

# NV-center qubits

*This virtual quantum device is inspired by devices reported by the Delft team*

## VQD setup

Set the main directory as the current directory

In[257]:=SetDirectory[NotebookDirectory[]];

Load the QuESTLink package  
*One may also use the off-line questlink.m file, change it to the location of the local file*

In[258]:=Import["https://qtechtheory.org/questlink.m"]

This will download a binary file **quest\_link** from the repo; some error will show if the system tries to override the file

Use **CreateLocalQuESTEnv[quest\_link\_file]** to use the existing binary

In[259]:=CreateDownloadedQuESTEnv[];

Load the **VQD** package; must be loaded after QuESTlink is loaded

In[260]:=Get["../vqd.wl"]

## User device configuration

**Qubit 0** indicates electron spin, and the rest are nuclear spins  $C^{13}$  and  $N^{14}$  – if applicable  
Time unit is **second (s)**  
Frequency unit is **Hertz (Hz)**

```
Options[NVCenterDelft] = {
  QubitNum → 6
  ,
  (* T1 of each qubit *)
  T1 → <|0 → 3600, 1 → 60, 2 → 60, 3 → 60, 4 → 60, 5 → 60 |>
  ,
  (* T2 of each qubit; we assume dynamical decoupling is actively applied *)
  T2 → <|0 → 1.5, 1 → 10, 2 → 10, 3 → 10, 4 → 9, 5 → 9 |>
  ,
  (* dipolar interaction among nuclear spins: cross-talk ZZ-coupling in order of a few Hz on passive noise *)
  FreqWeakZZ → 5
  ,
  (* direct single rotation on Nuclear spin is done via RF, put electron in state -1 leave out the Rx Ry on nuclear spins ideally. *)
  FreqSingleXY → <|0 → 15 * 106, 1 → 500, 2 → 500, 3 → 500, 4 → 500, 5 → 500 |>
  ,
  (* usually done virtually *)
  FreqSingleZ → <|0 → 32 * 106, 1 → 400 * 103, 2 → 400 * 103, 3 → 400 * 103, 4 → 400 * 103, 5 → 400 * 103 |>
  ,
  (* Frequency of CRot gate,
  conditional rotation done via dynamical decoupling or dd+RF. The gate is conditioned on electron spin state *)
  FreqCRot → <|1 → 1.5 * 103, 2 → 2.8 * 103, 3 → 0.8 * 103, 4 → 2 * 103, 5 → 2 * 103 |>
  ,
  (* Fidelity of CRot gate *)
  FidCRot → <|1 → 0.98, 2 → 0.98, 3 → 0.98, 4 → 0.98, 5 → 0.98 |>
  ,
  (* fidelity of x- and y- rotations on each qubit *)
  FidSingleXY → <|0 → 0.9995, 1 → 0.995, 2 → 0.995, 3 → 0.99, 4 → 0.99, 5 → 0.99 |>
  ,
  (* fidelity of z- rotations on each qubit *)
  FidSingleZ → <|0 → 0.9999, 1 → 0.9999, 2 → 0.99999, 3 → 0.9999, 4 → 0.999, 6 → 0.99 |>
  ,
  (* Error ratio of 1-qubit depolarising:dephasing of x- and y- rotations *)
  EFSingleXY → {0.75, 0.25}
  ,
  (* Error ratio of 2-qubit depolarising:dephasing of CRot gate *)
  EFCRot → {0.9, 0.1}
  ,
  (* initialization fidelity on the electron spin *)
  FidInit → 0.999
  ,
  (* initialization duration on the electron spin *)
  DurInit → 2 * 10-3
  ,
  (* measurement fidelity on the electron spin *)
  FidMeas → 0.946
  ,
  (* measurement duration on the electron spin *)
  DurMeas → 2 * 10-5
};
```

## Elementary guide

### Native gates

Direct ilitialisation and measurement are on the NV electron spin only

Init<sub>0</sub>, M<sub>0</sub>

Single-qubit gates

Rx<sub>q</sub>[θ], Ry<sub>q</sub>[θ], Rz<sub>q</sub>[θ]

Two-qubit gates are conditional rotation, where  $CR\sigma[\theta] := \begin{vmatrix} 0 & X & 0 \\ 0 & 0 & 1 \end{vmatrix} \otimes R\sigma[\theta] + \begin{vmatrix} 1 & X & 1 \\ 0 & 0 & 0 \end{vmatrix} \otimes R\sigma[-\theta]$

CRx<sub>0,q</sub>[θ], CRY<sub>0,q</sub>[θ]

others: doing nothing

Wait<sub>q</sub>[duration]

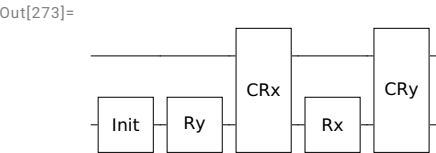
## Common nuclear spin gates, obtained by sequence of native gates

```
In[262]:=
cX::usage = "Controlled-X gate sequence on NV-center";
cY::usage = "Controlled-Y gate sequence on NV-center";
cZ::usage = "Controlled-Z gate sequence on NV-center";
initNcl::usage = "Nuclear spin qubit initialisation sequence on NV-center";
measZ::usage = "Nuclear spin qubit measurement sequence on NV-center";
```

```
In[267]:=
(* cotrolled-pauli gates, where control qubits are the electron spins *)
cXc□t- := Sequence @@ {CRxc□t[ $\pi/2$ ], Rzc[- $\pi/2$ ], Rxt[- $\pi/2$ ]}
cYc□t- := Sequence @@ {CRyc□t[ $\pi/2$ ], Rzc[- $\pi/2$ ], Ryt[- $\pi/2$ ]}
cZc□t- := Sequence @@ {Rxt[ $\pi/2$ ], CRyc□t[- $\pi/2$ ], Rzc[- $\pi/2$ ], Ryt[ $\pi/2$ ], Rxt[- $\pi/2$ ]}
(* initialisation the nuclear spins *)
initNclq-/♦q> := Sequence @@ {Init', Ry'[ $\frac{\pi}{2}$ ], CRx'□q[ $\frac{\pi}{2}$ ], Rx'[ $\frac{\pi}{2}$ ], CRy'□q[- $\frac{\pi}{2}$ ]}
(*measurement sequences on nuclear spins the computational basis *)
measZq-/♦q> := Sequence[Ry'[ $\frac{\pi}{2}$ ], Rxq[ $\frac{\pi}{2}$ ], CRy'□q[- $\frac{\pi}{2}$ ], Rx'[ $\frac{\pi}{2}$ ], M']
```

```
In[272]:=
{initNcl}
DrawCircuit@%
```

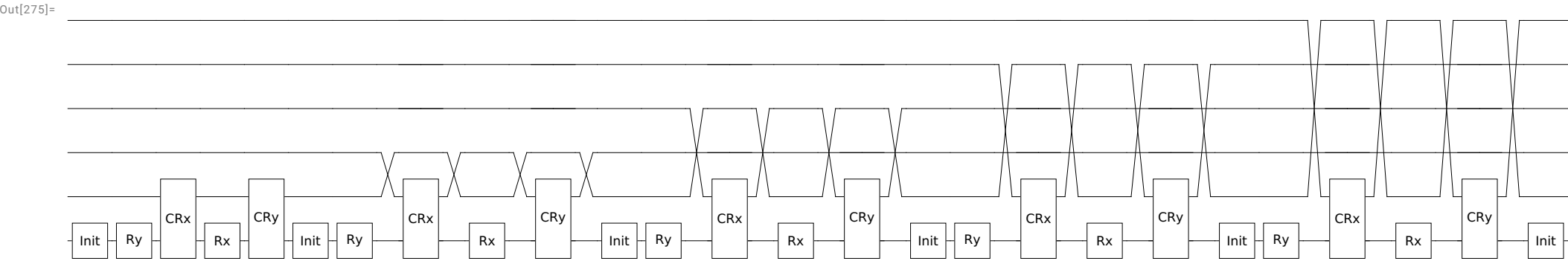
```
Out[272]=
{Init , Ry [ $\frac{\pi}{2}$ ], CRx [ $\frac{\pi}{2}$ ], Rx [ $\frac{\pi}{2}$ ], CRy [- $\frac{\pi}{2}$ ]}
```



## Example: 6 Qubits initialization

Initialize all qubits to zero

```
In[274]:=
circInit = {initNcl', initNcl', initNclμ, initNclσ, initNclι, Init};
DrawCircuit[circInit]
```



```
In[276]:=
ρ = CreateDensityQureg[6];
ρ2 = CreateDensityQureg[6];
ψ = CreateQureg[6];
```

First, create a random mix state. Notice that the fidelity is far from  $|000\,000\rangle$

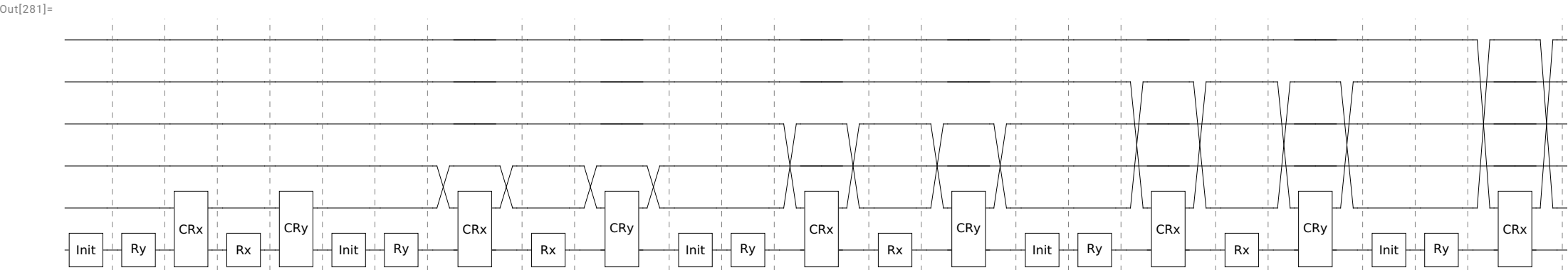
```
In[279]:=
SetQuregMatrix[ρ, RandomMixState[6]];
CalcFidelity[ρ, InitZeroState @ ψ]
```

```
Out[280]=
0.0148492
```

Initialization on the noisy circuit. Serialize[circ] removes parallelism in the circuit.

In practice, the operators are done in serial manner while dynamical-decoupling sequences are applied to passive qubits (qubits that are not operated upon)

```
In[281]:=
DrawCircuit@Serialize@circInit
```



In[282]:=

**circInit**

Out[282]=

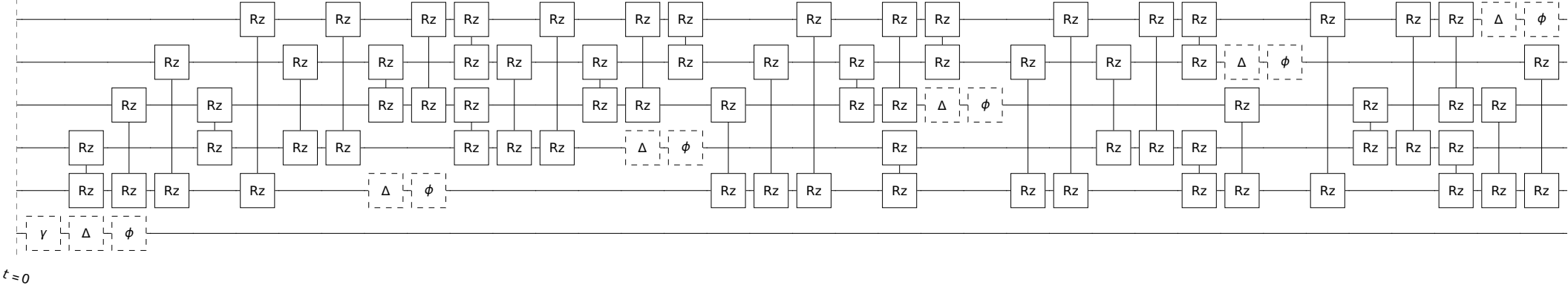
$\{ \text{Init}_0, \text{Ry}_0[\frac{\pi}{2}], \text{CRx}_{0,1}[\frac{\pi}{2}], \text{Rx}_0[\frac{\pi}{2}], \text{CRy}_{0,1}[-\frac{\pi}{2}], \text{Init}_0, \text{Ry}_0[\frac{\pi}{2}], \text{CRx}_{0,2}[\frac{\pi}{2}], \text{Rx}_0[\frac{\pi}{2}], \text{CRy}_{0,2}[-\frac{\pi}{2}], \text{Init}_0, \text{Ry}_0[\frac{\pi}{2}], \text{CRx}_{0,3}[\frac{\pi}{2}],$   
 $\text{Rx}_0[\frac{\pi}{2}], \text{CRy}_{0,3}[-\frac{\pi}{2}], \text{Init}_0, \text{Ry}_0[\frac{\pi}{2}], \text{CRx}_{0,4}[\frac{\pi}{2}], \text{Rx}_0[\frac{\pi}{2}], \text{CRy}_{0,4}[-\frac{\pi}{2}], \text{Init}_0, \text{Ry}_0[\frac{\pi}{2}], \text{CRx}_{0,5}[\frac{\pi}{2}], \text{Rx}_0[\frac{\pi}{2}], \text{CRy}_{0,5}[-\frac{\pi}{2}], \text{Init}_0 \}$

The full noisy initialisation operations

In[346]:=

**circInitOnDev = InsertCircuitNoise[Serialize @ circInit, NVCenterDelft[], ReplaceAliases → True];**  
**DrawCircuit[% , 6]**

Out[347]=



The fidelity is now so closer to the state  $|000\ 000\rangle$

In[285]:=

**ApplyCircuit[CloneQureg[p2, ρ], ExtractCircuit @ circInitOnDev];**  
**CalcFidelity[p2, InitZeroState @ ψ]**

Out[286]=

0.932385

In[287]:=

**DestroyAllQuregs[]**

Measurements

Measurements in the computational basis. Compare 4k shots of measurement to the fidelity set in the device

In[288]:=

**nshots = 1000;**  
**{ρ, ρinit} = CreateDensityQuregs[6, 2];**

On the electron spin

In[290]:=

**outputs =**  
**Flatten @ Table[**  
**ApplyCircuit[InitZeroState @ ρ, ExtractCircuit @ InsertCircuitNoise[{M0}, NVCenterDelft[], ReplaceAliases → True]**  
**,**  
**{nshots}**  
**];**  
**Print["correct outputs(0):" <> ToString[nshots - Total @ outputs],**  
**"\nflipped outputs(1):" <> ToString[Total @ outputs], "\nfidelity:" <> ToString[N[1 - Total @ outputs / nshots]]]**

correct outputs(0):953  
flipped outputs(1):47  
fidelity:0.953

Compare it to the targeted fidelity of measurement

In[292]:=

**OptionValue[NVCenterDelft, FidMeas]**

Out[292]=

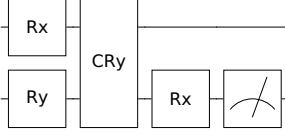
0.946

Measurement on the nuclear spins

In[293]:=

**DrawCircuit[{measZ1}]**

Out[293]=



Should be worse than direct measurement on the electron spin, because it is an indirect measurement

In[294]:=

**dev = NVCenterDelft[];**

In[295]:=

```
nshots = 1000;
outputs = Flatten@Table[
  ApplyCircuit[InitZeroState@ρ, ExtractCircuit@InsertCircuitNoise[{measZ1}, NVCenterDelft[], ReplaceAliases → True]], {nshots}];
Print["correct outputs(0):" <> ToString[nshots - Total@outputs],
  "\nflipped outputs(1):" <> ToString[Total@outputs], "\nfidelity:" <> ToString[N[1 - Total[outputs]/nshots]]]

correct outputs(0):937
flipped outputs(1):63
fidelity:0.937
```

# Paper supplement: BCS dynamic simulation

## (<https://arxiv.org/abs/2306.07342>)

### Trotterization

It requires around one thousand gates -- before conversion to the native NV-gates. See [supplement/BCSonVNCenterDelft/BCSDynamicsTrotter.nb](#)

### BCS simulation

#### Setting up the Hamiltonian

Set the constants for the Hamiltonian

In[298]:=

```
(* non-interacting harmonic oscillator-type energy levels *)
ϵ = ω (# + 0.5) & /@ Range[0, 4];
(* time-dependent coupling function *)
coupling[t_, g0_, gc_] := ExpandAll[
  (ArcTan[(t - t1) J / (ħ Γ)] + π / 2) (ArcTan[(t2 - t) J / (ħ Γ)] + π / 2) (gc - g0) / π^2 + g0
]
```

In[300]:=

```
constants = {
  (* time start to quench and reverse. J is an arbitrary energy unit *)
  t1 → 9 ħ / J,
  t2 → 18 ħ / J,
  (* initial coupling constant*)
  Γ → 0.1,
  (* frequency *)
  ω → 5 J / 3
}
```

Out[300]=

$$\left\{t1 \rightarrow \frac{9 \hbar}{J}, t2 \rightarrow \frac{18 \hbar}{J}, \Gamma \rightarrow 0.1, \omega \rightarrow \frac{5 J}{3}\right\}$$

In[301]:=

```
(* mean-field eigenvalues *)
Ej[ϵ_, Δ_] := Sqrt[ϵ^2 + Abs[Δ]^2]
(* superconducting gap *)
(*  $\frac{2}{g} = \sum_k \frac{1}{E_k} \tanh\left[\frac{E_k}{2k_b \text{Temp}}\right]$  *)
(* since we consider temperature Temp=0, tanh(∞)=1 *)
(* Superconducting gaps*)
Δ0 = J;
Δc = 2 J;
```

In[304]:=

$$g0 = 2 \bigg/ \text{Total}\left[\frac{1}{Ej[\epsilon, \Delta0]}\right];$$
$$gc = 2 \bigg/ \text{Total}\left[\frac{1}{Ej[\epsilon, \Delta c]}\right];$$

The entire Hamiltonain

In[306]:=

```
(* Gaudin term *)
Hgaudin[q_, n_, ϵ_, g_] := Total@Table[
  
$$\frac{\{X_q, Y_q, Z_q\} \cdot \{X_j, Y_j, Z_j\}}{2 (\epsilon[[q + 1]] - \epsilon[[j + 1]])}, \{j, \text{Complement[Range[0, n - 1], \{q\}]\}\right] + \frac{Z_q}{g}$$

]
```

```
(* HBCS *)
HBCS[n_, ε_, τ_] := With[{g = coupling[τ * ħ / Δ0, g0, gc] /. constants},
  SimplifyPaulis@Chop@ExpandAll[
    Total@Table[
      Simplify[ $\left(-g \epsilon[q+1] + \frac{g^2}{2}\right) \frac{\text{Hgaudin}[q, n, \epsilon, g]}{\Delta 0} /. constants, J > 0]$ 
      , {q, n-1}] +
      SimplifyPaulis@Chop@ExpandAll[SimplifyPaulis@Simplify[ $\frac{g^3}{4 \Delta 0} * (\text{Total@Table[Hgaudin}[q, n, \epsilon, g], \{q, 0, n-1\}]^2 /. constants, J > 0]$ ]]
    ]
  ]
```

Set up the time discretisation and the quench g(τ)

In[308]:=

```
(* Medium resolution *)
rs = Sort@DeleteDuplicates@Chop@Join[{0., 4., 8.}, Range[8., 20., 0.2], {20., 23.5, 27}]
(* the timesteps *)
δτ = Table[rs[[i]] - rs[[i - 1]], {i, 2, Length@rs}];
PrependTo[δτ, 0];
(*sanity check*)
And@@Table[rs[[i]] == Total[δτ[[#]] & /@ Range[i]], {i, Length@rs}]
(*τ=t J/ħ*)
```

Out[308]=

```
{0, 4., 8., 8.2, 8.4, 8.6, 8.8, 9., 9.2, 9.4, 9.6, 9.8, 10., 10.2, 10.4, 10.6, 10.8, 11., 11.2, 11.4, 11.6, 11.8, 12.,
  12.2, 12.4, 12.6, 12.8, 13., 13.2, 13.4, 13.6, 13.8, 14., 14.2, 14.4, 14.6, 14.8, 15., 15.2, 15.4, 15.6, 15.8, 16., 16.2,
  16.4, 16.6, 16.8, 17., 17.2, 17.4, 17.6, 17.8, 18., 18.2, 18.4, 18.6, 18.8, 19., 19.2, 19.4, 19.6, 19.8, 20., 23.5, 27}
```

Out[311]=

True

In[312]:=

```
(*τ=t J/ħ*)
```

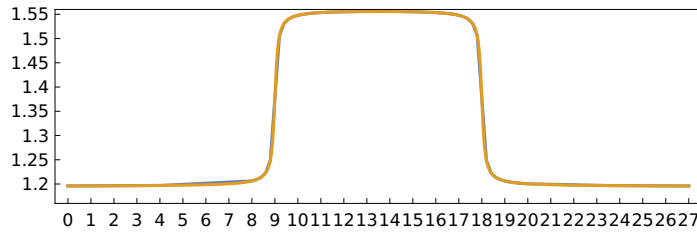
In[313]:=

```
(* dense quench for reference *)
gdense << "../supplement/BCSonNVCenterDelft/gdense.mx";
```

In[314]:=

```
(* See the quench almost overlap with the discretised one *)
gvals = Simplify[(coupling[# * ħ / Δ0, g0, gc] / Δ0 & /@ rs) /. constants, J > 0];
ListPlot[{Transpose@{rs, gvals}, gdense}, PlotRange → {1.16, 1.56}, Joined → True,
  AspectRatio → 0.3, Frame → True, FrameTicks → {{Range[1, 1.55, 0.05], None}, {Range[0, 27, 1], None}}]
```

Out[315]=



## Simulations on various noise scenarios

In[316]:=

```
summarycss2 << "../supplement/BCSonNVCenterDelft/summarycss2.mx";
```

In[317]:=

```
CustomGatesDefinitions = {SWindex1, index2[θ] → Uindex1, index2[{1, 0, 0, 0}, {0,  $e^{i\frac{\theta}{2}}$  Cos[ $\frac{\theta}{2}$ ], -i  $e^{i\frac{\theta}{2}}$  Sin[ $\frac{\theta}{2}$ ], 0}, {0, -i  $e^{i\frac{\theta}{2}}$  Sin[ $\frac{\theta}{2}$ ],  $e^{i\frac{\theta}{2}}$  Cos[ $\frac{\theta}{2}$ ], 0}, {0, 0, 0, 1}]},
  CRxe, n[θ] → Subscript[U, e, n][{Cos[θ/2], 0, -I Sin[θ/2], 0}, {0, Cos[θ/2], 0, I Sin[θ/2]}, {-I Sin[θ/2], 0, Cos[θ/2], 0}, {0, I Sin[θ/2], 0, Cos[θ/2]}]},
  CRYe, n[θ] → Subscript[U, e, n][{Cos[θ/2], 0, -Sin[θ/2], 0}, {0, Cos[θ/2], 0, Sin[θ/2]}, {Sin[θ/2], 0, Cos[θ/2], 0}, {0, -Sin[θ/2], 0, Cos[θ/2]}]}];
CustomGatesDraw = {SWindex1, index2[_] → SWAPindex1, index2};
```

In[319]:=

```
noisyBCS[ρ_, ρinit_, ψinit_, vdopt_ : {}] := Module[{τ, rexnactnoisy, noisycirc, fid},
  τ = 0;
  CloneQureg[ρ, ρinit];
  rexnactnoisy = {{0, 1}};
  Table[
    noisycirc = ExtractCircuit @ InsertCircuitNoise[List /@ sum["circnvc"], NVCenterDelft[Sequence @@ vdopt]];
    noisycirc = DeleteCases[DeleteCases[noisycirc, __[0.]], __[0]];
    ApplyCircuit[ρ, noisycirc /. CustomGatesDefinitions];
    fid = CalcFidelity[ρ, ψinit];
    τ += sum["δ"];
    AppendTo[rexnactnoisy, {τ, fid}];
    (*<|"τ"→τ,"δ"→sum["δ"],"fidnoisy"→fid,"εnoisy"→Abs[sum["fidexact"]-fid]|>*)
    , {sum, summarycss2}];
  rexnactnoisy
]
```

## A realistic setting of virtual NV-center device -- inspired from the paper

In[320]:=

```
Options[NVCenterDelft] = {
  QubitNum → 5
  ,
  T1 → <| 0 → 3600, 1 → 60, 2 → 60, 3 → 60, 4 → 60 |>
  ,
  T2 → <| 0 → 1.5, 1 → 10, 2 → 10, 3 → 10, 4 → 9 |>
  ,
  FreqWeakZZ → 5
  ,
  FreqSingleXY → <| 0 → 15 * 10^6, 1 → 500, 2 → 500, 3 → 500, 4 → 500 |>
  ,
  FreqSingleZ → <| 0 → 32 * 10^6, 1 → 400 * 10^3, 2 → 400 * 10^3, 3 → 400 * 10^3, 4 → 400 * 10^3 |>
  ,
  FreqCRot → <| 1 → 1.5 * 10^3, 2 → 2.8 * 10^3, 3 → 0.8 * 10^3, 4 → 2 * 10^3 |>
  ,
  FidCRot → <| 1 → 0.98, 2 → 0.98, 3 → 0.98, 4 → 0.98 |>
  ,
  FidSingleXY → <| 0 → 0.9995, 1 → 0.995, 2 → 0.995, 3 → 0.99, 4 → 0.99 |>
  ,
  FidSingleZ → <| 0 → 1, 1 → 1, 2 → 1, 3 → 1, 4 → 1 |>
  ,
  EFSingleXY → {0.75, 0.25}
  ,
  EFCRot → {0.9, 0.1}
  ,
  FidInit → 0.999
  ,
  DurInit → 2 * 10^-3
  ,
  FidMeas → 0.946
  ,
  DurMeas → 2 * 10^-5
};
```

Several tested error scenarios -- these can be flexibly changed/added :

- 1) Exact unitary using **MatrixExp[]**
- 2) Checking using the resulting CSS compilation
- 3) Realistic numbers from Mohammed
- 4) Perfect gates with realistic decoherence
- 5) Extremely high gates fidelity 99.999, realistic decoherence
- 6) 10x longer decoherece with excellent gates 99.999

In[321]:=

```
Labels = <|
  1 → "Exact propagator",
  2 → "Subspace compilation",
  3 → "Realistic noise",
  4 → "Gates fidelity 99.999, no cross-talk",
  5 → "Gates fidelity 99.999",
  6 → "10x of T1,T2",
  7 → "Gates fidelity 99.999, 10x of T1,T2",
  8 → "Gates fidelity 99.999, 10x of T1,T2, no cross-talk"
|>;
```

```
(*
Prepare initialisation state in  $\psi_{\text{init}}$  as an exact groundstate from  $H_{\text{BCS}}$ 
*)
DestroyAllQuregs[];
 $\psi_{\text{init}}$  = CreateQureg[5];
hbcs0 = HBCS[5,  $\epsilon$ , 0];
{eigval, eigvec} = Eigensystem[CalcPauliStringMatrix@hbcs0];
Ordering[eigval, 1];
initv = eigvec[[First@Ordering[eigval, 1]]];
initmat = (List/@initv).Conjugate[{initv}];
{ $\rho$ ,  $\rho_{\text{init}}$ } = CreateDensityQuregs[5, 2];
SetQuregMatrix[ $\rho_{\text{init}}$ , initmat];
SetQuregMatrix[ $\psi_{\text{init}}$ , initv];

(*

Load other data for result comparison:
    exact propagator,
    approximation by compilation in the subspace and converted to the native NVC gates

*)
rexactot2 << "../supplement/BCSonNVCenterDelft/rexactot2.mx";
rexactcompcss << "../supplement/BCSonNVCenterDelft/rexactcompcss.mx";
```

The main execution on scaling the noise.  
This is highly configurable.

```
(*

Here are some used options
    optgates: set all qubits fidelity to 99.999
    optdec: set all decoherece T1 and T2 to 10x longer

*)
optgates = {FidCRot → Association[{# → .99999} & /@ Range[4]], FidSingleXY → Association[{# → .99999} & /@ Range[0, 4]]];
optdec = {T1 → <|0 → 36 000, 1 → 600, 2 → 600, 3 → 600, 4 → 600 |>, T2 → <|0 → 15, 1 → 100, 2 → 100, 3 → 100, 4 → 90 |>};

(*

The main execution: notice that we can just change the options. Feel free to change/add here
*)
bcsfidelities = <|
    1 → rexactot2,
    2 → rexactcompcss,
    3 → noisyBCS[ $\rho$ ,  $\rho_{\text{init}}$ ,  $\psi_{\text{init}}$ ],
    4 → noisyBCS[ $\rho$ ,  $\rho_{\text{init}}$ ,  $\psi_{\text{init}}$ , Join[optgates, {FreqWeakZZ → False}]],
    5 → noisyBCS[ $\rho$ ,  $\rho_{\text{init}}$ ,  $\psi_{\text{init}}$ , optgates],
    6 → noisyBCS[ $\rho$ ,  $\rho_{\text{init}}$ ,  $\psi_{\text{init}}$ , optdec],
    7 → noisyBCS[ $\rho$ ,  $\rho_{\text{init}}$ ,  $\psi_{\text{init}}$ , Join[optgates, optdec]],
    8 → noisyBCS[ $\rho$ ,  $\rho_{\text{init}}$ ,  $\psi_{\text{init}}$ , Join[optgates, optdec, {FreqWeakZZ → False}]]
|>;
```

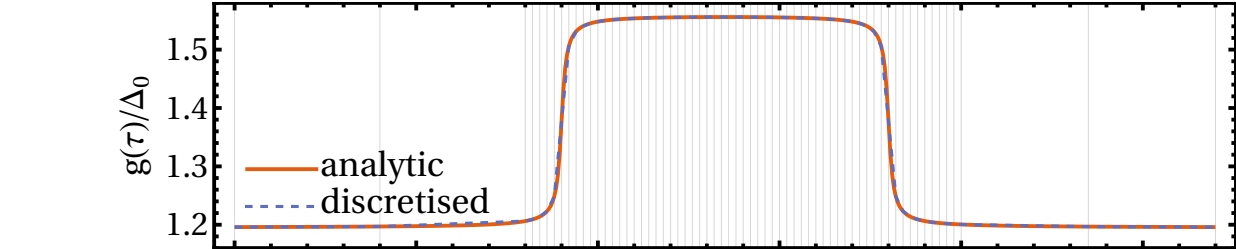
```
In[337]:=
plotstyles = {PlotRange → All,
    PlotTheme → "Scientific",
    AspectRatio → .6,
    Background → White,
    ImageSize → 600,
    Frame → True,
    FrameStyle → Directive[Thick, Black, 17],
    BaseStyle → {16},
    GridLines → {rs, None},
    GridLinesStyle → Directive[GrayLevel[0.8, 0.8], Thin]
};
```



In[338]:=

```
(*
Beautiful plot for the quench potential
*)
keys = {"analytic", "discretised"};
bcs1 = ListPlot[
  {gdense, Transpose@{rs, gvals}},
  PlotRange -> {1.16, 1.58},
  Joined -> {True, True},
  AspectRatio -> 0.24,
  PlotStyle -> {Thick, Dashed},
  PlotLegends -> Placed[LineLegend[keys, Spacings -> 0], {.15, .25}],
  FrameLabel -> {{{"g(τ)/Δ₀", None}, {None, None}},
  ImagePadding -> {{58, 10}, {0, 0}},
  Sequence @@ plotstyles]
```

Out[339]=

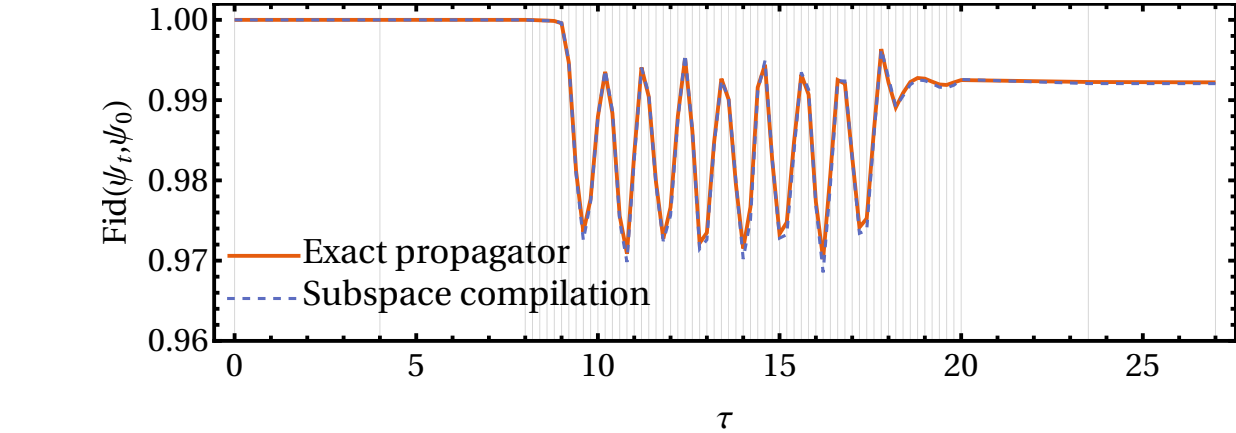


The compilation outputs for a reference

In[340]:=

```
keys = {1, 2};
bcs2 = ListPlot[
  bcsfidelities/@keys,
  Joined -> ConstantArray[True, Length@keys],
  PlotStyle -> Join[{Thick}, ConstantArray[Dashed, Length@keys - 1]],
  PlotLegends -> Placed[LineLegend[labels/@keys, Spacings -> 0], {.22, .2}],
  PlotRange -> {Automatic, {0.96, 1.002}},
  AspectRatio -> .33,
  ImagePadding -> {{58, 10}, {50, 0}},
  FrameLabel -> {"τ", "Fid(ψt, ψ0)"},
  Sequence @@ plotstyles
]
```

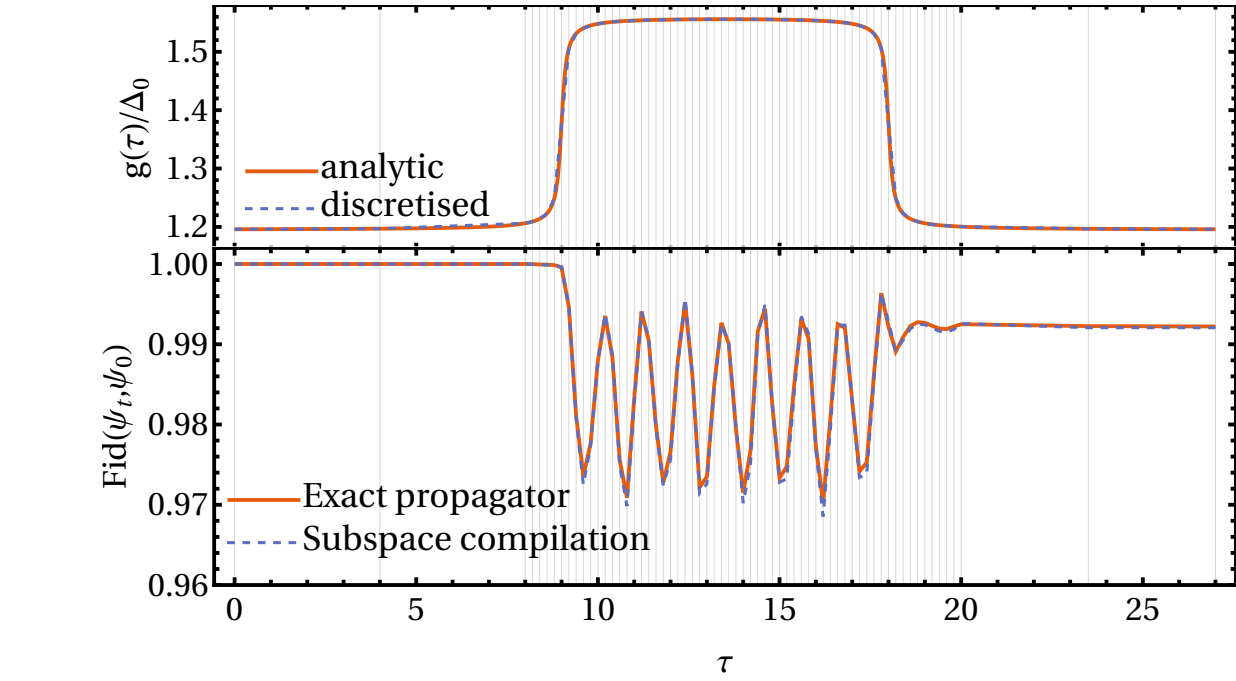
Out[341]=



In[342]:=

```
Column[{bcs1, bcs2}, Spacings -> -0.1]
(*Export["quench.pdf", %]*)
```

Out[342]=



```
(*
The final plot after various trials
*)
keys = {1, 2, 8, 7, 4, 5, 6, 3};
bcs3 = ListPlot[
  bcsfidelities/@keys,
  Joined -> ConstantArray[True, Length@bcsfidelities],
  PlotStyle -> {Thick, Dashed, Thick, Thick, Thick, Thick, Dashed, Thick},
  AspectRatio -> 0.8,
  PlotLegends ->
    Placed[LineLegend[labels/@keys, Spacings -> 0, LegendFunction -> (Framed[#, FrameStyle -> (Antialiasing -> False), FrameMargins -> 0] &)],
      {0.4, 0.2}],
  ImagePadding -> {{58, 10}, {50, 0}},
  FrameLabel -> {"τ", "Fid(ψ₀, ψₜ)"},
  PlotRange -> {{0, 27}, {0.0, 1.03}},
  BaseStyle -> {14},
  Sequence @@ plotstyles
]
(*Export["bcsall.pdf", %]*)
```

Out[344]=

