



of great importance to get to know such cyber-attacks, detect them, and develop effective preventive measures. This is

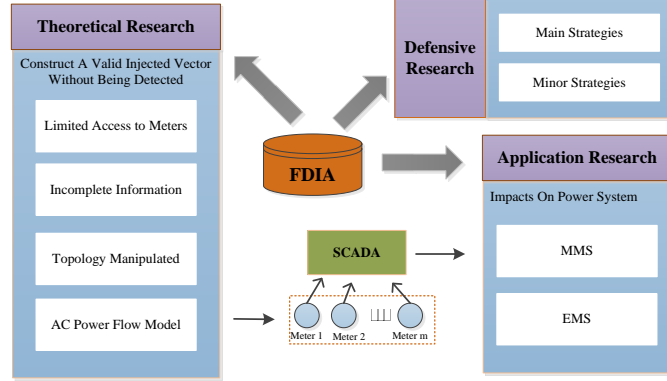


Fig. 2. The Main Research Directions of FDIAs

especially true for the future grid where the physical power system will be deeply integrated with the cyber system.

False data injection attacks (FDIAs) are an important type of cyber-attack capable of disturbing the power system state estimation process. A successful FDI can cause the state estimator to output erroneous values to the system operator, and thus make either physical or economic impacts on the power system. As depicted in Fig.2, research on FDIAs mainly focuses on the following three aspects: theoretical research, application research, and defensive research. In theoretical research, the key problem is the construction of injected vectors capable of evading detection by the control center under different situations, for example, when the attacker has limited access to meters, incomplete information, false topology, or an AC power flow model is used; the attacker then injects bad data into meters. In application research, the key problem is to analyze the impacts of FDIAs on power system operation, mainly on EMS and MMS (market management systems), for instance, economic dispatch, congestion managements, etc. In defensive research, the key problem is proposing defense strategies from the viewpoint of the system operator.

This paper gives a comprehensive review of the state-of-the-art research in the field of FDIAs against power systems. The existing works can be categorized as shown in Table I. Based on this, this paper is organized as follows: Section II gives some basic theoretical background on state estimation and FDIAs; Section III summarizes the different strategies of constructing a valid FDI; Section IV discusses the impacts of FDIAs on power systems; Section V summarizes the existing defence strategies against FDIAs; Section VI discusses some potential future research directions in this field. Finally, conclusions are drawn in Section VII.

## II. INTRODUCTION TO FALSE DATA INJECTION ATTACKS

In an FDI, the attacker aims to inject malicious measurements to mislead the state estimation process [9]. An attacker can also exploit the small measurement errors which are typically tolerated by the state estimation algorithms to further increase the impact of FDIAs on the power system [10].

In this section, the basic theory of state estimation and bad data detection are first introduced, followed by the FDIAs and generalized FDIAs theories.

TABLE I  
OVERVIEW OF FDI RESEARCHES

FDIA research	Categories	References
Theoretical researches on constructing a valid FDI	Construct a valid FDI under certain constraints	[10][12][14][15][16][17]
	Construct a valid FDI with incomplete information of matrix	[18][19][20][21]
	Construct a valid FDI with topology being falsified	[22][28][30]
	Construct a valid FDI under AC power flow model	[23][24][25]
Application researches on the impacts of FDIAs	Economic attack	[26][27][28][29][30]
	Load redistribution attack	[31][32]
	Energy deceiving attack	[33]
Defense strategies against FDIAs	Protect a set of basic measurements	[10][14][34][35]
	PMU-based protection	[36][37][38][39]
	Other ways of defending against FDIAs	[40][41][42][43][44][45][46]

### A. State Estimation and Bad Data Detection Theory

#### 1) State Estimation

The basic principle of state estimation is to infer the operational state of the power system from available measurements of the power network equipped with various meters [10]. Meter measurements include bus voltages, bus real and reactive power injections, and branch real and reactive power flows in each subsystem of the grid [10].

The AC-based state estimation model can be formulated as:

$$z = h(x) + e \quad (1)$$

where the vector  $z = (z_1, z_2, \dots, z_m)^T$  denotes the measurement data;  $x = (x_1, x_2, \dots, x_n)^T$  denotes the system states;  $e = (e_1, e_2, \dots, e_m)^T$  denotes measurement noise, here assumed to be Gaussian distributed, and  $h(x)$  denotes the functional dependency between measurements and state variables. The precise form of  $h(x)$  is determined by the grid structure and line parameters.

Model (1) is commonly solved by the weighted least squares method. In this method, the vector of estimated state variables  $\hat{x}$  is obtained by solving the following optimization problem:

$$\min J(x) = \frac{1}{2} (z - h(x))^T W (z - h(x)) \quad (2)$$

where  $W$  is a diagonal matrix represented as  $W = \text{diag}(\sigma_i^{-2}, 0)$ , where  $\sigma_i^2$  is the variance of the measurement errors associated with the  $i$ -th meter ( $1 \leq i \leq m$ ).

Iterative algorithms can be applied to solve model (2). Since solving the iterative AC-based state estimation problem can be computationally intensive, a DC-based state estimation model can be used to approximate the AC model as follows:

$$z = Hx + e \quad (3)$$

where the vectors  $z = (z_1, z_2, \dots, z_m)^T$ ,  $x = (x_1, x_2, \dots, x_n)^T$ , and  $e = (e_1, e_2, \dots, e_m)^T$  have the same meaning as those in model (1). In (3),  $H$  is a constant  $m \times n$  Jacobian matrix determined by the grid structure and line parameters.

The DC-based state estimation model can also be solved by the weighted least squares method:

$$\min J(x) = (z - Hx)^T W (z - Hx) \quad (4)$$

where now the solution can be computed in closed-form:

$$\hat{x} = (H^T W H)^{-1} H^T W z \quad (5)$$

## 2) Bad Data Detection

Bad data detection aims to detect, identify and eliminate measurement errors throughout the system [12], [13]. In power systems, bad data can be detected by two testing hypothesis: the *largest normalized residual* (LNR) and the  $J(\hat{x})$  *performance index* [12]. To achieve this, the chi-square test and  $J(\hat{x})$  test can be applied:

$$J(\hat{x}) < C \quad (6)$$

where  $J(\hat{x})$  assumed to follow a chi-square distribution, with threshold  $C$  set to some pre-determined significance level.

With the DC model, when  $W = I$ , the traditional bad data detection approaches often compute the square of the 2-norm of the measurement residual to check whether there exist bad measurements [10]. In this case,  $\varepsilon = C$ . That is:

$$\|z - H\hat{x}\|^2 < \varepsilon \quad (7)$$

For notational simplicity in the remainder of this paper, the notation  $LNR$  will be used to denote the measurement residual, where  $LNR = \|z - H\hat{x}\|$ .

## B. FDIAs and Generalized FDIAs

In FDIAs, an attacker can compromise the integrity of the state estimator by hacking a subset of meters and sending altered readings without changing the value of  $LNR$  [10]. To achieve this, the attacker needs to carefully design his/her actions to fool the estimator to avoid triggering the alarm. Denoting  $a$  as the nonzero injected vector which is injected into the measurement data  $z$ , the measurement vector after attack can be represented as  $z_{bad} = z + a$ . Denoting  $c$  as the deviation vector of the estimated state variables before and after the attack, the estimated system state vector after attack can be represented as  $\hat{x}_{bad} = \hat{x} + c$ .

With the DC model, the estimated state variables after FDIAs are as follows:

$$\begin{aligned} \hat{x}_{bad} &= (H^T W H)^{-1} H^T W z_{bad} \\ &= (H^T W H)^{-1} H^T W (z + a) \\ &= \hat{x} + (H^T W H)^{-1} H^T W a \\ &= \hat{x} + c \end{aligned} \quad (8)$$

and the new  $LNR$  value can be computed as:

$$\begin{aligned} LNR_{bad} &= \|z_{bad} - H\hat{x}_{bad}\| \\ &= \|z + a - H(\hat{x} + (H^T W H)^{-1} H^T W a)\| \\ &= \|z - H\hat{x} + (a - H(H^T W H)^{-1} H^T W a)\| \\ &= \|z - H\hat{x} + (a - Hc)\| \end{aligned} \quad (9)$$

If  $a = Hc$ , then  $LNR_{bad} = LNR$ , i.e., the attacker can inject bad data into meter measurements whilst keep the measurement residual unchanged. This type of attack is called a *FDIA*. It is noteworthy that the injected vector  $a$  can also be obtained without explicitly requiring  $c$ . In [10], it is shown that the relationship  $a = Hc$  can be transformed into an equivalent form without explicitly using  $c$ , and from which  $a$  can be generated.

If  $a \neq Hc$  but  $J(\hat{x}_{bad}) < C$ , then the attacker can still bypass bad data detection. This type of attack is called a *generalized FDIA*. In a generalized FDIA, the attacker can evade bad data detection by exploiting small measurement errors tolerated by the state estimation algorithms. Both FDIA and generalized FDIA are capable of degrading the economic efficiency and security of the power grid.

## III. CONSTRUCTING A VALID FDIA

Theoretically, if an attacker is capable of gaining knowledge of all system configuration information (i.e., grid topology information, system parameters, details of the state estimation algorithm and bad data detection method, etc.) and has the ability to manipulate all meter measurements, it is conceptually straightforward to launch a successful FDIA by constructing the injected vector directly using  $a = Hc$ . However, in a practical attack, constructing a valid injected vector is always complicated by less-than-perfect system information and constraints, which we now consider. In this section, we summarize four main scenarios, in which the attacker constructs a valid FDIA.

### A. Constructing a Valid FDIA under Certain Constraints

When constructing a valid FDIA under certain constraints, it is assumed that the attacker has full knowledge of all relevant system configuration information, (i.e., the Jacobian matrix  $H$  is known to the attacker), but he has limited ability to hack into meters.

In this case, the attacker can only access some specific measurements due to different physical protection of the meters. For example, meters located in substations with physical perimeter control might be much more difficult to access than those located in a locked box outside of a building [10].

In this case, it is assumed that the attacker has the ability to compromise at most  $k$  out of a possible  $m$  meters [14] in constructing the attack vector  $a$ , but that the particular meter set is free to be selected by the attacker. If the attacker uses a brute-force approach, i.e., the attacker may try all possible  $a$  consisting of  $k$  unknown elements and  $m-k$  zero elements, then the worst case is to try  $C_m^k$  times. This is clearly computationally intractable for large  $m$ . To solve the meter selection problem in a feasible time scale, Liu *et al.* [12] proposed a

heuristic-based approach based on column transformations of  $H$ . The approach is potentially slow for general  $H$ , but efficient when  $H$  is sparse, as is typical in practical power systems. Limitations of the approach in [10] are that it cannot guarantee the construction of  $a$  even if it exists; and also that it cannot guarantee the construction of  $a$  with the minimum possible number of nonzero elements [10].

The limited access to meter problem leads to a subset of researches on FDIAs: constructing a valid FDIA by minimizing the number of attacked meters.

For the attacker, minimizing the number of attacked meters can significantly reduce the risk and cost of an attack. For defenders, knowing the minimum attacked meter number of the attacker is helpful in identifying vulnerable measurements [15]. The objective of attacked meter minimization problem can be formulated as:

$$\alpha_k = \min_c \|Hc\|_0 \quad (10)$$

where  $\alpha_k$  denotes the minimum objective value;  $\|\cdot\|_0$  denotes the cardinality of a vector. The constraints to this optimization problem vary according to different requests.

The problem is known to be NP-hard for arbitrary  $H$ , but is often solved using the mixed-integer linear programming (MILP) method [15], matching pursuit [16], or LASSO algorithm [17]. Exploiting the fact that  $H$  exhibits special structure in power systems (i.e.,  $H$  is a sparse matrix on account of physical topology and measurement structure), Sou *et al.* [15] proposed a min-cut polynomial time algorithm which is shown to be as accurate as MILP yet faster than either matching pursuit or LASSO.

### B. Constructing a Valid FDIA with Incomplete Information of matrix $H$

Most research on FDIAs is based on the assumption that the attacker knows the complete configuration information of the power network. This assumption implies that if the attacker has no access to the grid configuration, it would be infeasible to launch a successful attack. However, research has established that it is still possible for an attacker to launch a valid attack with incomplete information. The following three scenarios show the different situations under which the attackers can obtain the topology information needed to launch a valid FDIA.

#### 1) By Collecting Offline and Online data

Rahman and Mohsenian-Rad [18] proved that  $H$  can be estimated by collecting both offline and online data. For offline data collection, the attacker collects grid topology information manually (e.g. utilizing company employees to get access to such information) before performing the actual attack; for the online data collection, the attacker deploys his/her own meters to access the grid.

#### 2) By Using Market Data

Under the DC model, locational marginal prices (LMPs) correspond to the Lagrange multipliers of the network-constrained economic dispatch problem. The topology related information can be extracted from the LMPs components. Kekatos *et al.* [19] proposed an iterative alternating direction method of multipliers (ADMM) based algorithm to

estimate the grid Laplacian matrix from the LMPs using a regularized maximum likelihood estimator (MLE). In [19], the authors solve the problem using an ADMM-based algorithm and demonstrated that the estimated Laplacian matrix is close to the real one.

#### 3) By Utilizing Power Flow Measurements

The idea of speculating the matrix  $H$  from power flow measurements to launch an attack is based on the observation that when the system parameters (e.g. active or passive loads) vary within a small range, topology information is in fact embedded into the correlations among power flow measurements [20]. Esmalifalak *et al.* [20] proposed an Independent Component Analysis (ICA) algorithm to obtain this information.

However, due to limited resources and restricted physical access to the grid, the estimated  $H$  may be inaccurate, deviating from the true one. Denoting the attacker's estimate of  $H$  as  $\bar{H} = H + \delta$  (where  $\delta$  is an  $m \times n$  error matrix), then,

$$a = \bar{H}c = Hc + \delta c \quad (11)$$

From Eq. (9), it follows:

$$\begin{aligned} \hat{z}_{bad} &= x + \bar{c} \\ &= \hat{x} + c + (H^T W H)^{-1} H^T W \delta c \end{aligned} \quad (12)$$

and hence,

$$\begin{aligned} LNR_{bad} &= \|z_{bad} - H\hat{x}_{bad}\| \\ &= \|z + a - H(\hat{x} + \bar{c})\| \\ &= \|z - H\hat{x} + \delta c + H(c - \bar{c})\| \\ &= \|z - H\hat{x} + (I - H(H^T W H)^{-1} H^T W) \delta c\| \end{aligned} \quad (13)$$

Eq. (13) shows that the residual test results depend not only on the attacker's modeling error  $\delta$ , but also some grid-specific parameters (i.e.,  $H$  and  $W$ ).

Therefore, if  $\delta c = 0$ ,  $LNR_{bad} = LNR$ . In this case, the attacker can launch a perfect attack even if the attacker's knowledge about matrix  $H$  is inaccurate. Furthermore, if  $\delta c \neq 0$ , the attacker can use a generalized FDIA, to minimize  $\|\delta c\|$  and thereby satisfying the threshold test  $J(\hat{x}_{bad}) < C$ .

Moreover, instead of trying concentrate on getting to know the whole network information, Liu *et al.* [21] showed that an attacker can launch a valid FDIA in a local region. In [21] it is shown that an attacker only needs to obtain the topology and parameter information of the local attacking region to design the false data. Moreover, it is unnecessary for the attacker to know any network information regarding the non-attacked region [21].

### C. Constructing a Valid FDIA with Topology being Falsified

Research integrating a topology attack with FDIA has appeared only very recently. In this type of attack, it is assumed that not only can continuous data (meter measurements) be manipulated by the attacker, but also that discrete data (on-off status of switching devices, reflecting the topology of the power network) can be tampered with. In order to evade being detected by both bad data detection and topology error identification, the attacker needs to simultaneously modify continuous data and discrete data to launch such an attack.

Denoting  $\bar{H}$  as the false topology matrix being used by the state estimation, in absence of FDIA, model (3) becomes:

$$\bar{z} = \bar{H}x + \bar{e} \quad (14)$$

where the vectors  $\bar{z} = (\bar{z}_1, \bar{z}_2, \dots, \bar{z}_r)^T$ ,  $x = (x_1, x_2, \dots, x_n)^T$ , and  $\bar{e} = (\bar{e}_1, \bar{e}_2, \dots, \bar{e}_r)^T$  have the same meaning as those in model (1).

In the presence of FDIA, denoting  $\bar{z}_{bad} = \bar{z} + a$  as the meter measurements after attack, the objective of the attacker is still to construct a valid injected vector  $a$  satisfying  $J(\hat{x}_{bad}) < C$ .

Kim and Tong [22] were among the first to study this problem. They made theoretical and instance analysis based on DC and AC model considering that the system states stay the same before and after the topology information has been falsified.

#### D. Constructing a Valid FDIA under AC Power Flow Model

At the present time, there are few published results on AC model-based methods of forming an injected vector that keeps the measurement residual unchanged. With the AC model, it is much more difficult for the attacker to construct an analytical formula of the injected vector  $a$  due to the complexity of the nonlinear system. Furthermore, it is impractical to implement DC model based FDIAs in the AC system. Rahman and Mohsenian-Rad [23] have shown that if the attacker implements FDIAs targeted at the DC state estimator but the system operator actually uses the nonlinear state estimator, then the attack will easily be detected.

Rahman and Mohsenian-Rad [23] proved that with the AC model, if  $a = h(\hat{x}_{bad}) - h(\hat{x})$ , then:

$$\begin{aligned} LNR_{bad} &= \|z_{bad} - h(\hat{x}_{bad})\| \\ &= \|z + a - h(\hat{x}_{bad}) + h(\hat{x}) - h(\hat{x})\| \\ &= \|z - h(\hat{x}) + a - h(\hat{x}_{bad}) + h(\hat{x})\| = LNR \end{aligned} \quad (15)$$

In Eq. (21),  $h(\hat{x}_{bad}) - h(\hat{x}) = 0$  needs to be satisfied at each iteration. One limitation of model (15) is that convergence of the Gauss-Newton Method cannot be guaranteed, and nor can the exact fixed point  $\bar{x}$  be obtained analytically.

Hug and Giampapa [24] proposed that with the AC model, if  $a_2 = h_2(\hat{x}_1, \hat{x}_2 + c) - h_2(\hat{x}_1, \hat{x}_2)$ , then:

$$\begin{aligned} LNR_{bad} &= \|z_{bad} - h(\hat{x}_{bad})\| \\ &= \|z + a - h(\hat{x} + c)\| \\ &= \left\| \begin{pmatrix} z_1 \\ z_2 + a_2 \end{pmatrix} - \begin{pmatrix} h_1(\hat{x}_1) \\ h_2(\hat{x}_1, \hat{x}_2 + c) \end{pmatrix} \right\| \\ &= \left\| \begin{pmatrix} z_1 \\ z_2 \end{pmatrix} - \begin{pmatrix} h_1(\hat{x}_1) \\ h_2(\hat{x}_1, \hat{x}_2) \end{pmatrix} \right\| \\ &= \|z - h(\hat{x})\| = LNR \end{aligned} \quad (16)$$

where variables with the subscript '1' correspond to the measurements and state variables which are not altered by the attacker; variables with subscript '2' correspond to measurements and state variables that are altered [24]. One limitation of (16) is that this function shows the attacker must also know the estimated values of the state variables that appear in  $h_2$ , information about which is not easy to obtain.

Overall, research on false data injection with the AC power flow model is based mainly on generalized FDIAs.

#### IV. THE IMPACTS OF FDIAS ON POWER SYSTEM

By launching a valid FDIA, an attacker can either gain economic benefit or disrupt the power system. Recently, some research has been conducted to study the impacts of FDIAs on the electricity market, power system operation, and distributed energy routing, respectively. This section reviews the impact of FDIAs on all three of these aspects.

##### A. Economic Attack

The economic attack is a type of FDIA proposed by Xie *et al.* [26] and [27] which can affect the operation of the deregulated electricity market.

The electricity market consists of two markets: day-ahead market and real-time market. The specific operation model and settlement method differs according to countries. Xie *et al.* in [26] and [27] analyze the potential for financial misconduct under FDIAs using both ex-ante market and ex-post market, which are the formulations adopted by PJM, ISO New England, in the U.S.

The independent system operator (ISO) in a wholesale electricity market collects data from various market participants. The locational marginal price (LMP) is an index that reflects the electricity price at each node. Based on state estimation obtained via the SCADA system, the ISO calculates the ex-post LMPs using the DC optimal power flow model.

The attacker under the aforementioned electricity market environment makes his/her profit by the following three steps: i) in the ex-ante market, the attacker buys and sells the virtual power  $P$  at locations  $j_1$  and  $j_2$  with prices  $\lambda_{j_1}^{DA}$  and  $\lambda_{j_2}^{DA}$ , respectively; ii) the attacker injects  $a$  to manipulate the nodal prices of the ex-post market; iii) in the ex-post market, the attacker sells and buys the virtual power  $P$  at  $j_1$  and  $j_2$  with prices  $\lambda_{j_1}$  and  $\lambda_{j_2}$ , respectively [26]. It can be formulated as:

$$\begin{aligned} Profit &= (\lambda_{j_1} - \lambda_{j_1}^{DA})P + (\lambda_{j_2}^{DA} - \lambda_{j_2})P \\ &= (\lambda_{j_1} - \lambda_{j_2} + \lambda_{j_2}^{DA} - \lambda_{j_1}^{DA})P \end{aligned} \quad (17)$$

The objective of an attacker in attacking the electricity market is to gain financial profit. In an economic attack, the attacker intends to buy virtual power at the lower priced node and sells at the higher priced node. Nevertheless, in this case, the attacker cannot always guarantee the non-negativity of the profit. References [26] and [27] develop a heuristic-based method for the attacker to improve the attack efficiency.

Furthermore, since the calculation of real-time LMPs is based on both real-time measurements of meters and on-off status of switching devices, some researchers have studied the impacts of integrated generalized FDIA and topology attacks (see Section. III) on LMPs. Jia *et al.* in [28] proposed several ways to calculate the injected vector  $a$  on the purpose of causing congestion pattern which affect the LMP most. Choi and Xie in [29] studied the impacts of topology errors on LMPs. Since the LMP is a by-product of OPF, Rahman *et al.* in [30] described a formal verification-based framework to systematically analyse the

impact of topology attacks on the integrity of OPF and economic operation.

### B. Load Redistribution Attack

The load redistribution (LR) attack is a type of FDIA proposed by Yuan *et al.* [31] which can affect the power grid operation by attacking the security-constrained economic dispatch (SCED).

In [31], the authors analyzed the damage of the LR attack on power systems and classified it into the immediate attack and delayed attack, based on the different attacking consequences.

The objective of SCED is to minimize the total system operation cost (generation cost, load shedding cost, etc.) by re-dispatching the generation outputs [31]. Once the estimated state is manipulated by an LR attack, the falsified SCED solution may drive the system to an uneconomic operating state. In a worst-case situation, this could lead to immediate load shedding or even wider load shedding in a delayed time without immediate corrective actions [31], [32]. In [31] and [32], the authors propose a bi-level model and tri-level model to model the immediate LR attack and delayed attack, respectively.

The main attacking processed is as follows. In the immediate attack, the attacker determines the injected vector and injects it into the targeted meters to maximize the operation cost of the system; the system operator then optimally reacts to the false state estimation that has been successfully manipulated by the injected vector. As a consequence of a successful immediate attack, the actual operation cost will increase no matter whether there is load shedding action or not.

In the delayed attack, the attacker determines the injected vector and injects it into the targeted meters; the control center performs the first round of SCED function based on the false state estimation, which would lead to the occurrence of the line overloading without being noticed; the control center then performs the second round of SCED after the tripping of the overload lines. A successful delayed attack results in line overloading undetected by the control center, which can lead to physical damage to the power system.

### C. Energy Deceiving Attack

The energy deceiving attack is a type of FDIA proposed by Lin *et al.* [33], which affects the distributed energy routing process.

In [33], the authors proposed a distributed energy routing scheme which determines the optimal energy route for transmitting energy among the nodes of the grid. It is assumed that each node can act both as the energy consumer and producer. The measuring component at the node (e.g., smart meter) determines whether the node is a producer-node or consumer-node. The nodes communicate with each other to share the measurements, demands, and requests. In the energy deceiving attack, the attacker is assumed to be capable of injecting either the forged energy information or forged link state information into the energy request and response message among nodes [33]. Once the memory of a measuring component is manipulated by the attacker, erroneous energy demand and supply messages can be injected into the grid.

Based on the proposed scheme, the authors studied the energy deceiving attack that manipulated the quantity of energy supply,

the quantity of energy response, and the link state information of the energy transmission, respectively. It is concluded in [33] that the energy deceiving attack can create an imbalance between power demand and supply, and can therefore further increase the cost of the energy distribution and disrupt the effectiveness of the energy distribution process.

## V. DEFENSE STRATEGIES AGAINST FDIAS

As FDIAs can severely threaten the economic and physical securities of the power system, it is important for the system operator to design proper defensive measures to protect the power grid. In this section, two main defense strategies and many other strategies against FDIAs are introduced.

### A. Protecting a set of Basic Measurements

A set of basic measurements is a minimum set of measurements whose corresponding rows in  $H$  are linearly independent and sufficient to solve for the corresponding state variables.

Liu *et al.* [10] demonstrated that if an attacker can compromise  $k$  meter measurements, where  $k \geq m - n + 1$ , there always exist successful attack vectors that can inject false data without being detected. On the other hand, if the number of the meters that the attacker can manipulate is less than  $m - n + 1$ , the attack will then be detected. Therefore, the size of the basic measurements based on DC state estimation model is  $n$ , the number of state variables. Bobba *et al.* [14] proved that it is necessary and sufficient to protect a set of basic measurements in order to be able to detect FDIAs.

This problem leads to another research direction on defences against FDIAs: how to locate and protect the set of basic measurements. Bi and Zhang [34] considered the location of protected meter problem using graphical methods. Anwar *et al.* [35] expanded the FDIA problem from the power transmission system to power distribution systems, and utilized a voltage stability index and improved constriction factor particle swarm optimization (CF-PSO) based hybrid cluster technique to rank each node according to vulnerability, from most- to least-vulnerable. The meter measurements on the node belonging to the least vulnerable group that needs to be protected are then located. In respect to the ways of protecting basic measurements, methods range from simple physical security (e.g. locking each meter in a box) through enhance communication security, to replacing meters with PMUs [36], etc.

### B. PMU-based Protection

Phasor measurement units (PMUs) are measurement devices equipped with the global positioning system (GPS) technology for precise timing. By synchronizing to GPS time, PMUs have the capability of providing accurate synchronous phasor measurements for geographically dispersed nodes in power grids [36]. It is much more difficult for an attacker to compromise the measurements which are collected by the PMUs. However, a major impediment to large-scale deployment of PMUs is their high capital cost. Therefore, it is important to find the best locations to place PMUs so that the number of PMUs can be minimized.

Chen and Abur [37] proposed a PMU placement algorithm, formulating it as an integer programming problem. They showed that extra PMUs can help improve the bad data detection and identification capability of a given system [37]. Similarly, Kim and Poor [36] also proposed a secure PMU placement algorithm to find the appropriate locations for these PMUs. The proposed algorithm has low complexity and is capable of handling different types of PMU measurements. In [36] it is shown it may become infeasible for an attacker to inject bad data without changing the measurement residual if approximately 1/3 of the buses are protected with PMUs.

References [36] and [37] show that by placing PMUs, the power system can effectively protect itself. However, Gong *et al.* [38] proposed a time stamp attack by spoofing the GPS. By sending a forged signal to the GPS receiver, attackers can mount an attack even without access to the communication network. This attack scheme can lead to the failure of the basic application of PMU system [38]. Liu *et al.* [39] also demonstrated that an attacker can mask the outage of a single line by attacking a set of critical measurements, even though PMUs are deployed in the system.

### C. Other Defense Strategies against FDIAs

Several other methods have been proposed to defend against FDIAs. Based on the fact that the network topology information is a key prior knowledge for the attacker, Talebi *et al.* [40] proposed a defense strategy against FDIAs by dynamically changing the information structure of micro-grids. Huang *et al.* [41] proposed an adaptive CUSUM algorithm to defend against FDIA in a smart grid. Zhu *et al.* [42] proposed an interleaved hop-by-hop authentication scheme to help the base station detect injected false data packets. Liu *et al.* [43] consider the detection problem as a matrix separation problem, and proposed nuclear norm minimization method and low rank matrix factorization approach. Li *et al.* [44] considered the online detection of FDIA by using a sequential detector based on the generalized likelihood ratio. Chaojun *et al.* [45] proposed a Kullback-Leibler distance (KLD) based method by tracking the dynamics of measurement variations to detect FDIAs under the AC state estimation model. Liu *et al.* [46] expanded meters from the power side to the user side, and proposed an intrusion detection mechanism that can achieve collaborative detection of FDIA by setting spying domain randomly in physical memory in combination with using secret information and event log.

## VI. FUTURE RESEARCH DIRECTIONS

Based on existing research, the following areas of research are suggested in the field of FDIAs against the power system:

(1) AC model-based FDIAs for future power system problems need to be more comprehensively studied. Despite the considerable research on DC model-based FDIAs, practical power systems operate under the conditions of the AC model. It would therefore be beneficial to power system operators if the characteristics of AC model-based FDIAs were more intensively studied. For instance, to better understand: i) nonlinear rules for constructing a valid FDIA when the attacker has some states or measurements as predetermined targets; ii) the influ-

ence of AC model based FDIAs on system control operation and system stability; and iii) the vulnerability assessment of the practical power system when FDIAs combine with other kinds of cyber-attacks.

(2) For enhancing security defense mechanisms, more work is required to focus on the higher-level security algorithm or structure. As the state estimator may not filter bad data using the existing bad data detection method in the presence of FDIAs, higher-level security algorithms or structures are required. For example, in addition to the existing bad data detection process, if the SCADA system has some other modules which are specially used to detect the false data using a new regulation, it would be much more difficult for any kind of attacks to success.

(3) For enriching the impact analysis of FDIA, more work is required to focus on the distribution system and user side. Besides transmission system, distribution system can also be influenced by using false meter measurements and fake topology information. On the other hand, meters deployed in the user side that transfer user's power consumption and utility company's command can also be manipulated. Therefore, the security of load management and demand side management should draw more attention in the future.

## VII. CONCLUSIONS

The cyber physical system security of modern power system is of utmost importance for the future grid. Recent research reveals that modern power systems face severe threats from cyber-attacks due to the tight integration of physical and cyber systems. False data injection attacks are an important type of cyber-attack which can disrupt the underlying control system of the electric power grid.

This paper provides a comprehensive review of the state-of-the-art research in the field of FDIAs against modern power systems. Firstly, the theoretical basis of state estimation, bad data detection, FDIAs and generalized FDIAs are introduced. Secondly, in the theoretical research of FDIAs, four main scenarios for constructing valid FDIAs are discussed. Following this, the paper discusses the impacts of FDIAs on different aspects of the power grid operation. Then, two common defense strategies together with many other defense strategies are summarized. This paper also ventures potential research directions in the field. These directions are principally based on extending the framework of FDIAs and defenses to the considerably more challenging case of AC power system models, distribution system, and user side.

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