

# Fitting nonlinear models using automatic differentiation in R via RTMB

Christopher Cahill

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Quantitative Fisheries Center  
MICHIGAN STATE UNIVERSITY

# Outline

- Demonstrate an exciting advance with AD
- Show a few examples that may be useful
  - Start with equations, move to code
- Talk about debugging via `browser()`
- Tips and trickery
- All code available at  
<https://github.com/QFCatMSU/RTMB/tree/main>

# What is RTMB?

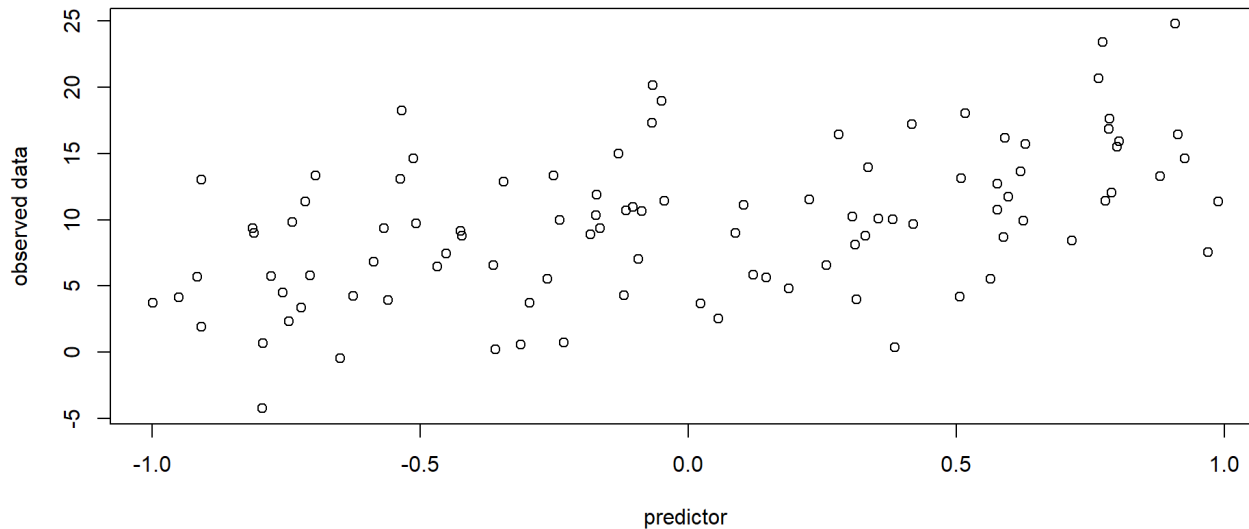
- RTMB is a new package that provides a native R interface for a subset of TMB so you can avoid coding in C++.
- See link: <https://kaskr.r-universe.dev/RTMB>
- No longer need to code a `.cpp` file to use AD
- All(?) the functionality of TMB
- Easier for others to read the code (no more `.cpp` files)
- A game changer *if* you know how to code in R, create an objective  $f(x)$  for your model
- Bottom line: less time developing and testing models, more intuitive code

# Linear regression

- The math:

$$y_i = \beta_0 + \beta_1 x_i + \epsilon_n \quad \text{where} \quad \epsilon_i \sim N(0, \sigma)$$

```
1 plot(y_obs~x1, xlab = "predictor", ylab = "observed data")
```



# Linear regression (RTMB)

```
1 # set up tagged data + parameters lists:
2 data = list(
3     n = n,
4     y_obs = y_obs,
5     x1 = x1
6 )
7
8 pars = list(
9     b0 = 1,
10    b1 = 1,
11    log_sd = log(3)
12 )
```

- see `linreg.r`

# Linear regression (RTMB)

```
1 library(RTMB)
2
3 # write an objective function returning negative log-likelihood
4 f = function(pars) {
5   getAll(data, pars) # replaces DATA_XX, PARAMETER_YY
6   y_pred = b0 + b1 * x1
7   nll = -sum(dnorm(y_obs, y_pred, exp(log_sd), log = TRUE))
8   nll
9 }
10
11 obj = MakeADFun(f, pars)
12 obj$fn() # objective function
```

```
[1] 777.5154
```

```
1 obj$gr() # gradients
```

```
outer mgc: 1051.521
```

```
      [,1]      [,2]      [,3]
[1,] -96.88602 -13.2133 -1051.521
```

- Stick to base R

# Linear regression (RTMB)

```
1 opt = nlminb(obj$par, obj$fn, obj$gr)
```

```
outer mgc: 1051.521  
outer mgc: 54.72716  
outer mgc: 36.6083  
outer mgc: 21.88026  
outer mgc: 35.7811  
outer mgc: 5.686432  
outer mgc: 1.353547  
outer mgc: 1.508322  
outer mgc: 0.08695211  
outer mgc: 0.04554657  
outer mgc: 0.0305969  
outer mgc: 0.002009656  
outer mgc: 1.470605e-05
```

# Linear regression (RTMB)

```
1 sdr = sdreport(obj)
```

```
outer mgc: 1.470605e-05
```

```
outer mgc: 0.004344401
```

```
outer mgc: 0.004344313
```

```
outer mgc: 0.001393873
```

```
outer mgc: 0.00140084
```

```
outer mgc: 0.1997855
```

```
outer mgc: 0.2002149
```

- We are done.



# Access fit

```
1 opt
```

```
$par
```

```
      b0      b1    log_sd  
9.730622 4.775419 1.568146
```

```
$objective
```

```
[1] 298.7085
```

```
$convergence
```

```
[1] 0
```

```
$iterations
```

```
[1] 12
```

```
$evaluations
```

```
function gradient  
      15      10
```

# Access fit

```
1 sdr
```

```
sdreport(.) result
      Estimate Std. Error
b0      9.730622 0.47978081
b1      4.775419 0.84596427
log_sd  1.568146 0.07071065
Maximum gradient component: 1.470605e-05
```

***RTMB works for more  
complicated models***

# RTMB objective $f(x)$ for a von Bertalanffy growth model:

```
1 f = function(pars) {  
2   getAll(data, pars)  
3   linf = exp(log_linf)  
4   vbk = exp(log_vbk)  
5   sd = exp(log_sd)  
6   l_pred = linf * (1 - exp(-vbk * (age_i - t0)))  
7   nll = -sum(dnorm(l_obs_i, l_pred, sd, TRUE))  
8   REPORT(linf)  
9   REPORT(vbk)  
10  ADREPORT(sd)  
11  nll  
12 }
```

- see `vonB.r`
- can use `REPORT()`, `ADREPORT()`

# Objective $f(x)$ for a Poisson hierarchical model:

```
1 f = function(pars) {
2   getAll(data, pars)
3   sd_site = exp(log_sd_site)           # back transform
4   jnll = 0                             # initialize
5   jnll = jnll - sum(dnorm(eps_site, 0, sd_site, TRUE)) # Pr(random effects)
6   lam_i = exp(                          # exp link f(x)
7     Xmat %*% bvec +                    # fixed effects
8     eps_site                          # random effects
9   )
10  jnll = jnll - sum(dpois(yobs, lam_i, TRUE)) # Pr(observations)
11  jnll
12 }
```

- see `glmm.r`

# Objective $f(x)$ for a hierarchical selectivity model, see Meyer and Millar 1999:

```
1 f = function(pars) {
2   getAll(data, pars)
3   jnll = 0
4   jnll = jnll - sum(dnorm(k1_dev, 0, exp(ln_sd_k1), TRUE))
5   jnll = jnll - sum(dnorm(k2_dev, 0, exp(ln_sd_k2), TRUE))
6   k1 = exp(ln_k1 + k1_dev)
7   k2 = exp(ln_k2 + k2_dev)
8   sel_mat = phi_mat = matrix(0, nrow(catches), ncol(catches))
9   for (i in 1:nrow(sel_mat)) {
10     for (j in 1:ncol(sel_mat)) {
11       sel_mat[i, j] = exp(-(lens[i] - k1[site[i]] * rel_size[j])^2 /
12         (2 * k2[site[i]]^2 * rel_size[j]^2))
13     }
14   }
15   sel_sums = rowSums(sel_mat)
16   for (i in 1:nrow(phi_mat)) {
17     for (j in 1:ncol(phi_mat)) {
18       phi_mat[i, j] = sel_mat[i, j] / sel_sums[i]
19     }
20   }
21   jnll = jnll - sum(catches * log(phi_mat))
22   jnll
23 }
```

- see `by_net.r`

# Objective $f(x)$ for a spatially explicit GLMM:

```
1 f = function(pars){
2   getAll(data, pars)
3   SIGMA = gp_sigma * exp(-dist_sites / gp_theta)
4   jnll = 0
5   jnll = jnll - sum(dmvnorm(eps_s, SIGMA, TRUE))
6   y_hat = exp(beta0 + eps_s) # index on site_i in more complex examples
7   jnll = jnll - sum(dpois(y_obs, y_hat), TRUE)
8   jnll
9 }
```

- wut dark majicks is this??!!
- see `grf.r`

# Objective f(x) for a Bence's fancy vonB:

```
1 f = function(pars) {
2   getAll(data, pars)
3   Linfmn = exp(logLinfmn)
4   logLinfscd = exp(loglogLinfscd)
5   Linfs = exp(logLinfs)
6   K = exp(logK)
7   Sig = exp(logSig)
8   nponds = length(Linfs)
9   nages = length(A)
10  predL = matrix(0, nrow = nages, ncol = nponds)
11  # fill one column (pond) at a time:
12  for (i in 1:nponds) {
13    predL[, i] = Linfs[i] * (1 - exp(-K * (A - t0)))
14  }
15  nll = -sum(dnorm(x = L, mean = predL, sd = Sig, log = TRUE))
16  nprand = -sum(dnorm(x = logLinfs, mean = logLinfmn, sd = logLinfscd, log = TRUE))
17  jnll = nll + nprand
18  jnll
19 }
```

- see `multilinf.r`



