

# Experimental bit commitment based on quantum communication and special relativity

T. Lunghi, J. Kaniewski, F. Bussières, R. Houlmann,  
M. Tomamichel, A. Kent, N. Gisin, S. Wehner, H. Zbinden

Group of Applied Physics, University of Geneva, Switzerland  
Centre for Quantum Technologies, National University of Singapore, Singapore  
Centre for Quantum Information and Foundations, University of Cambridge, UK  
Perimeter Institute for Theoretical Physics, Waterloo, Canada

August 9, 2013  
[arXiv:1306.4801]

# Bit commitment – the primitive

## Bit commitment – the primitive

**Commit phase:** Bob commits a bit to Alice.

**Open phase:** Bob opens his commitment and Alice accepts (or not).

## Bit commitment – the primitive

**Commit phase:** Bob commits a bit to Alice.

**Open phase:** Bob opens his commitment and Alice accepts (or not).

The protocol should be:

- **correct:** If Alice and Bob are honest then Alice always accepts the opening.

## Bit commitment – the primitive

**Commit phase:** Bob commits a bit to Alice.

**Open phase:** Bob opens his commitment and Alice accepts (or not).

The protocol should be:

- **correct:** If Alice and Bob are honest then Alice always accepts the opening.
- **binding:** If Alice is honest then there is at most one bit that Bob can successfully open.

## Bit commitment – the primitive

**Commit phase:** Bob commits a bit to Alice.

**Open phase:** Bob opens his commitment and Alice accepts (or not).

The protocol should be:

- **correct:** If Alice and Bob are honest then Alice always accepts the opening.
- **binding:** If Alice is honest then there is at most one bit that Bob can successfully open.
- **hiding:** If Bob is honest then Alice learns nothing about his commitment until the open phase.

## Bit commitment – the no-go

- Quantum mechanics does not allow for a bit commitment that gives perfect (or close to perfect) security to both parties [Lo,Chau'96; Mayers'96].
- There exist protocols that give partial security to both parties, the trade-offs are known [Spekkens,Rudolph'01; Chailloux,Kerenidis'11].

## Bit commitment – the no-go

- Quantum mechanics does not allow for a bit commitment that gives perfect (or close to perfect) security to both parties [Lo,Chau'96; Mayers'96].
- There exist protocols that give partial security to both parties, the trade-offs are known [Spekkens,Rudolph'01; Chailloux,Kerenidis'11].

***By imposing communication constraints  
one can evade the no-go***

## Bit commitment – the no-go

- Quantum mechanics does not allow for a bit commitment that gives perfect (or close to perfect) security to both parties [Lo,Chau'96; Mayers'96].
- There exist protocols that give partial security to both parties, the trade-offs are known [Spekkens,Rudolph'01; Chailloux,Kerenidis'11].

***By imposing communication constraints  
one can evade the no-go***



***Communication constraints can be  
enforced by special relativity***

## Bit commitment – the no-go

- Quantum mechanics does not allow for a bit commitment that gives perfect (or close to perfect) security to both parties [Lo,Chau'96; Mayers'96].
- There exist protocols that give partial security to both parties, the trade-offs are known [Spekkens,Rudolph'01; Chailloux,Kerenidis'11].

***By imposing communication constraints  
one can evade the no-go***



***Communication constraints can be  
enforced by special relativity***



**RELATIVISTIC BIT COMMITMENT**

# Relativistic bit commitment protocols

- ① Unconditionally Secure Bit Commitment  
A. Kent, Phys. Rev. Lett. 83, 1447 (1999)

# Relativistic bit commitment protocols

- ① Unconditionally Secure Bit Commitment  
A. Kent, Phys. Rev. Lett. 83, 1447 (1999)
- ② Secure Classical Bit Commitment Using Fixed Capacity Communication Channels  
A. Kent, Journal of Cryptology 18, 313 (2005)

# Relativistic bit commitment protocols

- ① Unconditionally Secure Bit Commitment  
A. Kent, Phys. Rev. Lett. 83, 1447 (1999)
- ② Secure Classical Bit Commitment Using Fixed Capacity Communication Channels  
A. Kent, Journal of Cryptology 18, 313 (2005)
- ③ Unconditionally Secure Bit Commitment with Flying Qudits  
A. Kent, New Journal of Physics 13, 113015 (2011)

# Relativistic bit commitment protocols

- ① Unconditionally Secure Bit Commitment  
A. Kent, Phys. Rev. Lett. 83, 1447 (1999)
- ② Secure Classical Bit Commitment Using Fixed Capacity Communication Channels  
A. Kent, Journal of Cryptology 18, 313 (2005)
- ③ Unconditionally Secure Bit Commitment with Flying Qudits  
A. Kent, New Journal of Physics 13, 113015 (2011)
- ④ Unconditionally Secure Bit Commitment by Transmitting Measurement Outcomes  
A. Kent, Phys. Rev. Lett. 109, 130501 (2012)

# BC by Transmitting Measurement Outcomes

# BC by Transmitting Measurement Outcomes

- ① (**commit**) Alice generates  $n$  random BB84 states and (simultaneously) sends them to Bob.

## BC by Transmitting Measurement Outcomes

- ① (**commit**) Alice generates  $n$  random BB84 states and (simultaneously) sends them to Bob.
- ② To commit to 0 (1) he measures all the incoming qubits in the computational (Hadamard) basis. Bob distributes the outcomes to agents occupying distant locations.

## BC by Transmitting Measurement Outcomes

- ① (**commit**) Alice generates  $n$  random BB84 states and (simultaneously) sends them to Bob.
- ② To commit to 0 (1) he measures all the incoming qubits in the computational (Hadamard) basis. Bob distributes the outcomes to agents occupying distant locations.
- ③ (**open**) Bob's agents have to simultaneously unveil the committed bit and the measurement outcomes to Alice's agents.

# BC by Transmitting Measurement Outcomes

- ① (**commit**) Alice generates  $n$  random BB84 states and (**simultaneously**) sends them to Bob.
- ② To commit to 0 (1) he measures all the incoming qubits in the computational (Hadamard) basis. Bob distributes the outcomes to agents occupying distant locations.
- ③ (**open**) Bob's agents have to simultaneously unveil the committed bit and the measurement outcomes to Alice's agents.
- ④ (**verify**) Alice's agents verify whether the outcomes provided by Bob are consistent with the BB84 states.

# Security

Proven **secure** in

[S. Croke and A. Kent, Phys. Rev. A 86, 052309 (2012),  
J. Kaniewski, M. Tomamichel, E. Hanggi, and S. Wehner,  
Information Theory, IEEE Transactions on 59, 4687 (2013)]

Secure you say, **mhhmmmm**, but what's the security model?

# Security

Proven **secure** in

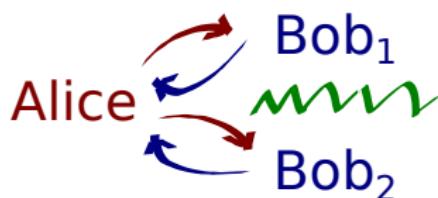
[S. Croke and A. Kent, Phys. Rev. A 86, 052309 (2012),  
J. Kaniewski, M. Tomamichel, E. Hanggi, and S. Wehner,  
Information Theory, IEEE Transactions on 59, 4687 (2013)]

Secure you say, **mhhmmmm**, but what's the security model?

Commit phase



Open phase



# Security

Proven **secure** in

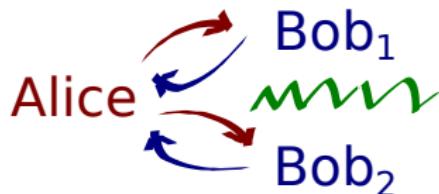
[S. Croke and A. Kent, Phys. Rev. A 86, 052309 (2012),  
J. Kaniewski, M. Tomamichel, E. Hanggi, and S. Wehner,  
Information Theory, IEEE Transactions on 59, 4687 (2013)]

Secure you say, **mhhmmmm**, but what's the security model?

Commit phase

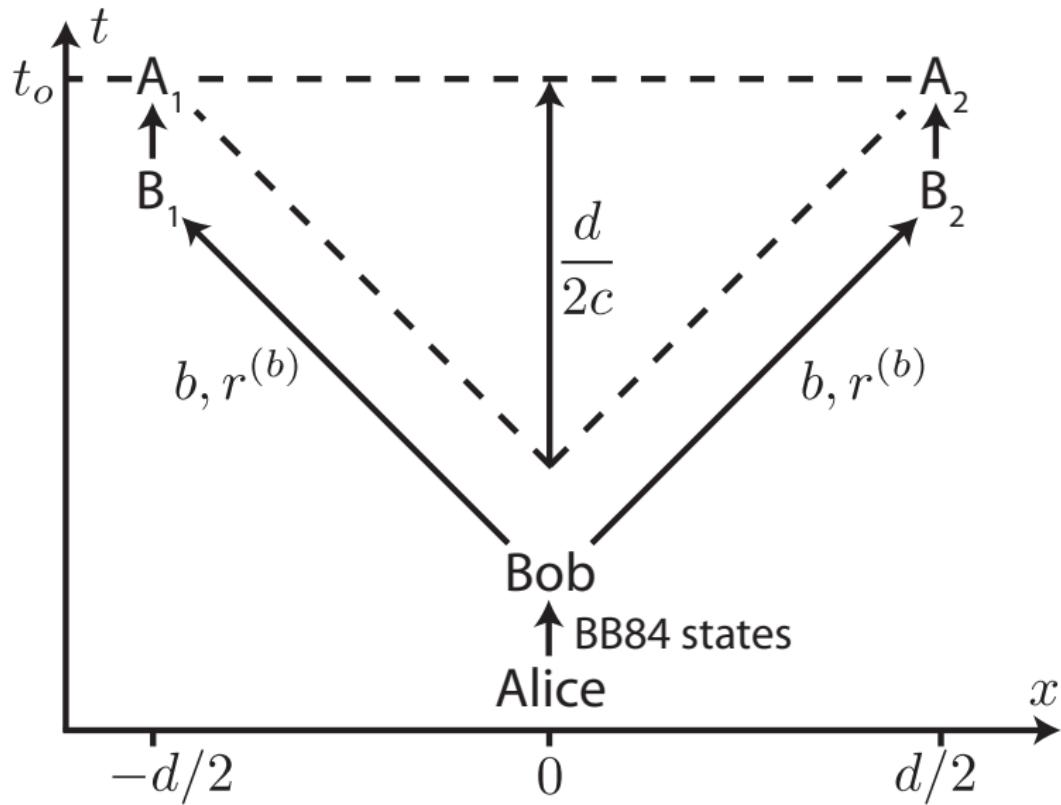


Open phase



*not possible classically  
[quantum advantage]*

# Relativistic realisation



# Implementation issues

**Source:** We **do not** use a single photon source. We use a **weak coherent source with phase randomisation**:

$$\rho = \sum_{r=0}^{\infty} p_r |r\rangle\langle r|,$$

$$\text{where } p_r = e^{-\mu} \cdot \frac{\mu^r}{r!},$$

$\mu$  is the average number of photons per pulse and  $|r\rangle$  is the Fock state of  $r$  photons.

# Implementation issues

**Source:** We **do not** use a single photon source. We use a **weak coherent source with phase randomisation**:

$$\rho = \sum_{r=0}^{\infty} p_r |r\rangle\langle r|,$$

$$\text{where } p_r = e^{-\mu} \cdot \frac{\mu^r}{r!},$$

$\mu$  is the average number of photons per pulse and  $|r\rangle$  is the Fock state of  $r$  photons.

**Channel and Bob's detectors:** They are **not perfect**. They introduce **bit-flip errors** and **losses**.

# Implementation issues and fixes...



on **ONE** hand  
noise or losses make  
honest Bob's life more  
difficult

# Implementation issues and fixes...



on **ONE** hand  
noise or losses make  
honest Bob's life more  
difficult

(obvious) fix: make Alice "more  
forgiving"

(undesired) result: cheating  
becomes easier

# Implementation issues and fixes...



on **ONE** hand  
noise or losses make  
honest Bob's life more  
difficult



on **THE OTHER** hand  
multi-photon emissions  
enable dishonest Bob to  
cheat more easily

(obvious) fix: make Alice "more  
forgiving"

(undesired) result: cheating  
becomes easier

# Implementation issues and fixes...



on **ONE** hand  
noise or losses make  
honest Bob's life more  
difficult

(obvious) fix: make Alice "more  
forgiving"

(undesired) result: cheating  
becomes easier



on **THE OTHER** hand  
multi-photon emissions  
enable dishonest Bob to  
cheat more easily

(obvious) fix: eliminate multi-photon  
emissions

(undesired) result: more vacuum  
rounds, honest Bob suffers

# Implementation issues and fixes...



on **ONE** hand  
noise or losses make  
honest Bob's life more  
difficult



on **THE OTHER** hand  
multi-photon emissions  
enable dishonest Bob to  
cheat more easily

(obvious) fix: make Alice "more  
forgiving"

(undesired) result: cheating  
becomes easier

(obvious) fix: eliminate multi-photon  
emissions

(undesired) result: more vacuum  
rounds, honest Bob suffers

*need to try a bit harder...*

# A fault-tolerant protocol

# A fault-tolerant protocol

- ① (commit) Alice generates  $n$  pulses of random BB84 states and sends them to Bob.

# A fault-tolerant protocol

- ① (commit) Alice generates  $n$  pulses of random BB84 states and sends them to Bob.
- ② To commit to 0 (1) he measures all the incoming qubits in the computational (Hadamard) basis. Bob distributes the outcomes to agents occupying distant locations. Bob tells Alice which photons he received. Alice accepts if the losses are below a specific threshold. All the other rounds are discarded.

# A fault-tolerant protocol

- ① (commit) Alice generates  $n$  pulses of random BB84 states and sends them to Bob.
- ② To commit to 0 (1) he measures all the incoming qubits in the computational (Hadamard) basis. Bob distributes the outcomes to agents occupying distant locations. Bob tells Alice which photons he received. Alice accepts if the losses are below a specific threshold. All the other rounds are discarded.
- ③ (open) Bob's agents have to simultaneously unveil the committed bit and the measurement outcomes to Alice's agents.

# A fault-tolerant protocol

- ① (**commit**) Alice generates  $n$  pulses of random BB84 states and sends them to Bob.
- ② To commit to 0 (1) he measures all the incoming qubits in the computational (Hadamard) basis. Bob distributes the outcomes to agents occupying distant locations. Bob tells Alice which photons he received. Alice accepts if the losses are below a specific threshold. All the other rounds are discarded.
- ③ (**open**) Bob's agents have to simultaneously unveil the committed bit and the measurement outcomes to Alice's agents.
- ④ (**verify**) Alice's agents verify whether the outcomes provided by Bob are consistent with the BB84 states up to a certain number of errors.

# A fault-tolerant protocol - Security

One-commitment steps (honest execution):

- Alice sends  $N$  pulses, Bob reports detecting  $n$  of them
- Let
- After Bob revealed the commitment, Alice calculates the **QBER**:

$$\text{QBER} = n_{\text{err}}/n'$$

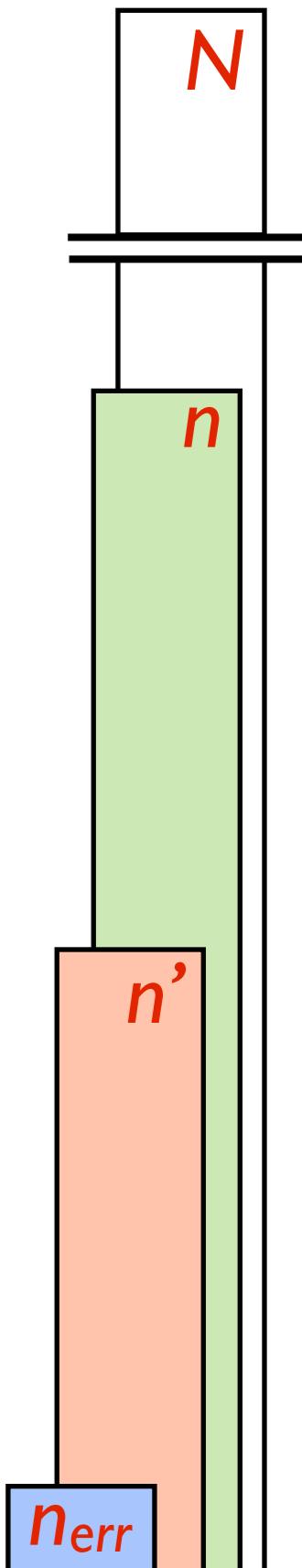
Number of errors within  $n'$

Number of detections with same basis  
for preparation and measurement

- Security is possible only if

$$p_{\text{det}} > \frac{1 - e^{-\mu}(1 + \mu)}{1 - \frac{\text{QBER}}{\lambda}} \quad \lambda \approx 14.6\%$$

- Calculate the security parameter from the finite stats



# A fault-tolerant protocol - Security

One-commitment steps (honest execution):

- Alice sends  $N$  pulses, Bob reports detecting  $n$  of them
- Let  $p_{\text{det}} = n/N$
- After Bob revealed the commitment, Alice calculates the **QBER**:

$$\text{QBER} = n_{\text{err}}/n'$$

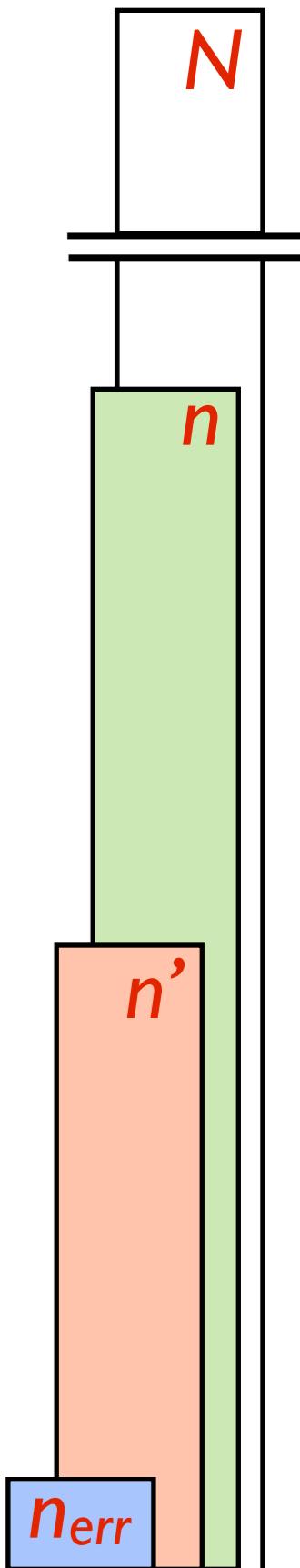
Number of errors within  $n'$

Number of detections with same basis  
for preparation and measurement

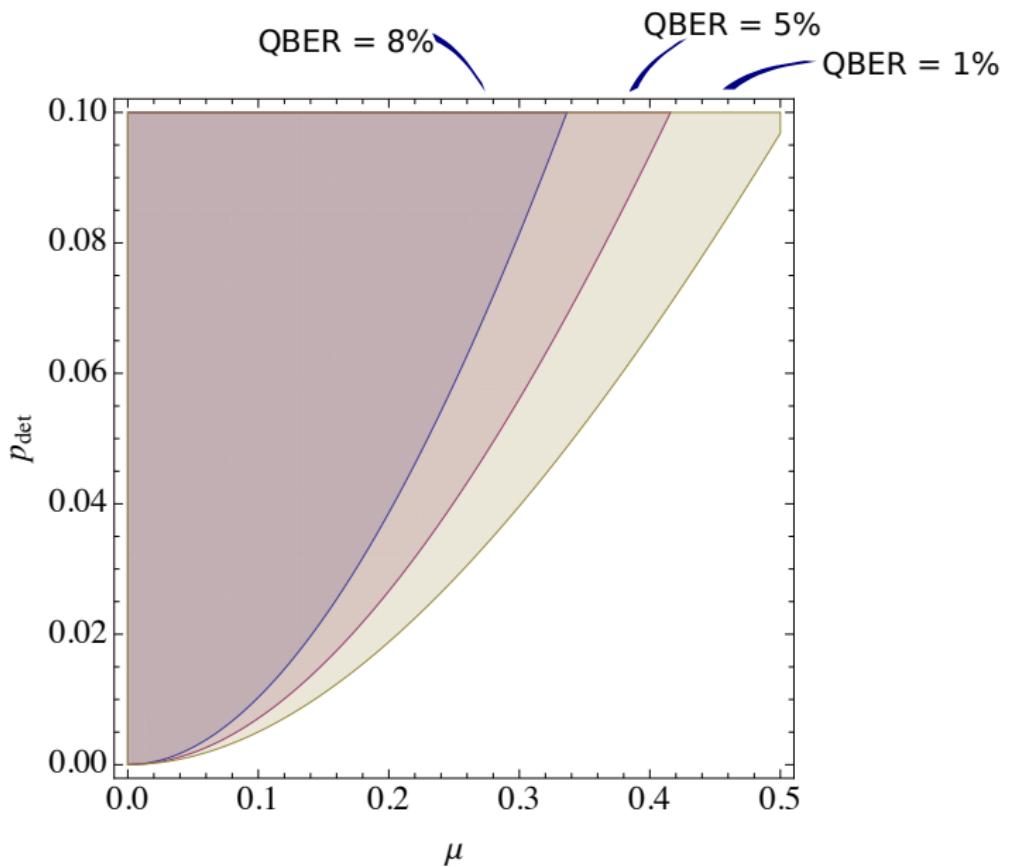
- Security is possible only if

$$p_{\text{det}} > \frac{1 - e^{-\mu}(1 + \mu)}{1 - \frac{\text{QBER}}{\lambda}} \quad \lambda \approx 14.6\%$$

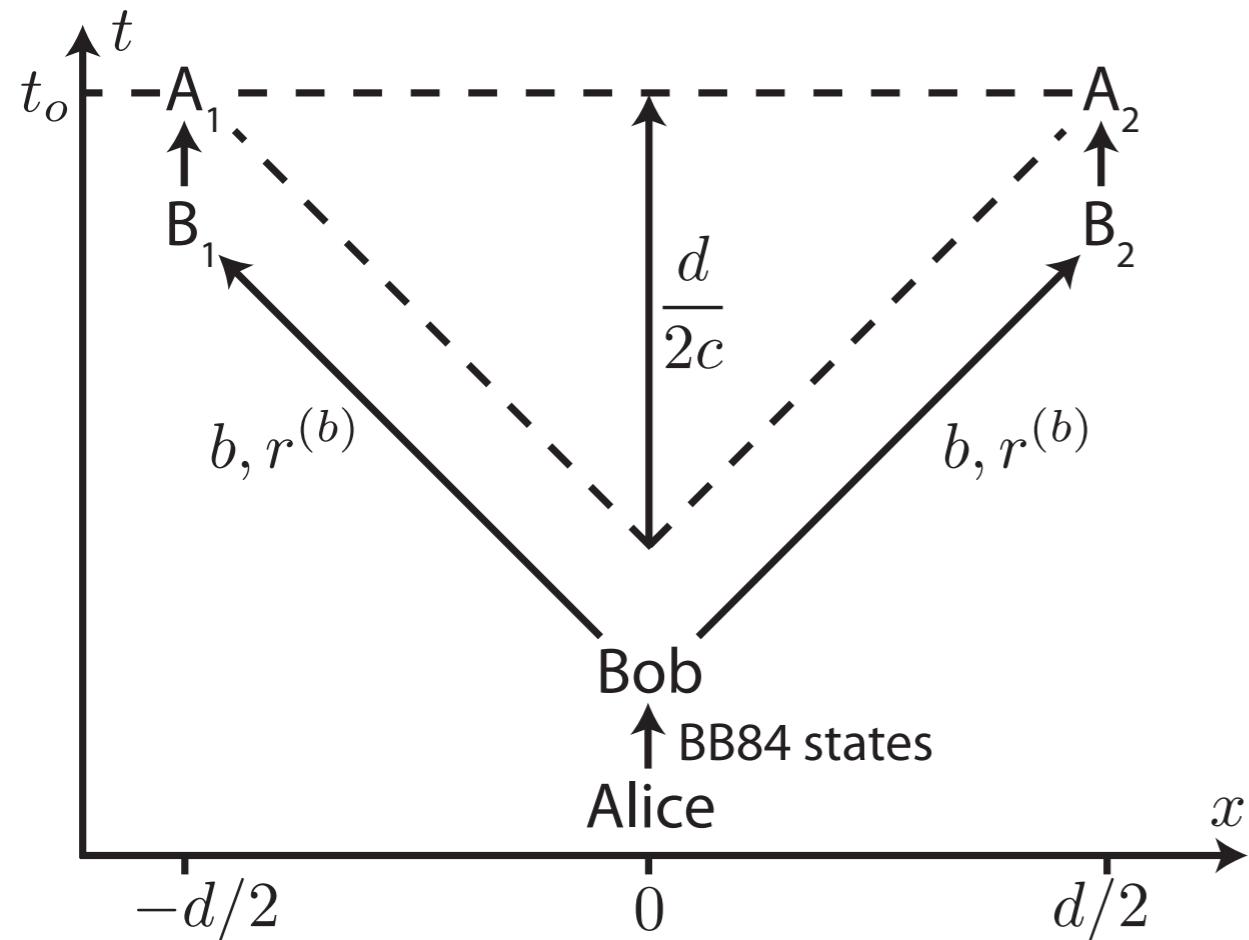
- Calculate the security parameter from the finite stats



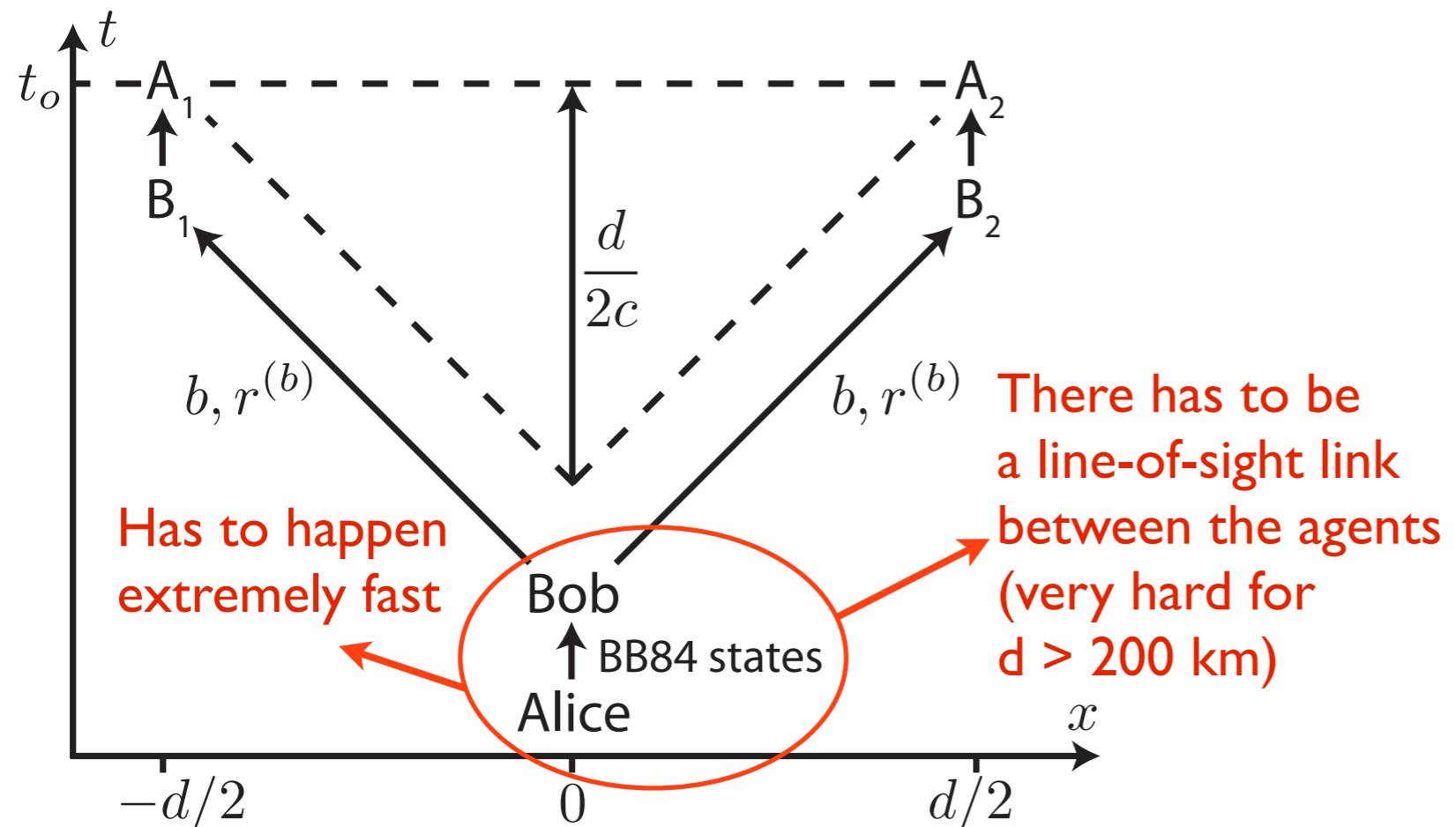
# Feasibility plot



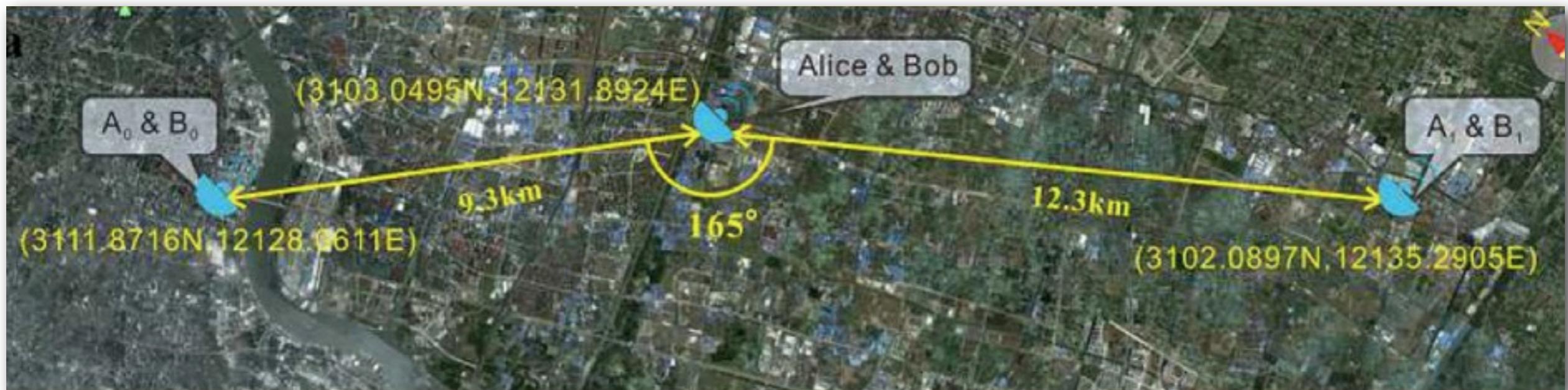
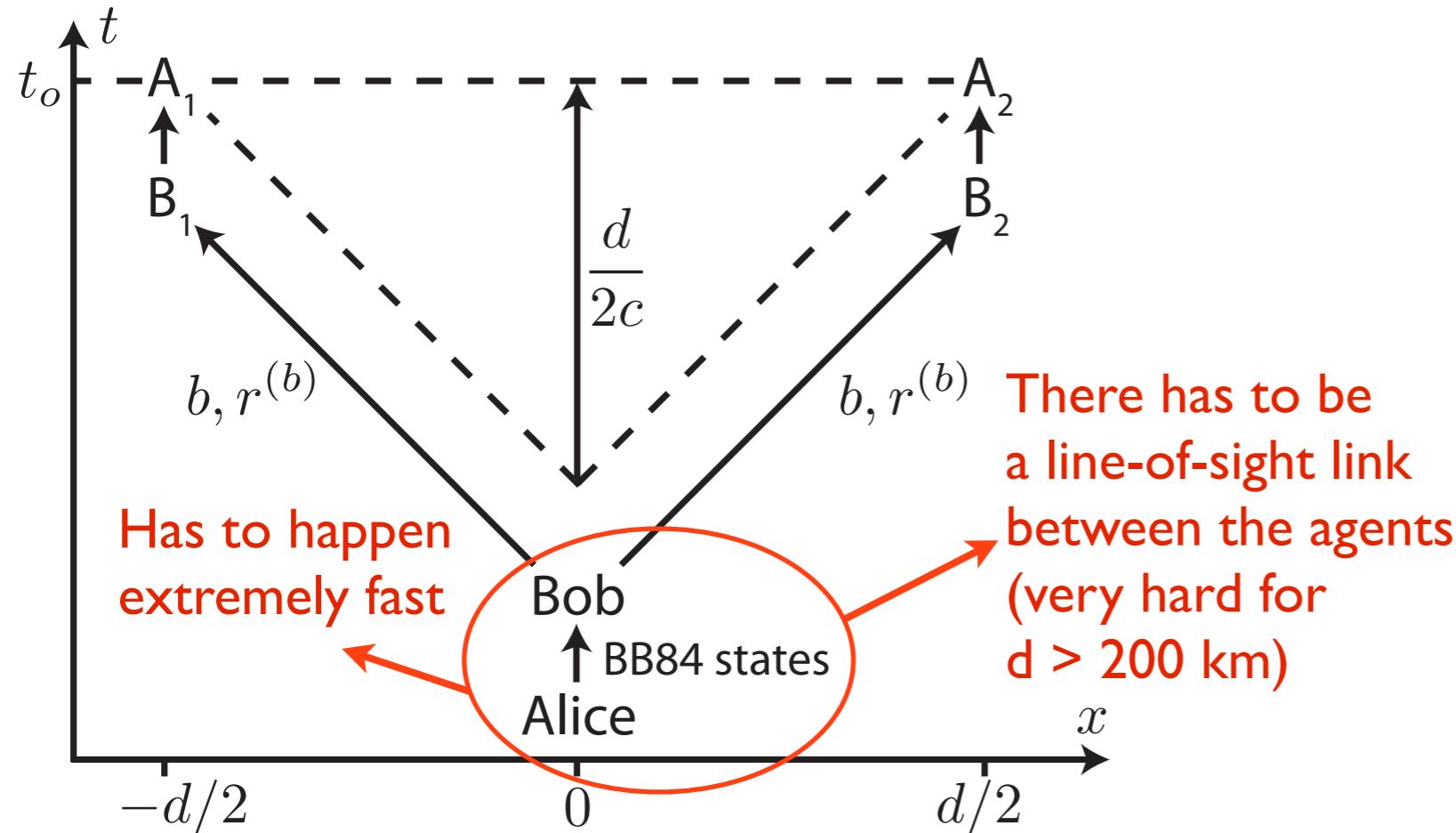
# A more practical version of Kent'12 protocol



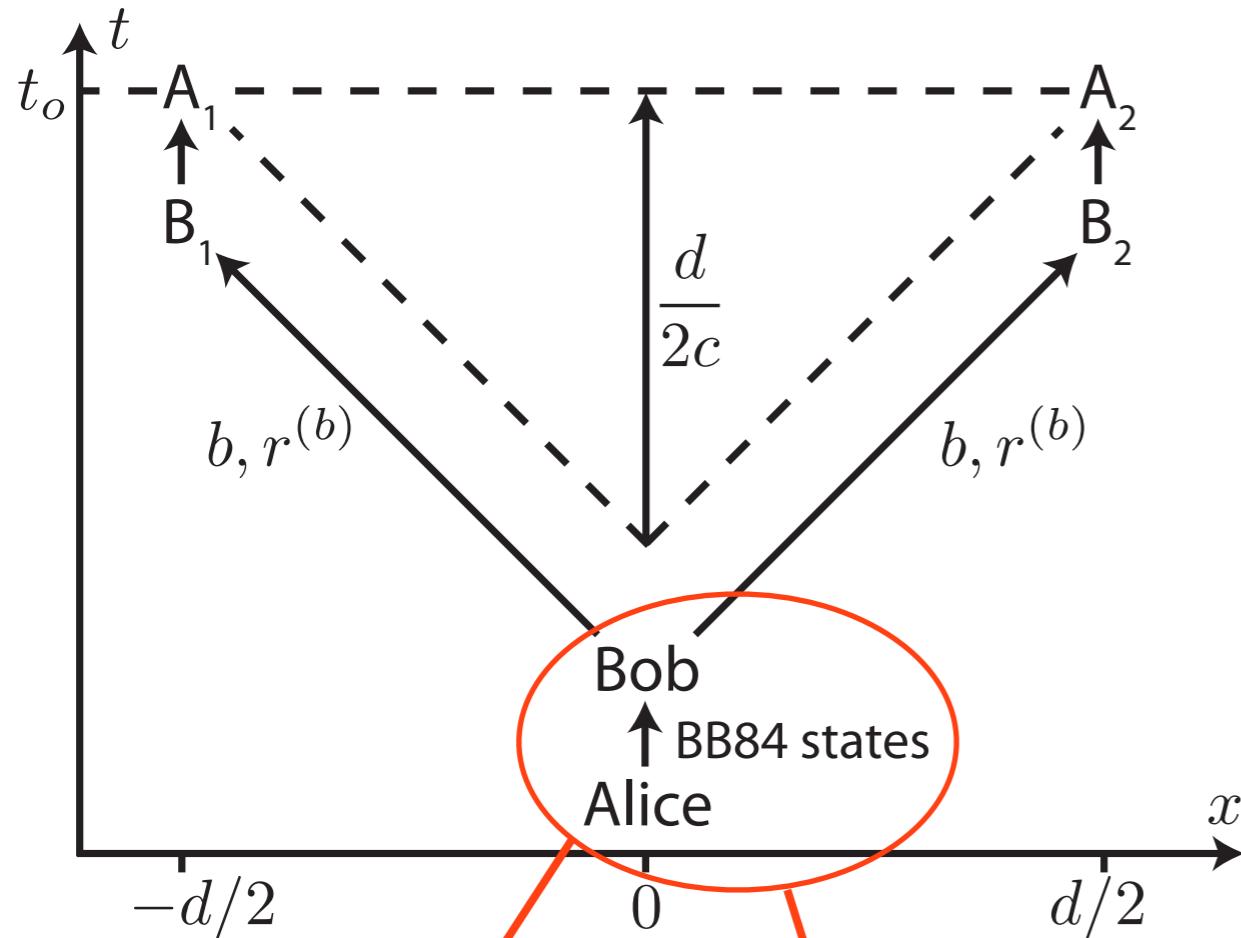
# A more practical version of Kent'12 protocol



# A more practical version of Kent'12 protocol



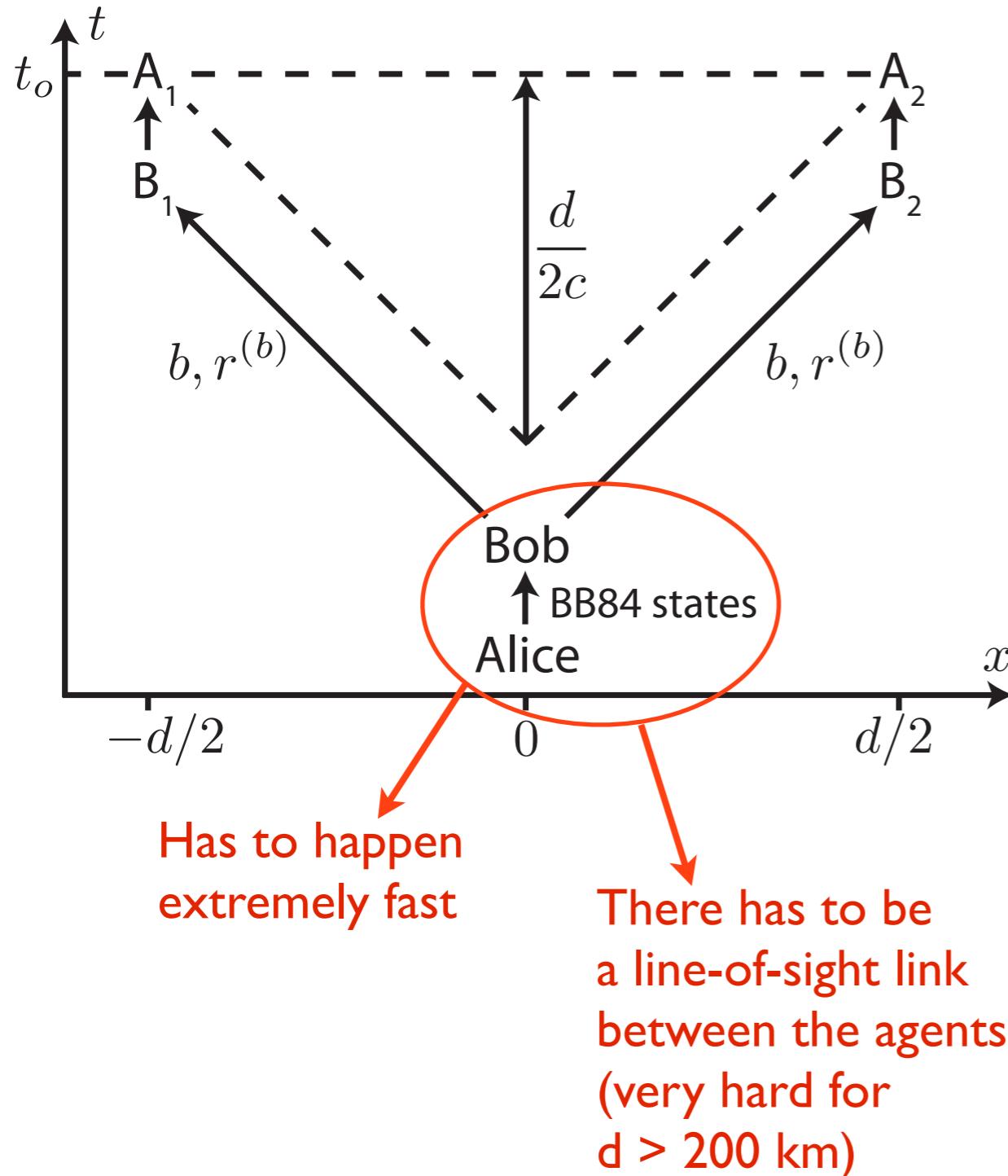
# A more practical version of Kent'12 protocol



Has to happen  
extremely fast

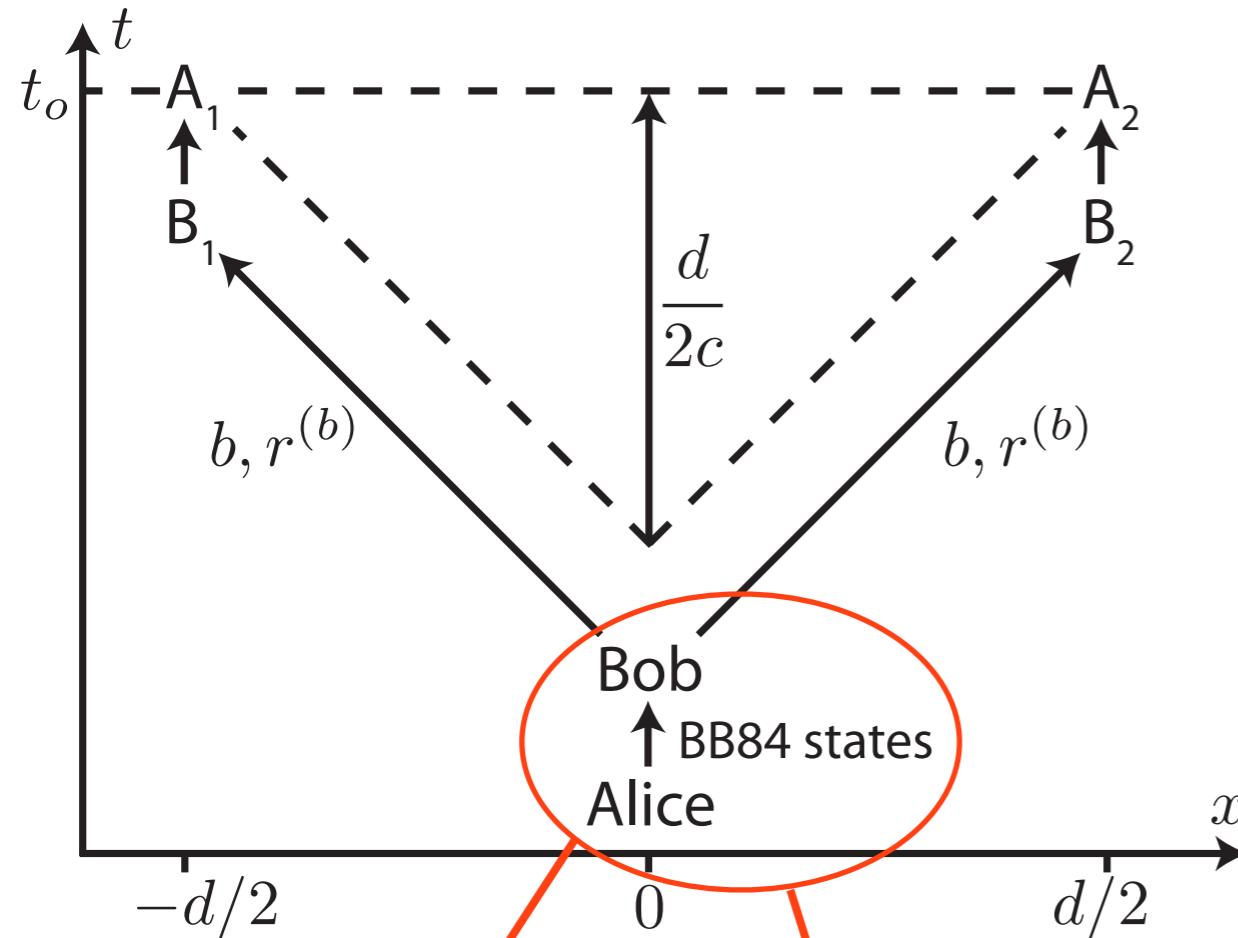
There has to be  
a line-of-sight link  
between the agents  
(very hard for  
 $d > 200$  km)

# A more practical version of Kent'12 protocol



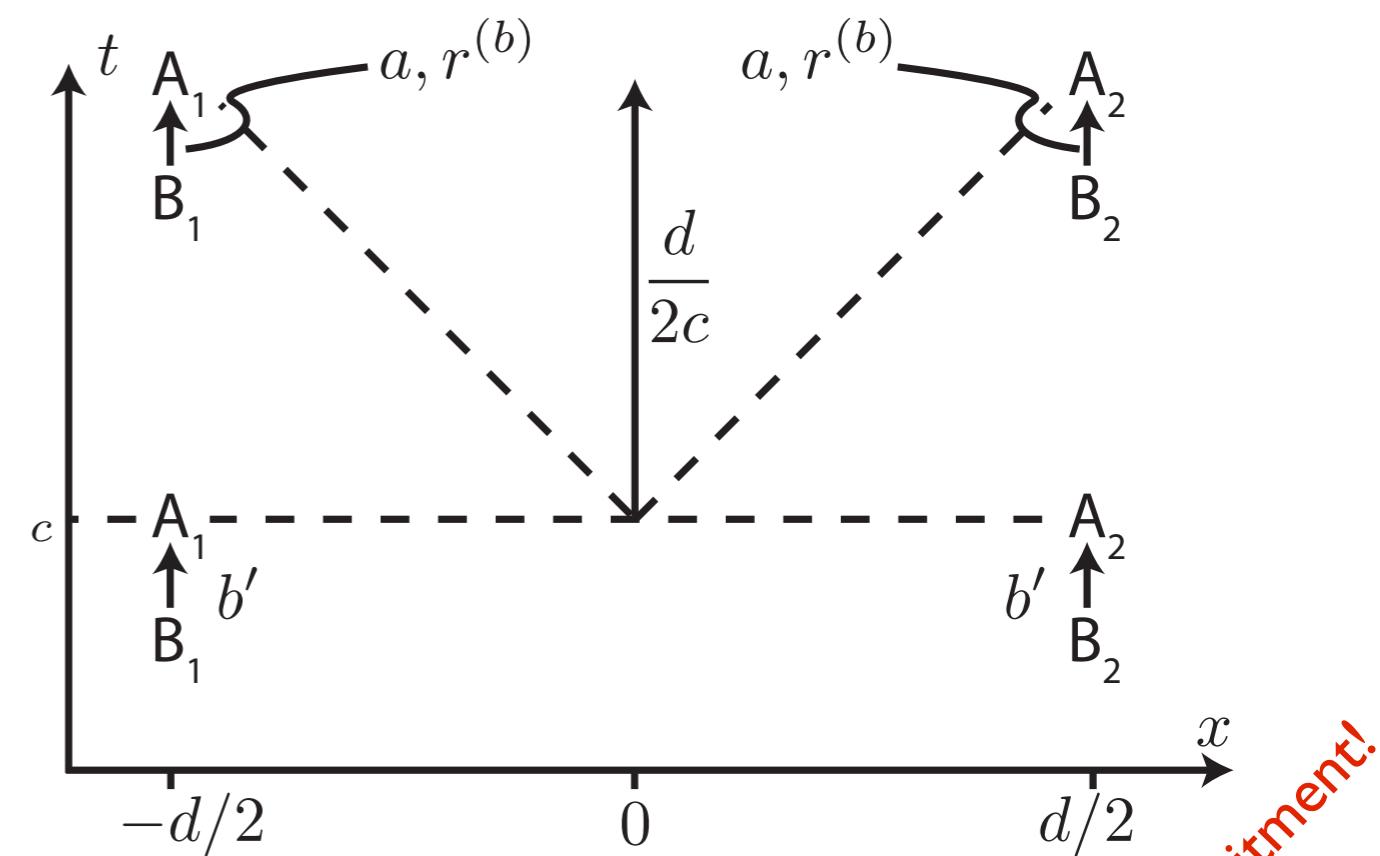
The quantum exchange happens in advance. Bob measures all qubits in a random basis  $b$  and informs  $B_1$  and  $B_2$  of the results  $r^{(b)}$

# A more practical version of Kent'12 protocol



Has to happen extremely fast

There has to be a line-of-sight link between the agents (very hard for  $d > 200$  km)

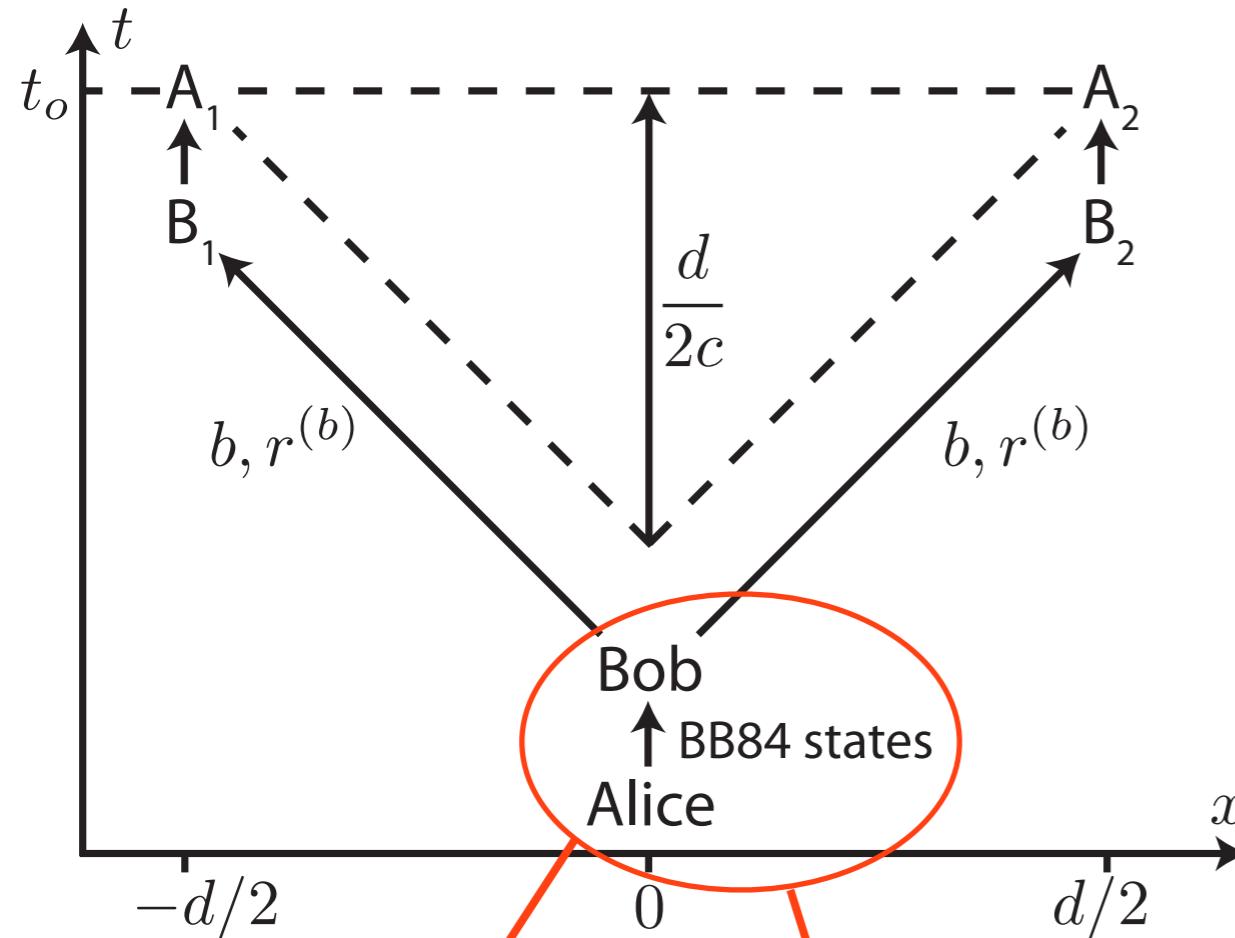


The quantum exchange happens in advance. Bob measures all qubits in a random basis  $b$  and informs  $B_1$  and  $B_2$  of the results  $r^{(b)}$

$B_1$  and  $B_2$  simultaneously commit to  $b' = b \oplus a$

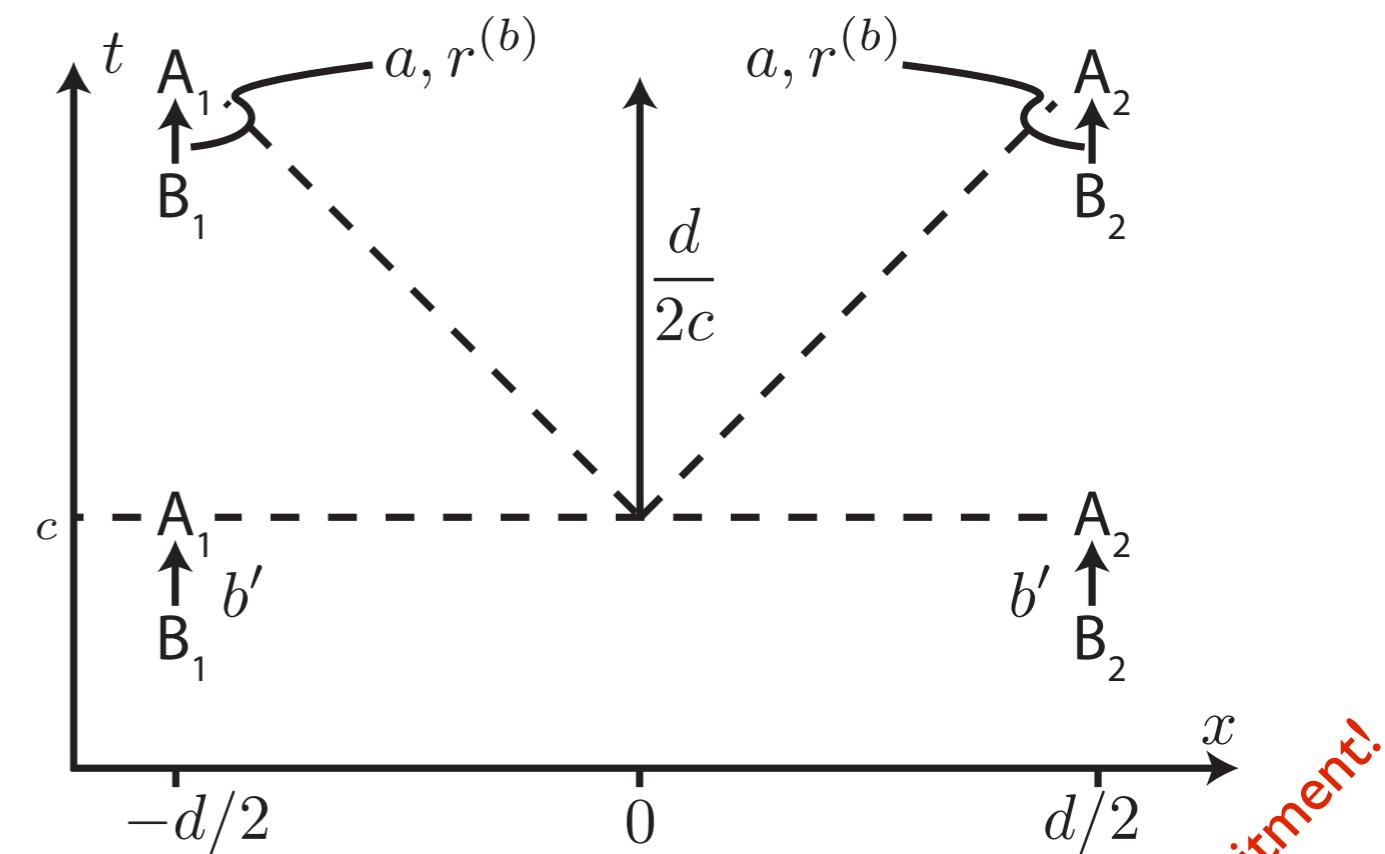
Commitment!

# A more practical version of Kent'12 protocol



Has to happen extremely fast

There has to be a line-of-sight link between the agents (very hard for  $d > 200$  km)

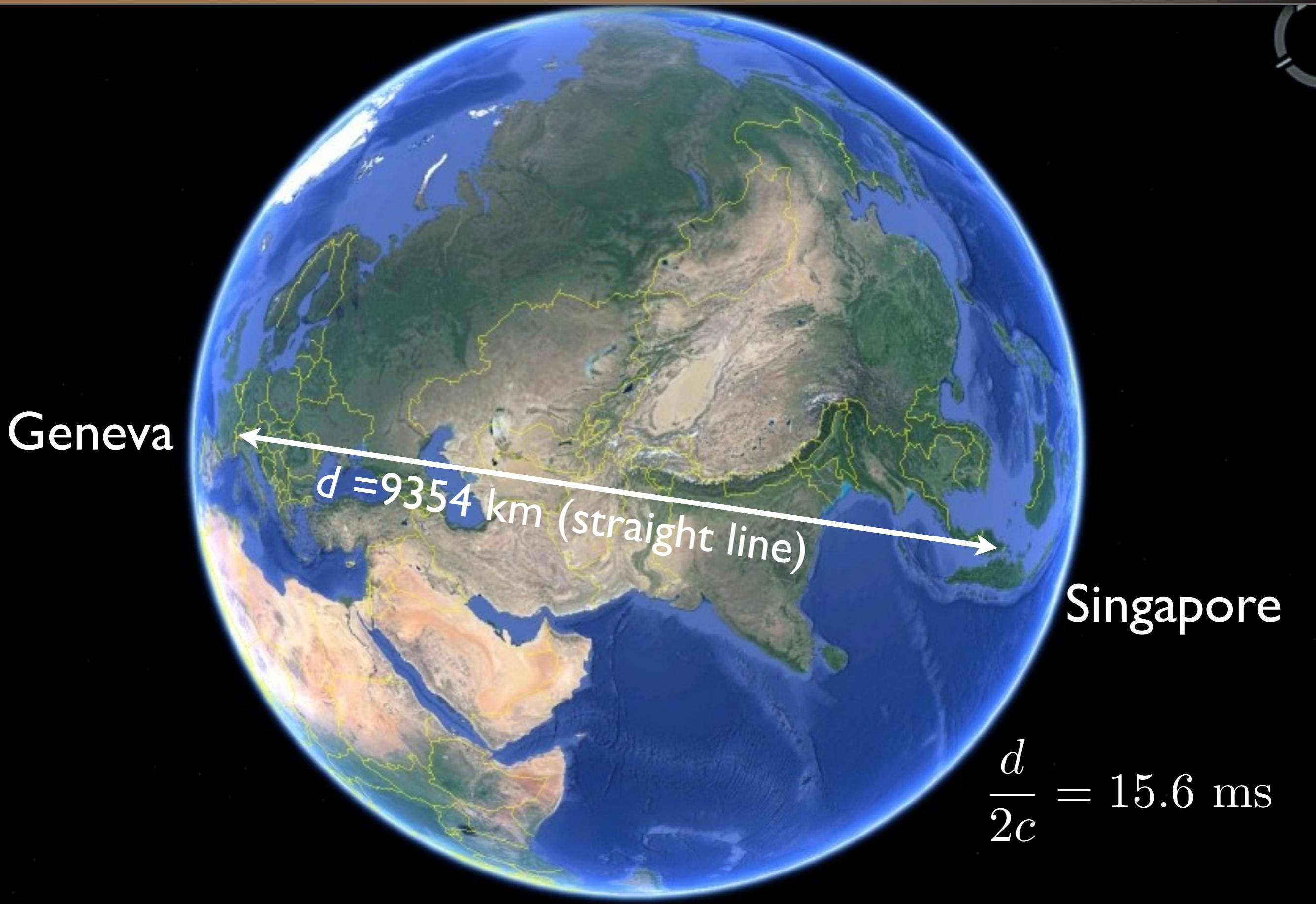


The quantum exchange happens in advance. Bob measures all qubits in a random basis  $b$  and informs  $B_1$  and  $B_2$  of the results  $r^{(b)}$

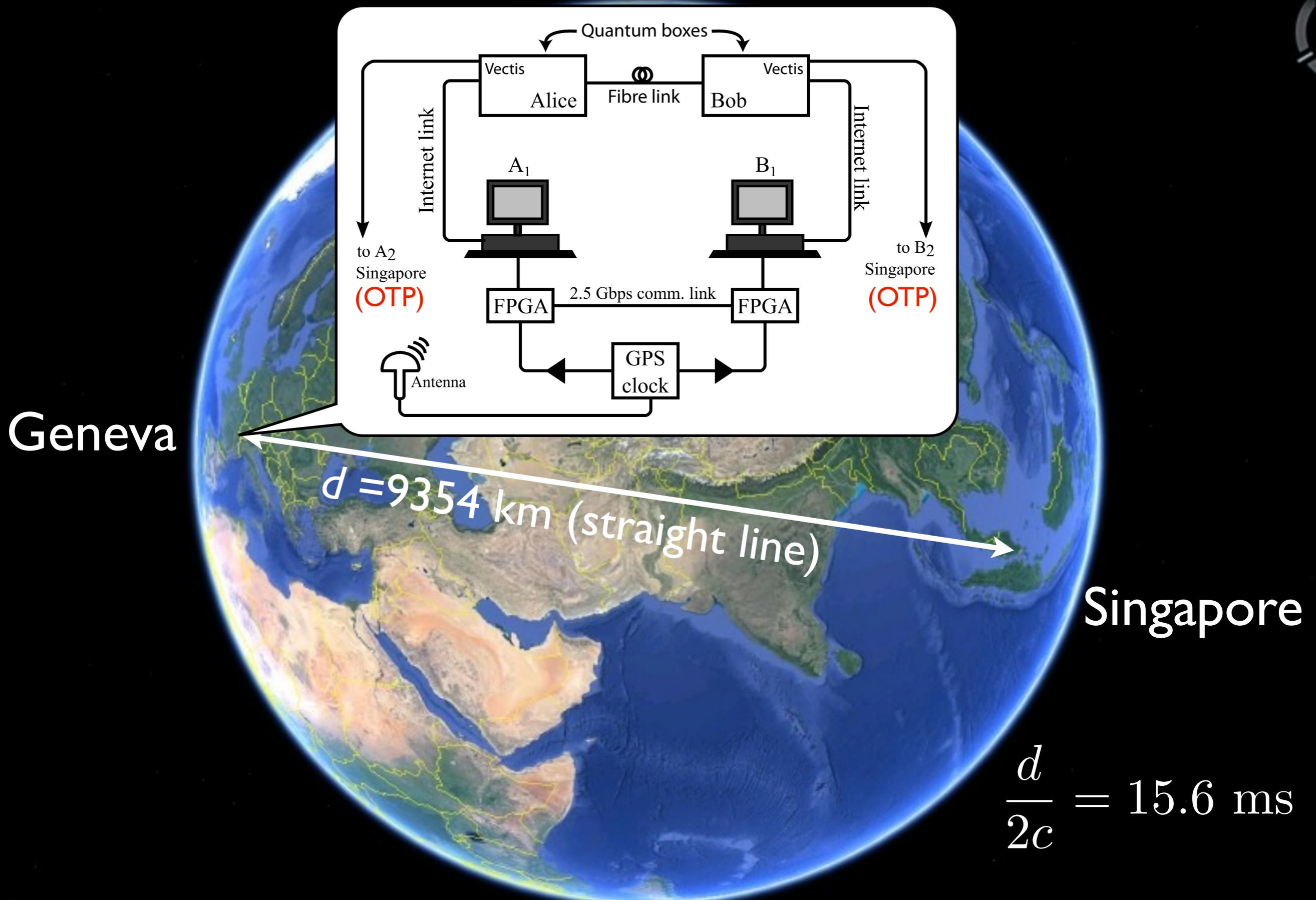
$B_1$  and  $B_2$  simultaneously commit to  $b' = b \oplus a$

$B_1$  and  $B_2$  simultaneously reveal  $a$  and  $r^{(b)}$

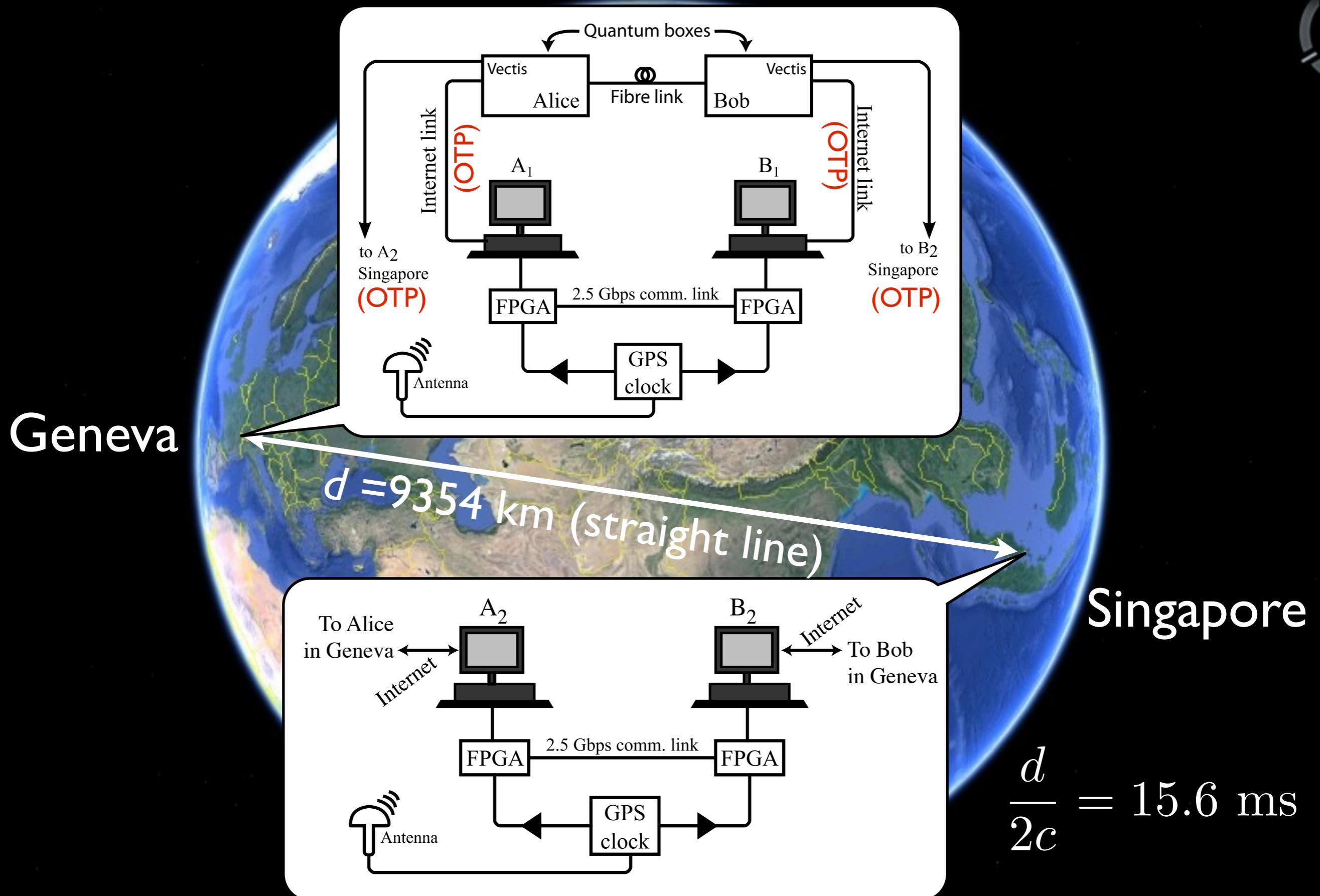
# Experimental setup - The global picture



# Experimental setup - The global picture

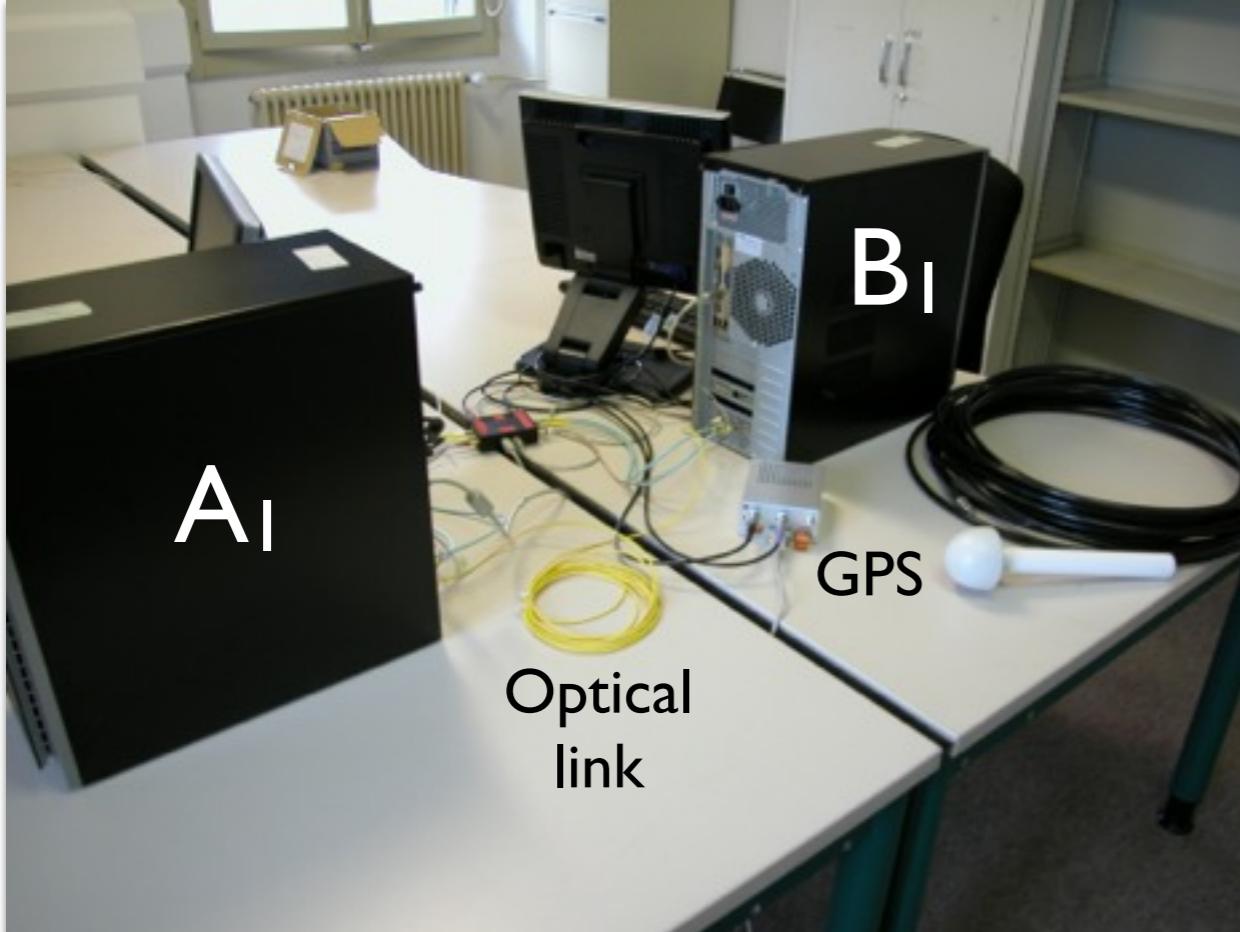


# Experimental setup - The global picture

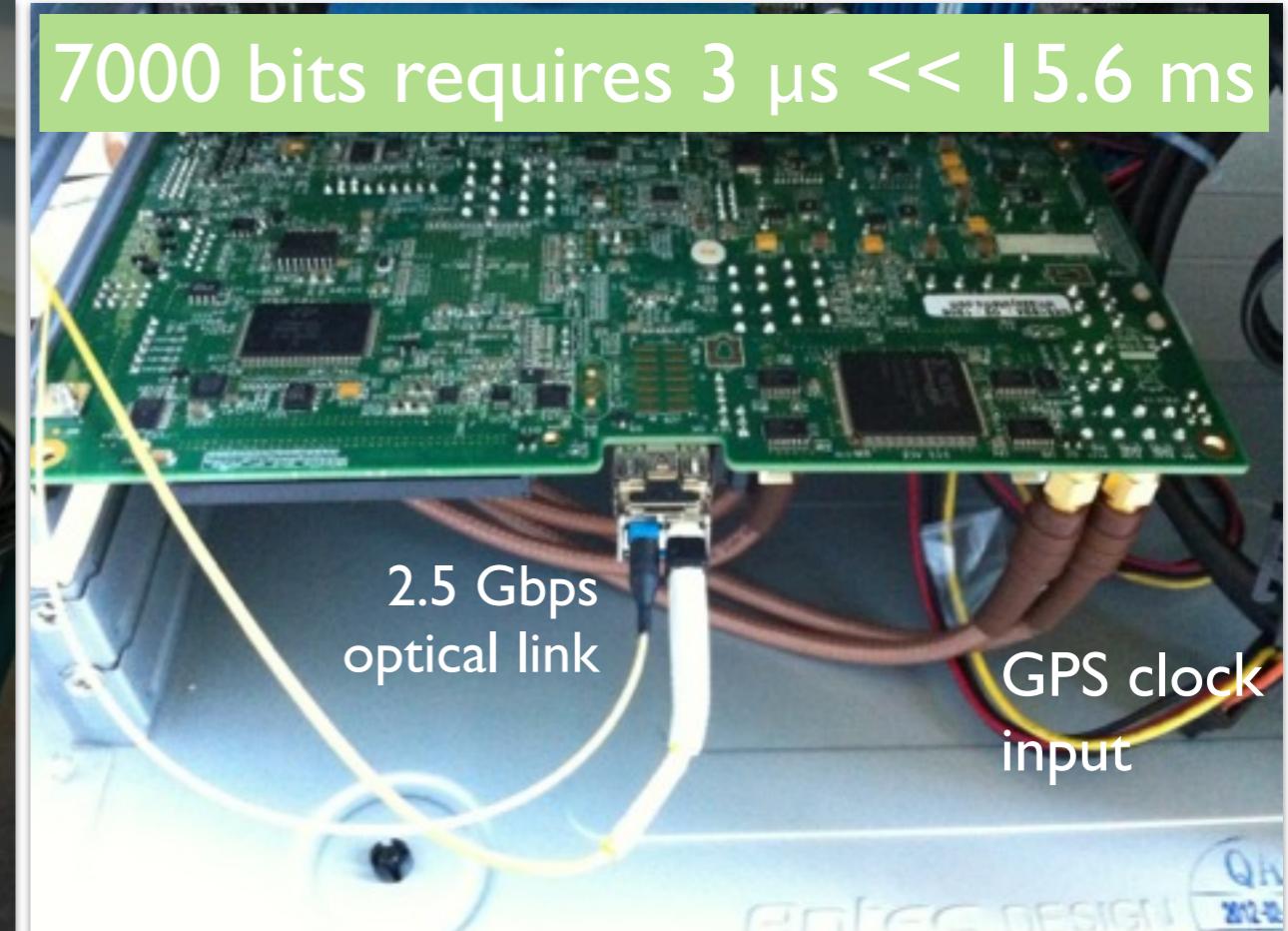


# The classical agents : timing performances

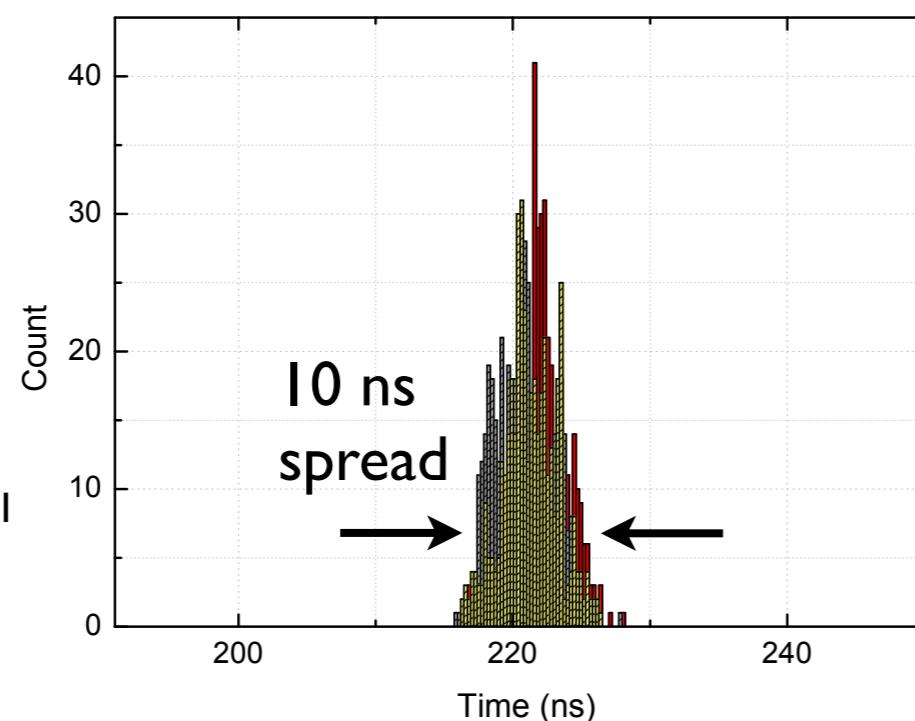
## Classical agents in Geneva



## FPGA boards



Timing accuracy  
of the FPGAs  
with a GPS for  $A_I$   
and another for  $B_I$

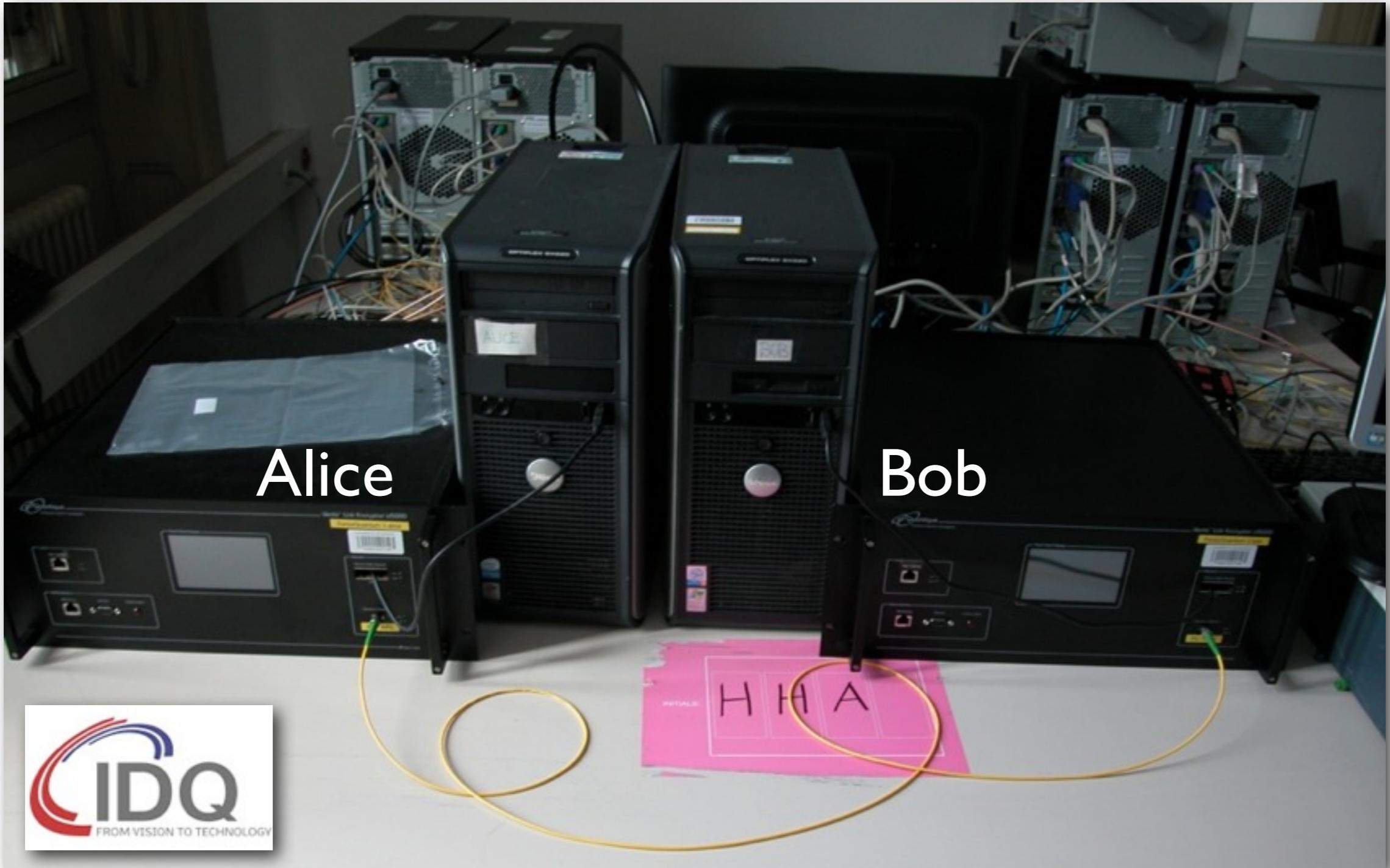


Other tests showed that

- $B_I$  and  $B_2$  are in sync to within 100 ns
- Synchronization is maintained over the 15 ms of the protocol

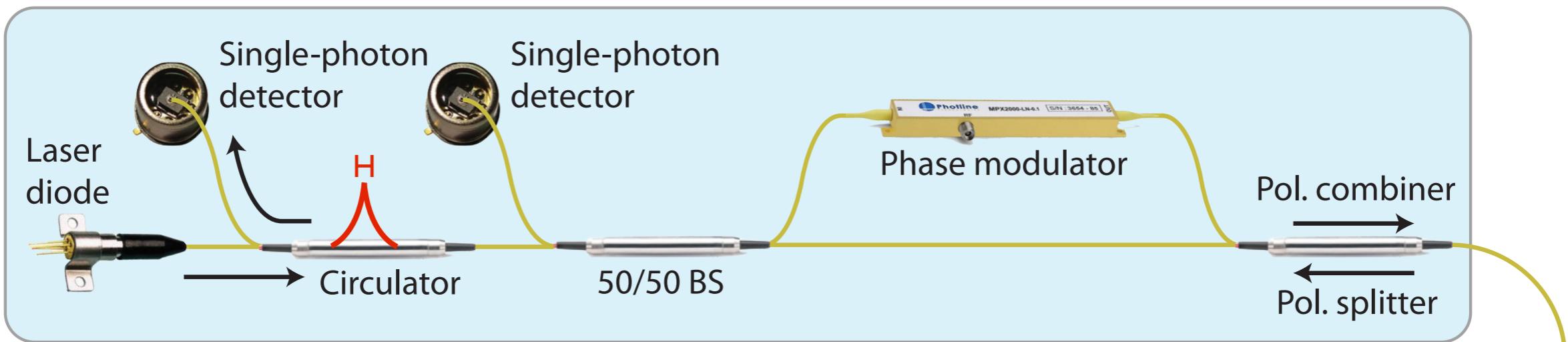
# The quantum boxes (Geneva)

Commercial QKD system by IDQ “Vectis 5100”

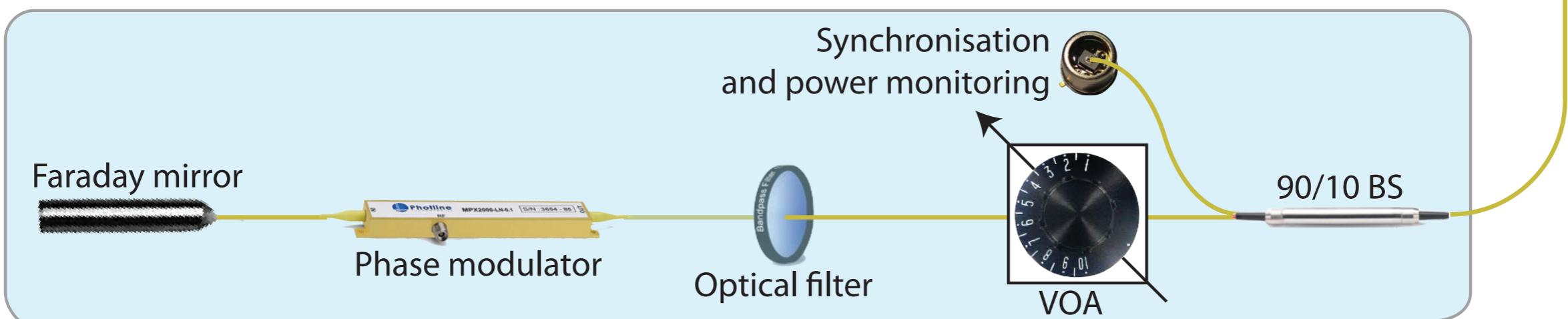


# The quantum boxes (Geneva)

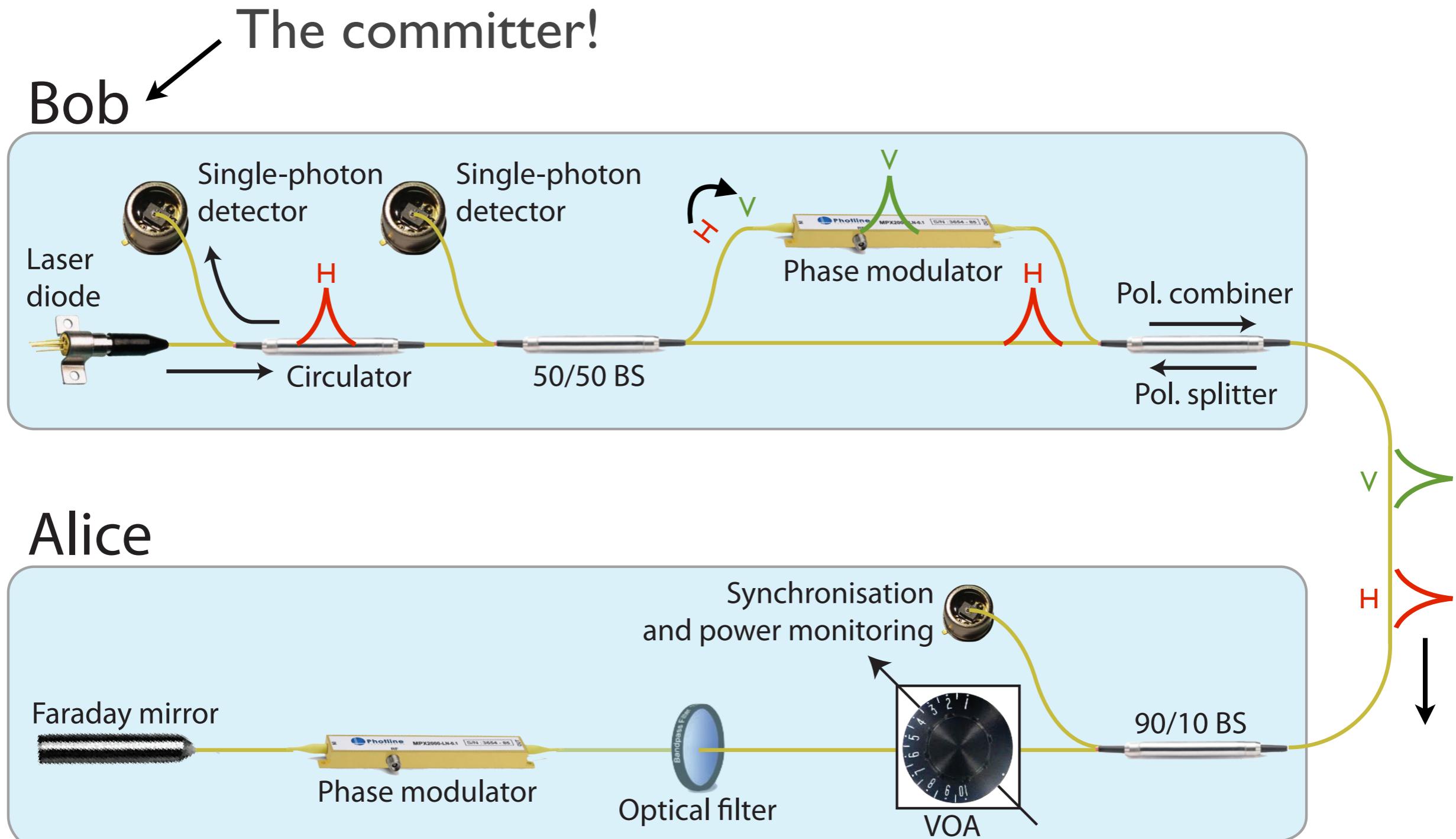
The committer!  
Bob



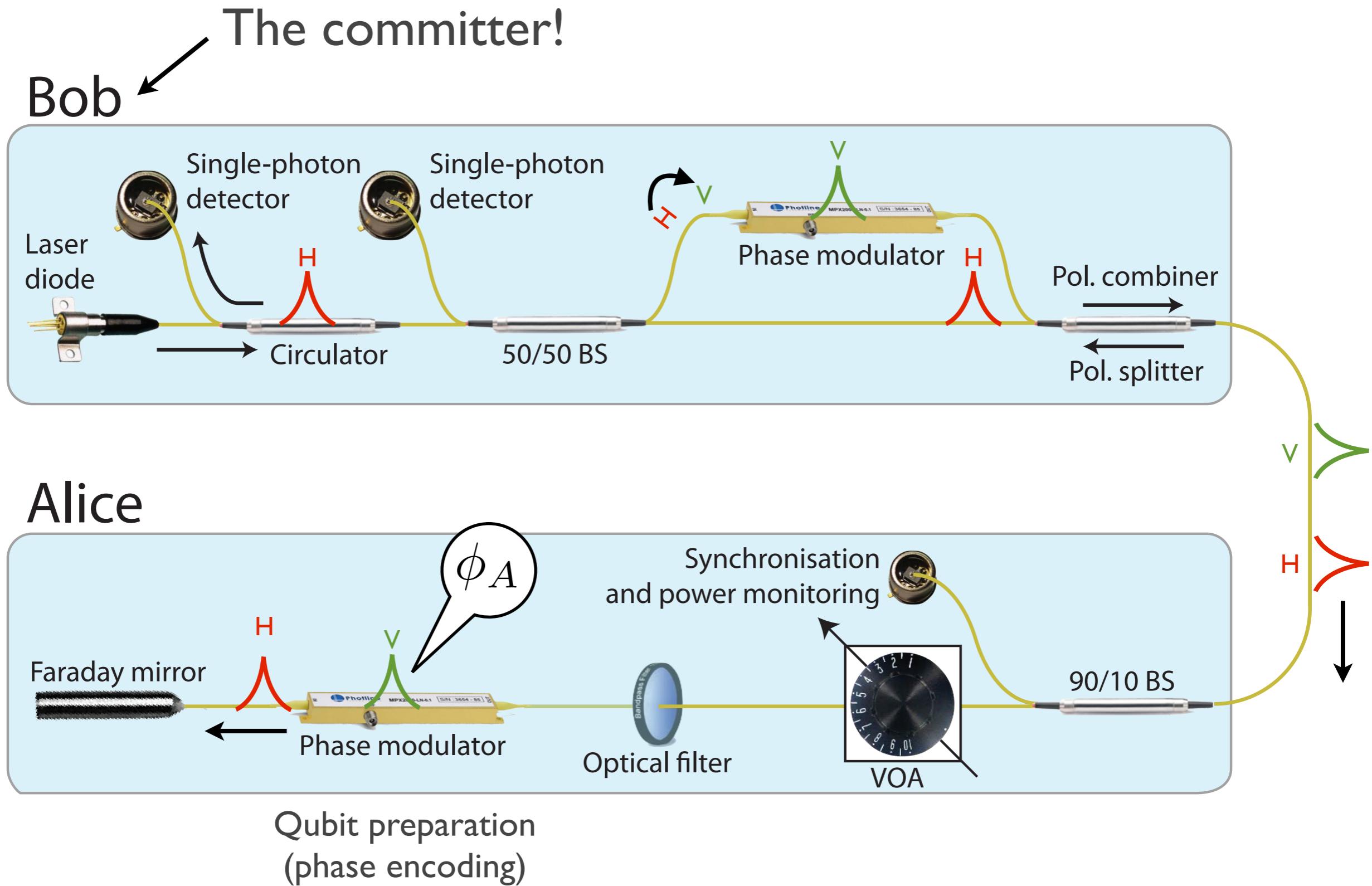
Alice



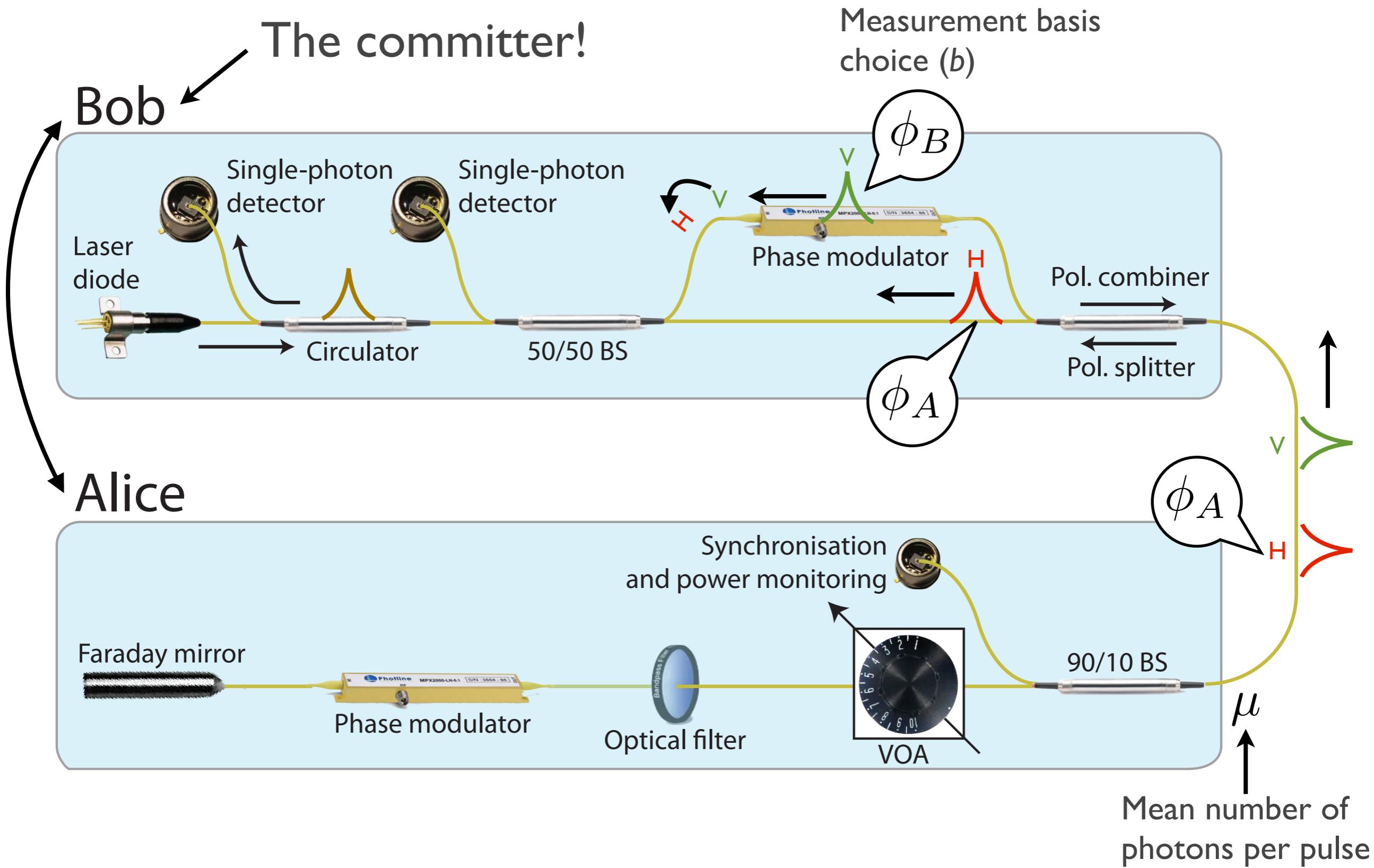
# The quantum boxes (Geneva)



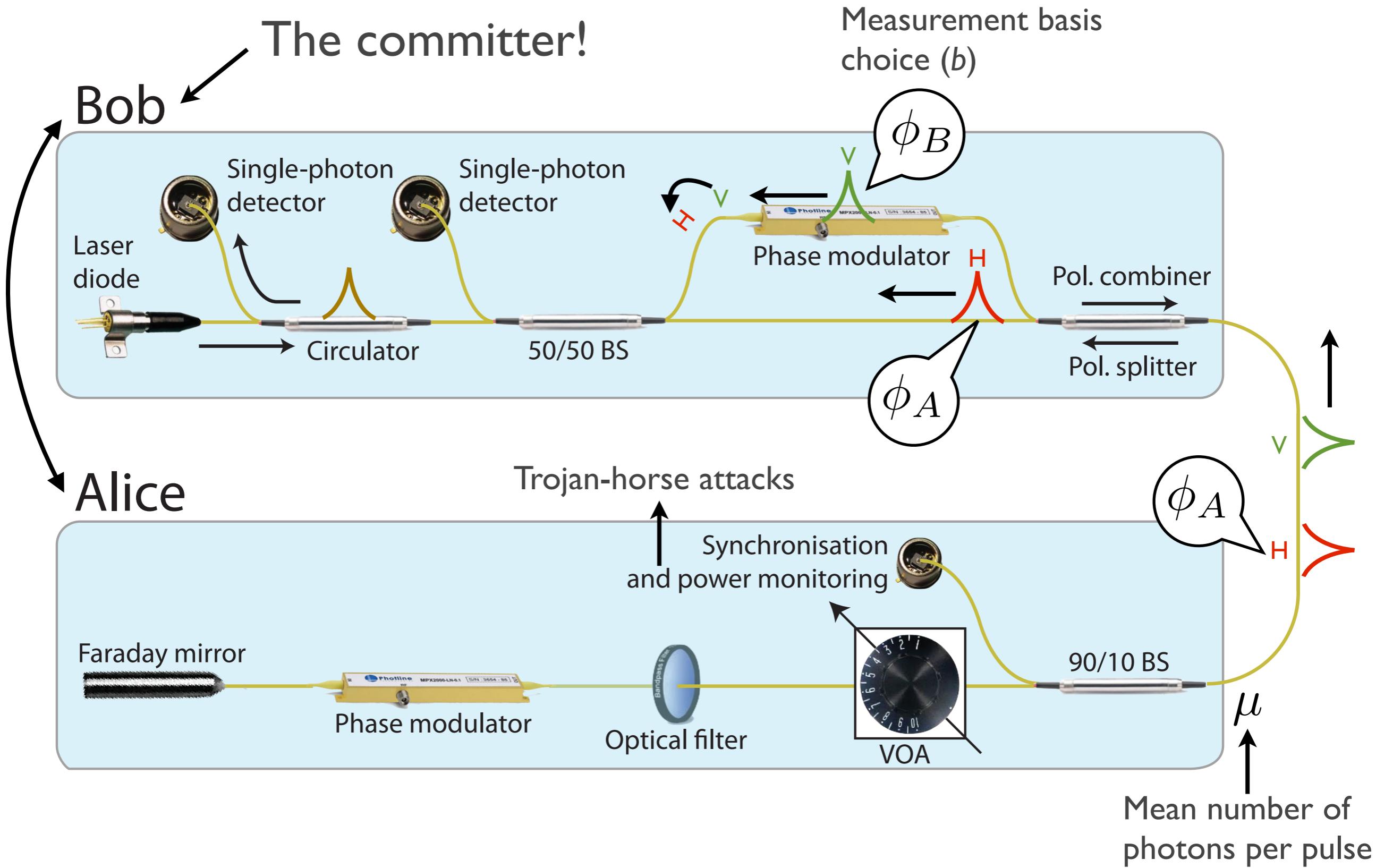
# The quantum boxes (Geneva)



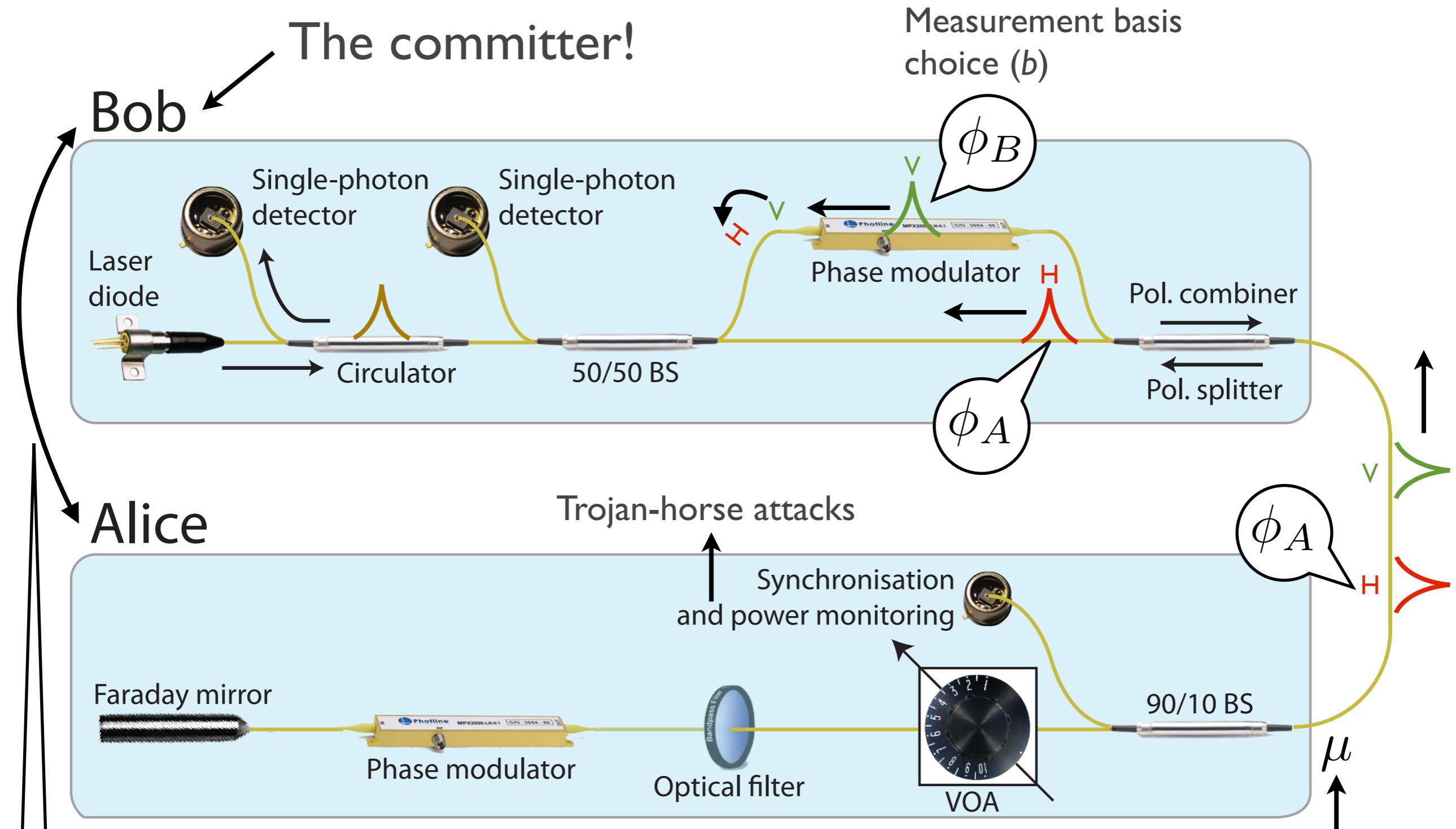
# The quantum boxes (Geneva)



# The quantum boxes (Geneva)



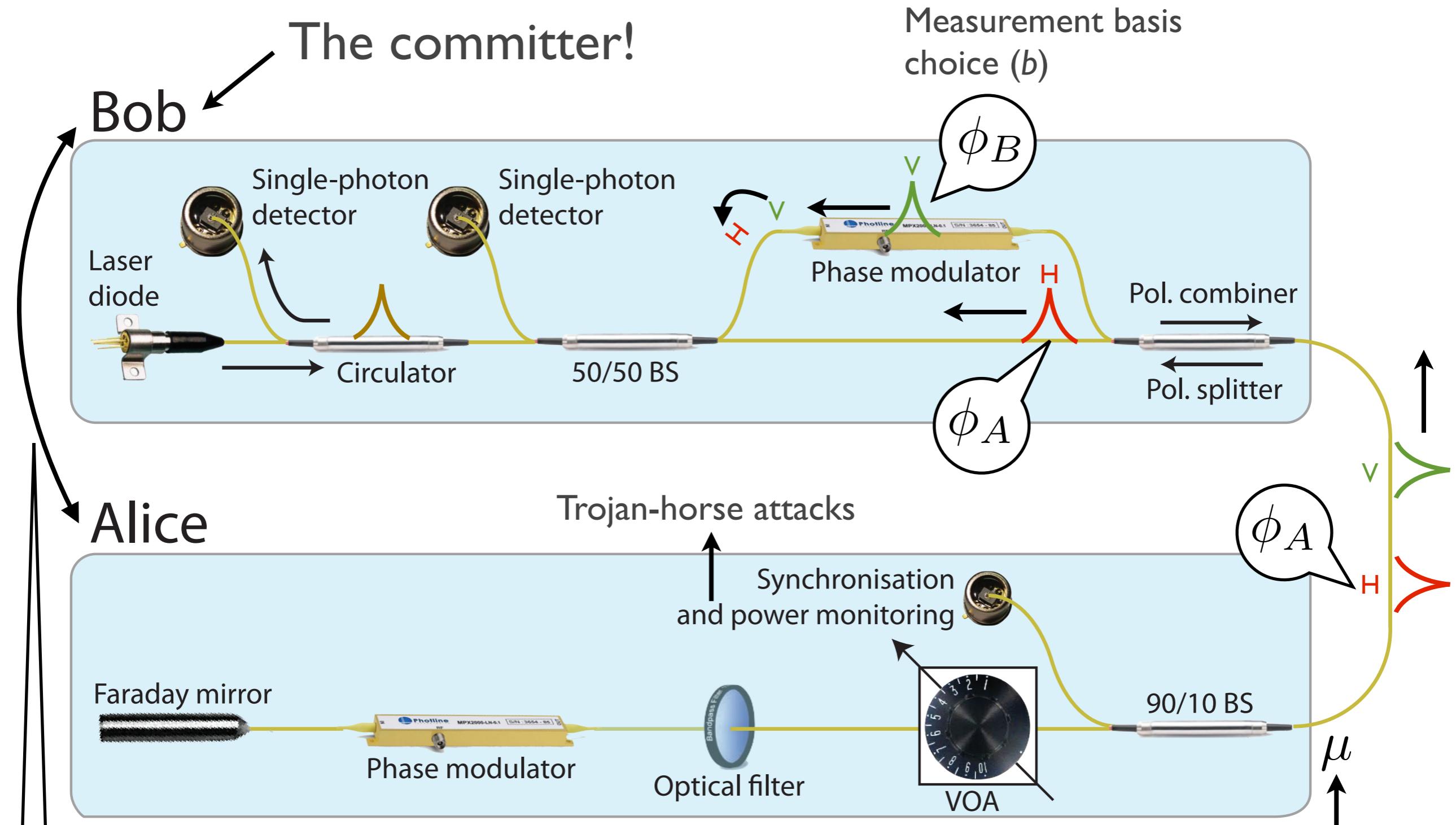
# The quantum boxes (Geneva)



- Which pulses were detected
- Basis reconciliation

Mean number of photons per pulse  
 $\mu$

# The quantum boxes (Geneva)

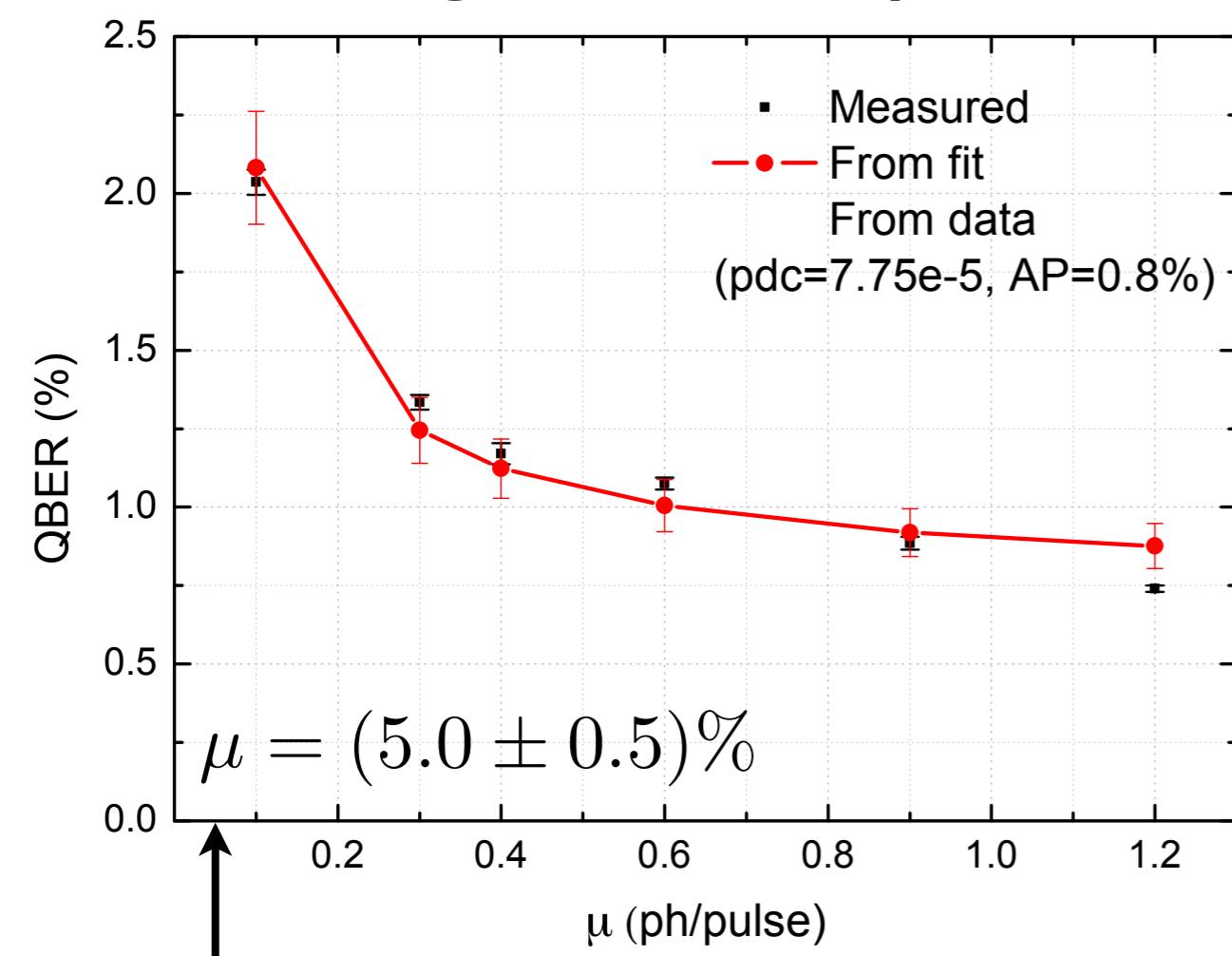


- Which pulses were detected
- Basis reconciliation

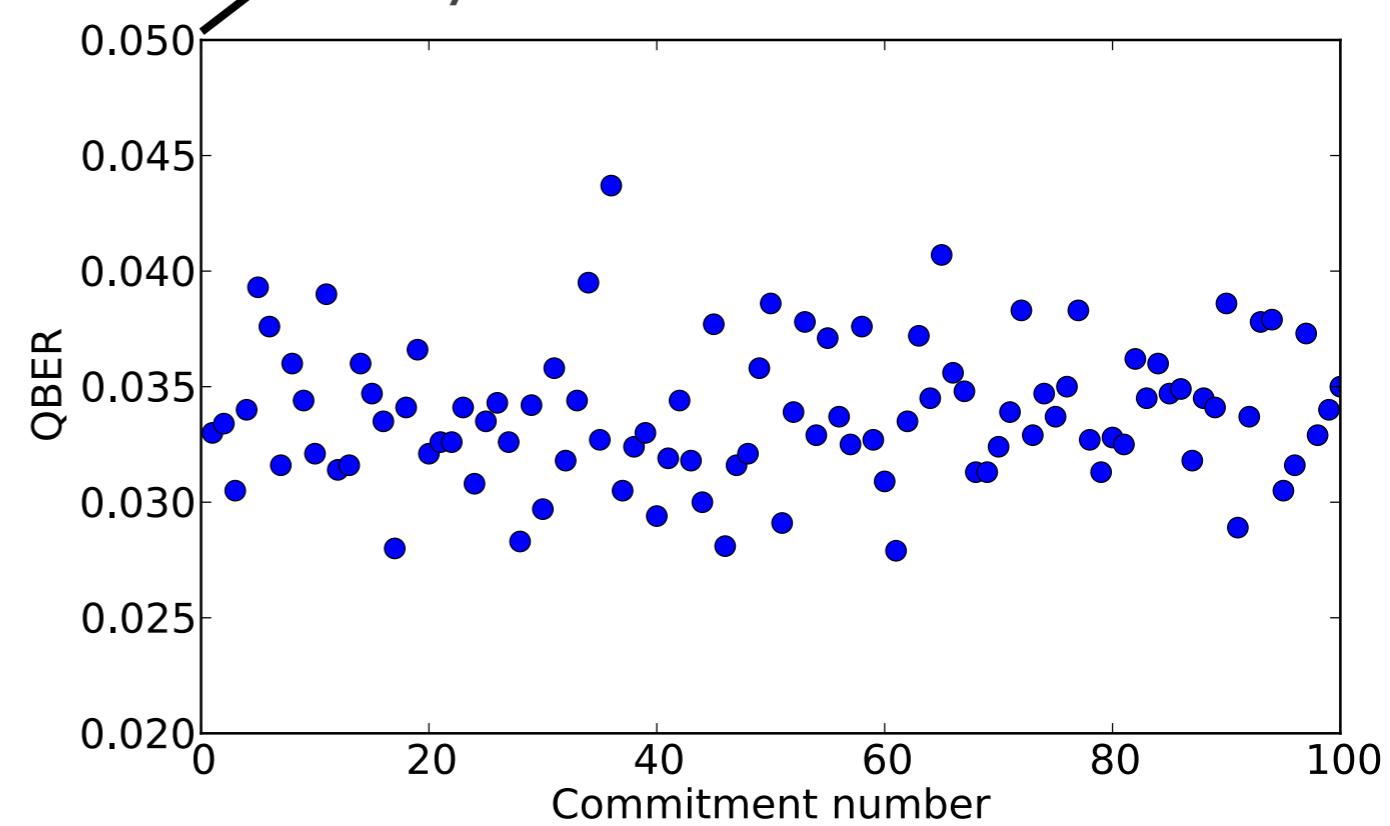
Mean number of photons per pulse

# The quantum boxes (Geneva) : performances

## Choosing $\mu$ : security trade-off

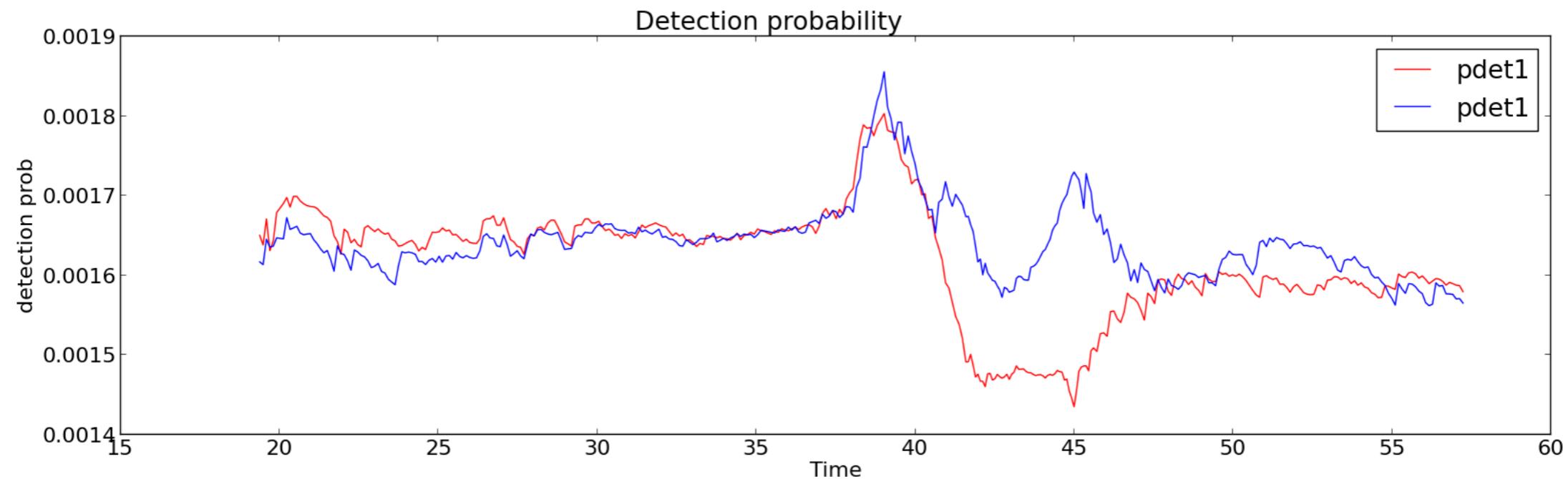


Took 5% as the maximum QBER for finite statistics analysis



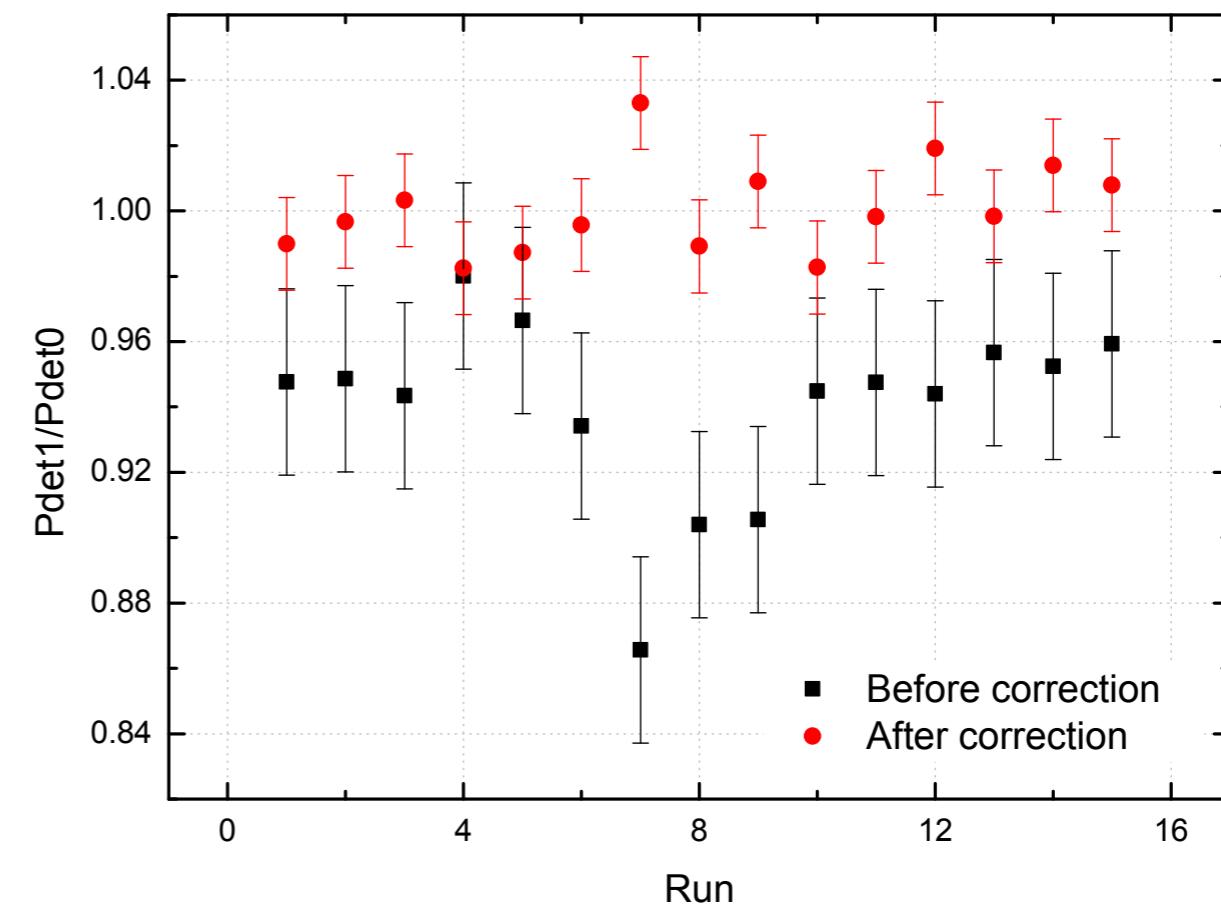
# The quantum boxes (Geneva) : performances

Stability of the detection probability : Bob must monitor!



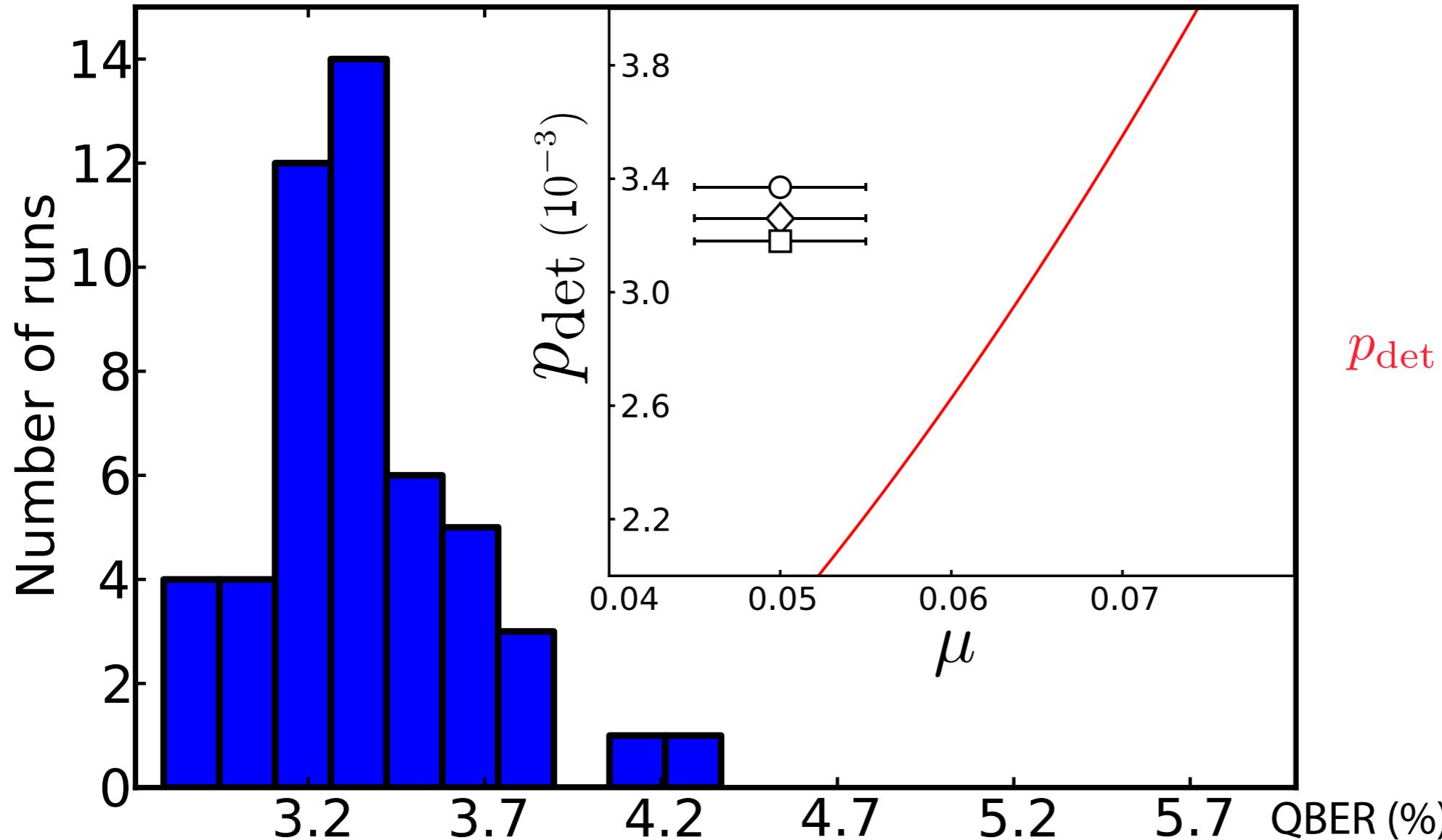
Basis detection probability mismatch: side-channel!

Software bias elimination.



# The quantum boxes (Geneva) : performances

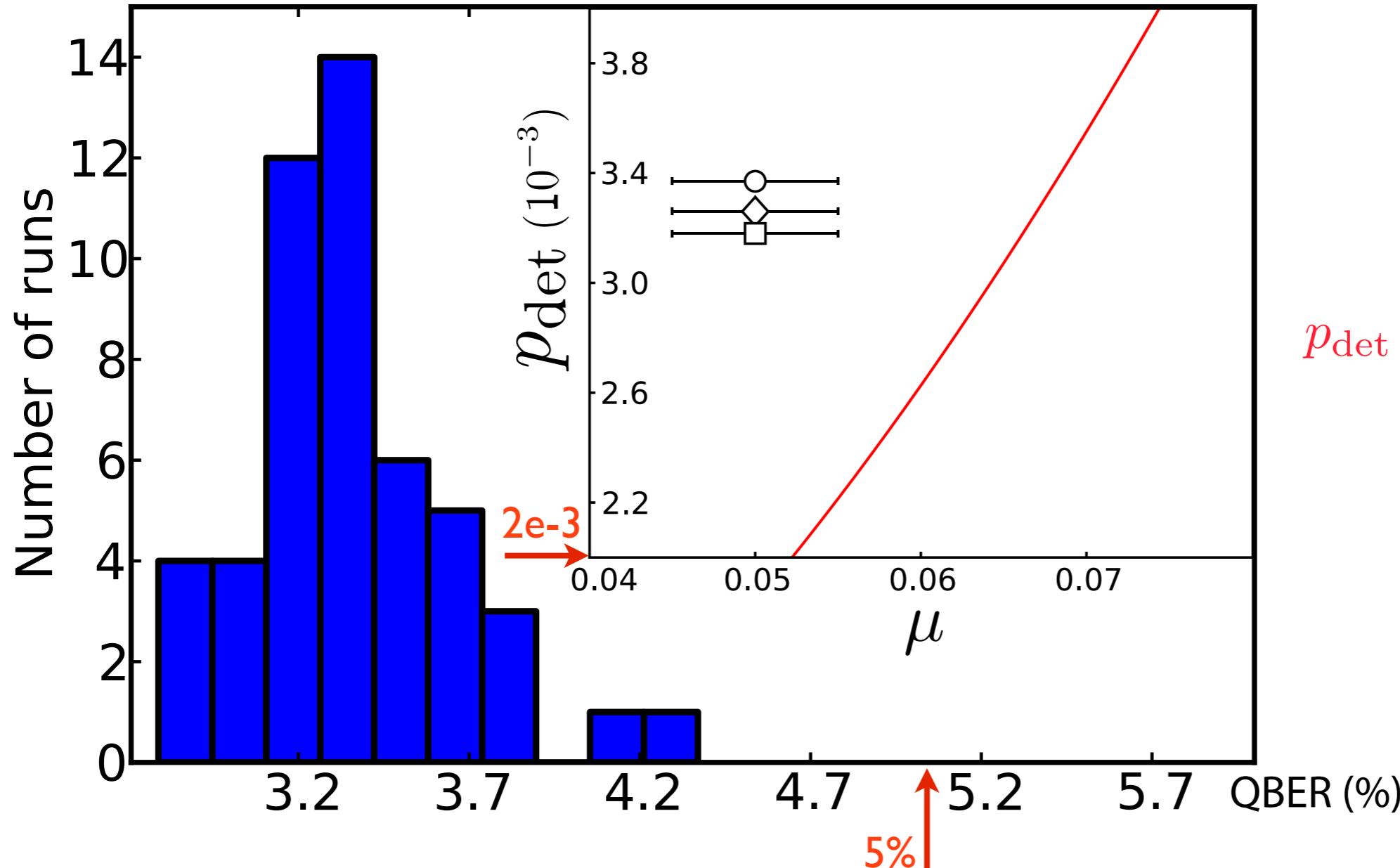
Results: 50 commitments of bit I from  
7000 detections at Bob's



$$p_{\text{det}} > \frac{1 - e^{-\mu}(1 + \mu)}{1 - \frac{\text{QBER}}{\lambda}}$$

# The quantum boxes (Geneva) : performances

Results: 50 commitments of bit I from  
7000 detections at Bob's



Security  
parameter       $\epsilon \leq 5.5 \times 10^{-8}$

$$p_{\text{det}} > \frac{1 - e^{-\mu}(1 + \mu)}{1 - \frac{\text{QBER}}{\lambda}}$$

# Summary and outlook

- First implementation of bit commitment using quantum communication and special relativity
- Closing on the maximum commitment time allowed on the surface of the Earth
- Possible extensions for sustained commitments with constant communication at each round? (Kent'05)



UNIVERSITÉ  
DE GENÈVE



NUS  
National University  
of Singapore



UNIVERSITY OF  
CAMBRIDGE

PI

**QSIT** Quantum  
Science and  
Technology  
National Centre of Competence in Research

**IDQ**  
FROM VISION TO TECHNOLOGY

 OSCILLOQUARTZ