



# Solid-state quantum memories for quantum repeaters

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N. Sangouard, M. Afzelius, N. Gisin

11 September 2012

# Quantum communication at a distance



State of the art from **field** experiments

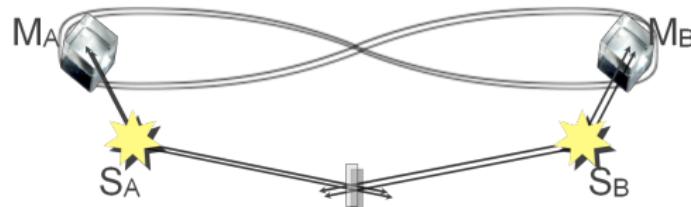
- Fibre length  $\sim 150$  km \*  
(250 km in the lab)
- Losses of 43 dB (0.29 dB/km)
- Base frequency  $> 300$  MBits/s
- Secret bit key rate of 2.5 bits/s

Longer distances require new technologies : quantum repeaters and quantum networks



# Quantum repeater

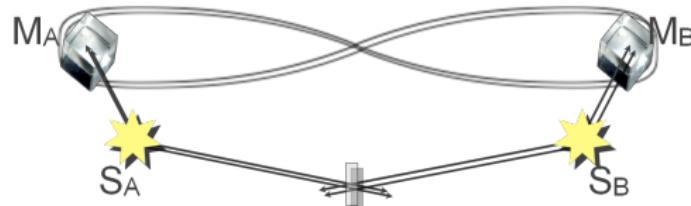
Creating entanglement



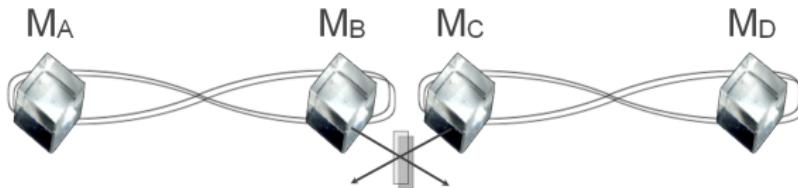


# Quantum repeater

Creating entanglement



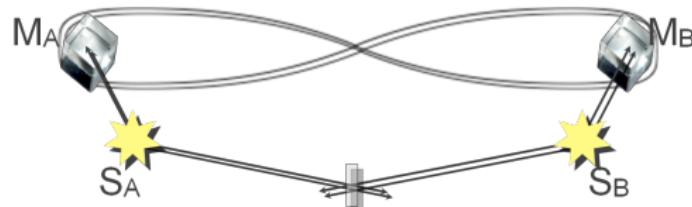
Entanglement swapping



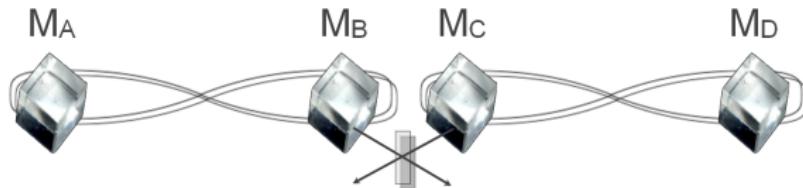


# Quantum repeater

Creating entanglement



Entanglement swapping



Increasing the distance.



## Quantum repeater: ingredients

- Efficient, long lived and multimode quantum memories
- Efficient quantum sources adapted to the memory bandwidth
- Efficient single photon detectors



# Quantum memories in rare earth doped crystals

- Weak interaction with crystal environment.
  - “Atom” like energy structure on the 4f-4f transitions
  - “Frozen gas” of ions, no motional decoherence
- High number of stationary ions ( $10^7 - 10^{10}$ )
- Long optical coherence times ( $T < 4K$ ),  $T_2^{opt}$  from  $\mu s$ -ms
- Long hyperfine coherence times ( $T < 4K$ ),  $T_2^{hyp}$  from ms-s
- Large optical inhomogeneous broadening 100 MHz – 10 GHz
- Light storage times great than 1 s \*



# Quantum memories in rare earth doped crystals

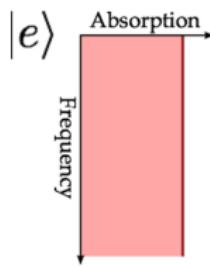
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As quantum memories:

- 69 % storage efficiency\*\*

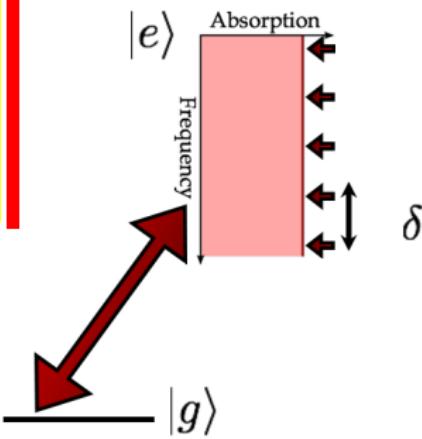
\* Longdell et al, PRL, 95, 06301 (2005), \*\*Hedges et al, Nature 465, 1052 (2010)

# Quantum memory: AFC technique

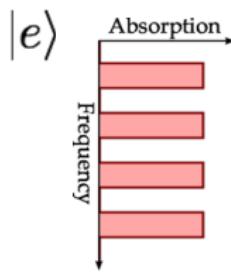


—  $|g\rangle$

# Quantum memory: AFC technique



# Quantum memory: AFC technique

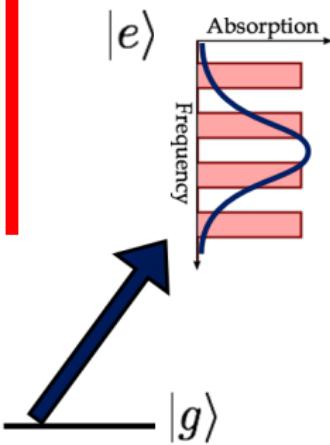


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# Quantum memory: AFC technique

State after absorption

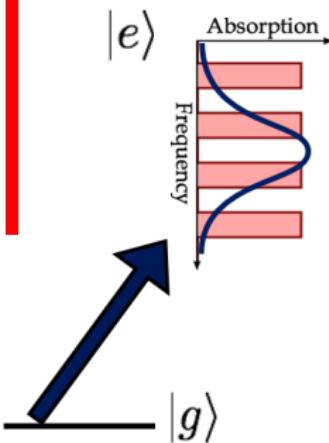
$$\sum_{k=1}^N c_k |g_1 g_2 \dots e_k \dots g_N\rangle$$



# Quantum memory: AFC technique

State after absorption

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Dephasing occurs:

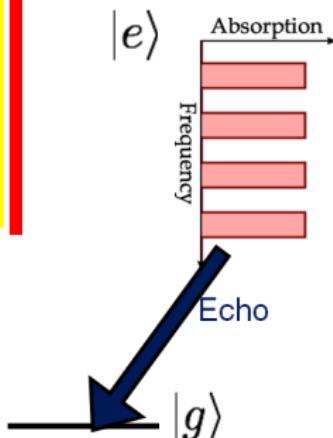
$$\sum_{k=1}^N c_k e^{-\delta_k t} |g_1 g_2 \dots e_k \dots g_N\rangle$$

$$\delta_k = m_k \Delta$$

# Quantum memory: AFC technique

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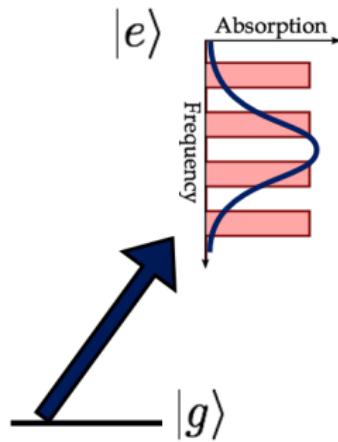
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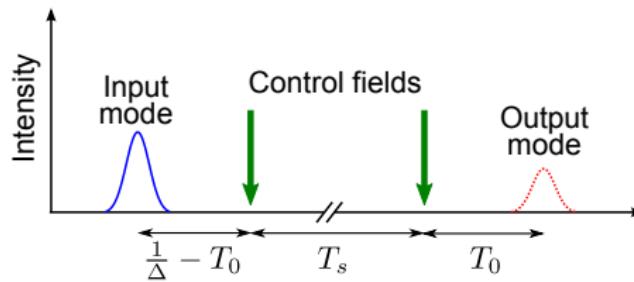
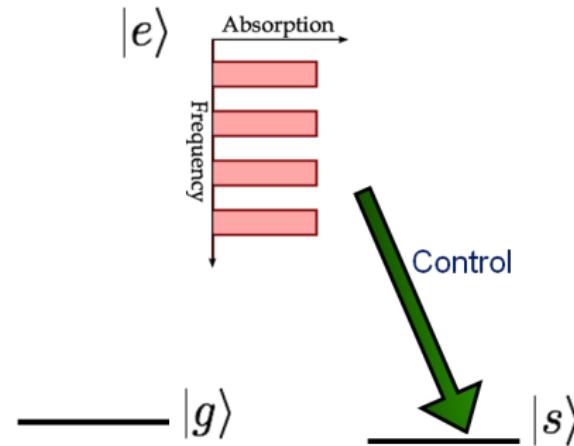
Rephasing after a time  $t_e = \frac{2\pi}{\Delta}$

Collective emission in the forward mode. Photon echo like emission.

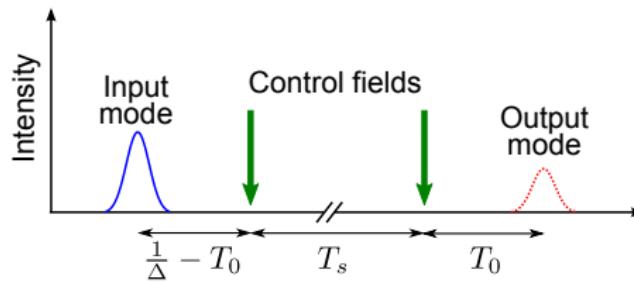
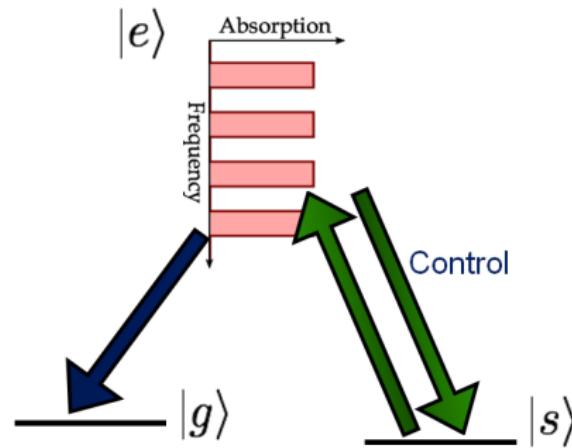
## Full AFC scheme



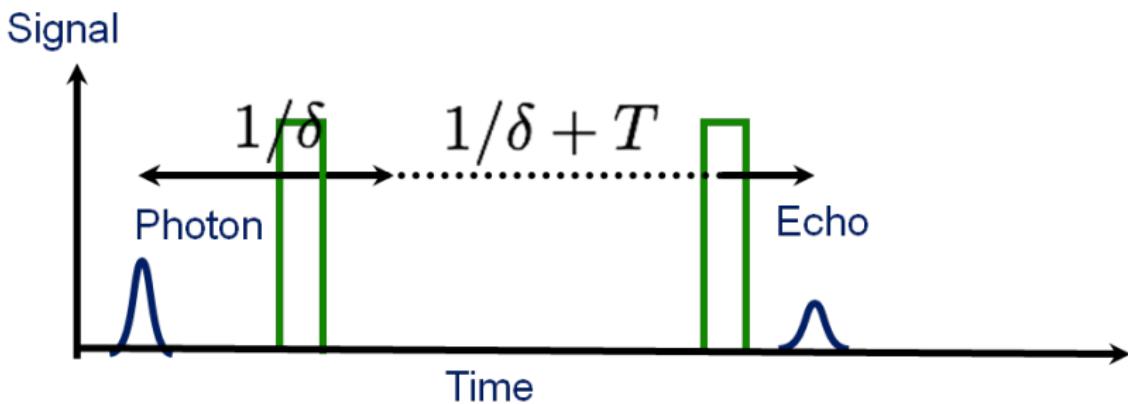
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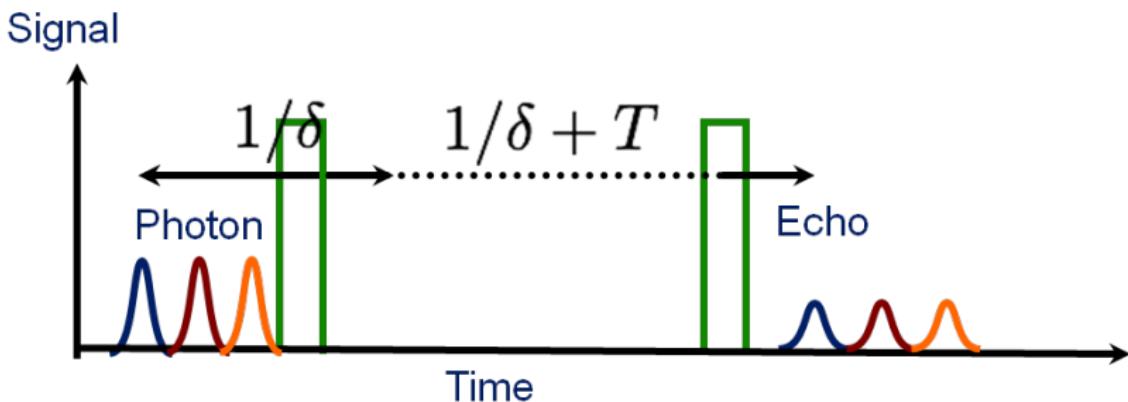
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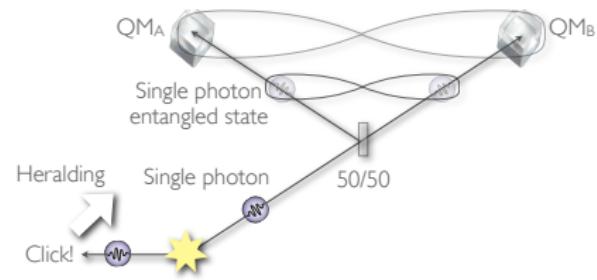
# Multimode memory



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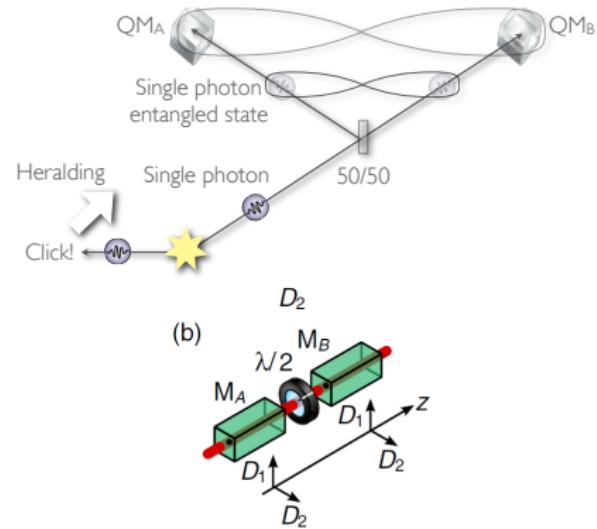
- Heralded entanglement of two crystals





- Heralded entanglement of two crystals
- Storing polarization entanglement

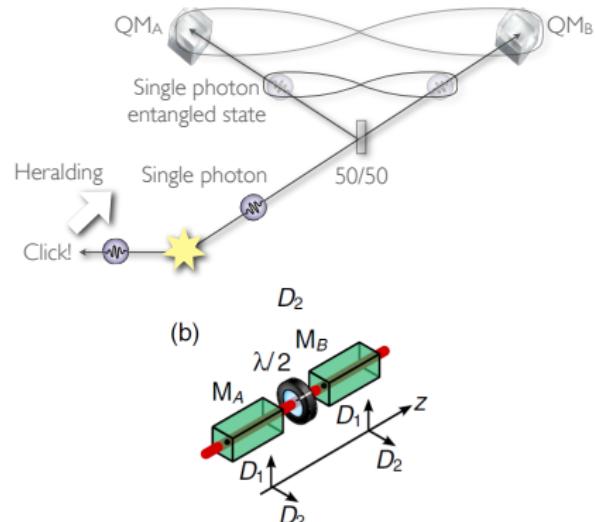
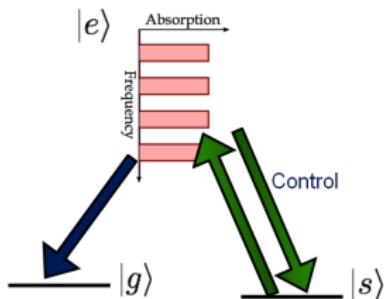
## Outline





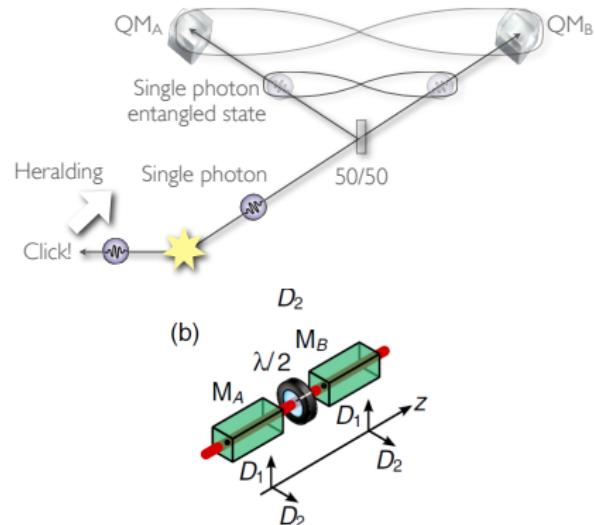
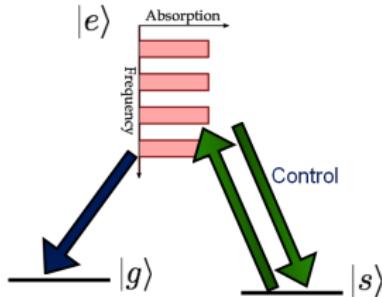
# Outline

- Heralded entanglement of two crystals
- Storing polarization entanglement
- Long storage times in an on demand memory.





- **Heralded entanglement of two crystals**
- Storing polarization entanglement
- Long storage times in an on demand memory.

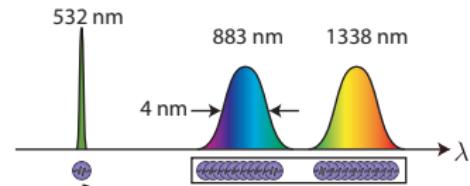
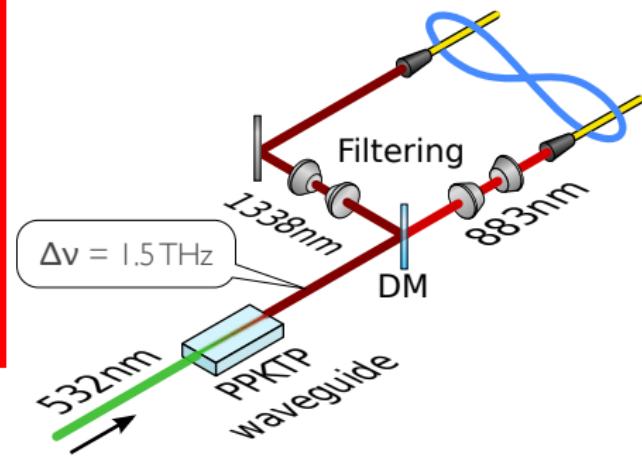


## Outline



GAP Optique Geneva University

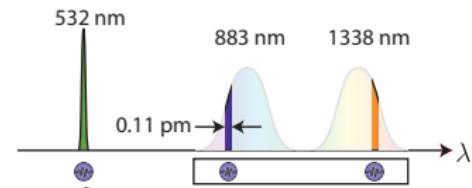
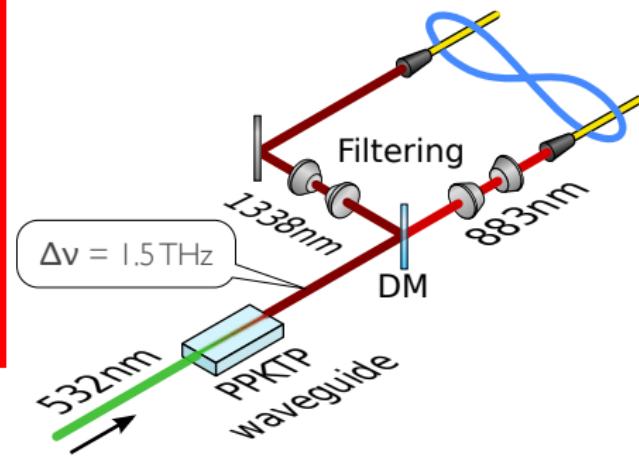
## Photon pair source



Clausen et al, Nature, 469, 508 (2011)



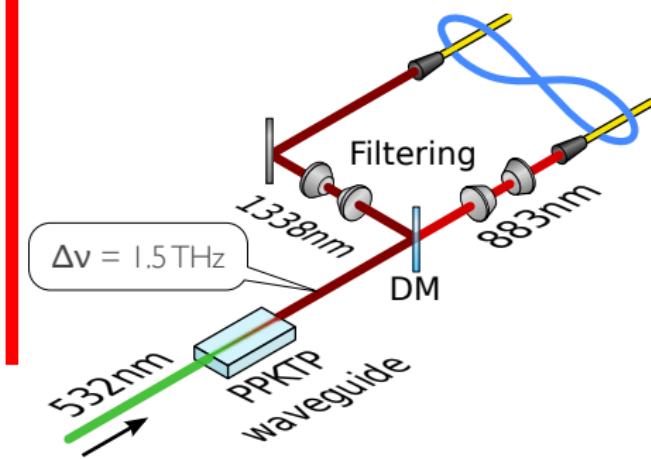
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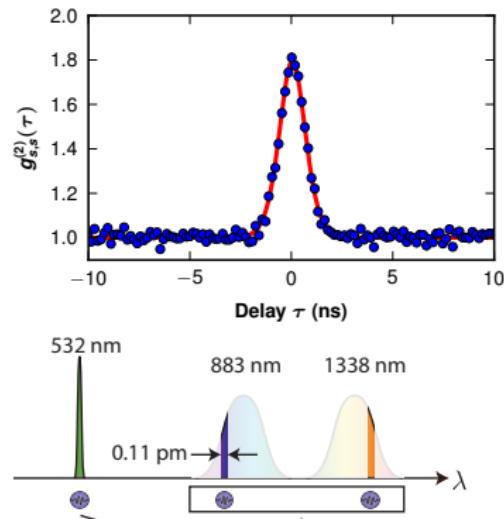
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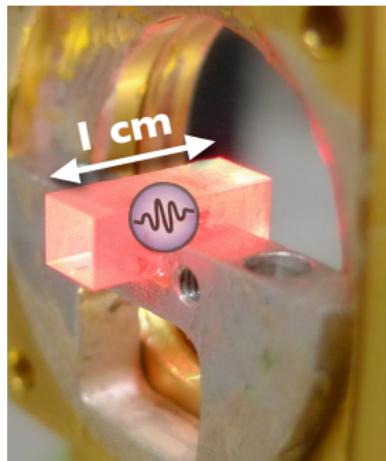


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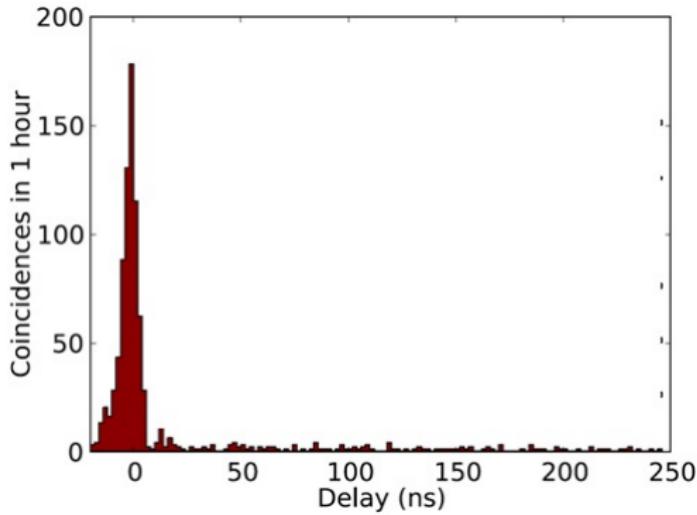
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# The memory

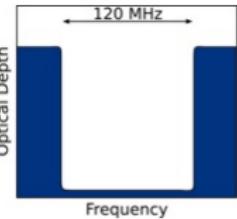


- Crystal :  $\text{Nd}^{3+}:\text{Y}_2\text{SiO}_5$  (@ 3 K)
- ${}^4\text{I}_{9/2} \rightarrow {}^4\text{F}_{3/2}$  (883 nm,  $\Gamma_{inh} = 6$  GHz)
- $B_{ext} = 300$  mT (Zeeman split)
- AFC  $1/\Delta$  from 30 ns to 1  $\mu\text{s}$

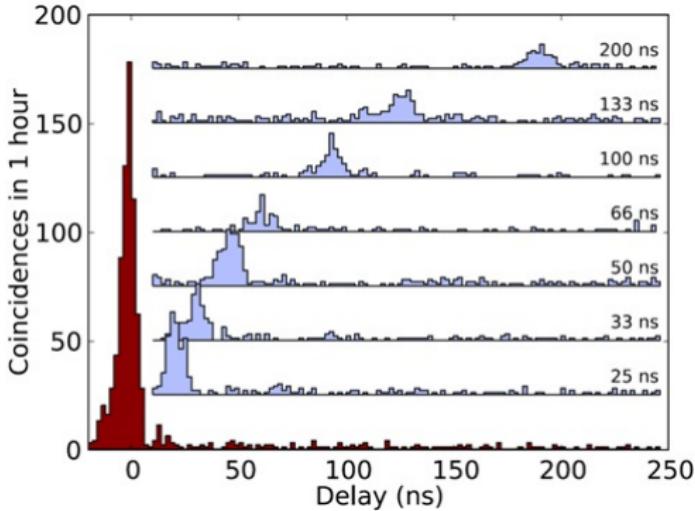
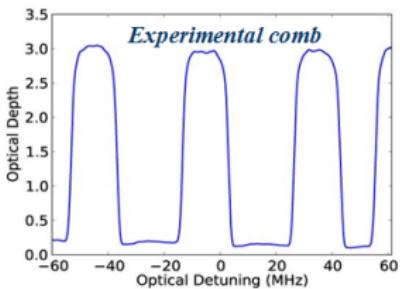
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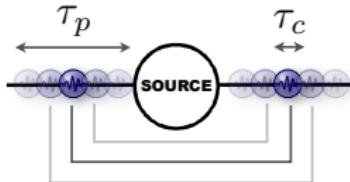
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# Storing photonic entanglement

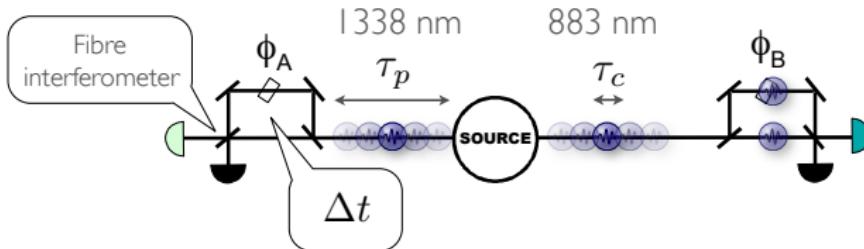


## Energy time entanglement

- Both photons are created simultaneously ( $\tau_c$ )
- Creation time is uncertain ( $\tau_p$ )



# Storing photonic entanglement



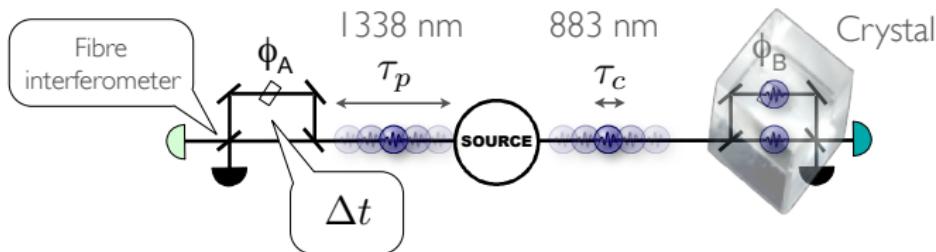
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- Entanglement in the creation time (and thus their energies)

$$\tau_p \gg \Delta t \gg \tau_c$$



# Storing photonic entanglement



## Energy time entanglement

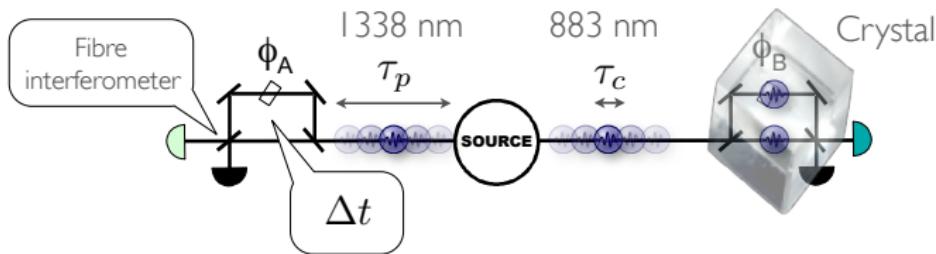
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## Bell-CHSH inequality

- $S_{CHSH} \leq 2$  (Local bound)
- $S_Q = 2\sqrt{2}$  (Quantum bound)
- $S_{exp} = 2.64 \pm 0.23$

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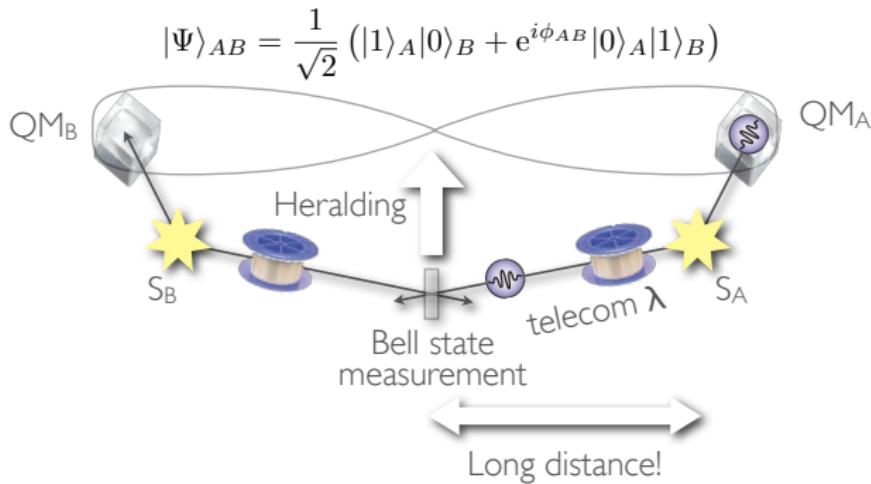
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Similar work in: Saglamyurek et al, Nature, **469**, 512 (2011)

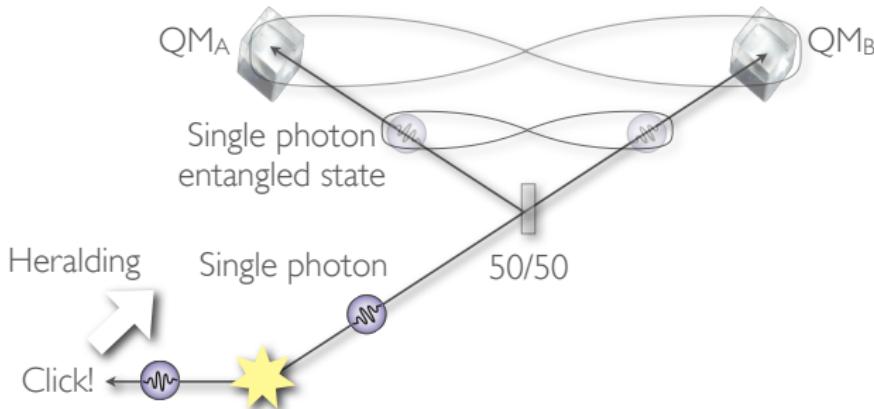
# Entangling two crystals





# Entangling two crystals

$$|\Psi\rangle_{AB} = \frac{1}{\sqrt{2}} (|1\rangle_A |0\rangle_B + e^{i\phi_{AB}} |0\rangle_A |1\rangle_B)$$



- **Prior work** Nature **438**, 828 (2005), PRL **99**, 180504 (2007), Nature **452** 67 (2008), Polzik group (2001), Vuletic group (2007)
- **Related work** Science **334** 1253, (2011)



# Entanglement?

- Ideal state :  $\frac{1}{\sqrt{2}}(|1\rangle_A|0\rangle_B + |0\rangle_A|1\rangle_B)$
- Actual state:

$$\begin{pmatrix} p_{00} & 0 & 0 & 0 \\ 0 & p_{01} & d & 0 \\ 0 & d^* & p_{10} & 0 \\ 0 & 0 & 0 & p_{11} \end{pmatrix}$$

- $C \geq \max(0, V(p_{01} + p_{10})) - 2(p_{11} p_{00})^{\frac{1}{2}}$



# Entanglement?

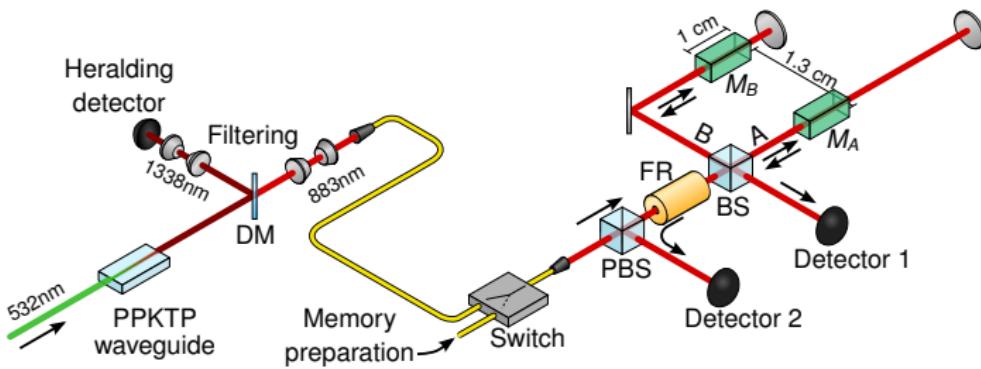
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- $C \geq \max(0, V(p_{01} + p_{10})) - 2(p_{11} p_{00})^{\frac{1}{2}}$

- ✓ Single excitation terms
- ✓ Single excitation coherence
- ✗ Loss
- ✗ Two-photon term

# Experiment to entangle two crystals

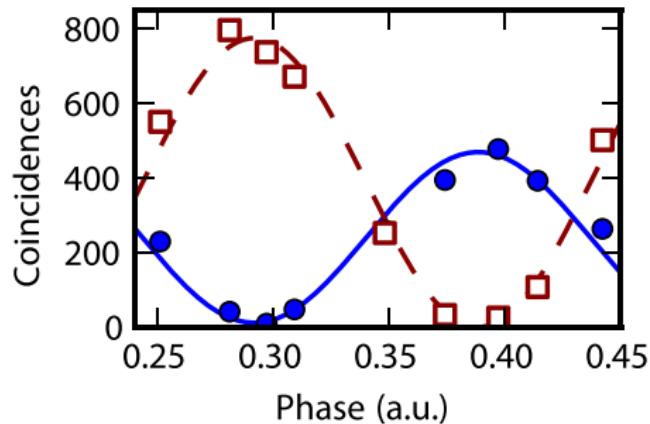


I Usmani et al, Nature Photonics, **6**, 234 (2012)

## State tomography

$$C \geq \max(0, V(p_{01} + p_{10}) - 2\sqrt{p_{11}p_{00}})$$

- Lock and scan the interferometer to measure the visibility



- $V = 96.5 \pm 1.2\%$ .
- Not enough to demonstrate entanglement.



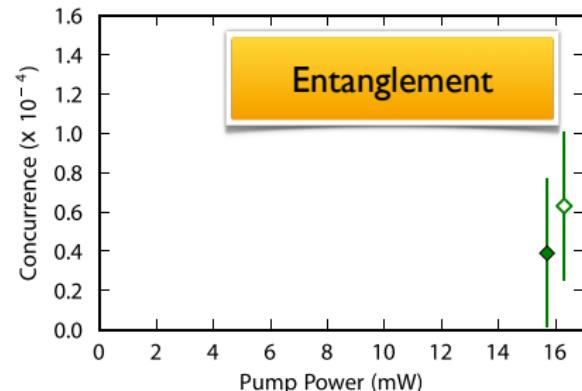
# State tomography

$$C \geq \max(0, V(p_{01} + p_{10})) - 2(p_{11} p_{00})^{\frac{1}{2}})$$

- The interferometer was let drift over 166 hours, where 2 threefold coincidences were measured

Results:

- $p_{01} + p_{10} = 1.7777(34) \times 10^{-4}$
- $p_{00} = 0.999822$
- $p_{11} = (2.9 \pm 2.1) \times 10^{-9}$
- $V = 96.5 \pm 1.2\%$
- $C \geq (6.3 \pm 3.8) \times 10^{-5}$



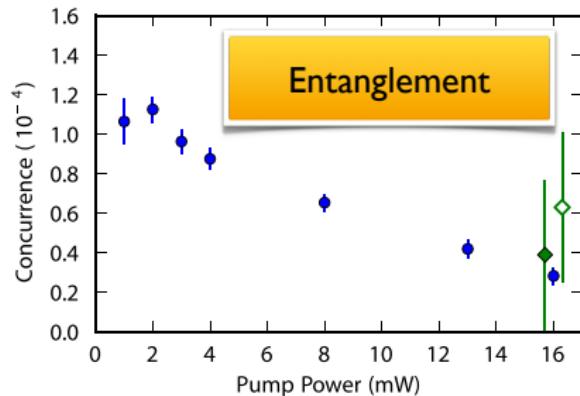


# State tomography

Conservative assumption two-mode squeezed state  $\rightarrow p_{11}$

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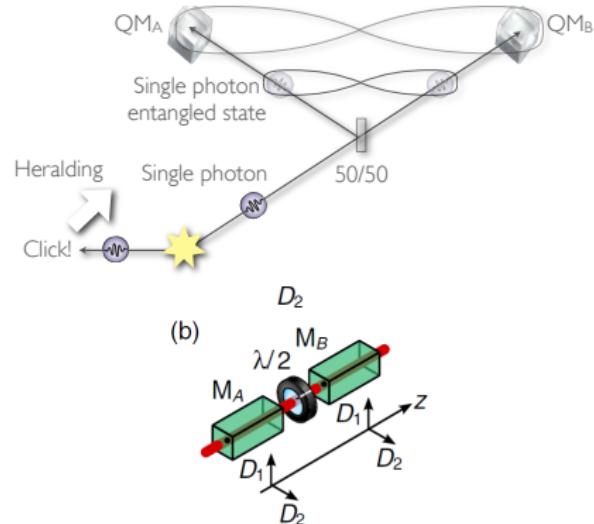
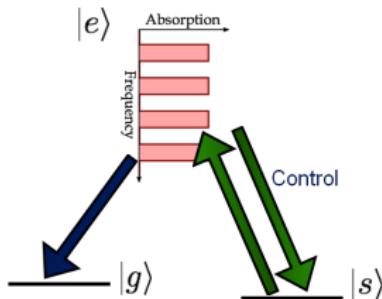


$10^6$  faster to get some statistics!



# Outline

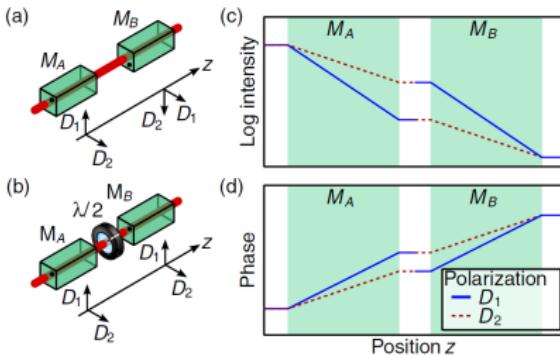
- Heralded entanglement of two crystals
- **Storing polarization entanglement**
- Long storage times in an on demand memory.



# Storing polarization entanglement

- Crystals have two different indices of refraction in xy ( $d_1, d_2$ )
- Crystals have two absorption coefficients in xy ( $d_1, d_2$ )

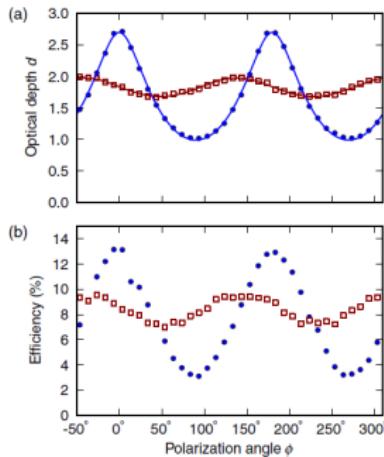
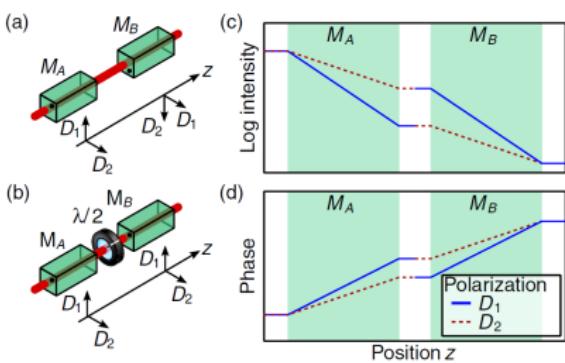
It is necessary to compensate for these effects



# Storing polarization entanglement

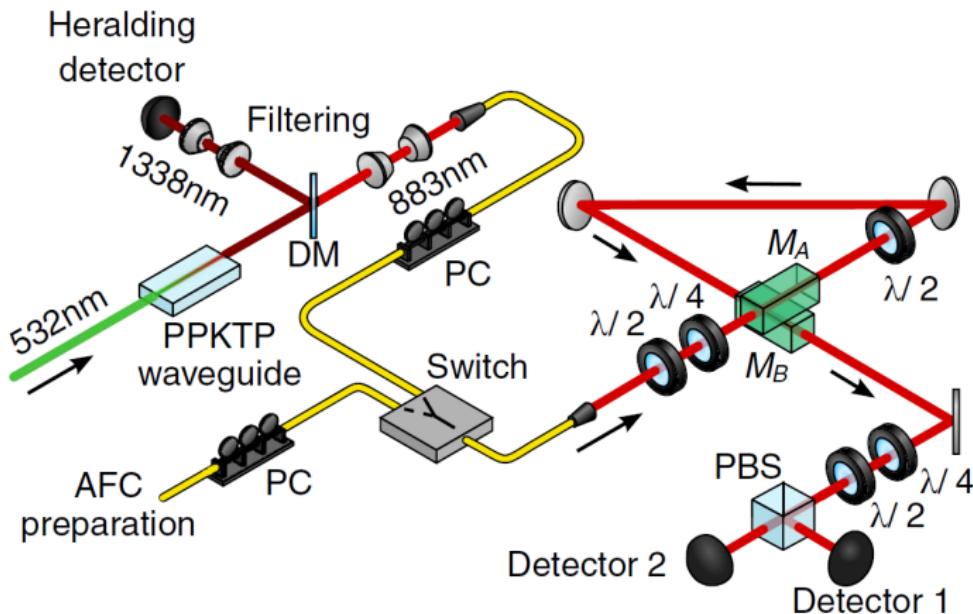
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# Storing polarization entanglement



Auto correlation before storage  $g_{s|i}^{(2)} < 0.06$

# Storing polarization entanglement

Input state	Fidelity	$\bar{g}_{si}^{(2)}$
$ H\rangle$	99.3(6)%	7.6(3)
$ V\rangle$	97(1)%	6.0(3)
$ L\rangle$	97.7(6)%	9.4(3)
$\frac{1}{\sqrt{2}}( H\rangle +  V\rangle)$	95(1)%	8.0(3)
$\alpha H\rangle + \beta V\rangle$	98.7(9)%	9.2(3)

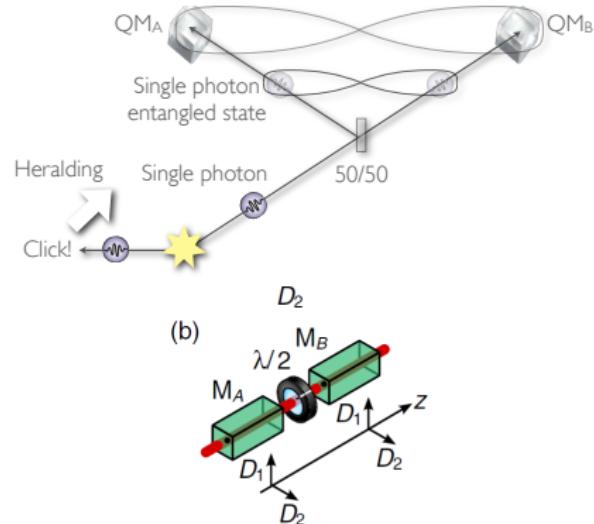
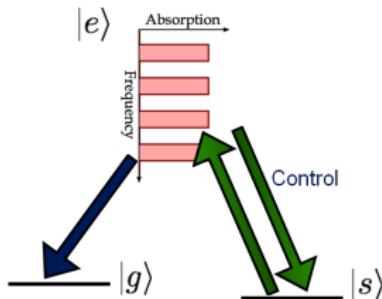
Similar work with weak coherent states in:

- Gündogan et al et al, PRL, **108**, 190504 (2012)
- Zhou et al, PRL, **108**, 190505 (2012)



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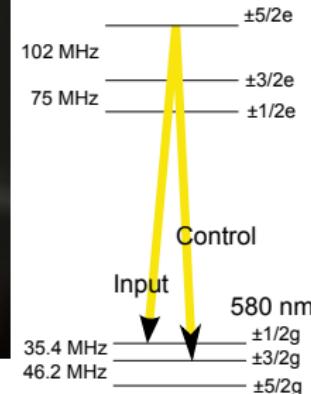
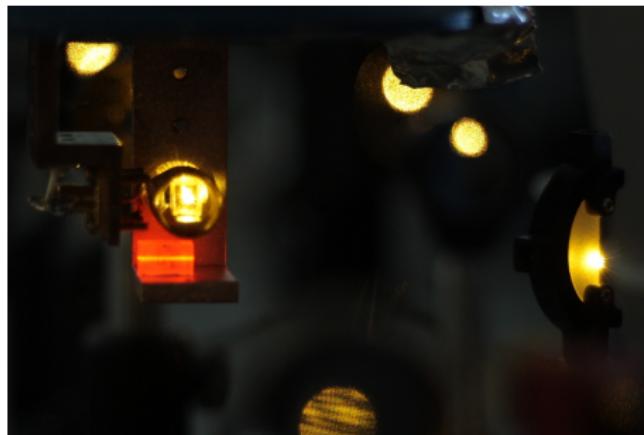
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## Candidate: Europium

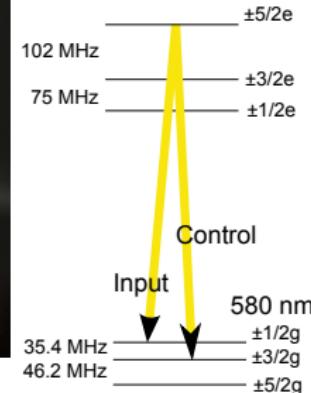
- Our sample (10 ppm) has an optical depth of  $1.5 \text{ cm}^{-1}$  and an inhomogeneous linewidth of 500 MHz
- The spin coherence time for  $^{151}\text{Eu} \sim 15 \text{ ms}$  ( $B = 0$ )





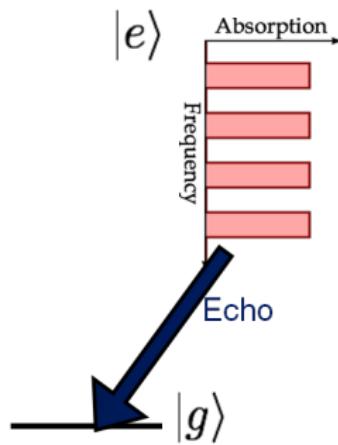
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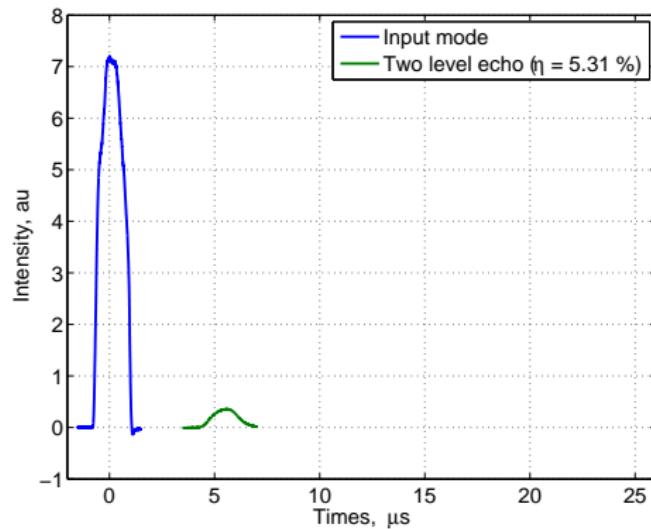


- Optical depth of the input transition is  $1 \text{ cm}^{-1}$
- Really good for a longlived multimode memory!

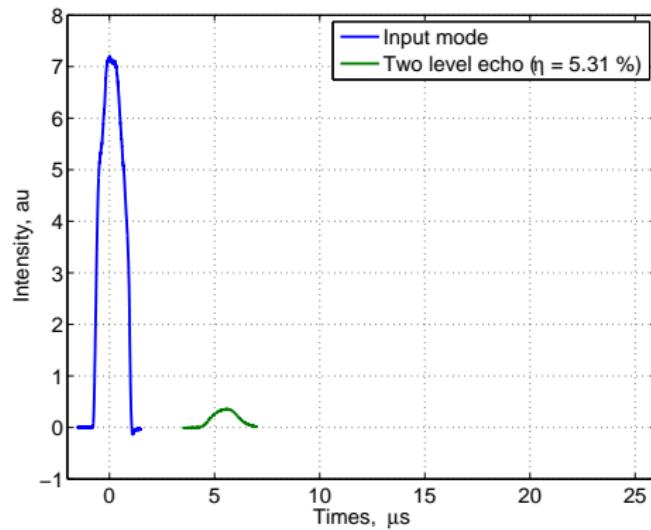
## Two level echo



## Two level echo efficiency

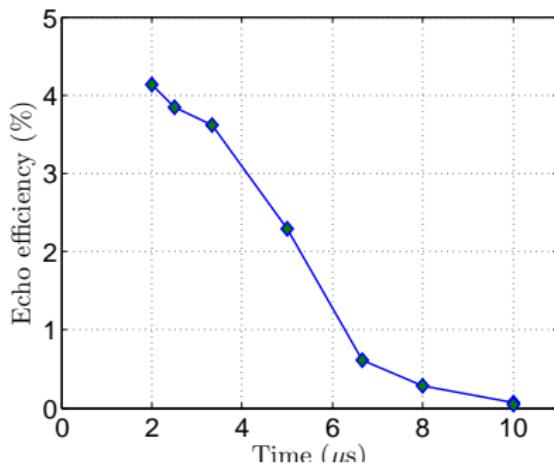


## Two level echo efficiency

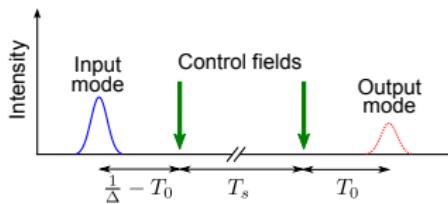
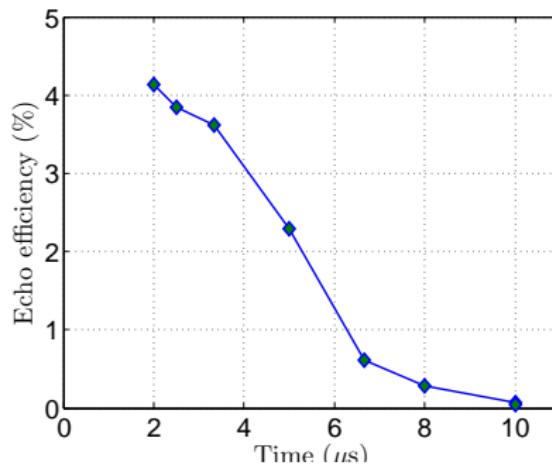


Comb spacing of 200 kHz  $\rightarrow$  5  $\mu\text{s}$  AFC

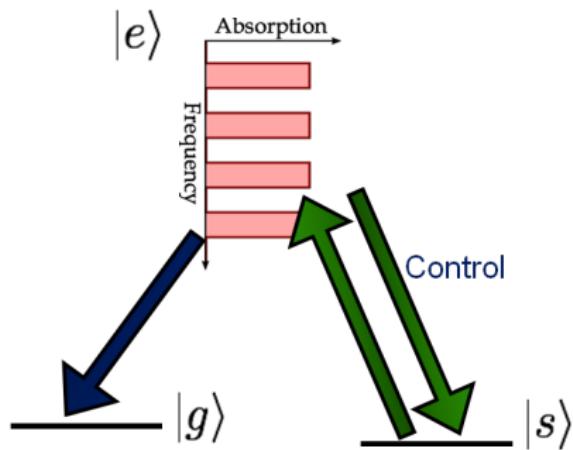
# Laser linewidth limitation



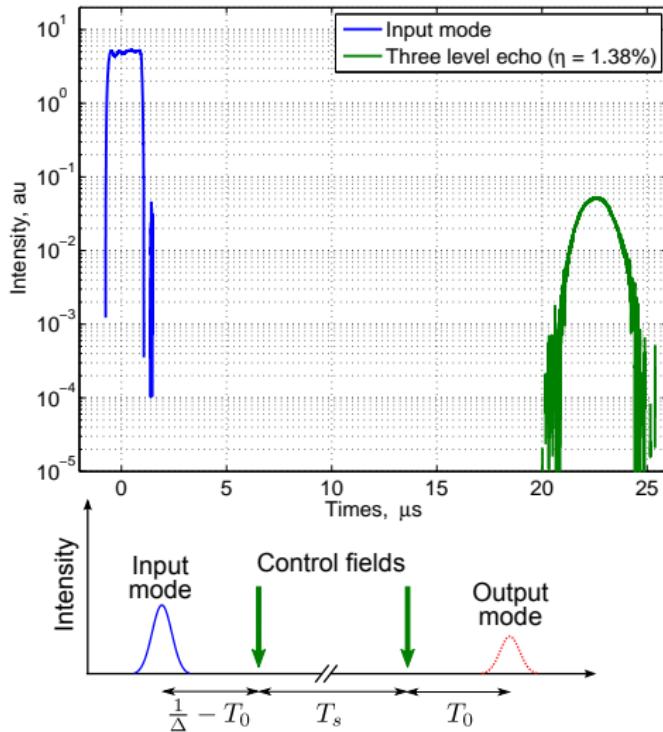
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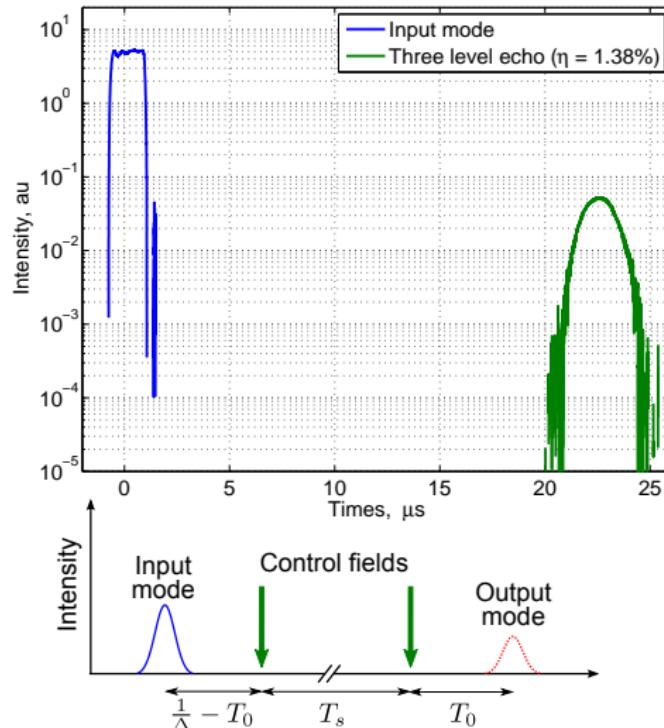
## Spin wave storage



# Spin wave storage

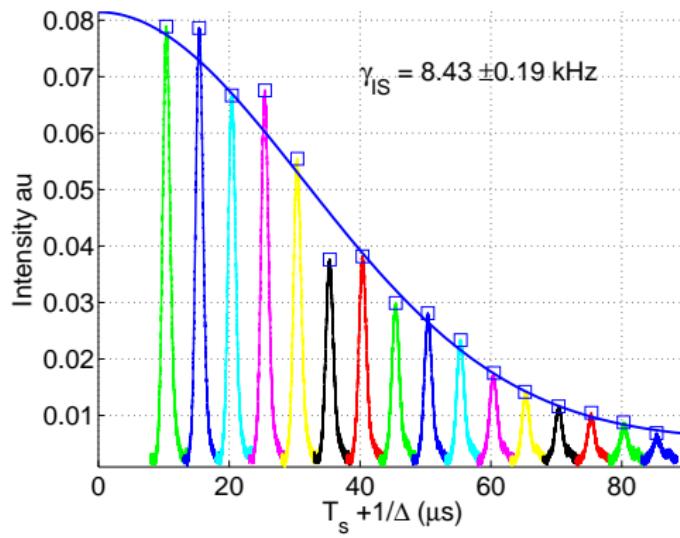


## Spin wave storage



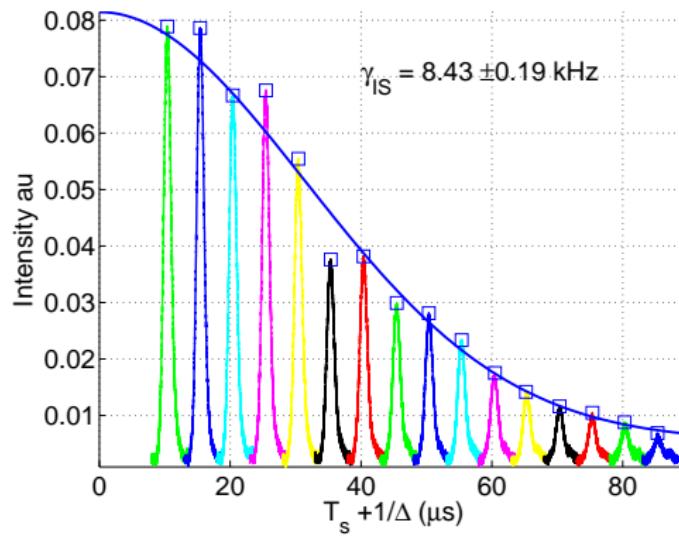
- Using square non chirped pulses estimate transfer efficiencies to be almost 50 %

# Inhomogeneous spin linewidth



$$\text{Echo height} = Ae^{\left(\frac{-t^2\gamma_{IS}^2\pi^2}{2\ln 2}\right)}$$

## Inhomogeneous spin linewidth



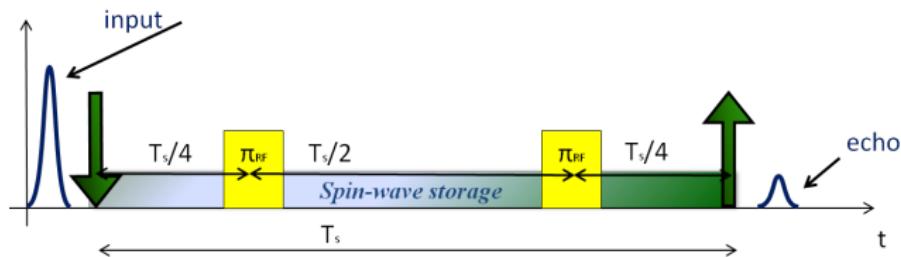
$$\text{Echo height} = Ae^{\left(\frac{-t^2\gamma_{IS}^2\pi^2}{2\ln 2}\right)}$$

- Possible to use spin echo techniques to increase the lifetime \*

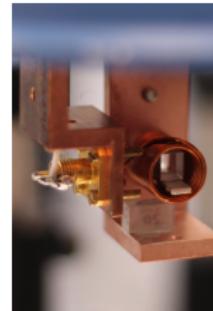
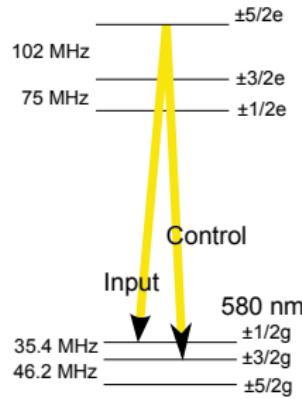
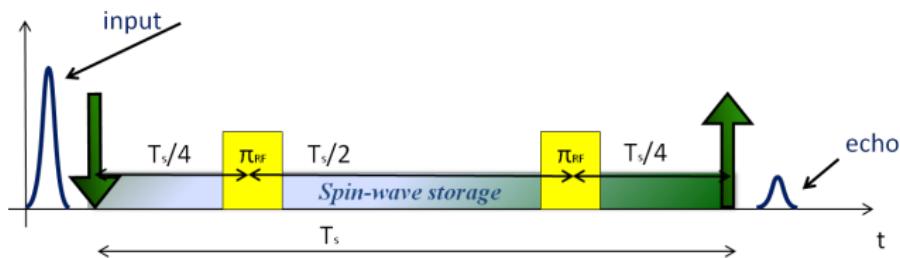
\* Longdell et al, PRL, 95, 063601 (2005)

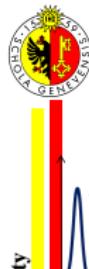


# Overcoming inhomogeneous spin linewidth

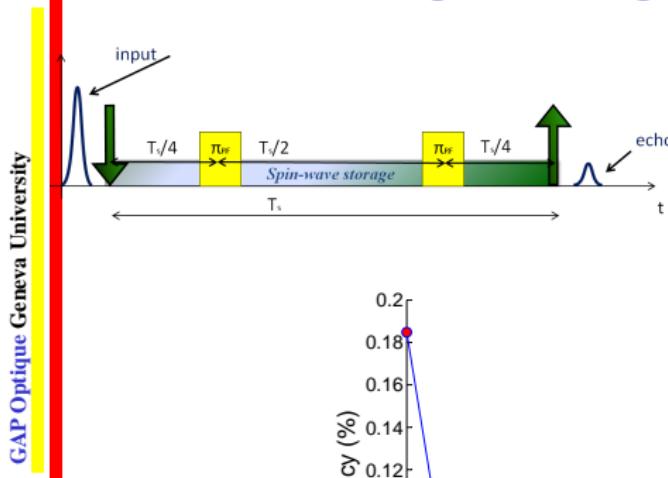


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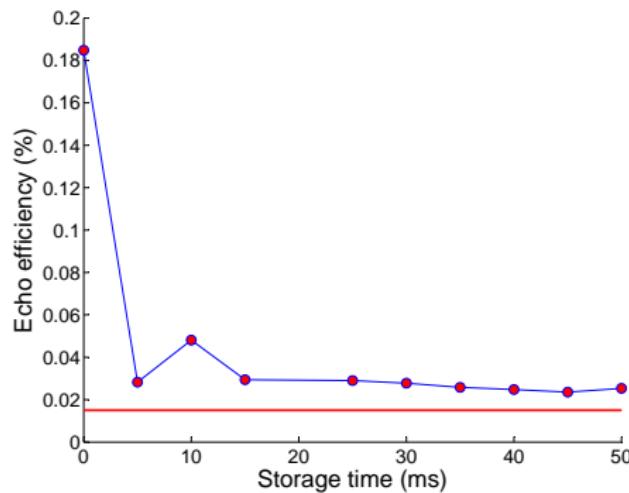




# Overcoming inhomogeneous spin linewidth



- Preliminary results
- Storage time of optical pulse for 50 ms!

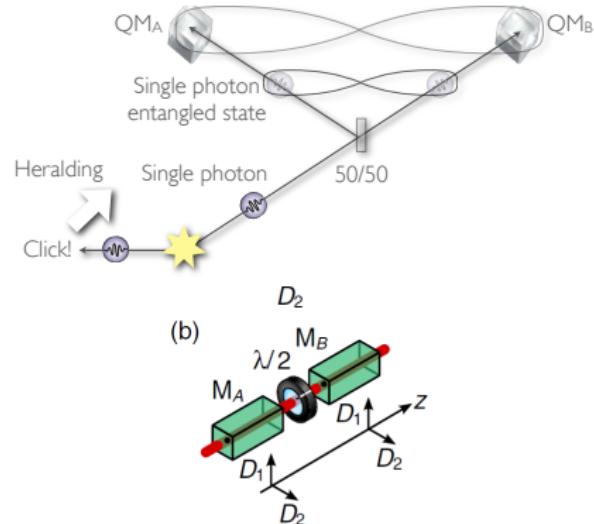
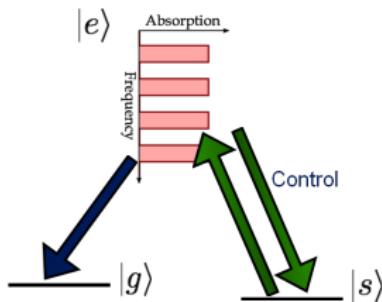


- Oscillation a quantum beat phenomenon?



# Summary

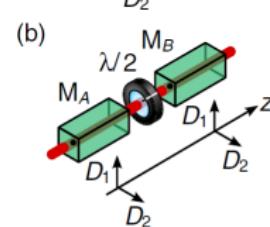
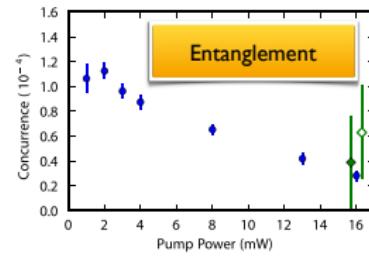
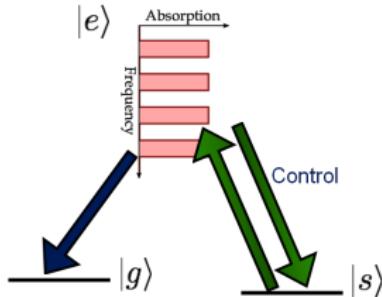
- Heralded entanglement of two crystals
- Storing polarization entanglement
- Long storage times in an on demand memory.





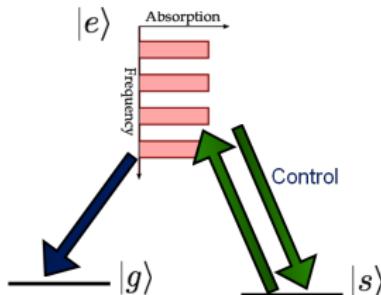
# Summary

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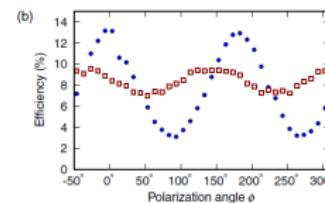
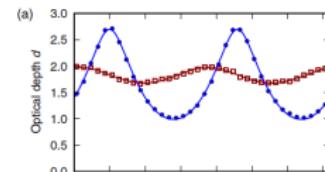
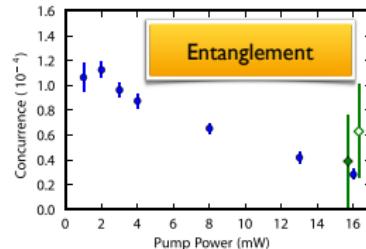




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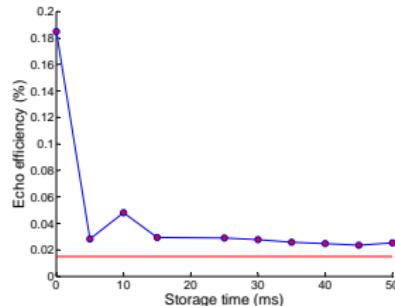


## Summary

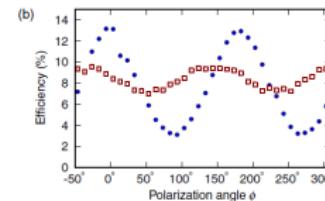
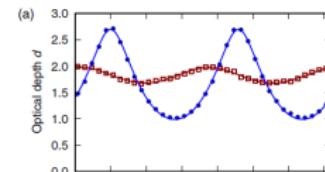
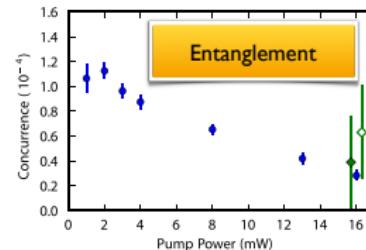




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## Summary





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- Our long term goal is to make an elementary quantum repeater link as long a distance as we can!



GAP Optique Geneva University

Thank you



We are grateful to Y Sun, R L Cone and RM Macfarlane for kindly lending us the  $^{151}\text{Eu}^{3+}$  doped  $\text{Y}_2\text{SiO}_5$  crystal.