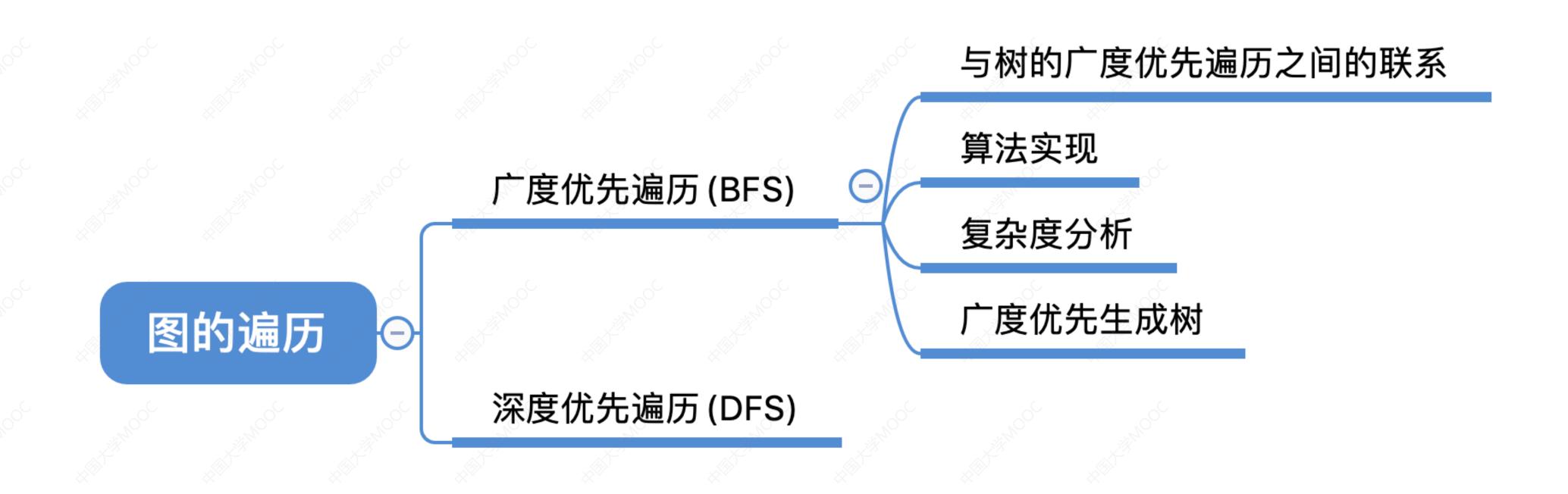
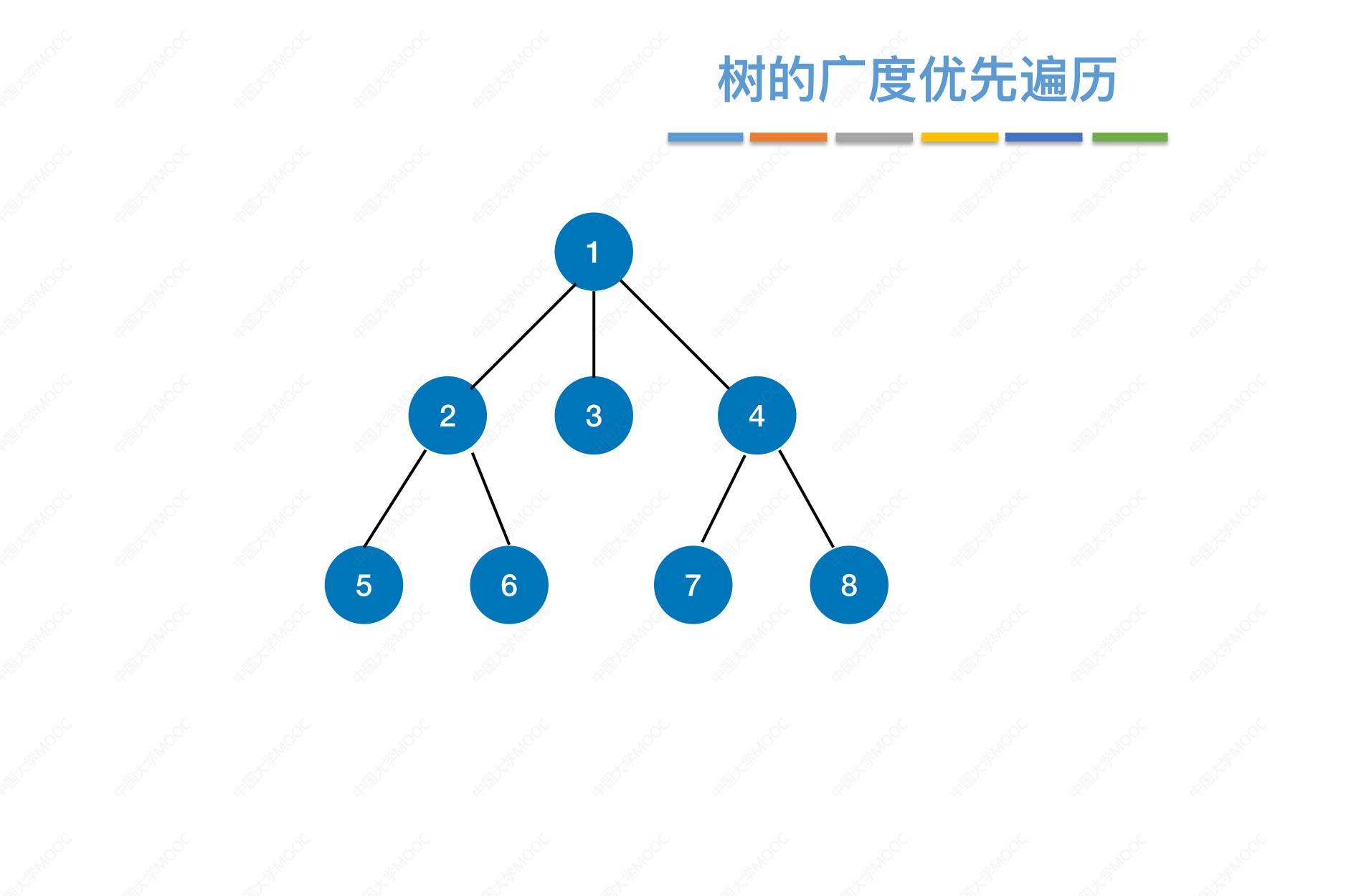
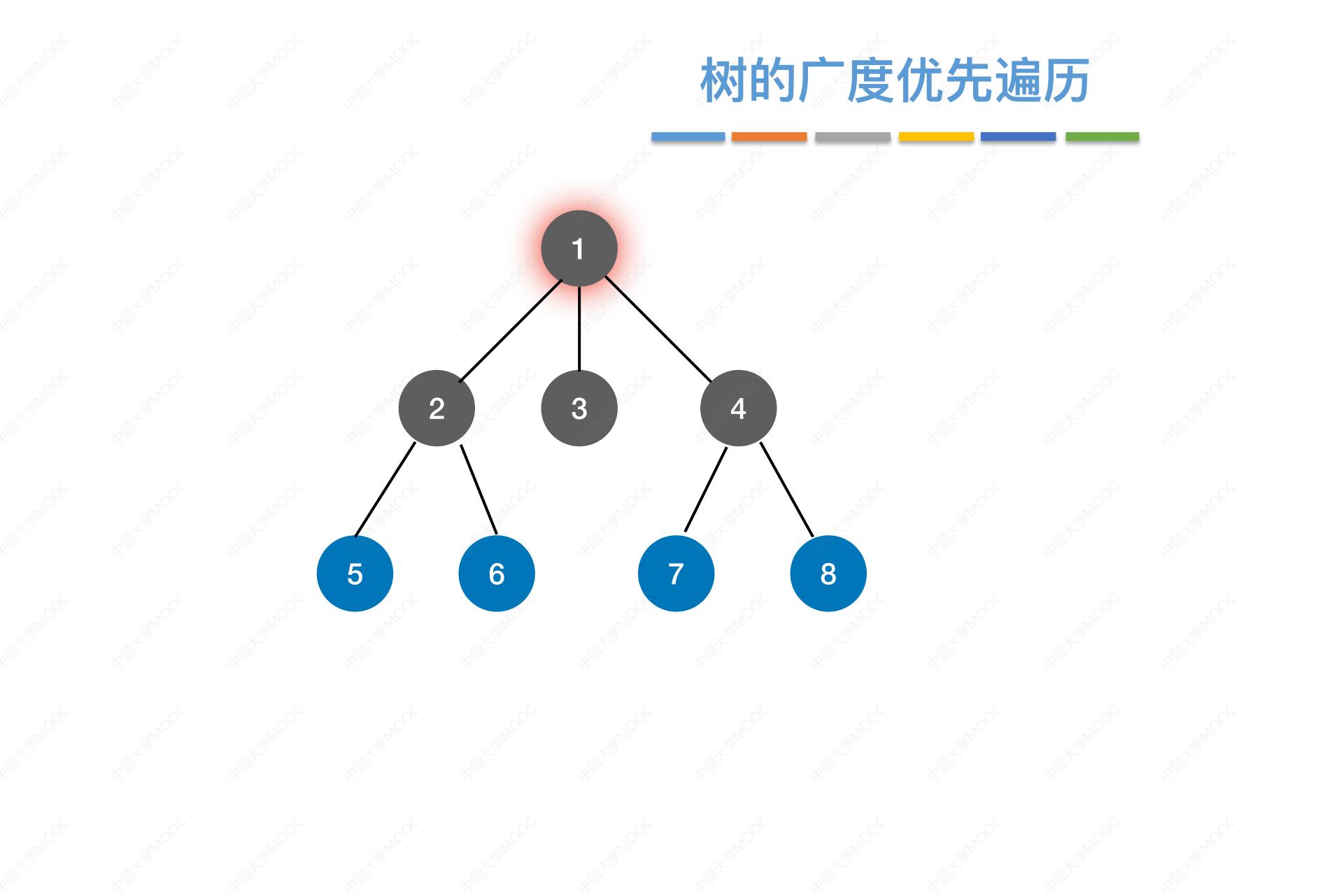
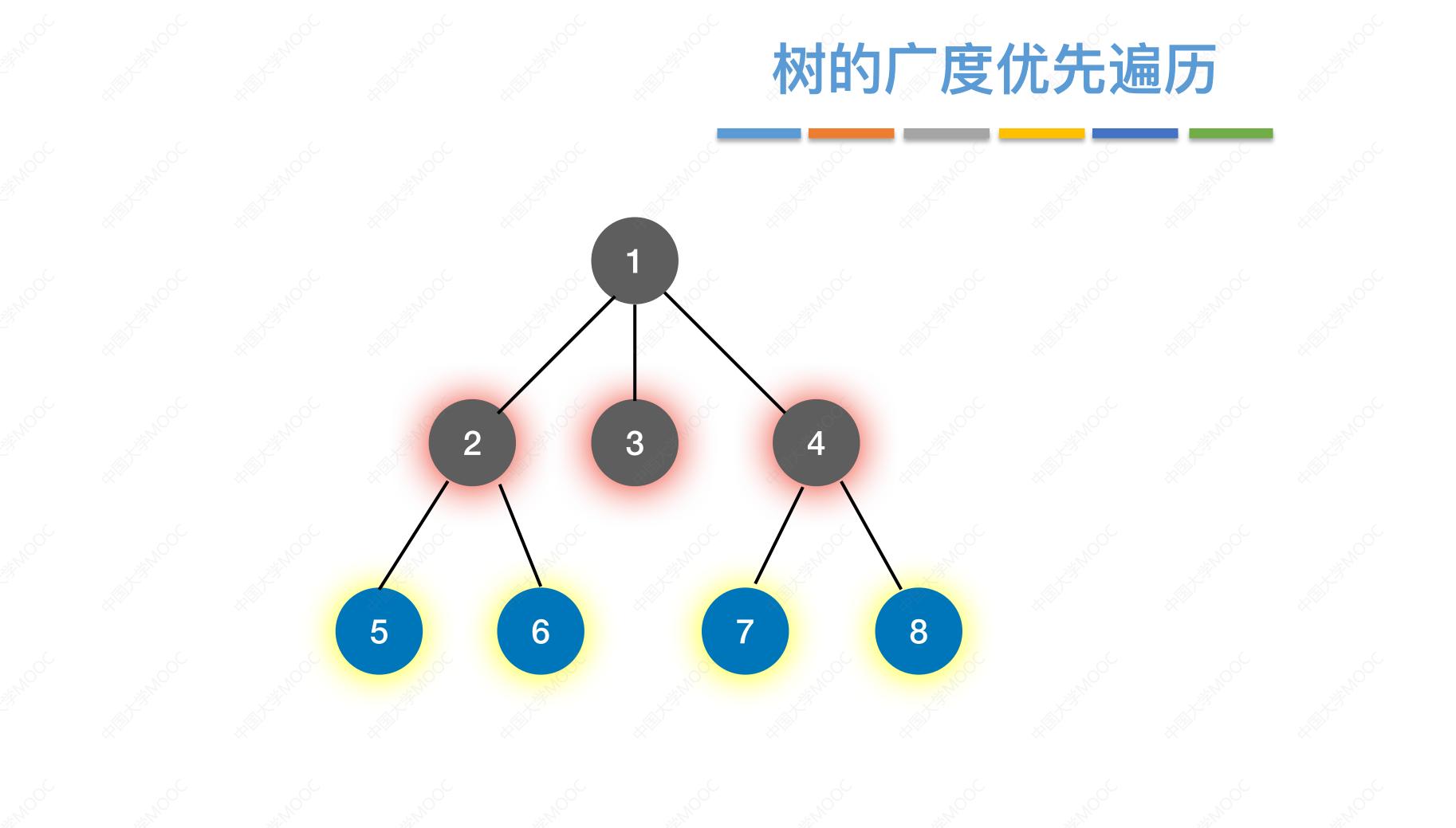
本节内容 图的遍历 BFS

知识总览

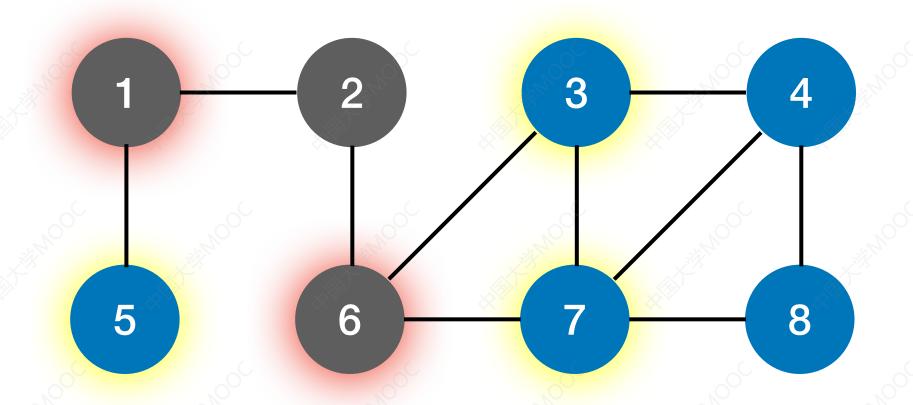




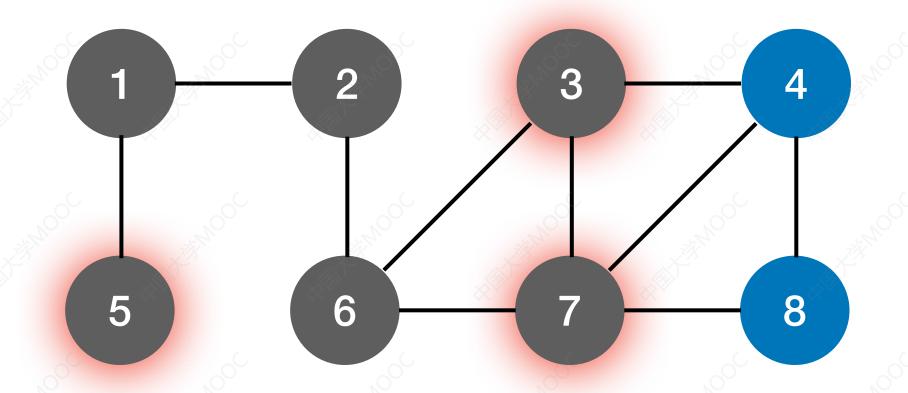




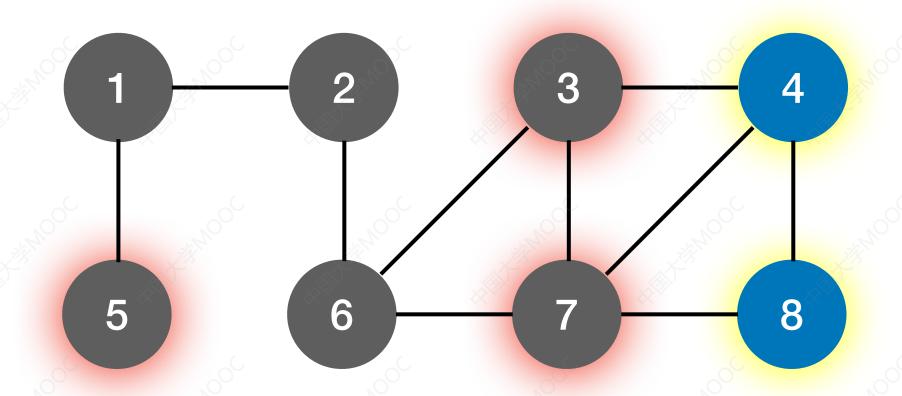
图的广度优先遍历



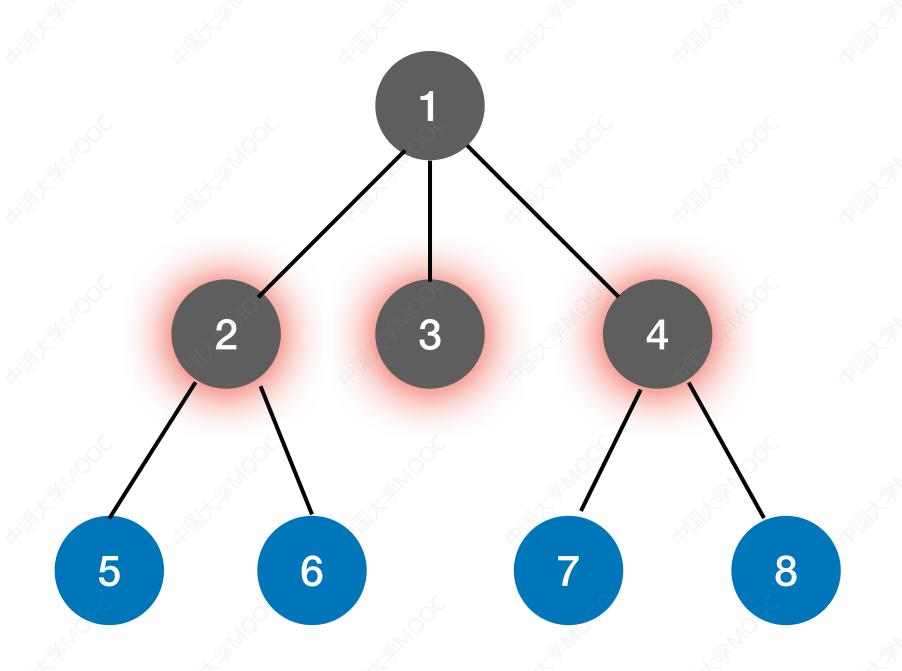
图的广度优先遍历



图的广度优先遍历



树 vs 图



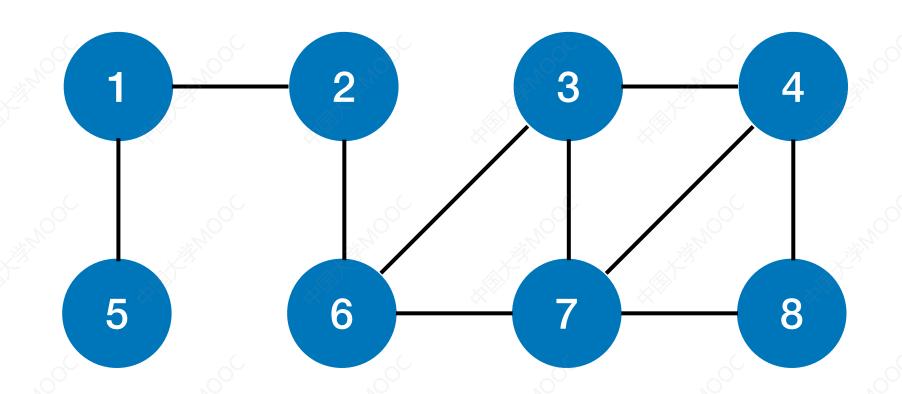
不存在"回路",搜索相邻的结点时,不可能搜到已经访问过的结点

1 2 3 4 5 6 7 8

搜索相邻的顶点时,有可能搜到已经访问过的顶点

树的广度优先遍历(层序遍历):

- ①若树非空,则根节点入队
- ②若队列非空,队头元素出队并访问,同时将该元素的孩子依次入队
- ③重复②直到队列为空



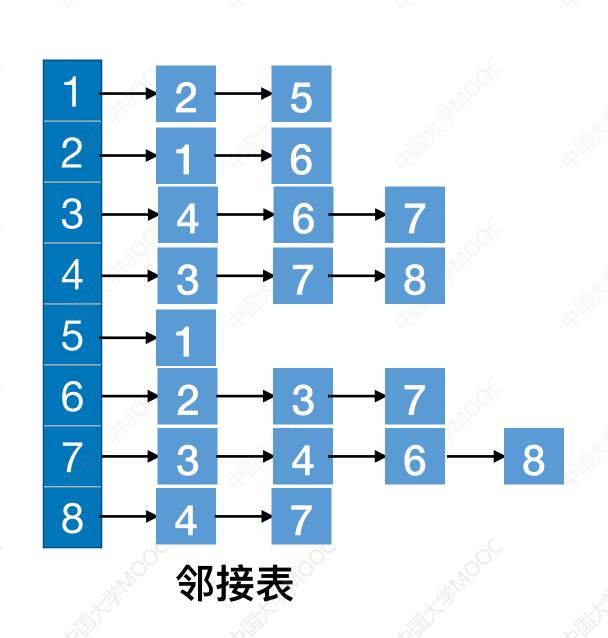
J	^一 度优先遍历	(Breadth-First-Search, BFS)	要点:
ı		(Broadtra riot Coaron, Dr. C)	× /111 '

- 1. 找到与一个顶点相邻的所有顶点
- 2. 标记哪些顶点被访问过
- 3. 需要一个辅助队列
- •FirstNeighbor(G,x):求图G中顶点x的第一个邻接点,若有则返回顶点号。若x没有邻接点或图中不存在x,则返回-1。
- •NextNeighbor(G,x,y):假设图G中顶点y是顶点x的一个邻接点,返回除y之外顶点x的下一个邻接点的顶点号,若y是x的最后一个邻接点,则返回-1。

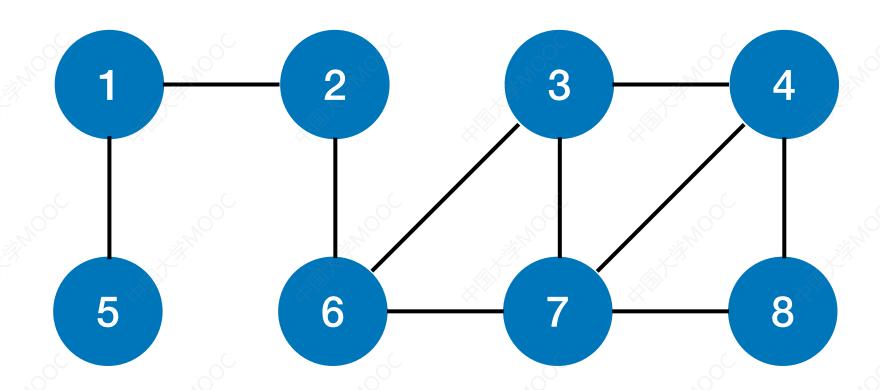
bool visited[MAX_VERTEX_NUM]; //访问标记数组

50	1	2	3	4	5	6	7	8
1	0		0	0	1	0	0	0
2	1	0	0	0	0	1	0	0
3	0	0	0	1	0	1	1	0
4	0	0	1	0	0	0	100	1
5	1	0	0	0	0	0	0	0
6	0	10	1	0	0	0	1	0
7	0	0	1	1	0	1	0	1
8	0	0	0	1	0	0	1	0
			ДД	/ 1 <> 	. 	_		

邻接矩阵



初始都为false



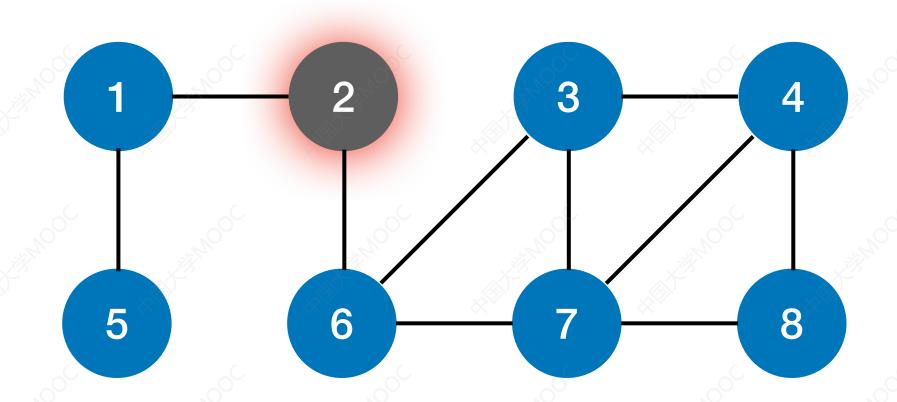
```
bool visited[MAX_VERTEX_NUM];
                               //访问标记数组
//广度优先遍历
void BFS(Graph G,int v){
                        //从顶点v出发,广度优先遍历图G
   visit(v);
                            //访问初始顶点v
   visited[v]=TRUE;
                            //对v做已访问标记
   Enqueue(Q,v);
                            //顶点v入队列Q
   while(!isEmpty(Q)){
       DeQueue(Q,v);
                            //顶点v出队列
       for(w=FirstNeighbor(G,v);w>=0;w=NextNeighbor(G,v,w))
          //检测v所有邻接点
          if(!visited[w]){
                           //w为v的尚未访问的邻接顶点
              visit(w);
                           //访问顶点w
              visited[w]=TRUE;//对w做已访问标记
              EnQueue(Q,w);
                           //顶点w入队列
          }//if
   }//while
```

visited false false false false false false

bool visited[MAX_VERTEX_NUM];

初始都为false

//访问标记数组



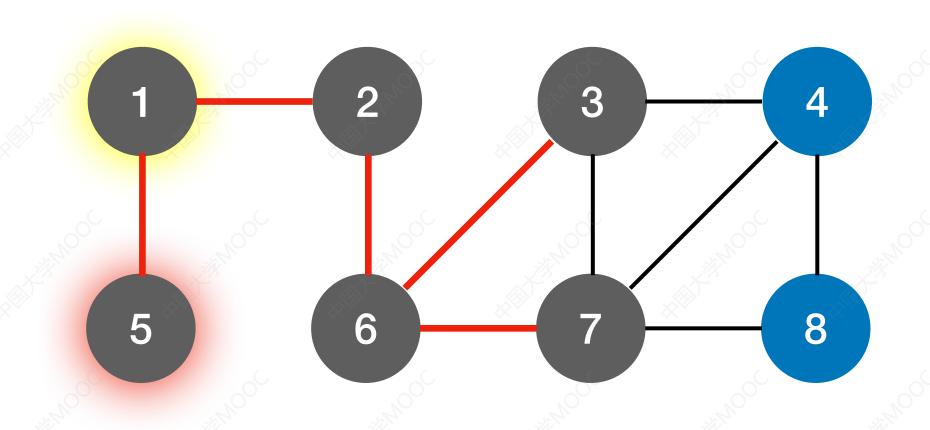
```
//广度优先遍历
void BFS(Graph G,int v){
                        //从顶点v出发,广度优先遍历图G
   visit(v);
                            //访问初始顶点v
   visited[v]=TRUE;
                            //对v做已访问标记
   Enqueue(Q,v);
                            //顶点v入队列Q
   while(!isEmpty(Q)){
       DeQueue(Q,v);
                            //顶点v出队列
       for(w=FirstNeighbor(G,v);w>=0;w=NextNeighbor(G,v,w))
          //检测v所有邻接点
          if(!visited[w]){
                           //w为v的尚未访问的邻接顶点
             visit(w);
                           //访问顶点w
              visited[w]=TRUE;//对w做已访问标记
              EnQueue(Q,w);
                           //顶点w入队列
          }//if
   }//while
```

visited false true false false false false false

bool visited[MAX_VERTEX_NUM];

初始都为false

//访问标记数组



```
2 1 6 5 3 7
```

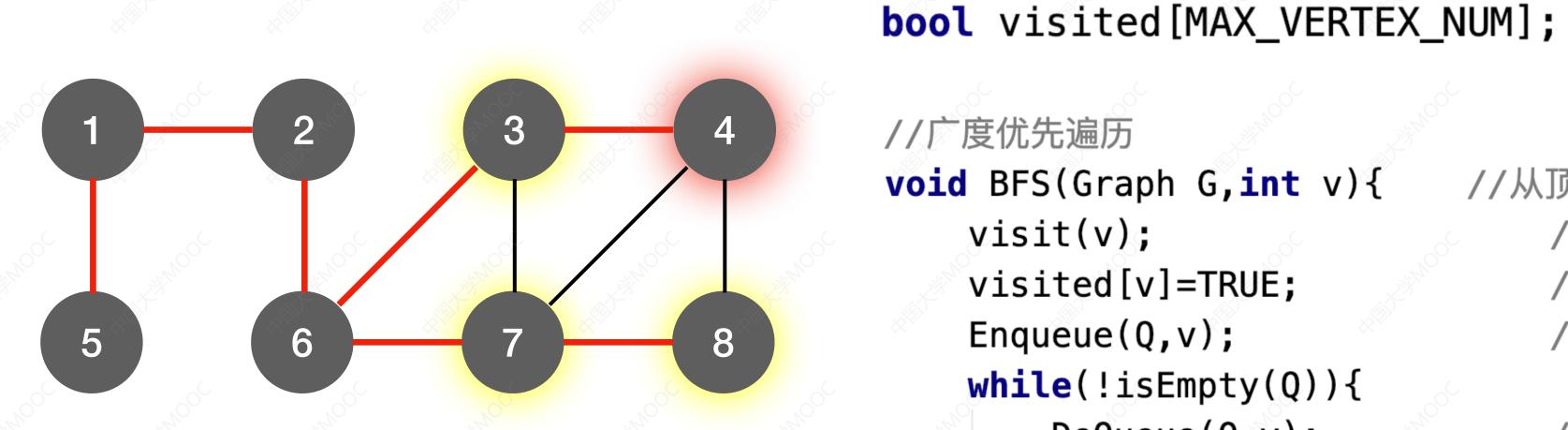
```
//广度优先遍历
                        //从顶点v出发,广度优先遍历图G
void BFS(Graph G,int v){
   visit(v);
                            //访问初始顶点v
   visited[v]=TRUE;
                            //对v做已访问标记
   Enqueue(Q,v);
                            //顶点v入队列Q
   while(!isEmpty(Q)){
       DeQueue(Q,v);
                            //顶点v出队列
       for(w=FirstNeighbor(G,v);w>=0;w=NextNeighbor(G,v,w))
          //检测v所有邻接点
          if(!visited[w]){
                           //w为v的尚未访问的邻接顶点
             visit(w);
                           //访问顶点w
              visited[w]=TRUE;//对w做已访问标记
              EnQueue(Q,w);
                           //顶点w入队列
          }//if
   }//while
```

visited true true false true true true false

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初始都为false

//访问标记数组



```
//广度优先遍历
void BFS(Graph G,int v){
                        //从顶点v出发,广度优先遍历图G
   visit(v);
                            //访问初始顶点v
                            //对v做已访问标记
   visited[v]=TRUE;
   Enqueue(Q,v);
                            //顶点v入队列Q
   while(!isEmpty(Q)){
      DeQueue(Q,v);
                            //顶点v出队列
       for(w=FirstNeighbor(G,v);w>=0;w=NextNeighbor(G,v,w))
          //检测v所有邻接点
          if(!visited[w]){
                           //w为v的尚未访问的邻接顶点
             visit(w);
                           //访问顶点w
              visited[w]=TRUE;//对w做已访问标记
              EnQueue(Q,w);
                          //顶点w入队列
   }//while
```

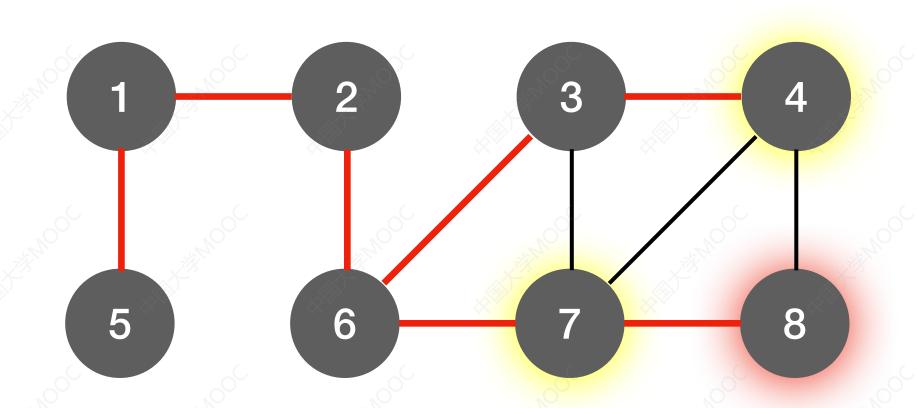
visited true true true true true true true

//广度优先遍历

bool visited[MAX_VERTEX_NUM];

初始都为false

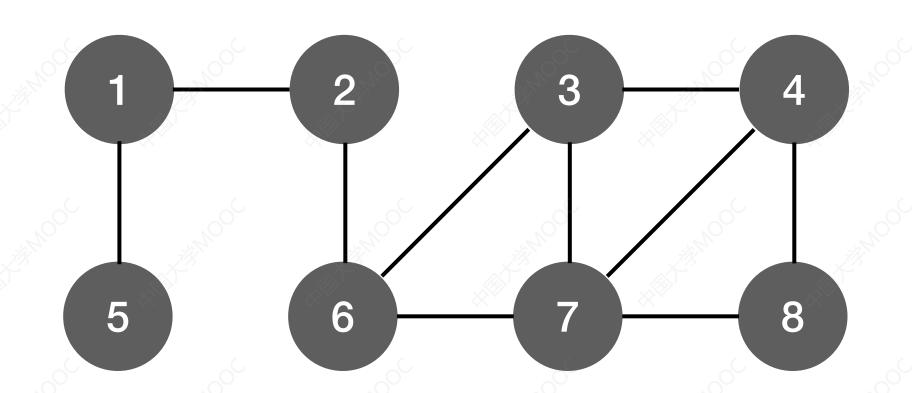
//访问标记数组



```
void BFS(Graph G,int v){
                        //从顶点v出发,广度优先遍历图G
   visit(v);
                            //访问初始顶点v
   visited[v]=TRUE;
                            //对v做已访问标记
   Enqueue(Q,v);
                            //顶点v入队列Q
   while(!isEmpty(Q)){
       DeQueue(Q,v);
                            //顶点v出队列
       for(w=FirstNeighbor(G,v);w>=0;w=NextNeighbor(G,v,w))
          //检测v所有邻接点
          if(!visited[w]){
                           //w为v的尚未访问的邻接顶点
             visit(w);
                           //访问顶点w
              visited[w]=TRUE;//对w做已访问标记
             EnQueue(Q,w);
                           //顶点w入队列
```

visited true true true true true true true

广度优先遍历序列



从顶点1出发得到的广度优先遍历序列:

1, 2, 5, 6, 3, 7, 4, 8

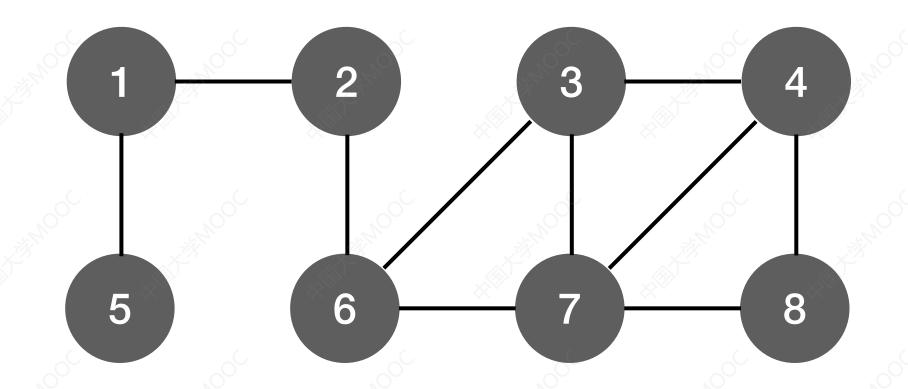
从顶点3出发得到的广度优先遍历序列:

3, 4, 6, 7, 8, 2, 1, 5

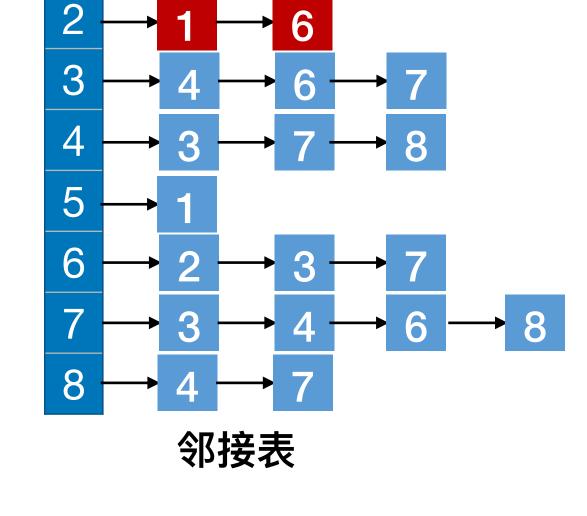


从顶点2出发得到的广 度优先遍历序列

遍历序列的可变性







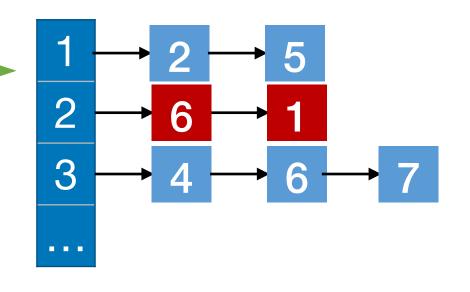
2 1 6 5 3 7 4 8

广度优先遍历序列: 2,6,1....

从顶点2出发得到的广 度优先遍历序列

同一个图的邻接矩阵表示方式唯一,因此广度优先遍历序列唯一

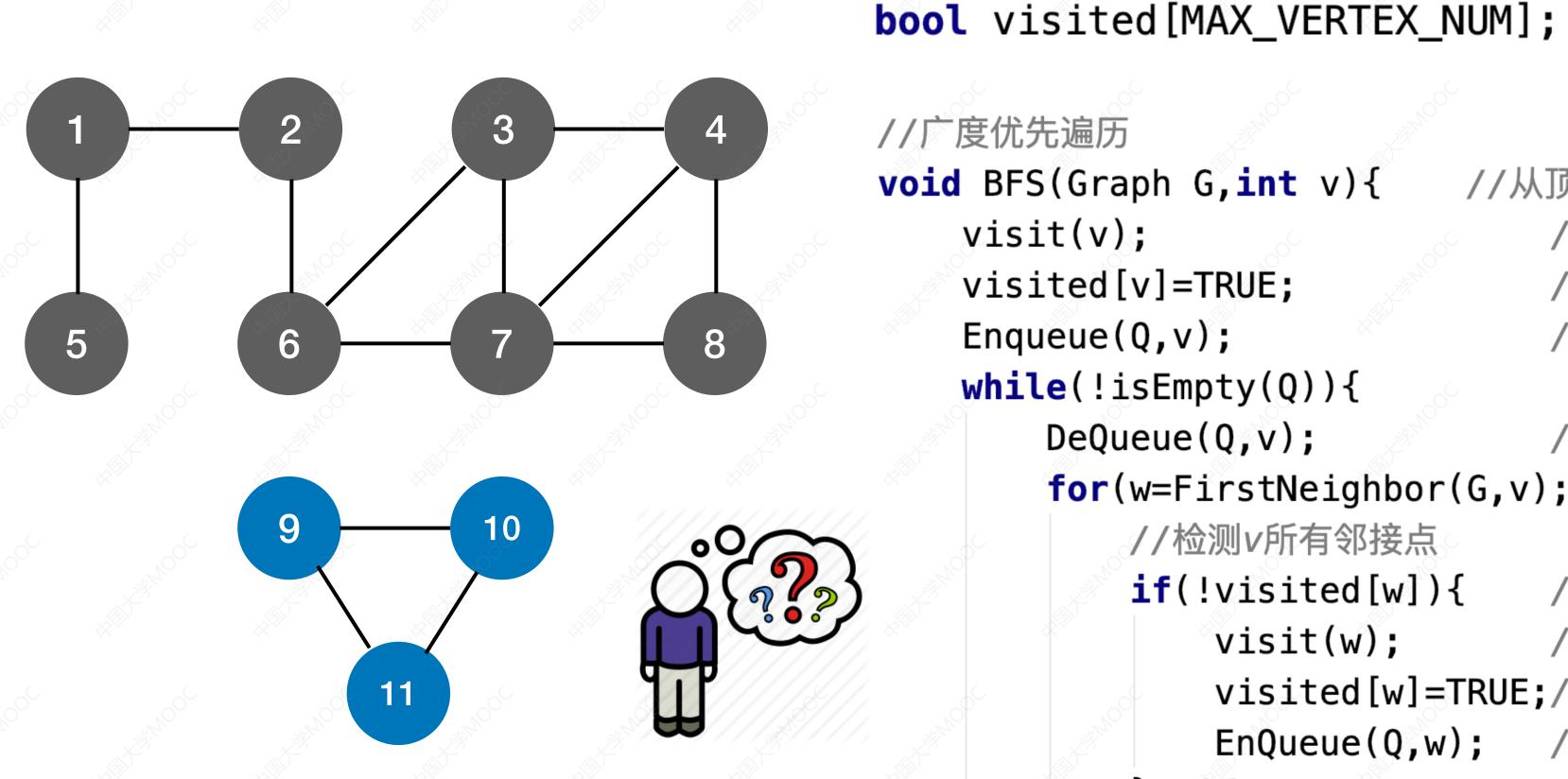
同一个图邻接表表示方式不唯一,因此广度优先遍历序列不唯一



算法存在的问题

初始都为false

//访问标记数组



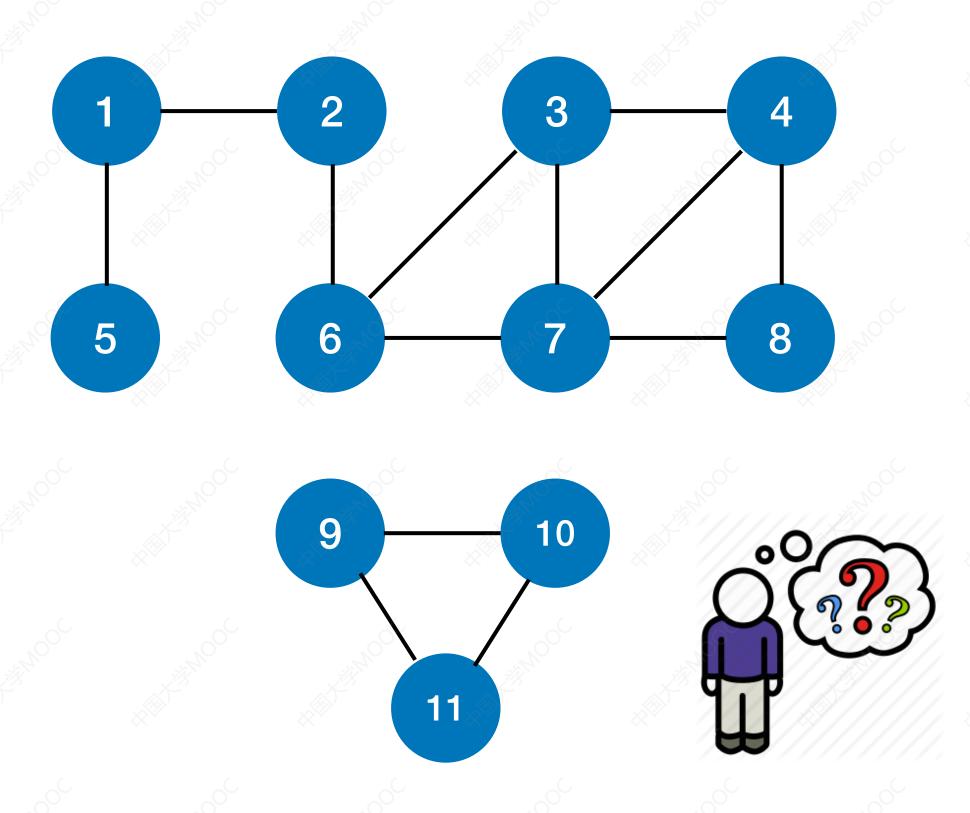
如果是非连通图,则无法遍历完所有结点

```
//广度优先遍历
void BFS(Graph G,int v){
                        //从顶点v出发,广度优先遍历图G
   visit(v);
                            //访问初始顶点v
   visited[v]=TRUE;
                            //对v做已访问标记
   Enqueue(Q,v);
                            //顶点v入队列Q
   while(!isEmpty(Q)){
       DeQueue(Q,v);
                            //顶点v出队列
       for(w=FirstNeighbor(G,v);w>=0;w=NextNeighbor(G,v,w))
          //检测v所有邻接点
          if(!visited[w]){
                           //w为v的尚未访问的邻接顶点
             visit(w);
                           //访问顶点w
              visited[w]=TRUE;//对w做已访问标记
              EnQueue(Q,w);
                          //顶点w入队列
          }//if
   }//while
```

visite true true true true true true true false false

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BFS算法 (Final版)



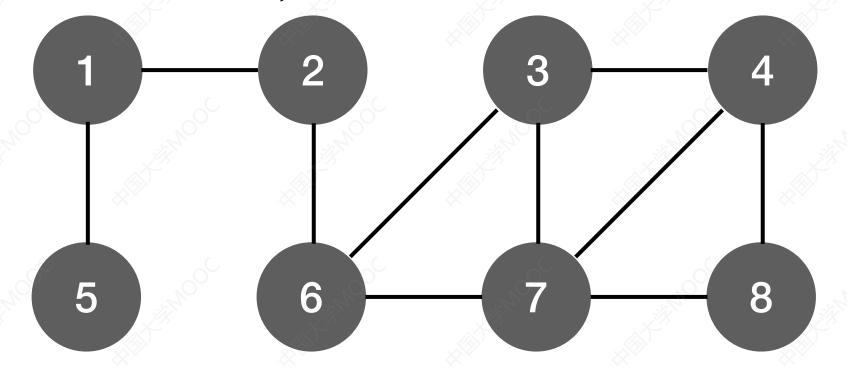
如果是非连通图,则无法遍历完所有结点

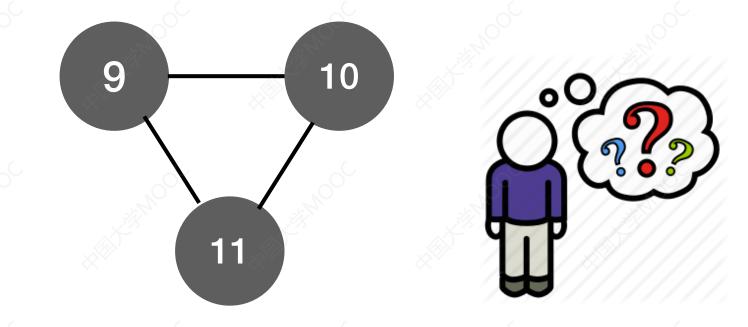
```
1 2 3 4 5 6 7 8 9 10 11 visited false false
```

```
bool visited[MAX_VERTEX_NUM];
                              //访问标记数组
void BFSTraverse(Graph G){ //对图G进行广度优先遍历
    for(i=0;i<G.vexnum;++i)</pre>
       visited[i]=FALSE;
                             //访问标记数组初始化
    InitQueue(Q);
                                 //初始化辅助队列Q
    for(i=0;i<G.vexnum;++i)</pre>
                             //从0号顶点开始遍历
       if(!visited[i])
                             //对每个连通分量调用一次BFS
           BFS(G,i);
                             //vi未访问过,从vi开始BFS
//广度优先遍历
void BFS(Graph G,int v){
                        //从顶点v出发,广度优先遍历图G
   visit(v);
                            //访问初始顶点v
   visited[v]=TRUE;
                            //对v做已访问标记
   Enqueue(Q,v);
                            //顶点v入队列Q
   while(!isEmpty(Q)){
       DeQueue(Q,v);
                            //顶点v出队列
       for(w=FirstNeighbor(G,v);w>=0;w=NextNeighbor(G,v,w))
          //检测v所有邻接点
          if(!visited[w]){
                           //w为v的尚未访问的邻接顶点
              visit(w);
                            //访问顶点w
              visited[w]=TRUE;//对w做已访问标记
              EnQueue(Q,w);
                           //顶点w入队列
          }//if
   }//while
```

BFS算法 (Final版)

结论:对于无向图,调用BFS函数的次数=连通分量数

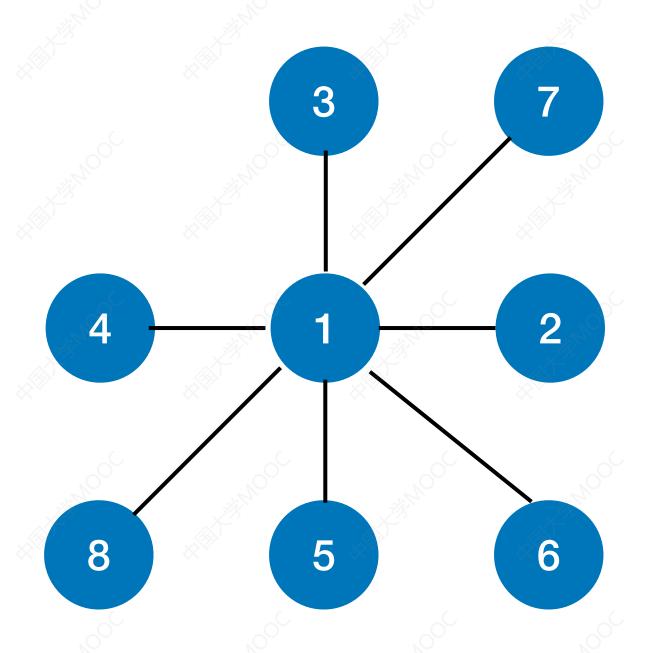




如果是非连通图,则无法遍历完所有结点

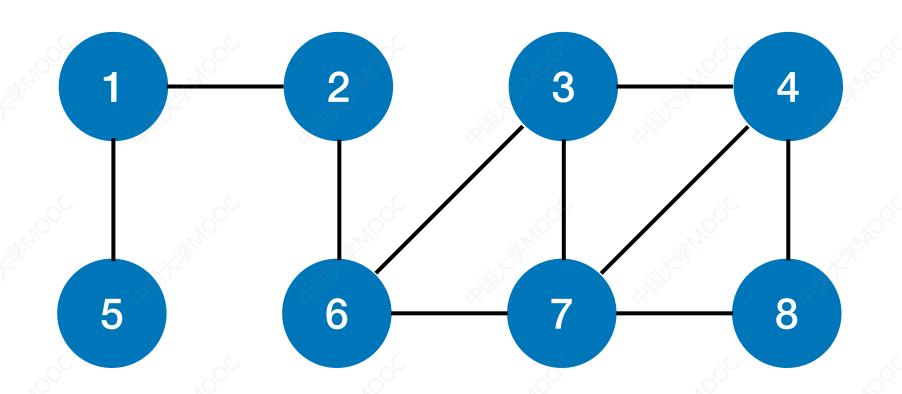
```
bool visited[MAX_VERTEX_NUM];
                              //访问标记数组
void BFSTraverse(Graph G){ //对图G进行广度优先遍历
    for(i=0;i<G.vexnum;++i)</pre>
       visited[i]=FALSE;
                             //访问标记数组初始化
    InitQueue(Q);
                                 //初始化辅助队列Q
    for(i=0;i<G.vexnum;++i)</pre>
                             //从0号顶点开始遍历
       if(!visited[i])
                             //对每个连通分量调用一次BFS
           BFS(G,i);
                             //vi未访问过,从vi开始BFS
//广度优先遍历
void BFS(Graph G,int v){
                        //从顶点v出发,广度优先遍历图G
   visit(v);
                            //访问初始顶点v
   visited[v]=TRUE;
                            //对v做已访问标记
   Enqueue(Q,v);
                            //顶点v入队列Q
   while(!isEmpty(Q)){
       DeQueue(Q,v);
                            //顶点v出队列
       for(w=FirstNeighbor(G,v);w>=0;w=NextNeighbor(G,v,w))
          //检测v所有邻接点
          if(!visited[w]){
                           //w为v的尚未访问的邻接顶点
              visit(w);
                            //访问顶点w
              visited[w]=TRUE;//对w做已访问标记
              EnQueue(Q,w);
                           //顶点w入队列
          }//if
   }//while
```

复杂度分析

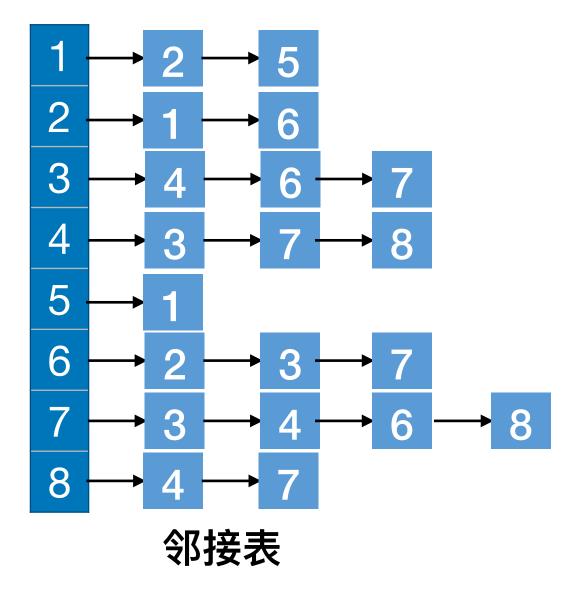


空间复杂度:最坏情况,辅助队列大小为 O(|V|)

复杂度分析





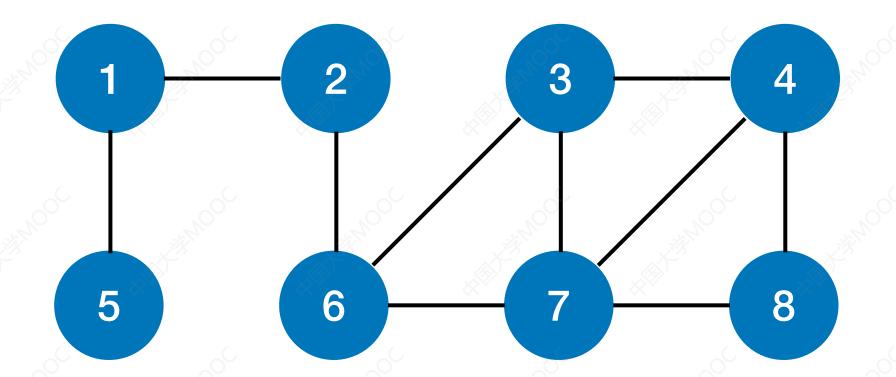


邻接矩阵存储的图:

访问 |V| 个顶点需要O(|V|)的时间 查找每个顶点的邻接点都需要O(|V|)的时间,而总共有|V|个顶点 时间复杂度= O(|V|²)

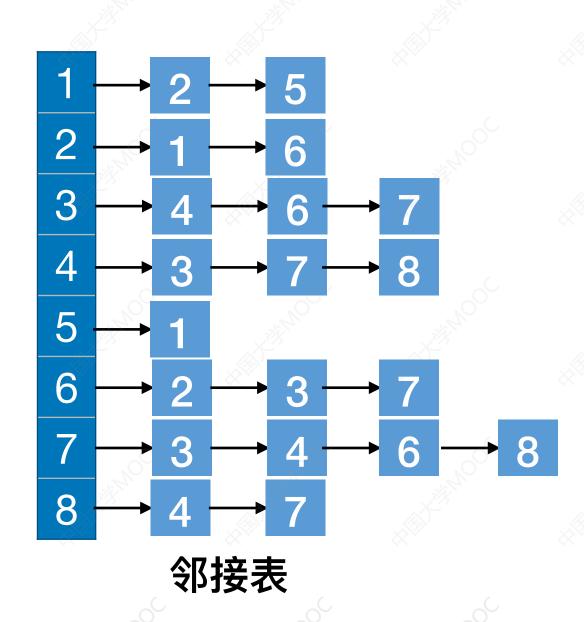
邻接表存储的图:

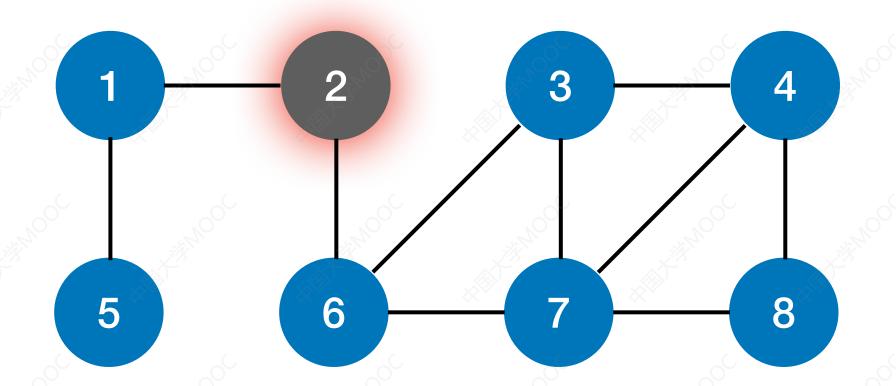
访问 |V| 个顶点需要O(|V|)的时间 查找各个顶点的邻接点共需要O(|E|)的时间, 时间复杂度= O(|V|+|E|)



	1	2	3	4	5	6	7	8
1	0	1	0	0	1	0	0	0
2	1	0	0	0	0	1	0	0
3	0	0	0	1	0	1	1	0
4	0	0	1	0	0	0	91	1
5	1	0	0	0	0	0	0	0
6	0	1	1	0	0	0	1	0
7	0	0	1-//		0		0	1
8	0	0	0	1	0	0	1	0

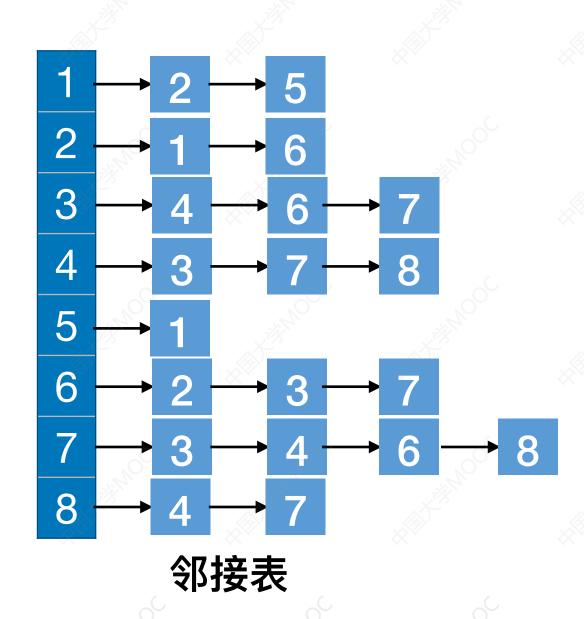
邻接矩阵

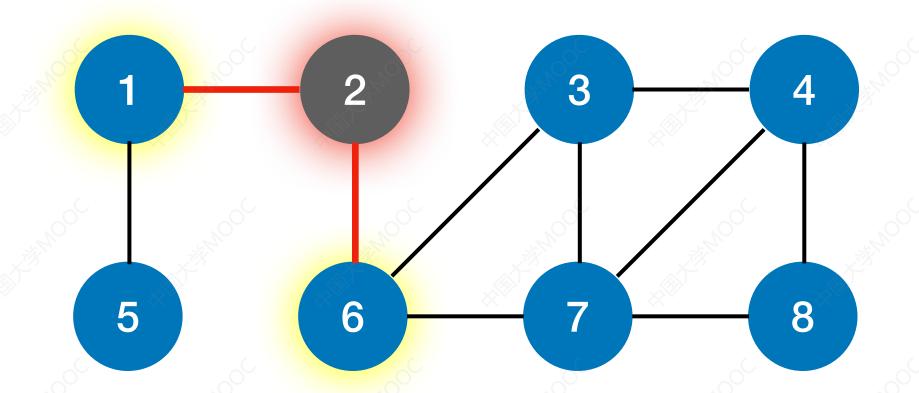




×× 	1	2	3	4	5	6	7	8
1	0	1	0	0	1	0	0	0
2	1	0	0	0	0	1	0	0
3	0	0	0	1	0	1	1	0
4	0	0	1	0	0	0	1	1
5	1	0	0	0	0	0	0	0
6	0	1	1	0	0	0	1	0
7	0	0	1	1	0	1	0	1
8	0	0	0	1	0	0	1	0

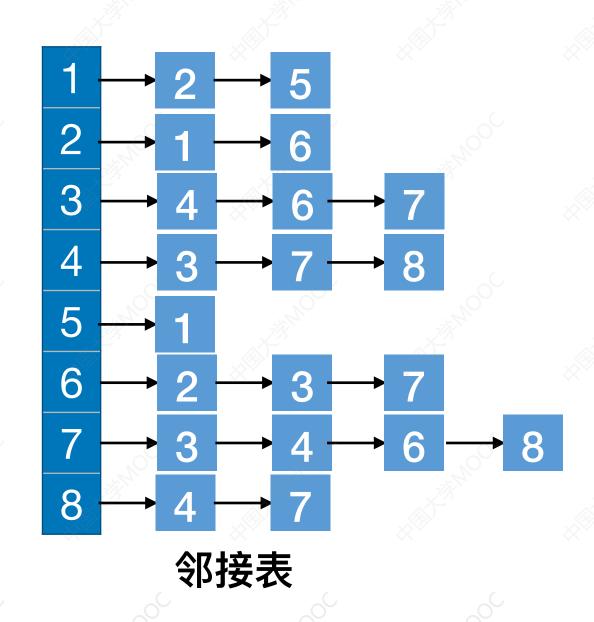
邻接矩阵



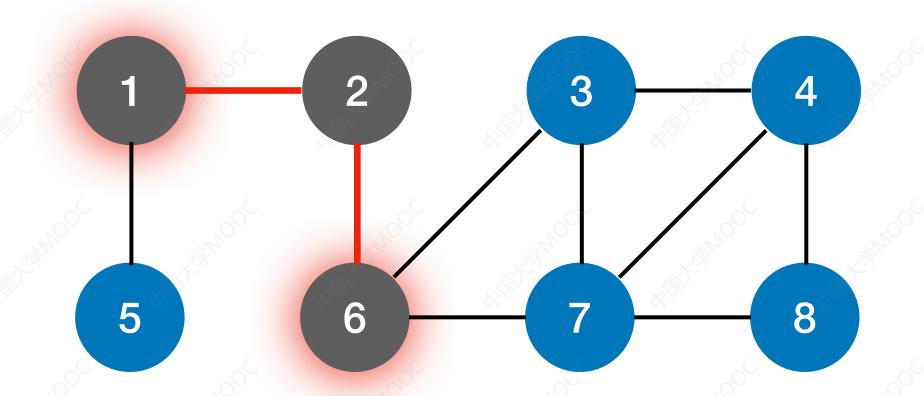


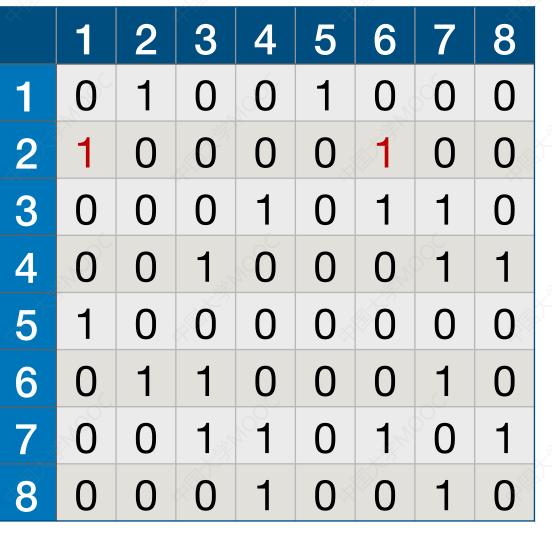
	l		\otimes			Y	l	\times	1
	1	2	3	4	5	6	7	8	
1	0	1	0	0	1	0	0	0	
2	1	0	0	0	0	1	0	0	X
3	0	0	0	1	0	1	1	0	
4	0	0	1	0	0	0	1	1	j
5	1	0	0	0	0	0	0	0	
6	0	1	1	0	0	0	1	0	
7	0	0	1	1	0		0	1	, ž
8	0	0	0	1	0	0	1	0	

邻接矩阵

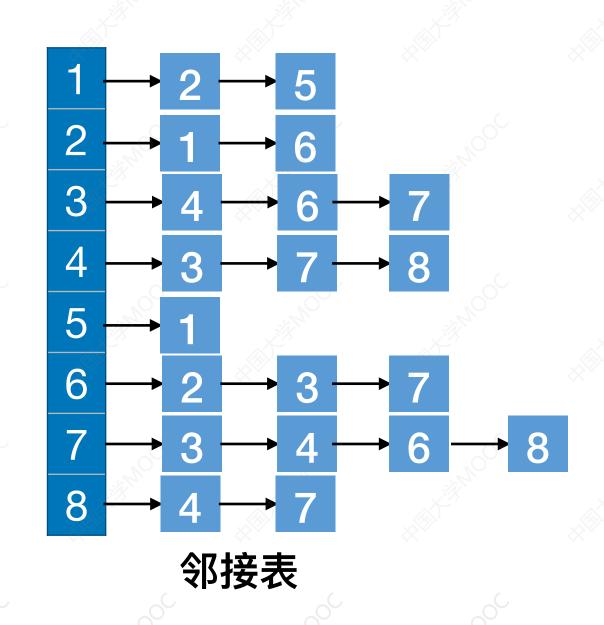


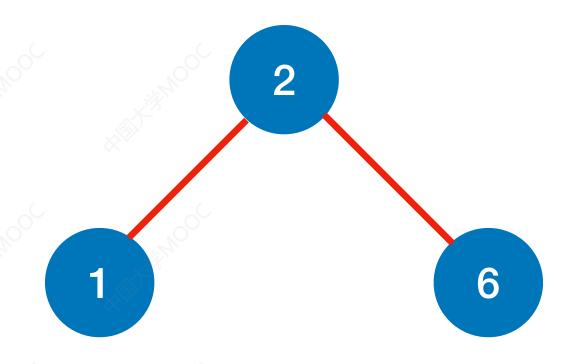
2

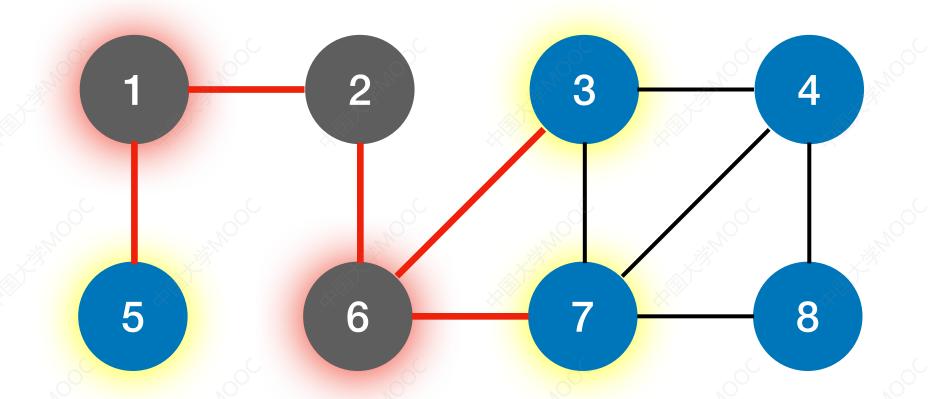




邻接矩阵

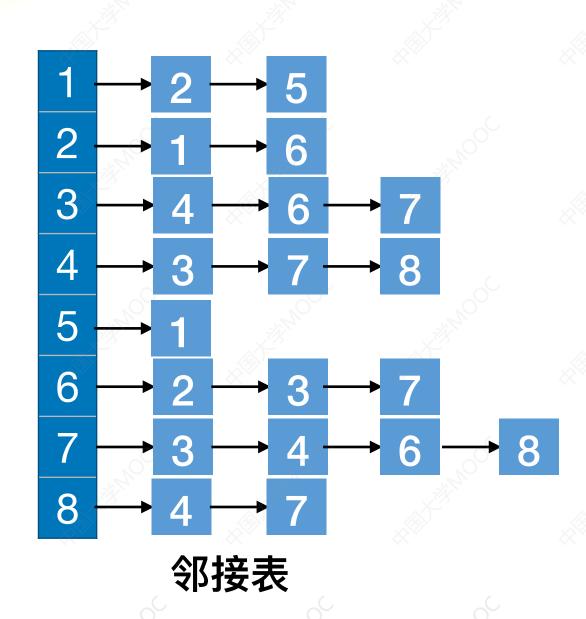


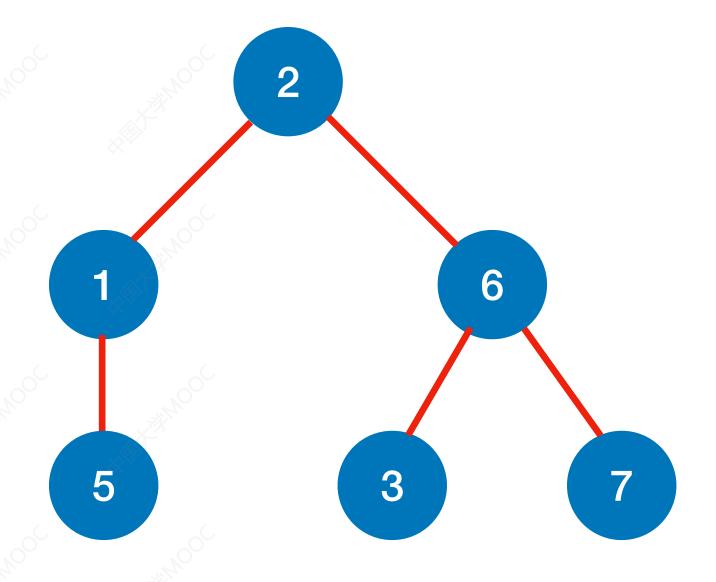


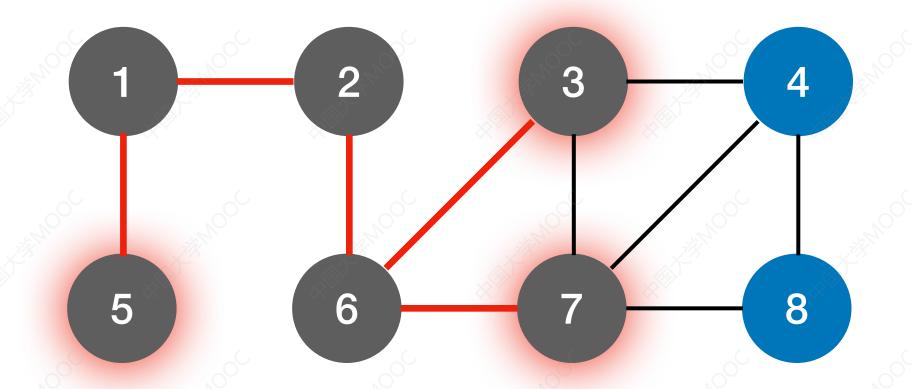


××	1	2	3	4	5	6	7	8
1	0	1	0	0	1	0	0	0
2	1	0	0	0	0	1	0	0
3	0	0	0	1	0	1	1	0
4	0	0	1	0	0	0	1	1
5	1	0	0	0	0	0	0	0
6	0	1	1	0	0	0	1	0
7	0	0	1	1	0	1	0	1
8	0	0	0	1	0	0	1	0

邻接矩阵

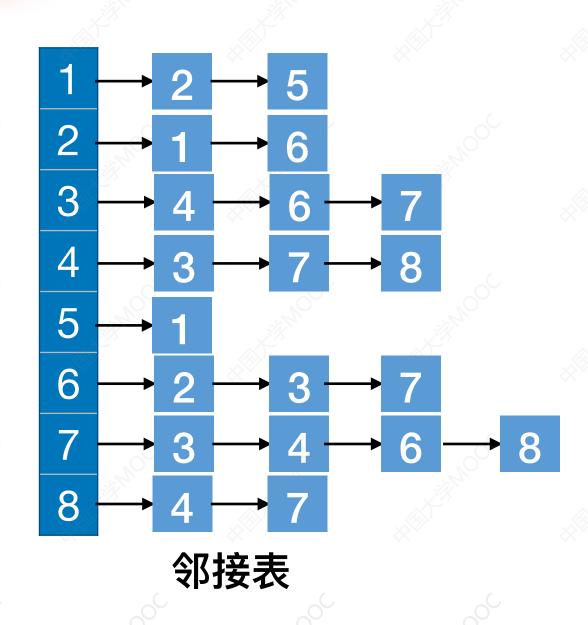


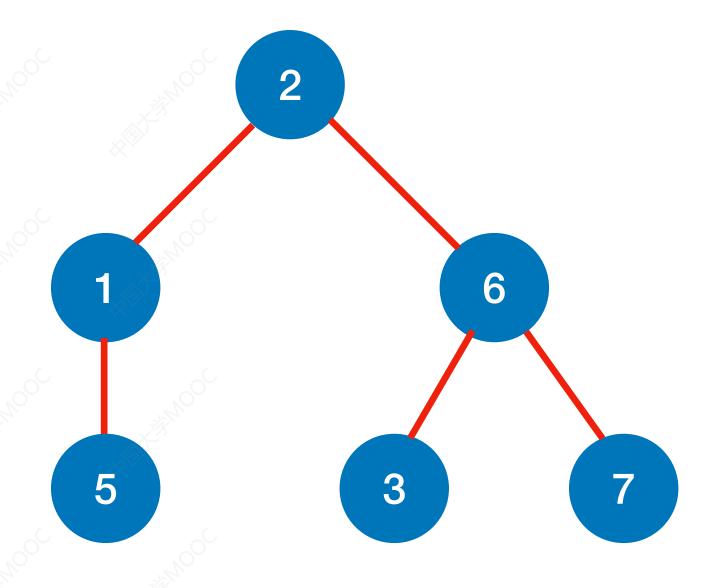


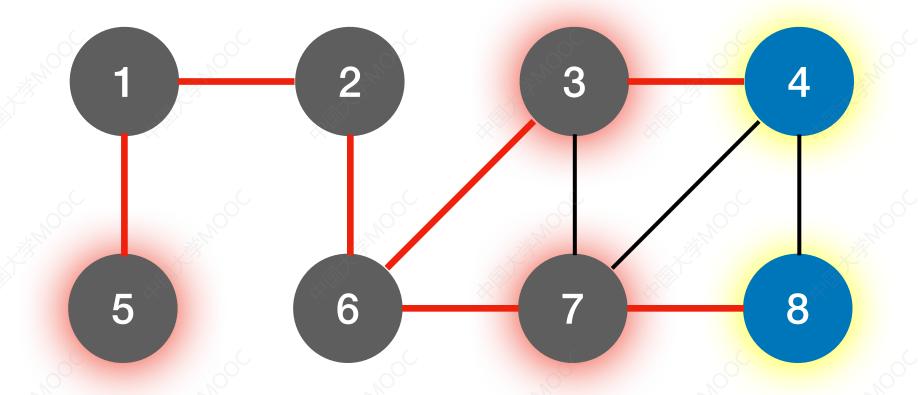


××	1	2	3	4	5	6	7	8
1	0	1	0	0	1	0	0	0
2	1	0	0	0	0	1	0	0
3	0	0	0	1	0	1	1	0
4	0	0	1	0	0	0	1	1
5	1	0	0	0	0	0	0	0
6	0	1	1	0	0	0	1	0
7	0	0	1	1	0	1	0	1
8	0	0	0	1	0	0	1	0

邻接矩阵

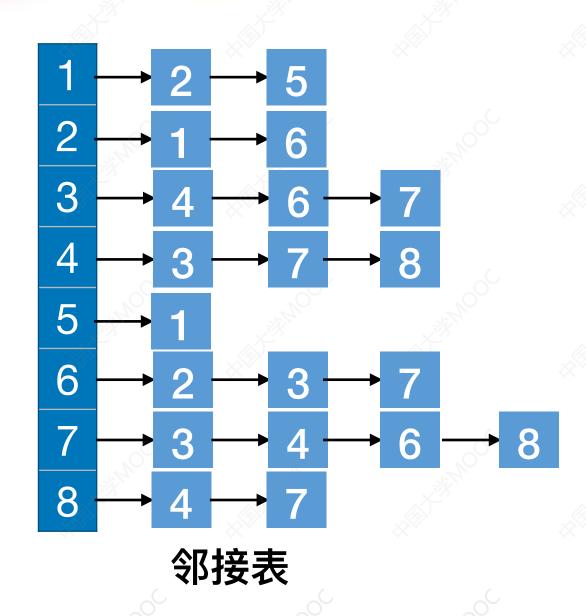


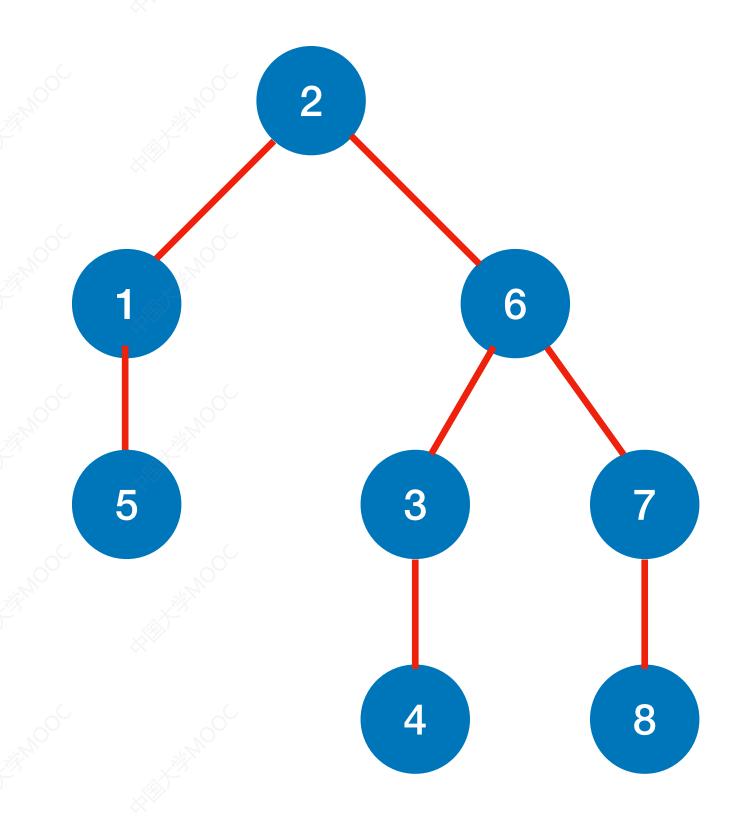


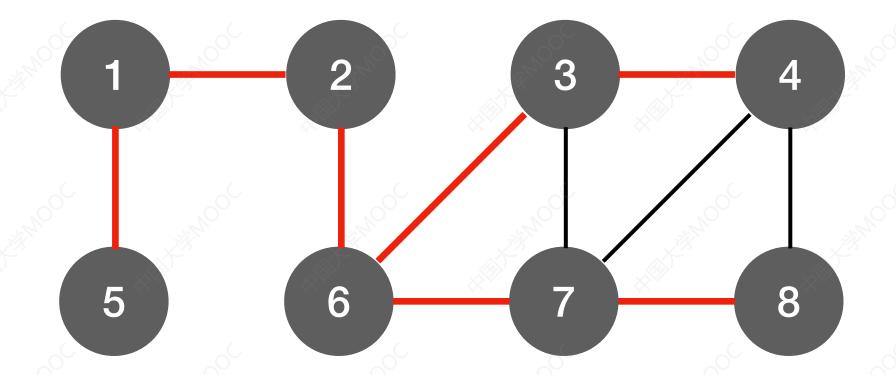


×× ×	1	2	3	4	5	6	7	8
1	0	1	0	0	1	0	0	0
2	1	0	0	0	0	1	0	0
3	0	0	0	1	0	1	1	0
4	0	0	1	0	0	0	1	1
5	1	0	0	0	0	0	0	0
6	0	1	1	0	0	0	1	0
7	0	0	1	1	0	1	0	1
8	0	0	0	1	0	0	1	0

邻接矩阵

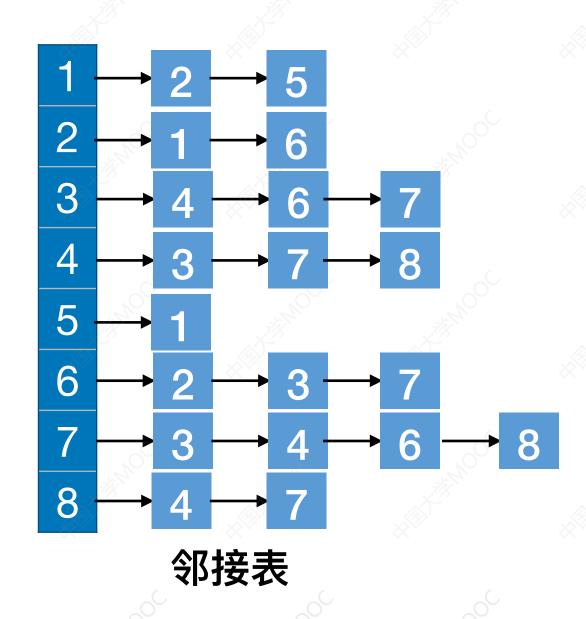


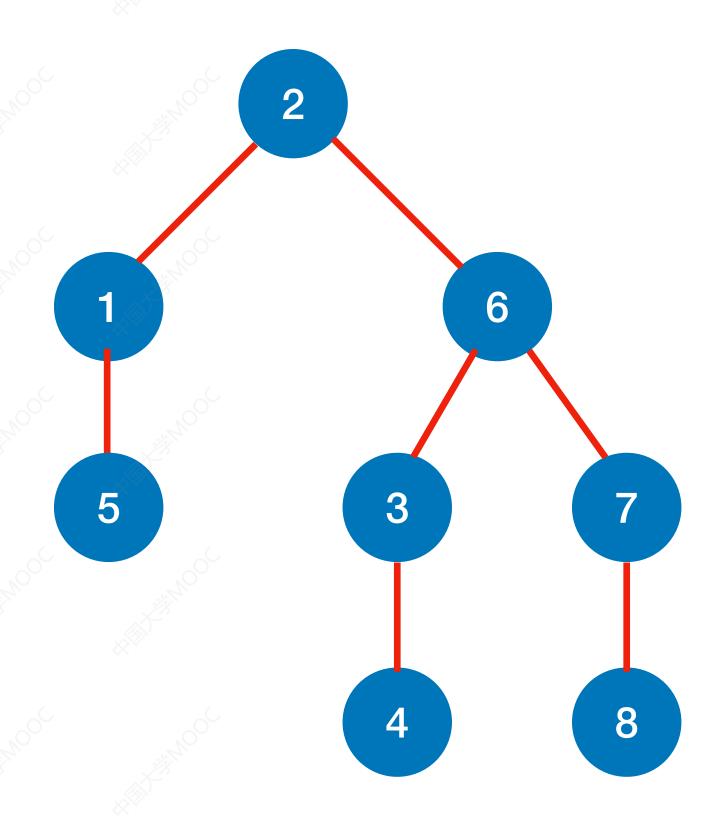




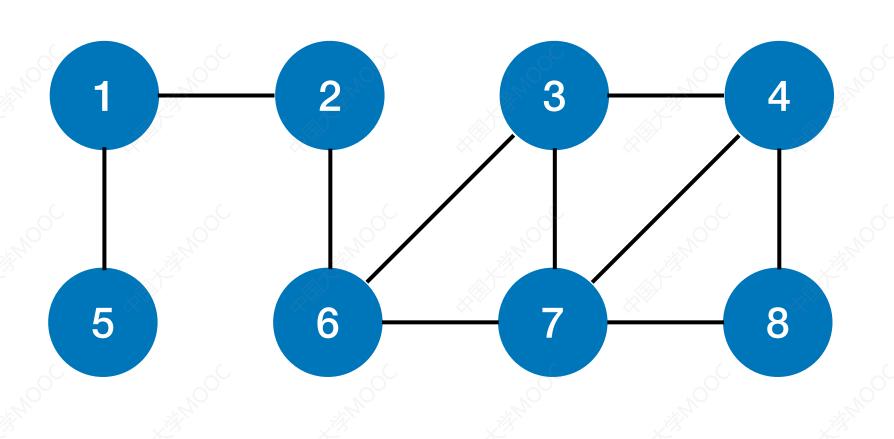
×××	1	2	3	4	5	6	7	8
1	0	1	0	0	1	0	0	0
2	1	0	0	0	0	1	0	0
3	0	0	0	1	0	1	1	0
4	0	0	1	0	0	0	1	1
5	1	0	0	0	0	0	0	0
6	0	1	1	0	0	0	1	0
7	0	0	1	1	0		0	1
8	0	0	0	1	0	0	1	0

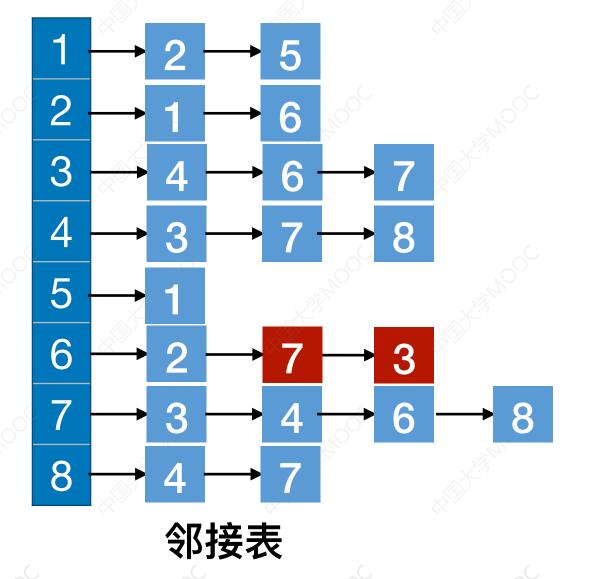
邻接矩阵

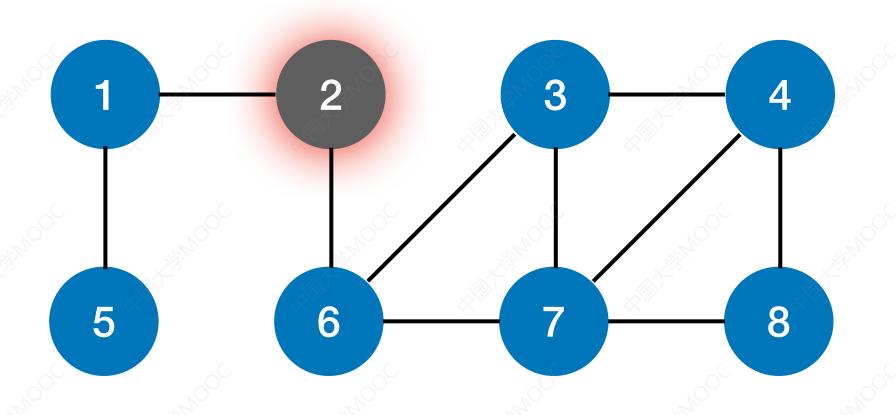


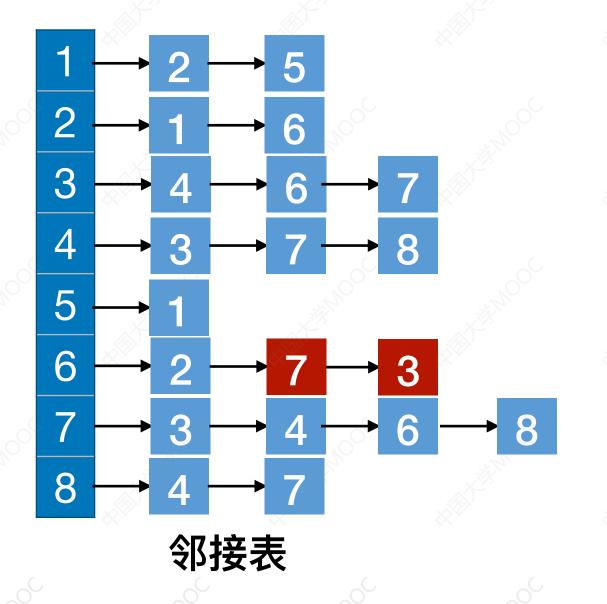


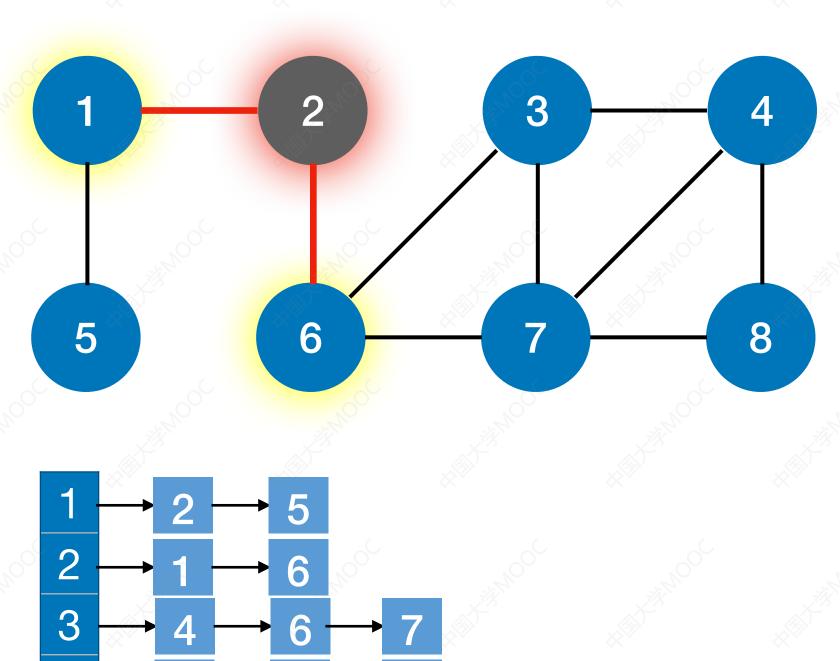
广度优先生成树



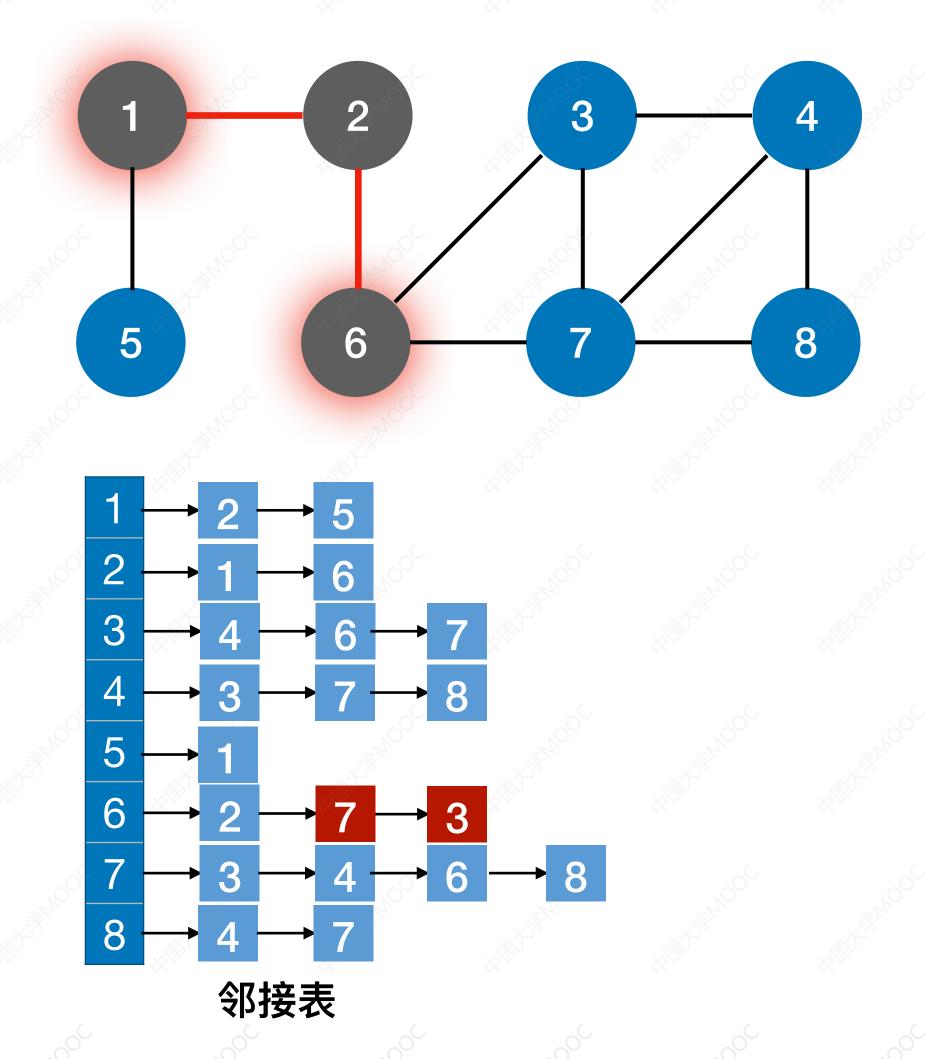


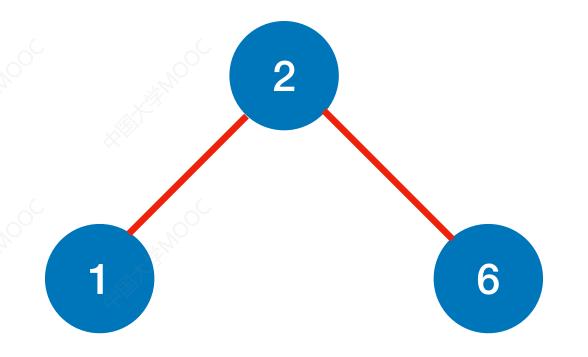


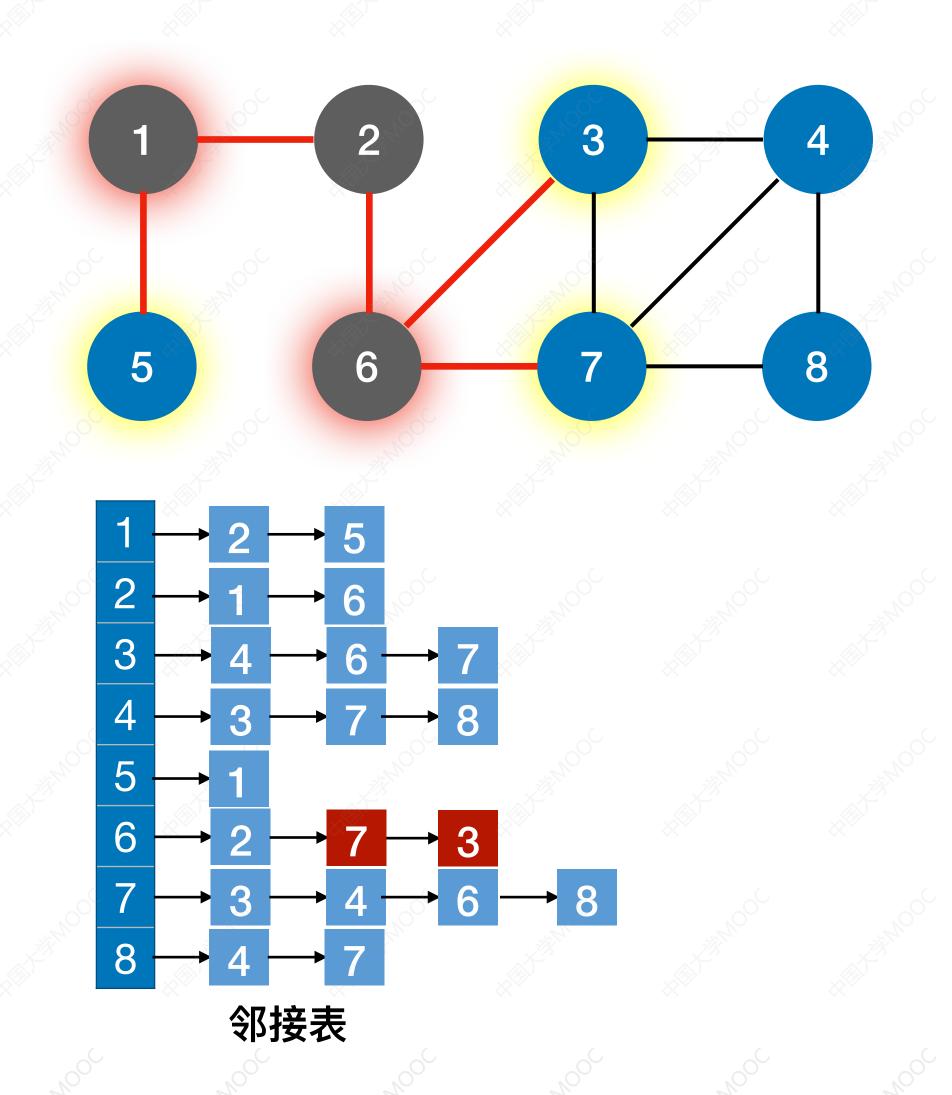


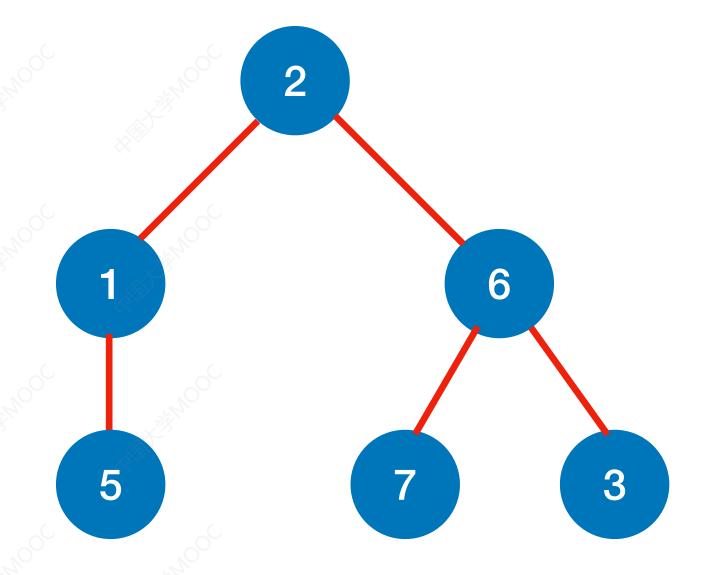


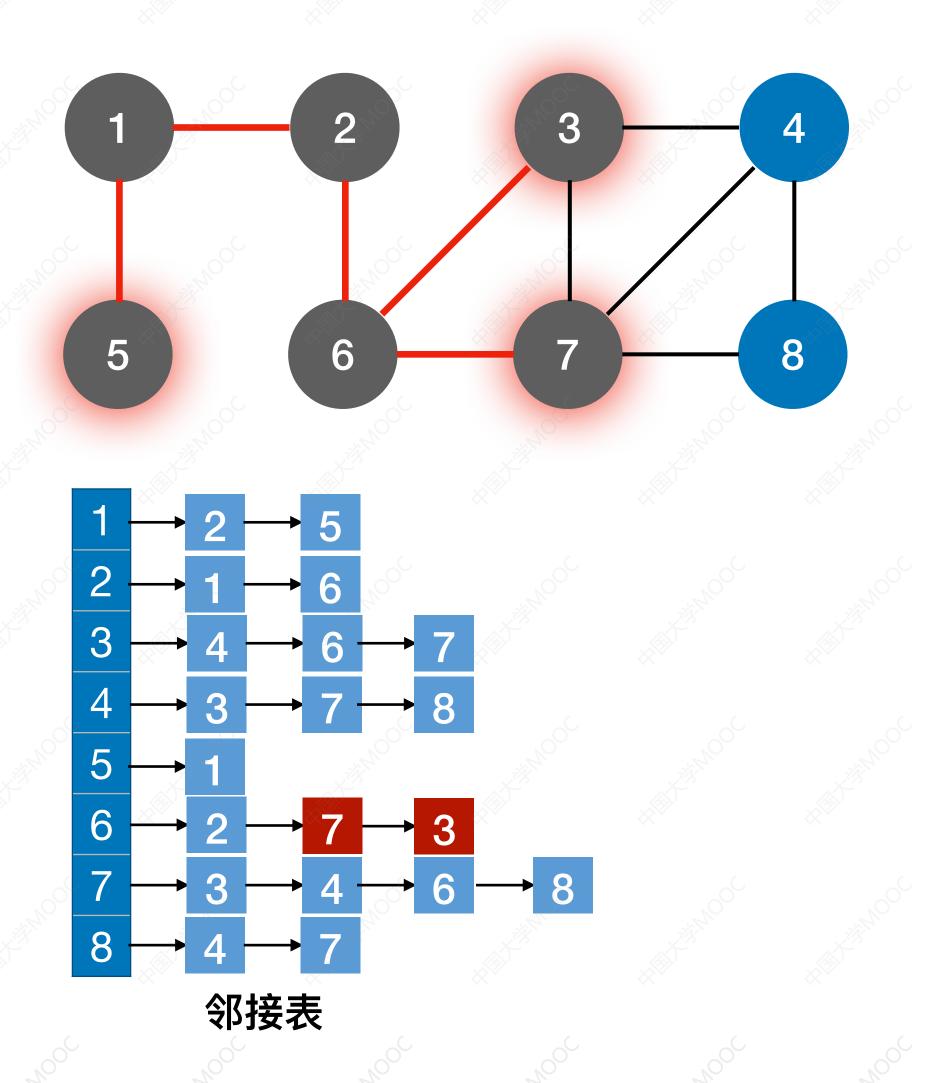
2

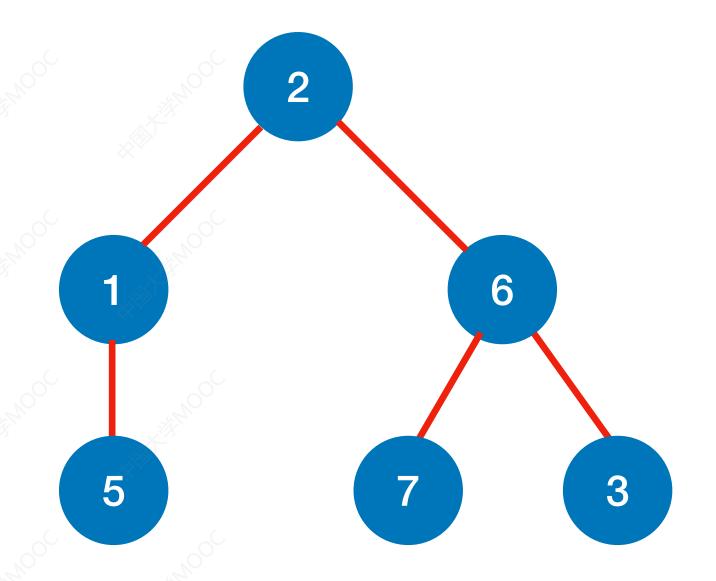


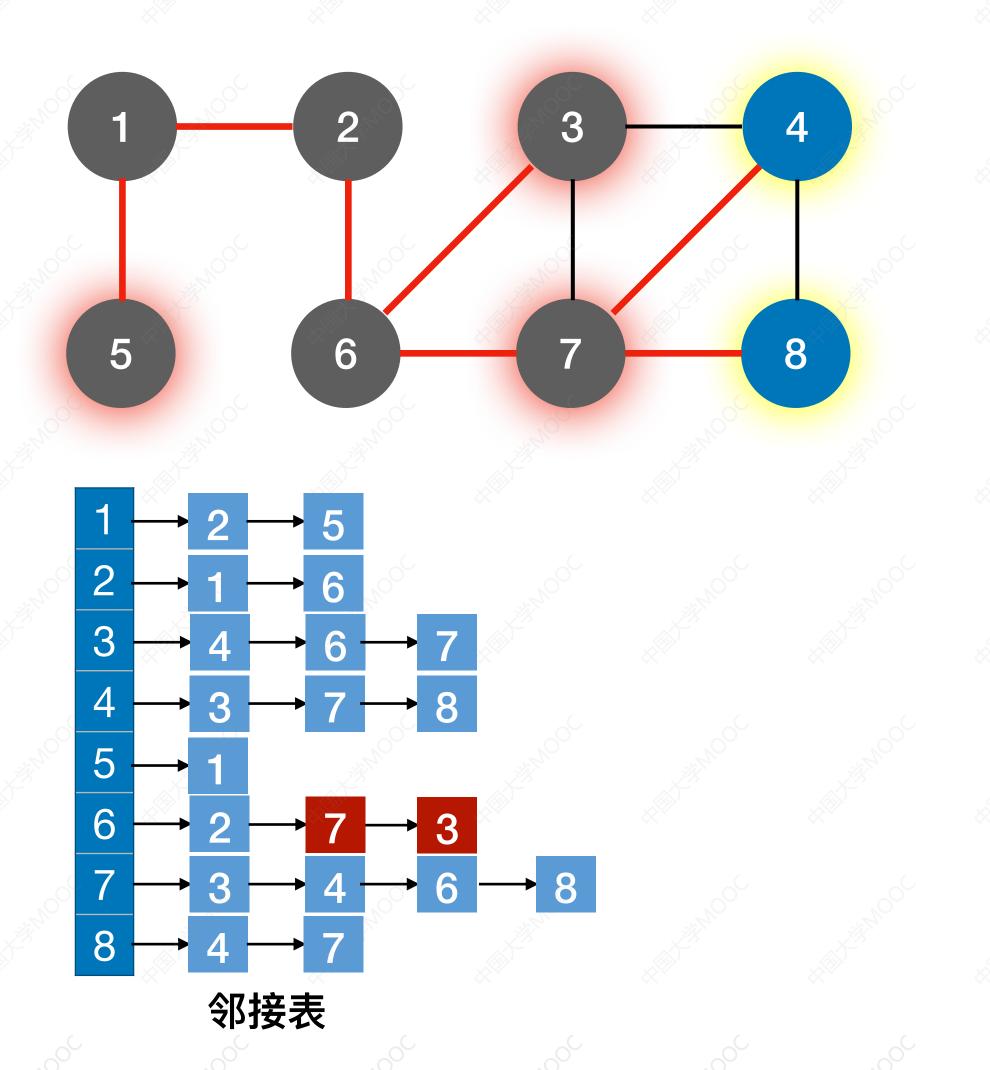


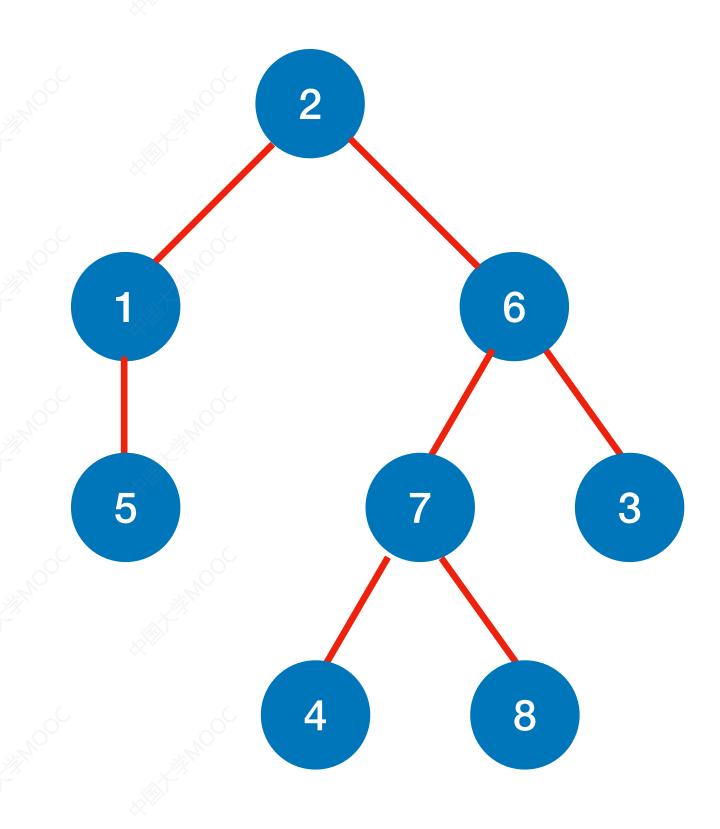


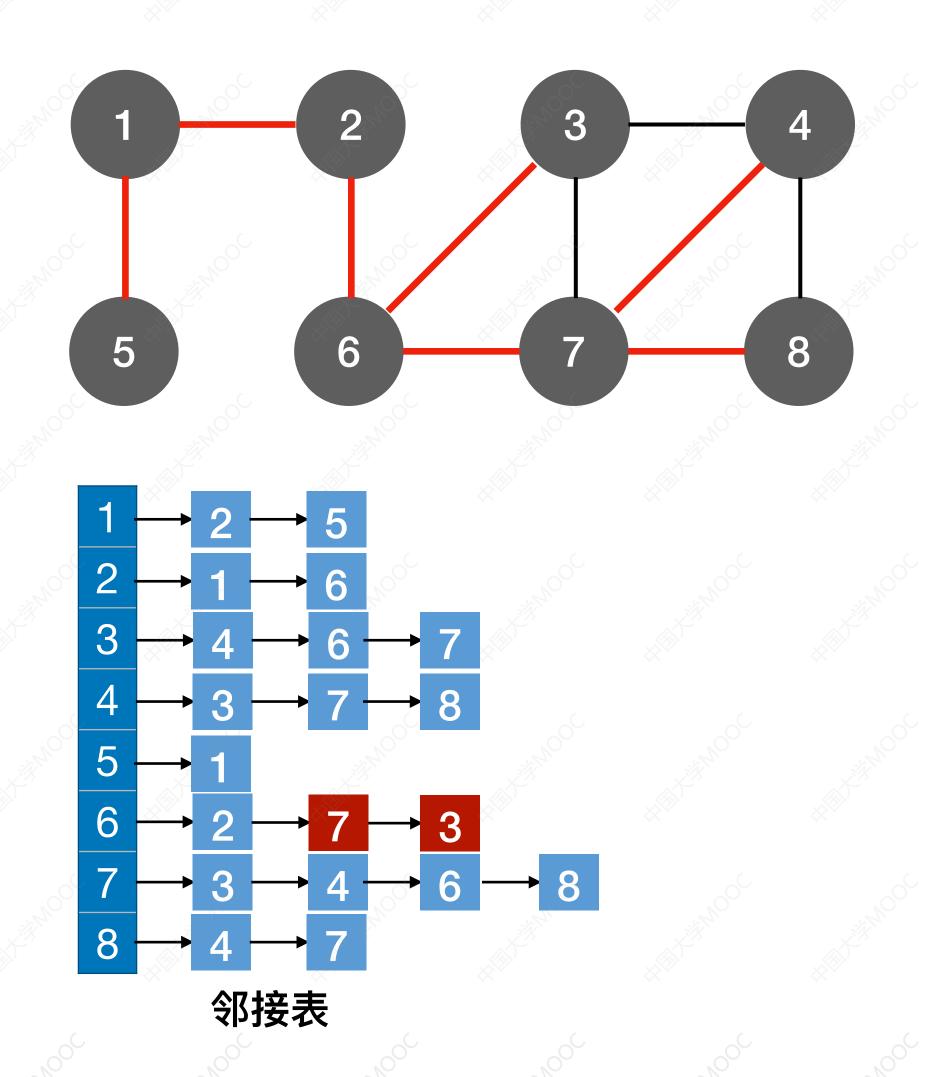


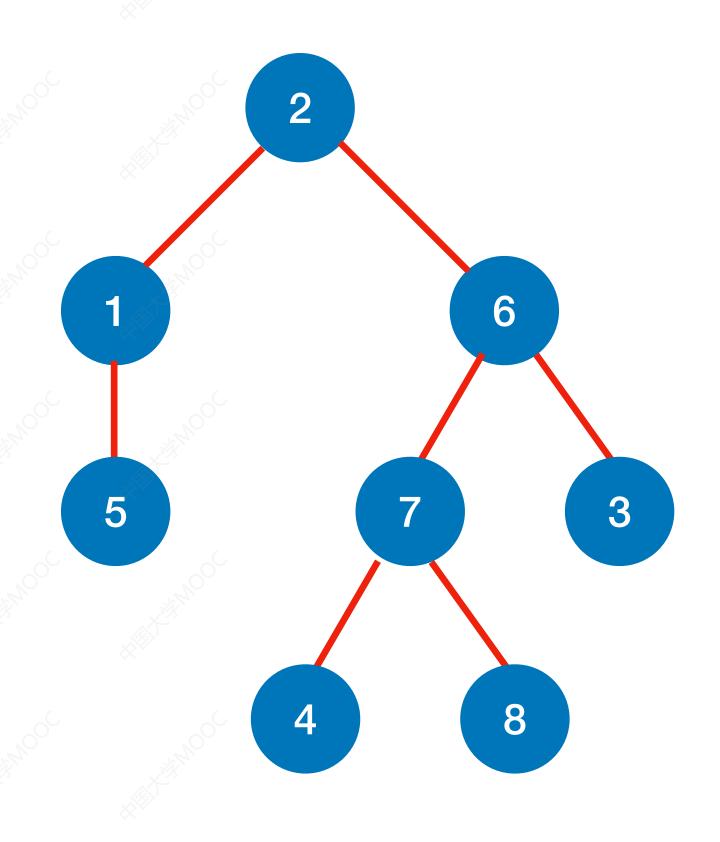


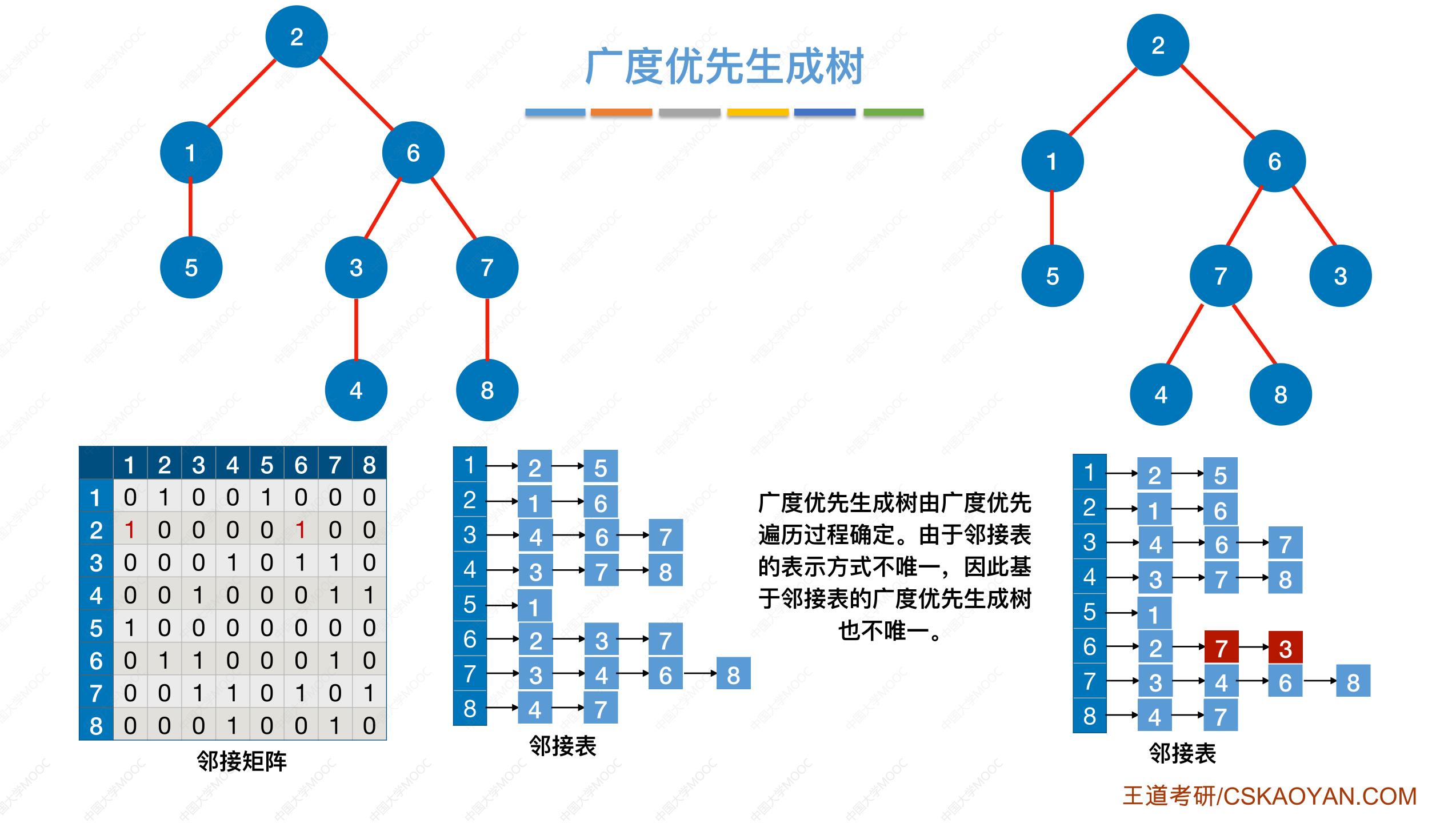




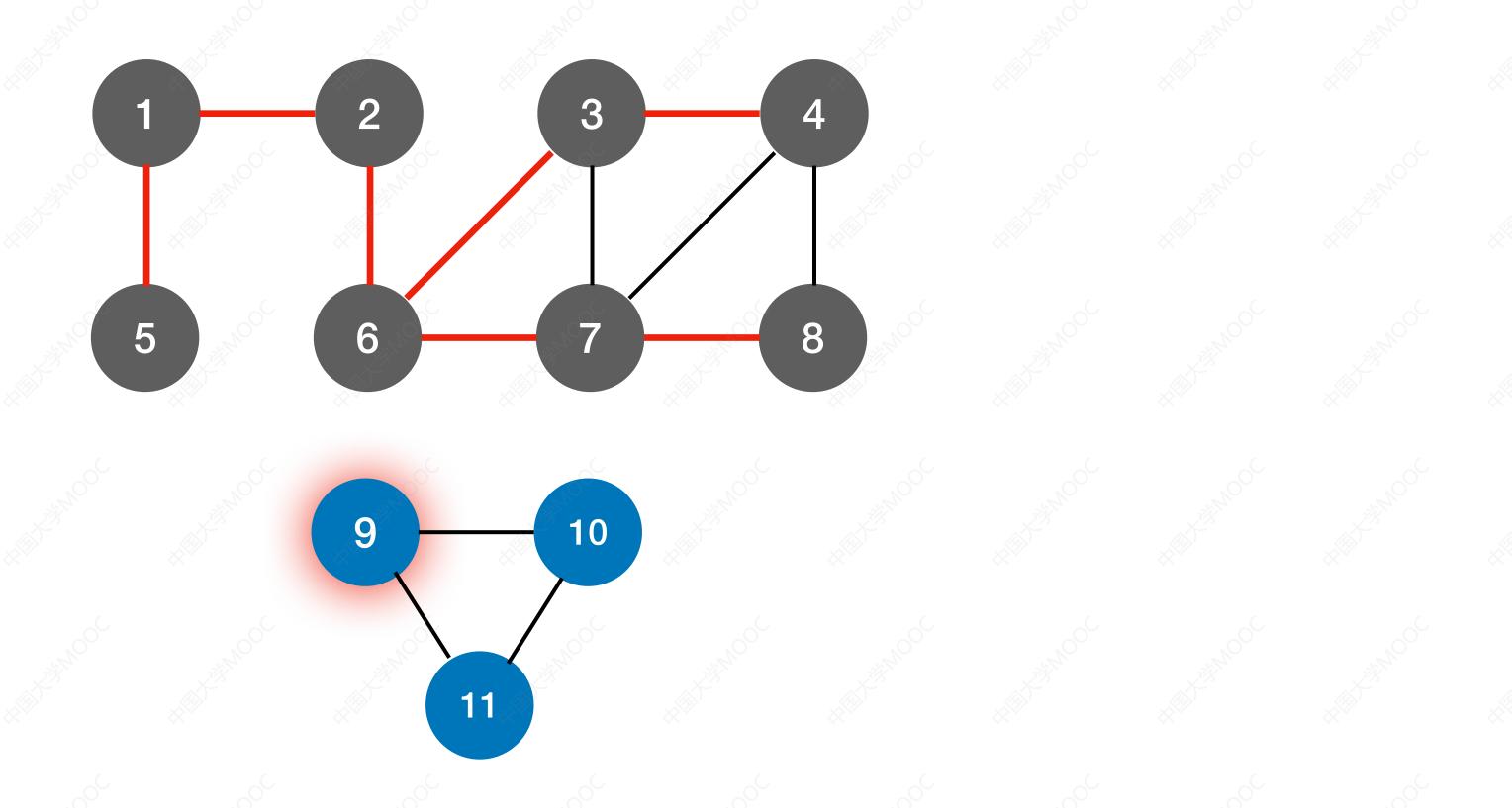






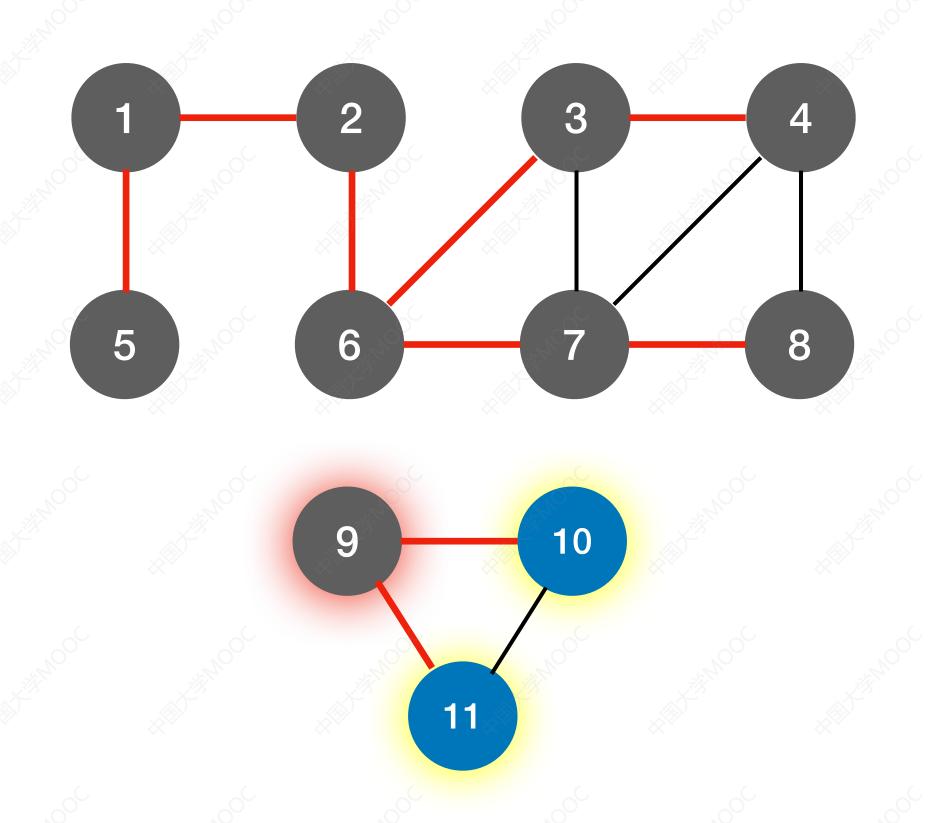


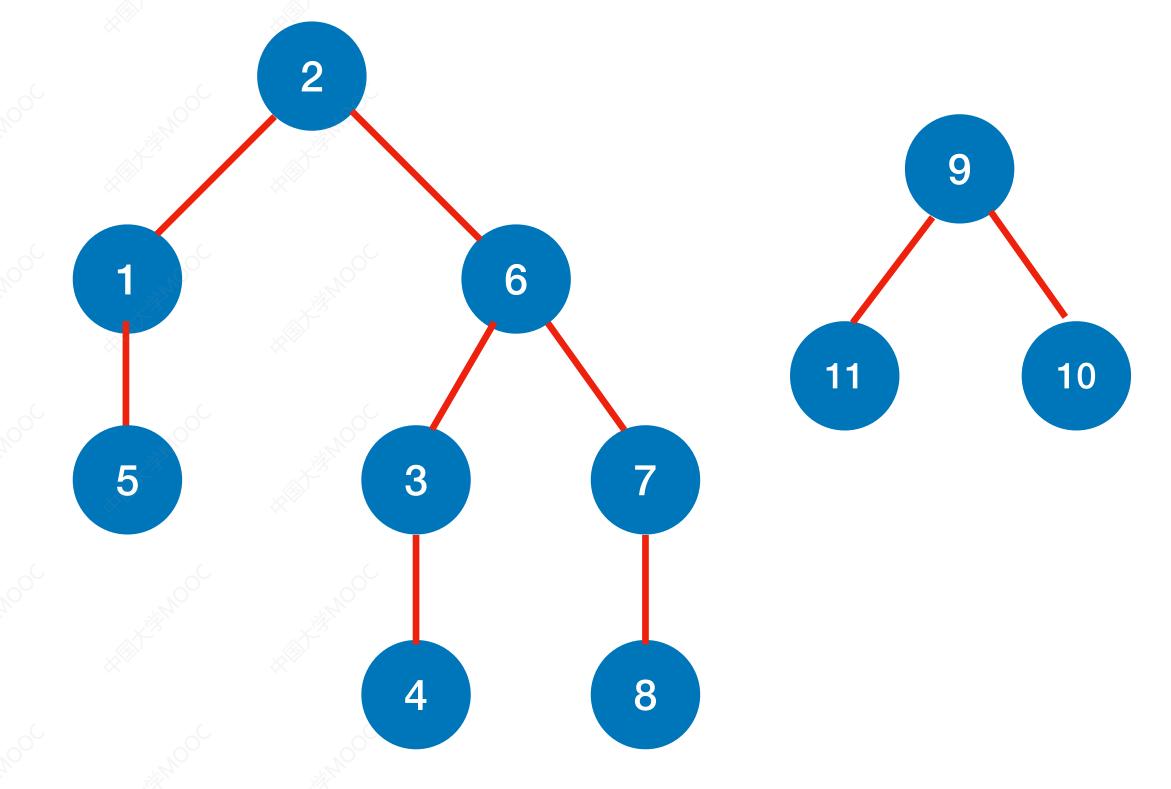
广度优先生成森林



对非连通图的广度优先遍历,可得到广度优先生成森林

广度优先生成森林



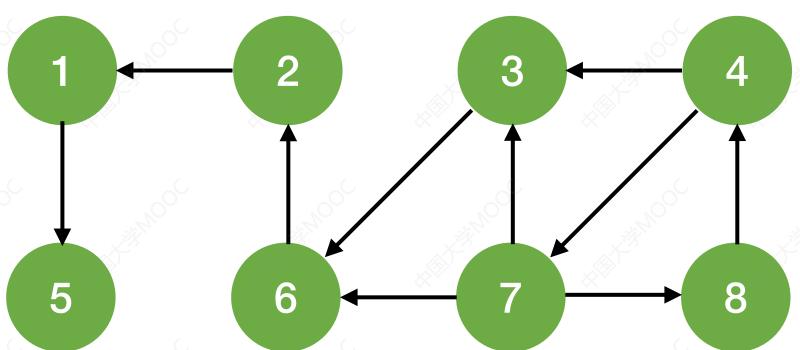


对非连通图的广度优先遍历,可得到广度优先生成森林

练习:有向图的BFS过程

思考:

- 1. 从1出发,需要调用几次BFS函数?
- 2. 从7出发,需要调用几次BFS函数?



	1	2	3	4	5	6	7	8		
1	0	0	0	0	1	0	0	0		
2	1	0	0	0	0	0	0	0		
3	0	0	0	0	0	1	0	0		
4	0	0	1	0	0	0	1	0		
5	0	0	0	0	0	0	0	0		
6	0	91	0	0	0	0	0	0		
7	0	0	1.0	0	0	1	0	1		
8	0	0	0	1	0	0	0	0		
邻接矩阵										

```
//广度优先遍历
         void BFS(Graph G,int v){
                                 //从顶点v出发,广度优先遍历图G
            visit(v);
                                     //访问初始顶点v
             visited[v]=TRUE;
                                     //对v做已访问标记
             Enqueue(Q,v);
                                     //顶点v入队列Q
            while(!isEmpty(Q)){
                DeQueue(Q,v);
                                     //顶点v出队列
                for(w=FirstNeighbor(G,v);w>=0;w=NextNeighbor(G,v,w))
                   //检测v所有邻接点
                   if(!visited[w]){
                                    //w为v的尚未访问的邻接顶点
                       visit(w);
                                    //访问顶点w
                       visited[w]=TRUE;//对w做已访问标记
                       EnQueue(Q,w);
                                     //顶点w入队列
                   }//if
             }//while
邻接表
                                       王道考研/CSKAOYAN.COM
```

bool visited[MAX_VERTEX_NUM];

for(i=0;i<G.vexnum;++i)</pre>

for(i=0;i<G.vexnum;++i)</pre>

if(!visited[i])

BFS(G,i);

InitQueue(Q);

visited[i]=FALSE;

void BFSTraverse(Graph G){ //对图G进行广度优先遍历

//访问标记数组

//访问标记数组初始化

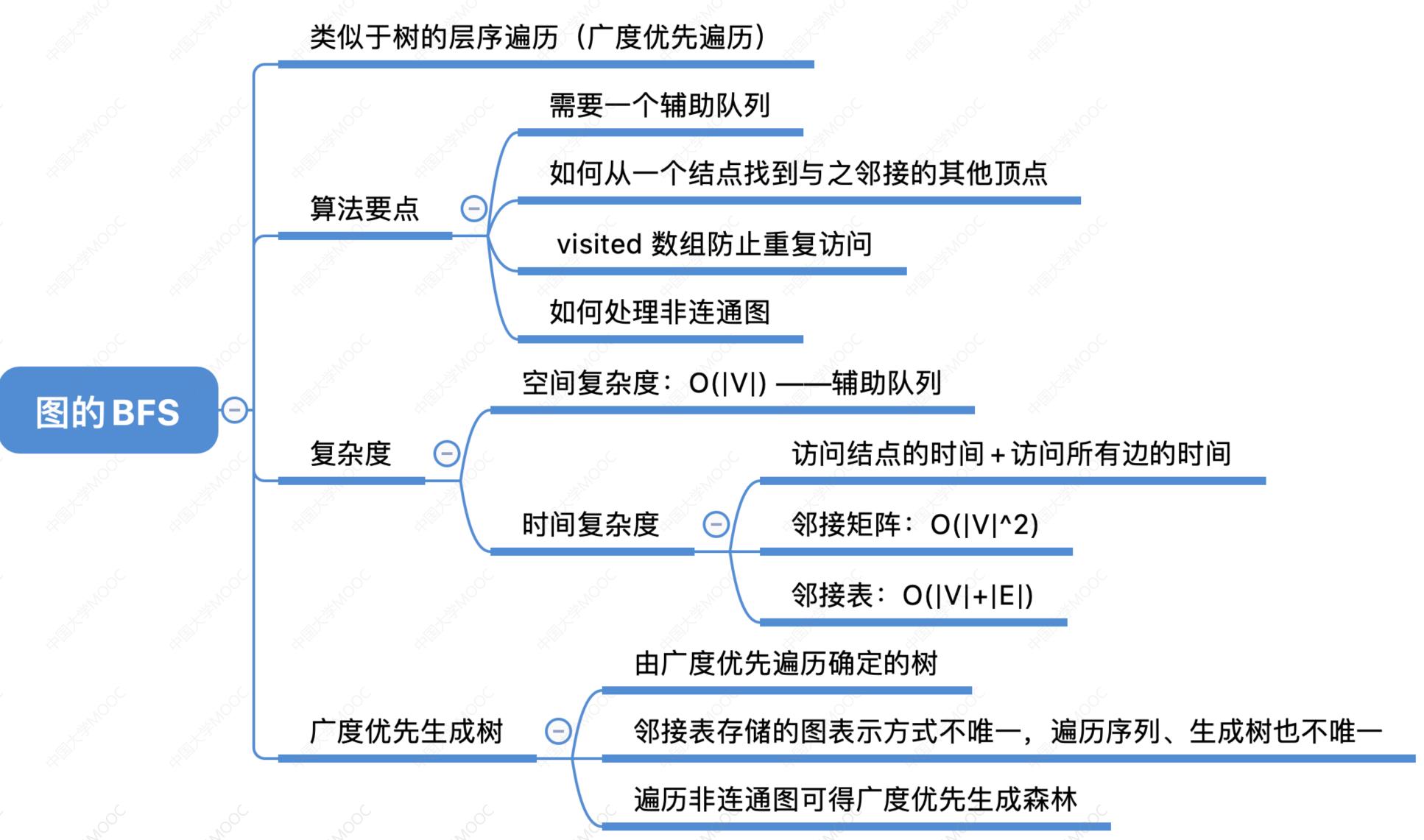
//从0号顶点开始遍历

//初始化辅助队列Q

//对每个连通分量调用一次BFS

//vi未访问过,从vi开始BFS

知识回顾与重要考点



欢迎大家对本节视频进行评价~



学员评分: 6.3.1 图的...





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b站: 王道计算机教育



抖音: 王道计算机考研