

Fibre-based high-dimensional quantum communications

Davide Bacco, Daniele Cozzolino, Beatrice Da Lio, Y. Ding,
Karsten Rottwitt, and Leif Katsuo Oxenløwe

High-Speed Optical Communication Group (HSOC)
Centre for Silicon Photonics for Optical Communication (SPOC)

dabac@fotonik.dtu.dk

$$E_{ph} = h \frac{c}{\lambda} \int_a^b \mathcal{E} \Theta + \Omega \delta e^{i\pi} = \sum \dots$$

A mathematical equation where the variables are represented by optical components and symbols. E_{ph} is the energy density, h is Planck's constant, c is the speed of light, λ is wavelength, \int_a^b is the path length, \mathcal{E} is electric field, Θ is phase, Ω is angular frequency, δ is a small change, $e^{i\pi}$ is a complex exponential, and the summation symbol \sum is followed by a series of optical symbols like \gg , ∞ , χ^2 , and $!$.

Outline

- SPOC centre (DTU Fotonik)
- Quantum communications with Hi-D (qudits)
- Examples: Multicore and OAM fibres for QCs
- Application: Hi-D Quantum key Distribution
- Comparison between Hi-D encoding and key multiplexing
- Conclusion

Centre of excellence for **Silicon Photonics for Optical Communication**

Aim: find solutions to the major challenges of communication systems – security, energy consumption and capacity



Kresten Yvind,
Assoc. Professor,
DTU Fotonik



Karsten Rottwitt,
Professor,
DTU Fotonik



Leif K. Oxenløwe,
Centre Leader,
DTU Fotonik



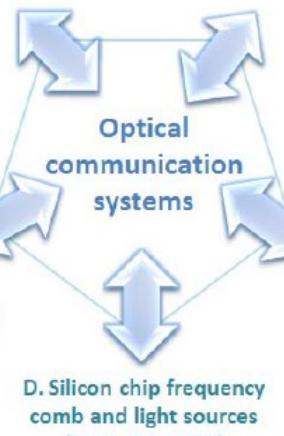
Toshio Morioka,
Professor,
DTU Fotonik



Jan W. Thomsen,
Assoc. Professor,
Niels Bohr Institute

A. Nonlinear silicon wires:
ultra-fast, ultra-broadband, low-energy OSP
(DTU, Ugent)

E. Quantum communication sources
(DTU, USYD, ACS)



B. Advanced multiplexing for ultimate capacity
(DTU, BU, UBris)

C. Information theory & coding:
capacity limits and beyond
(DTU, TUM)

D. Silicon chip frequency comb and light sources
(DTU, KU, UCSB)

Quantum communication:

 $|\psi\rangle$

"The art of transferring a quantum state from one place to another"

[N. Gisin, R. Thew, Nat. Photon. 1(3), 165 (2007)]

 $|\psi\rangle$

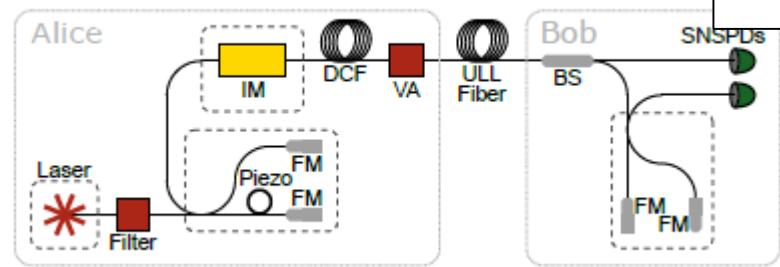
Satellite teleportation/QKD

Science. AAAS



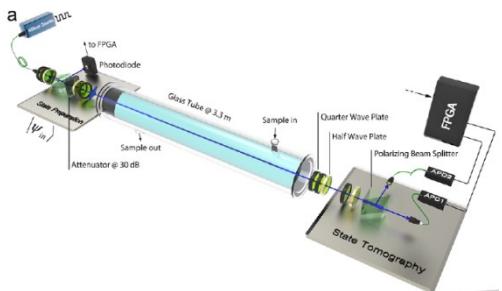
J. Yin et al., Science 356 (1140)
J. G. Ren et al., Nature 549 (70)

421 km QKD in fibre



A. Boaron et al., arXiv:1807.03222

Underwater QCs



L. Ji et al., Opt. Expr. 25 (17)
F. Bouchard et al., Opt. Expr. 26 (17)

Quantum communications with qudits



- ✓ larger PIE and noise robustness for quantum communications

[N. J. Cerf, et al., *P.R.L.*, 88(12) 2002]

- ✓ reduction of cloning fidelity in Hi-D quantum states

[M. Erhard et al., *Light: Science & Applications* 7,17146 (2018)]

- ✓ higher efficiency and flexibility in quantum computing [J. Wang, et al., *Science*, 360 (2018)]

University of BRISTOL QET Labs |>

DTU SPOC
CENTRE FOR SILICON PHOTONICS
FOR OPTICAL COMMUNICATIONS

PEKING UNIVERSITY 北京大學

ICFO

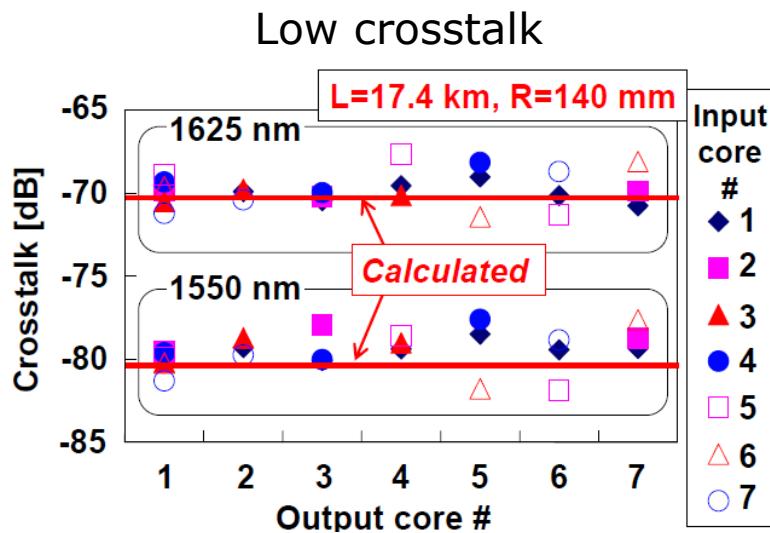
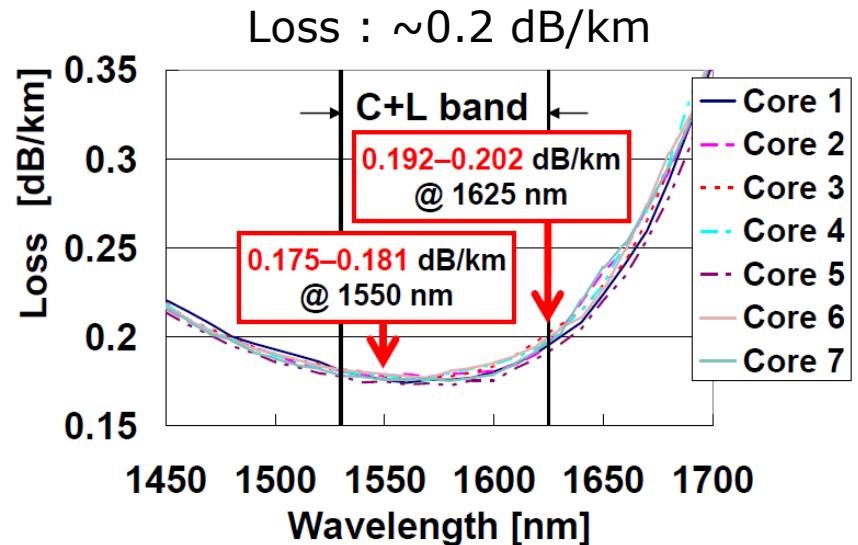
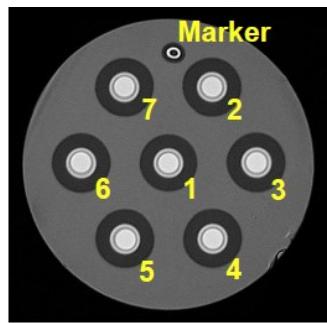
Multidimensional quantum entanglement with large-scale integrated optics.

J. Wang, et al., *Science*, 360 (2018)

HARVARD UNIVERSITY SIGILLUM

ast 2018

Multicore fibre for QCs

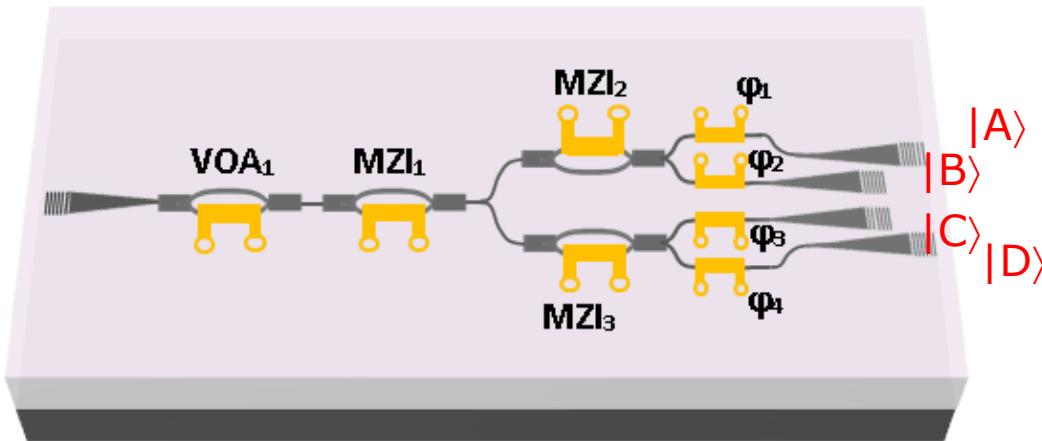


SOTA

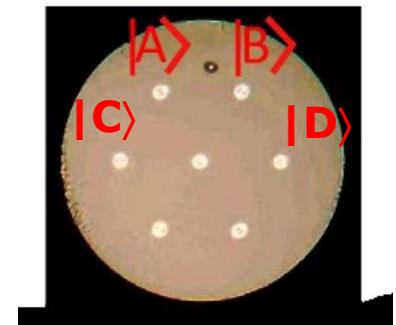
- 37 cores heterogeneous MCF
- Distance >10 km
- Few deployed fibres

Setup of QCs with MCF

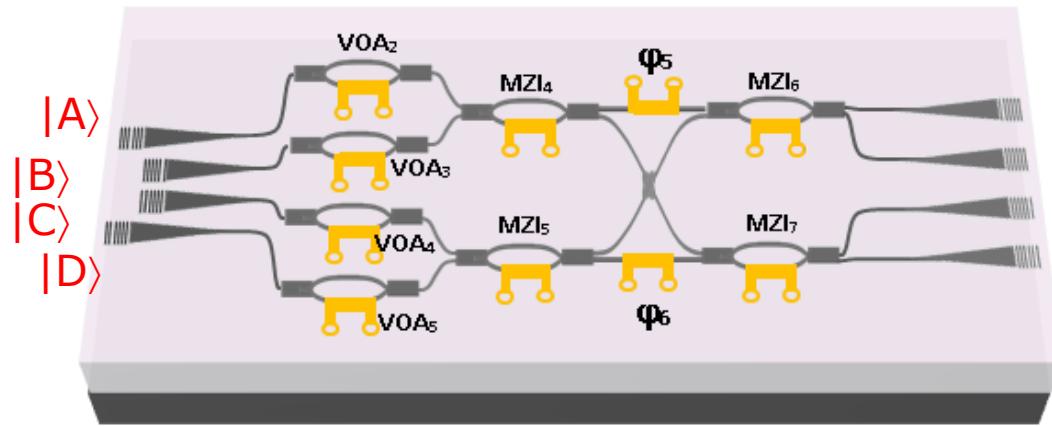
Transmitter



MCF



Receiver



Quantum states

2D

$$\begin{pmatrix} |A\rangle \\ |B\rangle \end{pmatrix}$$

$$\begin{pmatrix} |A+B\rangle \\ |A-B\rangle \end{pmatrix}$$

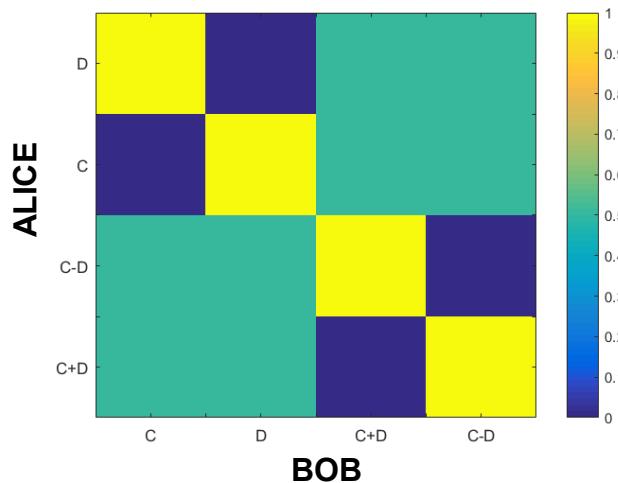
4D

$$\begin{pmatrix} |A+B\rangle \\ |A-B\rangle \\ |C+D\rangle \\ |C-D\rangle \end{pmatrix}$$

$$\begin{pmatrix} |A+C\rangle \\ |A-C\rangle \\ |B+D\rangle \\ |B-D\rangle \end{pmatrix}$$

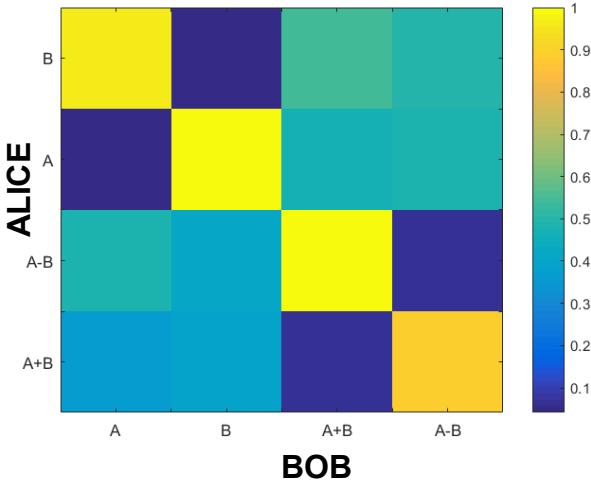
$$\begin{pmatrix} |A+D\rangle \\ |A-D\rangle \\ |B+C\rangle \\ |B-C\rangle \end{pmatrix}$$

Fidelity of MUBs

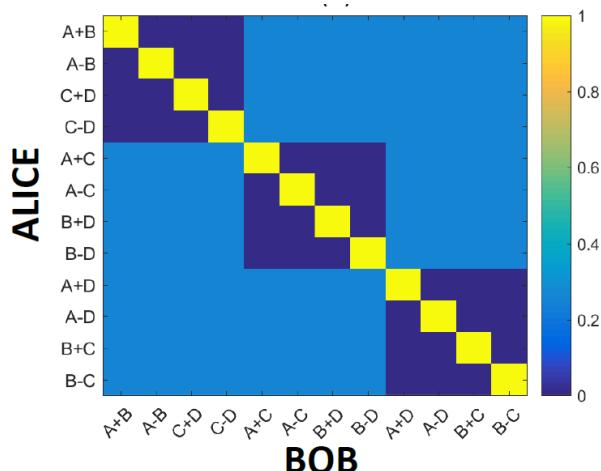


Theory

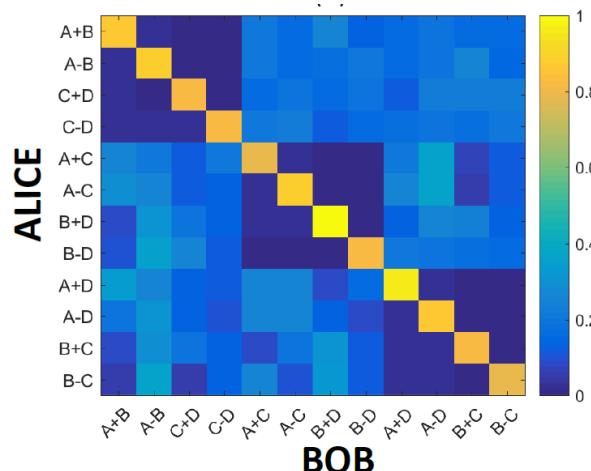
2D



Experiment



4D
 $F \approx 98\%$



Problems:

- ✓ few meters between transmitter and receiver (5m)
- ✓ Slow repetition rate
- ✓ difficult to keep stability over time

OAM for QCs

Free-Space Quantum Key Distribution by Rotation-Invariant Twisted Photons

Giuseppe Vallone,¹ Vincenzo D'Ambrosio,² Anna Sponselli,³ Sergei Slussarenko,^{4,*} Lorenzo Marrucci,⁴ Fabio Sciarrino,² and Paolo Villoresi^{1,†}

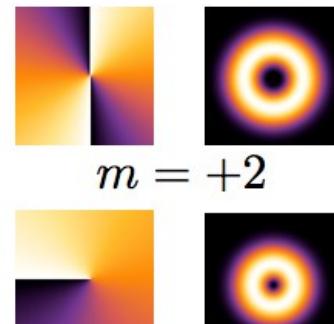
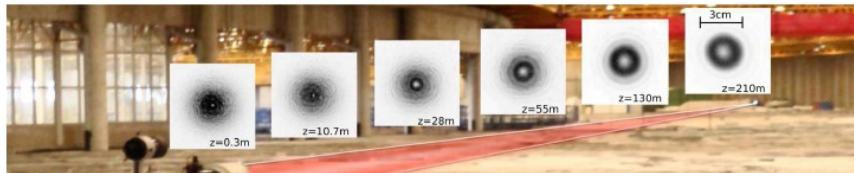
¹Dipartimento di Ingegneria dell'Informazione, Università di Padova, I-35131 Padova, Italy

²Dipartimento di Fisica, Sapienza Università di Roma, I-00185 Roma, Italy

³Dipartimento di Fisica e Astronomia, Università di Padova, I-35131 Padova, Italy

⁴Dipartimento di Fisica, Università di Napoli Federico II and CNR-SPIN, I-80126 Napoli, Italy

(Received 29 April 2014; published 8 August 2014)

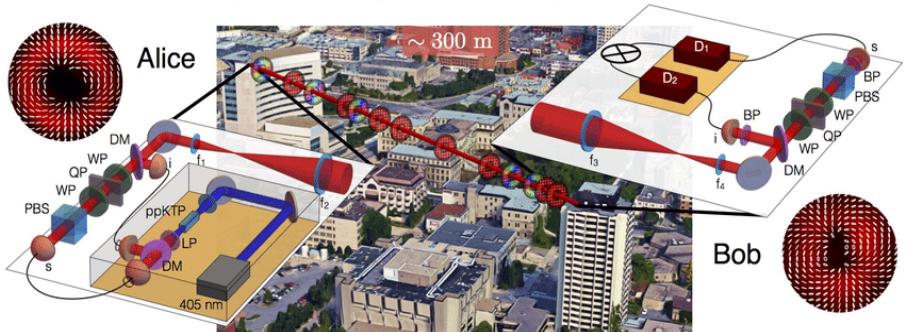


Fibre based QC with twisted photons was not demonstrated!

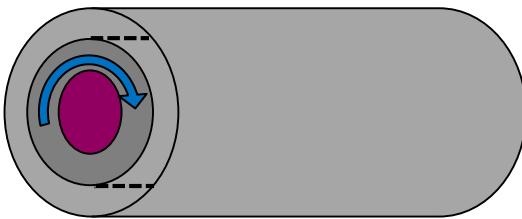
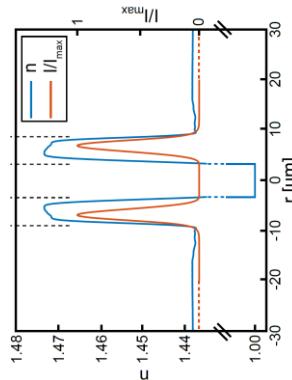
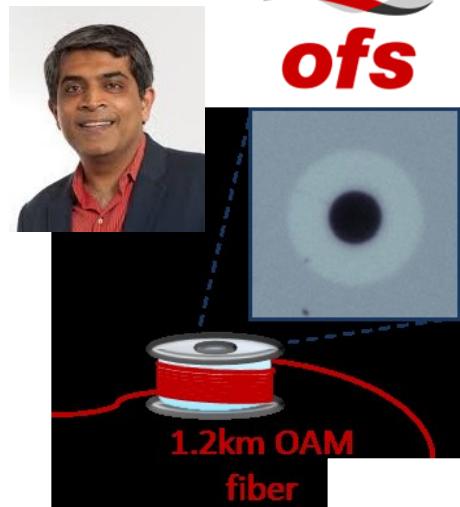


High-dimensional intracity quantum cryptography with structured photons

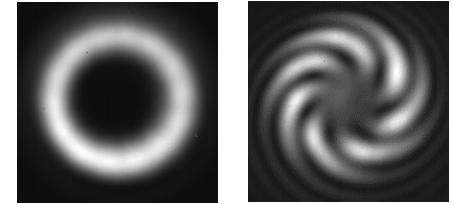
ALICIA SIT,¹ FRÉDÉRIC BOUCHARD,¹ ROBERT FICKLER,¹ JÉRÉMIE GAGNON-BISCHOFF,¹ HUGO LAROCQUE,¹ KHBAT HESHAMI,² DOMINIQUE ELSER,^{3,4} CHRISTIAN PEUNTINGER,^{3,4} KEVIN GÜNTHER,^{3,4} BETTINA HEIM,^{3,4} CHRISTOPH MARQUARDT,^{3,4} GERD LEUCHS,^{1,3,4} ROBERT W. BOYD,^{1,5} AND EBRAHIM KARIMI^{1,6,*} 



HOM fibre for QCs



Loss : ~ 1 dB/km



Terabit-Scale Orbital Angular Momentum Mode Division Multiplexing in Fibers, **S. Ramachandran, A. Willner groups**

Science 2013, **340** (6140), DOI: 10.1126/science.1237861

Mode Division Multiplexing Using Orbital Angular Momentum Modes Over 1.4-km Ring Core Fiber **Uni. Laval**,

Journal of Lightwave Technology 34(18), 2016, DOI: 10.1109/JLT.2016.2594698

18 km low-crosstalk OAM + WDM transmission with 224 individual channels enabled by a ring-core fiber with large high-order mode group separation, **Siyuan Yu group**

Optics Letters **43**(8), 2018 DOI: 10.1364/OL.43.001890

12 mode, WDM, MIMO-free orbital angular momentum transmission, **DTU, BU, OFS, Uni.Napoli**

Optics Express **26** (16) 2018, DOI: 10.1364/OE.26.020225

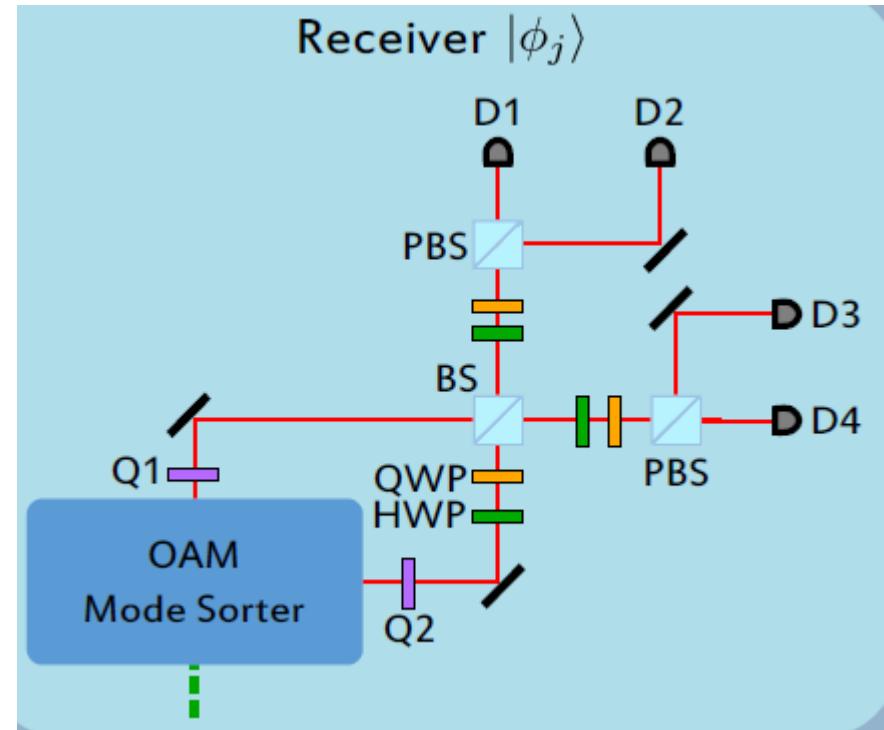
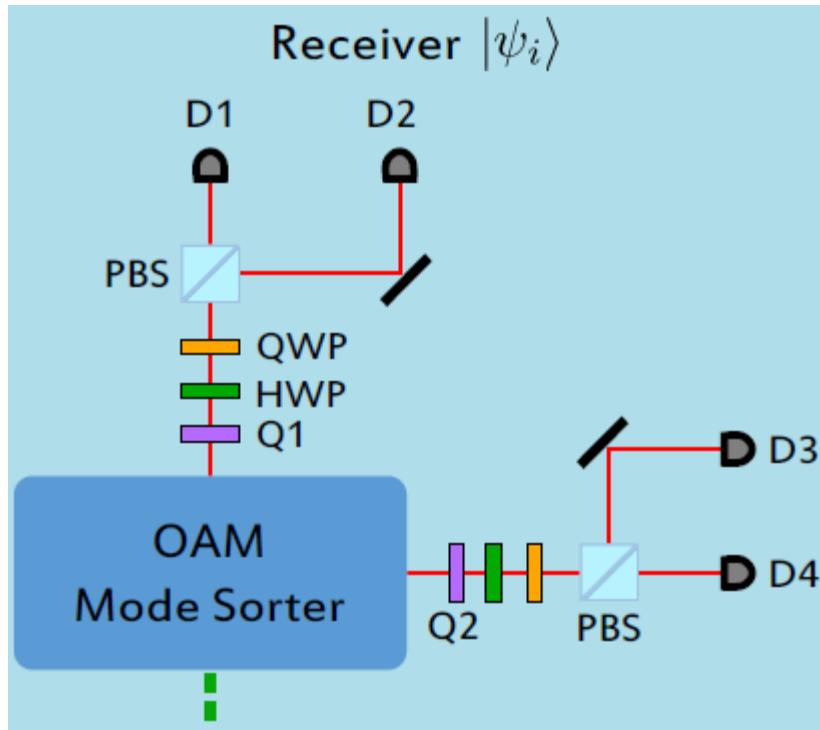
Orbital Angular Momentum

Conserved: OAM more robust against mode-mixing

Fibre based QCs with twisted photons

Vortex half plate (q-plate)

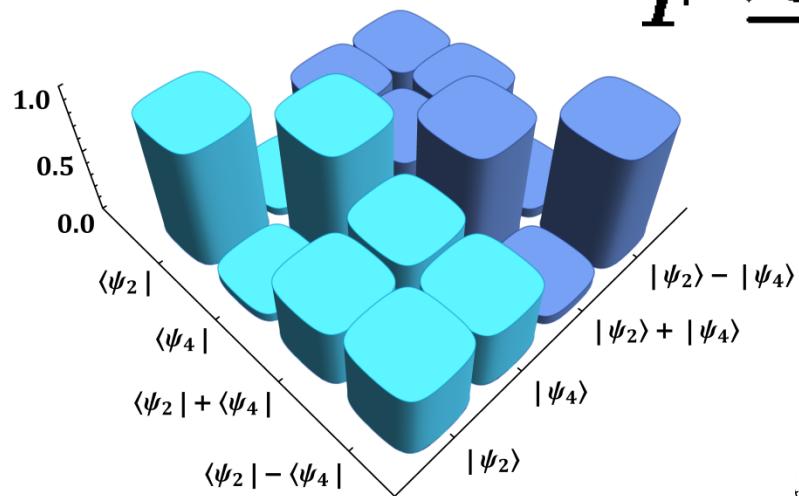
L. Marrucci et al., P.R.L. 96.16 (2006)



Results with OAM fibre

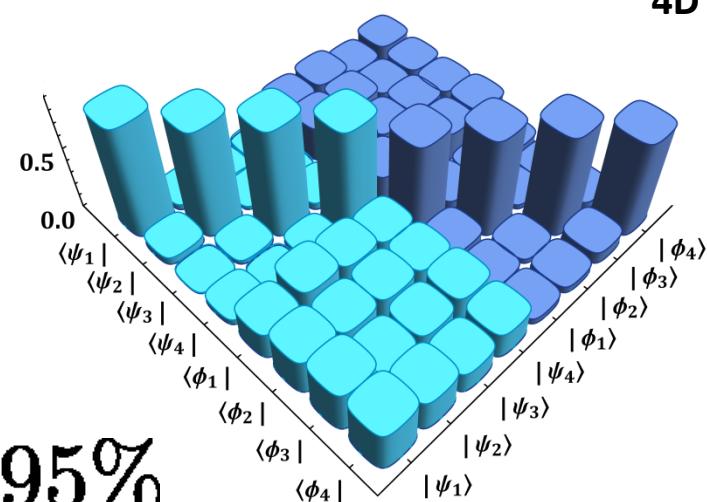
2D

$$F \simeq 98\%$$

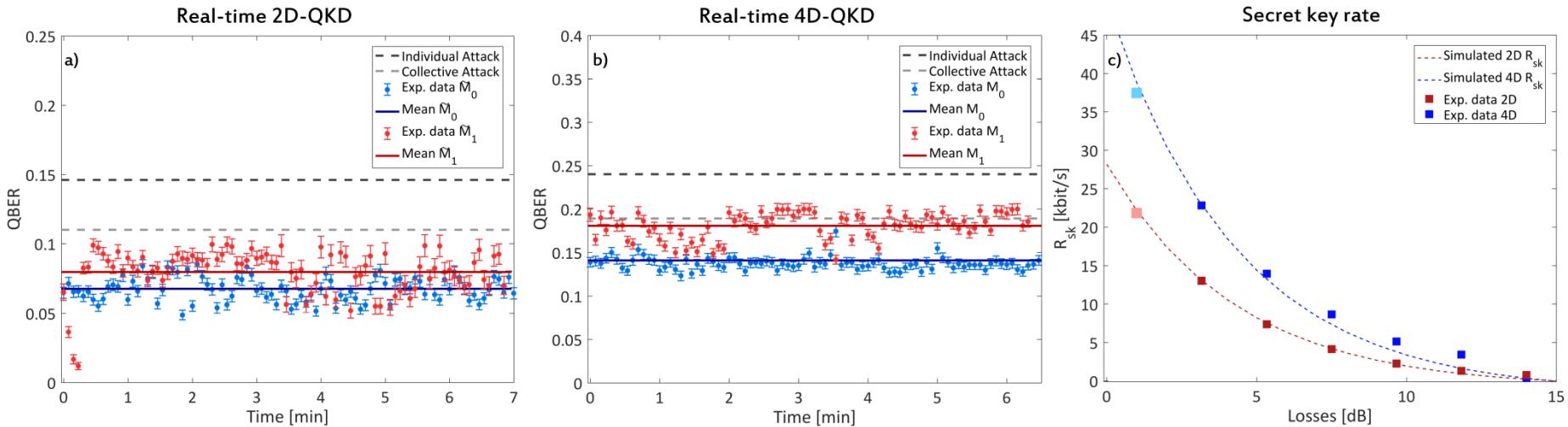


$$F \simeq 95\%$$

4D



Application Hi-D QKD (OAM)



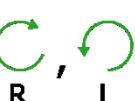
- First demonstration of Hi-D-QKD at 600 MHz using OAM fibre of 1.2 km
- Enhancement of 71% in key generation compared to 2D case
- Proved feasibility of OAM Quantum Communications in a fibre

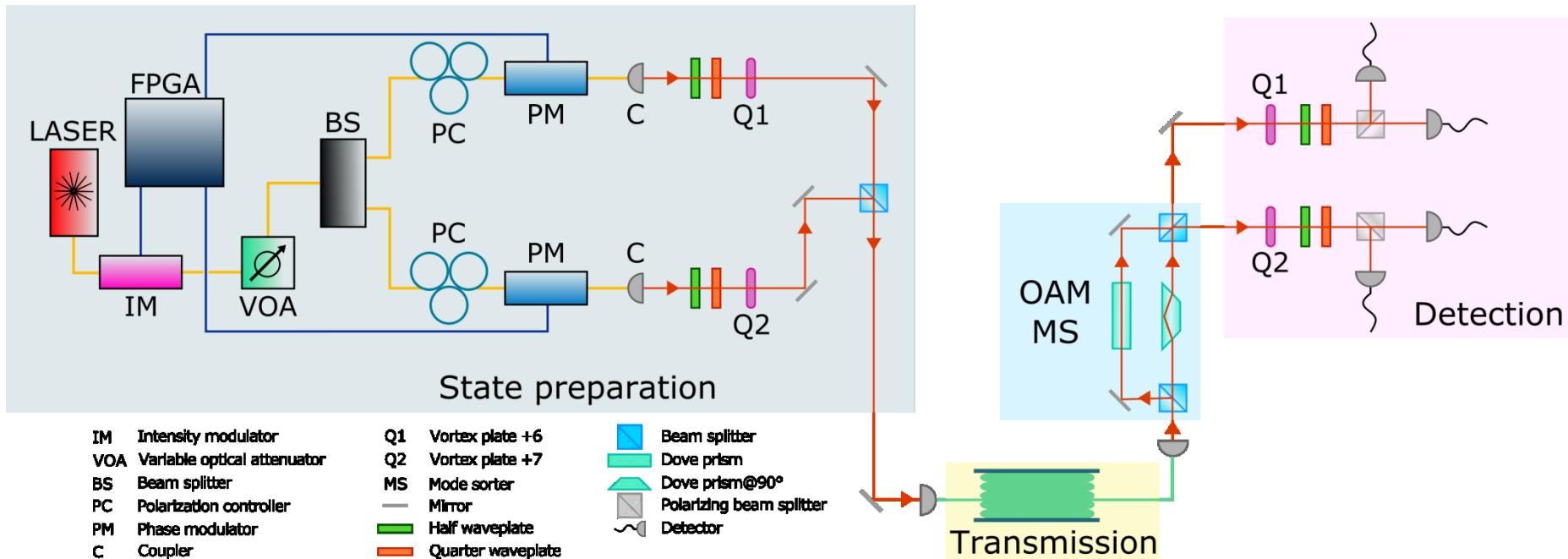
D.Cozzolino, D.Bacco, et al., PDP CLEO Pacific RIM (2018)

D. Cozzolino, D. Bacco et al., arXiv:1803.10138 [quant-ph]

OAM key multiplexing

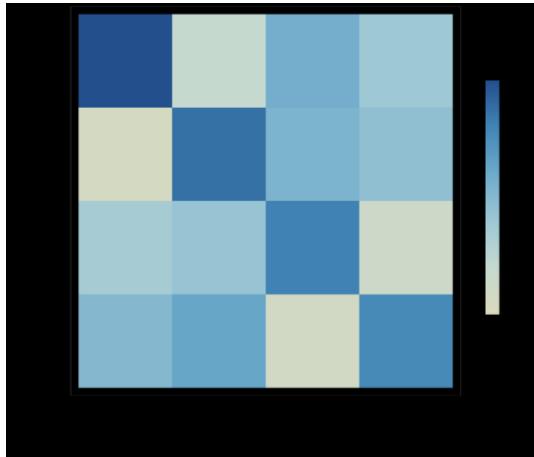
Independent decoy state BB84 QKD over OAM

OAM order mode	 $ \ell =6$	 $ \ell =7$
Z bases polarizations	 R, L	 R, L
X bases polarizations	 D, A	 D, A



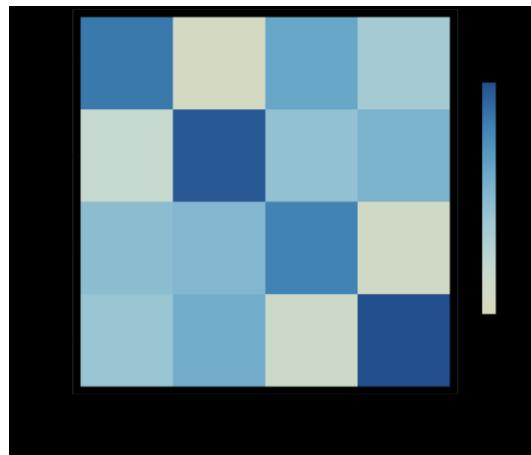
Experimental results MUX OAM

MODE 7

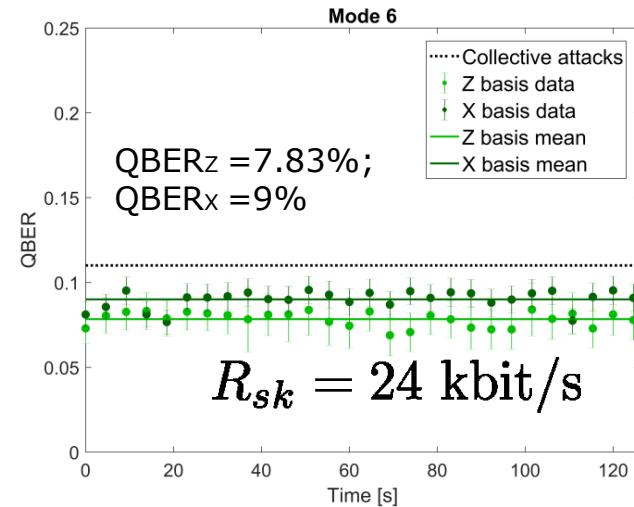
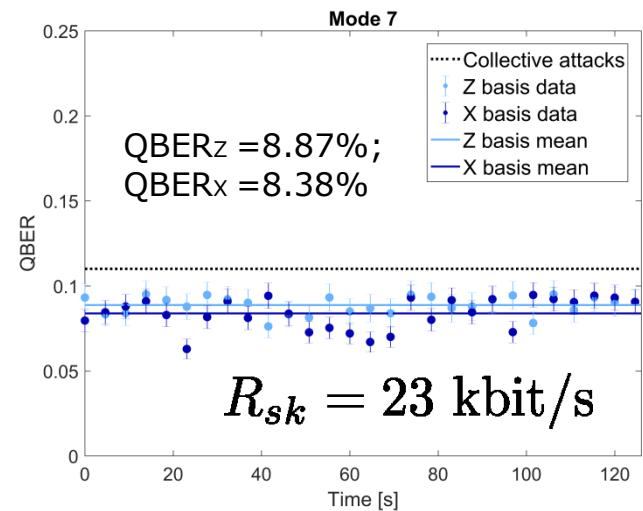


$$F \simeq 96.6\%$$

MODE 6



$$F \simeq 96.7\%$$



Chip-to-chip key multiplexing

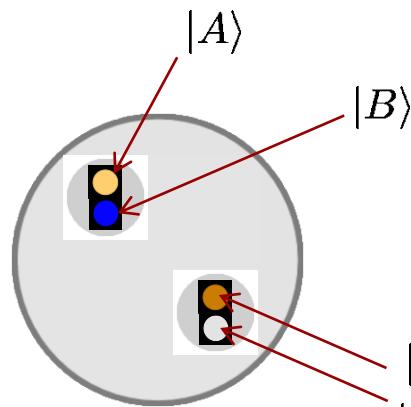
Independent decoy state BB84 QKD over MCF

Base 1

$$\begin{pmatrix} |A\rangle \\ |B\rangle \end{pmatrix}$$

Base 2

$$\begin{pmatrix} |A+B\rangle \\ |A-B\rangle \end{pmatrix}$$

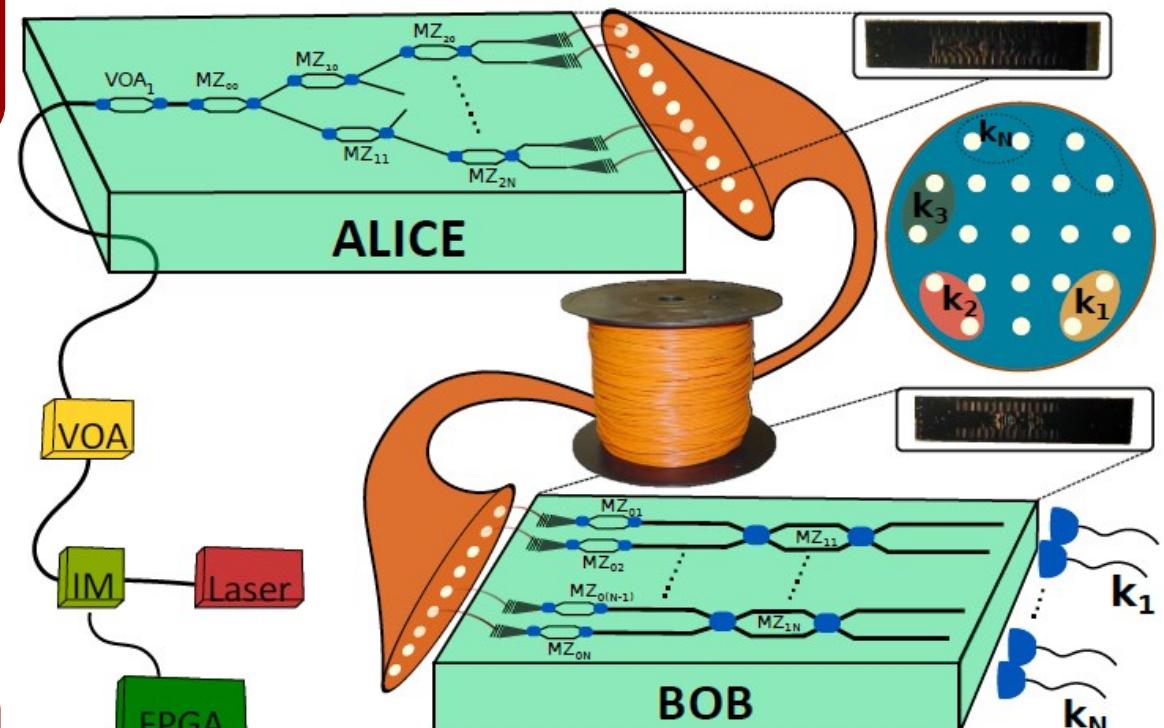


Base 1

$$\begin{pmatrix} |C\rangle \\ |D\rangle \end{pmatrix}$$

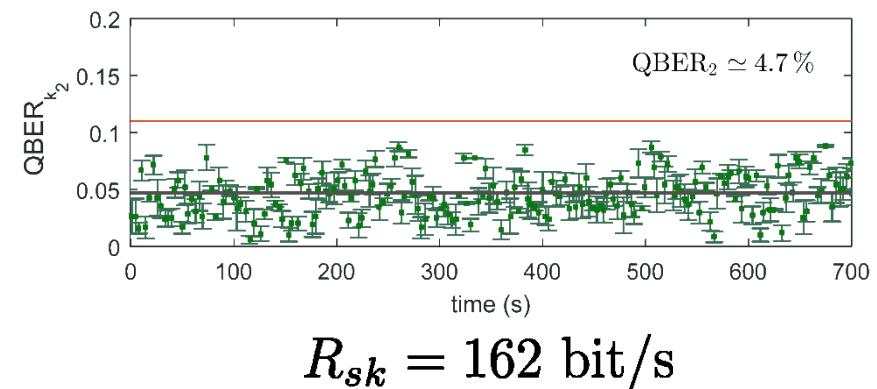
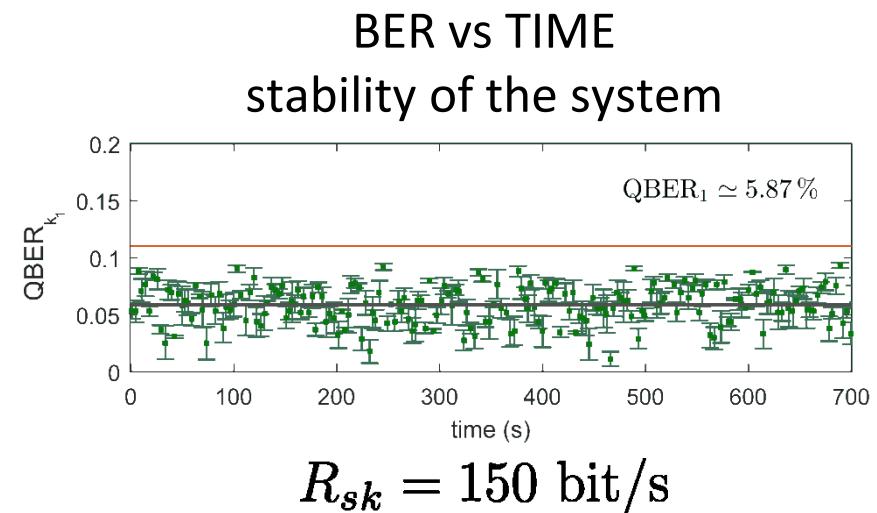
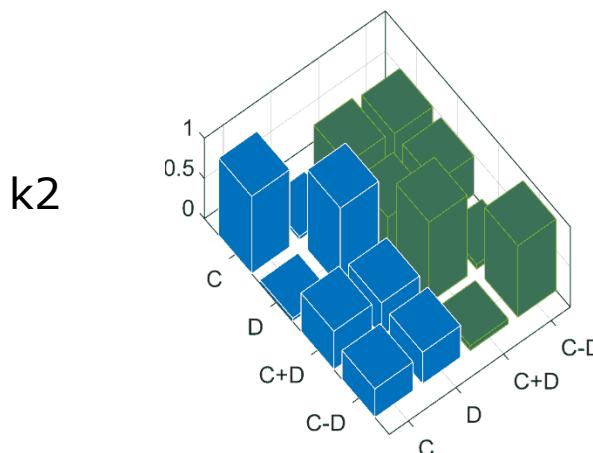
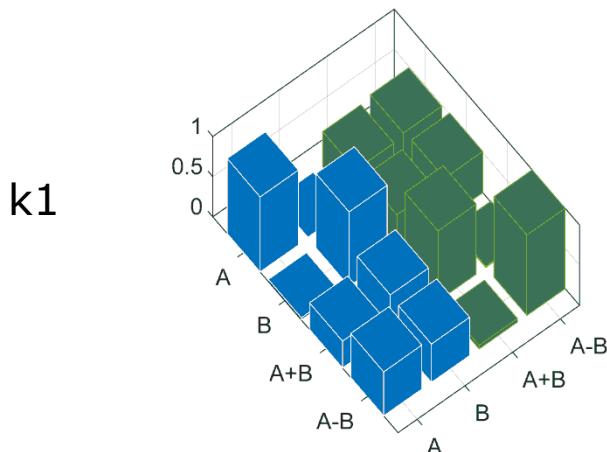
Base 2

$$\begin{pmatrix} |C+D\rangle \\ |C-D\rangle \end{pmatrix}$$

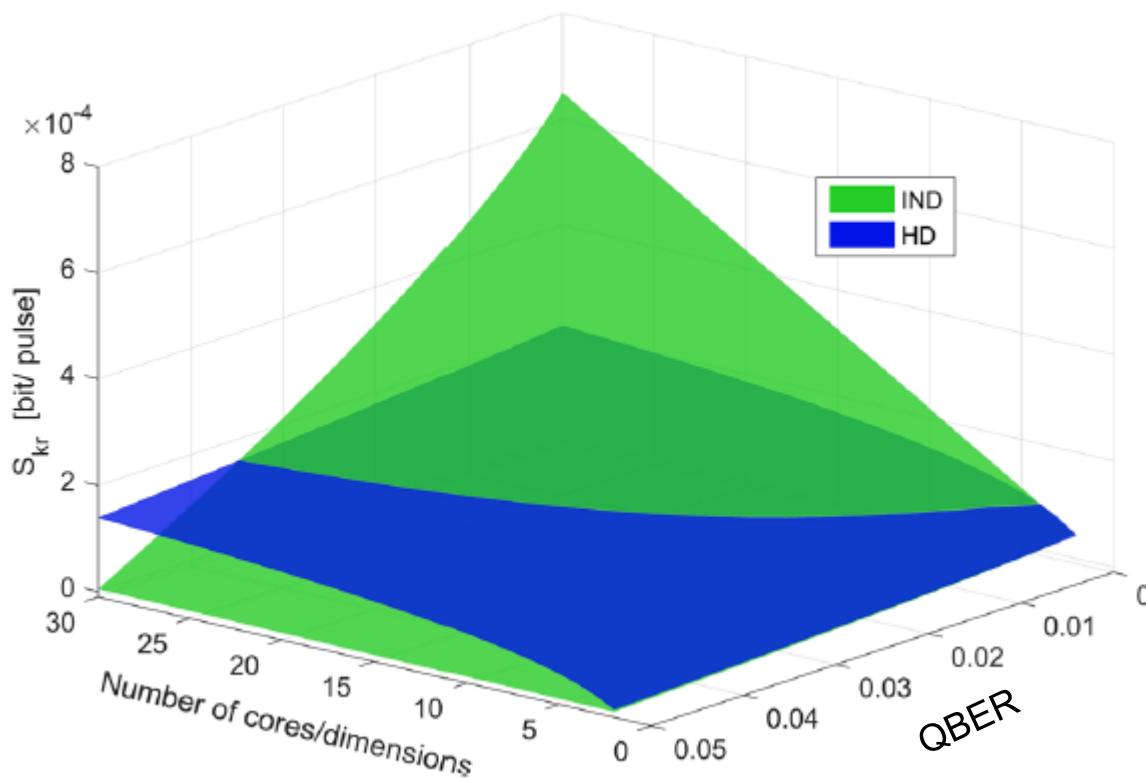


Experimental results MUX MCF

- SDM: Two parallel decoy state BB84 protocol



Comparison HD-QKD and keys MUX



- High noise HD gain compared to IND
- Low noise better to use MUX technique

Conclusions

- space encoding qudits can be transferred over fibre
 - demonstration of a ququart through a MCF
 - first transmission of a ququart over an OAM fibre
- applications of qudits
 - Decoy state chip-to-chip Hi-D QKD over MCF fibre
 - Decoy state Hi-D QKD over 1.2 km OAM fibre
- Hi-D or keys multiplexing?
 - low channel noise convenient key MUX
 - high noise, only qudits allow key distillation

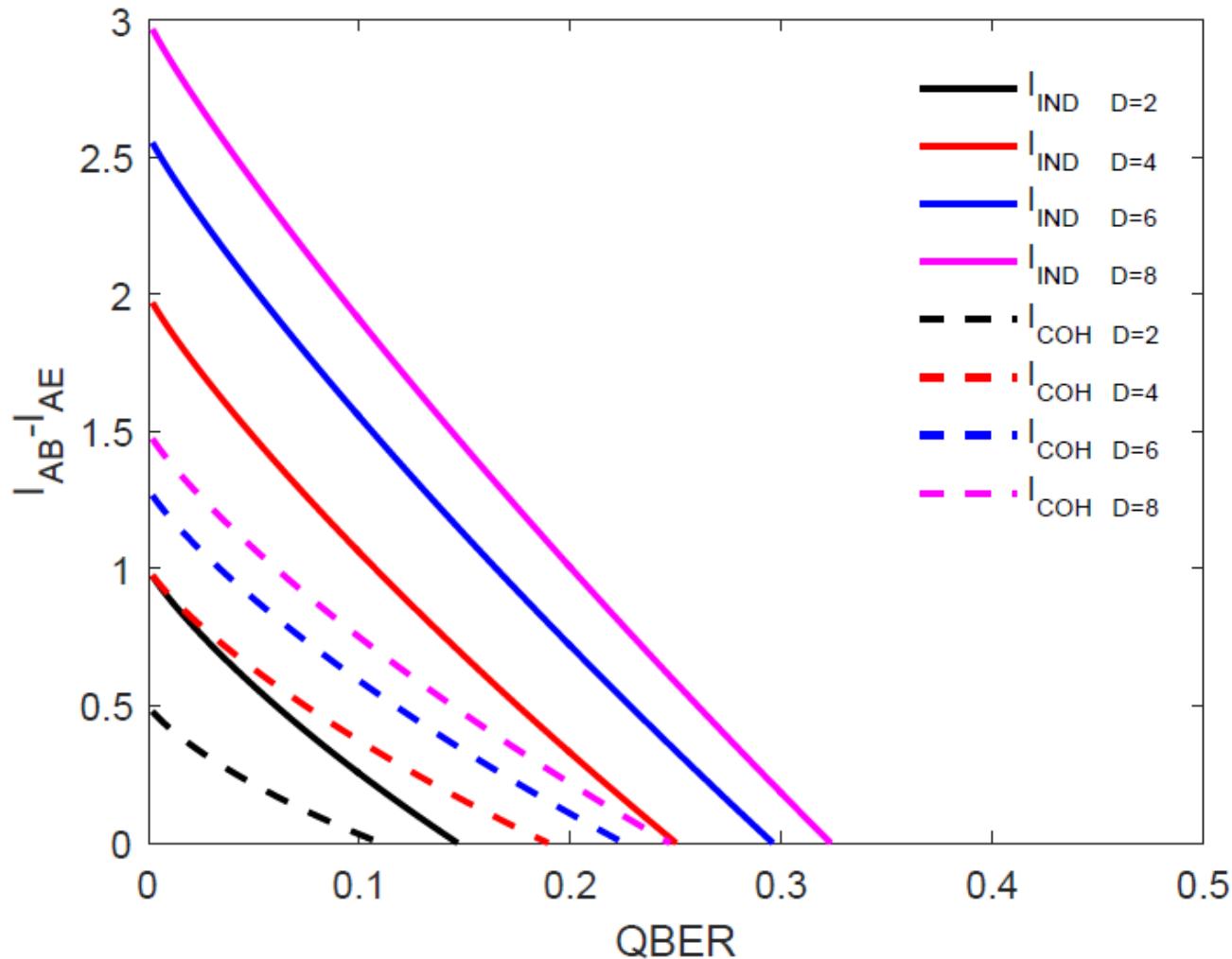


**Thanks
for
your
attention!**

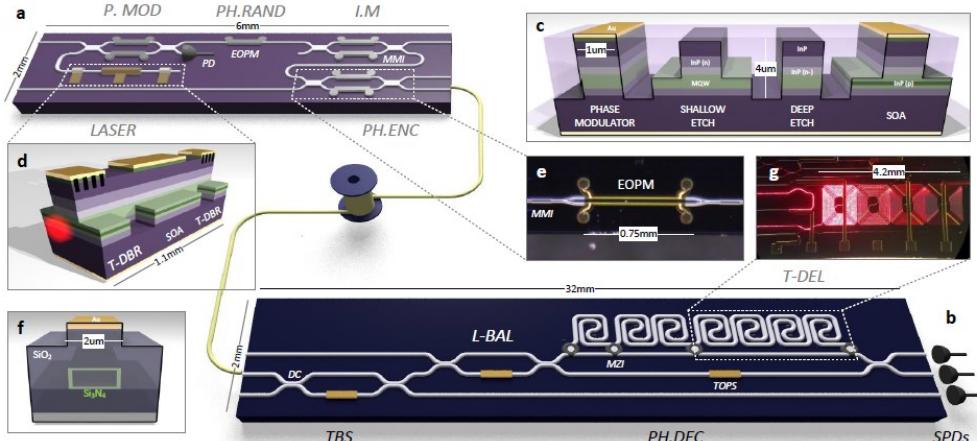
Additional Slides

Qudits encoding

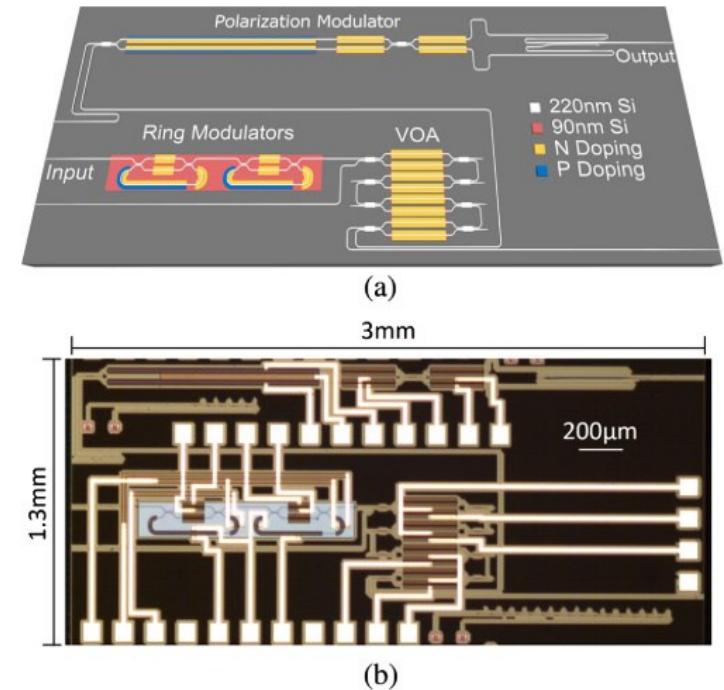
More robust against noise [N. J. Cerf, et al., *P.R.L.*, 88(12) 2002]



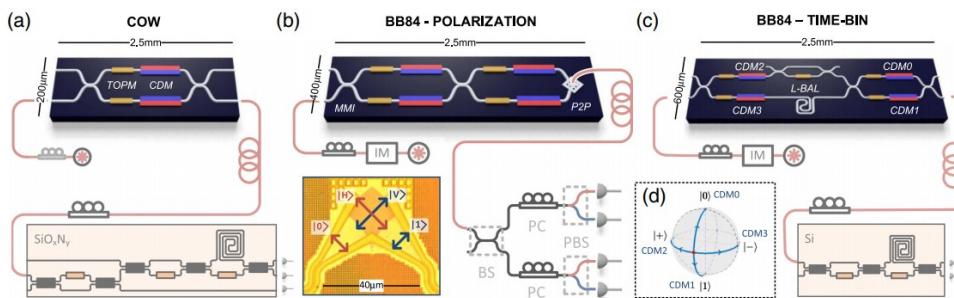
Integrated devices for QCs



P. Sibson et al., Nat. Commun. 8:13984 (2017)

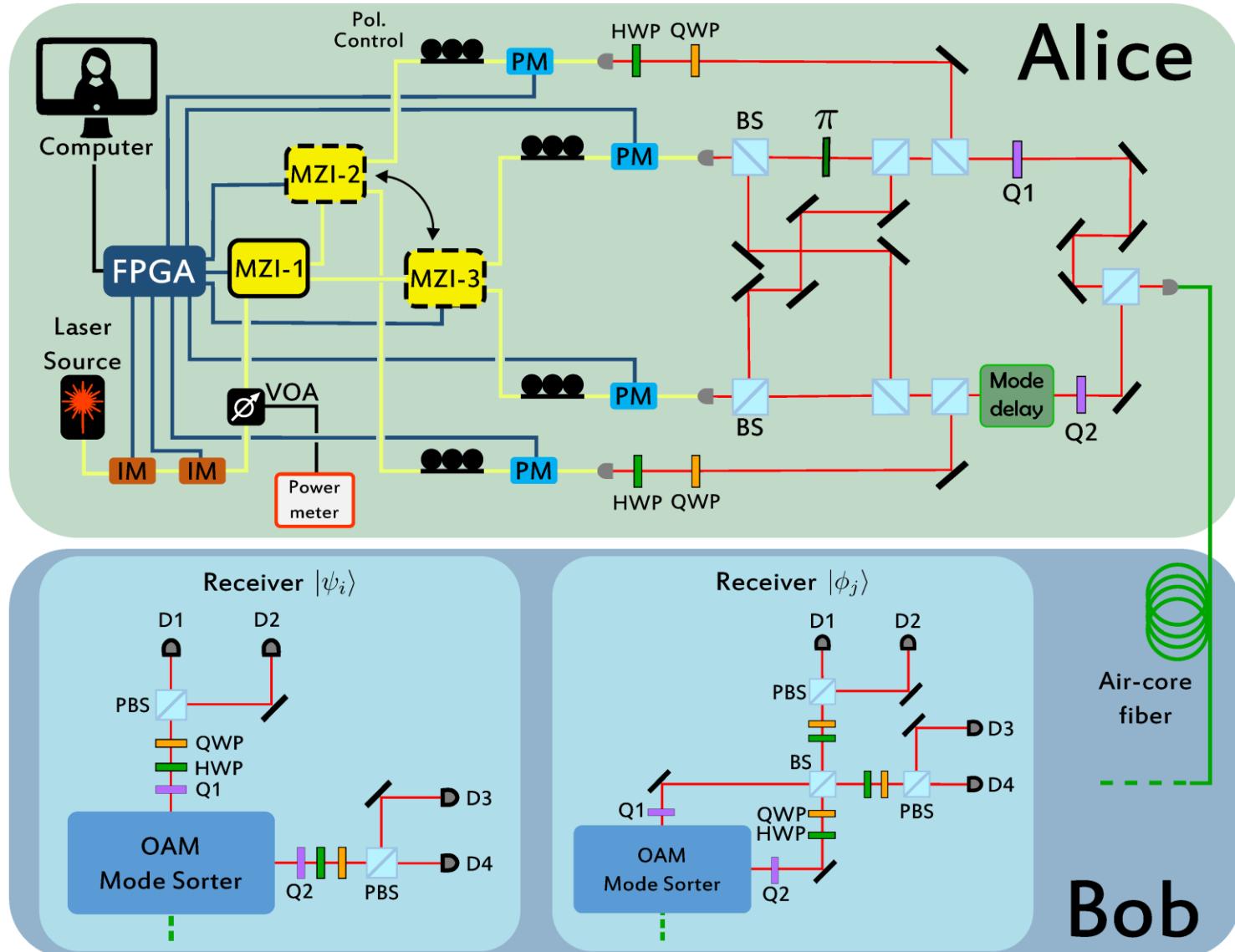


C. Ma et al, Optica 3, 1274-1278 (2016)

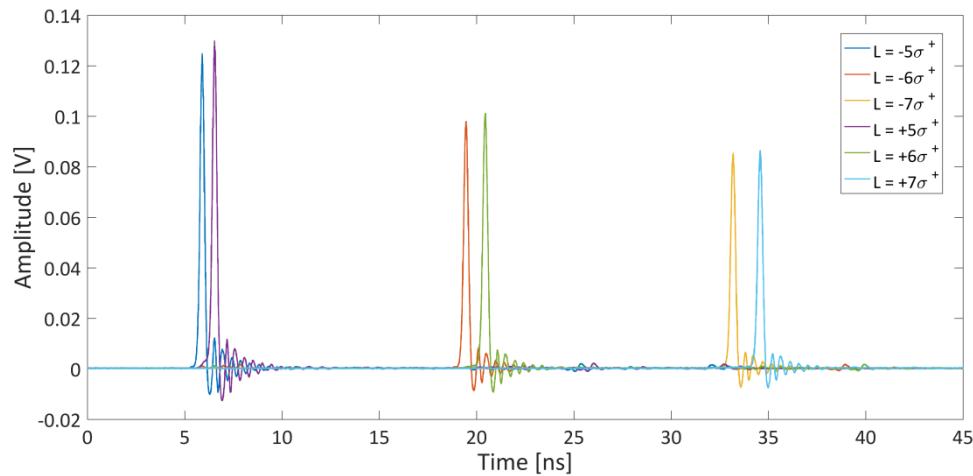
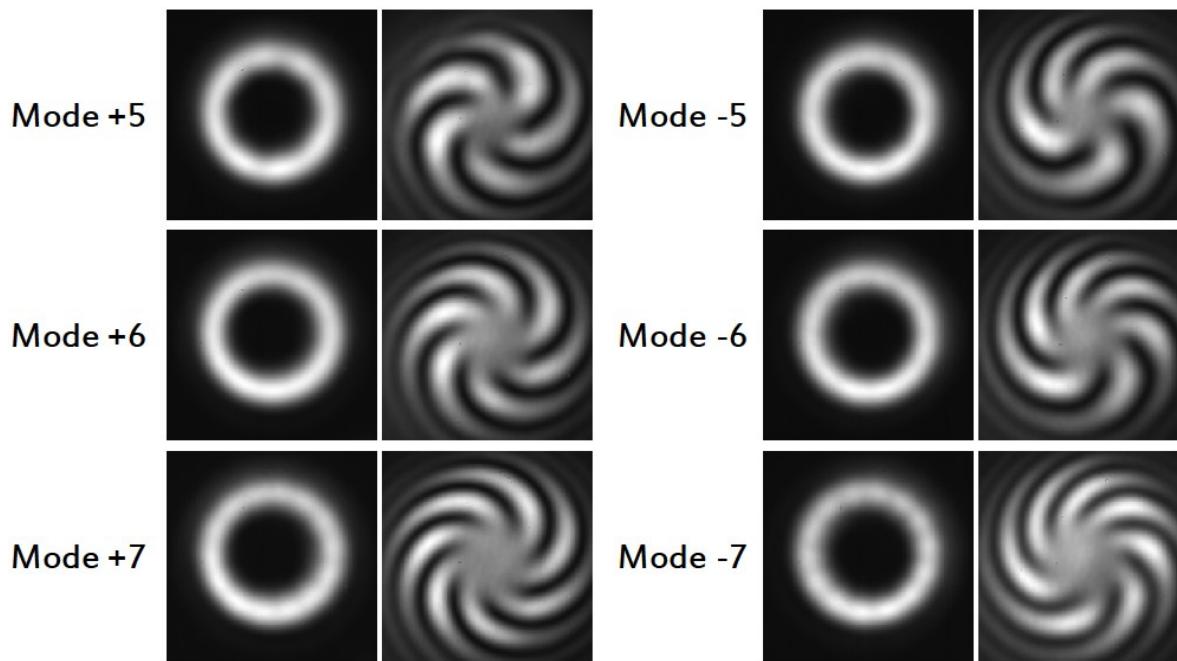


P. Sibson et al, Optica 4, 172-177 (2017)

Main setup OAM



Modes characterization



Experimental Results Hi-D OAM

Stability measurement in the M0 basis

