## A Living Review of Quantum Computing for Plasma Physics

## Abstract

Quantum Computing promises accelerated simulation of certain classes of problems, in particular in plasma physics. The goal of this document is to provide a comprehensive list of citations for those developing and applying these approaches to experimental or theoretical analyses. As a living document, it will be updated as often as possible to incorporate the latest developments. Suggestions are most welcome.

The purpose of this note is to collect references for quantum algorithms already relevant to plasma physics. A minimal number of categories is chosen in order to be as useful as possible. Note that papers may be referenced in more than one category.

To facilitate search, the tags  $\overline{\text{NISQ}}$  (noisy-intermediate scale quantum computing),  $\overline{\text{FTol}}$  (fault-tolerant quantum computing),  $\overline{\text{QAnn}}$  (quantum annealing),  $\overline{\text{QIns}}$  (quantum-inspired), and  $\overline{\text{Tool}}$  (generally useful tool) are applied if clearly appropriate.

Color-filled tags indicate the type of content. Since most papers contain some form of theoretical analysis, we use the theoretical tag **Theo** solely for the papers with analytical results, and no considerable numerical or experimental results. The tag **Num** marks papers with numerical simulations, but no experimental results run on quantum devices. Finally, **Exp** marks papers with displayed experimental results. We may ommit this tag if the paper is referenced and tagged in a subsequent subsection.

The fact that a paper is listed in this document does not endorse or validate its content - that is for the community (and for peer-review) to decide. Furthermore, the classification here is a best attempt and may have flaws - please let us know if (a) we have missed a paper you think should be included, (b) a paper has been misclassified or wrongly tagged, or (c) a citation for a paper is not correct or if the journal information is now available.

In order to be as useful as possible, this document will continue to evolve so please check back<sup>1</sup> before you write your next paper. You can simply download the .bib file to get all of the latest references. Please consider citing Ref. [AC22] when referring to this living review.

## • Modern Reviews

Below are links to (static) general and specialized reviews.

- Review of Plasma Physics Problems Reformulated for Quantum Computing [DS20]
- Review of Fusion Plasma Physics Problems Reformulated for Quantum Computing[Jos+22]
- System of linear equations NISQ Num [HBR19] Exp[Bra+20; Xu+21], FTol Theo [HHL09; CJS13; CKS17; WX22], QAnn Exp [BL22], QIns Theo [SM21].
- System of nonlinear equations FTol Theo [DS21] Num [XWG21; Xue+22].
  - System of polynomial equations QAnn Exp [Cha+19].
- Ordinary differential equations QAnn Exp [Zan+21].
  - Linear FTol Theo [Ber14; Ber+17; CL20; FLT22; JLY22a], Num [JLY22b],
     QAnn Exp [Zan+21].
    - \* Second-order QAnn Exp [SS19].

<sup>&</sup>lt;sup>1</sup>See http://epp.ist.utl.pt/qppq/.

- · Quantum harmonic oscillator FTol Num [Ric+22].
- Nonlinear NISQ [KPE21; Shi+21] FTol Theo [LO08; DS21] Num [JLY22b; Liu+20; SGS22], QAnn Num [Zan+21].
  - \* Laguerre QAnn Num [CS22].
- Partial differential equations FTol Theo [CLO21], QIns [Gar21]
  - Linear NISQ [OMa+22], FTol Theo [JLY22a], Num [JLY22b], QAnn Num [CS22].
    - \* Non-homogeneous NISQ Exp [Bra+20], FTol Theo [Arr+19; Ric+22].
      - · Vlasov FTol Num [ESP19]
      - · Poisson NISQ [Bra+20; Sat+21; AK22; Sah+22; Lub+20], FTol Theo [Cao+13], Num [Arr+19; Ric+22; Liu+21; Wan+20].
    - \* Semi-classical Schrödinger FTol Num [JLL22].
    - \* Time-dependent Schrödinger NISQ [Jou22] FTo1 Num [JLL22].
    - \* Stochastic PDE NISQ Num [Kub+21; Alg+22]
      - · Fokker-Planck FTol Num [JLY22b], QIns Num [Gar21].
      - · Linear Boltzmann FTol Num [JLY22b].
    - \* Hyperbolic/Wave-related FTol Theo [JLY22d; JL22].
      - · Wave FTol Num [CJO19], QAnn Num [CS22].
      - · Maxwell's FTol Theo [CJO19], Num [NSD21; NDS22]
      - · Klein-Gordon FTol Theo [CJO19].
      - · Helmholtz NISQ Num [Ewe+22].
    - \* Parabolic QIns Num [Pat+22].
      - · Heat NISQ [LEK22; Alb+22], FTol Theo [LMS22; JLY22a; JLY22d] Num [JLY22b].
      - · Black-Scholes NISQ [FJO21; MK22], FTol Num [JLY22b].
      - · Convection FTol Num [JLY22b].
      - · Hamilton-Jacobi-Bellman QIns Num [Pat+22].
  - Nonlinear FTol Theo [JL22].
    - \* Vlasov-Poisson  $\overline{\mathtt{QIns}}$  Num  $[\mathrm{YL}22]$
    - \* Schrödinger-Poisson NISQ Num [MS21]
    - \* Nonlinear-Schrödinger NISQ Exp [Lub+20]
    - \* Burger's FTol Num [Oz+21].
    - \* Evolution equation NISQ Theo [LEK22].
    - \* Reaction-diffusion NISQ Num [LEK22] NISQ Exp [Dem+22], FTol Num [An+22].
    - \* Navier-Stokes FTol Num [Gai20].

- · Incompressible NISQ [LEK22], QIns Num [Lap22].
- \* Hamilton-Jacobi FTol Theo [JLY22c; JL22].
- \* Black-Scholes-Barenblatt QIns Num [Pat+22].
- Koopman-von Neumann formulation FTol Theo [Jos20; JLY22c].
- Nonlinear Schrödinger equation formulation FTol Theo [Llo+20]
- Linear embedding of nonlinear dynamical systems FTol Theo [ESP21; JLY22c] Num [Liu+20]
- Finite element method **FTol Theo** [MP16].
- Quantum simulation FTol Theo [BCK15].
  - Sparse Hamiltonians FTol Theo [Ber+07; Ber+14].
  - Imaginary time evolution NISQ Num [McA+19].
- Lattice Boltzmann algorithms Ftol Num [Bud21]
- Quantum lattice algorithms QIns Num [And+22; Kou+22; Oga+18; Ram+21; Vah+20a; Vah+20b; Vah+21a; Vah+21b; Vah+22; VSV20; VVS20; Vah+21c; Vah+20c; Vah+19; Vah+20d; Yep02; Yep05; Yep16; VYV03; Vah+11; Vah+10; Oga+16a; Oga+16b; Oga+15; Shi+18; And+23]

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