

## Lattice.query

### Find a path between two poses

**P.query(start, goal)** finds a path ( $N \times 3$ ) from pose **start** ( $1 \times 3$ ) to pose **goal** ( $1 \times 3$ ). The pose is expressed as [X,Y,THETA].

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## Link

### manipulator Link class

A Link object holds all information related to a robot joint and link such as kinematics parameters, rigid-body inertial parameters, motor and transmission parameters.

### Constructors

Link	general constructor
Prismatic	construct a prismatic joint+link using standard DH
PrismaticMDH	construct a prismatic joint+link using modified DH
Revolute	construct a revolute joint+link using standard DH
RevoluteMDH	construct a revolute joint+link using modified DH

### Information/display methods

display	print the link parameters in human readable form
dyn	display link dynamic parameters
type	joint type: 'R' or 'P'

### Conversion methods

char	convert to string
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### Operation methods

A	link transform matrix
friction	friction force
nofriction	Link object with friction parameters set to zero%

## Testing methods

islimit	test if joint exceeds soft limit
isrevolute	test if joint is revolute
isprismatic	test if joint is prismatic
issym	test if joint+link has symbolic parameters

## Overloaded operators

+ concatenate links, result is a SerialLink object

## Properties (read/write)

theta	kinematic: joint angle
d	kinematic: link offset
a	kinematic: link length
alpha	kinematic: link twist
jointtype	kinematic: 'R' if revolute, 'P' if prismatic
mdh	kinematic: 0 if standard D&H, else 1
offset	kinematic: joint variable offset
qlim	kinematic: joint variable limits [min max]
m	dynamic: link mass
r	dynamic: link COG wrt link coordinate frame $3 \times 1$
I	dynamic: link inertia matrix, symmetric $3 \times 3$ , about link COG.
B	dynamic: link viscous friction (motor referred)
Tc	dynamic: link Coulomb friction
G	actuator: gear ratio
Jm	actuator: motor inertia (motor referred)

## Examples

```
L = Link([0 1.2 0.3 pi/2]);
L = Link('revolute', 'd', 1.2, 'a', 0.3, 'alpha', pi/2);
L = Revolute('d', 1.2, 'a', 0.3, 'alpha', pi/2);
```

## Notes

- This is a reference class object.
- Link objects can be used in vectors and arrays.
- Convenience subclasses are Revolute, Prismatic, RevoluteMDH and PrismaticMDH.

## References

- Robotics, Vision & Control, P. Corke, Springer 2011, Chap 7.

## See also

[Link](#), [Revolute](#), [Prismatic](#), [SerialLink](#), [RevoluteMDH](#), [PrismaticMDH](#)

# Link.Link

## Create robot link object

This the class constructor which has several call signatures.

**L** = **Link**() is a **Link** object with default parameters.

**L** = **Link**(**lnk**) is a **Link** object that is a deep copy of the link object **lnk** and has type **Link**, even if **lnk** is a subclass.

**L** = **Link**(**options**) is a link object with the kinematic and dynamic parameters specified by the key/value pairs.

## Options

'theta', TH	joint angle, if not specified joint is revolute
'd', D	joint extension, if not specified joint is prismatic
'a', A	joint offset (default 0)
'alpha', A	joint twist (default 0)
'standard'	defined using standard D&H parameters (default).
'modified'	defined using modified D&H parameters.
'offset', O	joint variable offset (default 0)
'qlim', L	joint limit (default [])
'I', I	link inertia matrix ( $3 \times 1$ , $6 \times 1$ or $3 \times 3$ )
'r', R	link centre of gravity ( $3 \times 1$ )
'm', M	link mass ( $1 \times 1$ )
'G', G	motor gear ratio (default 1)
'B', B	joint friction, motor referenced (default 0)
'Jm', J	motor inertia, motor referenced (default 0)
'Tc', T	Coulomb friction, motor referenced ( $1 \times 1$ or $2 \times 1$ ), (default [0 0])
'revolute'	for a revolute joint (default)
'prismatic'	for a prismatic joint 'p'
'standard'	for standard D&H parameters (default).
'modified'	for modified D&H parameters.
'sym'	consider all parameter values as symbolic not numeric

## Notes

- It is an error to specify both ‘theta’ and ‘d’
- The joint variable, either theta or d, is provided as an argument to the A() method.
- The link inertia matrix ( $3 \times 3$ ) is symmetric and can be specified by giving a  $3 \times 3$  matrix, the diagonal elements [Ixx Iyy Izz], or the moments and products of inertia [Ixx Iyy Izz Ixy Iyz Ixz].
- All friction quantities are referenced to the motor not the load.
- Gear ratio is used only to convert motor referenced quantities such as friction and inertia to the link frame.

## Old syntax

**L** = **Link**(**dh**, **options**) is a link object using the specified kinematic convention and with parameters:

- **dh** = [THETA D A ALPHA SIGMA OFFSET] where SIGMA=0 for a revolute and 1 for a prismatic joint; and OFFSET is a constant displacement between the user joint variable and the value used by the kinematic model.
- **dh** = [THETA D A ALPHA SIGMA] where OFFSET is zero.
- **dh** = [THETA D A ALPHA], joint is assumed revolute and OFFSET is zero.

## Options

‘standard’	for standard D&H parameters (default).
‘modified’	for modified D&H parameters.
‘revolute’	for a revolute joint, can be abbreviated to ‘r’ (default)
‘prismatic’	for a prismatic joint, can be abbreviated to ‘p’

## Notes

- The parameter D is unused in a revolute joint, it is simply a placeholder in the vector and the value given is ignored.
- The parameter THETA is unused in a prismatic joint, it is simply a placeholder in the vector and the value given is ignored.

## Examples

A standard Denavit-Hartenberg link

```
L3 = Link('d', 0.15005, 'a', 0.0203, 'alpha', -pi/2);
```

since ‘theta’ is not specified the joint is assumed to be revolute, and since the kinematic convention is not specified it is assumed ‘standard’.

Using the old syntax

```
L3 = Link([ 0, 0.15005, 0.0203, -pi/2], 'standard');
```

the flag 'standard' is not strictly necessary but adds clarity. Only 4 parameters are specified so sigma is assumed to be zero, ie. the joint is revolute.

```
L3 = Link([ 0, 0.15005, 0.0203, -pi/2, 0], 'standard');
```

the flag 'standard' is not strictly necessary but adds clarity. 5 parameters are specified and sigma is set to zero, ie. the joint is revolute.

```
L3 = Link([ 0, 0.15005, 0.0203, -pi/2, 1], 'standard');
```

the flag 'standard' is not strictly necessary but adds clarity. 5 parameters are specified and sigma is set to one, ie. the joint is prismatic.

For a modified Denavit-Hartenberg revolute joint

```
L3 = Link([ 0, 0.15005, 0.0203, -pi/2, 0], 'modified');
```

## Notes

- Link object is a reference object, a subclass of Handle object.
- Link objects can be used in vectors and arrays.
- The joint offset is a constant added to the joint angle variable before forward kinematics and subtracted after inverse kinematics. It is useful if you want the robot to adopt a 'sensible' pose for zero joint angle configuration.
- The link dynamic (inertial and motor) parameters are all set to zero. These must be set by explicitly assigning the object properties: m, r, I, Jm, B, Tc.
- The gear ratio is set to 1 by default, meaning that motor friction and inertia will be considered if they are non-zero.

## See also

[Revolute](#), [Prismatic](#), [RevoluteMDH](#), [PrismaticMDH](#)

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# Link.A

## Link transform matrix

$T = L.A(q)$  is an SE3 object representing the transformation between link frames when the link variable  $q$  which is either the Denavit-Hartenberg parameter THETA (revolute) or D (prismatic). For:

- standard DH parameters, this is from the previous frame to the current.
- modified DH parameters, this is from the current frame to the next.

## Notes

- For a revolute joint the THETA parameter of the link is ignored, and **q** used instead.
- For a prismatic joint the D parameter of the link is ignored, and **q** used instead.
- The link offset parameter is added to **q** before computation of the transformation matrix.

## See also

[SerialLink.fkine](#)

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# Link.char

## Convert to string

**s** = **L.char()** is a string showing link parameters in a compact single line format. If **L** is a vector of **Link** objects return a string with one line per **Link**.

## See also

[Link.display](#)

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# Link.display

## Display parameters

**L.display()** displays the link parameters in compact single line format. If **L** is a vector of **Link** objects displays one line per element.

## Notes

- This method is invoked implicitly at the command line when the result of an expression is a Link object and the command has no trailing semicolon.

## See also

[Link.char](#), [Link.dyn](#), [SerialLink.showlink](#)

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## Link.dyn

### Show inertial properties of link

`L.dyn()` displays the inertial properties of the link object in a multi-line format. The properties shown are mass, centre of mass, inertia, friction, gear ratio and motor properties.

If `L` is a vector of **Link** objects show properties for each link.

### See also

[SerialLink.dyn](#)

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## Link.friction

### Joint friction force

$\mathbf{f} = \mathbf{L}.\text{friction}(\mathbf{q}\dot{\mathbf{d}})$  is the joint **friction** force/torque ( $1 \times N$ ) for joint velocity  $\mathbf{q}\dot{\mathbf{d}}$  ( $1 \times N$ ). The **friction** model includes:

- Viscous **friction** which is a linear function of velocity.
- Coulomb **friction** which is proportional to  $\text{sign}(\mathbf{q}\dot{\mathbf{d}})$ .

### Notes

- The **friction** value should be added to the motor output torque, it has a negative value when  $\mathbf{q}\dot{\mathbf{d}} > 0$ .
- The returned **friction** value is referred to the output of the gearbox.
- The **friction** parameters in the Link object are referred to the motor.
- Motor viscous **friction** is scaled up by  $G^2$ .
- Motor Coulomb **friction** is scaled up by  $G$ .
- The appropriate Coulomb **friction** value to use in the non-symmetric case depends on the sign of the joint velocity, not the motor velocity.
- The absolute value of the gear ratio is used. Negative gear ratios are tricky: the Puma560 has negative gear ratio for joints 1 and 3.

### See also

[Link.nofriction](#)

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## Link.horzcat

### Concatenate link objects

[L1 L2] is a vector that contains deep copies of the **Link** class objects L1 and L2.

### Notes

- The elements of the vector are all of type Link.
- If the elements were of a subclass type they are converted to type Link.
- Extends to arbitrary number of objects in list.

### See also

[Link.plus](#)

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## Link.islimit

### Test joint limits

L.**islimit**(q) is true (1) if q is outside the soft limits set for this joint.

### Note

- The limits are not currently used by any Toolbox functions.
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## Link.isprismatic

### Test if joint is prismatic

L.**isprismatic**() is true (1) if joint is prismatic.

### See also

[Link.isrevolute](#)

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## Link.isrevolute

### Test if joint is revolute

`L.isrevolute()` is true (1) if joint is revolute.

### See also

[Link.isprismatic](#)

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## Link.issym

### Check if link is a symbolic model

`res = L.issym()` is true if the **Link** `L` has any symbolic parameters.

### See also

[Link.sym](#)

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## Link.nofriction

### Remove friction

`ln = L.nofriction()` is a link object with the same parameters as `L` except nonlinear (Coulomb) friction parameter is zero.

`ln = L.nofriction('all')` as above except that viscous and Coulomb friction are set to zero.

`ln = L.nofriction('coulomb')` as above except that Coulomb friction is set to zero.

`ln = L.nofriction('viscous')` as above except that viscous friction is set to zero.

### Notes

- Forward dynamic simulation can be very slow with finite Coulomb friction.

### See also

[Link.friction](#), [SerialLink.nofriction](#), [SerialLink.fdyn](#)

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## Link.plus

### Concatenate link objects into a robot

$L1+L2$  is a `SerialLink` object formed from deep copies of the **Link** class objects  $L1$  and  $L2$ .

### Notes

- The elements can belong to any of the Link subclasses.
- Extends to arbitrary number of objects, eg.  $L1+L2+L3+L4$ .

### See also

[SerialLink](#), [SerialLink.plus](#), [Link.horzcat](#)

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## Link.set.I

### Set link inertia

$L.I = [I_{xx} \ I_{yy} \ I_{zz}]$  sets link inertia to a diagonal matrix.

$L.I = [I_{xx} \ I_{yy} \ I_{zz} \ I_{xy} \ I_{yz} \ I_{xz}]$  sets link inertia to a symmetric matrix with specified inertia and product of inertia elements.

$L.I = M$  set **Link** inertia matrix to  $M$  ( $3 \times 3$ ) which must be symmetric.

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## Link.set.r

### Set centre of gravity

$L.r = R$  sets the link centre of gravity (COG) to  $R$  (3-vector).

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## Link.set.Tc

### Set Coulomb friction

$L.Tc = F$  sets Coulomb friction parameters to  $[F \ -F]$ , for a symmetric Coulomb friction model.

`L.Tc = [FP FM]` sets Coulomb friction to `[FP FM]`, for an asymmetric Coulomb friction model. `FP > 0` and `FM < 0`. `FP` is applied for a positive joint velocity and `FM` for a negative joint velocity.

## Notes

- The friction parameters are defined as being positive for a positive joint velocity, the friction force computed by `Link.friction` uses the negative of the friction parameter, that is, the force opposing motion of the joint.

## See also

[Link.friction](#)

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# Link.sym

## Convert link parameters to symbolic type

`LS = L.sym` is a **Link** object in which all the parameters are symbolic ('sym') type.

## See also

[Link.issym](#)

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# Link.type

## Joint type

`c = L.type()` is a character 'R' or 'P' depending on whether joint is revolute or prismatic respectively. If `L` is a vector of **Link** objects return an array of characters in joint order.

## See also

[SerialLink.config](#)

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