Online Contests Solutions

Saman Saadi

# Contents

| _ | HackerRank |                 |   |  |  |
|---|------------|-----------------|---|--|--|
|   | 1.1        | New Year Chaos  | 1 |  |  |
|   | 1.2        | Minimum Swaps 2 | 2 |  |  |

iv CONTENTS

## Chapter 1

## **HackerRank**

#### 1.1 New Year Chaos

You can find the question in this link.

We define  $index_i$  as the current index for person i. For example if we have 1,2,3,4 and 4 bribes 3, the queue looks like 1,2,4,3. So  $index_4=3$ . Since no body can bribe more than 2 times,  $index_i \geq i-2$  for  $1 \leq i \leq n$ . Consider person n. No body can bribe that person. So  $n-2 \leq index_n \leq n$ . After we retruned that person to his actual place we can consider n-1. So we have  $n-3 \leq index_{n-1} \leq n-1$  (note that at this moment  $index_n=n$ ).

}

#### 1.2 Minimum Swaps 2

See the problem statement in this link.

Note that this solution is based on Selection Sort in which the number of swaps are minimum. According to Wikipedia: "One thing which distinguishes selection sort from other sorting algorithms is that it makes the minimum possible number of swaps, n-1 in the worst case." Altourh Selection sort has minimum number of swaps among all sorts agorithms, it has  $O(n^2)$  comparisons. Since the final result is  $\{1, 2, \ldots, n\}$ , it's like we have the set in sorted order so we can bypass comparisons and use Selection Sort advantage which is the minimum number of swaps.

We define  $index_i$  as the current index of number i. Suppose we have n numbers, so  $1 \le index_i \le n$ . The goal is to have  $index_i = i$ . Without losing generality suppose  $i < j \land index_i = j$ . There are two cases to consider:

- 1. If  $index_j = i$ , then by swapping  $arr_i$  and  $arr_j$ , we put both i and j in their corresponding positions.
- 2. If  $index_j = k \land k \neq i \land k \neq j$ . In this case by swapping  $arr_i$  and  $arr_j$  we only put i in its corresponding position. So we need to do an extra swap to put j in its correct position.

We can start from i = 1 to i = n and make sure i is in correct position; otherwise we perform a swap. In each iteration we fix the position of one or two numbers. A good example is  $\{4, 3, 2, 1\}$ .

```
1.2. MINIMUM SWAPS 2
```

3

```
return cnt;
}
```