A Living Review of Quantum Computing for Plasma Physics

Abstract

Quantum Computing promises accelerated simulation of certain classes of problems, in particular in plasma physics. The goal of this document is to provide a comprehensive list of citations for those developing and applying these approaches to experimental or theoretical analyses. As a living document, it will be updated as often as possible to incorporate the latest developments. Suggestions are most welcome.

The purpose of this note is to collect references for quantum algorithms already relevant to plasma physics. A minimal number of categories is chosen in order to be as useful as possible. Note that papers may be referenced in more than one category.

To facilitate search, if clearly appropriate, the following tags are applied

- NISQ noisy-intermediate scale quantum computing
- FTol fault-tolerant quantum computing
- QAnn quantum annealing
- QIns quantum-inspired

Color-filled tags indicate the type of content. Since most papers contain some form of theoretical analysis, we use the following tags

- Theo theoretical tag solely for the papers with analytical results, and no considerable numerical or experimental results
- Num marks papers with numerical simulations, but no experimental results run on quantum devices
- Exp marks papers with displayed experimental results.

We may omit tags if the paper is referenced and tagged in a subsequent subsection, or the paper is an overview of some topic, and covers many different approaches.

The fact that a paper is listed in this document does not endorse or validate its content - that is for the community (and for peer-review) to decide. Furthermore, the classification here is a best attempt and may have flaws - please let us know if (a) we have missed a paper you think should be included, (b) a paper has been misclassified or wrongly tagged, or (c) a citation for a paper is not correct or if the journal information is now available.

In order to be as useful as possible, this document will continue to evolve so please check back before you write your next paper. You can simply download the .bib file to get all of the latest references. Please consider citing Ref. [AC23] when referring to this living review.

• Modern Reviews

Below are links to (static) general and specialized reviews.

- Applications of Quantum Computing to Plasma Simulations [DS21a].
- Quantum Computing for Fusion Energy Science Applications [Jos+23].
- System of linear equations NISQ Num [HBR21] Exp[Bra+20; Xu+21], FTol Theo [HHL09; CJS13; CKS17; WX22], QAnn Num [SSO19], Exp [BL22], QIns Theo [SM21].

Many problems in plasma physics may be formulated, either exactly or approximately, as a problem of the form Ax = b, where A and b encode the information about the system (including its initial conditions, if applicable), and the goal is to compute x, which encodes the desired data.

- System of nonlinear equations FTol Theo [DS21b] Num [XWG21; Xue+22]. Nonlinear equations depend nonlinearly on x, and they are generally much harder to solve. As quantum mechanics is inherently linear, many techniques rely on mapping the original nonlinear problem to a (usually approximate) linear one, that is easier to solve.
 - System of polynomial equations QAnn Exp [Cha+19]. System where each equation is a polynomial.
- Ordinary differential equations (ODEs) QAnn Exp [Zan+21].

 Many plasma systems can be described by ordinary differential equations. Some techniques attempt to solve them directly, while others map the ODE to (larger) systems of linear equations, and solve those.
 - Linear FTol Theo [Ber14; Ber+17; CL20; FLT22; JLY22a], Num [JLY22b], QAnn Exp [Zan+21].

As quantum mechanics is inherently linear, linear ODEs are often more straightforward to solve with quantum computers than nonlinear ones.

- * Second-order QAnn Exp [SS19].

 The highest derivative appearing in these ODEs is the second derivative.
 - Quantum harmonic oscillator FTo1 Num [Ric+22]. Here, the time-independent Schrödinger equation has a Hamiltonian with a potential proportional to x^2 .
 - · Laguerre QAnn Num [CS22].

 The Laquerre equation is of the form

$$x\frac{\mathrm{d}^2 y}{\mathrm{d}x^2} + (1-x)\frac{\mathrm{d}y}{\mathrm{d}x} + n \ y = 0$$

- Nonlinear $\overline{\tt NISQ}$ [KPE21; Shi+21] $\overline{\tt FTol}$ (Theo [LO08; DS21b; Llo+20] Num [JLY22b; Liu+21b; SGS22; SGS24], $\overline{\tt QAnn}$ Num [Zan+21].

There is no general reliable procedure to solve nonlinear ODEs, but some methods have been proposed.

• Partial differential equations (PDEs) NISQ [GRG22], FTol Theo [CLO21; Kro22], QIns [Gar21].

In general, plasma systems are described by partial differential equations. Although some of the equations presented here do not commonly describe plasma systems, the techniques employed to solve them are often general enough that they could be adapted to tackle plasma PDEs.

For ease of search, PDEs arising from stochastic processes are indicated both here and in the following section.

- Linear NISQ [OMa+22], FTol Theo [JLY22a], Num [JLY22b], QAnn Num [CS22].
 - * Non-homogeneous NISQ Exp [Bra+20], FTol Theo [Arr+19; Ric+22].

The Vlasov equation models the evolution of the distribution functions of (charged) particles in a plasma system, including their long-range Coulomb interactions. It can be written in the general form

$$\frac{\partial}{\partial t}f(x,p,t) + \frac{dr}{dt}\frac{\partial}{\partial r}f + \frac{dp}{dt}\frac{\partial}{\partial p}f = C$$

where C is a collision term. The dp/dt term can be coupled the (Electromagnetic) fields either through to the Poisson or the set of Maxwell's equations.

· Poisson NISQ [Bra+20; Sat+21; AK22; Sah+22; Lub+20], Exp [Cui+22], FTol Theo [Cao+13], Num [Arr+19; Ric+22; Liu+21a; Wan+20].

The Poisson equation is an elliptic PDE that relates a charge/mass density or velocity field with the electrical/gravitational potential or pressure field it originates, respectively. It takes the form

$$\nabla^2 \phi(x, y, z) = f(x, y, z)$$

This equation has significant applications in fluid dynamics (see Navier-Stokes equations).

- * Semi-classical Schrödinger FTol Num [JLL22]. The semi-classical regime of the Schrödinger equation corresponds to the case when $\hbar \ll 1$. Possible applications include: quantum chemistry, including Born-Oppenheimer molecular dynamics and Ehrenfest dynamics.
- * Time-dependent Schrödinger NISQ Num [Jou22; Oll+23] FTol Num [JLL22] QIns Num [LMJ18]
- * 3-wave mixing FTol Exp [Shi+21; Shi+24] FTol Num [MQ23; MQ24]

* SFQED Hamiltonian FTol Exp [HD24]

Many problems can be mapped to the Schrödinger equation

$$i\hbar \frac{\mathrm{d}}{\mathrm{d}t} |\psi(t)\rangle = H |\psi(t)\rangle$$

described by some Hamiltonian H. Solving the Schrödinger equation can often be done much more efficiently with quantum computers.

- * Parabolic QIns Num [Pat+22].
 - · Heat/Convection NISQ [LEK22; Alb+22], Num [Liu+22], FTol Theo [LMS22; JLY22a; JLY22d] Num [JLY22b].

The prototypical parabolic linear PDE. This equation describes the diffusion of heat in a material

$$\partial_t u(t,x) = \alpha \Delta u$$

where α is the thermal diffusivity. Its applications are of fundamental importance in most branches of physics and engineering.

Black-Scholes NISQ [FJO21; MK22], FTol Num [JLY22b; An+21]. The Black-Scholes equation is a PDE which describes the price of the option V(S,t) over time t and price of underlying asset S(t), r is the "force of interest", μ is the annualized drift rate of S, and σ is the standard deviation of the stock's returns.

$$\frac{\partial V}{\partial t} + \frac{1}{2}\sigma^2 S^2 \frac{\partial^2 V}{\partial S^2} + rS \frac{\partial V}{\partial S} - rV = 0$$

· Fokker-Planck FTol Num [JLY22b], QIns Num [Gar21].

The Fokker-Planck equation for the probability density p(x,t) can be written as

$$\frac{\partial}{\partial t}p(x,t) = -\frac{\partial}{\partial x}\left(\mu(x,t)\ p(x,t)\right) + \frac{\partial^2}{\partial x^2}\left(D(x,t)\ p(x,t)\right)$$

where μ and D are the drift and diffusion coefficients (which may be time-dependent).

- · Hamilton-Jacobi-Bellman QIns Num [Pat+22].
- * Hyperbolic/Wave-related FTol Theo [JLY22d; JL22].
 - Wave FTol Num [CJO19; SSC21], QAnn Num [CS22].

 The prototypical hyperbolic equation in physics, it describes oscillatory and propagating perturbations in a medium

$$\partial_{tt}u(t,x) = c^2 \nabla^2 u$$

· Maxwell's FTol Theo [CJO19], Num [NSD22; NDS22].

The Maxwell equations are a set of coupled PDEs that are foundational to the modeling of electromagnetic phenomena, which important applications in fundamental physics, classical optics and electric circuits.

$$\nabla \cdot \mathbf{E} = \frac{\rho}{\varepsilon_0}, \nabla \cdot \mathbf{B} = 0, \nabla \times \mathbf{E} = -\frac{\partial \mathbf{B}}{\partial t}, \nabla \times \mathbf{B} = \mu_0 \left(\mathbf{J} + \varepsilon_0 \frac{\partial \mathbf{E}}{\partial t} \right)$$

· Klein-Gordon FTol Theo [CJO19].

The Klein-Gordon relativistic wave equation is a 2nd order equation both in space and time

$$\left(\frac{1}{c^2}\frac{\partial^2}{\partial t^2} - \nabla^2 + \frac{m^2c^2}{\hbar^2}\right)\psi(t, \mathbf{x}) = 0$$

· Helmholtz NISQ Num [Ewe+22].

The Helmholtz equation is the eigenvalue problem for the Laplace operator

$$\nabla^2 f = -k^2 f$$

Important applications include wave-like phenomena and diffusion processes.

- Nonlinear FTol Theo [JL22; Lin+22].
 - * Evolution equation $\overline{\text{NISQ}}$ Theo [LEK22]. General class of PDEs with time-domain.
 - * Vlasov-Poisson QIns Num [YL22].

 The coupled Vlasov-Poisson system describes the self-consistent evolution of charges and their (electrical) potentials. Because of this, the system is nonlinear.
 - * Schrödinger-Poisson NISQ Num [MS21].

 Similar to the Vlasov-Poisson system, the Schrödinger-Poisson equation attempts to describe the self-consistent evolution of a wave-function and a potential.
 - * Nonlinear-Schrödinger NISQ Num [GRG22], Exp [Lub+20]. Similar to the Schrödinger-Poisson system, however the potential is created by the square absolute value of the wave-function $V = |\psi|^2$, which induces a cubic nonlinearity in the equations.
 - * Burger's NISQ Exp [Zyl+22], FTol Num [Oz+21].

 This nonlinear PDE with a quadratic nonlinearity is of fundamental importance to fluid dynamics and in particular in plasma physics. It is also a prototypical equation in turbulence related studies, and can be written in the form

$$\frac{\partial}{\partial t}u(x,t) + u\frac{\partial u}{\partial x} = \nu \frac{\partial^2 u}{\partial x^2}$$

* Reaction-diffusion NISQ Num [LEK22] NISQ Exp [Dem+22], FTol Num [An+22]. Reaction-diffusion equations describe transport/diffusion of substances and their transformation into other substances, for example to model the concentration of chemical components.

$$\partial_t p = D\nabla^2 q + R(q)$$

where D is the diffusion coefficient and R is the local reaction rate.

* Navier-Stokes FTol Num [Gai20].

The Navier-Stokes equations describe the motion of viscous fluids. They describe conservation of mass and momentum and often require equations of state for pressure, temperature and density to close the system of equations.

$$\partial_t \rho(x,t) + \nabla \cdot (\rho u) = 0, \frac{\partial}{\partial t} (\rho \mathbf{u}) + \nabla \cdot (\rho \mathbf{u} \otimes \mathbf{u}) = -\nabla p + \mu \nabla^2 \mathbf{u} + \frac{1}{3} \mu \nabla (\nabla \cdot \mathbf{u}) + \rho \mathbf{g}$$

· Incompressible NISQ [LEK22], QIns (Num) [Lap22].

The incompressible Navier-Stokes equations can be applied for low enough Mach numbers, and cannot be used to accurately simulate density or pressure waves like sound or shock waves. The fluid density is considered constant $\rho = \rho_0$.

* Hamilton-Jacobi FTol Theo [JLY22c; JL22].

A particular case of the Hamilton-Jacobi-Bellman. The Hamilton-Jacobi is an alternative formulation of classical mechanics, where given a Hamiltonian H(q, p, t) of a mechanical system, the Hamilton-Jacobi equation is a first-order, non-linear PDE for the Hamilton's principal function S. One of its advantages is in efficiently identifying conserved quantities of mechanical systems.

* Black-Scholes-Barenblatt QIns Num [Pat+22].

The Black-Scholes-Barenblatt equation is a nonlinear extension to the Black-Scholes equation, which models uncertain volatility and interest rates derived from the Black-Scholes equation.

- * Stefan problems FTol Theo [Sar22].

 Stefan problems are a particular kind of boundary value problems for a system of PDEs in which the boundary between the phases can move with time.
- Stochastic/diffusive processes $\overline{\mathtt{NISQ}}$ Num $[\mathrm{Kub}+20;\ \mathrm{Alg}+22],$ $\overline{\mathtt{FTol}}$ Num $[\mathrm{An}+21].$

(Integro-)differential equations in which one or more of the terms is a stochastic process, leading to a solution which is stochastic in nature. Stochastic Differential Equations (SDEs) can be used to model physical systems subject to thermal fluctuations.

Through the Feynman-Kac formula, many common SDEs can be reduced to solving a PDE for the probability density of interest, as is the case for the Fokker-Planck equation.

For ease of search, PDEs arising from stochastic processes are indicated both here and in the previous section.

- Fokker-Planck FTol Num [JLY22b], QIns Num [Gar21].

The Fokker-Planck equation for the probability density p(x,t) can be written as

$$\frac{\partial}{\partial t}p(x,t) = -\frac{\partial}{\partial x}\left(\mu(x,t)\ p(x,t)\right) + \frac{\partial^2}{\partial x^2}\left(D(x,t)\ p(x,t)\right)$$

where μ and D are the drift and diffusion coefficients (which may be time-dependent).

- Linear Boltzmann/Rate equation FTol Num [JLY22b; IKK24].

The linear Boltzmann or Rate equation is a stochastic integro-differential equation for the probability density p(x,t) can be written as

$$\frac{d}{dt}p(x,t) = \int p(x',t)W(x,x')dx' - p(x,t)\int W(x',x)dx'$$

where W(x, x') is the probability rate of transition from state x' to state x. where dp/dt can include partial derivatives of p(x, t).

• Other techniques

- Linear embedding of nonlinear dynamical systems FTol Theo [ESP21; JLY22c] Num [Liu+21b].

Several linear embedding of nonlinear dynamical systems have been developed to extend the class of problems that can be tackled by quantum computers. These include Koopman-von Neumann formulation, Quantum nonlinear Schrödinger linearization formulation and Carleman linearization, amongst others.

- Koopman-von Neumann formulation FTol Theo [Jos20; JLY22c; TF23], Num [Lin+22].

Koopman-von Neumann mechanics is a description of classical mechanics embedded in a Hilbert space. The dynamical equation can be written as $i\partial_t \psi = \mathcal{H}_{KvN} \psi$, where the operator $\mathcal{H}_{KvN} = -i\sum_j \left(F_j \frac{\partial}{\partial x_j} + \frac{1}{2} \frac{\partial F_j}{\partial x_j}\right)$. Furthermore, the probability density is interpreted as $\rho = |\psi|^2$. Applications may include the Vlasov-Maxwell coupled system of equations.

- Quantum nonlinear Schrödinger linearization formulation FTol Theo [Llo+20]. Formulation of ODEs/PDEs of the type dx/dt+f(x)x=b(t), with $f=x^{\dagger\otimes m}Fx^{\otimes m}$, as nonlinear Schrödinger equations. Potential applications of the method may include the Navier-Stokes equation, plasma hydrodynamics, epidemiology.
- Madelung transform for nonlinear relativistic fluids Num [Hat+19], NISQ Exp [Zyl+22].

The Madelung equations are an alternative formulation to the Schrödinger equation, written in terms of hydrodynamical variables, with the addition of the Bohm quantum potential Q

$$\partial_t \rho_m + \nabla \cdot (\rho_m \mathbf{u}) = 0, \ \frac{d\mathbf{u}}{dt} = \partial_t \mathbf{u} + \mathbf{u} \cdot \nabla \mathbf{u} = -\frac{1}{m} \nabla (Q + V)$$

Applications include modeling of shocks in plasmas.

- Finite element method FTol Theo [MP16].

This approach relies on dividing a system/domain into smaller regions called finite elements. The discretization process applied to a boundary value problem leads

to a system of algebraic equations, which can be less computationally expensive to resolve than the original PDE. Important applications include fluid flow, heat transfer, and electromagnetic potentials.

- Lattice Boltzmann algorithms Ftol Num [Lju22].
 - Originally developed as a classical algorithm, this approach can be used to simulate fluid dynamics without having to solve the Navier-Stokes equations directly. The fluid density is represented on a lattice and evolves in time with streaming and collision processes. One of the advantages of the method is its efficiency/scalability in parallel architectures.
- Quantum lattice algorithms (QLA) QIns Num [And+22; Kou+22; Oga+18; Ram+21; Vah+20a; Vah+20b; Vah+21a; Vah+21b; Vah+22; VSV20; VVS20; Vah+21c; Vah+20c; Vah+19; Yep02; Yep05; Yep16; VYV03; Vah+11; Vah+10; Oga+16a; Oga+16b; Oga+15; Shi+18; Kou+23].

 Highly parallelizable approach amenable to classical supercomputers, allowing the study of (Klein-Gordon-)Maxwell's equations, the Gross-Pitaevski equation, the nonlinear Schrödinger equation, and the KdV equation. In some cases, the method may also be suitable for fault-tolerant quantum computers.

References

- [AC23] Óscar Amaro and Diogo Cruz. A Living Review of Quantum Computing for Plasma Physics. 2023. DOI: 10.48550/ARXIV.2302.00001. URL: https://arxiv.org/abs/2302.00001.
- [AK22] Mazen Ali and Matthias Kabel. A Performance Study of Variational Quantum Algorithms for Solving the Poisson Equation on a Quantum Computer. Nov. 2022. DOI: 10.48550/arXiv.2211.14064. arXiv: 2211.14064 [quant-ph]. (Visited on 12/08/2022).
- [Alb+22] Anton Simen Albino et al. Solving Partial Differential Equations on Near-Term Quantum Computers. Aug. 2022. DOI: 10.48550/arXiv.2208. 05805. arXiv: 2208.05805 [physics, physics:quant-ph]. (Visited on 09/14/2022).
- [Alg+22] Hedayat Alghassi et al. "A Variational Quantum Algorithm for the Feynman-Kac Formula". In: *Quantum* 6 (June 2022), p. 730. DOI: 10.22331/q-2022-06-07-730. (Visited on 01/19/2023).
- [Ame+23] Abtin Ameri et al. "Quantum Algorithm for the Linear Vlasov Equation with Collisions". In: *Physical Review A* 107.6 (June 2023), p. 062412. ISSN: 2469-9926, 2469-9934. DOI: 10.1103/PhysRevA.107.062412. (Visited on 01/20/2024).
- [An+21] Dong An et al. "Quantum-Accelerated Multilevel Monte Carlo Methods for Stochastic Differential Equations in Mathematical Finance". In: *Quantum* 5 (June 2021), p. 481. ISSN: 2521-327X. DOI: 10.22331/q-2021-06-24-481. (Visited on 01/19/2023).
- [An+22] Dong An et al. "Efficient Quantum Algorithm for Nonlinear Reaction-Diffusion Equations and Energy Estimation". In: (2022). DOI: 10.48550/ ARXIV.2205.01141. (Visited on 01/12/2023).
- [And+22] Paul Anderson et al. Some Comments on Unitary Qubit Lattice Algorithms for Classical Problems. Nov. 2022. arXiv: 2211.16661 [physics, physics:quant-ph]. (Visited on 12/08/2022).
- [Arr+19] Juan Miguel Arrazola et al. "Quantum Algorithm for Nonhomogeneous Linear Partial Differential Equations". In: *Physical Review A* 100.3 (Sept. 2019), p. 032306. ISSN: 2469-9926, 2469-9934. DOI: 10.1103/PhysRevA. 100.032306. (Visited on 09/23/2022).
- [Ber+17] Dominic W. Berry et al. "Quantum Algorithm for Linear Differential Equations with Exponentially Improved Dependence on Precision". In: Communications in Mathematical Physics 356.3 (Dec. 2017), pp. 1057–1081. ISSN: 0010-3616, 1432-0916. DOI: 10.1007/s00220-017-3002-y. (Visited on 01/12/2023).

- [Ber14] Dominic W Berry. "High-Order Quantum Algorithm for Solving Linear Differential Equations". In: *Journal of Physics A: Mathematical and Theoretical* 47.10 (Mar. 2014), p. 105301. ISSN: 1751-8113, 1751-8121. DOI: 10.1088/1751-8113/47/10/105301. (Visited on 01/12/2023).
- [BL22] Ajinkya Borle and Samuel J. Lomonaco. How Viable Is Quantum Annealing for Solving Linear Algebra Problems? June 2022. DOI: 10.48550/arXiv.2206.10576. arXiv: 2206.10576 [quant-ph]. (Visited on 09/26/2022).
- [Bra+20] Carlos Bravo-Prieto et al. Variational Quantum Linear Solver. June 2020. arXiv: 1909.05820 [quant-ph]. (Visited on 09/23/2022).
- [Cao+13] Yudong Cao et al. "Quantum Algorithm and Circuit Design Solving the Poisson Equation". In: New Journal of Physics 15.1 (Jan. 2013), p. 013021. ISSN: 1367-2630. DOI: 10.1088/1367-2630/15/1/013021. (Visited on 09/23/2022).
- [Cap+23] Luca Cappelli et al. From Vlasov-Poisson to Schr\"odinger-Poisson: Dark Matter Simulation with a Quantum Variational Time Evolution Algorithm.

 July 2023. DOI: 10.48550/arXiv.2307.06032. arXiv: 2307.06032
 [astro-ph, physics:quant-ph]. (Visited on 07/15/2023).
- [Cha+19] Chia Cheng Chang et al. "Quantum Annealing for Systems of Polynomial Equations". In: *Scientific Reports* 9.1 (July 2019), p. 10258. ISSN: 2045-2322. DOI: 10.1038/s41598-019-46729-0. (Visited on 09/26/2022).
- [CJO19] Pedro C. S. Costa, Stephen Jordan, and Aaron Ostrander. "Quantum Algorithm for Simulating the Wave Equation". In: *Physical Review A* 99.1 (Jan. 2019), p. 012323. ISSN: 2469-9926, 2469-9934. DOI: 10.1103/PhysRevA.99.012323. (Visited on 01/12/2023).
- [CJS13] B. D. Clader, B. C. Jacobs, and C. R. Sprouse. "Preconditioned Quantum Linear System Algorithm". In: *Physical Review Letters* 110.25 (June 2013), p. 250504. ISSN: 0031-9007, 1079-7114. DOI: 10.1103/PhysRevLett.110. 250504. (Visited on 01/12/2023).
- [CKS17] Andrew M. Childs, Robin Kothari, and Rolando D. Somma. "Quantum Algorithm for Systems of Linear Equations with Exponentially Improved Dependence on Precision". In: SIAM Journal on Computing 46.6 (Jan. 2017), pp. 1920–1950. ISSN: 0097-5397, 1095-7111. DOI: 10.1137/16M1087072. (Visited on 01/12/2023).
- [CL20] Andrew M. Childs and Jin-Peng Liu. "Quantum Spectral Methods for Differential Equations". In: Communications in Mathematical Physics 375.2 (Apr. 2020), pp. 1427–1457. ISSN: 1432-0916. DOI: 10.1007/s00220-020-03699-z. (Visited on 11/26/2022).

- [CLO21] Andrew M. Childs, Jin-Peng Liu, and Aaron Ostrander. "High-Precision Quantum Algorithms for Partial Differential Equations". In: Quantum 5 (Nov. 2021), p. 574. ISSN: 2521-327X. DOI: 10.22331/q-2021-11-10-574. arXiv: 2002.07868 [quant-ph]. (Visited on 09/23/2022).
- [CS22] Juan Carlos Criado and Michael Spannowsky. Qade: Solving Differential Equations on Quantum Annealers. Apr. 2022. arXiv: 2204.03657 [hep-ph, physics:hep-th, physics:quant-ph]. (Visited on 09/23/2022).
- [Cui+22] Guolong Cui et al. "Optimization and Noise Analysis of the Quantum Algorithm for Solving One-Dimensional Poisson Equation". In: *Quantum Information and Computation* 22.7&8 (May 2022), pp. 569–593. ISSN: 15337146. DOI: 10.26421/QIC22.7-8-2. (Visited on 01/19/2023).
- [Dem+22] Reuben Demirdjian et al. Variational Quantum Solutions to the Advection-Diffusion Equation for Applications in Fluid Dynamics. Aug. 2022. DOI: 10.48550/arXiv.2208.11780. arXiv: 2208.11780 [physics, physics:quant-ph]. (Visited on 09/14/2022).
- [DS21a] I. Y. Dodin and E. A. Startsev. "On Applications of Quantum Computing to Plasma Simulations". In: *Physics of Plasmas* 28.9 (Sept. 2021), p. 092101. ISSN: 1070-664X. DOI: 10.1063/5.0056974. (Visited on 01/19/2023).
- [DS21b] I. Y. Dodin and E. A. Startsev. Quantum Computation of Nonlinear Maps. May 2021. DOI: 10.48550/arXiv.2105.07317. arXiv: 2105.07317 [physics, physics:quant-ph]. (Visited on 01/19/2023).
- [ESP19] Alexander Engel, Graeme Smith, and Scott E. Parker. "Quantum Algorithm for the Vlasov Equation". In: *Physical Review A* 100.6 (Dec. 2019), p. 062315. DOI: 10.1103/PhysRevA.100.062315. (Visited on 01/19/2023).
- [ESP21] Alexander Engel, Graeme Smith, and Scott E. Parker. "Linear Embedding of Nonlinear Dynamical Systems and Prospects for Efficient Quantum Algorithms". In: *Physics of Plasmas* 28.6 (June 2021), p. 062305. ISSN: 1070-664X. DOI: 10.1063/5.0040313. (Visited on 01/19/2023).
- [Ewe+22] Wei-Bin Ewe et al. "Variational Quantum-Based Simulation of Waveguide Modes". In: *IEEE Transactions on Microwave Theory and Techniques* 70.5 (May 2022), pp. 2517–2525. ISSN: 1557-9670. DOI: 10.1109/TMTT.2022. 3151510.
- [FJO21] Filipe Fontanela, Antoine Jacquier, and Mugad Oumgari. "Short Communication: A Quantum Algorithm for Linear PDEs Arising in Finance". In: SIAM Journal on Financial Mathematics 12.4 (Jan. 2021), SC98–SC114. ISSN: 1945-497X. DOI: 10.1137/21M1397878. (Visited on 09/23/2022).
- [FLT22] Di Fang, Lin Lin, and Yu Tong. Time-Marching Based Quantum Solvers for Time-Dependent Linear Differential Equations. Aug. 2022. DOI: 10. 48550/arXiv.2208.06941. arXiv: 2208.06941 [quant-ph]. (Visited on 09/14/2022).

- [Gai20] Frank Gaitan. "Finding Flows of a Navier–Stokes Fluid through Quantum Computing". In: npj Quantum Information 6.1 (July 2020), pp. 1–6. ISSN: 2056-6387. DOI: 10.1038/s41534-020-00291-0. (Visited on 12/08/2022).
- [Gar21] Juan José García-Ripoll. "Quantum-Inspired Algorithms for Multivariate Analysis: From Interpolation to Partial Differential Equations". In: Quantum 5 (Apr. 2021), p. 431. ISSN: 2521-327X. DOI: 10.22331/q-2021-04-15-431. arXiv: 1909.06619. (Visited on 05/04/2021).
- [GRG22] Paula García-Molina, Javier Rodríguez-Mediavilla, and Juan José García-Ripoll. "Quantum Fourier Analysis for Multivariate Functions and Applications to a Class of Schr\"odinger-Type Partial Differential Equations". In: *Physical Review A* 105.1 (Jan. 2022), p. 012433. DOI: 10.1103/PhysRevA.105.012433. (Visited on 01/19/2023).
- [Hat+19] Mohamed Hatifi et al. "Quantum Walk Hydrodynamics". In: *Scientific Reports* 9.1 (Feb. 2019), p. 2989. ISSN: 2045-2322. DOI: 10.1038/s41598-019-40059-x. (Visited on 01/19/2023).
- [HBR21] Hsin-Yuan Huang, Kishor Bharti, and Patrick Rebentrost. "Near-Term Quantum Algorithms for Linear Systems of Equations with Regression Loss Functions". In: *New Journal of Physics* 23.11 (Nov. 2021), p. 113021. ISSN: 1367-2630. DOI: 10.1088/1367-2630/ac325f. (Visited on 09/23/2022).
- [HD24] Luis Hidalgo and Patrick Draper. "Quantum Simulations for Strong-Field QED". In: *Physical Review D* 109.7 (Apr. 2024), p. 076004. DOI: 10.1103/PhysRevD.109.076004. (Visited on 09/14/2024).
- [HHL09] Aram W. Harrow, Avinatan Hassidim, and Seth Lloyd. "Quantum Algorithm for Linear Systems of Equations". In: *Physical Review Letters* 103.15 (Oct. 2009), p. 150502. ISSN: 0031-9007, 1079-7114. DOI: 10.1103/PhysRevLett.103.150502. (Visited on 01/12/2023).
- [IKK24] Asuka Igarashi, Tadashi Kadowaki, and Shiro Kawabata. "Quantum Algorithm for the Radiative-Transfer Equation". In: *Physical Review Applied* 21.3 (Mar. 2024), p. 034010. DOI: 10.1103/PhysRevApplied.21.034010. (Visited on 09/14/2024).
- [JL22] Shi Jin and Nana Liu. Quantum Algorithms for Computing Observables of Nonlinear Partial Differential Equations. Feb. 2022. DOI: 10.48550/arXiv.2202.07834. arXiv: 2202.07834 [physics, physics:quant-ph]. (Visited on 01/12/2023).
- [JLL22] Shi Jin, Xiantao Li, and Nana Liu. "Quantum Simulation in the Semi-Classical Regime". In: *Quantum* 6 (June 2022), p. 739. DOI: 10.22331/q-2022-06-17-739. (Visited on 12/08/2022).
- [JLY22a] Shi Jin, Nana Liu, and Yue Yu. Quantum Simulation of Partial Differential Equations via Schrodingerisation. Dec. 2022. DOI: 10.48550/arXiv.2212. 13969. arXiv: 2212.13969 [quant-ph]. (Visited on 01/02/2023).

- [JLY22b] Shi Jin, Nana Liu, and Yue Yu. Quantum Simulation of Partial Differential Equations via Schrodingerisation: Technical Details. Dec. 2022. DOI: 10. 48550/arXiv.2212.14703. arXiv: 2212.14703 [quant-ph]. (Visited on 01/07/2023).
- [JLY22c] Shi Jin, Nana Liu, and Yue Yu. "Time Complexity Analysis of Quantum Algorithms via Linear Representations for Nonlinear Ordinary and Partial Differential Equations". In: (2022). DOI: 10.48550/ARXIV.2209.08478. (Visited on 01/12/2023).
- [JLY22d] Shi Jin, Nana Liu, and Yue Yu. "Time Complexity Analysis of Quantum Difference Methods for Linear High Dimensional and Multiscale Partial Differential Equations". In: *Journal of Computational Physics* 471 (Dec. 2022), p. 111641. ISSN: 00219991. DOI: 10.1016/j.jcp.2022.111641. (Visited on 01/12/2023).
- [Jos+23] I. Joseph et al. "Quantum Computing for Fusion Energy Science Applications". In: *Physics of Plasmas* 30.1 (Jan. 2023), p. 010501. ISSN: 1070-664X. DOI: 10.1063/5.0123765. (Visited on 09/14/2024).
- [Jos20] Ilon Joseph. "Koopman-von Neumann Approach to Quantum Simulation of Nonlinear Classical Dynamics". In: *Physical Review Research* 2.4 (Oct. 2020), p. 043102. DOI: 10.1103/PhysRevResearch.2.043102. (Visited on 01/19/2023).
- [Jou22] Loïc Joubert-Doriol. "A Variational Approach for Linearly Dependent Moving Bases in Quantum Dynamics: Application to Gaussian Functions". In: arXiv:2205.02358 [physics, physics:quant-ph] (May 2022). arXiv: 2205.02358 [physics, physics:quant-ph]. (Visited on 05/09/2022).
- [Kou+22] Efstratios Koukoutsis et al. Dyson Maps and Unitary Evolution for Maxwell Equations in Tensor Dielectric Media. Sept. 2022. DOI: 10.48550/arXiv. 2209.08523. arXiv: 2209.08523 [physics, physics:quant-ph]. (Visited on 12/08/2022).
- [Kou+23] Efstratios Koukoutsis et al. "Quantum Computing Perspective for Electromagnetic Wave Propagation in Cold Magnetized Plasmas". In: *Physics of Plasmas* 30.12 (Dec. 2023), p. 122108. ISSN: 1070-664X. DOI: 10.1063/5.0177589. (Visited on 09/14/2024).
- [KPE21] Oleksandr Kyriienko, Annie E. Paine, and Vincent E. Elfving. "Solving Nonlinear Differential Equations with Differentiable Quantum Circuits". In: *Physical Review A* 103.5 (May 2021), p. 052416. DOI: 10.1103/PhysRevA.103.052416. (Visited on 01/19/2023).
- [Kro22] Hari Krovi. "Improved Quantum Algorithms for Linear and Nonlinear Differential Equations". In: arXiv:2202.01054 [physics, physics:quant-ph] (Feb. 2022). arXiv: 2202.01054 [physics, physics:quant-ph]. (Visited on 02/07/2022).

- [Kub+20] Kenji Kubo et al. "Variational Quantum Simulations of Stochastic Differential Equations". In: arXiv:2012.04429 [quant-ph] (Dec. 2020). arXiv: 2012.04429 [quant-ph]. (Visited on 12/15/2020).
- [Lap22] Leigh Lapworth. A Hybrid Quantum-Classical CFD Methodology with Benchmark HHL Solutions. June 2022. DOI: 10.48550/arXiv.2206.00419. arXiv: 2206.00419 [quant-ph]. (Visited on 06/18/2022).
- [LEK22] Fong Yew Leong, Wei-Bin Ewe, and Dax Enshan Koh. "Variational Quantum Evolution Equation Solver". In: Scientific Reports 12.1 (Dec. 2022), p. 10817. ISSN: 2045-2322. DOI: 10.1038/s41598-022-14906-3. arXiv: 2204.02912 [physics, physics:quant-ph]. (Visited on 09/23/2022).
- [Lin+22] Yen Ting Lin et al. Koopman von Neumann Mechanics and the Koopman Representation: A Perspective on Solving Nonlinear Dynamical Systems with Quantum Computers. Feb. 2022. DOI: 10.48550/arXiv.2202.02188. arXiv: 2202.02188 [quant-ph]. (Visited on 01/19/2023).
- [Liu+21a] Hai-Ling Liu et al. "Variational Quantum Algorithm for the Poisson Equation". In: Physical Review A 104.2 (Aug. 2021), p. 022418. ISSN: 2469-9926, 2469-9934. DOI: 10.1103/PhysRevA.104.022418. (Visited on 09/23/2022).
- [Liu+21b] Jin-Peng Liu et al. "Efficient Quantum Algorithm for Dissipative Non-linear Differential Equations". In: *Proceedings of the National Academy of Sciences* 118.35 (Aug. 2021), e2026805118. DOI: 10.1073/pnas.2026805118. (Visited on 01/19/2023).
- [Liu+22] Y. Y. Liu et al. "Application of a Variational Hybrid Quantum-Classical Algorithm to Heat Conduction Equation and Analysis of Time Complexity". In: *Physics of Fluids* 34.11 (Nov. 2022), p. 117121. ISSN: 1070-6631. DOI: 10.1063/5.0121778. (Visited on 01/19/2023).
- [Lju22] Budinski Ljubomir. "Quantum Algorithm for the Navier–Stokes Equations by Using the Streamfunction-Vorticity Formulation and the Lattice Boltzmann Method". In: *International Journal of Quantum Information* 20.02 (Mar. 2022), p. 2150039. ISSN: 0219-7499. DOI: 10.1142/S0219749921500398. (Visited on 01/19/2023).
- [Llo+20] Seth Lloyd et al. Quantum Algorithm for Nonlinear Differential Equations. Dec. 2020. DOI: 10.48550/arXiv.2011.06571. arXiv: 2011.06571 [nlin, physics:quant-ph]. (Visited on 01/19/2023).
- [LMJ18] Michael Lubasch, Pierre Moinier, and Dieter Jaksch. "Multigrid Renormalization". In: *Journal of Computational Physics* 372 (Nov. 2018), pp. 587–602. ISSN: 0021-9991. DOI: 10.1016/j.jcp.2018.06.065. (Visited on 11/26/2022).

- [LMS22] Noah Linden, Ashley Montanaro, and Changpeng Shao. "Quantum vs. Classical Algorithms for Solving the Heat Equation". In: *Communications in Mathematical Physics* (Aug. 2022). ISSN: 1432-0916. DOI: 10.1007/s00220-022-04442-6. (Visited on 09/23/2022).
- [LO08] Sarah K. Leyton and Tobias J. Osborne. A Quantum Algorithm to Solve Nonlinear Differential Equations. Dec. 2008. DOI: 10.48550/arXiv.0812.4423. arXiv: 0812.4423 [quant-ph]. (Visited on 01/12/2023).
- [Lub+20] Michael Lubasch et al. "Variational Quantum Algorithms for Nonlinear Problems". In: *Physical Review A* 101.1 (Jan. 2020), p. 010301. ISSN: 2469-9926, 2469-9934. DOI: 10.1103/PhysRevA.101.010301. (Visited on 09/23/2022).
- [MK22] Koichi Miyamoto and Kenji Kubo. "Pricing Multi-Asset Derivatives by Finite-Difference Method on a Quantum Computer". In: *IEEE Transactions on Quantum Engineering* 3 (2022), pp. 1–25. ISSN: 2689-1808. DOI: 10.1109/TQE.2021.3128643.
- [MP16] Ashley Montanaro and Sam Pallister. "Quantum Algorithms and the Finite Element Method". In: *Physical Review A* 93.3 (Mar. 2016), p. 032324. DOI: 10.1103/PhysRevA.93.032324. (Visited on 11/26/2022).
- [MQ23] Michael Q. May and Hong Qin. "Quantum Three-Wave Instability". In: $Physical\ Review\ A\ 107.6$ (June 2023), p. 062204. DOI: 10.1103/PhysRevA. 107.062204. (Visited on 10/28/2023).
- [MQ24] Michael May and Hong Qin. Nonlinear Solution of Classical Three-Wave Interaction via Finite Dimensional Quantum Model. Jan. 2024. DOI: 10. 48550/arXiv.2401.03995. arXiv: 2401.03995 [physics]. (Visited on 03/21/2024).
- [MS21] Philip Mocz and Aaron Szasz. "Toward Cosmological Simulations of Dark Matter on Quantum Computers". In: *The Astrophysical Journal* 910.1 (Mar. 2021), p. 29. ISSN: 0004-637X. DOI: 10.3847/1538-4357/abe6ac. (Visited on 01/19/2023).
- [NDS22] I. Novikau, I. Y. Dodin, and E. A. Startsev. Simulation of Linear Non-Hermitian Boundary-Value Problems with Quantum Singular Value Transformation. Dec. 2022. DOI: 10.48550/arXiv.2212.09113. arXiv: 2212.09113 [physics, physics:quant-ph]. (Visited on 01/11/2023).
- [NDS24] Ivan Novikau, Ilya Y. Dodin, and Edward A. Startsev. Encoding of Linear Kinetic Plasma Problems in Quantum Circuits via Data Compression. Mar. 2024. arXiv: 2403.11989. (Visited on 03/19/2024).
- [NSD22] I. Novikau, E. A. Startsev, and I. Y. Dodin. "Quantum Signal Processing for Simulating Cold Plasma Waves". In: *Physical Review A* 105.6 (June 2022), p. 062444. DOI: 10.1103/PhysRevA.105.062444. (Visited on 01/19/2023).

- [Oga+15] Armen Oganesov et al. "Unitary Quantum Lattice Gas Algorithm Generated from the Dirac Collision Operator for 1D Soliton–Soliton Collisions". In: Radiation Effects and Defects in Solids 170.1 (Jan. 2015), pp. 55–64. ISSN: 1042-0150. DOI: 10.1080/10420150.2014.988625. (Visited on 12/08/2022).
- [Oga+16a] Armen Oganesov et al. "Benchmarking the Dirac-generated Unitary Lattice Qubit Collision-Stream Algorithm for 1D Vector Manakov Soliton Collisions". In: Computers & Mathematics with Applications 72.2 (July 2016), pp. 386–393. ISSN: 08981221. DOI: 10.1016/j.camwa.2015.06.001. (Visited on 12/08/2022).
- [Oga+16b] Armen Oganesov et al. "Imaginary Time Integration Method Using a Quantum Lattice Gas Approach". In: Radiation Effects and Defects in Solids 171.1-2 (Feb. 2016), pp. 96–102. ISSN: 1042-0150. DOI: 10.1080/10420150.2015.1137916. (Visited on 12/08/2022).
- [Oga+18] Armen Oganesov et al. "Effect of Fourier Transform on the Streaming in Quantum Lattice Gas Algorithms". In: *Radiation Effects and Defects in Solids* 173.3-4 (Apr. 2018), pp. 169–174. ISSN: 1042-0150. DOI: 10.1080/10420150.2018.1462364. (Visited on 12/08/2022).
- [Oll+23] Pauline J. Ollitrault et al. "Quantum Algorithms for Grid-Based Variational Time Evolution". In: *Quantum* 7 (Oct. 2023), p. 1139. DOI: 10. 22331/q-2023-10-12-1139. (Visited on 11/01/2023).
- [OMa+22] Daniel O'Malley et al. "A Near-Term Quantum Algorithm for Solving Linear Systems of Equations Based on the Woodbury Identity". In: arXiv:2205.00645 [quant-ph] (May 2022). arXiv: 2205.00645 [quant-ph]. (Visited on 05/09/2022).
- [Oz+21] Furkan Oz et al. "Solving Burgers' Equation with Quantum Computing". In: Quantum Information Processing 21.1 (Dec. 2021), p. 30. ISSN: 1573-1332. DOI: 10.1007/s11128-021-03391-8. (Visited on 12/01/2022).
- [Pat+22] Raj Patel et al. Quantum-Inspired Tensor Neural Networks for Partial Differential Equations. Aug. 2022. DOI: 10.48550/arXiv.2208.02235. arXiv: 2208.02235 [cond-mat, physics:physics, physics:quant-ph]. (Visited on 09/14/2022).
- [Ram+21] Abhay K. Ram et al. "Reflection and Transmission of Electromagnetic Pulses at a Planar Dielectric Interface: Theory and Quantum Lattice Simulations". In: *AIP Advances* 11.10 (Oct. 2021), p. 105116. DOI: 10.1063/5.0067204. (Visited on 12/08/2022).
- [Ric+22] Alexandre C. Ricardo et al. "Alternatives to a Nonhomogeneous Partial Differential Equation Quantum Algorithm". In: *Physical Review A* 106.5 (Nov. 2022), p. 052431. DOI: 10.1103/PhysRevA.106.052431. (Visited on 12/08/2022).

- [Sah+22] Kamal K. Saha et al. Advancing Algorithm to Scale and Accurately Solve Quantum Poisson Equation on Near-term Quantum Hardware. Oct. 2022.

 DOI: 10.48550/arXiv.2210.16668. arXiv: 2210.16668 [quant-ph]. (Visited on 12/08/2022).
- [Sar22] Merey M. Sarsengeldin. "A Hybrid Classical-Quantum Framework for Solving Free Boundary Value Problems and Applications in Modeling Electric Contact Phenomena". In: arXiv:2205.02230 [quant-ph] (May 2022). arXiv: 2205.02230 [quant-ph]. (Visited on 05/09/2022).
- [Sat+21] Yuki Sato et al. "Variational Quantum Algorithm Based on the Minimum Potential Energy for Solving the Poisson Equation". In: *Physical Review A* 104.5 (Nov. 2021), p. 052409. ISSN: 2469-9926, 2469-9934. DOI: 10.1103/PhysRevA.104.052409. (Visited on 09/23/2022).
- [SGS22] Amit Surana, Abeynaya Gnanasekaran, and Tuhin Sahai. Carleman Linearization Based Efficient Quantum Algorithm for Higher Order Polynomial Differential Equations. Dec. 2022. arXiv: 2212.10775 [quant-ph]. (Visited on 01/12/2023).
- [SGS24] Amit Surana, Abeynaya Gnanasekaran, and Tuhin Sahai. "An Efficient Quantum Algorithm for Simulating Polynomial Dynamical Systems". In: Quantum Information Processing 23.3 (Mar. 2024), p. 105. ISSN: 1573-1332. DOI: 10.1007/s11128-024-04311-2. (Visited on 03/16/2024).
- [Shi+18] Yuan Shi et al. "Simulations of Relativistic Quantum Plasmas Using Real-Time Lattice Scalar QED". In: *Physical Review E* 97.5 (May 2018), p. 053206. DOI: 10.1103/PhysRevE.97.053206. (Visited on 01/19/2023).
- [Shi+21] Yuan Shi et al. "Simulating Non-Native Cubic Interactions on Noisy Quantum Machines". In: *Physical Review A* 103.6 (June 2021), p. 062608. DOI: 10.1103/PhysRevA.103.062608. (Visited on 01/19/2023).
- [Shi+24] Yuan Shi et al. Simulating Nonlinear Optical Processes on a Superconducting Quantum Device. June 2024. arXiv: 2406.13003 [physics, physics:quant-ph]. (Visited on 06/21/2024).
- [SM21] Changpeng Shao and Ashley Montanaro. "Faster Quantum-Inspired Algorithms for Solving Linear Systems". In: arXiv:2103.10309 [quant-ph] (Mar. 2021). arXiv: 2103.10309 [quant-ph]. (Visited on 03/22/2021).
- [SS19] Siddhartha Srivastava and Veera Sundararaghavan. "Box Algorithm for the Solution of Differential Equations on a Quantum Annealer". In: *Physical Review A* 99.5 (May 2019), p. 052355. ISSN: 2469-9926, 2469-9934. DOI: 10.1103/PhysRevA.99.052355. (Visited on 09/23/2022).
- [SSC21] Adrien Suau, Gabriel Staffelbach, and Henri Calandra. "Practical Quantum Computing: Solving the Wave Equation Using a Quantum Approach". In: *ACM Transactions on Quantum Computing* 2.1 (Feb. 2021), 2:1–2:35. ISSN: 2643-6809. DOI: 10.1145/3430030. (Visited on 01/19/2023).

- [SSO19] Yiğit Subaşı, Rolando D. Somma, and Davide Orsucci. "Quantum Algorithms for Systems of Linear Equations Inspired by Adiabatic Quantum Computing". In: *Physical Review Letters* 122.6 (Feb. 2019), p. 060504. DOI: 10.1103/PhysRevLett.122.060504. (Visited on 01/19/2023).
- [TF23] Yu Tanaka and Keisuke Fujii. Quantum Solvable Nonlinear Differential Equations. May 2023. DOI: 10.48550/arXiv.2305.00653. arXiv: 2305.00653 [quant-ph]. (Visited on 05/02/2023).
- [TYH23] Kiichiro Toyoizumi, Naoki Yamamoto, and Kazuo Hoshino. *Hamiltonian Simulation Using Quantum Singular Value Transformation: Complexity Analysis and Application to the Linearized Vlasov-Poisson Equation.* Apr. 2023. DOI: 10.48550/arXiv.2304.08937. arXiv: 2304.08937 [physics, physics:quant-ph]. (Visited on 04/19/2023).
- [Vah+10] George Vahala et al. "Unitary Quantum Lattice Gas Algorithms for Quantum to Classical Turbulence". In: 2010 DoD High Performance Computing Modernization Program Users Group Conference. June 2010, pp. 184–191. DOI: 10.1109/HPCMP-UGC.2010.15.
- [Vah+11] George Vahala et al. "Unitary Qubit Lattice Simulations of Multiscale Phenomena in Quantum Turbulence". In: SC '11: Proceedings of 2011 International Conference for High Performance Computing, Networking, Storage and Analysis. Nov. 2011, pp. 1–11. DOI: 10.1145/2063384.2063416.
- [Vah+19] Linda Vahala et al. "Unitary Qubit Lattice Algorithm for Three-Dimensional Vortex Solitons in Hyperbolic Self-Defocusing Media". In: Communications in Nonlinear Science and Numerical Simulation 75 (Aug. 2019), pp. 152–159. ISSN: 1007-5704. DOI: 10.1016/j.cnsns.2019.03.016. (Visited on 12/08/2022).
- [Vah+20a] George Vahala et al. "Building a Three-Dimensional Quantum Lattice Algorithm for Maxwell Equations". In: Radiation Effects and Defects in Solids 175.11-12 (Nov. 2020), pp. 986–990. ISSN: 1042-0150. DOI: 10.1080/10420150.2020.1845685. (Visited on 12/08/2022).
- [Vah+20b] George Vahala et al. The Effect of the Pauli Spin Matrices on the Quantum Lattice Algorithm for Maxwell Equations in Inhomogeneous Media. Oct. 2020. DOI: 10.48550/arXiv.2010.12264. arXiv: 2010.12264 [physics, physics:quant-ph]. (Visited on 12/08/2022).
- [Vah+20c] George Vahala et al. "Unitary Quantum Lattice Simulations for Maxwell Equations in Vacuum and in Dielectric Media". In: *Journal of Plasma Physics* 86.5 (Oct. 2020), p. 905860518. ISSN: 0022-3778, 1469-7807. DOI: 10.1017/S0022377820001166. (Visited on 12/08/2022).

- [Vah+21a] George Vahala et al. "One- and Two-Dimensional Quantum Lattice Algorithms for Maxwell Equations in Inhomogeneous Scalar Dielectric Media I: Theory". In: Radiation Effects and Defects in Solids 176.1-2 (Feb. 2021), pp. 49–63. ISSN: 1042-0150. DOI: 10.1080/10420150.2021.1891058. (Visited on 12/08/2022).
- [Vah+21b] George Vahala et al. "One- and Two-Dimensional Quantum Lattice Algorithms for Maxwell Equations in Inhomogeneous Scalar Dielectric Media. II: Simulations". In: Radiation Effects and Defects in Solids 176.1-2 (Feb. 2021), pp. 64–72. ISSN: 1042-0150. DOI: 10.1080/10420150.2021. 1891059. (Visited on 12/08/2022).
- [Vah+21c] George Vahala et al. Two Dimensional Electromagnetic Scattering from Dielectric Objects Using Quantum Lattice Algorithm. SSRN Scholarly Paper. Rochester, NY, Dec. 2021. DOI: 10.2139/ssrn.3996913. (Visited on 12/08/2022).
- [Vah+22] George Vahala et al. "Quantum Lattice Representation for the Curl Equations of Maxwell Equations". In: Radiation Effects and Defects in Solids 177.1-2 (Feb. 2022), pp. 85–94. ISSN: 1042-0150. DOI: 10.1080/10420150. 2022.2049784. (Visited on 12/08/2022).
- [VSV20] George Vahala, Min Soe, and Linda Vahala. "Qubit Unitary Lattice Algorithm for Spin-2 Bose-Einstein Condensates: II Vortex Reconnection Simulations and Non-Abelain Vortices". In: Radiation Effects and Defects in Solids 175.1-2 (Jan. 2020), pp. 113–119. ISSN: 1042-0150. DOI: 10.1080/10420150.2020.1718136. (Visited on 12/08/2022).
- [VVS20] George Vahala, Linda Vahala, and Min Soe. "Qubit Unitary Lattice Algorithm for Spin-2 Bose–Einstein Condensates. I Theory and Pade Initial Conditions". In: *Radiation Effects and Defects in Solids* 175.1-2 (Jan. 2020), pp. 102–112. ISSN: 1042-0150. DOI: 10.1080/10420150.2020. 1718135. (Visited on 12/08/2022).
- [VYV03] George Vahala, Jeffrey Yepez, and Linda Vahala. "Quantum Lattice Gas Representation of Some Classical Solitons". In: *Physics Letters A* 310.2 (Apr. 2003), pp. 187–196. ISSN: 0375-9601. DOI: 10.1016/S0375-9601(03) 00334-7. (Visited on 12/08/2022).
- [Wan+20] Shengbin Wang et al. "Quantum Fast Poisson Solver: The Algorithm and Complete and Modular Circuit Design". In: *Quantum Information Processing* 19.6 (Apr. 2020), p. 170. ISSN: 1573-1332. DOI: 10.1007/s11128-020-02669-7. (Visited on 12/08/2022).
- [WX22] Hefeng Wang and Hua Xiang. Efficient Quantum Algorithms for Solving Quantum Linear System Problems. Aug. 2022. DOI: 10.48550/arXiv. 2208.06763. arXiv: 2208.06763 [quant-ph]. (Visited on 09/14/2022).

- [Xu+21] Xiaosi Xu et al. "Variational Algorithms for Linear Algebra". In: Science Bulletin 66.21 (Nov. 2021), pp. 2181–2188. ISSN: 2095-9273. DOI: 10.1016/j.scib.2021.06.023. (Visited on 09/23/2022).
- [Xue+22] Cheng Xue et al. "Quantum Algorithm for Solving a Quadratic Nonlinear System of Equations". In: *Physical Review A* 106.3 (Sept. 2022), p. 032427. ISSN: 2469-9926, 2469-9934. DOI: 10.1103/PhysRevA.106.032427. (Visited on 01/12/2023).
- [XWG21] Cheng Xue, Yuchun Wu, and Guoping Guo. "Quantum Newton's Method for Solving the System of Nonlinear Equations". In: *SPIN* 11.03 (Sept. 2021), p. 2140004. ISSN: 2010-3247. DOI: 10.1142/S201032472140004X. (Visited on 01/12/2023).
- [Yep02] Jeffrey Yepez. An Efficient and Accurate Quantum Algorithm for the Dirac Equation. Oct. 2002. DOI: 10.48550/arXiv.quant-ph/0210093. arXiv: quant-ph/0210093. (Visited on 12/08/2022).
- [Yep05] Jeffrey Yepez. "Relativistic Path Integral as a Lattice-based Quantum Algorithm". In: Quantum Information Processing 4.6 (Dec. 2005), pp. 471–509. ISSN: 1573-1332. DOI: 10.1007/s11128-005-0009-7. (Visited on 12/08/2022).
- [Yep16] Jeffrey Yepez. "Quantum Lattice Gas Algorithmic Representation of Gauge Field Theory". In: Quantum Information Science and Technology II. Vol. 9996. SPIE, Oct. 2016, pp. 66–87. DOI: 10.1117/12.2246702. (Visited on 12/08/2022).
- [YL22] Erika Ye and Nuno F. G. Loureiro. A Quantum-Inspired Method for Solving the Vlasov-Poisson Equations. May 2022. arXiv: 2205.11990 [physics]. (Visited on 09/26/2022).
- [YL23] Erika Ye and Nuno Loureiro. Quantized Tensor Networks for Solving the Vlasov-Maxwell Equations. Nov. 2023. arXiv: 2311.07756 [physics, physics:quant-ph]. (Visited on 11/16/2023).
- [Zan+21] Benjamin Zanger et al. "Quantum Algorithms for Solving Ordinary Differential Equations via Classical Integration Methods". In: *Quantum* 5 (July 2021), p. 502. ISSN: 2521-327X. DOI: 10.22331/q-2021-07-13-502. arXiv: 2012.09469 [quant-ph]. (Visited on 09/23/2022).
- [Zyl+22] Julien Zylberman et al. Hybrid Quantum-Classical Algorithm for Hydrodynamics. Feb. 2022. DOI: 10.48550/arXiv.2202.00918. arXiv: 2202.00918 [physics, physics:quant-ph]. (Visited on 01/19/2023).