

# Observation of a many-body dynamical phase transition with a 53-qubit quantum simulator

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**A quantum simulator is a type of quantum computer that controls the interactions between quantum bits (or qubits) in a way that can be mapped to certain quantum many-body problems<sup>1,2</sup>. As it becomes possible to exert more control over larger numbers of qubits, such simulators will be able to tackle a wider range of problems, such as materials design and molecular modelling, with the ultimate limit being a universal quantum computer that can solve general classes of hard problems<sup>3</sup>. Here we use a quantum simulator composed of up to 53 qubits to study non-equilibrium dynamics in the transverse-field Ising model with long-range interactions. We observe a dynamical phase transition after a sudden change of the Hamiltonian, in a regime in which conventional statistical mechanics does not apply<sup>4</sup>. The qubits are represented by the spins of trapped ions, which can be prepared in various initial pure states. We apply a global long-range Ising interaction with controllable strength and range, and measure each individual qubit with an efficiency of nearly 99 per cent. Such high efficiency means that arbitrary many-body correlations between qubits can be measured in a single shot, enabling the dynamical phase transition to be probed directly and revealing computationally intractable features that rely on the long-range interactions and high connectivity between qubits.**

There have been many recent demonstrations of quantum simulators with varying numbers of qubits and degrees of individual qubit control<sup>2</sup>. For instance, small numbers of qubits stored in trapped atomic ions<sup>5,6</sup> and superconducting circuits<sup>7,8</sup> have been used to simulate various magnetic spin or Hubbard models, with preparation and measurement of individual qubit states. Large numbers of atoms have been used to simulate similar models, but with global control and measurements<sup>9</sup> or with correlations that appear over only a few atom sites<sup>10</sup>. Such quantum simulators are excellent platforms for studying quantum systems out of equilibrium<sup>11</sup>. However, an outstanding challenge is to increase the number of qubits while maintaining control and measurement of individual qubits, with the goal of performing simulations or implementing algorithms to tackle problems that cannot be solved efficiently using classical means. Atomic systems are excellent candidates for this challenge, because their qubits can be made to be virtually identical, with flexible and reconfigurable control through external optical fields and high initialization and detection efficiency for individual qubits. Recent work with Rydberg atoms<sup>12,13</sup> has demonstrated many-body quantum dynamics with up to 51 atoms coupled through van der Waals interactions. Here we present quantum simulations at a similar scale using the more controllable system of trapped atomic ions, the many-body qubit interactions of which are mediated by their long-range Coulomb-coupled motion.

We perform a quantum simulation of a dynamical phase transition (DPT) with up to 53 qubits. The understanding of such non-equilibrium behaviour is of interest in a wide range of subjects, including social science<sup>14</sup>, cellular biology<sup>15</sup>, astrophysics and quantum

condensed matter physics<sup>16</sup>. Recent theoretical studies of DPTs<sup>17–19</sup> involve the transverse-field Ising model—the quintessential model of quantum phase transitions<sup>20</sup>. Recent experiments have investigated DPT with cold neutral atoms<sup>21</sup> and up to 10 trapped-ion qubits, with the transverse field dominating the interactions<sup>22</sup>. These studies have considered long-time spin relaxation dynamics<sup>17,19</sup> and non-analytic time evolution of non-local quantities<sup>18,19,22</sup>.

In this experiment, we use a quantum quench—a sudden change in the Hamiltonian of the system—to bring a collection of interacting trapped-ion qubits out of equilibrium<sup>5,6,22,23</sup>. The theoretical description of the dynamics is made difficult by the population of exponentially many excited states of the many-body spectrum as the number of qubits is increased, typically accompanied by high entanglement density between the qubits. Given the long-range interactions between the qubits, the growth in entanglement can be much faster than in locally connected systems<sup>12,13,24</sup>, limiting efficient numerical simulation using matrix product states to short-time dynamics<sup>25</sup>. The nature of the long-range Ising interaction also leads to unique dynamical features (discussed below) and an emergent higher dimensionality of the system<sup>19,26</sup>.

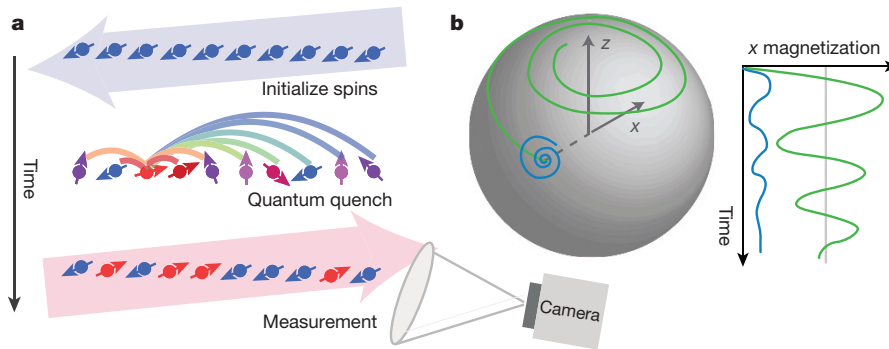
We experimentally realize a quantum many-body Hamiltonian with long-range Ising interactions and flexible tuning parameters<sup>27</sup>, where the strength and the range of the interactions can both be tuned. As outlined in Fig. 1, we initialize the qubits (effective spin-1/2 systems) in a product state, all polarized along the  $x$  direction of the Bloch sphere, and then suddenly turn on the Hamiltonian of the transverse-field Ising model (setting the Planck constant  $\hbar = 1$ )

$$H = \sum_{i < j} J_{ij} \sigma_i^x \sigma_j^x + B_z \sum_i \sigma_i^z \quad (1)$$

Here  $\sigma_i^\gamma$  ( $\gamma \in \{x, y, z\}$ ) is the Pauli matrix acting on the  $i$ th spin along the  $\gamma$  direction of the Bloch sphere,  $J_{ij}$  is the Ising coupling between spins  $i$  and  $j$ , and  $B_z$  denotes the transverse magnetic field, which acts as the control parameter for crossing dynamical criticality in the DPT. In Fig. 1b we show a simplified Bloch-sphere representation of the DPT. The spins quickly evolve from the longitudinally polarized initial state, and then either precess about a large transverse magnetic field (green curves) or stay pinned near the initial conditions when the transverse field is small (blue curves).

To implement the quantum Hamiltonian (see Methods), each spin in the chain is encoded in the  $^2S_{1/2}|F=0, m_F=0\rangle \equiv |\downarrow\rangle_z$  and  $|F=1, m_F=0\rangle \equiv |\uparrow\rangle_z$  hyperfine ‘clock’ states of a  $^{171}\text{Yb}^+$  ion and separated by a frequency of  $\nu_0 = 12.642821$  GHz. We store a chain of up to  $N=53$  ions in a linear radio-frequency Paul trap (Methods) and initialize the qubits in the product state  $|\downarrow\downarrow\downarrow\downarrow\rangle_x$ , where  $|\downarrow\rangle_x \equiv \frac{1}{2}(|\downarrow\rangle_z - |\uparrow\rangle_z)$ . Spin–spin interactions are generated by spin-dependent optical dipole forces from an applied laser field, which give rise to tunable long-range Ising couplings that fall off approximately algebraically as  $J_{ij} \approx J_0/|i-j|^\alpha$  (refs 27, 28). The power-law exponent  $\alpha$  is set to between 0.8 and 1.0 in the experiment, and the maximum interaction strengths are

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**Figure 1 | Illustration of the DPT from a quantum quench.** We subject a system of interacting spins to a sudden change in the Hamiltonian and study the resulting quantum dynamics. **a**, An isolated spin system is prepared in a product state, and then an Ising spin–spin interaction is suddenly turned on, along with a tunable transverse magnetic field (see text for details). At the end of the evolution, we measure the spin magnetizations along the initial spin orientation direction using a camera. Blue spins and shaded arrows indicate the initial spin polarization; red spins and arrow indicate the projective measurement of spin-down in the measurement basis; and spin and lines of other colours indicate

interacting spins in superpositions. **b**, A Bloch-sphere representation<sup>19</sup> of the average spin magnetization. Spins are initially fully polarized along the longitudinal  $x$  direction of the Bloch sphere, and then evolve with Ising interactions along  $x$  competing with the transverse field along  $z$ , resulting in oscillations and relaxations. Blue curves illustrate the quench dynamics with a low transverse field; green curves indicate the dynamics with a large transverse field across criticality. The grey line indicates a level of zero average magnetization along  $x$ .

$J_0 = (0.82, 0.56, 0.38, 0.65)$  kHz, for 8, 12, 16 and 53 spins, respectively. The transverse field is generated by a controllable Stark shift of the spin qubit splitting from the same laser field (Methods).

Finally, we measure the magnetization of each spin  $\langle \sigma_i^x \rangle$ . We rotate all of the spins by  $\pi/2$  about the  $y$  axis of the Bloch sphere (exchanging  $\sigma_i^x \leftrightarrow \sigma_i^z$ ) and then illuminate the ions with resonant radiation and collect the  $\sigma_i^z$ -dependent fluorescence on a camera with site-resolved imaging<sup>28</sup>. We estimate a spin detection efficiency of about 99% for each qubit (see Methods), providing access to all possible many-body correlators in a single shot.

The simplest observable of quench dynamics, after evolving the system under the transverse-field Ising model for time  $t$ , is the average magnetization of the spins along  $x$ :

$$\langle \sigma^x(t) \rangle = \frac{1}{N} \sum_i \langle \sigma_i^x(t) \rangle$$

In Fig. 2 we show the measured average magnetization for  $N = 16$  spins through  $2\pi J_0 t = 4.8$ , for different values of the transverse field. We formulate a renormalized field  $\tilde{B}_z$  to account for the divergence of the energy density of the long-range Ising interactions, so that the ratio  $\tilde{B}_z/J_0$  is meaningful in the thermodynamic limit (see Methods). This

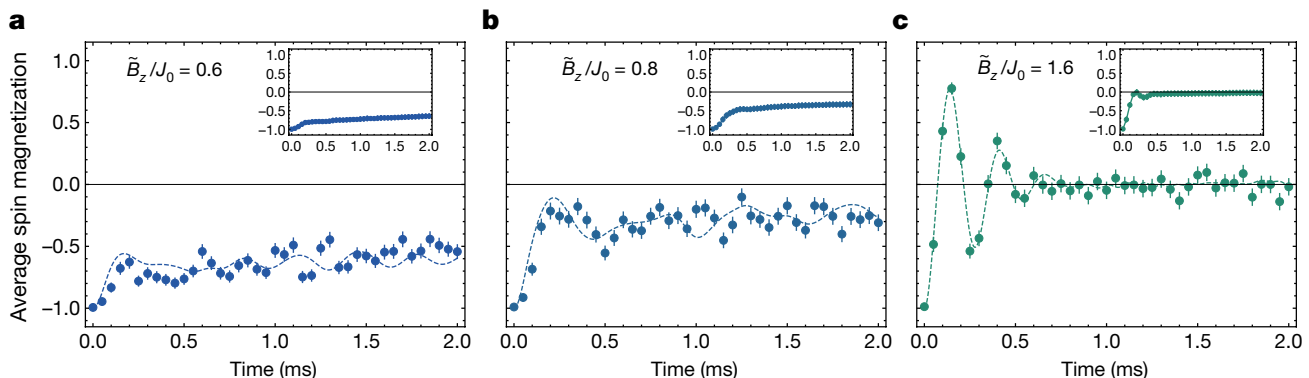
enables a fair comparison of the DPT for different numbers of spins in the chain.

The evolution of the time-dependent magnetization separates into two distinctive regimes: one that breaks the global  $\mathbb{Z}_2$  symmetry ( $\sigma_i^x \rightarrow -\sigma_i^x$ ) of the Ising Hamiltonian (Fig. 2a), as was set by the initial conditions explicitly, and one that restores this symmetry (Fig. 2c), with the intermediate time dynamics oscillating around and relaxing to zero average magnetization. Between these two regimes we observe a relaxation to a non-zero steady value (Fig. 2b). Cumulative time-averages (insets in Fig. 2)

$$\overline{\langle \sigma^x \rangle}(t) = \frac{1}{t} \int_0^t \langle \sigma^x(\tau) \rangle d\tau$$

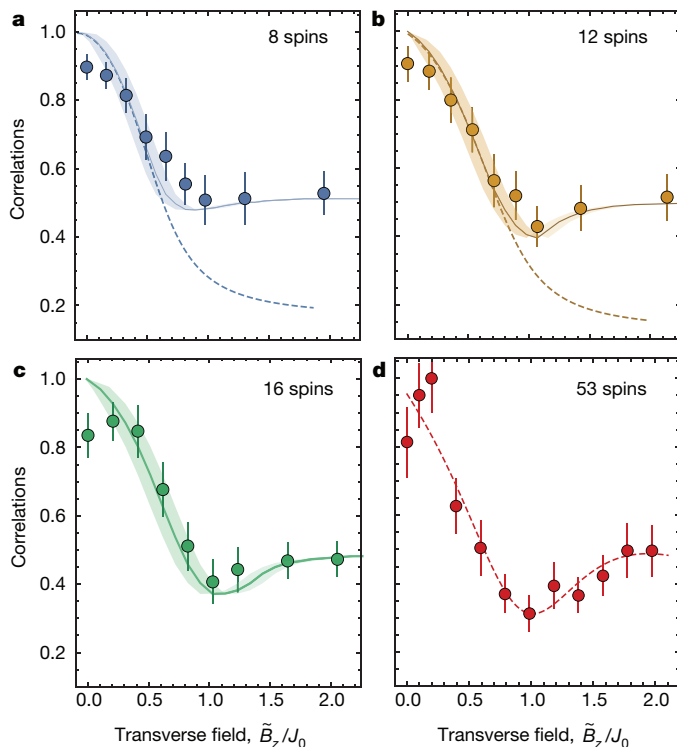
reveal the long-time magnetization plateaus.

The DPT is expected to occur between the small- and large-transverse-field regimes as the spin alignment changes abruptly from ferromagnetic to paramagnetic in the long-time limit (Fig. 1). This phase transition is well-established for  $\alpha = 0$ , as shown in Methods. There is strong numerical evidence that such a transition will survive<sup>20,29</sup> for the small values of  $\alpha$  chosen in our experiments, but not for  $\alpha \rightarrow \infty$ , in which case interactions are nearest-neighbour only.



**Figure 2 | Real-time spin dynamics after a quantum quench of 16 spins in an Ising chain.** **a**, Polarized spins evolve under the long-range Ising Hamiltonian with a small transverse field ( $\tilde{B}_z/J_0 = 0.6$ ). The broken symmetry given by the initial polarized state is preserved during the evolution. **b**, When the transverse field is increased ( $\tilde{B}_z/J_0 = 0.8$ ), the dynamics shows a faster initial relaxation, before settling to a non-zero plateau. **c**, Under larger transverse fields ( $\tilde{B}_z/J_0 = 1.6$ ), the Larmor

precession takes over and the spins oscillate and relax to zero average magnetization. The dashed lines are numerical simulations based on exact diagonalization. Insets show cumulative time averages of the spin magnetization, smoothing out temporal fluctuations and showing the plateaus. Each point is the average of 200 experimental repetitions. Error bars are statistical, computed from quantum projection noise and detection infidelities as described in Methods.



**Figure 3 | Two-body correlations.** **a–d**, Long-time-averaged values of the two-body correlations  $C_2$  over all pairs of spins as a function of the transverse field  $\tilde{B}_z/J_0$  for different numbers of spins in the chain. The final evolution times correspond to  $2\pi J_0 t = (10.3, 5.3, 4.8, 6.5)$  for 8 (**a**), 12 (**b**), 16 (**c**) and 53 (**d**) spins, respectively. Statistical error bars are  $\pm 1$  s.d. from measurements covering 21 different time steps. Solid lines in **a–c** are exact numerical solutions to the Schrödinger equation; the shaded regions take into account uncertainties from experimental Stark shift calibration errors. Dashed lines in **a** and **b** are calculations using a canonical (thermal) ensemble with an effective temperature corresponding to the initial energy density. For  $N = 53$  spins (**d**), the correlations are uniformly degraded from residual Stark shifts across the ion chain, so in this case we normalize to the maximum correlation at small field (see Methods). Exact diagonalization for  $N = 53$  spins is not possible, so we instead fit the experimental data to a Lorentzian function with linear background (dashed line).

Further signatures of the DPT are observed by measuring the spatially averaged two-spin correlations

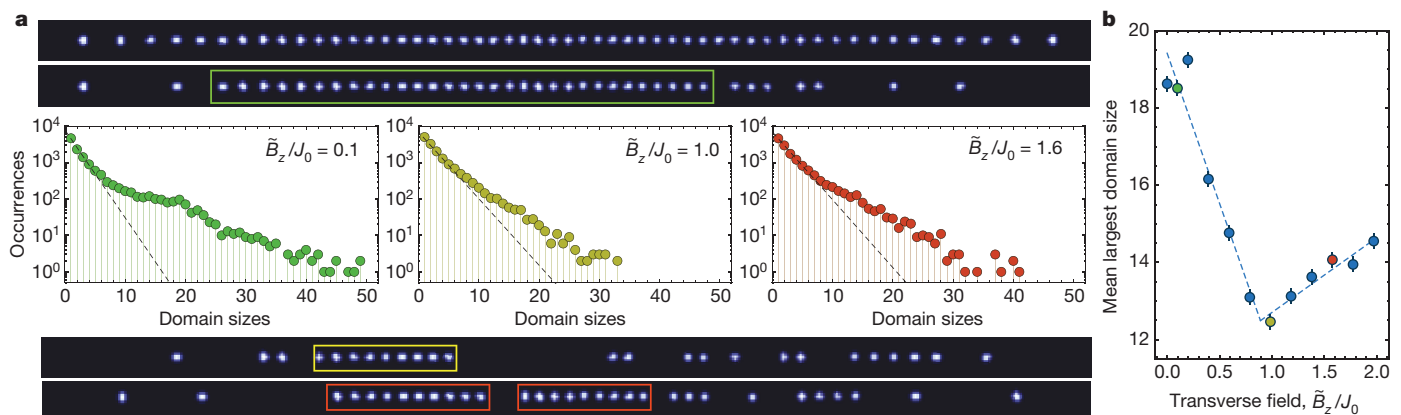
$$C_2 = \frac{1}{N^2} \sum_{i,j} \langle \sigma_i^x \sigma_j^x \rangle$$

From the behaviour of the magnetizations described above, we expect that  $C_2 \rightarrow 1$  for small  $\tilde{B}_z$  and  $C_2 \rightarrow 1/2$  for large  $\tilde{B}_z$  at long times, because the collective spin precesses around the  $z$  axis and  $C_2$  oscillates between 1 and 0. In Fig. 3 we show the cumulative time-averaged correlations. Near the critical value of  $\tilde{B}_z$  we observe the emergence of a dip in  $C_2$ , which is a direct signature of the DPT. The sharpening of the dip for larger system sizes is not strong, which might be due to a logarithmic finite-size scaling (see Methods).

For a non-integrable system such as the long-range transverse-field Ising model studied here, it might be conjectured that the spins eventually reach a thermal distribution<sup>30</sup>. However, we find that this is true only for small  $\tilde{B}_z$  (Fig. 3a, b). We note that the thermal values of the correlator  $C_2$  do not exhibit a dip or signatures of a phase transition with varying  $\tilde{B}_z/J_0$  for the system sizes that we are able to model numerically. Interestingly, thermalization appears to break down in this quenched system, which we suspect is a consequence of the inherent long-range nature of the Ising interactions<sup>31</sup>.

We further explore many-body dynamical properties of this system by investigating higher-order correlations, which are even harder to calculate classically<sup>25</sup>. Through high-efficiency single-shot state detection of all of the spins, we measure the distribution of domain sizes in the chain directly as a higher-order correlation observable (see Methods). Single-shot images for  $N = 53$  spins are shown in Fig. 4a and are reconstructed from binary thresholding and image convolution of the fluorescence distribution of the ion chain (see Methods).

The occurrence of long domains of correlated spins in the state  $|\uparrow\rangle_x$  (fluorescing spins) signifies the fully polarized initial state, in which the correlations are largely preserved by the interactions. With an increasing transverse field, the absence of spin ordering is reflected by exponentially small probabilities of observing long strings. We plot the domain length statistics at late times in Fig. 4a (see Methods) for three transverse field strengths,  $\tilde{B}_z/J_0 = (0.1, 1.0, 1.6)$ . The dashed lines in Fig. 4a are fits to exponentials on the histogram of domain sizes. The rare occurrence of especially large domains (see, for example, the red boxes in Fig. 4a) demonstrates the existence of many-body high-order



**Figure 4 | Domain statistics and reconstructed single-shot images of 53 spins.** **a**, Top and bottom, reconstructed images based on binary detection of spin states (see Methods). The top image shows a chain of 53 ions in ‘bright’ (corresponding to  $|\uparrow\rangle_x$ ) spin states. The other three images show 53 ions in combinations of ‘bright’ and ‘dark’ (corresponding to  $|\downarrow\rangle_x$ ) spin states. Centre, statistics of the domain size, or of blocks with spins pointing along the same direction, for different values of the transverse field. Histograms are plotted on a logarithmic scale to visualize the rarity of regions with large domains; example large domains for the different transverse fields (coloured coded) are boxed in the top and bottom images.

Dashed lines are fits to exponential functions, which are expected for a thermal state of the spins and could thus characterize defects such as imperfect preparation and measurement of the qubits. Long tails of deviations from the exponential are clearly visible, and vary depending on  $\tilde{B}_z/J_0$ . **b**, Mean largest domain size over the repeated single experimental shots. Error bars are the standard deviation of the mean (see Methods). Dashed line represents a piecewise linear fit, from which we extract the transition point (see text). The green, yellow and red data points correspond to the transverse fields shown in the domain statistics data in **a**.

correlations, with the order given by the length of the domain. In Fig. 4b we plot the mean largest domain size as a function of the normalized transverse field strength, for late times and repeated experimental shots. The average longest domain size ranges from 12 to 20 and exhibits a sharp transition across the critical point of the DPT. We fit this observable using a piecewise linear function and extract the critical point to be  $\tilde{B}_z/J_0 = 0.89(7)$  (see Methods for more details).

The DPT studied here, with up to 53 trapped-ion qubits, is to our knowledge the largest quantum simulation ever performed with high-efficiency single-shot measurements of individual qubits. This provides access to arbitrary many-body correlators that carry information that is difficult or impossible to model classically. This experimental platform can be extended to tackle provably hard quantum problems such as Ising sampling<sup>32</sup>. Given an even higher level of control over the interactions between spins, as already demonstrated for smaller numbers of trapped-ion qubits<sup>33</sup>, this same system can be upgraded to a universal quantum computer.

**Online Content** Methods, along with any additional Extended Data display items and Source Data, are available in the online version of the paper; references unique to these sections appear only in the online paper.

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## METHODS

**Confinement of long ion chains.** The ion chain is confined in a three-layer linear Paul trap with a transverse centre-of-mass motional frequency<sup>34</sup> of  $\nu_{\text{cm}} = 4.85$  MHz. The harmonic axial confinement is kept low enough that the lowest energy conformation of the ions is linear; for 8–16 ions the axial centre-of-mass frequency is about 400 kHz and for 53 ions it is about 200 kHz. The ion spacing is anisotropic across the chain, with typical spacings of 1.5  $\mu\text{m}$  at the centre of the chain and 3.5  $\mu\text{m}$  at either end<sup>35</sup>.

The effective lifetime of an ion chain is limited by Langevin collisions with the residual background gas in the ultrahigh-vacuum apparatus<sup>36</sup>, which in general re-order the crystal but can also melt the crystal and even ultimately eject the ions as a result of radio-frequency heating or other mechanisms. The chain melting can be mitigated by quickly re-cooling the chain, and we expect that occasionally it returns to the crystalized phase without notice. Occasionally, such collisions with the background gas are inelastic, either populating the  $^{171}\text{Yb}^+$  ion in the metastable  $F_{7/2}$  state or forming a  $\text{YbH}^+$  molecule. The 355-nm Raman laser quickly returns the ions to their atomic ground-state manifold, with a small probability of creating doubly charged ions. The mean time between Langevin collisions is expected to be of the order of one collision per hour per trapped ion, and we expect that the mean lifetime of a chain of ions might therefore scale inversely with the number of ions. For 53 ions we observe an average lifetime of about 5 min. However, we observe rare events whereby a long ion chain survives for about 30 min. We speculate that either the chain is consistently re-captured instantaneously, or the local pressure in the chamber is anomalously low during these periods. Because we can load an ion chain in less than 1 min, we achieve a reasonable duty cycle of collecting data. To further scale up the system size, a cryogenic ion trap system could be used to efficiently reduce the pressure and the collision energies, which could enable quantum simulations with well over 100 ions.

**State preparation.** Two off-resonant laser beams at 355 nm globally address the ions and drive stimulated Raman transitions between the two hyperfine qubit clock states  $^2S_{1/2}|F=0, m_F=0\rangle$  and  $|F=1, m_F=0\rangle$ . The Raman beatnotes (frequency difference between two beams) are provided by the frequency comb from the mode-locked laser, resulting in coherent qubit rotations<sup>37,38</sup>. The ion chain is about 100  $\mu\text{m}$  in length, and the beams are focused to a 200- $\mu\text{m}$  full-width at half-maximum along the ion chain, resulting in a 30%–40% intensity imbalance between the centre and edges of the chain. To prepare each individual ion in the  $|\downarrow\rangle_x \equiv |\downarrow\rangle_z - |\uparrow\rangle_z$  state, we first optically pump the ions in the  $|\downarrow\rangle_z$  state with an efficiency of more than 99%<sup>37</sup> and then apply a  $\pi/2$  rotation around the  $y$  axis. However, if we use a single pulse for the rotation, then the inhomogeneity of the beam leads to reduced Rabi frequencies near the edge of the chain and hence an imperfect qubit rotation to the desired initial state.

To mitigate this effect, we use a composite pulse compensation sequence (BB1 dynamical decoupling<sup>39</sup>), written for each spin  $i$  as

$$U_i(\pi/2) = \exp\left(-i\frac{\pi}{2}\sigma_i^\theta\right)\exp(-i\pi\sigma_i^\theta)\exp\left(-i\frac{\pi}{2}\sigma_i^\theta\right)\exp\left(-i\frac{\pi}{4}\sigma_i^y\right)$$

where, in addition to the  $\pi/2$  rotation  $\exp(-i\pi\sigma_i^y/4)$ , three additional rotations are applied: a  $\pi$  pulse along an angle  $\theta = \cos^{-1}(-1/16) = 93.6^\circ$ , a  $2\pi$  pulse along  $3\theta$ , and another  $\pi$  pulse along  $\theta$ , where the axes of these additional rotations are in the  $x$ - $y$  plane of the Bloch sphere with the specified angle referenced to the  $x$  axis. With this scheme, we estimate a state preparation fidelity of up to 99% per spin for the well-compensated ions at the middle of the chain, and an average fidelity of 93%, limited by the ions at the edges of the chain.

**Generating the Ising Hamiltonian.** We generate spin–spin interactions by applying a spin-dependent optical dipole force that is induced by the global Raman beams, which are aligned with a wavevector difference  $\Delta k$  along a principal axis of transverse motion<sup>34</sup>. Two beatnotes of the non-copropagating Raman beams are tuned near the transverse upper and lower motional sideband frequencies at  $\nu_0 \pm \mu$ , in the usual Mølmer–Sørensen configuration<sup>40</sup>. In the Lamb–Dicke regime, this gives rise to the Ising-type Hamiltonian<sup>34</sup> in equation (1) with Ising coupling between ions  $i$  and  $j$ ,

$$J_{ij} = \Omega^2 \nu_R \sum_m \frac{b_{im} b_{jm}}{\mu^2 - \nu_m^2} \approx \frac{J_0}{|i-j|^\alpha} \quad (2)$$

Here  $\Omega$  is the global (carrier) Rabi frequency,  $\nu_R = \hbar \Delta k^2 / (8\pi^2 M)$  is the recoil frequency,  $b_{im}$  is the normal-mode transformation matrix of the  $i$ th ion with the  $m$ th normal mode ( $\sum_i |b_{im}|^2 = \sum_m |b_{im}|^2 = 1$ )<sup>35</sup>,  $M$  is the mass of a single ion and  $\nu_m$  is the frequency of the  $m$ th normal mode. Here, the beatnote frequency detuning  $\mu$  is assumed to be sufficiently far from all sidebands,  $|\mu - \nu_m| \gg \Omega b_{im} \sqrt{\nu_R / \nu_m}$ , so that the spins only couple through the motion virtually and phonon production is suppressed.

The approximate power-law exponent in equation (2) can in principle be tuned in the range  $0 < \alpha < 3$ , but in practice we are restricted to  $0.5 < \alpha < 1.8$  so as to avoid motional decoherence and experimental drifts. We set  $\alpha$  to be roughly constant across different system sizes by adjusting the detuning from the nearest (centre-of-mass) sideband to the values  $\mu - \nu_m = (56, 69, 82, 60)$  kHz for  $N = (8, 12, 16, 53)$  ions, with respective nearest-neighbour Ising couplings  $J_0 = (0.82, 0.56, 0.38, 0.65)$  kHz. For the case of 53 spins, we use a higher Raman laser intensity to produce a relatively high Ising coupling strength, and whereas  $\alpha \approx 0.8$  for  $N = (8, 12, 16)$ ,  $\alpha \approx 1$  for  $N = 53$ .

The ratio of the spontaneous emission rate from the off-resonant Raman beams to the Ising coupling is expected to be less than 0.003 for  $N = 53$  ions. However, as the system is scaled to larger numbers of spins, the intensity must ultimately be reduced to prevent the creation of phonons from the increasing number of nearby sideband transitions. The residual entanglement between phonons and spin would lead to effective spin decoherence. The scaling of these errors with the number of spins depends on the details of the Ising interactions and sideband detuning, but holding these parameters constant while keeping phonon errors low will lead to a ratio of spontaneous emission to Ising coupling that is expected to grow as  $\sqrt{N}$ . Nevertheless, these fundamental sources of decoherence are not expected to be substantial, even for hundreds of spins.

With  $\alpha < 1$ , the long-range interaction term in the Hamiltonian in equation (1) is non-extensive for a one-dimensional linear chain. To have a well-defined thermodynamic limit of the Hamiltonian, the couplings are typically rescaled to  $\tilde{J}_{ij} = J_{ij}/N$  using the Kac normalization constant<sup>41</sup>

$$\mathcal{N} = \frac{1}{N} \sum_{i,j} \frac{J_{ij}}{J_0}$$

Because all of our observables are functions of the ratio of the field to the Ising coupling strength ( $B_z/J_0$ ), we instead equivalently renormalize the magnetic field using  $\tilde{B}_z = B_z/\mathcal{N}$  and retain the original form of the Ising coupling.

**Generating the transverse magnetic field.** To generate the effective magnetic field, we adjust the two Raman beatnotes asymmetrically to  $\nu_0 \pm \mu + B_z$ , resulting in a uniform effective transverse magnetic field of  $B_z$  in equation (1) (not yet Kac-normalized as described above).

To induce the quantum quench, the sidebands are switched on in about 100 ns using acousto-optic modulators, which control the detuning and amplitude of the Raman beatnotes. These two beatnotes correspond to different beam angles out of the acousto-optic modulator, so we image these beams onto the ion chain to maximize the overlap of all frequency components. We measure a residual effective linear gradient of magnetic field across the chain, resulting from a fourth-order Stark shift gradient<sup>42</sup> that arises from the non-perfect overlap of the two beatnotes. This effect is measured to be  $\Delta B_z = \pm 0.65$  kHz end-to-end on a 16-ion chain, and was included in the numerics. This gradient is dominated by uniform magnetic fields  $B_z > 2$  kHz, but still plays a part at zero or small magnetic fields, causing an effective depolarization of the initial state  $|\downarrow\downarrow\downarrow\downarrow\rangle_x$ . Additional spin depolarizations can be caused by Stark-shift fluctuations and calibration errors, or by residual spin–phonon coupling. These effects are responsible for the slight decay that is seen in Fig. 2a and for the zero-field error in Fig. 3c, d.

**Single-shot detection and image processing.** We detect the ion spin state by globally rotating all of the spins into the measurement basis (composite (BB1)  $\pi/2$  pulse as describe above, to rotate  $x$  basis into  $z$  basis), followed by the scattering of resonant laser radiation on the  $^2S_{1/2}|F=1\rangle - ^2P_{1/2}|F=0\rangle$  cycling transition (wavelength near 369.5 nm and radiative line width  $\gamma/2\pi \approx 20$  MHz). The  $|\uparrow\rangle_z$  ‘bright’ state fluoresces strongly whereas the  $|\downarrow\rangle_z$  ‘dark’ state fluoresces almost no photons because the laser is far from resonance<sup>37</sup>.

The fluorescence of the ion chain is imaged onto an electron-multiplying (EM) CCD camera (Model Andor iXon 897) using an imaging objective with a numerical aperture of 0.4 and a magnification of 60. The fluorescence of each ion covers roughly a  $5 \times 5$  array of pixels on the EMCCD. After collecting the fluorescence for an integration time of 300  $\mu\text{s}$ , we collect a mean of about 20 photons per bright ion, distributed in a circular region of interest around the centre of the ion’s position. In every single shot, we use a simple binary threshold to determine the state of each ion ( $|\downarrow\rangle_z$  or  $|\uparrow\rangle_z$ ), providing a binary detection of the quantum state of any ion with nearly 99% accuracy. The residual 1% errors include off-resonant optical pumping of the ion between states during detection, readout noise and background counts, and crosstalk between adjacent ions.

The regions of interest of the individual ions on the camera are determined from periodically acquiring diagnostic images, whereby a resonant re-pumper laser is applied, causing each ion to fluoresce strongly regardless of its state. The signal-to-background-noise ratio in the diagnostic shots is larger than 100, yielding precise knowledge of the centre locations. Ion separations range from 1.5  $\mu\text{m}$  to 3.5  $\mu\text{m}$  depending on the trap settings and the distance from the chain centre, and are

always much larger than the resolution limit of the diffraction-limited imaging system ( $500_{-0}^{+100}$  nm Airy ring radius projected at the ion position). We use the pre-determined ion centres to process the individual detection shots, and optimize the integration area on the EMCCD camera to collect each ion's fluorescence while minimizing crosstalk. We estimate crosstalk to be dominated by nearest-neighbour fluorescence, which can bias a dark ion to be erroneously read as bright with less than 1% probability. The larger inhomogeneities of inter-ion spacings near the edge of the chain do not introduce additional infidelities, as long as they are well illuminated by the detection laser beam.

**Statistical data analysis of domain size.** Here we present a detailed analysis of the domain statistics presented in Fig. 4. The domain size is directly related to 'formation probabilities', which have recently attracted theoretical interest<sup>43</sup>. The raw domain statistics are analysed from the binary tally of bright and dark ions, after sorting them into domains with consecutive spins up (bright) or down (dark). The collection of all 200 experimental repetitions for the last 5 time steps (out of 21 time steps overall) are treated equally, resulting in the distribution shown in Fig. 4a. The particular choice of the last 5 time steps is a compromise between being insensitive to early-time dynamics in the magnetic field and increasing the sample size for reduced statistical errors.

To analyse the large domains, or the outliers of the distributions in Fig. 4, we find the largest domain in each single shot and plot the statistical distribution in Extended Data Fig. 1. In the main text, the mean (standard error of the mean) is used to extract the data (error bars) presented in Fig. 4b. This has an underlying assumption that the central limit theorem holds for our largest-domain-size statistics.

We analyse the distribution in the observed data and fit the histogram to a two-parameter Gamma distribution, shown as the dashed lines in Extended Data Fig. 1. From the fit parameters we extract the mean, taking the skewness of the distribution into account. This systematically shifts the largest domain size by about 1 for all datasets, and a piecewise fit similar to that described in the main text yields the critical point  $\tilde{B}_z/J_0 = 0.92(7)$  from this alternative method of data analysis, in good agreement with that obtained in the main text. As a comparison with theory, in Extended Data Fig. 2 we plot the observed mean domain size for 16 spins next to an exact calculation of the mean domain size under the same conditions. The general trend of the data is qualitatively reproduced by theory, although the extremes are tempered in the data, possibly from imperfections in the preparation or measurement of the spins and inhomogeneous fields.

**Analytical study of the DPT for  $\alpha = 0$ .** In this section, we show analytically that in the limit  $\alpha \rightarrow 0$  ( $J_{ij} = J_0$  for  $i \neq j$ ) the spatially averaged two-point correlation  $C_2$  measured in the experiment undergoes a DPT when  $\tilde{B}_z/J_0$  crosses unity, in the thermodynamic and long-time limit. (The average magnetization  $\langle \sigma^x \rangle$  (ref. 43) undergoes a similar DPT, but the second-order correlator that we study here has the advantage that its infinite-time average can be used as a static order parameter.) The case  $\alpha \approx 1$  in our experiment cannot be treated analytically or numerically for large system sizes, but appears to have dynamics qualitatively similar to the  $\alpha = 0$  case treated here analytically.

We first rewrite the Hamiltonian for  $\alpha = 0$

$$H_0 = \frac{J_0}{N} (\Sigma^x)^2 + \tilde{B}_z \Sigma^z \quad (3)$$

using collective spin operators

$$\Sigma^{x,y,z} = \sum_{i=1}^N \sigma_i^{x,y,z}$$

Here the Ising interactions are normalized to make  $H_0$  extensive (see above), which enables a well-defined thermodynamic limit. According to the Heisenberg equation, we have (setting  $\hbar = 1$ )

$$\frac{d\Sigma^x}{dt} = i[H_0, \Sigma^x] = -2\tilde{B}_z \Sigma^y$$

We note that the thermodynamic limit ( $N \rightarrow \infty$ ) coincides with the semi-classical limit for the Hamiltonian in equation (3). We can thus assign to the values of  $\Sigma^{x,y,z}$  classical vectors of length  $N$  on a Bloch sphere:  $(\Sigma^x, \Sigma^y, \Sigma^z) = N(\cos\theta, \sin\theta\sin\phi, \sin\theta\cos\phi)$ . The above equation of motion can then be reduced to

$$\frac{d\theta}{dt} = 2\tilde{B}_z \sin\phi$$

together with the equation  $\cos\phi = (J_0/\tilde{B}_z)\sin\theta$  that comes from energy conservation.

Given the initial state  $\theta(t=0)=0$ , the dynamics of the correlation  $C_2 = \cos^2\theta$  can be obtained analytically. In the long-time limit, we find a time-averaged value of

$$\begin{aligned} \overline{C_2}(\infty) &\equiv \lim_{T \rightarrow \infty} \frac{1}{T} \int_0^T \langle C_2(t) \rangle dt \\ &= \frac{\int_0^\xi \frac{\cos^2\theta d\theta}{2\sqrt{(\tilde{B}_z/J_0)^2 - \sin^2\theta}}}{\int_0^\xi \frac{d\theta}{2\sqrt{(\tilde{B}_z/J_0)^2 - \sin^2\theta}}} \end{aligned} \quad (4)$$

where  $\xi = \sin^{-1}[\min(|\tilde{B}_z/J_0|, 1)]$ . We plot  $\overline{C_2}(\infty)$  as a function of  $\tilde{B}_z/J_0$  in Extended Data Fig. 3. A sharp dip is observed, confirming the existence of the DPT.

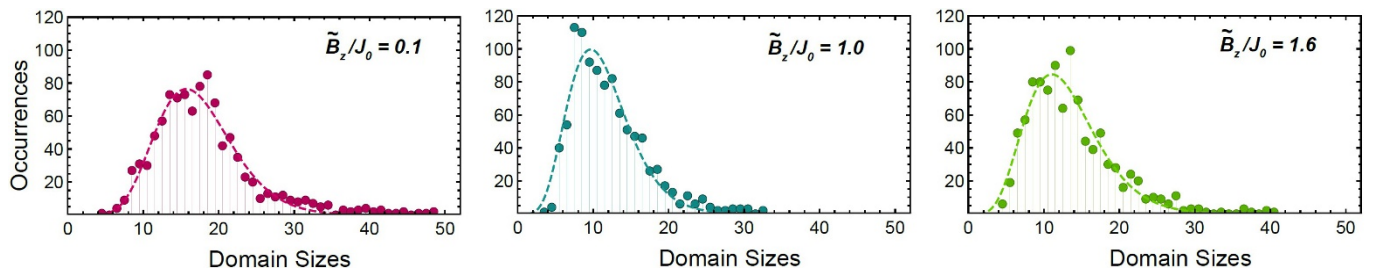
To understand how  $\overline{C_2}(\infty)$  at  $\tilde{B}_z/J_0 = 1$  scales with  $N$ , we note that although there are only  $N+1$  orthogonal quantum states for the collective spin  $\Sigma$  with length  $N$ , the Bloch sphere has a surface area of  $4\pi$ . Thus, each orthogonal quantum state occupies a small area on the Bloch sphere with a radius that scales as  $1/\sqrt{N}$ , owing to the usual uncertainty relation between the different projections of spin. As a result, the upper limit of the integral over  $\theta$  in equation (4) can reach only  $\pi/2 - \varepsilon$ , with  $\varepsilon \sim 1/\sqrt{N}$  as  $N \rightarrow \infty$ . It can therefore be shown that for large  $N$

$$\lim_{\tilde{B}_z/J_0 \rightarrow 1} \overline{C_2}(\infty) \sim \frac{1}{\log(N)}$$

We conclude that the size of the dip in the DPT decreases logarithmically with  $N$ , which may qualitatively explain why only a weak sharpening of the DPT is observed in the experiment as the spin chain grows in size.

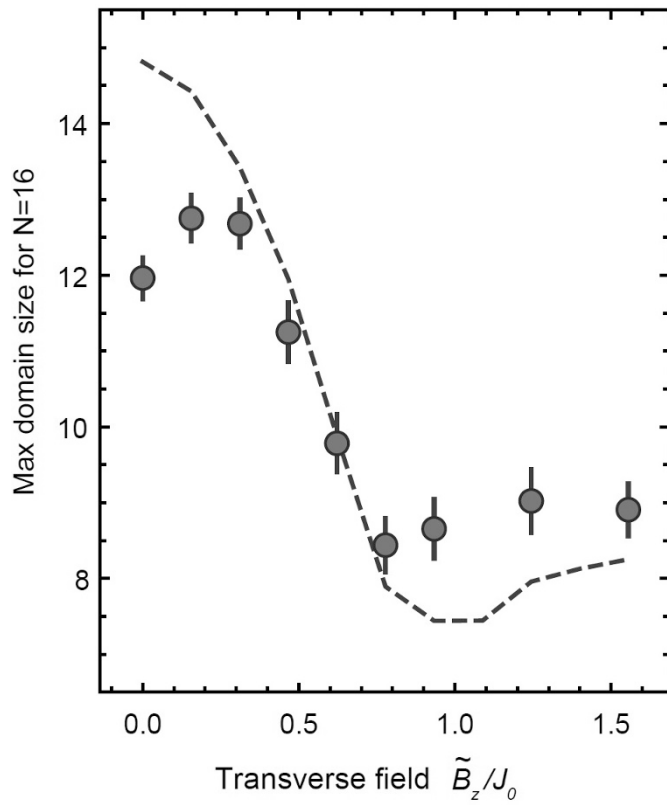
**Data availability.** The data presented in the figures and that support the other findings of this study are available from the corresponding author on reasonable request.

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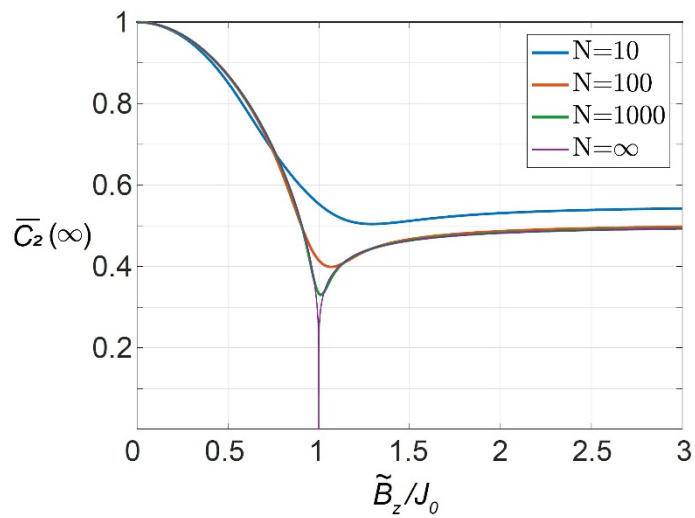
**Extended Data Figure 1 | Distributions of the largest domain size.** Statistics of the largest domain size in each experimental shot (200 experiments for each of the last 5 time steps). Considering only the largest domains of each shot eliminates the undesirable biasing towards small domain sizes that is present in Fig. 4a. Domain sizes are related

to many-body correlators, with a domain size of  $N$  corresponding to an  $N$ -body correlator. Dashed lines are fits to a two-parameter Gamma distribution proportional to  $e^{-x/\beta}x^{\alpha-1}$ , with shape parameter  $\alpha$  and scale parameter  $\beta$ .



**Extended Data Figure 2 | Domain size observable for 16 spins.** Mean maximum domain size as a function of the (Kac-normalized<sup>41</sup>) transverse field for 16 spins. Experimental data are analysed as for Fig. 4b. The dashed line is a numerical simulation of the Hamiltonian determined from the experimental parameters. Error bars, 1 s.d.





**Extended Data Figure 3 | Theoretical calculations of the correlations.** The spatially and long-time averaged correlation  $\bar{C}_2(\infty)$  (defined in equation (4)), calculated as a function of  $\tilde{B}_z/J_0$  for  $\alpha = 0$ . The finite- $N$  curves are calculated using exact diagonalization; the  $N = \infty$  curve is calculated analytically from equation (4).