert(trie, 'bull', '公牛')
insert(trie, 'buy', '买')
import pprint
pprint.pprint(trie, width=40)
```

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Space-Time Tradeoffs

We can sometimes significantly speed up the execution of a program by building an auxiliary data structure, such as an index.

Example: implements a simple text retrieval system for the Movie Reviews Corpus by indexing the document collection.

```
import re
def raw(file):
 contents = open(file).read()
 contents = re.sub(r'<.*?>', ' ', contents)
 contents = re.sub('\s+', ' ', contents) # 将空白字符替换为空格
 return contents
def snippet(doc, term):
 text = ' *30 + raw(doc) + ' *30
 pos = text.index(term)
 return text[pos-30:pos+30] # 上下文窗口为左右30个字符
```

```
import nltk
# 对movie reviews构建索引
files = nltk.corpus.movie_reviews.abspaths()
print("Building Index...")
idx = nltk.Index((w, f) for f in files for w in raw(f).split())
# 使用构建的索引进行查询
query = ''
while query != "quit":
 query = input("query> ")
  if query in idx:
   for doc in idx[query]:
     print(snippet(doc, query))
 else:
   print("Not found")
```

Example: replace the tokens of a corpus with integer identifiers.

- Create a vocabulary dict for the corpus, in which each word is stored once;
- Each document is preprocessed to become a list of integers;
- Any language models can now work with integers.

```
def preprocess(tagged_corpus):
  # 使用集合存储词表和标签表
 words = set()
 tags = set()
 for sent in tagged_corpus:
   for word, tag in sent:
     words.add(word)
     tags.add(tag)
 word2idx = dict((w, i) for (i, w) in enumerate(words))
  tag2idx = dict((t, i) for (i, t) in enumerate(tags))
 return word2idx, tag2idx
```

```
from nltk.corpus import brown
tagged_brown = brown.tagged_sents()
word2idx, tag2idx = preprocess(tagged_brown)
word_list = [[(word2idx[w]) for (w, _) in sent] for sent in

    tagged_brown[:20]]

pos_list = [[(tag2idx[t]) for (_, t) in sent] for sent in

    tagged brown[:20]]

# [20312, 40664, 53115, 43127, ...]
print(word_list[3])
# [99, 188, 353, 62, 218, ...]
print(pos_list[3])
```

If you need to process an input text to check that all words are in an existing vocabulary, the vocabulary should be stored as a set, not a list.

The elements of a set are automatically indexed, so testing membership of a large set will be much faster than testing membership of the corresponding list.

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Basic idea: Dynamic programming is a general technique for designing algorithms and used when a problem contains overlapping sub-problems. Instead of computing solutions to these sub-problems repeatedly, we simply store them in a lookup table.

Example: 在梵文中,短音节 S 的占一个长度单位,长音节 L 占两个长度单位,找出所有可能的长短音节组合方式,使得组合之后的结果长度为 n。例如 $V_4 = \{LL, SSL, SLS, LSS, SSSS\}$, V_4 可以进一步划分为两个子集合:

$$V_4=$$
 LL,LSS i.e. L prefixed to each item of $V_2=L,SS$ $SSL,SLS,SSSS$ i.e. S prefixed to each item of $V_3=SL,LS,SSS$

下面提供四种实现方式:

```
# 1. 递归实现
def virahanka1(n):
  #第一种基本情况
  if n == 0:
   return [""]
  # 第二种基本情况
  elif n == 1:
   return ["S"]
  else:
    s = ["S" + prosody for prosody in virahanka1(n-1)]
    1 = ["L" + prosody for prosody in virahanka1(n-2)]
  return s + 1
virahanka1(4)
# ['SSSSS', 'SSSL', 'SSLS', 'SLS', 'SLL', 'LSSS', 'LSL', 'LLS']
virahanka1(5)
```

思考:上述实现有什么显著缺陷?

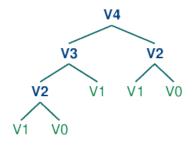


Figure 6: Call Structure of the Recursion Solution

第一种递归解法存在重复计算,例如,对于 V_2 ,计算 V_{20} 时,需要计算 4181 次,计算 V_{40} 时,需要计算 63245986 次。

思考: V_2 的计算次数是如何得出的(V_2 的计算次数与 n 的存在怎样的关系)?

改进第一种递归解法: 将子问题的计算结果保存到一个查找表中。

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1. Algorithm Design

```
# 2. 自底向上的动态规划
def virahanka2(n):
 # VO, V1
 lookup = [[""], ["S"]]
 # n>=2才会执行下面的循环语句
 for i in range(n-1):
   s = ["S" + prosody for prosody in lookup[i+1]]
   1 = ["L" + prosody for prosody in lookup[i]]
   lookup.append(s + 1)
 return lookup[n]
```

```
n = 3 时上述函数的执行过程如下:
i = 0, "S" + lookup[1], ---> V2
i = 0, "L" + lookup[0], ---> V2
lookup = [[""], ["S"], V2]
i = 1, "S" + lookup[2], ---> V3
i = 1, "L" + lookup[1], ---> V3
lookup = [[""], ["S"], V2, V3]
```

1. Algorithm Design

```
# 3. 自顶向下的动态规划
def virahanka3(n, lookup={0:[""], 1:["S"]}):
    # n>=2下面语句才会执行
    if n not in lookup:
    s = ["S" + prosody for prosody in virahanka3(n-1)]
    1 = ["L" + prosody for prosody in virahanka3(n-2)]
    lookup[n] = s + 1
    return lookup[n]
```

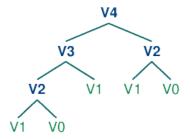


Figure 7: Call Structure of the Above Solution

- 上述自顶向下的递归调用过程虽然与第一种方法一样,但是由于存在一个查找表保存中间计算结果,因此,不存在重复计算;
- 在某些应用中,自底向上的动态规划可能会计算一些对求解主问题 没有用的子问题,因而会造成一些资源浪费;
- 自顶向下的动态规划可以避免这种不必要的资源浪费,因为其首先 将主问题逐步分解,仅计算对求解主问题有用的子问题。

```
# 4. Python memoize decorator
from nltk import memoize
@memoize
def virahanka4(n):
 if n == 0:
   return [""]
 elif n == 1:
   return ["S"]
 else:
    s = ["S" + prosody for prosody in virahanka4(n-1)]
   1 = ["L" + prosody for prosody in virahanka4(n-2)]
 return s + 1
```

- 第四种方法使用了 Python 的 memoize 装饰器;
- 该装饰器存储函数调用的结果及对应的参数;
- 当该函数使用同样的参数被调用时,不再重复计算,直接返回存储的结果。

4.8 A Sample of Python Libraries

Please refer to chapter 4 of *Natural Language Processing with Python* for the following topics:

- Matplotlib
- CSV
- NetworkX
- Numpy
- Other Python Libraries

THE END