

# NV-center qubits

*This virtual quantum device is inspired by devices reported by the Delft team*

---

## VQD setup

Set the main directory as the current directory

```
In[1]:= SetDirectory[NotebookDirectory[]];
```

Load the QuESTLink package

*One may also use the off-line questlink.m file, change it to the location of the local file*

```
In[2]:= Import["https://qtechtheory.org/questlink.m"]
```

This will download a binary file **quest\_link** if there is no such file found

Otherwise, use a locally-compiled that called **quest\_link\***

```
In[3]:= (* Search for existing files that match the pattern "quest_link*" *)
With[{questLinkFiles = Sort@FileNames["quest_link*", {NotebookDirectory[]}]},
,
If[Length[questLinkFiles] > 0,
(* If one or more matching files are found,
use the first one alphabetically *)
Print["Using the existing link file: ", First@questLinkFiles];
CreateLocalQuESTEnv[First@questLinkFiles];
,
(*If no matching files are found, download the link file*)
Print["No link file found, download quest_link"];
CreateDownloadedQuESTEnv[];
];
]
```

Load the **VQD** package; must be loaded after QuESTlink is loaded

```
In[4]:= Get["../vqd.wl"]
```

## User device configuration

**Qubit 0** indicates electron spin, and the rest are nuclear spins  $C^{13}$  and  $N^{14}$  – if applicable  
 Time unit is **second (s)**  
 Frequency unit is **Hertz (Hz)**

```
In[5]:= Options[NVCenterDelft] = {
  QubitNum → 6
  ,
  (* T1 of each qubit *)
  T1 → <| 0 → 3600, 1 → 60, 2 → 60, 3 → 60, 4 → 60, 5 → 60 |>
  ,
  (* T2 of each qubit; we assume dynamical decoupling is actively applied *)
  T2 → <| 0 → 1.5, 1 → 10, 2 → 10, 3 → 10, 4 → 9, 5 → 9 |>
  ,
  (* dipolar interaction among nuclear
    spins: cross-talk ZZ-coupling in order of a few Hz on passive noise *)
  FreqWeakZZ → 5
  ,
  (* direct single rotation on Nuclear spin is done via RF,
    put electron in state -1 leave out the Rx Ry on nuclear spins ideally. *)
  FreqSingleXY → <| 0 → 15 * 106, 1 → 500, 2 → 500, 3 → 500, 4 → 500, 5 → 500 |>
  ,
  (* usually done virtually *)
  FreqSingleZ → <| 0 → 32 * 106, 1 → 400 * 103,
    2 → 400 * 103, 3 → 400 * 103, 4 → 400 * 103, 5 → 400 * 103 |>
  ,
  (* Frequency of CRot gate,
    conditional rotation done via dynamical decoupling or dd+
    RF. The gate is conditioned on electron spin state *)
  FreqCRot → <| 1 → 1.5 * 103, 2 → 2.8 * 103, 3 → 0.8 * 103, 4 → 2 * 103, 5 → 2 * 103 |>
  ,
  (* Fidelity of CRot gate *)
  FidCRot → <| 1 → 0.98, 2 → 0.98, 3 → 0.98, 4 → 0.98, 5 → 0.98 |>
  ,
  (* fidelity of x- and y- rotations on each qubit *)
  FidSingleXY → <| 0 → 0.9995, 1 → 0.995, 2 → 0.995, 3 → 0.99, 4 → 0.99, 5 → 0.99 |>
  ,
}
```

```

(* fidelity of z- rotations on each qubit *)
FidSingleZ → <| 0 → 0.9999,
  1 → 0.9999, 2 → 0.99999, 3 → 0.9999, 4 → 0.999, 6 → 0.99 |>
,
(* Error ratio of 1-qubit depolarising:dephasing of x- and y- rotations *)
EFSingleXY → {0.75, 0.25}
,
(* Error ratio of 2-qubit depolarising:dephasing of CRot gate *)
EFCRot → {0.9, 0.1}
,
(* initialization fidelity on the electron spin *)
FidInit → 0.999
,
(* initialization duration on the electron spin *)
DurInit → 2 * 10-3
,
(* measurement fidelity on the electron spin *)
FidMeas → 0.946
,
(* measurement duration on the electron spin *)
DurMeas → 2 * 10-5
};

```

---

## Elementary guide

### Native gates

*Direct initialization and measurement are on the NV electron spin only*

$\text{Init}_0, M_0$

*Single-qubit gates*

$\text{Rx}_q[\theta], \text{Ry}_q[\theta], \text{Rz}_q[\theta]$

*Two-qubit gates are conditional rotation, where  $\text{CR}\sigma[\theta] := \begin{vmatrix} 0 & X & 0 \\ \end{vmatrix} \otimes \text{R}\sigma[\theta] + \begin{vmatrix} 1 & X & 1 \\ \end{vmatrix} \otimes \text{R}\sigma[-\theta]$*

$\text{CR}_{x_0,q}[\theta], \text{CR}_{y_0,q}[\theta]$

*others: doing nothing*

$\text{Wait}_q[\text{duration}]$

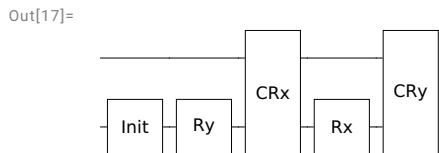
## Common nuclear spin gates, obtained by sequence of native gates

```
In[6]:= cX::usage = "Controlled-X gate sequence on NV-center";
cY::usage = "Controlled-Y gate sequence on NV-center";
cZ::usage = "Controlled-Z gate sequence on NV-center";
initNcl::usage = "Nuclear spin qubit initialisation sequence on NV-center";
measZ::usage = "Nuclear spin qubit measurement sequence on NV-center";
```

```
In[11]:= (* cotrolled-pauli gates, where control qubits are the electron spins *)
cXc,t := Sequence @@ {CRx,c,t[ $\pi/2$ ], Rz,c[- $\pi/2$ ], Rx,t[- $\pi/2$ ]}
cYc,t := Sequence @@ {CRy,c,t[ $\pi/2$ ], Rz,c[- $\pi/2$ ], Ry,t[- $\pi/2$ ]}
cZc,t := Sequence @@ {Rx,t[ $\pi/2$ ], CRy,c,t[- $\pi/2$ ], Rz,c[- $\pi/2$ ], Ry,t[ $\pi/2$ ], Rx,t[- $\pi/2$ ]}
(* initialisation the nuclear spins *)
initNclq,; := Sequence @@ {Init0, Ry0[ $\frac{\pi}{2}$ ], CRx,0,q[ $\frac{\pi}{2}$ ], Rx0[ $\frac{\pi}{2}$ ], CRy,0,q[- $\frac{\pi}{2}$ ]}
(*measurement sequences on nuclear spins the computational basis *)
measZq,; := Sequence[Ry0[ $\frac{\pi}{2}$ ], Rxq[ $\frac{\pi}{2}$ ], CRy,0,q[- $\frac{\pi}{2}$ ], Rx0[ $\frac{\pi}{2}$ ], M0]
```

```
In[16]:= {initNcl1}
DrawCircuit@%
```

```
Out[16]= {Init0, Ry0[ $\frac{\pi}{2}$ ], CRx,0,1[ $\frac{\pi}{2}$ ], Rx0[ $\frac{\pi}{2}$ ], CRy,0,1[- $\frac{\pi}{2}$ ]}
```

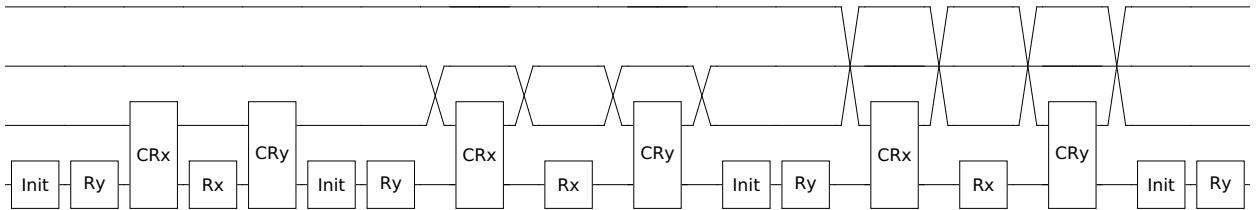


## Example: 6 Qubits initialization

Initialize all qubits to zero

```
In[18]:= circInit = {initNcl , initNcl , initNcl , initNcl , initNcl , Init };
DrawCircuit[circInit]
```

Out[19]=



```
In[20]:=  $\rho$  = CreateDensityQureg[6];
 $\rho_2$  = CreateDensityQureg[6];
 $\psi$  = CreateQureg[6];
```

First, create a random mix state. Notice that the fidelity is far from  $|000\ 000\rangle$

```
In[23]:= SetQuregMatrix[ $\rho$ , RandomMixState[6]];
CalcFidelity[ $\rho$ , InitZeroState @  $\psi$ ]
```

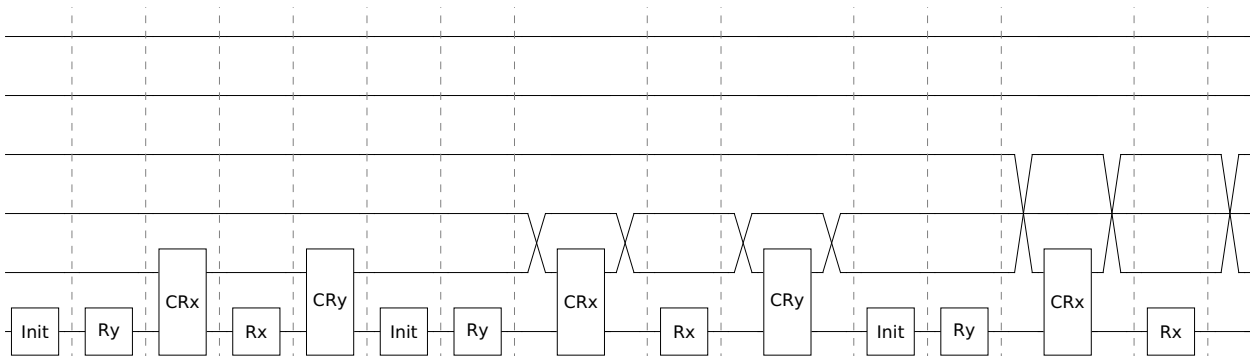
Out[24]=

0.0194058

Initialization on the noisy circuit. Serialize[circ] removes parallelism in the circuit.  
In practice, the operators are done in serial manner while dynamical-decoupling sequences are applied to passive qubits (qubits that are not operated upon)

```
In[25]:= DrawCircuit@Serialize@circInit
```

Out[25]=



In[26]:= **circInit**

Out[26]=

$$\left\{ \text{Init}_0, \text{Ry}_0\left[\frac{\pi}{2}\right], \text{CRx}_{0,1}\left[\frac{\pi}{2}\right], \text{Rx}_0\left[\frac{\pi}{2}\right], \text{CRY}_{0,1}\left[-\frac{\pi}{2}\right], \text{Init}_0, \text{Ry}_0\left[\frac{\pi}{2}\right], \text{CRx}_{0,2}\left[\frac{\pi}{2}\right], \text{Rx}_0\left[\frac{\pi}{2}\right], \right. \\ \left. \text{CRY}_{0,2}\left[-\frac{\pi}{2}\right], \text{Init}_0, \text{Ry}_0\left[\frac{\pi}{2}\right], \text{CRx}_{0,3}\left[\frac{\pi}{2}\right], \text{Rx}_0\left[\frac{\pi}{2}\right], \text{CRY}_{0,3}\left[-\frac{\pi}{2}\right], \text{Init}_0, \text{Ry}_0\left[\frac{\pi}{2}\right], \right. \\ \left. \text{CRx}_{0,4}\left[\frac{\pi}{2}\right], \text{Rx}_0\left[\frac{\pi}{2}\right], \text{CRY}_{0,4}\left[-\frac{\pi}{2}\right], \text{Init}_0, \text{Ry}_0\left[\frac{\pi}{2}\right], \text{CRx}_{0,5}\left[\frac{\pi}{2}\right], \text{Rx}_0\left[\frac{\pi}{2}\right], \text{CRY}_{0,5}\left[-\frac{\pi}{2}\right], \text{Init}_0 \right\}$$

In[27]:= (\*

noisy initialisation circuit on the specified device

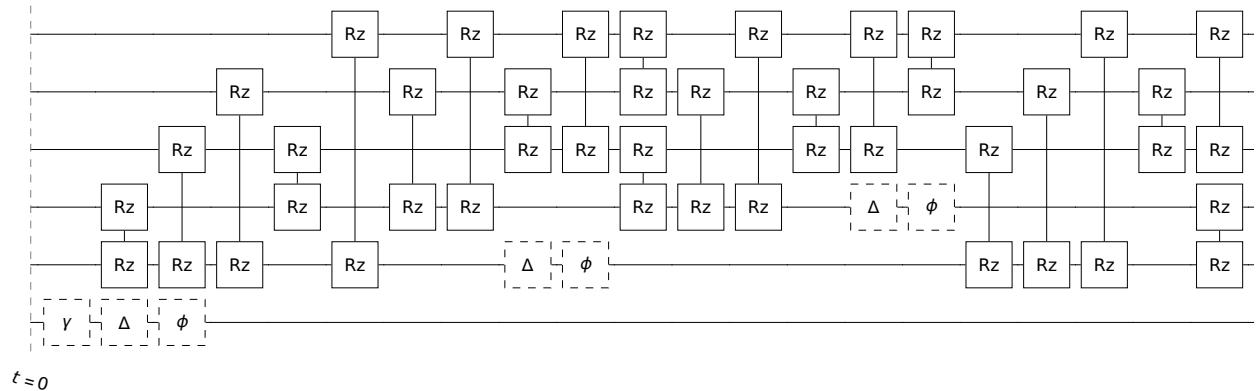
\*)

**circInitOnDev =**

**InsertCircuitNoise[Serialize @ circInit, NVCenterDelft[], ReplaceAliases → True];**

**DrawCircuit[%, 6]**

Out[28]=



The fidelity is now so closer to the state  $|000\,000\rangle$

In[29]:= **ApplyCircuit[CloneQureg[ρ2, ρ], ExtractCircuit @ circInitOnDev];**

**CalcFidelity[ρ2, InitZeroState @ ψ]**

Out[30]=

0.932416

In[31]:= **DestroyAllQuregs[]**

## Measurements

Measurements in the computational basis. Compare 4k shots of measurement to the fidelity set in the device

```
In[32]:= nshots = 1000;
        { $\rho$ ,  $\rho_{\text{init}}$ } = CreateDensityQuregs[6, 2];
```

## On the electron spin

```
In[34]:= outputs =
  Flatten @ Table[
    ApplyCircuit[InitZeroState @  $\rho$ , ExtractCircuit @
      InsertCircuitNoise[{M}, NVCenterDelft[], ReplaceAliases → True]]
    ,
    {nshots}
  ];
  Print["correct outputs(0):" <> ToString[nshots - Total @ outputs],
    "\nflipped outputs(1):" <> ToString[Total @ outputs],
    "\nfidelity:" <> ToString[N[1 - Total @ outputs / nshots]]]

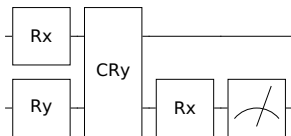
correct outputs(0):941
flipped outputs(1):59
fidelity:0.941
```

Compare it to the targeted fidelity of measurement

```
In[36]:= OptionValue[NVCenterDelft, FidMeas]
Out[36]=
0.946
```

## Measurement on the nuclear spins

```
In[37]:= DrawCircuit[{measZ}]
Out[37]=
```



Should be worse than direct measurement on the electron spin, because it is an indirect measurement

```
In[38]:= dev = NVCenterDelft[];
```

```

In[39]:= nshots = 1000;
outputs = Flatten@Table[
  ApplyCircuit[InitZeroState@ρ, ExtractCircuit@
    InsertCircuitNoise[{measZ}, NVCenterDelft[], ReplaceAliases → True]], {nshots}];
Print["correct outputs(0):" <> ToString[nshots - Total@outputs],
  "\nflipped outputs(1):" <> ToString[Total@outputs],
  "\nfidelity:" <> ToString[N[1 - Total[outputs] / nshots]]]

correct outputs(0):938
flipped outputs(1):62
fidelity:0.938

```

## Paper supplement: BCS dynamic simulation

### Trotterization

It requires around one thousand gates -- before conversion to the native NV-gates. See **supplement/BCSonNVCenterDelft/BCSDynamicsTrotter.nb**

### BCS simulation

#### Setting up the Hamiltonian

Set the constants for the Hamiltonian

```

In[42]:= (* non-interacting harmonic oscillator-type energy levels *)
ε = ω (# + 0.5) & /@ Range[0, 4];
(* time-dependent coupling function *)
coupling[t_, g0_, gc_] := ExpandAll[
  (ArcTan[(t - t1) J / (ħ Γ)] + π / 2) (ArcTan[(t2 - t) J / (ħ Γ)] + π / 2) (gc - g0) / π + g0
]

```



```
In[44]:= constants = {
  (* time start to quench and reverse. J is an arbitrary energy unit *)
  t1 → 9 ħ/J,
  t2 → 18 ħ/J,
  (* initial coupling constant*)
  Γ → 0.1,
  (* frequency *)
  ω → 5 J/3
}
```

Out[44]=

$$\left\{ t1 \rightarrow \frac{9 \hbar}{J}, t2 \rightarrow \frac{18 \hbar}{J}, \Gamma \rightarrow 0.1, \omega \rightarrow \frac{5 J}{3} \right\}$$

```
In[45]:= (* mean-field eigenvalues *)
Ej[ε_, Δ_] := Sqrt[ε^2 + Abs[Δ]^2]
(* superconducting gap *)
(* g = Σ_k 1/E_k tanh[E_k/(k_B Temp)] *)
(* since we consider temperature Temp=0, tanh(∞)=1 *)
(* Superconducting gaps*)
Δ0 = J;
Δc = 2 J;
```

```
In[48]:= g0 = 2 / Total[1/Ej[ε, Δ0]];
gc = 2 / Total[1/Ej[ε, Δc]];
```

The entire Hamiltonian

```
In[50]:= (* Gaudin term *)
Hgaudin[q_, n_, ε_, g_] :=
  Total@Table[
    {Xq, Yq, Zq} · {Xj, Yj, Zj} /
    2 (ε[[q + 1]] - ε[[j + 1]]), {j, Complement[Range[0, n - 1], {q}]}] +
  Zq / g
```

```
In[51]:= (* HBCS *)
HBCS[n_, ε_, τ_] := With[{g = coupling[τ*ħ/Δ0, g0, gc] /. constants},
  SimplifyPaulis@Chop@ExpandAll[
    Total@Table[
      Simplify[ $\left(-g \epsilon[q+1] + \frac{g}{2}\right) \frac{\text{Hgaudin}[q, n, \epsilon, g]}{\Delta 0}$  /. constants, J > 0]
      , {q, n-1}] +
    SimplifyPaulis@Chop@ExpandAll[SimplifyPaulis@Simplify[
       $\frac{g^\mu}{4 \Delta 0} * (\text{Total}@\text{Table}[\text{Hgaudin}[q, n, \epsilon, g], \{q, 0, n-1\}])$  /. constants, J > 0]]
  ]
]
```

Set up the time discretisation and the quench  $g(\tau)$

```
In[52]:= (* Medium resolution *)
rs =
  Sort@DeleteDuplicates@Chop@Join[{0., 4., 8.}, Range[8., 20., 0.2], {20., 23.5, 27}]
(* the timesteps *)
δτ = Table[rs[[i]] - rs[[i - 1]], {i, 2, Length@rs}];
PrependTo[δτ, 0];
(*sanity check*)
And @@ Table[rs[[i]] == Total[δτ[[#]] & /@ Range[i]], {i, Length@rs}]
(*τ=t J/ħ*)
```

```
Out[52]=
{0, 4., 8., 8.2, 8.4, 8.6, 8.8, 9., 9.2, 9.4, 9.6, 9.8, 10., 10.2, 10.4,
 10.6, 10.8, 11., 11.2, 11.4, 11.6, 11.8, 12., 12.2, 12.4, 12.6, 12.8,
 13., 13.2, 13.4, 13.6, 13.8, 14., 14.2, 14.4, 14.6, 14.8, 15., 15.2, 15.4,
 15.6, 15.8, 16., 16.2, 16.4, 16.6, 16.8, 17., 17.2, 17.4, 17.6, 17.8,
 18., 18.2, 18.4, 18.6, 18.8, 19., 19.2, 19.4, 19.6, 19.8, 20., 23.5, 27}
```

```
Out[55]=
True
```

```
In[56]:= (*τ=t J/ħ*)
```

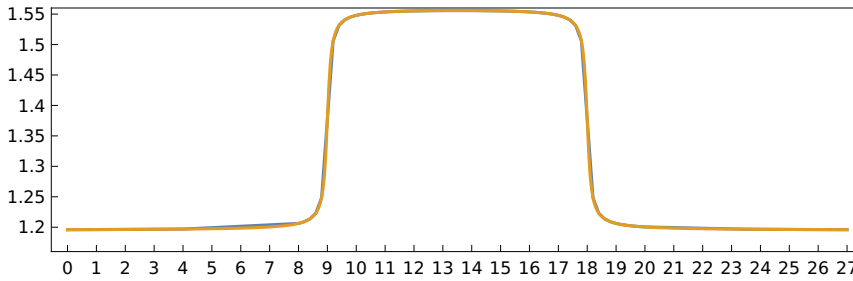
```
In[57]:= (* dense quench for reference *)
gdense << "supplement/BCSonNVCenterDelft/gdense.mx";
```

```

In[58]:= (* See the quench almost overlap with the discretised one *)
gvals = Simplify[(coupling[#,  $\hbar/\Delta\theta$ , g0, gc]/ $\Delta\theta$  & /@ rs) /. constants, J > 0];
ListPlot[Transpose@{rs, gvals}, gdense,
  PlotRange → {1.16, 1.56}, Joined → True, AspectRatio → 0.3, Frame → True,
  FrameTicks → {{Range[1, 1.55, 0.05], None}, {Range[0, 27, 1], None}}]

```

Out[59]=



## Simulations on various noise scenarios

```

In[60]:= summarycss2 << "supplement/BCSonNVCenterDelft/summarycss2.mx";

```

```

In[61]:= CustomGatesDefinitions =

```

$$\begin{aligned}
 &\{SW_{index\_index\_}[\theta] \Rightarrow U_{index\_index\_}[\{ \{1, 0, 0, 0\}, \{0, e^{\frac{i\theta}{2}} \cos[\frac{\theta}{2}], -i e^{\frac{i\theta}{2}} \sin[\frac{\theta}{2}], 0\}, \\
 &\quad \{0, -i e^{\frac{i\theta}{2}} \sin[\frac{\theta}{2}], e^{\frac{i\theta}{2}} \cos[\frac{\theta}{2}], 0\}, \{0, 0, 0, 1\} \} \\
 &\quad , \\
 &\quad CR_{e,n}[\theta] \Rightarrow \\
 &\quad \text{Subscript}[U, e, n][\{ \{ \cos[\theta/2], 0, -i \sin[\theta/2], 0 \}, \{0, \cos[\theta/2], 0, i \sin[\theta/2]\}, \\
 &\quad \quad \{-i \sin[\theta/2], 0, \cos[\theta/2], 0\}, \{0, i \sin[\theta/2], 0, \cos[\theta/2]\} \} ] \\
 &\quad , \\
 &\quad CR_{e,n}[\theta] \Rightarrow \text{Subscript}[U, e, n][\{ \{ \cos[\theta/2], 0, -\sin[\theta/2], 0 \}, \{0, \cos[\theta/2], 0, \sin[\theta/2]\}, \\
 &\quad \quad \{\sin[\theta/2], 0, \cos[\theta/2], 0\}, \{0, -\sin[\theta/2], 0, \cos[\theta/2]\} \} ] \\
 &\quad \};
 \end{aligned}$$

```

CustomGatesDraw = {SWindex1_index2[_] => SWAPindex1_index2};

```

```

In[63]:= noisycirc[ $\rho$ _,  $\rho$ init_,  $\psi$ init_, vdopt_ : {}] := Module[{ $\tau$ , rexnactnoisy, noisycirc, fid},
   $\tau$  = 0;
  CloneQureg[ $\rho$ ,  $\rho$ init];
  rexnactnoisy = {{0, 1}};
  Table[
    noisycirc = ExtractCircuit @
      InsertCircuitNoise[List /@ sum["circnvc"], NVCenterDelft[Sequence @@ vdopt]];
    noisycirc = DeleteCases[DeleteCases[noisycirc, __[0.]], __[0]];
    ApplyCircuit[ $\rho$ , noisycirc /. CustomGatesDefinitions];
    fid = CalcFidelity[ $\rho$ ,  $\psi$ init];
     $\tau$  += sum[" $\delta$ "];
    AppendTo[rexnactnoisy, { $\tau$ , fid}];
    (*<|" $\tau$ "→ $\tau$ , " $\delta$ "→sum[" $\delta$ "], "fidnoisy"→fid, "enoisy"→Abs[sum["fidexact"]-fid]|>*)
    , {sum, summarycss2}];
  rexnactnoisy
]

```

## A realistic setting of virtual NV-center device -- inspired from the paper

```
In[64]:= Options[NVCenterDelft] = {
  QubitNum → 5
  ,
  T1 → <| 0 → 3600, 1 → 60, 2 → 60, 3 → 60, 4 → 60 |>
  ,
  T2 → <| 0 → 1.5, 1 → 10, 2 → 10, 3 → 10, 4 → 9 |>
  ,
  FreqWeakZZ → 5
  ,
  FreqSingleXY → <| 0 →  $15 \times 10^6$ , 1 → 500, 2 → 500, 3 → 500, 4 → 500 |>
  ,
  FreqSingleZ → <| 0 →  $32 \times 10^6$ , 1 →  $400 \times 10^3$ , 2 →  $400 \times 10^3$ , 3 →  $400 \times 10^3$ , 4 →  $400 \times 10^3$  |>
  ,
  FreqCRot → <| 1 →  $1.5 \times 10^3$ , 2 →  $2.8 \times 10^3$ , 3 →  $0.8 \times 10^3$ , 4 →  $2 \times 10^3$  |>
  ,
  FidCRot → <| 1 → 0.98, 2 → 0.98, 3 → 0.98, 4 → 0.98 |>
  ,
  FidSingleXY → <| 0 → 0.9995, 1 → 0.995, 2 → 0.995, 3 → 0.99, 4 → 0.99 |>
  ,
  FidSingleZ → <| 0 → 1, 1 → 1, 2 → 1, 3 → 1, 4 → 1 |>
  ,
  EFSingleXY → {0.75, 0.25}
  ,
  EFCRot → {0.9, 0.1}
  ,
  FidInit → 0.999
  ,
  DurInit →  $2 \times 10^{-3}$ 
  ,
  FidMeas → 0.946
  ,
  DurMeas →  $2 \times 10^{-5}$ 
};
```

**Several tested error scenarios -- these can be flexibly changed/added :**

1) Exact unitary using **MatrixExp[]**

- 2) Checking using the resulting CSS compilation
- 3) Realistic numbers from Mohammed
- 4) Perfect gates with realistic decoherence
- 5) Extremely high gates fidelity 99.999, realistic decoherence
- 6) 10x longer decoherence with excellent gates 99.999

```
In[65]:= labels = <|
  1 → "Exact propagator",
  2 → "Subspace compilation",
  3 → "Realistic noise",
  4 → "Gates fidelity 99.999, no cross-talk",
  5 → "Gates fidelity 99.999",
  6 → "10x of T1,T2",
  7 → "Gates fidelity 99.999, 10x of T1,T2",
  8 → "Gates fidelity 99.999, 10x of T1,T2, no cross-talk"
|>;

In[66]:= (*
Prepare initialisation state in  $\psi_{\text{init}}$  as an exact groundstate from  $H_{\text{BCS}}$ 
*)
DestroyAllQuregs[];
 $\psi_{\text{init}}$  = CreateQureg[5];
hbcs0 = HBCS[5,  $\epsilon$ , 0];
{eigval, eigvec} = Eigensystem[CalcPauliStringMatrix@hbcs0];
Ordering[eigval, 1];
initv = eigvec[[First@Ordering[eigval, 1]]];
initmat = (List/@ initv).Conjugate[{initv}];
{ $\rho$ ,  $\rho_{\text{init}}$ } = CreateDensityQuregs[5, 2];
SetQuregMatrix[ $\rho_{\text{init}}$ , initmat];
SetQuregMatrix[ $\psi_{\text{init}}$ , initv];

In[76]:= (*
Load other data for result comparison:
  exact propagator,
  approximation by compilation in the
  subspace and converted to the native NVC gates
*)
rexactot2 << "supplement/BCSonNVCenterDelft/rexactot2.mx";
rexactcompcss << "supplement/BCSonNVCenterDelft/rexactcompcss.mx";
```

The main execution on scaling the noise.  
Highly configurable

```

In[78]:= (*
Here are some options used
  optgates: set all qubits fidelity to 99.999
  optdec: set all decoherence T1 and T2 to 10x longer
*)
optgates = {FidCRot → Association[{# → .99999} & /@ Range[4]],
  FidSingleXY → Association[{# → .99999} & /@ Range[0, 4]]};
optdec = {T1 → <|0 → 36 000, 1 → 600, 2 → 600, 3 → 600, 4 → 600|>,
  T2 → <|0 → 15, 1 → 100, 2 → 100, 3 → 100, 4 → 90|>};

(*
The main execution:
  notice that we can just change the options. Feel free to change/add here
*)
bcsfidelities = <|
  1 → reexactot2,
  2 → reexactcompss,
  3 → noisyBCS[ρ, ρinit, ψinit],
  4 → noisyBCS[ρ, ρinit, ψinit, Join[optgates, {FreqWeakZZ → False}]],
  5 → noisyBCS[ρ, ρinit, ψinit, optgates],
  6 → noisyBCS[ρ, ρinit, ψinit, optdec],
  7 → noisyBCS[ρ, ρinit, ψinit, Join[optgates, optdec]],
  8 → noisyBCS[ρ, ρinit, ψinit, Join[optgates, optdec, {FreqWeakZZ → False}]]
|>;

In[81]:= plotstyles = {PlotRange → All,
  PlotTheme → "Scientific",
  AspectRatio → .6,
  Background → White,
  ImageSize → 600,
  Frame → True,
  FrameStyle → Directive[Thick, Black, 17],
  BaseStyle → {16},
  GridLines → {rs, None},
  GridLinesStyle → Directive[GrayLevel[0.8, 0.8], Thin]
};

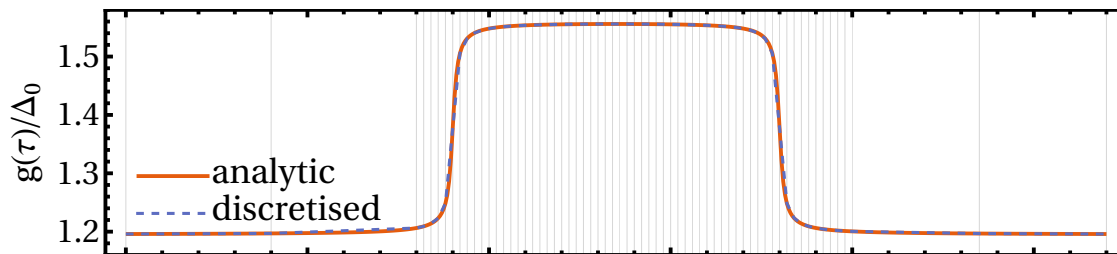
```

```

In[82]:= (*
Beautiful plot for the quench potential
*)
keys = {"analytic", "discretised"};
bcs1 = ListPlot[
  {gdense, Transpose@{rs, gvals}},
  PlotRange → {1.16, 1.58},
  Joined → {True, True},
  AspectRatio → 0.24,
  PlotStyle → {Thick, Dashed},
  PlotLegends → Placed[LineLegend[keys, Spacings → 0], {.15, .25}],
  FrameLabel → {"g(τ)/Δ₀", None}, {None, None}},
  ImagePadding → {{58, 10}, {0, 0}},
  Sequence @@ plotstyles]

```

Out[83]=



The compilation outputs for a reference

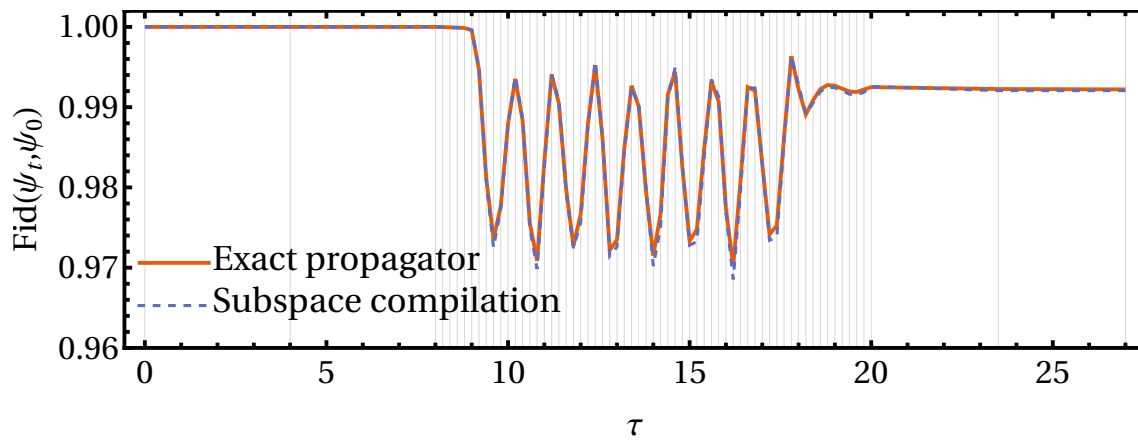


```

In[84]:= keys = {1, 2};
bcs2 = ListPlot[
  bcsfidelities /@ keys,
  Joined → ConstantArray[True, Length@keys],
  PlotStyle → Join[{Thick}, ConstantArray[Dashed, Length@keys - 1]],
  PlotLegends → Placed[LineLegend[labels /@ keys, Spacings → 0], {.22, .2}],
  PlotRange → {Automatic, {0.96, 1.002}},
  AspectRatio → .33,
  ImagePadding → {{58, 10}, {50, 0}},
  FrameLabel → {" $\tau$ ", "Fid( $\psi_t, \psi_0$ )"},
  Sequence @@ plotstyles
]

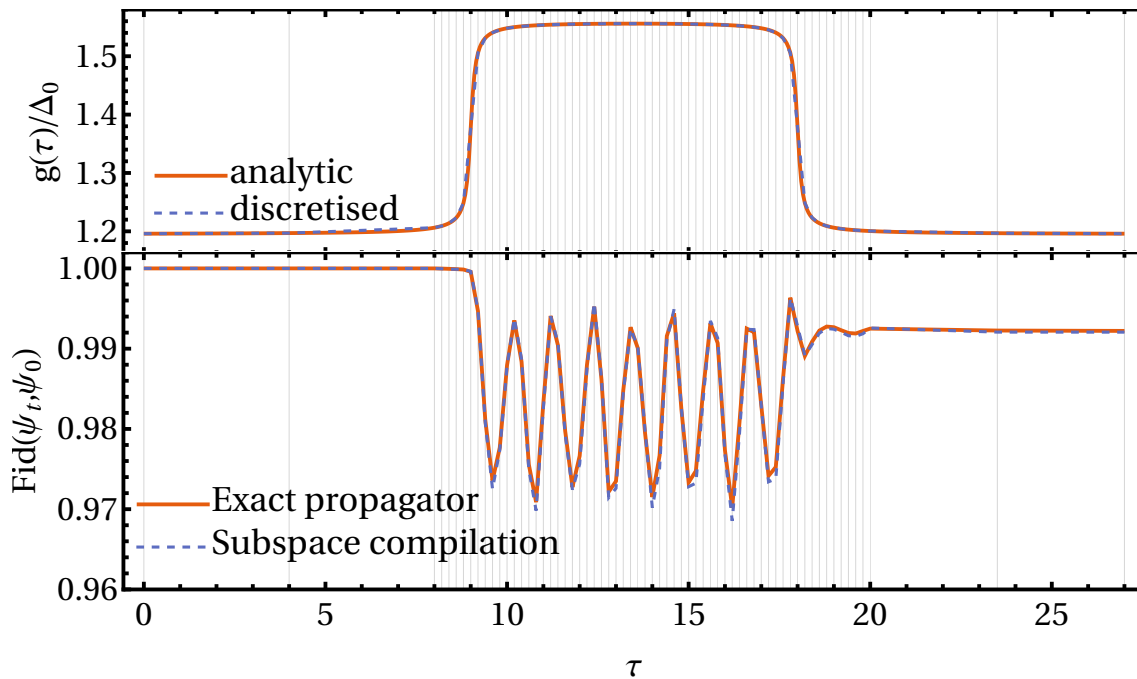
```

Out[85]=



```
In[86]:= Column[{bcs1, bcs2}, Spacings → -0.1]
(*Export["quench.pdf", %]*)
```

```
Out[86]=
```



```
In[87]:= (*
The final plot after various trials
*)
keys = {1, 2, 8, 7, 4, 5, 6, 3};
bcs3 = ListPlot[
  bcsfidelities /@ keys,
  Joined → ConstantArray[True, Length@bcsfidelities],
  PlotStyle → {Thick, Dashed, Thick, Thick, Thick, Thick, Dashed, Thick},
  AspectRatio → 0.8,
  PlotLegends → Placed[LineLegend[labels /@ keys, Spacings → 0, LegendFunction →
    (Framed[#, FrameStyle → (Antialiasing → False), FrameMargins → 0] &)],
    {0.4, 0.2}],
  ImagePadding → {{58, 10}, {50, 0}},
  FrameLabel → {"τ", "Fid(ψ₀, ψₜ)"},
  PlotRange → {{0, 27}, {0.0, 1.03}},
  BaseStyle → {14},
  Sequence @@ plotstyles
]
(*Export["bcsall.pdf", %]*)
```

