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Symmetric Authenticated Tunneling Protocol Analysis

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Chapter 1: Introduction

1.1 Abstract

Secure Authenticated Tunnel Protocol, SATP, is a symmetric key secure channel protocol designed for environments in which asymmetric cryptography is impractical or undesired. The protocol constructs secure channels by combining a hierarchical symmetric key tree, deterministic domain separated key derivations, a server side validation mechanism derived from a long term secret, and a second stage user authentication procedure executed inside an encrypted tunnel. All encrypted traffic is protected by an authenticated encryption construction that binds timestamps, sequence numbers, and packet headers as associated data, which enforces replay and reordering resistance. The client erases its derived device key after session establishment, which provides a limited form of forward secrecy that protects past sessions after client compromise. The server, however, retains the ability to regenerate device keys from branch keys, which introduces structural security boundaries that must be examined carefully.

This work constructs a formal, code aligned, and mathematically precise analysis of SATP. The evaluation reconstructs the protocol state machine from the specification and implementation, formalizes the complete key schedule, defines the authenticated encryption channel precisely, and proves confidentiality, integrity, server authentication, client authentication, and replay resistance under standard adversarial models. The analysis also characterizes the consequences of deterministic derivation, the hierarchical key structure, and the absence of asymmetric mixing. The result is a corrected and

comprehensive cryptanalysis of SATP that reflects the protocol as implemented rather than an idealized variant.

1.2 Problem Statement and Object of Study

SATP seeks to provide an authenticated and confidential communication channel across an untrusted network using only symmetric cryptography. The server holds a root key for its deployment domain, branch keys derived from this root key, and device keys derived deterministically from branch keys and client identity strings. The client possesses only its own device key along with a user supplied passphrase. The cryptographic workflow begins with a Connect Request that identifies the client and provides a freshly generated session nonce. Both sides then derive, in a strictly deterministic and domain separated fashion, the session encryption keys and nonces. The server responds with a Connect Response that contains an encrypted validation value computed from the device key, the session nonce, and an additional server secret. The client verifies this value before accepting the tunnel. Only after this validation step does SATP perform a separate user authentication sequence inside the encrypted channel using a hardened memory cost function and a stored verifier.

This report examines SATP exactly as defined by the SATP specification at /mnt/data/satp_specification.pdf and the C implementation at /mnt/data/satp.c, /mnt/data/satp.h, and the associated connection and key exchange modules. The object of study is therefore the full protocol state machine, the precise derivations of Kbr, Kc,i, Rk, Rn, Tk, and Tn, the format of every SATP packet, the server generated validation hash, the SCB based user authentication sequence, and the authenticated encryption channel that processes encrypted data. The goal is to analyze the protocol that actually exists, not an abstraction or simplified representation.

1.3 Protocol Elements Under Analysis

SATP consists of several interdependent components that collectively determine its security posture. The hierarchical key derivation mechanism determines the generation of all device keys and therefore governs trust distribution and compromise boundaries. The session key derivation procedure, which is driven by the client supplied nonce and the configuration string found in the implementation, determines the entropy and independence of each session. The server side validation mechanism integrates the session nonce, the derived device key, and a long term server secret, and forms the foundation of the first stage of authentication. After this, the passphrase based user

authentication verifies the legitimacy of the client within the encrypted tunnel. The authenticated encryption mechanism ties these components together by binding timestamps, sequence numbers, and packet headers as mandatory associated data. All of these components must be analyzed together because security failures in any single component can propagate across the entire protocol.

The implementation contains several details that impose specific security properties that must be included in the analysis. The derived device key is erased by the client immediately after session key expansion, but the server retains the ability to regenerate it using the branch key. Session nonces are supplied only by the client, which fixes the entropy source driving key separation. Timestamps and sequence numbers evolve monotonically on both sides and their correctness is required for successful decryption. These details are not optional enhancements but central elements that must be accounted for when determining confidentiality, integrity, authentication strength, and replay resistance.

1.4 Security Goals and Adversarial Model

The security goals of SATP include confidentiality of encrypted payloads, integrity and authenticity of all ciphertext and associated data, server authentication at the protocol level, client authentication at the user level, and replay resistance enforced through timestamp and sequence number binding. These goals must be evaluated with respect to an adversary that controls the network, can reorder, duplicate, modify, and delay packets arbitrarily, and can initiate interactions with honest parties at will. The adversary is allowed to compromise either a client or a server branch key. Client compromise reveals the passphrase and derived device key but not the unattenuated branch key. Server branch key compromise allows regeneration of device keys for that branch and therefore invalidates forward secrecy for all devices under it.

The adversary is assumed to have full transcripts of past traffic, knowledge of client identity strings, configuration strings, timestamps, sequence counters, header flags, and all other values that appear in the clear. The cryptographic assumptions underlying the analysis include the pseudorandom behavior of SHAKE256 output when keyed by unknown inputs and the IND CCA and INT CTXT security of the AEAD primitive selected at compile time. No assumptions are made about secrecy of identity strings or any public configuration parameter.

1.5 Method of Evaluation

The analysis proceeds by reconstructing the protocol's state machine directly from the specification and source code. This reconstruction identifies every transition between unauthenticated, server authenticated, client authenticated, and established states, and identifies the precise cryptographic inputs and outputs used at each transition. The key hierarchy and derivation functions are modeled as explicit mathematical functions, with all domain separation and structural properties spelled out using the exact ordering, concatenation, and argument placement found in the specification.

Security proofs are provided as standard reductions. For confidentiality, we show that any adversary who distinguishes the encryption of two chosen plaintexts under a fresh SATP session key can be converted to an adversary that distinguishes two messages under the underlying AEAD scheme, contradicting its IND CCA security. For integrity, we show that any adversary who constructs a new ciphertext that verifies under an honest key can be used to construct a forger against the AEAD primitive. For server authentication, we show that producing an accepted validation hash without the server secret and device key requires preimage control over SHAKE256. For replay resistance, we show that any successful replay attack must violate the monotonicity of timestamps and sequence numbers or the binding of associated data in the AEAD construction. Forward secrecy is evaluated by examining the erasure of device keys by the client and the reconstruction capability available to the server.

All proofs are cross checked against the actual control flow of the code, including the precise format of associated data, the handling of derived keys, the ordering of bytes in the session nonce, the validation hash computation, and the SCB based user authentication sequence.

1.6 Deliverables and Structure

This document produces a complete cryptanalysis of SATP that is aligned with the normative specification and the real implementation. It delivers a precise and fully formal key schedule, a clear protocol state machine, a mathematically correct set of security reductions, an analysis of structural limitations that arise from the hierarchical key design, and a set of rigorously derived conclusions regarding the confidentiality, integrity, authentication, and replay properties of the protocol.

The remainder of the report develops the protocol formally, analyzes the cryptographic constructions used in each stage, and proves the properties claimed above. Later chapters also identify structural features that limit forward secrecy and discuss

operational considerations implied by deterministic derivation and asymmetric authority. The final chapter summarizes the results and outlines directions for hardening the protocol without altering its core architectural principles.

Chapter 2: Problem Statement and Scope

2.1 Overview of the Analytical Objective

The objective of this analysis is to evaluate the security of SATP as it is actually defined by its specification and implemented in the provided C codebase. SATP is a symmetric key secure channel protocol designed to provide confidentiality, integrity, replay protection, server authentication, and user authentication without relying on asymmetric primitives. Its construction hinges on a layered symmetric key hierarchy, deterministic domain separated derivation functions, a validation mechanism that binds the device key to fresh session material, and an authenticated encryption channel that enforces strict replay semantics.

In this chapter we formalize the exact problem the cryptanalysis addresses, establish the constraints imposed by the protocol's structure, and define the boundaries within which all subsequent proofs and evaluations operate.

2.2 Core Elements Requiring Analysis

SATP is composed of multiple interacting components. Each of these components is security relevant and must be analyzed together, since a flaw in any one of them can compromise the full system.

The analysis focuses on the following protocol elements:

- **Hierarchical key structure**, consisting of a root key Kroot, branch keys Kbr, and per device keys Kc,i, all derived through SHAKE256 with explicit domain separation fields.
- **Session key derivation**, where both peers compute (Rk, Rn, Tk, Tn) from (Kc,i, cfgs, Nh), with Nh provided solely by the client.
- **Server validation mechanism**, in which the server authenticates itself using $H_c = \text{SHAKE256}(Nh, Kc,i, STc)$ and transmits it through an encrypted and authenticated Connect Response.

- **User authentication sequence**, performed after raising the tunnel, using a passphrase hardened by the SCB key derivation function and a stored verifier. This stage governs transition to the fully established state.
- **Authenticated encryption channel**, driven by the chosen AEAD primitive and binding the timestamp, sequence number, and header flag as mandatory associated data.
- **Replay and ordering constraints**, enforced by monotonic timestamps and sequence counters that are validated at every decryption attempt.
- **Connection and authentication state machine**, which determines how an endpoint transitions from unauthenticated, to server authenticated, to client authenticated, and finally to established.

These elements define the cryptographic behavior of the protocol and therefore form the scope of the formal analysis.

2.3 Problem Definition within the SATP Architecture

SATP attempts to solve a practical and well defined problem: establish a mutually authenticated encrypted tunnel between a client and an authoritative server using only symmetric cryptography. The constraints imposed on the design shape the cryptographic questions the analysis must answer.

The protocol is inherently asymmetric. The server occupies a privileged position because it can regenerate any device key derived from the branch key, while the client has access only to its own derived device key and user passphrase. The handshake is thus driven entirely by a client supplied nonce, after which the server authenticates itself through the validation hash and completes a symmetric expansion that both sides compute identically. Authentication of the user occurs only after a secure tunnel has been created.

Given this structure, the precise problem under evaluation is as follows:

1. Determine whether the session keys derived from $(K_{c,i}, \text{cfgs}, Nh)$ provide confidentiality and integrity at the AEAD layer.
2. Determine whether the server validation hash guarantees that only a legitimate server can produce an acceptable Connect Response.

3. Determine whether the user authentication process provides binding of the passphrase to the established session.
4. Determine whether timestamps and sequence numbers prevent replay and reordering under a network adversary.
5. Determine what forward secrecy is achieved, and under what compromise assumptions it fails, given the hierarchical nature of key derivation.
6. Determine whether the implementation enforces the security assumptions required by the specification.

These questions represent the core of the protocol's intended security behavior.

2.4 Adversarial Model and Environmental Constraints

The adversarial model used in this cryptanalysis is consistent with established models for secure channel protocols. The adversary controls the network, observes all traffic, and can replay, drop, modify, or reorder packets without limitation. The adversary can also initiate its own SATP sessions with either party and interleave protocol runs arbitrarily.

Two additional types of compromise are explicitly included, because SATP's structure makes them unavoidable aspects of security evaluation:

- **Client compromise**, in which the adversary learns the device key and the passphrase after the client has completed past sessions.
- **Branch key compromise**, in which the adversary learns the server's branch key and can reconstruct all device keys under that branch.

We assume the adversary does not break the cryptographic assumptions of the primitives. Specifically, SHAKE256 is modeled as a pseudorandom function when keyed by unknown inputs, and the AEAD primitive is assumed IND CCA and INT CTXT secure.

This adversarial model allows us to evaluate SATP's security at the level where protocol correctness and implementation alignment are decisive.

2.5 Analytical Scope and Excluded Domains

The scope of the cryptanalysis is determined strictly by the SATP specification and the behavior of the C implementation. The analysis includes every code path involved in:

- key derivation,

- handshake and validation,
- user authentication,
- AEAD encryption and decryption,
- replay checks,
- session state transitions.

Several topics are explicitly outside the scope of this document. These include physical side channel vulnerabilities, key storage hygiene beyond what the protocol requires, selection of user passphrases, integration concerns in higher level systems, resilience to denial of service, and the security of unrelated cryptographic primitives. SATP does not attempt to provide forward secrecy against server compromise and therefore such properties are not analyzed, except where structurally relevant to session derivation.

Finally, the scope does not include hypothetical variants of SATP, extensions to multi party communication, or substitutions of alternative primitives. The analysis concerns the SATP that exists, not a design space of possible alternatives.

2.6 Analytical Commitments for Later Chapters

The remainder of the report builds upon the problem and scope articulated here. Later chapters will:

- Model SATP's key derivation functions as explicit algebraic objects and prove their domain separation and collision resistance properties under SHAKE256 assumptions.
- Define the authenticated encryption channel formally and show how confidentiality and integrity reduce to the underlying AEAD guarantees.
- Provide proofs for server authentication and replay resistance, structured as adversarial experiments aligned with the specification and code.
- Analyze forward secrecy properties and show precisely when session confidentiality survives a given compromise event.
- Reconcile theoretical properties with implementation details to confirm or refute fidelity between specification and code.

This chapter thus establishes the analytical environment and scope required for the formal treatment of SATP that follows.

Chapter 3: Model and Assumptions

This chapter defines the analytical model used throughout the cryptanalysis. All notation and terminology are compatible with the SATP specification and the C implementation. The goal is to provide a complete, Word compatible foundation for the security proofs that follow, without relying on specialized fonts or mathematical typesetting.

3.1 Participants and Identity Model

SATP involves two parties: a client device and a server. The client is assigned an identity string "ID(c,i)". The server maintains three long term values: the root key "Kroot", the branch key "Kbr", and the server secret "STc". The branch key is derived from the root key, and the device key "Kc,i" is derived from the branch key and the client identity.

The client stores only its own device key and the user passphrase. The server can recompute any device key from the branch key and the corresponding identity string. All identities are public values. Only the keys and secrets listed above are intended to remain confidential.

Both peers maintain internal state variables such as timestamps, sequence numbers, connection state flags, and session keys. These variables change according to the state machine defined in the SATP implementation.

3.2 Hierarchical Key Structure

SATP uses a deterministic key hierarchy.

1. The server derives the branch key using:
$$Kbr = \text{SHAKE256}(Kroot, Ddom, Dbr)$$
2. The device key is derived using:
$$Kc,i = \text{SHAKE256}(Kbr, ID(c,i))$$

The values Ddom and Dbr are domain separation fields that ensure uniqueness across deployments.

This hierarchy is asymmetric. The client knows only $K_{c,i}$. The server can reconstruct any $K_{c,i}$ for any authorized identity string. This structural asymmetry determines the consequences of compromise events. For example, compromise of a branch key allows the attacker to regenerate all device keys derived under that branch.

3.3 Session Key Derivation

Both peers derive the same four session values from the device key, a configuration string, and a fresh client generated nonce " N_h ". These values are:

R_k = receive direction key

R_n = receive direction nonce

T_k = transmit direction key

T_n = transmit direction nonce

The derivation is:

$$(R_k, R_n, T_k, T_n) = \text{SHAKE256}(K_{c,i}, \text{cfgs}, N_h)$$

The derivation is fully deterministic. No randomness is contributed by the server. All security of session separation depends on the uniqueness of N_h . The analysis therefore assumes the client generates N_h with high entropy and that the adversary cannot force nonce reuse.

In the security model, the function above behaves as a pseudorandom function keyed by the unknown device key.

3.4 Server Validation Hash

The server authenticates itself to the client by computing the validation hash:

$$H_c = \text{SHAKE256}(N_h, K_{c,i}, S_{Tc})$$

This value is encrypted and authenticated under the session keys during the Connect Response packet. The client decrypts the value and verifies it by recomputing H_c locally.

The model assumes that an adversary cannot produce a valid H_c without knowing both $K_{c,i}$ and S_{Tc} . Any successful forgery would imply either breaking SHAKE256 or forging a valid AEAD ciphertext tag, both of which are outside the adversary's abilities under the security assumptions.

3.5 User Authentication Under Encryption

Once the tunnel is raised, the client performs a second authentication step. The client uses its passphrase to compute a hardened value using the SCB key derivation mechanism. The server stores a reference value for each client and checks the client's proof.

All authentication messages are themselves encrypted under the session keys. The model assumes SCB behaves as a one way, memory hard function. The analysis does not require internal details of SCB, because this stage does not influence the confidentiality or integrity of the tunnel. It affects only whether the server accepts the user as authenticated.

3.6 Authenticated Encryption Channel

SATP uses an AEAD construction to protect all encrypted packets. The encryption function takes:

- Key (either R_k or T_k)
- Nonce (either R_n or T_n)
- Associated data (timestamp, sequence number, and header flag)
- Plaintext payload

The AEAD scheme outputs ciphertext and an authentication tag. Decryption verifies the tag, checks the associated data, and rejects any packet with mismatched timestamp or sequence number.

The security model assumes the AEAD primitive satisfies standard IND-CCA confidentiality and INT-CTXT integrity. All later proofs reduce SATP security properties to these primitive guarantees.

3.7 Replay, Timestamp, and Ordering Rules

Each encrypted SATP packet includes:

- A timestamp
- A sequence number
- A header flag identifying the packet type

All three values are included as associated data in the AEAD operation. Any modification to them results in authentication failure.

The implementation requires timestamps to be monotonic within acceptable tolerance and requires sequence numbers to increase strictly. These constraints ensure that replays, reordering attempts, or retroactive insertions of ciphertext fail the AEAD verification step.

The model assumes endpoints follow these rules exactly, and that the adversary has no ability to force violations other than through normal network manipulation.

3.8 Adversary Model

The adversary controls the entire network. It may read, drop, modify, replay, or reorder packets at will. It may initiate its own SATP sessions with honest peers and interleave these sessions arbitrarily.

Two types of compromise are explicitly modeled:

1. Client compromise after session completion. The adversary learns $K_{c,i}$ and the user's passphrase.
2. Server branch key compromise. The adversary learns K_{br} and can regenerate all device keys derived from this branch.

The adversary is assumed unable to do the following:

- Distinguish SHAKE256 output from random when keyed with unknown values.
- Forge AEAD ciphertexts that pass integrity verification.
- Reconstruct ST_c or $K_{c,i}$ without direct compromise.

These are the only cryptographic assumptions used.

3.9 Alignment With Implementation

Every element of the model in this chapter matches the SATP specification and the C implementation in:

- satp.c
- satp.h

- kex.c and kex.h
- connections.c
- client.c
- server.c

No part of the model introduces behavior or data structures not present in the implementation. All proofs in later chapters rely on these definitions, making the model both internally consistent and externally faithful to the deployed SATP protocol.

Chapter 4: Related Work and Theoretical Context

SATP belongs to a class of symmetric key secure channel protocols that construct authenticated and confidential communication layers without relying on asymmetric cryptography. The design is influenced by several decades of research on key hierarchies, deterministic derivation mechanisms, authenticated encryption, and password based authentication. This chapter situates SATP within that body of work to clarify the theoretical foundations on which the protocol relies, the existing security arguments that inform the SATP construction, and the ways SATP departs from or extends established designs. This context is necessary because many of the proofs presented in later chapters depend on assumptions and reduction structures that originate in prior research.

4.1 Symmetric Key Tunneling Protocols

Protocols that use only symmetric primitives to bootstrap secure tunnels are not new. Early examples include Kerberos ticket based channels and cluster level symmetric tunnels used in high performance computing systems. In these systems, trusted authority nodes distribute keys to all devices and rely on deterministic key schedules to refresh session material. SATP adopts this approach by assigning the server complete derivation authority over all device keys and by allowing the server to regenerate any device key from the corresponding branch key.

Unlike Kerberos or early symmetric VPN models, SATP does not rely on trusted third party ticket issuance, nor does it introduce expiration based delegation mechanisms. Instead it uses a pure derivation based architecture where the root key acts as a master

secret for the full domain. This places SATP in alignment with modern deterministic hierarchy designs rather than ticket based authentication systems.

4.2 Key Hierarchies and Deterministic Derivation

Key hierarchies have been studied extensively in secure group communication, scalable identity based systems, and large scale distributed architectures. Most hierarchical designs use deterministic derivation functions so that servers can recover or verify subordinate keys without storing them explicitly. SATP follows this principle precisely.

The derivation:

$$K_{br} = \text{SHAKE256}(K_{root}, D_{dom}, D_{br})$$

$$K_{c,i} = \text{SHAKE256}(K_{br}, ID(c,i))$$

is consistent with the general theory of pseudorandom key expansion, in which a single uncompromised root value determines the security of an entire deployment. SATP differs from hierarchical public key systems because it uses no asymmetric operations and therefore places all trust for key regeneration in the server. This structural choice affects the forward secrecy analysis, because it enables post hoc reconstruction of device keys in a way that hierarchical public key systems do not permit.

4.3 Authenticated Encryption as a Transport Layer Primitive

The authenticated encryption layer used by SATP fits within the framework introduced by modern AEAD constructions such as AES GCM and Keccak derived schemes. The use of associated data to bind packet headers, timestamps, and sequence numbers is consistent with standard models of channel security developed in the literature on robust transport encryption. Under these models, confidentiality reduces to IND CCA security of the AEAD primitive, and integrity reduces to INT CTXT security. SATP inherits these reduction structures directly.

The theoretical foundation for this approach is the general paradigm that secure transport channels can be built safely on top of an IND CCA and INT CTXT secure AEAD scheme, provided that all session keys and nonces meet freshness and uniqueness requirements. SATP satisfies these conditions through deterministic expansion driven by a fresh client nonce. The protocol then binds timestamp and sequence number values inside the AEAD associated data in order to enforce replay and ordering guarantees.

4.4 Password Based Authentication in Encrypted Channels

SATP incorporates a password based authentication stage that operates inside the encrypted tunnel. This is conceptually related to techniques used in SSH, TLS with password authenticated key exchange extensions, and various symmetric authenticated login protocols. SATP differs in two respects. First, it does not use a password based key

exchange mechanism to derive session keys; the device key and client nonce already determine the session keys before the user authentication stage begins. Second, SATP uses a hardened memory intensive KDF, SCB, to produce a verifier that the server checks inside the encrypted channel.

The theoretical context for this approach is the principle of proof within confidentiality, in which password authentication is performed only after a secure transport layer has been established. This separation minimises the likelihood that user authentication failures leak information about the passphrase. The security of this stage derives not from the SATP key exchange itself but from the hardness properties of the SCB function and the confidentiality of the enclosing channel.

4.5 Replay Protection and Freshness Guarantees

Replay and ordering control in secure channel protocols has a long history in systems such as IPsec, SSH, and the original Needham Schroeder protocol corrections. Most secure channel designs bind a monotonically increasing counter or timestamp to the encryption operation so that ciphertexts cannot be accepted out of order. SATP follows this principle by including the timestamp, sequence number, and header flag in the AEAD associated data. This design situates SATP within the family of protocols that enforce stateful freshness, rather than using purely stateless nonces supplied externally. SATP's freshness guarantees depend on the assumption that both peers maintain monotonic counters and that AEAD binding correctly enforces rejection of any attempted reuse. This is consistent with the established theoretical results that show that replay resistance reduces to the unforgeability of the associated data binding provided by AEAD.

4.6 Deterministic Key Schedules and Forward Secrecy Considerations

The literature on deterministic key derivation contains several results relevant to SATP. Deterministic hierarchies simplify provisioning, but they complicate forward secrecy analysis because compromise of a high level key often reveals all subordinate keys. SATP follows this pattern. The server can derive all device keys from the branch key. As a result, compromise of a branch key eliminates forward secrecy for all clients under that branch. This property is not anomalous but rather inherent to deterministic symmetric hierarchies.

SATP partially mitigates this structural limitation through client side erasure of $K_{c,i}$. Once a session has derived (R_k, R_n, T_k, T_n) , the client deletes the device key so that compromise of the client after the session does not reveal past traffic. This approach aligns with forward secrecy by consumption, a concept explored in symmetric key

literature where ephemeral secrets can compensate for deterministic long term hierarchies. However, because the server retains K_{br} , complete forward secrecy is not achievable under this architecture.

4.7 Summary of Theoretical Dependencies

The security analysis of SATP relies on theoretical foundations that are well established in several areas:

1. Pseudorandom function behavior of SHAKE256 when keyed with unknown material.
2. The IND CCA and INT CTXT definitions for authenticated encryption and their use in constructing secure transport channels.
3. Standard adversarial models for replay control based on counters and associated data.
4. Deterministic hierarchical key derivation as used in symmetric key management systems.
5. Password verification inside encrypted channels as a method of binding a user secret to an already established tunnel.

Taken together, these results form the theoretical context in which SATP operates. The protocol does not attempt to exceed these foundations, and its security proof structure follows the established reduction patterns used for modern secure channel protocols.

Chapter 5: Protocol Overview

This chapter presents a complete overview of SATP as it is defined in the specification and implemented in the C codebase. The objective is to describe the protocol in a manner that is faithful to the real system, suitable for formal analysis, and consistent with all security properties proven later. The overview is organized to highlight the interaction between the hierarchical key structure, the session derivation functions, the server validation mechanism, the user authentication sequence, and the authenticated encryption transport layer. All packet formats, state transitions, and cryptographic computations referenced here are taken directly from the corresponding SATP source files.

5.1 High Level Workflow

SATP establishes a secure tunnel in two stages. First, the client authenticates the server by verifying a server produced value derived from the device key, the session nonce, and

the long term server secret. This step completes before any encrypted traffic is allowed to flow. Second, the client authenticates itself to the server using a hardened password derived value inside the encrypted tunnel. Only after both stages succeed does the session reach the established state.

The protocol flow is therefore:

1. Client sends a Connect Request that contains its identity and a fresh session nonce.
2. Server derives the session keys and returns a Connect Response containing an encrypted validation hash.
3. Client verifies the server by decrypting and recomputing the validation hash.
4. Client and server enter the encrypted channel.
5. Client performs user authentication inside the channel.
6. Once accepted, the server transitions the state to established and both sides exchange encrypted data.

This workflow strictly separates server authentication and user authentication, and ensures that no user authentication data is transmitted outside the encrypted tunnel.

5.2 Key Material and Derivation Flow

SATP's key hierarchy connects long term secrets to session keys through deterministic derivation:

1. Root key K_{root} identifies the deployment domain.
2. Branch key K_{br} is derived using $\text{SHAKE256}(K_{root}, D_{dom}, D_{br})$.
3. Device key $K_{c,i}$ is derived using $\text{SHAKE256}(K_{br}, ID(c,i))$.
4. Session keys (R_k, R_n, T_k, T_n) are derived using $\text{SHAKE256}(K_{c,i}, \text{cfgs}, N_h)$.

The configuration string cfgs is compiled into the SATP implementation and identifies the AEAD configuration in use. The client generated nonce N_h is the sole source of fresh entropy. All values above appear explicitly in the implementation.

The session derivation produces two keys and two nonces:

- Rk and Rn are used when receiving packets.
- Tk and Tn are used when transmitting packets.

This separation enforces direction specific encryption and prevents reflection attacks inside the channel.

5.3 Packet Structure and Message Types

All SATP packets share a consistent header structure that contains three fields:

- A timestamp representing the sender's local time.
- A sequence number that increases monotonically.
- A header flag identifying the packet type.

The packet types include:

- Connect Request
- Connect Response
- Client Authentication Request
- Server Authentication Response
- Client Authentication Verification
- Encrypted Data
- Keepalive
- Session Terminated

These flags are processed exactly as implemented in satp.c, server.c, and client.c, and are used both to route packets and to bind packet meaning during authenticated encryption.

5.4 Connect Request

The first message in the protocol is sent by the client. It contains the identity string ID(c,i) and the session nonce Nh. The identity is sent in plaintext, as is customary in symmetric tunnel designs. The nonce Nh is a mandatory fresh random value generated by the client and is passed directly to the session derivation function.

Upon receiving the Connect Request, the server reconstructs the device key $K_{c,i}$ using the branch key and the identity. It then derives the session keys and prepares to authenticate itself.

5.5 Connect Response and Server Authentication

To prove that it is the legitimate server for the client's identity, the server constructs a validation hash:

$$H_c = \text{SHAKE256}(N_h, K_{c,i}, S_{Tc})$$

This value is encrypted and authenticated under the session keys and placed into the Connect Response. The client decrypts the response and verifies it by recomputing H_c . A mismatch indicates that the responder does not possess the correct device key or the server secret.

Only after this step does the client accept that it is talking to the intended server.

5.6 Establishment of the Encrypted Tunnel

Once server authentication succeeds, both sides enter the encrypted channel. All subsequent packets, including user authentication messages, are encrypted under R_k , R_n , T_k , and T_n . The timestamp, sequence number, and header flag are placed in the associated data field of the AEAD primitive, so any modification of these values results in immediate packet rejection.

The tunnel remains in a pre authentication state until the user authentication stage completes.

5.7 User Authentication Under Encryption

The client proves knowledge of its passphrase using a hardened SCB based function. The SCB output is not used to derive session keys. Instead, it is used purely as a verifier that the server compares with a stored reference value. The server returns an authenticated success or failure message inside the encrypted channel.

This step binds the user's secret to the session without exposing any password related information outside the encrypted tunnel.

5.8 Transition to Established Session

Once the server accepts the client's authentication, the internal state on both sides transitions to "established". At this point:

- All encrypted data is processed normally.
- Timestamps and sequence numbers advance on each packet.
- Replay and reorder checks are enforced by AEAD associated data binding.

This state persists until one side closes the session or either timestamp or sequence validation fails.

5.9 Replay Protection and Transport Semantics

SATP enforces replay control through:

- Monotonic sequence numbers that must always increase.
- Timestamps that must remain within acceptable drift limits.
- Binding both values to the authenticated data of the AEAD operation.

Any replayed ciphertext, even if structurally correct, is rejected because its timestamp or sequence number will not match the expected values. This mechanism is fully consistent with the SATP code and represents a core security property of the tunnel.

5.10 Summary

This chapter has presented a complete overview of the SATP protocol as it is specified and implemented. The description includes the hierarchical key structure, the derivation of session keys, the server authentication mechanism, the user authentication stage, the packet formats, the tunnel operation, and the replay handling mechanisms. This overview forms the structural basis for the formal definitions and proofs in the next chapters, where each component is precisely analyzed under the adversarial model defined earlier.

Chapter 6: Formal Specification and Mathematical Model

This chapter provides a complete algebraic specification of SATP. All constructions are presented as explicit functions over bitstrings so that confidentiality, integrity, authentication, and replay protection can be evaluated in a precise mathematical

setting. Every definition here corresponds directly to an operational behavior in the SATP code and specification. No symbolic notation outside normal ASCII is used so the content renders correctly in Microsoft Word.

The mathematical model captures four principal components: the hierarchical key derivation process, the session derivation function, the server validation mechanism, and the authenticated encryption channel. The final subsection formalizes the SATP state machine as a sequence of deterministic transitions.

6.1 Notation and Conventions

All values are treated as bitstrings. Concatenation is written as:

$X \parallel Y$

The SHAKE256 and SHAKE128 extendable output functions are written as:

SHAKE256(input1 , input2 , ...)
SHAKE128(input1 , input2 , ...)

Multiple inputs indicate domain separated concatenation. The output size is determined by context. All functions map bitstrings to bitstrings and are deterministic.

Let:

- K_{root} denote the domain root key.
- K_{branch} denote a branch key.
- $K_{c,i}$ denote the device key for client identity $ID(c,i)$.
- $cfgs$ denote the configuration string in the implementation.
- N_h denote the client generated session nonce.
- ST_c denote the server secret used for validation.

Constants D_{dom} and D_{br} are domain separation labels supplied in the specification.

6.2 Hierarchical Key Derivation

The SATP hierarchy is defined as a deterministic tree rooted at K_{root} .

1. Branch key derivation:

$K_{br} = \text{SHAKE256}(K_{root}, D_{dom}, D_{br})$

The arguments K_{root} , D_{dom} , and D_{br} are concatenated with explicit separators in the implementation and passed into SHAKE256 as a single domain separated input. The model treats them as concatenated inputs.

2. Device key derivation:

$K_{c,i} = \text{SHAKE256}(K_{br}, ID(c,i))$

This derivation is deterministic for each identity. Both specification and implementation require that $ID(c,i)$ be unique within a branch so that the mapping from identities to device keys is injective with respect to SHAKE256 domain separation.

No randomness is introduced at any point. From the server perspective, the key hierarchy behaves as a deterministic pseudorandom function family indexed by identities.

6.3 Session Key Derivation

The session derivation function produces the set of transport keys and nonces used for authenticated encryption. SATP defines:

$(R_k, R_n, T_k, T_n) = \text{SHAKE256}(K_{c,i}, \text{cfgs}, N_h)$

The interpretation is:

- Input 1: $K_{c,i}$ (secret).
- Input 2: cfgs (implementation specific configuration string).
- Input 3: N_h (fresh random nonce generated by the client).

The SHAKE256 output is then partitioned into four contiguous segments of equal predetermined lengths:

R_k = first segment of output

R_n = second segment

T_k = third segment

T_n = fourth segment

These lengths match the AEAD key length and nonce length of the chosen encryption backend. For example, if AES-256 is selected, Rk and Tk are 256 bit encryption keys and Rn and Tn are 96 bit or 128 bit nonces depending on compile time parameters.

The mathematical model assumes:

1. For unknown $K_{c,i}$, the mapping
 $(K_{c,i}, \text{cfgs}, Nh) \rightarrow (R_k, R_n, T_k, T_n)$
is computationally indistinguishable from drawing four independent random values.
2. Distinct values of Nh lead to independent session key tuples.

These assumptions follow from the cryptographic properties of SHAKE256.

6.4 Server Validation Hash

Before any encrypted data flows, the server must prove possession of the long term secrets $K_{c,i}$ and ST_c . SATP defines the validation hash as:

$$H_c = \text{SHAKE256}(Nh, K_{c,i}, ST_c)$$

This output is included in the Connect Response as ciphertext protected by $\text{AEAD}(Tk, Tn)$. The client reconstructs H_c using its local copies of Nh and $K_{c,i}$ (it does not know ST_c). The validation hash is accepted only if:

$$H_c(\text{received}) == \text{SHAKE256}(Nh, K_{c,i}, ST_c)$$

This binds the server's identity to the session nonce and prevents replay or substitution of validation messages.

The mathematical model assumes that for an adversary who does not know $K_{c,i}$ or ST_c , the function:

$$(Nh, K_{c,i}, ST_c) \rightarrow H_c$$

is collision resistant and preimage resistant. Producing a correct H_c without knowing these values would require breaking SHAKE256 or forging a valid AEAD ciphertext.

6.5 AEAD Encryption and Associated Data Binding

SATP uses an AEAD primitive defined by the implementation, either an RCS based scheme or AES based scheme. The encryption function is:

$C, Tag = AEAD_Enc(Key, Nonce, AD, P)$

The corresponding decryption is:

$P = AEAD_Dec(Key, Nonce, AD, C, Tag)$

where AD denotes associated data. For SATP, the associated data is:

$AD = \text{Timestamp} \parallel \text{Sequence} \parallel \text{HeaderFlag}$

These fields are extracted from the SATP packet header. The AEAD primitive is treated as a black box satisfying:

1. IND-CCA confidentiality
2. INT-CTXT integrity with respect to both ciphertext and associated data

Thus, SATP transport security reduces to the security of the AEAD channel provided that session keys and nonces are unique per session, which is enforced by the session derivation function and the client's nonce N_h .

6.6 Formal Replay Model

SATP enforces replay protection by incorporating timestamp and sequence number into AD. Define:

$AD_t = \text{Time}_t \parallel \text{Seq}_t \parallel \text{Flag}_t$

A ciphertext C_t is accepted by the receiver only if:

1. $AEAD_Dec$ returns a valid plaintext.
2. Time_t is within allowable drift.
3. Seq_t is greater than any previously accepted sequence number for the session.

Formally:

$\text{Accept}(C_t) = 1$ if and only if all three conditions are satisfied.

An adversary cannot cause $\text{accept}(C_i)$ for any $i < j$ without breaking AEAD integrity, because $AD_i \neq AD_j$ implies a tag mismatch.

Thus, the replay model for SATP is stateful and monotonic.

6.7 State Machine Specification

We formalize the SATP state machine as a tuple:

State = (Mode , Keys , Counters , Flags)

Mode takes one of the following values:

- INIT
- SERVER_AUTH_PENDING
- TUNNEL_RAISED
- USER_AUTH_PENDING
- ESTABLISHED
- TERMINATED

The transitions are deterministic and correspond exactly to SATP packet processing:

1. INIT -> SERVER_AUTH_PENDING
Trigger: receipt of Connect Response and availability of $K_{c,i}$
Condition: successful construction of session keys
2. SERVER_AUTH_PENDING -> TUNNEL_RAISED
Trigger: validation hash H_c decrypts and matches local recomputation
3. TUNNEL_RAISED -> USER_AUTH_PENDING
Trigger: first encrypted authentication request received
4. USER_AUTH_PENDING -> ESTABLISHED
Trigger: server verifies SCB derived proof
5. Any state -> TERMINATED
Trigger: explicit termination packet or failure of timestamp or sequence validation or AEAD tag failure

These transitions define the canonical SATP execution path. All proofs in later chapters quantify adversarial success probabilities with respect to this state machine.

6.8 Summary of the Mathematical Model

This formal specification gives a complete, Word compatible algebraic description of SATP:

- deterministic hierarchical key derivation,
- deterministic session derivation from fresh nonce,
- server validation through keyed SHAKE256 structure,
- encryption and integrity through AEAD with associated data binding,
- replay semantics enforced by timestamp and sequence monotonicity,
- and a well defined state machine governing protocol flow.

All later security proofs rely on these definitions.

Chapter 7: Security Definitions and Proof Structure

This chapter introduces the formal security definitions used to analyze SATP and explains the proof structure employed in subsequent chapters. The goal is to provide precise adversarial games for confidentiality, integrity, server authentication, client authentication, and replay protection, then explain how SATP's security arguments reduce to the security of its underlying primitives and the structural properties formalized in earlier chapters. These definitions are aligned with the model, assumptions, and mathematical constructions already introduced, and they reflect the operational behavior of the SATP implementation.

The chapter is divided into five thematic parts: channel confidentiality, channel integrity, server authentication, client authentication, and replay resistance. The final section describes the unified reduction structure that the formal proofs adopt.

7.1 Confidentiality Definition (IND-CPA and IND-CCA Channel Security)

SATP aims to provide confidentiality for all encrypted payloads once the tunnel is raised. This property is defined through a standard indistinguishability under chosen ciphertext attack experiment adapted to SATP's deterministic session derivation.

The confidentiality experiment proceeds as follows:

1. The adversary selects two equal length plaintexts P0 and P1.
2. A bit b is chosen uniformly by the experiment.
3. SATP derives session keys using the real device key Kc,i and a fresh Nh.
4. The AEAD encryption function encrypts Pb using the transmit direction key, nonce, and associated data.

5. The adversary receives the ciphertext and may issue arbitrary decryption queries subject to the restriction that the challenge ciphertext cannot be queried.
6. The adversary outputs a guess bit b' .

SATP provides confidentiality if every adversary has only negligible advantage:

$$\text{Adv_conf} = |\Pr[b' = b] - 1/2|$$

Under the model from Chapter 6, we say SATP satisfies IND-CCA confidentiality if any such attacker can be converted into an attacker against the underlying AEAD primitive with non negligible probability. The reduction is straightforward, since the keys used by the AEAD scheme are derived from SHAKE256 with a secret device key and fresh N_h , which is indistinguishable from random as long as $K_{c,i}$ is secret.

7.2 Integrity and Authenticity Definition (INT-CTXT)

Integrity of ciphertext and associated data is defined through the standard INT-CTXT experiment for authenticated encryption. An adversary succeeds if it produces a ciphertext-tag-associated-data triple that decrypts successfully under keys used by an honest endpoint, with the condition that the triple was not produced by previous queries to the encryption oracle.

In the SATP context:

1. The experiment simulates the state machine for an honest endpoint.
2. The adversary receives encryption oracle access to $\text{AEAD_Enc}(R_k, R_n, AD, P)$.
3. The adversary outputs a forged ciphertext C^* , tag T^* , and associated data AD^* .
4. The forgery succeeds only if $\text{AEAD_Dec}(R_k, R_n, AD^*, C^*, T^*)$ returns a plaintext and AD^* matches the timestamp and sequence constraints of the implementation.

SATP provides integrity if the probability of producing any such forgery is negligible.

Any successful SATP forgery corresponds directly to an INT-CTXT forgery against the AEAD primitive, because AD is strictly enforced and the session keys remain unknown to the adversary.

7.3 Server Authentication Definition

Server authentication means that the client accepts a server as legitimate only if it holds both the correct device key $K_{c,i}$ and the correct server secret S_{Tc} . The adversarial experiment for server authentication proceeds as follows:

1. The adversary interacts with the server as in a normal SATP session.
2. The adversary then attempts to impersonate the server to the client by producing a Connect Response that contains a ciphertext encapsulating a validation hash H_c^* .

3. The client accepts the server if the decrypted Hc^* matches $\text{SHAKE256}(Nh, Kc, i, STc)$.

An adversary succeeds if it causes the client to accept without the adversary knowing both Kc, i and STc . SATP provides server authentication if the probability of success is negligible.

The security reduction shows that any adversary who forges a valid Hc^* must either invert the SHAKE256 construction or forge the AEAD tag. Since both operations are assumed infeasible, server authentication holds.

7.4 Client Authentication Definition

Client authentication concerns proving knowledge of the user's passphrase after the tunnel is raised. We define the client authentication experiment:

1. The adversary interacts with the server and observes all encrypted messages.
2. The adversary attempts to impersonate the client by producing valid SCB derived authentication messages after the tunnel has been established.
3. The adversary succeeds if the server accepts the SCB verifier as correct.

Because all authentication messages are encrypted, an impersonation attack requires either breaking the SCB function or breaking the confidentiality of AEAD. Under the assumption that SCB is one way and that AEAD is IND-CCA secure, SATP provides client authentication.

7.5 Replay Resistance Definition

Replay resistance requires that ciphertext accepted by an endpoint must be fresh with respect to timestamp and sequence number. SATP defines freshness via:

1. Monotonic sequence numbers enforced per direction.
2. Monotonic timestamps within allowed drift.
3. Inclusion of both values in AEAD associated data.

The replay experiment is:

1. The adversary records a ciphertext C_{old} with $AD_{\text{old}} = (\text{Time}_{\text{old}}, \text{Seq}_{\text{old}}, \text{Flag}_{\text{old}})$.
2. The adversary attempts to inject C_{old} at a later point in the session.
3. The receiver accepts a replay only if AEAD-Dec succeeds and the timestamp and sequence number are valid.

SATP provides replay resistance if no adversary can cause acceptance of any previously used ciphertext. Because the AEAD primitive authenticates AD_{old} , and the receiver's counters reject stale values, any attempt to replay packets results in rejection unless the adversary can forge a new valid tag.

7.6 Forward Secrecy in the SATP Model

SATP does not provide traditional forward secrecy. Instead, it provides limited secrecy under client compromise but not under branch key compromise. To define this property formally:

- The adversary may compromise the client after a session and learn $K_{c,i}$ and the passphrase.
- The adversary must not recover past session plaintexts unless it can break AEAD confidentiality.

SATP provides forward secrecy under this restricted definition because the device key is erased after use and past session keys cannot be reconstructed without $K_{c,i}$.

No forward secrecy is retained under branch key compromise, because the attacker can regenerate $K_{c,i}$ and redo the entire session derivation. This is a structural limitation formalized in Chapter 6.

7.7 Unified Proof Strategy

The proofs in later chapters follow a structured pattern:

1. Replace session keys generated by SHAKE256 with uniformly random keys.
2. Argue that any adversary able to distinguish real session keys from random would break the pseudorandomness of SHAKE256 on secret inputs.
3. Condition on the keys being indistinguishable from random and reduce all confidentiality claims to the IND-CCA security of the AEAD primitive.
4. Condition on keys being indistinguishable from random and reduce all integrity and replay claims to the INT-CTXT security of AEAD.
5. Reduce server authentication to the collision and preimage resistance of SHAKE256 plus the integrity of AEAD.
6. Reduce client authentication to the one way security of SCB and the confidentiality of AEAD.

This modular proof structure ensures that SATP's security follows directly from well understood cryptographic assumptions and from correct implementation of protocol state transitions.

7.8 Summary

This chapter has defined the formal adversarial experiments for each major SATP security property and explained the reduction structure used in later proofs. These definitions are consistent with the SATP model, reflect the real behavior of the C implementation, and provide a rigorous foundation for the formal security analysis that follows.

Chapter 8: Cryptanalytic Evaluation and Attack Surface

This chapter evaluates SATP from a cryptanalytic perspective, using the model and definitions established in the preceding chapters. The objective is to characterize, with precision, the attack surface that an adversary encounters when interacting with a correctly implemented SATP deployment. The analysis considers both black box cryptanalytic attacks on primitives and structural attacks on the protocol's deterministic key hierarchy, session construction, validation logic, and replay semantics. Because SATP relies entirely on symmetric cryptography and deterministic derivation, its attack surface is fundamentally different from protocols that rely on ephemeral asymmetric secrets. The evaluation here therefore emphasizes structural weaknesses, compromise boundaries, and adversarial leverage points that arise from SATP's design.

8.1 Exposure of Public Values and Adversarial Knowledge

SATP exposes several values to the adversary as part of normal protocol operation. These include the identity string $ID(c,i)$, the client nonce Nh , timestamps, sequence numbers, header flags, and all ciphertext produced by the AEAD layer. The adversary also learns that the branch key and device key derivation structure is deterministic and that $cfgs$ is known and constant.

This exposure is not, by itself, a vulnerability. The security of SATP does not rely on secrecy of public identifiers or deterministic inputs. However, because SATP uses deterministic derivation, an attacker with complete knowledge of public inputs can mount structural reasoning attacks if any secret component leaks even partially. The cryptanalytic evaluation therefore examines whether these exposures enable narrowing of the key space or partial information recovery. Under the SHAKE256 assumptions, they do not, but the structural implications are important for later compromise scenarios.

8.2 Attacks on Hierarchical Key Derivation

The derivation functions $K_{br} = \text{SHAKE256}(K_{root}, D_{dom}, D_{br})$ and $K_{c,i} = \text{SHAKE256}(K_{br}, ID(c,i))$ behave as pseudorandom keyed functions when K_{root} is unknown. An adversary observing $ID(c,i)$ and Nh gains no advantage in recovering $K_{c,i}$ beyond brute forcing K_{br} or K_{root} . Since SHAKE256 output space is large, generic attacks are impractical.

However, deterministic key hierarchies introduce specific weaknesses under compromise:

1. If Kroot is compromised, the entire system collapses, because all branch keys and device keys follow directly.
2. If Kbr is compromised, all device keys for that branch are exposed.
3. If Kc,i is compromised, only sessions for that identity are exposed, and only until the client erases the device key.

These structural properties are fundamental aspects of SATP. They do not arise from cryptanalytic weakness in SHAKE256 but from architectural trust placement. In particular, no amount of session level hardening can mitigate a compromise of Kbr.

8.3 Attacks on Session Key Derivation

The session key derivation $(Rk, Rn, Tk, Tn) = \text{SHAKE256}(Kc,i, \text{cfgs}, Nh)$ presents a single realistic attack vector: withdrawal of entropy in Nh. If Nh is not generated randomly or if an adversary can induce reuse of Nh, then session keys become dependent on deterministic values alone, enabling replay of Connect Requests to cause key reuse.

In practical terms:

- If Nh repeats, an adversary replaying the old Connect Request forces the server to regenerate identical session keys.
- Identical session keys allow ciphertexts from past sessions to decrypt under the present session.

However, this attack fails in correctly implemented SATP because the server immediately detects reuse of timestamp and sequence numbers, and ciphertexts from earlier sessions carry those values in the associated data. Decryption therefore fails even if keys repeat. Nevertheless, predictable or repeated Nh weakens SATP's defense against related key attacks and violates the assumptions of the confidentiality proofs. For this reason SATP places responsibility for Nh generation entirely on the client and expects high quality randomness.

8.4 Attacks on Server Validation Hash

The server validation hash $H_c = \text{SHAKE256}(N_h, K_{c,i}, S_Tc)$ is vulnerable to cryptanalysis only if the adversary can guess $K_{c,i}$ or S_Tc or find a preimage for SHAKE256 under these inputs. Since each component is 256 bits or larger, brute force attacks are not feasible. Collision attacks have no effect on H_c because malicious collisions would require injecting a different N_h or $K_{c,i}$, which the adversary cannot influence legitimately.

The attack surface here consists of protocol misuse:

- If S_Tc is weak or shared across deployments, compromise affects all servers using that secret.
- If $K_{c,i}$ is weak or derived from low entropy identity strings (contrary to the specification), it becomes more predictable.
- If endpoints skip validation or fail to recompute H_c correctly, server authentication collapses.

The cryptanalytic surface is minimal; the protocol surface is more consequential.

8.5 Attacks on the AEAD Transport Layer

SATP's confidentiality and integrity reduce to the AEAD primitive. Common attacks include:

- Attempting to forge ciphertext or associated data.
- Modifying timestamps or sequence numbers to bypass ordering rules.
- Manipulating length or padding to induce decryption oracles.
- Hosting chosen ciphertext queries to extract timing information.

Because SATP uses standard AEAD constructions (RCS based or AES based), cryptanalytic attacks target the underlying primitives rather than SATP itself. There is no evidence in the implementation of nonce reuse, variable time comparisons, or malleable decrypt paths that would open SATP to chosen ciphertext or side channel attacks.

Replay attempts fail because the associated data binds ordering metadata. Modification attacks fail because AEAD integrity checks abort processing. The AEAD layer is therefore cryptanalytically robust as long as the underlying primitive is sound.

8.6 Attacks on the Replay and Ordering Mechanism

Replay control in SATP depends on the monotonic progression of timestamps and sequence numbers. An adversary can attempt:

- Replay of old ciphertexts.
- Reordering within a valid sequence window.
- Injection of artificially advanced timestamps to desynchronize peers.

Because timestamps and sequence numbers are included in AEAD associated data, any modification results in immediate failure. Replays are rejected because the timestamp and sequence number no longer satisfy the monotonicity requirements enforced by the receiver. Attempts to desynchronize timestamps are blocked by drift checks in the implementation. This subsystem therefore behaves as a cryptographically enforced state machine rather than a statistical detection system.

The attack surface is minimal as long as both endpoints maintain correct counters.

8.7 Attacks on the User Authentication Stage

User authentication relies on SCB derived values transmitted inside the encrypted channel. Attacks on this stage fall into two categories:

1. Attacks on SCB itself, attempting to invert the hardened KDF.
2. Attacks on the encrypted tunnel to extract authentication messages or modify them.

Because SCB is not used to derive session keys, its compromise does not affect confidentiality of traffic. The encrypted tunnel prevents passive observation of SCB values. Modification attacks are prevented by AEAD integrity. The only realistic attack vector is a weak passphrase chosen by the user. SATP cannot mitigate this cryptographically, but it does not amplify the risk beyond SCB's intrinsic vulnerability to dictionary attacks.

8.8 Compromise-Induced Attacks

SATP exhibits sharply different behavior depending on which secret, if any, is compromised.

8.8.1 Client compromise

If the adversary obtains $K_{c,i}$ and the passphrase after a session completes, replaying past ciphertext still fails because timestamps and sequence numbers prevent decryption under new AD values. Past traffic remains confidential because the device key is erased after use.

8.8.2 Branch key compromise

If the adversary learns K_{br} , all device keys under that branch follow. All past and future sessions for those clients become decryptable. Session derivation does not mitigate this, because the adversary reconstructs $K_{c,i}$ and replays session derivations with recorded N_h values.

8.8.3 Server secret compromise

If ST_c is compromised, server authentication fails. The adversary can impersonate the server but cannot read old ciphertexts without also compromising $K_{c,i}$ or K_{br} .

These boundaries are structural and cannot be changed without redesigning SATP.

8.9 Multi-Session and Cross-Session Attacks

SATP's deterministic derivation implies that an adversary may attempt to correlate sessions to identify patterns or weaken assumptions. Attempts include:

- Testing whether two N_h values are equal across sessions.
- Checking relationships between AEAD keys derived from predictable inputs.
- Attempting to mount cross session related key attacks.

Because N_h must be unpredictable and because SHAKE256 behaves as a pseudorandom function, cross session correlation does not reveal exploitable structure. Cross session interaction is therefore limited to denial of service or replay attempts, neither of which breaks the cryptographic layer.

8.10 Summary of Cryptanalytic Exposure

The cryptanalytic attack surface of SATP is small and strongly bounded by its reliance on SHAKE256 and AEAD as its only cryptographic primitives. No algebraic attacks on these primitives are known that would result in practical breaks. The structural vulnerabilities center on compromise of long term symmetric keys and on the deterministic design of

the hierarchy rather than on exploitable weaknesses in the derivation functions themselves.

SATP resists all known active cryptanalytic attacks under its intended deployment model, provided that:

- The client generates Nh with full entropy.
- The server protects $Kroot$, Kbr , and STc .
- Implementation correctly enforces AEAD integrity and replay constraints.
- User passphrases possess sufficient entropy to resist offline guessing against SCB.

The next chapter presents the formal confidentiality and integrity proofs, using the adversarial definitions and reduction structures established earlier.

9. Confidentiality and Integrity Proofs

This chapter provides the formal proofs that SATP satisfies the confidentiality and integrity properties defined in Chapter 7, assuming the cryptographic assumptions stated in Chapter 6. All proofs follow the reduction style standard in modern symmetric cryptography. The objective is not to claim absolute resistance but to show that breaking SATP's channel security would require breaking the IND-CCA or INT-CTXT properties of the underlying AEAD primitive or the pseudorandomness of SHAKE256 when keyed with unknown inputs.

The proofs in this chapter apply only after the secure tunnel has been raised. Server authentication and user authentication proofs appear in later chapters.

9.1 Preliminaries

For clarity, we restate the core assumptions needed for this chapter:

1. The derivation
 $(Rk, Rn, Tk, Tn) = \text{SHAKE256}(Kc,i, \text{cfgs}, Nh)$
behaves as a pseudorandom function when Kc,i is unknown to the adversary.
2. The AEAD primitive satisfies IND-CCA confidentiality.
3. The AEAD primitive satisfies INT-CTXT integrity.

4. Associated data binding (timestamp || sequence || header flag) is enforced exactly as in the SATP implementation.
5. The adversary cannot force nonce reuse except by causing N_h to repeat, which is prevented by the protocol model.

Using these assumptions, we now analyze confidentiality and integrity in turn.

9.2 Confidentiality Proof

Confidentiality is defined by the IND-CCA experiment in Chapter 7. The goal is to prove that the adversary cannot distinguish encryptions of chosen plaintexts under a fresh SATP session.

The proof has three steps:

1. Replace the session keys with random keys.
2. Argue that the adversary cannot distinguish real session keys from random keys.
3. Reduce any successful distinguisher to a distinguisher against the AEAD primitive.

9.2.1 Hybrid 1: Replacement of Session Keys

Define Hybrid 1 as a version of SATP in which session keys (R_k, R_n, T_k, T_n) are replaced with uniformly random values of the same lengths, independent of $K_{c,i}$, $cfgs$, and N_h .

Let Adv_{real} denote the adversary's advantage in the real IND-CCA experiment, and Adv_{H1} its advantage in Hybrid 1.

Suppose the adversary can distinguish between the real SATP session keys and the Hybrid 1 keys. Then it can distinguish between:

$SHAKE256(K_{c,i}, cfgs, N_h)$

and a uniform random tuple of the same size.

This contradicts the pseudorandomness of SHAKE256 on secret inputs. Therefore:

$$|Adv_{real} - Adv_{H1}| \leq \text{negligible}$$

9.2.2 Hybrid 2: Replacement of AEAD Encryption with Idealized AEAD

In Hybrid 2, the AEAD encryption is replaced with an ideal IND-CCA encryption oracle using the random keys from Hybrid 1.

Since the adversary cannot distinguish Hybrid 1 from Hybrid 2 without breaking AEAD confidentiality:

$$| \text{Adv_H1} - \text{Adv_H2} | \leq \text{negligible}$$

9.2.3 Reduction to AEAD IND-CCA

In Hybrid 2, the adversary interacts with a standard IND-CCA encryption scheme with random keys and nonces. The adversary receives one challenge ciphertext. Any advantage it gains constitutes an advantage against the AEAD primitive itself.

Thus:

$$\text{Adv_H2} \leq \text{Adv_AEAD_INDCCA}$$

Since the AEAD primitive is assumed IND-CCA secure, this value is negligible.

9.2.4 Conclusion of the Confidentiality Proof

Combining these results:

$$\text{Adv_real}$$

$$\leq |\text{Adv_real} - \text{Adv_H1}| + |\text{Adv_H1} - \text{Adv_H2}| + \text{Adv_H2}$$

$$\leq \text{negligible} + \text{negligible} + \text{negligible}$$

Therefore SATP provides IND-CCA confidentiality under the stated assumptions.

9.3 Integrity Proof

Integrity is defined by the INT-CTXT experiment. The adversary succeeds if it produces any ciphertext-tag-associated-data triple that decrypts successfully under SATP keys, without having been produced by an encryption query.

The proof structure mirrors the confidentiality proof.

9.3.1 Hybrid 1: Replacement of Session Keys

As in the confidentiality proof, replacing the session keys with random values produces a hybrid distribution that is indistinguishable from the real distribution. The pseudorandomness of SHAKE256 ensures:

$$| \text{Adv_real_INT} - \text{Adv_H1_INT} | \leq \text{negligible}$$

9.3.2 Hybrid 2: Replacement of AEAD with Ideal Integrity Oracle

In Hybrid 2, the AEAD encryption and decryption are replaced with an oracle that maintains perfect INT-CTXT security.

Any adversary distinguishing Hybrid 1 from Hybrid 2 would break AEAD integrity.

Thus:

$$| \text{Adv_H1_INT} - \text{Adv_H2_INT} | \leq \text{negligible}$$

9.3.3 Integrity Reduction

In Hybrid 2, the only way the adversary can create a forgery is by producing a ciphertext-tag pair that the ideal AEAD oracle accepts. By definition of INT-CTXT, this has negligible probability.

Therefore:

$$\text{Adv_H2_INT} \leq \text{negligible}$$

9.3.4 Associated Data Binding

SATP enforces integrity not only of ciphertext but also of timestamps, sequence numbers, and header flags. Because all these values are placed into AEAD associated data:

- Any replay of old ciphertext fails because associated data no longer matches.
- Any modification of timestamps or sequence numbers causes AEAD tag rejection.
- Any attempt to reorder ciphertext fails because sequence number monotonicity is strictly enforced.

Thus the proof ensures transport-level integrity as well as ciphertext integrity.

9.3.5 Conclusion of the Integrity Proof

Combining the hybrid steps:

Adv_real_INT

<= negligible + negligible + negligible

SATP therefore satisfies INT-CTXT integrity under the AEAD assumptions.

9.4 Robustness Against Combined Confidentiality and Integrity Attacks

In many practical scenarios, the adversary attempts combined attacks, such as:

- Using chosen ciphertext queries to extract information (padding oracle style).
- Attempting to manipulate timestamps or counters to induce state corruption.
- Combining ciphertext modification with replay attempts.
- Using malformed packets to probe the behavior of the validation state machine.

Because SATP:

1. uses a single AEAD primitive that enforces both confidentiality and integrity,
2. binds timestamps, sequence numbers, and header flags in associated data,
3. rejects any AEAD tag failure without exposing decryption information,
4. and maintains a deterministic and monotonic state machine,

none of these hybrid or chained attacks succeed without breaking AEAD confidentiality or integrity.

9.5 Summary

This chapter proves that:

1. SATP provides IND-CCA confidentiality after the tunnel is raised.
2. SATP provides INT-CTXT integrity for ciphertext, tags, and associated data.
3. Violation of either property would require either breaking SHAKE256 pseudorandomness or breaking AEAD confidentiality or integrity, all assumed infeasible.

These results establish the foundational cryptographic strength of SATP's transport layer. The next chapter addresses **authentication**, which requires a distinct set of proofs.

10. Authentication Security Proofs

Authentication in SATP occurs in two distinct stages. The first stage authenticates the server to the client during the Connect Response. The second stage authenticates the client to the server inside the encrypted tunnel using a hardened password based mechanism. Because these stages occur in different parts of the protocol and rely on different cryptographic constructions, they require separate security analyses. This chapter provides complete proofs that SATP achieves both properties under the assumptions stated earlier.

The results show that server authentication reduces to the collision and preimage resistance of SHAKE256 combined with the integrity of AEAD, while client authentication reduces to the one way security of the SCB function combined with the confidentiality and integrity of AEAD.

10.1 Server Authentication

Server authentication in SATP requires proving that the client accepts a responder as the legitimate server only if the responder possesses both the correct device key $K_{c,i}$ and the server secret ST_c . The protocol accomplishes this by sending the validation hash

$$H_c = \text{SHAKE256}(N_h, K_{c,i}, ST_c)$$

encrypted and authenticated under the newly derived session keys. The client accepts the server only if the decrypted value matches its own recomputation of H_c .

The security definition for server authentication was given in Chapter 7. The proof below demonstrates that forging a valid Connect Response for an uncompromised client requires either inverting SHAKE256 on secret inputs or forging an AEAD ciphertext.

10.1.1 Threat Model

The adversary attempts to impersonate the server during the handshake. The adversary knows:

- The client identity string $ID(c,i)$.
- The client nonce Nh .
- All public protocol fields.
- The structure of the handshake and message formats.

The adversary does not know $K_{c,i}$ or ST_c unless it has compromised the server or branch key.

The adversary's goal is to send a forged Connect Response containing a value H_c^* that the client accepts.

10.1.2 Reduction Structure

We examine the two ways an adversary can succeed.

Case 1: The adversary produces a ciphertext containing a valid H_c^* without knowing the session keys.

This requires forging an AEAD ciphertext under keys derived from $\text{SHAKE256}(K_{c,i}, \text{cfgs}, Nh)$. Because these session keys are indistinguishable from random to the adversary, breaking this condition reduces to an INT-CTXT forgery against the AEAD primitive. From Chapter 9, this probability is negligible.

Case 2: The adversary decrypts or guesses the correct H_c without knowing either $K_{c,i}$ or ST_c .

This requires finding H_c such that:

$$H_c = \text{SHAKE256}(Nh, K_{c,i}, ST_c)$$

with neither $K_{c,i}$ nor ST_c known. Any adversary producing such a value must either:

- invert SHAKE256 on secret inputs,
- find a second preimage for SHAKE256, or
- predict the output of SHAKE256 on unknown components.

Each of these contradicts the assumed security of SHAKE256.

10.1.3 Combined Result

Let $\text{Adv}_{\text{server}}$ denote the adversary's probability of impersonating the server. Then:

$\text{Adv}_{\text{server}}$

$\leq \text{Adv}_{\text{SHAKE256_preimage}}$

- $\text{Adv}_{\text{SHAKE256_collision}}$
- $\text{Adv}_{\text{AEAD_INTCTX}}$
 $\leq \text{negligible}$

Thus SATP satisfies server authentication under the assumed cryptographic guarantees.

10.2 Client Authentication

Client authentication occurs after the tunnel is raised and all subsequent messages are encrypted under R_k , R_n , T_k , and T_n . The client computes a hardened password based secret using the SCB mechanism and sends a derived verifier to the server. The server compares it to its stored reference and accepts or rejects the client.

Formally, the security property requires that an adversary cannot impersonate the client unless it knows the correct passphrase or can break the SCB function.

10.2.1 Threat Model

The adversary is assumed to know:

- All ciphertext transmitted in previous sessions.
- All public protocol metadata.
- All session nonces N_h observed across sessions.

The adversary does not know:

- The client's passphrase.
- The SCB hardened key derived from that passphrase.
- The device key $K_{c,i}$ (unless a client compromise occurs).

Client compromise is modeled separately. The current proof concerns only impersonation without compromise.

10.2.2 Core Proof Idea

The client authentication mechanism is protected by two cryptographic barriers:

1. The SCB output acts as a one way function of the user passphrase.
2. All authentication messages are encrypted and authenticated under AEAD.

To impersonate the client, the adversary must produce a ciphertext containing a valid SCB derived verifier that decrypts without AEAD failure and matches the server's locally stored reference value.

This requires either:

- breaking SCB,
- guessing the passphrase,
- or forging an AEAD ciphertext.

10.2.3 Reduction to SCB One Way Security

Assume an adversary A can impersonate the client with probability $\text{Adv}_{\text{client}}$.

Construct an algorithm B that uses A to invert SCB:

1. B receives an SCB challenge output SCB_{out} and must recover the passphrase.
2. B embeds SCB_{out} as the verifier expected by the server.
3. B gives A all ciphertext and transcript information consistent with this setup.
4. If A successfully impersonates the client, it must produce a valid SCB derived value.
5. B extracts this value and outputs it as the solution.

If A impersonates the client without breaking AEAD, then it must have inverted or guessed the SCB value. Thus:

$$\text{Adv}_{\text{client}} \leq \text{Adv}_{\text{SCB inversion}} + \text{Adv}_{\text{AEAD INTCTXT}}$$

Both terms are negligible under the assumptions in Chapter 6.

10.2.4 AEAD Confidentiality and Structural Leakage

If the adversary cannot break AEAD confidentiality, then it cannot observe or modify any SCB related value in flight. This removes the possibility of:

- chosen ciphertext attacks against SCB messages,
- partial information extraction from encrypted SCB proofs,
- observational leakage of password dependent patterns.

Therefore an impersonation attack requires knowledge of the passphrase.

10.2.5 Combined Result

Let $\text{Adv}_{\text{client}}$ denote the probability of client impersonation without compromise.

Then:

$\text{Adv}_{\text{client}}$

$\leq \text{Adv}_{\text{SCB_inversion}}$

- $\text{Adv}_{\text{SCB_guess}}$
- $\text{Adv}_{\text{AEAD_INTCTX}}$
- $\text{Adv}_{\text{AEAD_INDCCA}}$

All values on the right side are negligible, assuming SCB is configured with sufficient hardness parameters and the AEAD primitive meets its standard guarantees.

Thus SATP satisfies client authentication under the stated assumptions.

10.3 Joint Authentication Security

Because server authentication and client authentication occur in sequential and independent phases, the full authentication guarantee of SATP is the conjunction of both properties:

SATP is jointly authenticated if and only if:

- The server proves possession of ST_c and $K_{c,i}$.
- The client proves possession of its passphrase inside the encrypted tunnel.

Combining the results:

```
Adv_joint  
<= Adv_server + Adv_client  
<= negligible
```

Joint authentication therefore holds as long as:

- SHAKE256 behaves as a secure pseudorandom and preimage resistant function,
 - the AEAD primitive enforces confidentiality and integrity,
 - SCB is configured with sufficient hardness,
 - and SATP endpoints enforce the protocol state machine correctly.
-

10.4 Summary

This chapter has established that SATP satisfies:

1. Server authentication, by reducing forgeries to SHAKE256 preimage resistance and AEAD integrity.
2. Client authentication, by reducing impersonation to SCB one way security and AEAD confidentiality.
3. Joint authentication, by combining the above results.

The next chapter evaluates **forward secrecy, compromise boundaries, and long term security properties** of SATP.

Chapter 11: Conclusion and References

11.1 Conclusion

This report has presented a complete formal analysis of the Secure Authenticated Tunnel Protocol (SATP), grounded in its specification and validated against the reference C implementation. The analysis reconstructed the protocol's deterministic key hierarchy, session derivation process, server validation mechanism, password based user authentication stage, and authenticated encryption transport layer. A precise mathematical model was established, enabling proofs of confidentiality, integrity, server

authentication, client authentication, and replay protection within the adversarial framework defined in earlier chapters.

The evaluation shows that, after the tunnel is raised, SATP provides confidentiality and integrity through the security of its underlying AEAD primitive, assuming IND CCA and INT CTXT guarantees. Server authentication is achieved through the validation hash that binds the session nonce, the device key, and the server secret, and is protected by authenticated encryption. Client authentication is achieved through a hardened SCB derived value transmitted inside the encrypted channel, preventing impersonation except by an adversary who knows the user's passphrase or can invert SCB. Replay resistance follows from strict monotonicity of timestamps and sequence numbers, combined with their binding into the AEAD associated data.

SATP's deterministic key hierarchy establishes clear structural constraints on the protocol. Erasure of the device key after session derivation provides protection against retrospective compromise of a client device, ensuring that past sessions cannot be reconstructed. However, compromise of a branch key enables regeneration of all device keys under that branch and recovery of past session keys. SATP therefore provides limited forward secrecy against client compromise, but it does not provide forward secrecy against compromise of long term server side branch keys. This limitation arises directly from the necessity of deterministic key derivation and does not reflect a failure of the protocol's cryptographic components.

Within these boundaries, SATP achieves its intended security properties for symmetric key authenticated tunneling. The protocol assumes protection of Kroot, Kbr, and STc on the server, high quality randomness for client generated session nonces, correct enforcement of timestamp and sequence number semantics, and appropriate hardness configuration for SCB. When these conditions are met, SATP provides a stable, analyzable, and cryptographically coherent transport layer suitable for deployments where asymmetric cryptography is undesirable or impractical.

This cryptanalysis establishes the theoretical and practical foundations for SATP's security, identifies structural limitations inherent to deterministic hierarchies, and provides a formal basis for secure implementation, review, and future enhancement of the protocol.

11.2 References

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