

# PROOF-OF-PRINCIPLE QUANTUM KEY DISTRIBUTION IMMUNE TO DETECTOR ATTACKS

Allison Rubenok, Joshua A. Slater, Philip Chan,  
Itzel Lucio-Martinez & Wolfgang Tittel

Institute for Quantum Information Science  
University of Calgary, Canada

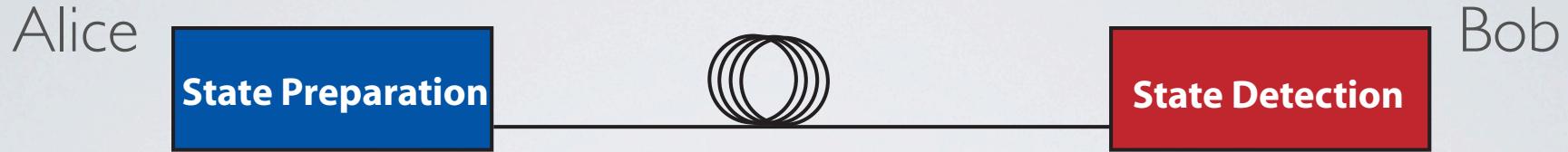


Institute for  
**Quantum Information Science**  
at the University of Calgary



QCrypt 2012 - Sept 10 2012

# QUANTUM KEY DISTRIBUTION



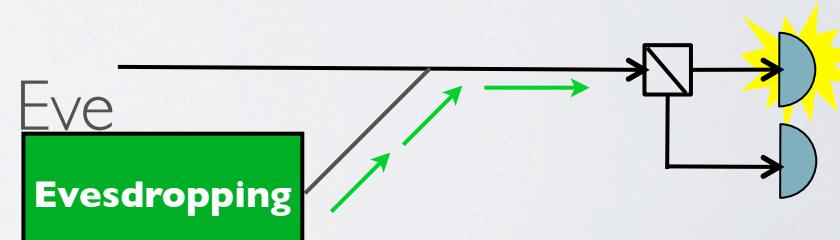
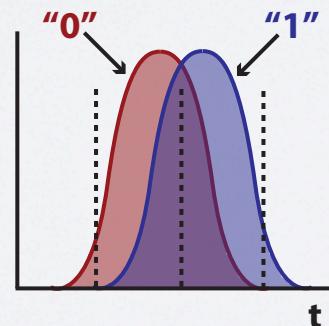
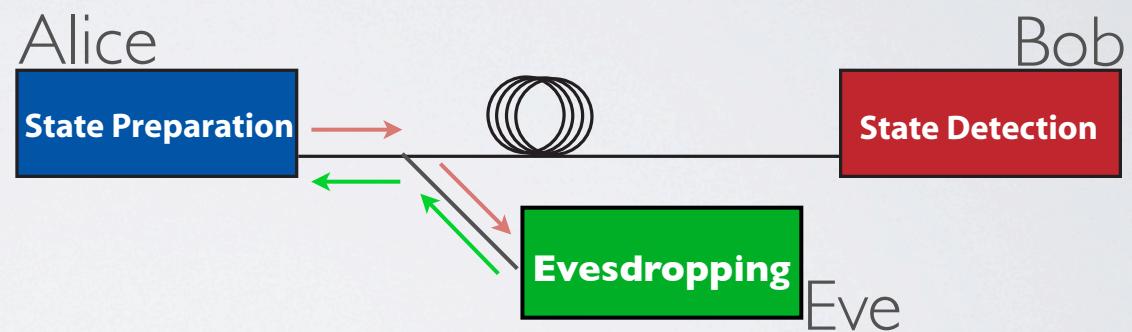
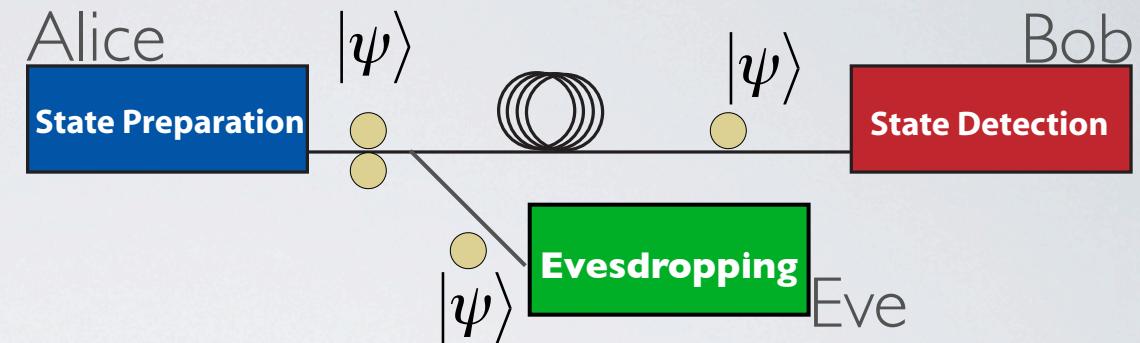
- Experimental (level 2):
  - 100s of km of optical fibre
  - 100 km through free space
- Trusted node networks: Tokyo, Swiss, SECOQC, DARPA
- Commercial Products: idQuantique, MagiQ

# SIDE-CHANNEL ATTACKS

Photon Number Splitting  
Counter:  
Decoy Analysis

Trojan Horse  
Counter:  
Optical Isolators

Detector Weaknesses  
i.e. time-shift attack  
or blinding & faked states  
Counter:  
Robust Detectors



# SIDE-CHANNEL ATTACKS

Photon Number Splitting

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Decoy Analysis

Trojan Horse

Can we implement QKD such that it is secure against any known or yet-to-be-proposed side-channel attack??

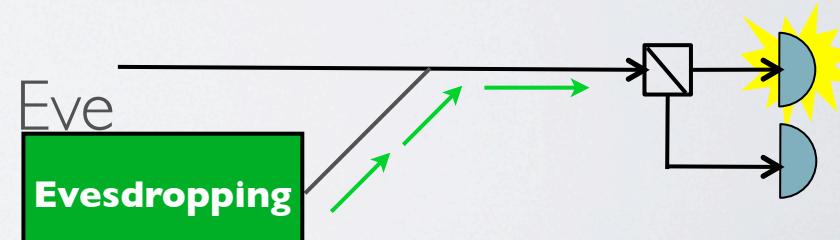
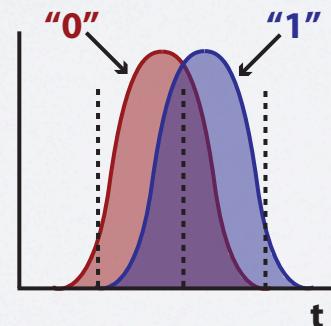
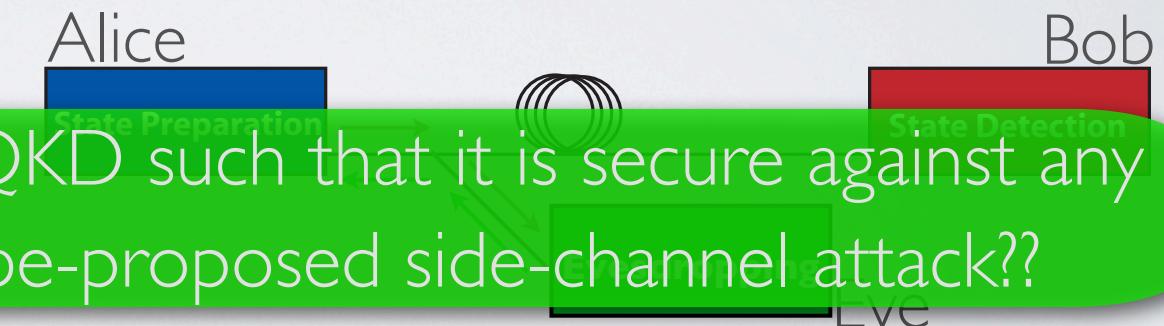
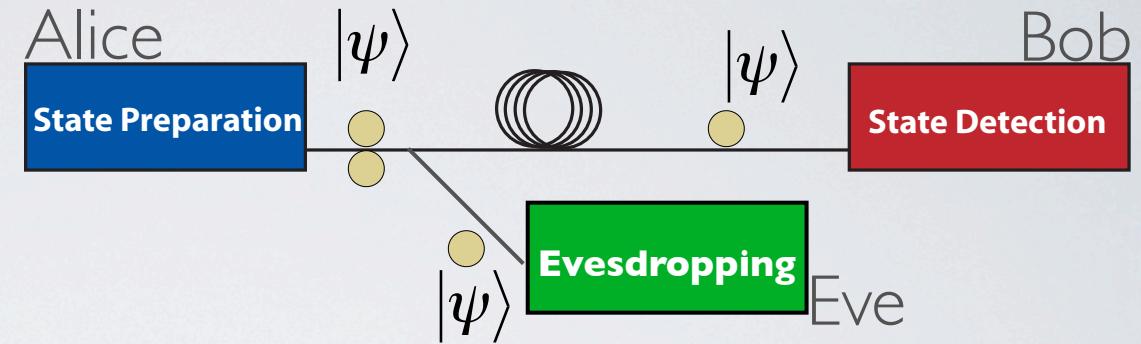
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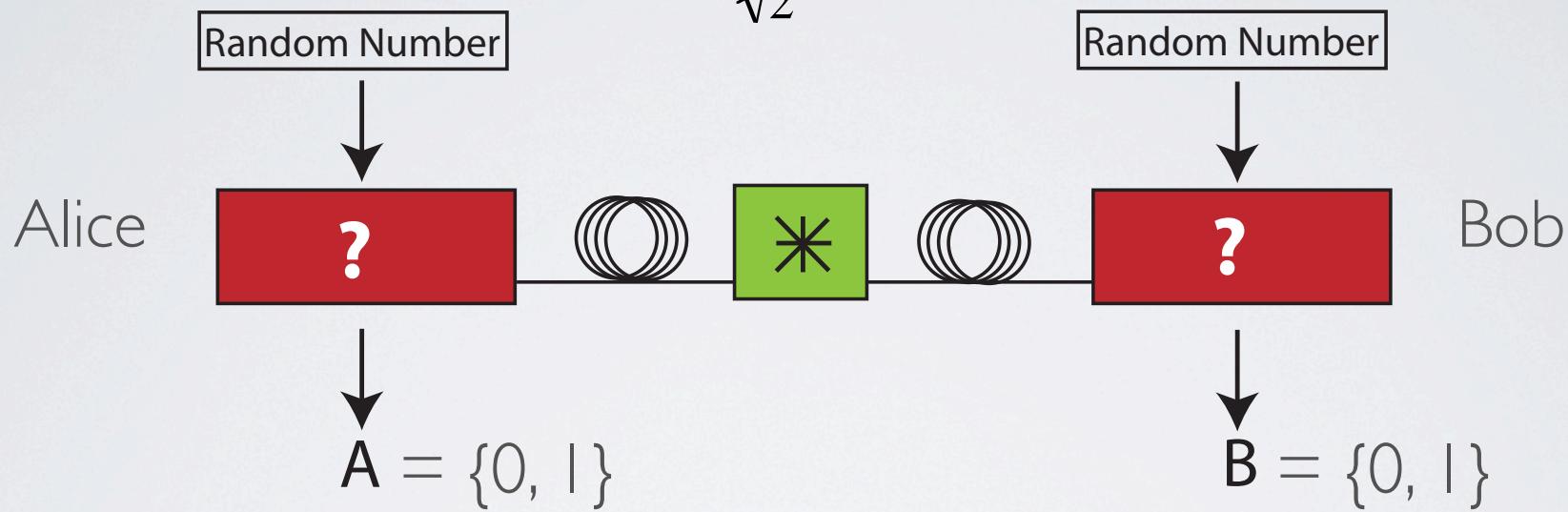
Robust Detectors



# DEVICE-INDEPENDENT QKD

Protection against side-channel attacks:

$$|\psi^-\rangle = \frac{1}{\sqrt{2}}(|01\rangle - |10\rangle)$$



Requires:

- qubit projection measurements, entanglement source
- loophole-free Bell Test

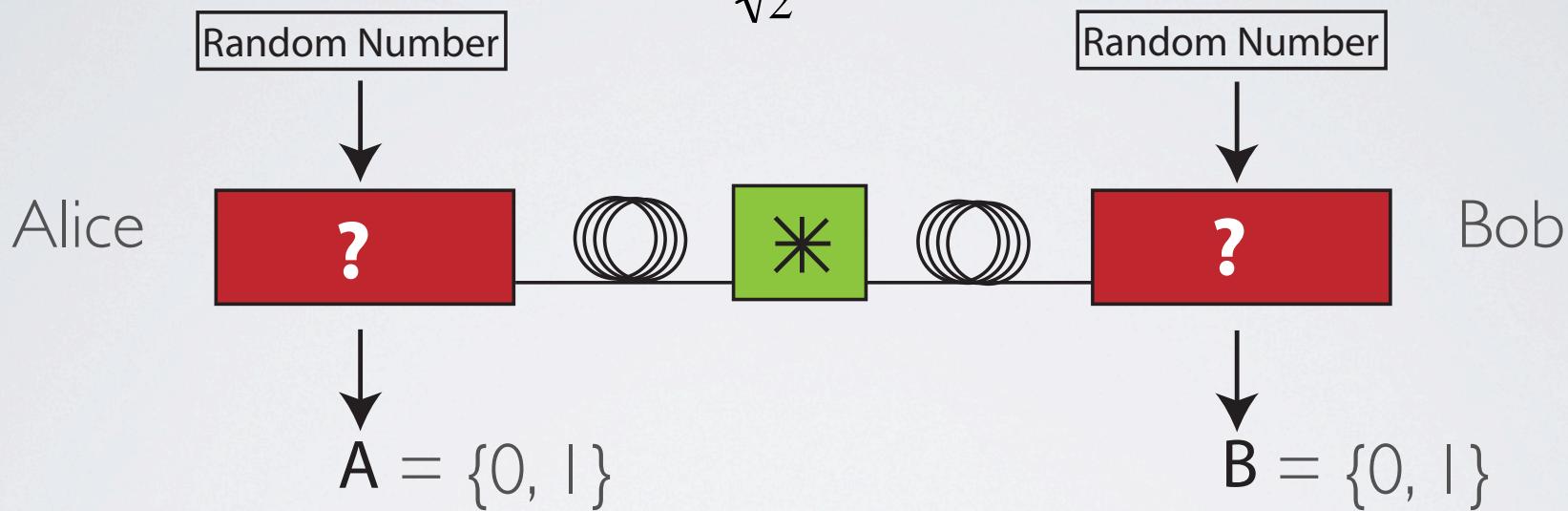
To produce secret key:

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Currently Infeasible:  
Detection Loophole

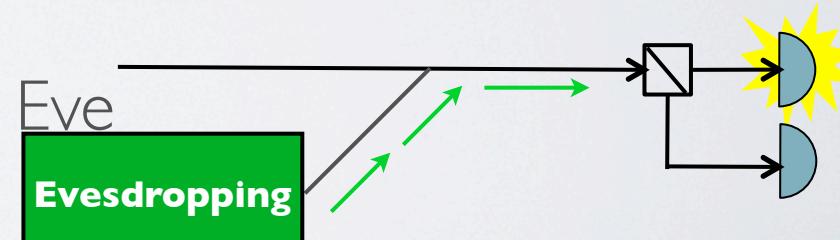
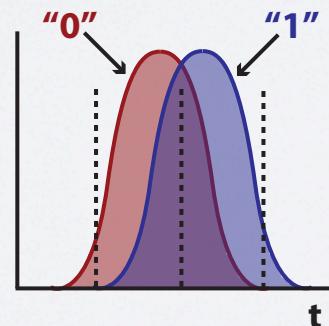
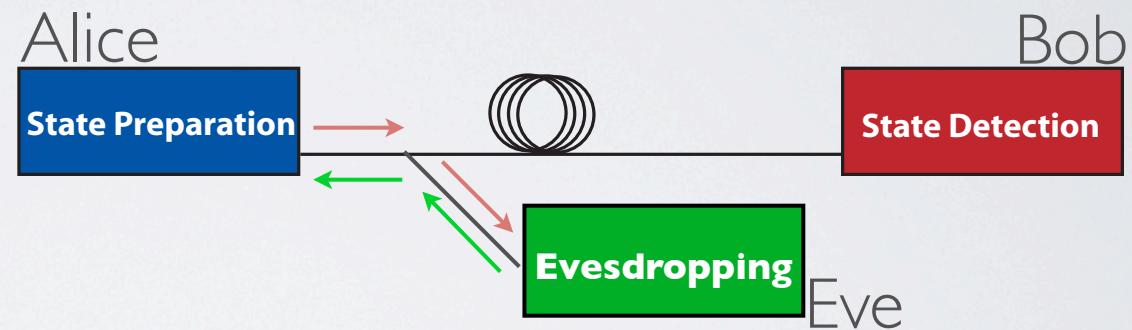
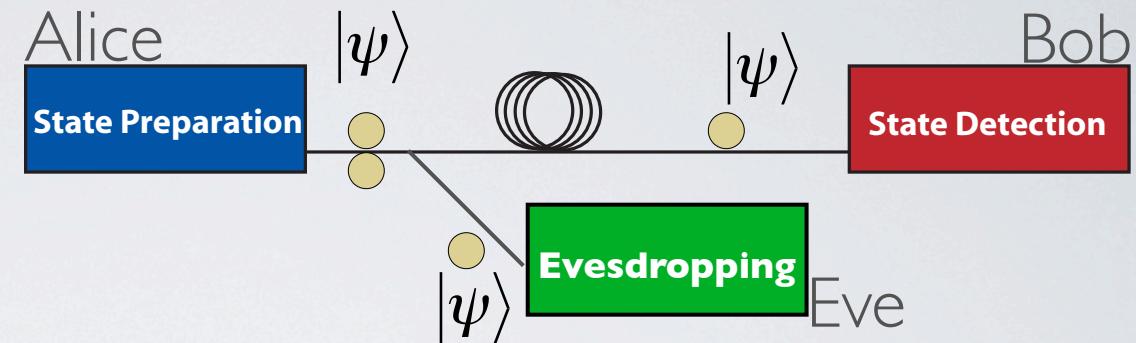
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Detector Weaknesses  
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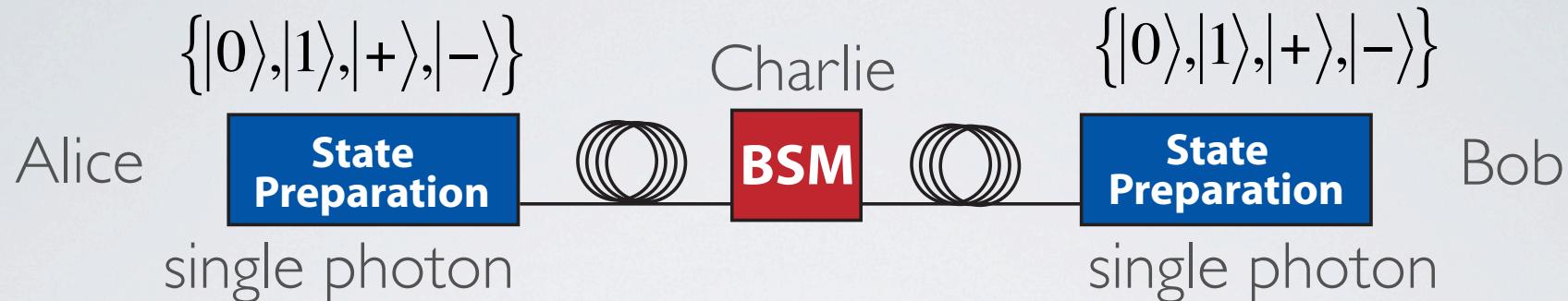
Counter:  
Robust Detectors?  
Or New Protocols?



# TABLE OF CONTENTS

- **New Protocol: MDI-QKD (level 3)**
- Experimental Demonstration
  - Setup
  - Results
- Conclusions

# NEW QKD PROTOCOL: TIME-REVERSED QKD



Requires:

$$|\psi^-\rangle = \frac{1}{\sqrt{2}}(|01\rangle - |10\rangle) = \frac{1}{\sqrt{2}}(|+-\rangle - |-+\rangle)$$

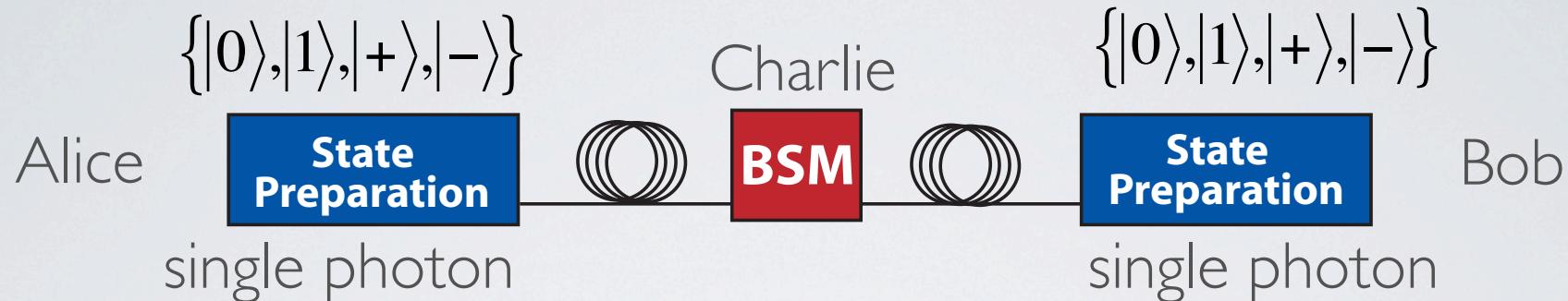
- Bell-state measurements
- single photon source

To produce secret key:

- Psi- projection & same bases implies different key bits
- sifting, Bob flip bits, error correction & privacy amplification

De-correlates detector response from secret key bits  
→ Immune to detector attacks

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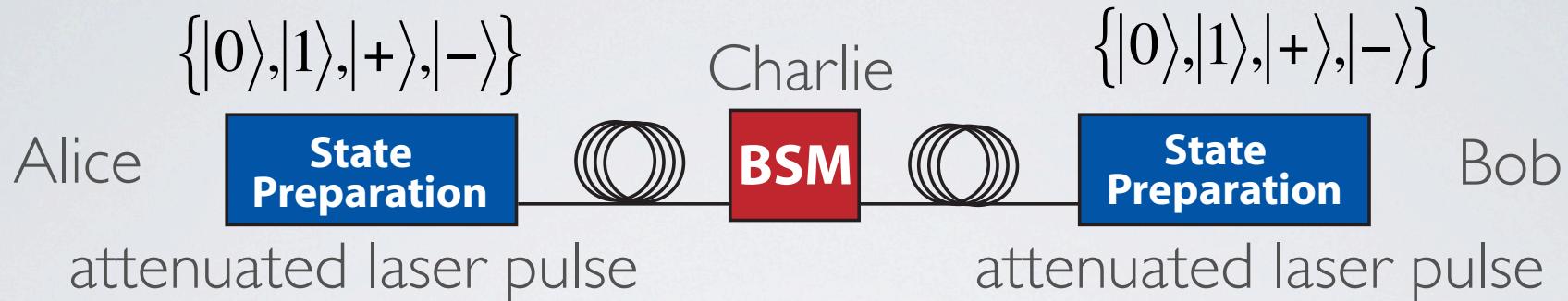
Currently Difficult

To produce secret key:

- Psi- projection & same bases implies different key bits
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De-correlates detector response from secret key bits  
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# MEASUREMENT DEVICE INDEPENDENT QKD (MDI-QKD)



$$|\psi^-\rangle = \frac{1}{\sqrt{2}}(|01\rangle - |10\rangle) = \frac{1}{\sqrt{2}}(|+-\rangle - |--\rangle)$$

Requires:

- Bell-state measurements
- random  $\mu$  variation (signal & decoy states) to avoid PNS

Decoy Analysis to assess:  $Q_{11}^Z, Q_{11}^X, e_{11}^Z, e_{11}^X$

To produce secret key:

- z-basis for key, x-basis for eavesdropping detection

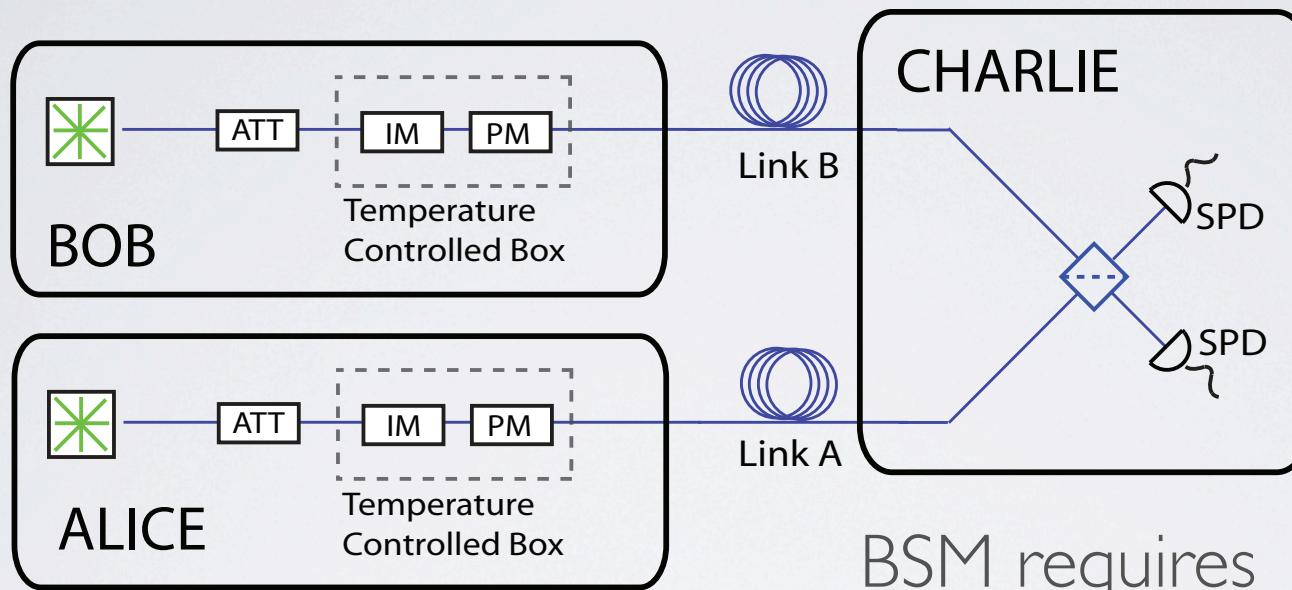
$$S = Q_{11}^z \left( 1 - h_2(e_{11}^x) \right) - Q_{\mu\mu}^z f h_2(e_{\mu\mu}^z)$$

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# EXPERIMENT

Achievable with present technology



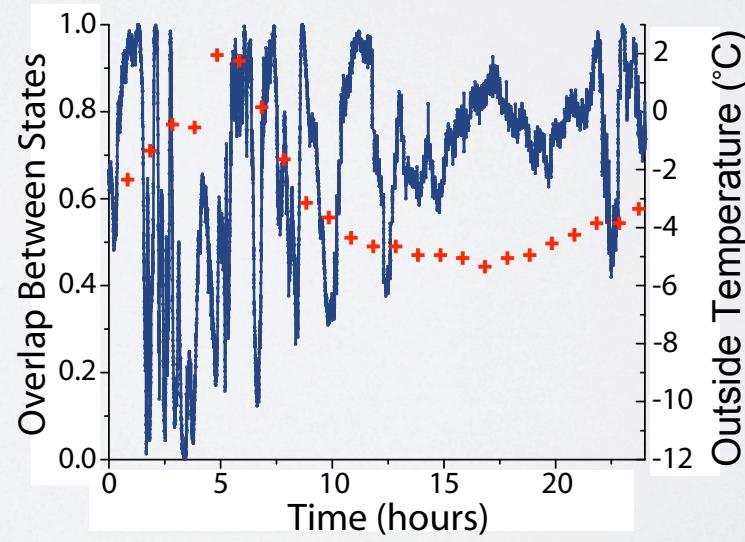
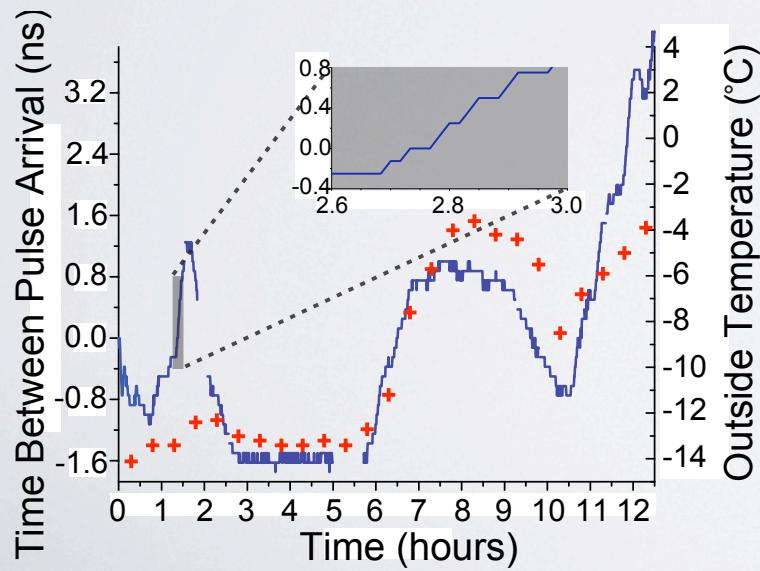
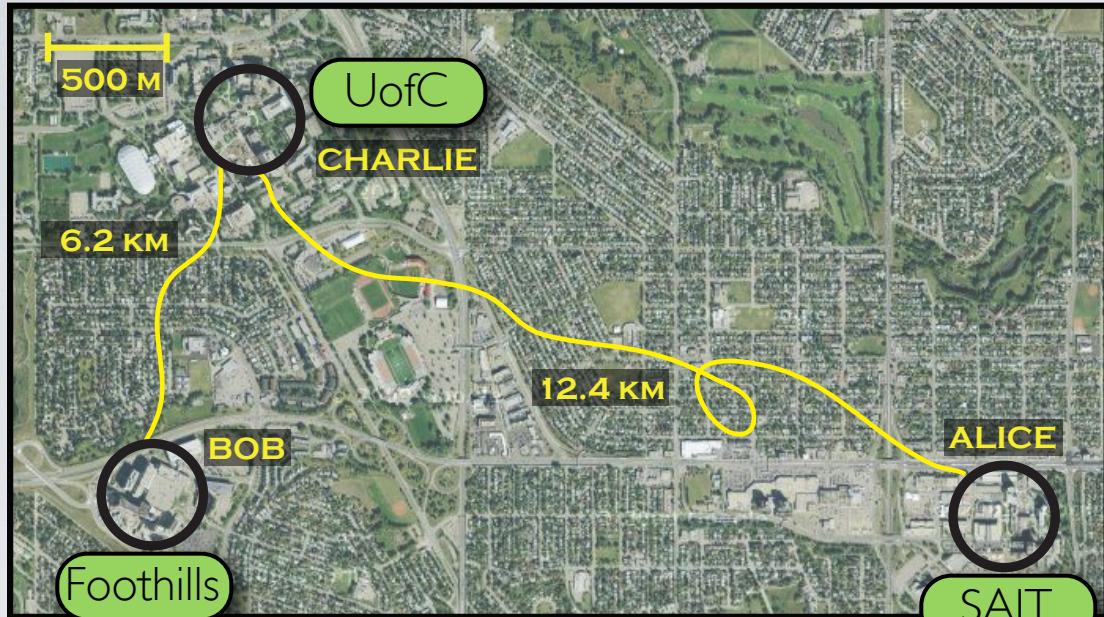
| 1550 nm time-bin qubits

- 500 ps FWHM, 1.4 ns time separation
- standard off-the-shelf telecommunication components
- pm fibre components (non-pm links)

BSM requires  
indistinguishable photons:

- temporal overlap
- polarization overlap
- spectral overlap
- spatial overlap

# EXPERIMENT

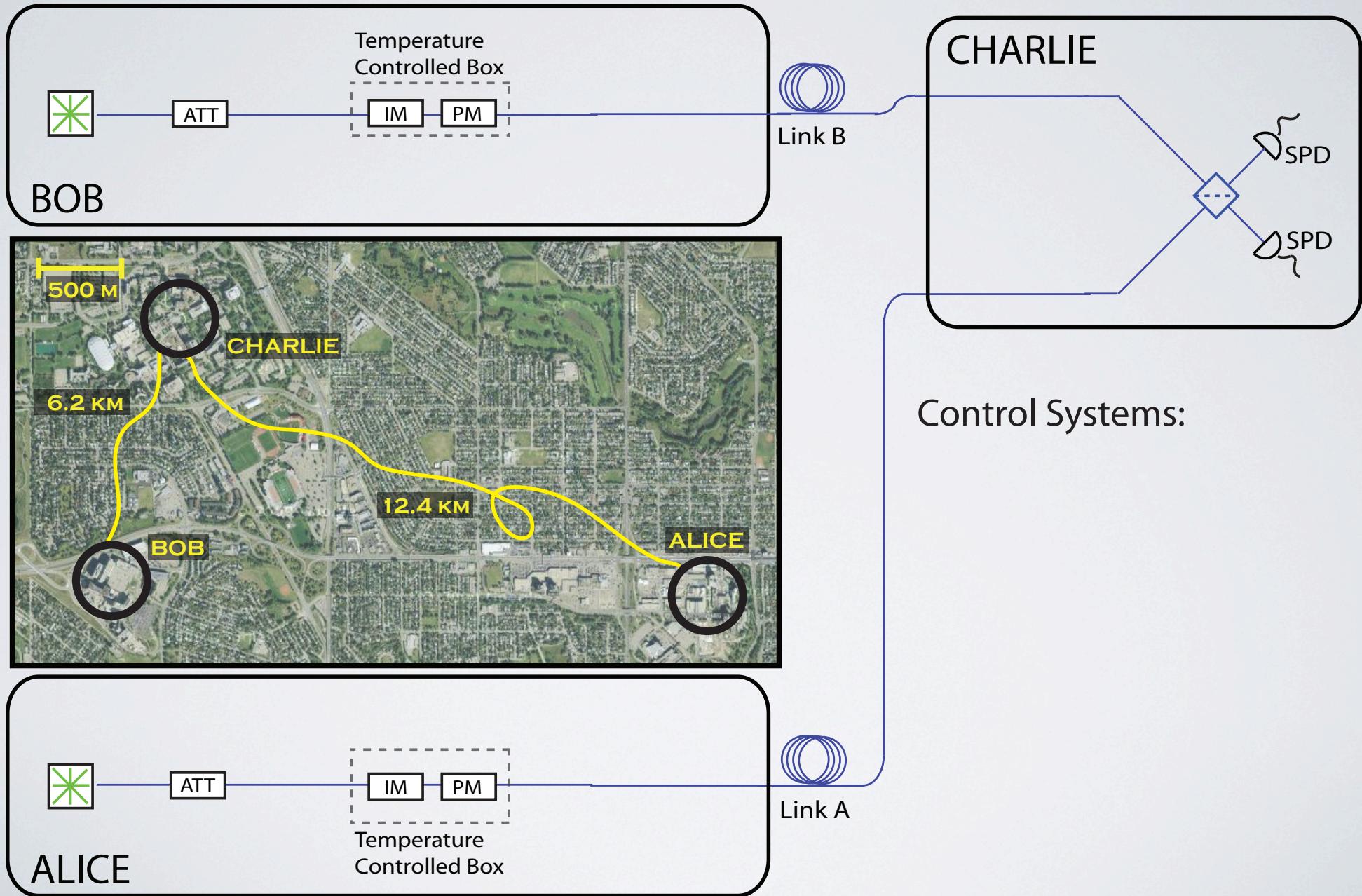


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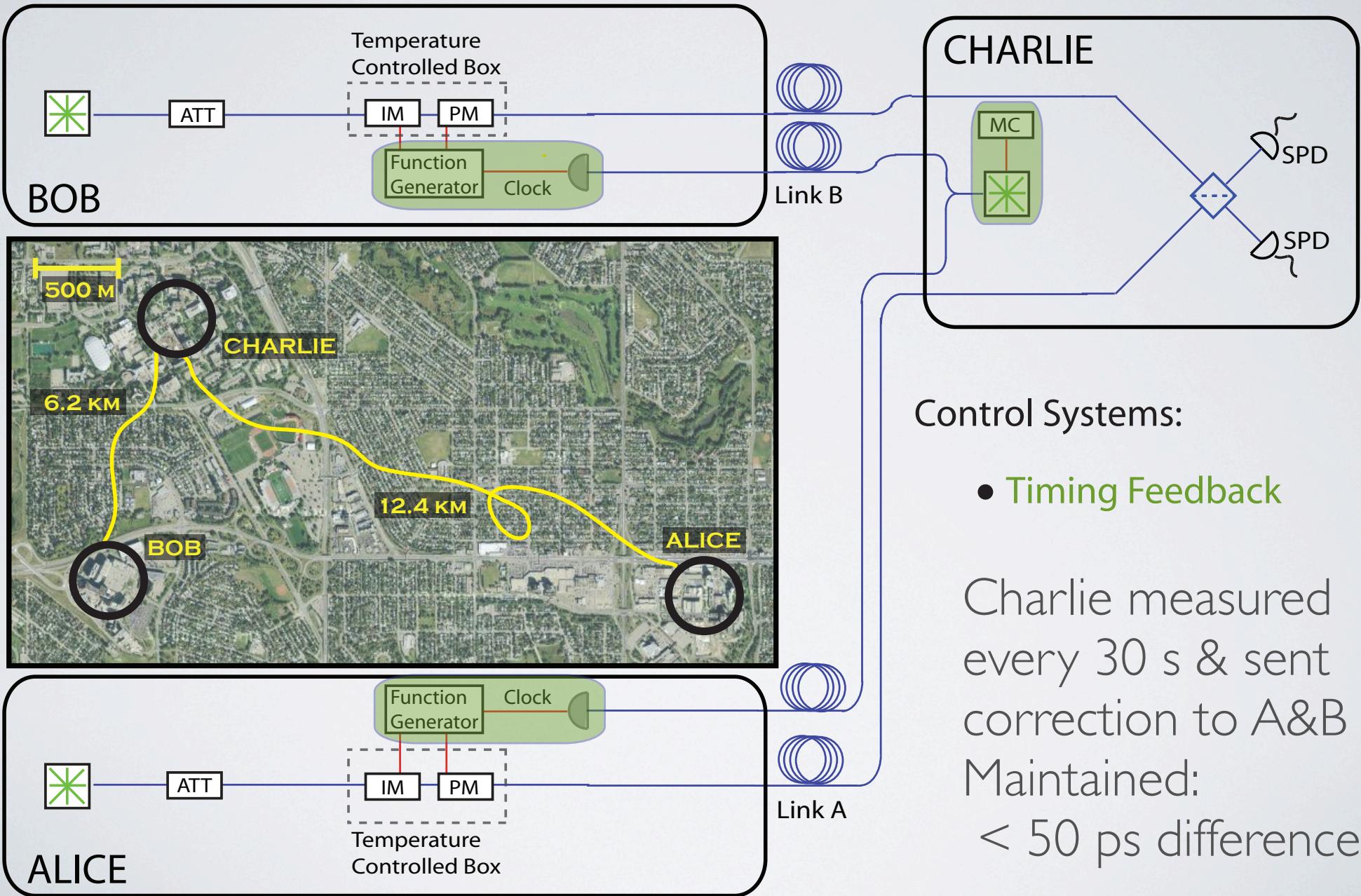
- temporal overlap
- polarization overlap
- spectral overlap
- spatial overlap

Also, relative frequency drift of 20 MHz/h

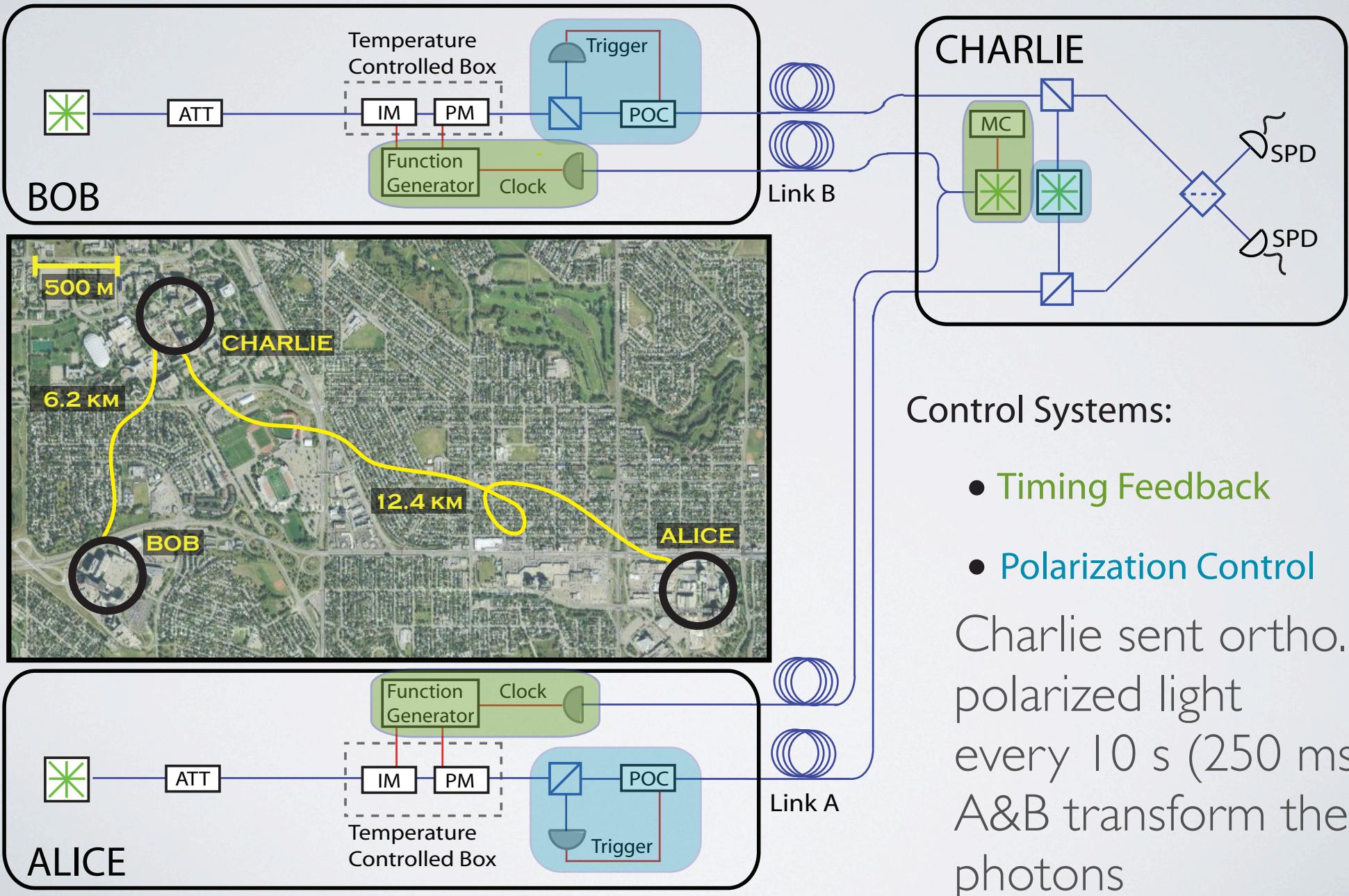
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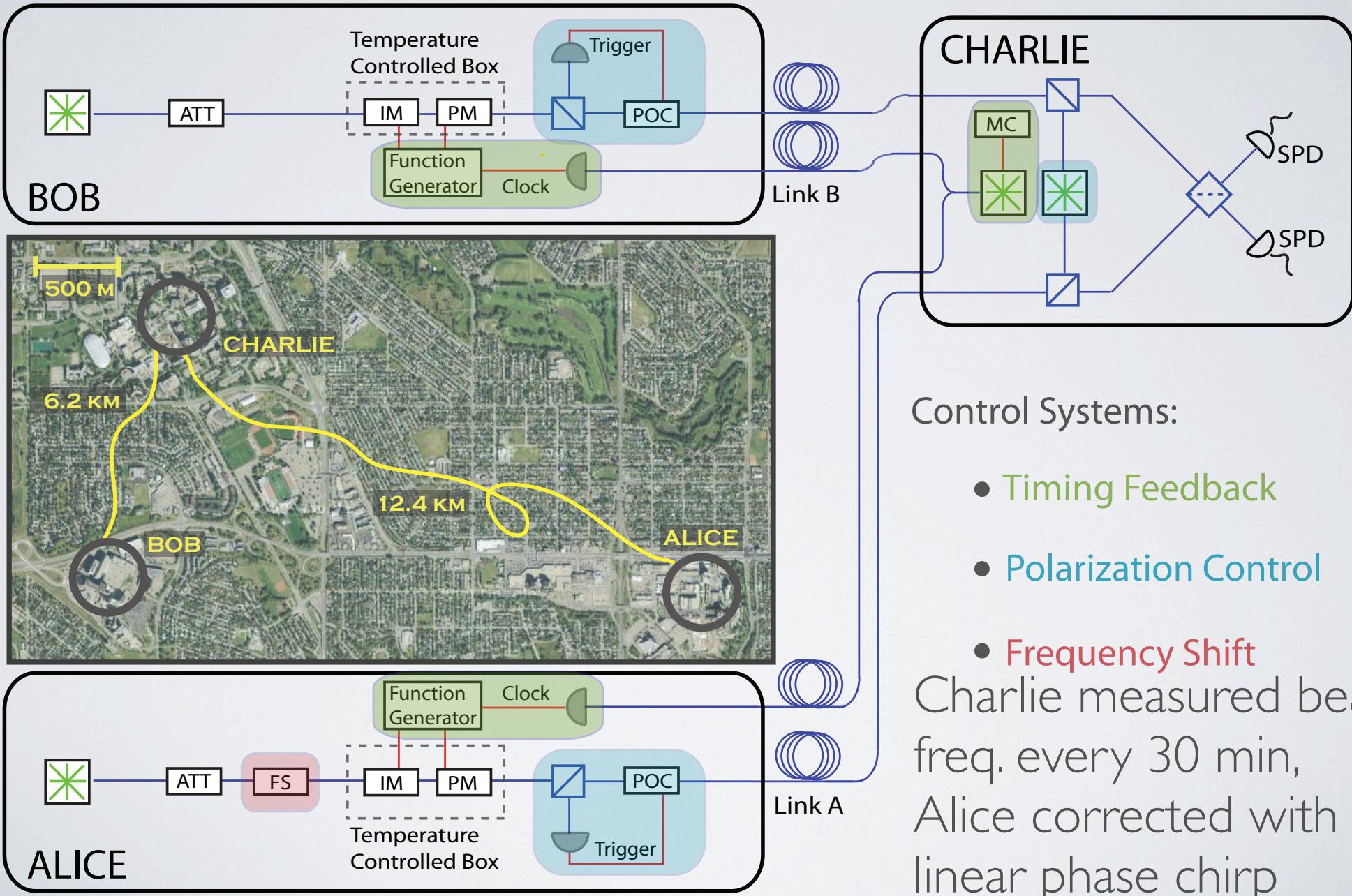
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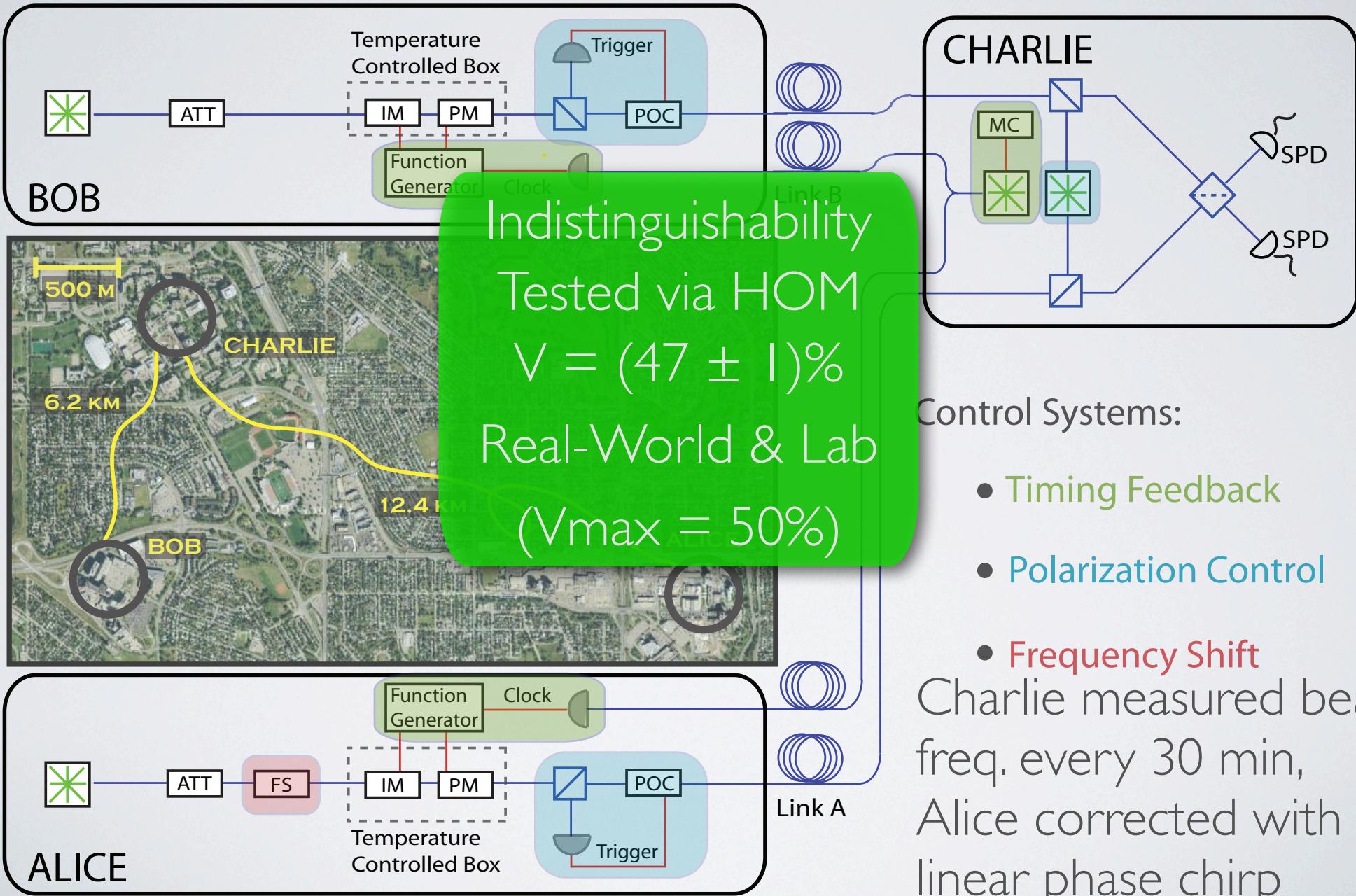
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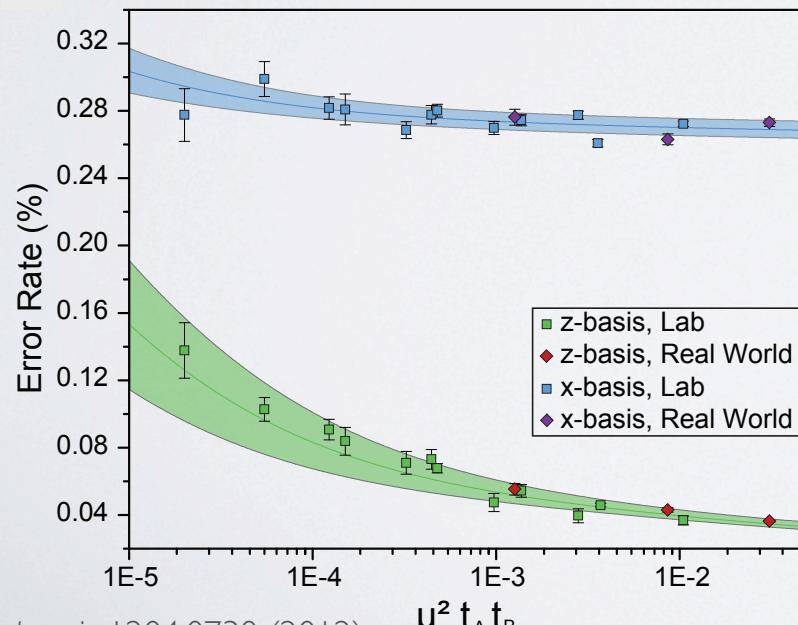
# RESULTS: MDI-QKD

Measured Error Rates & Gains (Alice/Bob sending same basis):

$$Q_{\mu\mu}^Z, Q_{\mu\mu}^X, e_{\mu\mu}^Z, e_{\mu\mu}^X$$

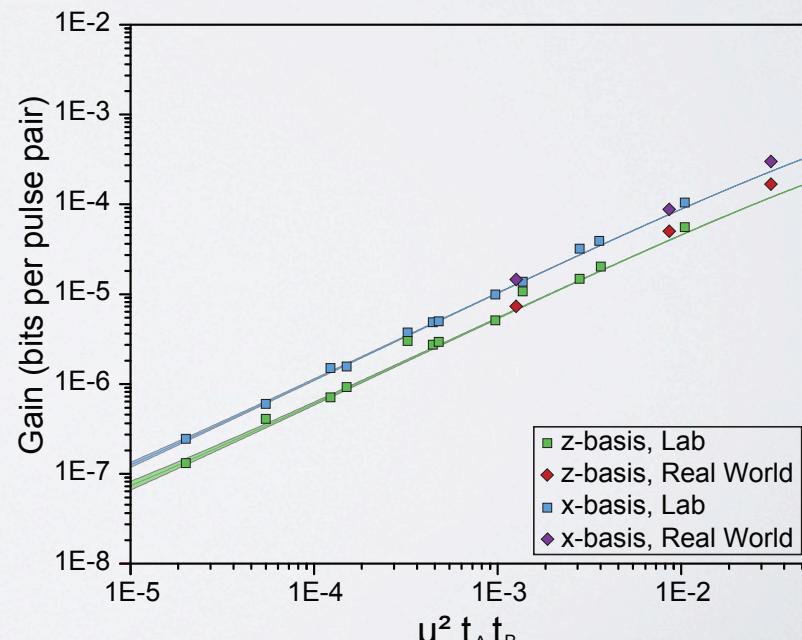
Repeated for:

- different distances:
  - different  $\mu_A = \mu_B$ :
- $$\mu_{A,B} = \{0.1, 0.25, 0.5\}$$



$I_A$ [km]	$I_A$ [dB]	$I_B$ [km]	$I_B$ [dB]	$I_{TOTAL}$ [dB]
30.98	6.8	11.75	6.8	13.6
40.80	9.1	40.77	9.1	18.2
51.43	11.3	32.19	11.3	22.7
61.15	13.7	42.80	13.6	27.2
12.40	4.5	6.20	4.5	9.0

Lab  
Real-world  
 $l_A = l_B$



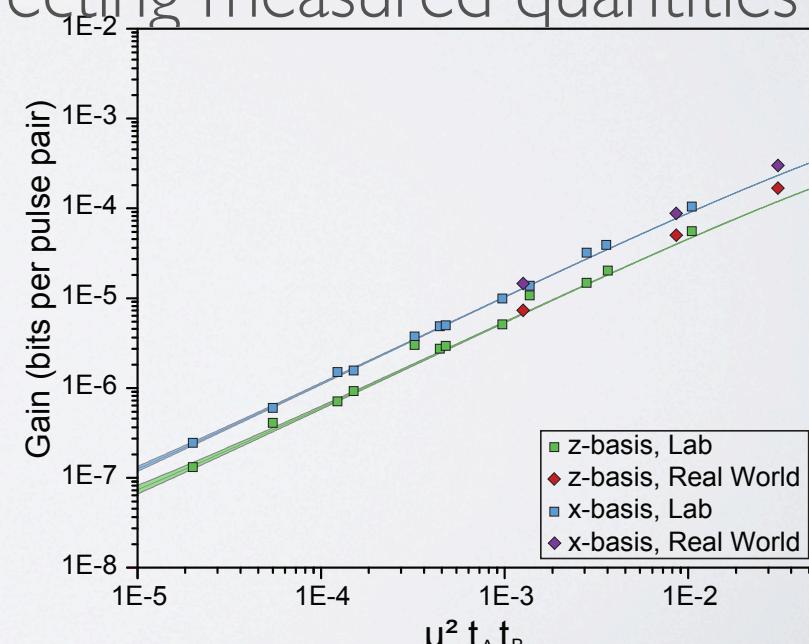
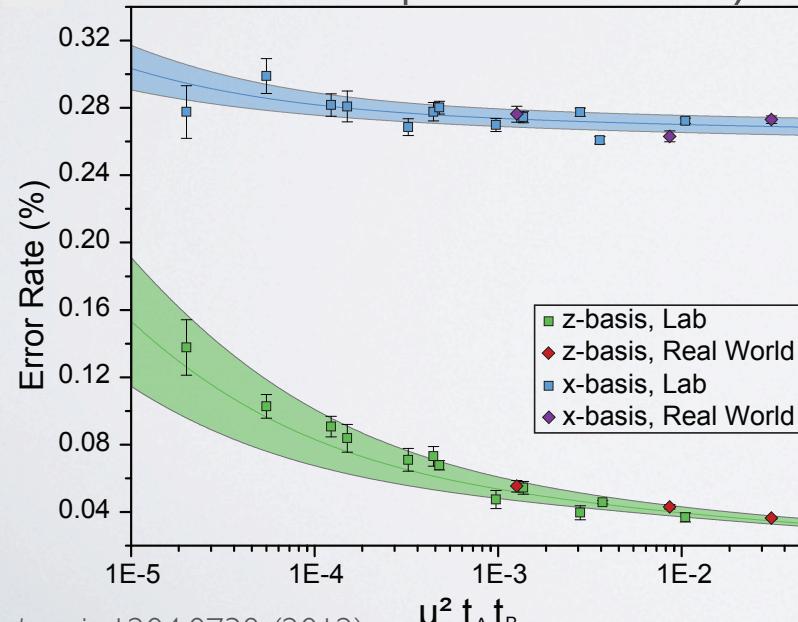
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$$Q_{\mu\mu}^Z, Q_{\mu\mu}^X, e_{\mu\mu}^Z, e_{\mu\mu}^X$$

Simulations using independently measured parameters

- agree with experimental measured quantities
- we understand imperfections (i.e. state generation & detector imperfections) affecting measured quantities



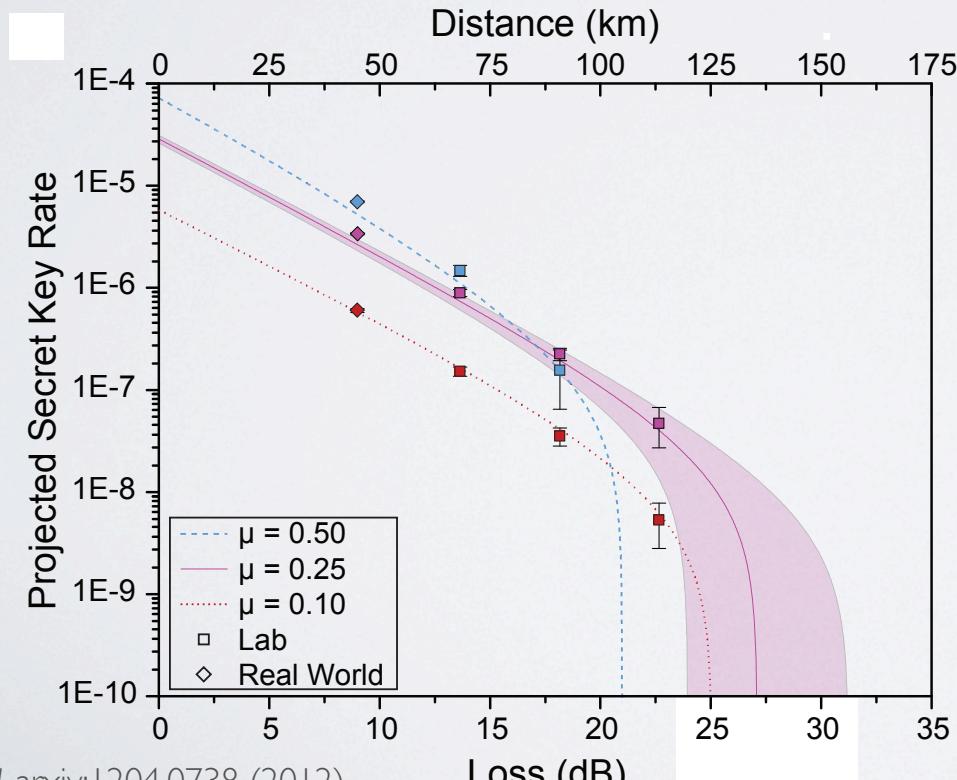
# RESULTS

Estimate Secret Key Rate:  $S = Q_{11}^z \left(1 - h_2(e_{11}^x)\right) - Q_{\mu\mu}^z f h_2(e_{\mu\mu}^z)$

With Alice/Bob sending same basis:

Measured Error Rates & Gains:  $Q_{\mu\mu}^Z, Q_{\mu\mu}^X, e_{\mu\mu}^Z, e_{\mu\mu}^X$

Use simulation to estimate:  $Q_{11}^Z, Q_{11}^X, e_{11}^Z, e_{11}^X$



Secret key possible up to 27 dB (127 km), (but, assuming efficient decoy analysis)

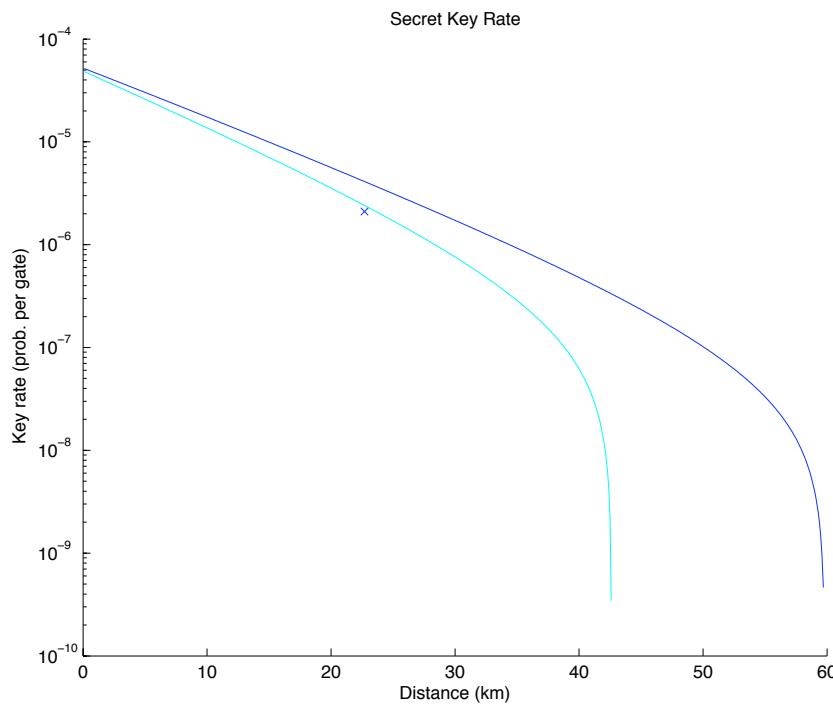
# NEW RESULTS

Recently proposed Decoy analysis for MDI-QKD:

- random modulation between 3  $\mu$ : vacuum, decoy & signal
- lower bounds  $Q_{11}^z$  & upper bounds  $e_{11}^x$ 
  - But how tight?

$$S = Q_{11}^z \left(1 - h_2(e_{11}^x)\right) - Q_{\mu\mu}^z f h_2(e_{\mu\mu}^z)$$

Optimized  $\mu$  (signal & decoy) to maximize secret key rate



Simulation (100% efficient):  
 $S = 4.2 \text{e-}6$

Simulation of Decoy Analysis:  
 $S = 2.4 \text{e-}6$   
Efficiency: 57%

Experiment:  $S = 2.2 \text{e-}6$

# CONCLUSIONS

MDI-QKD removes side-channel detector attacks

Technology sufficiently developed to implement MDI-QKD

Straight-forward work required to build complete system

Efficiency of decoy analysis likely can be improved

Real-world, controlled Bell-State Measurements demonstrated, also a requirement for quantum repeaters, quantum networks, LOQC...