Space: the final frontier

FW 891

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Purpose

- Background
- Recognizing dependency in simple models
- How can we deal with dependency problems
  - Introduction to spatial random effects

Why do we care about space

- Most of our problems in ecology and mgmt are inherently spatial

Special Feature

Space: The Final Frontier for Ecological Theory[1]

Most ecologists realize that the interplay of dispersal, disturbance, and spatial mosaics can profoundly alter the outcome of species interactions. Indeed, an appreciation of the spatial dimension and spatial heterogeneity is well established in natural history. Nonetheless, for many ecologists, "spatial complications" are used as a catch-all for explaining away surprising results, or as a condemnation of ecological theory that is accused of oversimplification because of its neglect of spatial variation. What is missing are serious experiments that explicitly test major hypotheses emerging from recent theoretical explorations of spatial effects. The purposes of this Special Feature are to alert ecologists to the general insights emerging from spatial models, and to show how these concepts apply to the natural world.

Tillman et al. 1994

Nearby things tend to be more alike

Photo credit: accuweather.com

Paraphrased from Fisher 1935 and Tobler 1970

However…

- It is really hard to estimate spatial (or spatial-temporal) dynamics in most statistical models

Cressie and Wikle 2010

Spatial dependency poses issues for traditional experimental design

Sir Ronald Fisher

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- Statistical theory of experimental designs (Fisher 1935)

Paraphrased from Fisher 1935

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  - *After choosing the area we usually have no guidance beyond the widely verified fact that patches in close proximity are commonly more alike…than those which are further apart*

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- We have hustled spatial dependence to the back door
  - Not rejecting this paradigm of experimental inference

Paraphrased from Fisher 1935

Observational data represent the wilder side of science and statistical inference

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- Great potential for biased inference

sensu Walters 1986; Cressie and Wikle 2010

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  - Wrong operating model
  - Unmeasured yet influential covariates
  - Lack of replication or randomization

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- Notions of space and time even more relevant?
- This is most of our data!

sensu Walters 1986; Cressie and Wikle 2010

Observational data represent the wilder side of science and statistical inference

Hierarchical modeling as a powerful tool for ecological inference

- Unifying field of statistics
- Many technical benefits
- Helps deal with dependency
  - i.e., Hurlburt's pseudoreplication
- So we are going to use these to address the spatial dependency issue

Hurlburt 1984; Royle and Dorazio 2008

Recognizing dependency in statistical models

What do we look for when checking statistical models?

- Zuur and Ieno 2016 offered a 10 step approach

Protocol for presenting regression-type analyses

1. State appropriate questions
2. Visualize the experimental design
3. Conduct data exploration
4. Identify the dependency structure in the data
5. Present a statistical model
6. Fit said model
7. “validate” the model
8. Interpret and present output
9. Model visualizations
10. Simulate from the model

Zuur and Ieno 2016

The take home point from Zuur and Ieno

"*Before starting the analysis carefully consider which observations for your response variable can be dependent. If dependency is present, apply a statistical technique that is able to cope with it*"

Zuur et al. 2017

Thinking about dependency

- Suppose samples are collected by different laboratories
  - Perhaps due to differences in techniques or scientists themselves among laboratories, we likely have among-lab dependency

Zuur et al. 2017

Thinking about dependency

- Suppose related species are analyzed together in one analysis
  - Perhaps due to similarities between the species we have among-species dependency

Zuur et al. 2017

Thinking about dependency

- Suppose we take repeated measurements on individual rats
  - Perhaps due to individual differences among rats, the data scientists collect from one rat is more likely to be similar to other data from collected from that rat

Zuur et al. 2017

What dependency is not

- Two sites have high bird counts, and they weren't sampled by the same person or lab
- However, both sites have a low cover measurement, which is the cause of the high bird counts

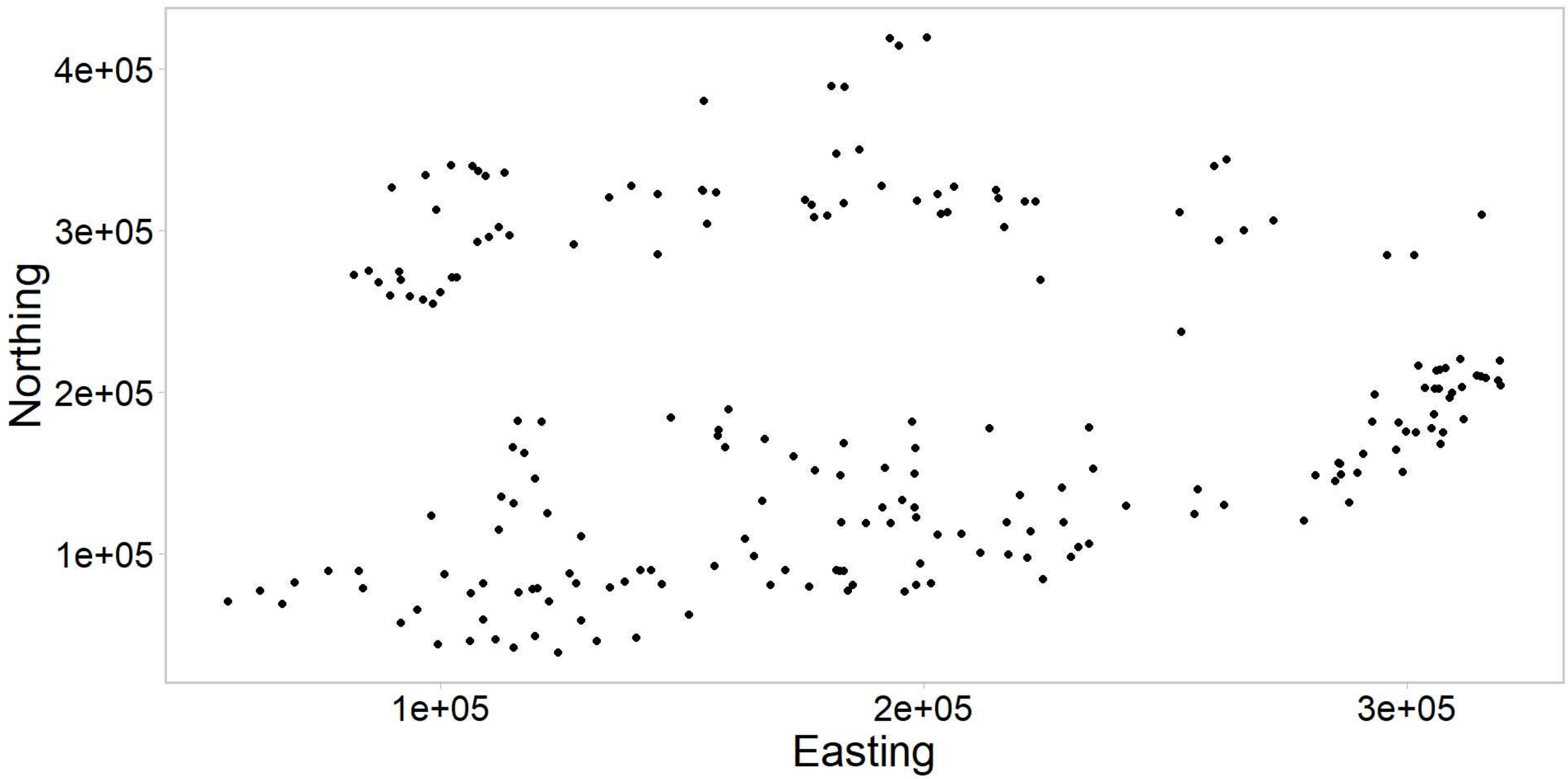
Zuur et al. 2017

Visualize experimental design: spatial dependency

```r
library(tidyverse)
library(ggqfc)
data <- read.table(file = "data/ph_dat.txt", header = TRUE, dec = ".")
data %>%
  ggplot(aes(x = Easting, y = Northing)) +
  geom_point(shape = 16) + theme_qfc()
```

Zuur et al. 2017

Visualize experimental design: spatial dependency



Zuur et al. 2017

Running an analysis

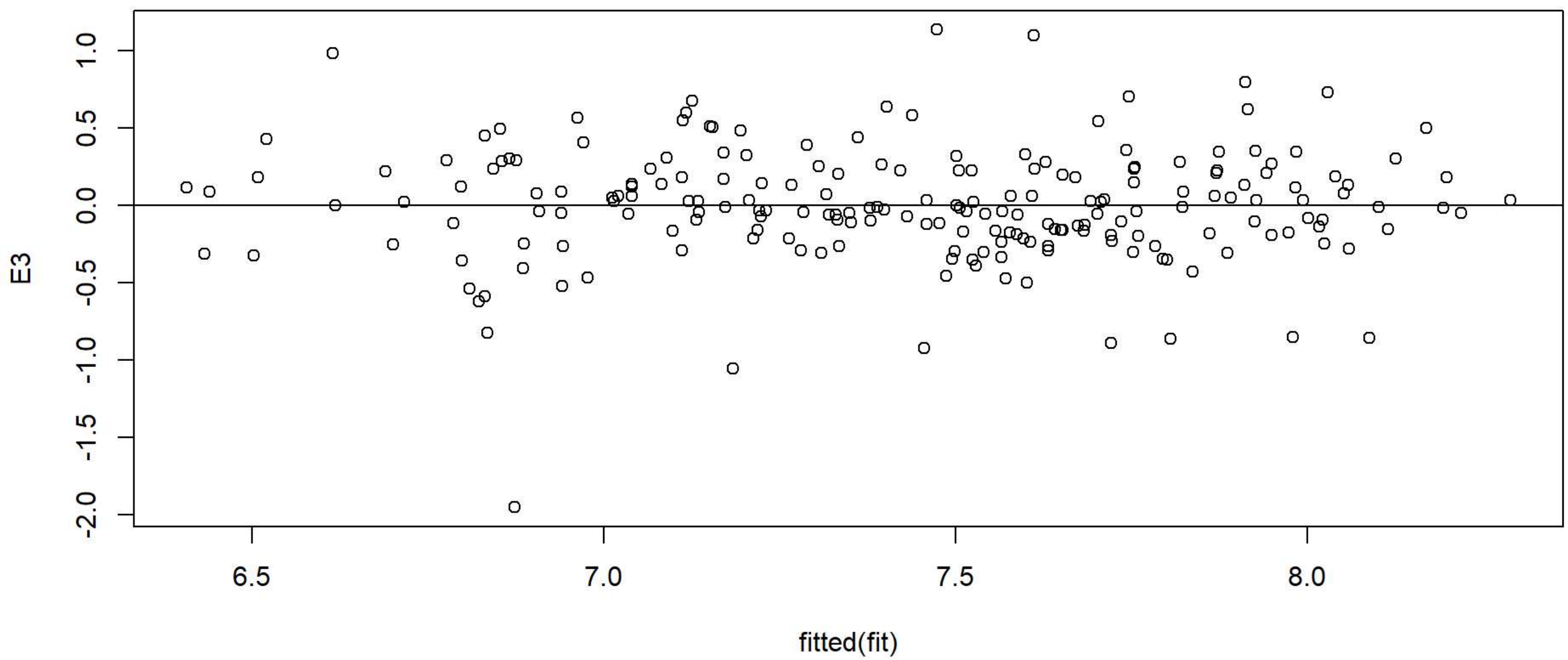
```r
data$fForested <- factor(data$Forested,
                         levels = c(1, 2),
                         labels = c("Yes", "No"))
data$LOGAltitude <- log10(data$Altitude)

# Model selected using some stepwise AIC approach
fit <- lm(pH ~ LOGAltitude + SDI + fForested + LOGAltitude:fForested,
          data = data)
E3 <- resid(fit)
```

Zuur et al. 2017

Validating the model

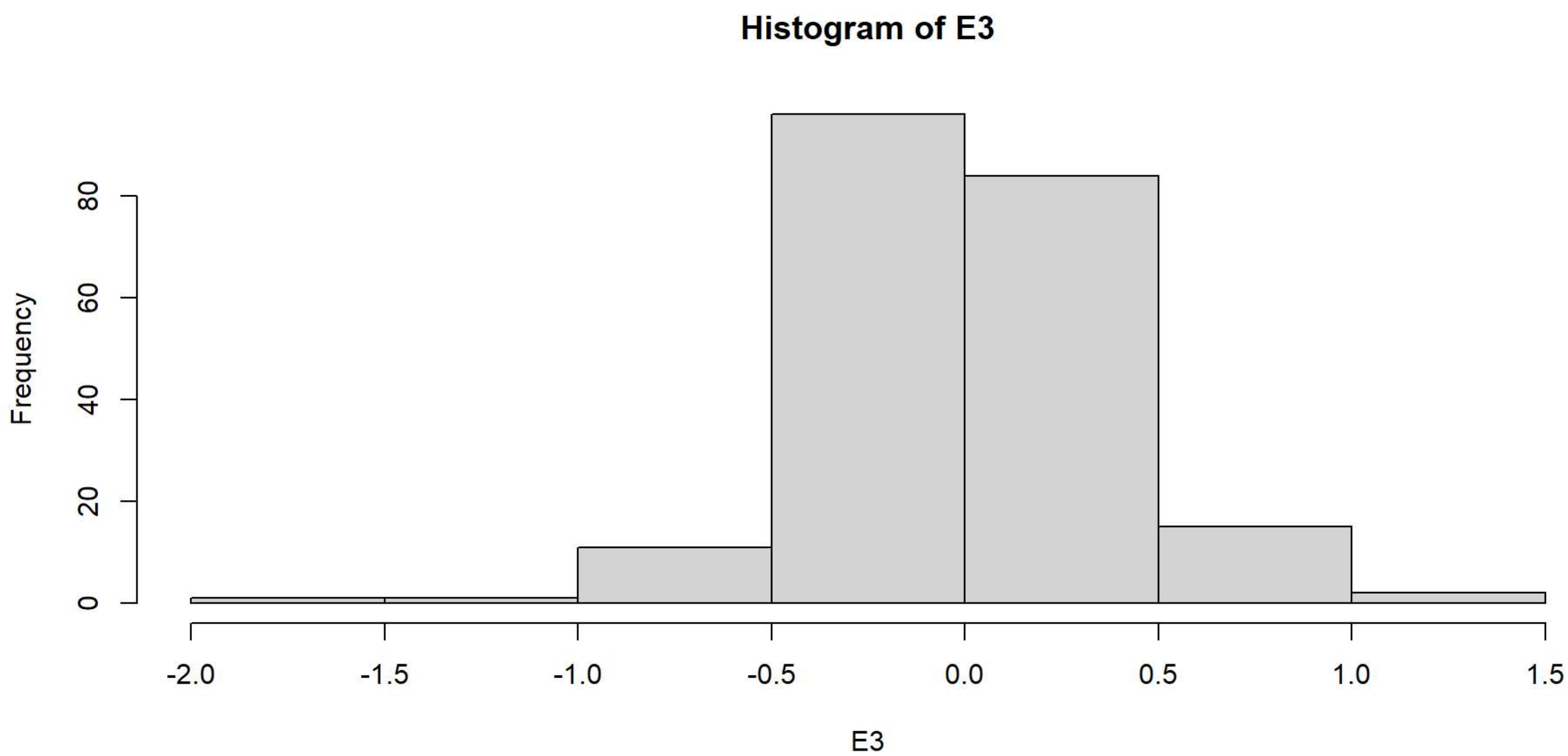
```
plot(x = fitted(fit), y = E3)
abline(h = 0, v = 0)
```



Zuur et al. 2017

Validating the model

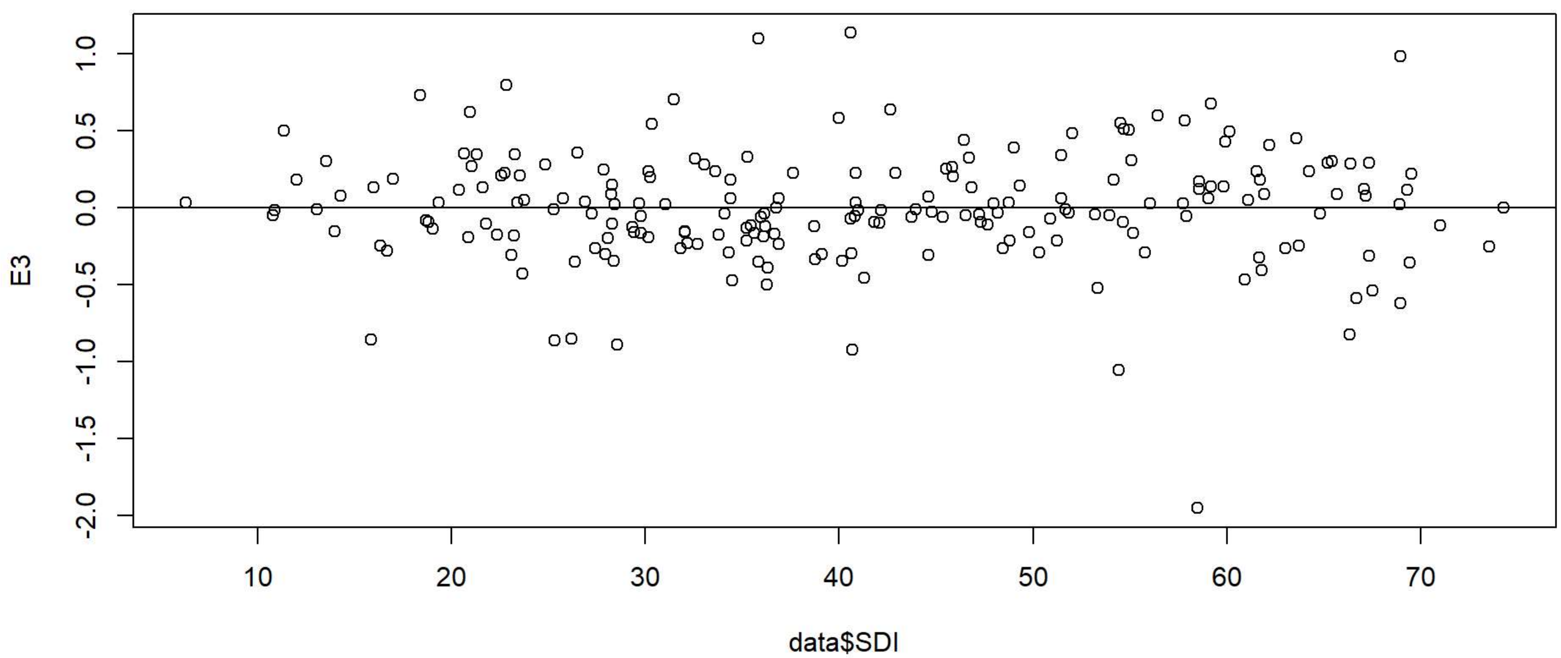
```r
hist(E3)
```



Zuur et al. 2017

Validating the model

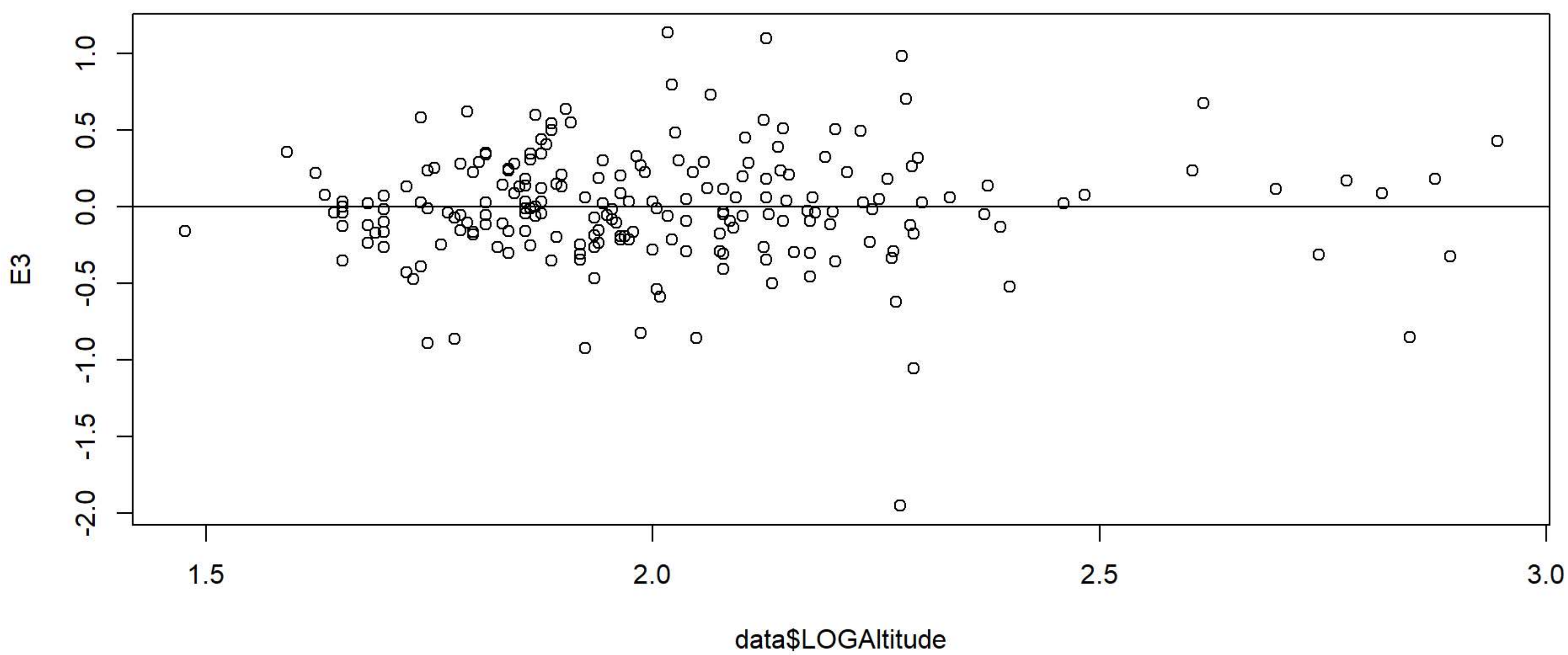
```
# Independence due to model misfit
plot(x = data$SDI, y = E3) # residuals vs. predictors
abline(h = 0, v = 0)
```



Zuur et al. 2017

Validating the model

```r
# Independence due to model misfit
plot(x = data$LOGAltitude, y = E3) # residuals vs. predictors
abline(h = 0, v = 0)
```



Zuur et al. 2017

Can we find spatial patterns?

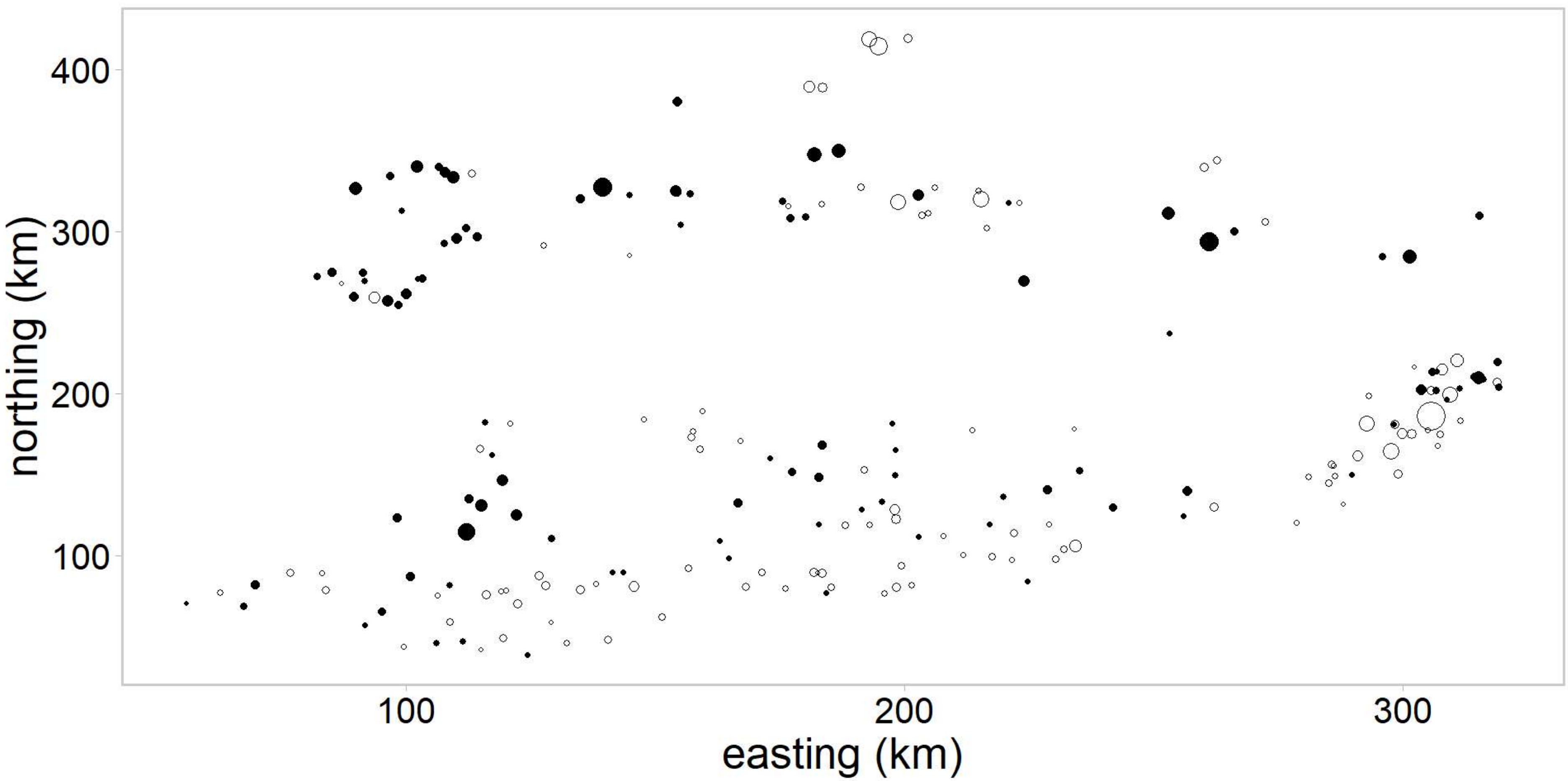
```r
# Can we find spatial patterns in the residuals?
data$E3 <- resid(fit)
data$my_cex <- 3 * abs(data$E3) / max(data$E3) + 0.75
data$sign <- as.numeric(data$E3 >=0) + 1
data$my_pch <- c(1, 16)[data$sign]

# Convert Easting / Northing to km
data$easting_km <- data$Easting/1000
data$northing_km <- data$Northing/1000

data %>%
  ggplot(aes(x = easting_km, y = northing_km)) +
  geom_point(size = data$my_cex, shape = data$my_pch) +
  ylab("northing (km)") + xlab("easting (km)")
```

Zuur et al. 2017

Can we find spatial patterns?



Zuur et al. 2017

Introduction to spatially explicit random effects

- Point process vs. areal data
- Gaussian Random Fields
- Exponential covariance function

References

- Cressie and Wikle 2010. Spatio-temporal Statistics.
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- Zuur and Ieno 2016. A protocol for conducting and presenting results of regression-type analyses. Methods in Ecology and Evolution. 7: 636–664.
- Zuur, A.F., Ieno, E.N., and Saveliev, A.A. 2017. Spatial, temporal and spatial–temporal ecological data analysis with R-INLA. Highland Statistics Ltd.