# Silicon qubits Delft

This device is based on reference: https://arxiv.org/abs/2202.09252

## **VQD** setup

Set the main directory as the current directory

In[300]:=

SetDirectory[NotebookDirectory[]];

Load the QuESTLink package

One may also use the off-line questlink.m file, change it to the location of the local file

In[301]:=

In[302]:=

Import["https://qtechtheory.org/questlink.m"]

This will download a binary file **quest\_link** if there is no such file found Otherwise, use a locally-compiled that called **quest\_link\*** 

```
(* Search for existing files that match the pattern "quest_link*" *)
With[{questLinkFiles = Sort@FileNames["quest_link*", {NotebookDirectory[]}]}
,
    If[Length[questLinkFiles] > 0,
        (* If one or more matching files are found,
        use the first one alphabetically *)
    Print["Using the existing link file: ", First@questLinkFiles];
    CreateLocalQuESTEnv[First@questLinkFiles];
,
    (*If no matching files are found, download the link file*)
    Print["No link file found, download quest_link"];
    CreateDownloadedQuESTEnv[];
];
```

Load the **VQD** package; must be loaded after QuESTlink is loaded

```
In[303]:=
        Get["../vqd.wl"]
```

# Set the default configuration of the virtual Silicon device

```
frequency unit: MHz
time unit: µs
```

```
In[304]:=
         Options[SiliconDelft] =
              QubitNum → 6
              (* average of T1 *)
              T1 \rightarrow 10^4
              (* In practice, T2 is obtained by echo RX[\pi/2]-\tau-RX[\pi]-\tau-RX[\pi/2],
             where \tau=1\mus. We assume the T2* is echoed out to T2 *)
             T2 \rightarrow \langle | 0 \rightarrow 14, 1 \rightarrow 21.1, 2 \rightarrow 40.1, 3 \rightarrow 37.2, 4 \rightarrow 44.7, 5 \rightarrow 26.7 \rangle
              (* Qubit frequency of each qubit *)
              QubitFreq \rightarrow < | 0 \rightarrow 15.62 \times 10^3, 1 \rightarrow 15.88 \times 10^3,
                 2 \rightarrow 16.3 \times 10^{3}, 3 \rightarrow 16.1 \times 10^{3}, 4 \rightarrow 15.9 \times 10^{3}, 5 \rightarrow 15.69 \times 10^{3}|>
              (* Rabi frequency of single rotations on each qubit *)
              RabiFreq \rightarrow \langle |0 \rightarrow 5, 1 \rightarrow 5, 2 \rightarrow 5, 3 \rightarrow 5, 4 \rightarrow 5, 5 \rightarrow 5| \rangle
              (* Set the noise form of off-resonant Rabi
                 oscillation. This takes RabiFreq information to produce the noise.*)
             OffResonantRabi → True
              (* Set the standard depolarising
               and dephasing passive noise using T1 and T2 *)
             StdPassiveNoise → True
              (* Fidelities of X- and Y- rotations by random benchmarking *)
              FidSingleXY \rightarrow \langle | 0 \rightarrow 0.9977,
                 1 \rightarrow 0.9987, 2 \rightarrow 0.9996, 3 \rightarrow 0.9988, 4 \rightarrow 0.9991, 5 \rightarrow 0.9989 \rangle
              (* Error fraction/ratio {depolarising, dephasing} sum is either one or zero *)
              EFSingleXY \rightarrow {0, 1}
```

```
(* The rabi Frequency and fidelities of controlled-Z(C[Z]),
nearest-neighbors. Keys are the smallest qubit
  number. This applies to controlled-Ph gates *)
FreqCZ \rightarrow \langle |0 \rightarrow 12.1, 1 \rightarrow 11.1, 2 \rightarrow 6.6, 3 \rightarrow 9.8, 4 \rightarrow 5.4 \rangle
(* Fidelity of controlled-Z; the numbers shown here are
 obtained from a simple optimisation via bell state fidelity *)
FidCZ \rightarrow \langle | 0 \rightarrow 0.9374945614729504^{\circ}, 1 \rightarrow 0.9339691831083574^{\circ},
   2 \rightarrow 0.9286379436705322, 3 \rightarrow 0.9967228426036524, 4 \rightarrow 0.9793017377403548)
(* Fidelity of CROT/Controlled-X rotation *)
FidCRot → 0.9988
(* Rabi frequency of CROT, obtained by conditional microwave drive *)
FreqCRot → 5
(* Error fraction/ratio {depolarising, dephasing} of controled-
 Ph(\pi) or controlled-Z. The error for other \theta is scalled from \pi. *)
EFCZ \rightarrow \{0, 1\}
(* Crosstalks error (C-Rz[ex])on the passive qubits when applying CZ gates;
square matrix with dims nqubit-2 *)
ExchangeRotOn \rightarrow {{0, 0.023, 0.018, 0.03, 0.04},
  \{0.05, 0, 0.03, 0.03, 0.04\}, \{0.05, 0.03, 0, 0.07, 0.042\},
  \{0.038, 0.03, 0.031, 0, 0.25\}, \{0.033, 0.03, 0.02, 0.03, 0\}
(* Crosstalks error (C-Rz[ex])on the passive qubits when no CZ gates applied;
the qubits below indicate the controlled-qubit *)
ExchangeRotOff \rightarrow \langle | 0 \rightarrow 0.039, 1 \rightarrow 0.015, 2 \rightarrow 0.03, 3 \rightarrow 0.02, 4 \rightarrow 0.028 | \rangle
(* Parity readout fidelity/charge readout fidelity between Q0,Q1 or Q5,Q6 *)
FidRead → 0.9997
(*Parity readout duration *)
DurRead → 10
```

#### **Device connectivity**

```
In[305]:=
       With[{nq = OptionValue[SiliconDelft, QubitNum]},
        nodes =
         Labeled[\#, Placed[\#, "Q" \iff ToString[\# + 1]}, {Below, Center}]] & /@ Range[0, nq - 1];
        Graph[nodes, Table[j \rightarrow j+1, {j, nodes[All, 1][[;; -2]]}],
         VertexSize → 0.6, VertexStyle → Directive[White, EdgeForm[Thick]],
         BaseStyle → {11, FontFamily → "Serif"}, ImageSize → Automatic,
         EdgeStyle → Directive[Black, Thick, Dashed]]
      1
Out[ • ]=
```

Native gates:  $Rx_j[\theta]$ ,  $Ry_j[\theta]$ ,  $C_i[X_j]$ ,  $C_i[Ph_j[\theta]]$ , Read, Init,  $Wait_i[\Delta t]$ 

### Native gates

```
Initialisation must be done from edge qubits, for example:
Init_{a1,a2}, Init_{q1,q2,q3}, Init_{q5,q6}, Init_{q4,q5,q6}
Parity readout only on edge qubits, for example
MeasP<sub>q1,q2</sub>, MeasP<sub>q5,q6</sub>
Single-qubit gates
Rx_q[\theta], Ry_q[\theta], Rz_q[\theta]
Two-qubit gates
C_p[Z_q], C_p[Ph_q],
others: doing nothing
Wait<sub>q</sub>[duration]
```

# **Basic operations**

### Doing nothing, observe the passive noise

The passive noise when no gates are applied.

The noise forms:

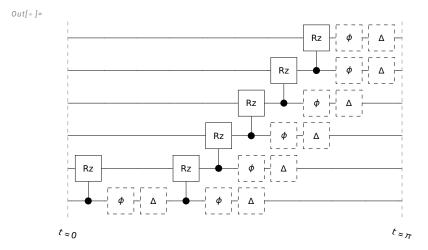
- 1) Cross-talk  $C_i[Rz_{i+1}(\Delta t)]$  from input ExchangeRotOff, which is exchange rotation when no C[Z] gate is applied.
- 2) Standard dephasing from T2 input and depolarising from T1 inputs. We assume the T2\* is echoed out to T2

The standard passivenoise (2) can be eliminated by setting **StdPassiveNoise** → **False**. The Cross-talk (1) can be set off by setting **ExchangeRotOff** → **False** 

In[306]:=

#### InsertCircuitNoise[{Wait [π]}, SiliconDelft[]] DrawCircuit[%]

```
Out[ . ]=
        {{0, {C [Rz, [0.039]], Deph [0.100502], Depol [0.000235582]}},
           {C [Rz,[0.]], Deph [0.], Depol [0.], C, [Rz,[0.015]], Deph, [0.0691683], Depol, [0.000235582],
             C<sup>-</sup>[Rz<sup>-</sup>[0.03]], Deph<sup>-</sup>[0.0376768], Depol<sup>-</sup>[0.000235582], C<sup>-</sup>[Rz<sup>-</sup>[0.02]],
             Deph-[0.0404918], Depol-[0.000235582], C-[Rz-[0.028]], Deph-[0.0339344],
             Depol [0.000235582], Deph [0.055502], Depol [0.000235582]}, \{\pi, \{\}, \{\}\}\}
```



### Single qubit gates

Single qubit gates: x- and y- rotations have the same error

The noise forms:

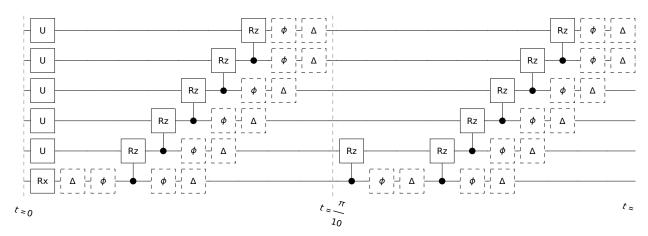
- 1) Off-resonant Rabi Oscillation. This takes RabiFreq input and applied when **OffResonantRabi**→ True.
- 2) Standard Dephasing and Depolarising noise. This takes FidSingleXY and EFSingleXY inputs to estimate the error parameters. Set **EFSingleXY**→{**0,0**} to set this off.

In[308]:=

 $InsertCircuitNoise \Big[ CircSiliconDelft \Big[ \{Rx_0[\pi/2], Wait_0[1]\}, Parallel \rightarrow False \Big], \\ SiliconDelft \Big[ StdPassiveNoise \rightarrow True, OffResonantRabi \rightarrow True \Big] \\ DrawCircuit [\%]$ 

```
Out[ • ]=
                   \left\{\left\{0, \left\{Rx_{0}\left[\frac{\pi}{2}\right], Depol_{0}[0.], Deph_{0}[0.001725],\right.\right\}\right\}
                               U_1\Big[\Big\{\big\{0.999287 - 0.0377401\,i,\, -1.35127 \times 10^{-17} - 0.000725771\,i\Big\},
                                      \left\{-1.35127 \times 10^{-17} - 0.000725771 i, 0.999287 + 0.0377401 i\right\}\right\}
                               U_{2}[\{\{0.999896-0.0144364\,i,\,-1.45569\times10^{-18}-0.00010615\,i\},
                                      \left\{-1.45569\times10^{-18}-0.00010615\,i,\,0.999896+0.0144364\,i\right\}\right],
                               U_{3}\Big[\Big\{\Big\{0.999791-0.02045\,i,\ 3.05645\times10^{-16}-0.000213021\,i\Big\},
                                      \left\{3.05645\times10^{-16}-0.000213021\,i,\;0.999791+0.02045\,i\right\}\right],
                               U_{4}\Big[\Big\{\Big\{0.999385-0.0350469\,i\,,\,-9.81184\times10^{-18}-0.000625837\,i\Big\},
                                      \left\{-9.81184\times10^{-18}-0.000625837\,i\,,\,0.999385+0.0350469\,i\right\}\right\}\right],
                               U_{5}\Big[\Big\{\Big\{0.98769-0.139614\,i,\ 0.0705493-2.76517\times10^{-16}\,i\Big\},
                                      \left\{0.0705493 - 2.76517 \times 10^{-16} \, i, \, -0.98769 - 0.139614 \, i\right\}\right\}\right\},
                            \{C_0[Rz_1[0.]], Deph_0[0.], Depol_0[0.], C_1[Rz_2[0.0015]], Deph_1[0.00738939], C_1[Rz_2[0.0015]], C_1[Rz_2[0.0015]
                                Depol_1[0.0000235616], C_2[Rz_3[0.003]], Deph_2[0.00390189],
                                Depol<sub>2</sub>[0.0000235616], C<sub>3</sub>[Rz<sub>4</sub>[0.002]], Deph<sub>3</sub>[0.00420479],
                                Depol<sub>3</sub>[0.0000235616], C_4[Rz_5[0.0028]], Deph<sub>4</sub>[0.00350177],
                                Depol_{4}[0.0000235616], Deph_{5}[0.00584866], Depol_{5}[0.0000235616]]
                        \left\{\frac{\pi}{10}, \{C_0[Rz_1[0.0124141]], Deph_0[0.0344686], Depol_0[0.0000749963]\},\right\}
                            \{C_0[Rz_1[0.]], Deph_0[0.], Depol_0[0.], C_1[Rz_2[0.00477465]], Deph_1[0.0231439],
                                Depol<sub>1</sub>[0.0000749963], C<sub>2</sub>[Rz<sub>3</sub>[0.0095493]], Deph<sub>2</sub>[0.0123146],
                                Depol<sub>2</sub>[0.0000749963], C<sub>3</sub>[Rz<sub>4</sub>[0.0063662]], Deph<sub>3</sub>[0.0132618],
                                Depol_3[0.0000749963], C_4[Rz_5[0.00891268]], Deph_4[0.0110615],
                                Depol<sub>4</sub>[0.0000749963], Deph<sub>5</sub>[0.0183802], Depol<sub>5</sub>[0.0000749963]}, \left\{1 + \frac{\pi}{10}, \left\{\right\}, \left\{\right\}\right\}
```





### Controlled - Z, Coltrolled-Phase

#### The noisy forms:

- 1) Standard 2-qubits dephasing and depolarising noise. This takes information FidCZ (fidelities) and **EFCZ** (error fraction). Set it off by **EFCZ**→{0,0}
- 2) Exchange rotation when a two-qubit gate is on. Takes information ExchangeRotOn. Set **ExchangeRotOn** → **False** to turn it off.

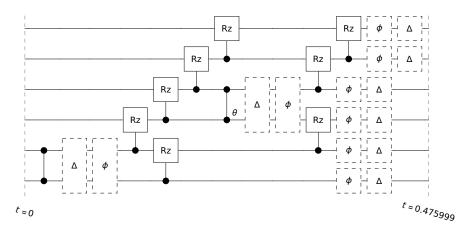
In[310]:=

InsertCircuitNoise[ $\{C_0[Z_1], C_2[Ph_3[\pi]]\},$ SiliconDelft[StdPassiveNoise → True, EFCZ → {0, 0}]] DrawCircuit[%]

Out[ • ]=

 $\{[0, \{C_0[Z_1], Depol_{0,1}[0], Deph_{0,1}[0], C_1[Rz_2[0.023]], C_2[Rz_3[0.018]], C_3[Rz_4[0.03]], C_4[Rz_5[0.04]], C_4[Rz_5[0.04]], C_4[Rz_5[0.04]], C_4[Rz_5[0.04]], C_4[Rz_5[0.04]], C_4[Rz_5[0.04]], C_4[Rz_5[0.04]], C_4[Rz_5[0.04]], C_4[Rz_5[0.04]], C_5[Rz_4[0.04]], C_5[Rz$  $C_2[Ph_3[\pi]], Depol_{2.3}[0], Deph_{2.3}[0], C_0[Rz_1[0.05]], C_1[Rz_2[0.03]], C_3[Rz_4[0.07]], C_4[Rz_5[0.042]]$  $\{Deph_0[0.00766785], Depol_0[0.0000162271], Deph_1[0.00510089], Depol_1[0.0000162271], \}$ Deph<sub>2</sub>[0.], Depol<sub>2</sub>[0.], Deph<sub>3</sub>[0.], Depol<sub>3</sub>[0.], Deph<sub>4</sub>[0.00529612],  $Depol_{4}[0.0000356991], Deph_{5}[0.00883485], Depol_{5}[0.0000356991]\}, {0.475999, {}, {}}$ 

Out[ • ]=



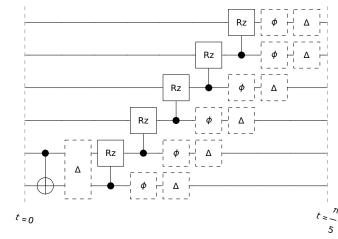
In[312]:=

 $InsertCircuitNoise[\{CRot_{1,0}\}, SiliconDelft[], ReplaceAliases \rightarrow False] \\ DrawCircuit[\%]$ 

Out[•]=

$$\begin{split} \Big\{ &\{0, \{C_1[X_0], \, \mathsf{Depol}_{1,0}[0.0012]\}, \, \{C_0[\mathsf{Rz}_1[0.]], \, \mathsf{Deph}_0[0.], \, \mathsf{Depol}_0[0.], \, C_1[\mathsf{Rz}_2[0.]], \, \mathsf{Deph}_1[0.], \\ & \, \mathsf{Depol}_1[0.], \, C_2[\mathsf{Rz}_3[0.006]], \, \mathsf{Deph}_2[0.00777334], \, \mathsf{Depol}_2[0.0000471224], \, C_3[\mathsf{Rz}_4[0.004]], \\ & \, \mathsf{Deph}_3[0.00837422], \, \mathsf{Depol}_3[0.0000471224], \, C_4[\mathsf{Rz}_5[0.0056]], \, \mathsf{Deph}_4[0.00697901], \\ & \, \mathsf{Depol}_4[0.0000471224], \, \mathsf{Deph}_5[0.0116289], \, \mathsf{Depol}_5[0.0000471224]\} \big\}, \, \Big\{ \frac{\pi}{5}, \, \{\}, \, \{\} \Big\} \Big\} \end{split}$$

Out[•]=



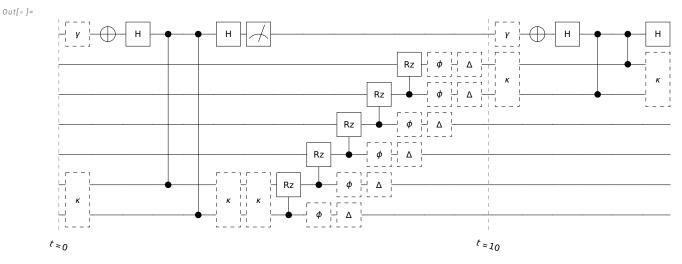
### Readout: parity measurement

**Note:** see *supplement/BellsonSiliconDelft/SiDelftReadInit.nb* for further details on this measurement model

In[314]:=

 $InsertCircuitNoise[List/@\{MeasP_{1,0},\,MeasP_{4,5}\},\,SiliconDelft[],\,ReplaceAliases \rightarrow True];\\$ 

In[315]:= DrawCircuit@%



# Reproducing results from the paper

Initialisation is obtained by 2 readouts and a partial swap with single qubit errors The gubits are initialised to state 100 ... 001

# Realtime feedback initialisation to $|10\rangle$ and $|100\rangle$

```
In[316]:=
        \rho = CreateDensityQureg[7];
```

The initialisation process done in the experiment paper

```
In[317]:=
       SetAttributes[readInit, HoldFirst]
       readInit[ρ_, q0_, q1_, opt_:{}] := Module[{m1, m2},
          m1 = First@Flatten@ApplyCircuit[ρ, ExtractCircuit@InsertCircuitNoise[
                  {MeasP<sub>q0,q1</sub>}, SiliconDelft[Sequence @@ opt], ReplaceAliases \rightarrow True];
          If[m1 == 1, ApplyCircuit[ρ, ExtractCircuit@InsertCircuitNoise[
               \{Rx_{q0}[\pi]\}, SiliconDelft[Sequence @@ opt], ReplaceAliases \rightarrow True]]];
          \verb|m2 = First@Flatten@ApplyCircuit|| \rho, ExtractCircuit@InsertCircuitNoise||
                  {MeasP<sub>q0,q1</sub>}, SiliconDelft[Sequence@@opt], ReplaceAliases \rightarrow True];
          {m1, m2}
```

Initialise the qubits to mixed state for a proper test

Readout (QND) on middle qubits Q2,Q3 and initialising it at the same time to state | 100)

Only works if the output the last measurement is 0; repeat the initialisation process otherwise

```
In[322]:=
       readInit3[ρ_, q0_, q1_, q2_, opt_:{}] := Module[{m1, m2, m3},
          m1 = First@Flatten@ApplyCircuit[ρ, ExtractCircuit@InsertCircuitNoise]
                  {MeasP<sub>q0,q1</sub>}, SiliconDelft[Sequence @@ opt], ReplaceAliases \rightarrow True]];
          If [m1 == 1, ApplyCircuit[\rho, ExtractCircuit@InsertCircuitNoise[
               \{Rx_{q0}[\pi]\}, SiliconDelft[Sequence@@opt], ReplaceAliases \rightarrow True]]];
          m2 = First@Flatten@ApplyCircuit[ρ, ExtractCircuit@InsertCircuitNoise[
                  {MeasP<sub>q0,q1</sub>}, SiliconDelft[Sequence @@ opt], ReplaceAliases \rightarrow True]];
          m3 = First@Flatten@ApplyCircuit[ρ, ExtractCircuit@InsertCircuitNoise]
                  {CRot<sub>q2,q1</sub>, MeasP<sub>q0,q1</sub>}, SiliconDelft[Sequence@@opt], ReplaceAliases → True]];
          If[m3 == 1, ApplyCircuit[ρ, ExtractCircuit@InsertCircuitNoise[
               \{Rx_{q2}[\pi]\}, SiliconDelft[Sequence@@opt], ReplaceAliases \rightarrow True]]];
          {m1, m2, m3}
In[323]:=
       (* initialise the qubits to mixed state *)
       SetQuregMatrix[ρ, RandomMixState[7]];
In[324]:=
       (* Keep doing it until the fidelity is high: Readout repetition in practice *)
In[325]:=
       readInit3[\rho, 0, 1, 2]
       Re@PartialTrace[\rho, 3, 4, 5, 6][[2, 2]]
Out[ • ]=
       \{0, 0, 0\}
Out[ • ]=
       0.998154
```

```
In[327]:=
       readInit3[\rho, 5, 4, 3]
       Re@PartialTrace[\rho, 0, 1, 2, 6][[5, 5]]
Out[ • ]=
       \{1, 0, 1\}
Out[ • ]=
       0.000137176
    Full device initialisation to |100001\rangle
In[329]:=
       \psi5 = CreateQureg[7];
       ApplyCircuit[InitZeroState@\psi5, {X<sub>0</sub>, X<sub>5</sub>}];
       (* initialise the qubits to mixed state *)
       SetQuregMatrix[ρ, RandomMixState[7]];
       (* repeat the measurement process: ideally all outputs are zeros *)
       repeat = 4;
       opt = {};
       Table[readInit3[\rho, 5, 4, 3, opt], {repeat}]
       Table[readInit3[\rho, 0, 1, 2, opt], {repeat}]
       CalcFidelity[\rho, \psi5]
Out[ • ]=
       \{\{1, 0, 1\}, \{1, 0, 0\}, \{0, 0, 0\}, \{0, 0, 0\}\}
Out[0]=
       \{\{1, 0, 1\}, \{1, 0, 0\}, \{0, 0, 1\}, \{1, 0, 1\}\}
Out[ • ]=
       0.
    Obtaining T1: X180-τ- with perfect measurement
In[337]:=
       RelaxationExperiment[dev_, qubit_, initrep_: 3] := Module[{init},
          Table
           (* initialise the qubits to mixed state *)
           SetQuregMatrix[\rho, RandomMixState[7]];
           Table[readInit3[\rho, 5, 4, 3], {initrep}];
           Table[readInit3[\rho, 0, 1, 2], {initrep}];
           ApplyCircuit[ρ, ExtractCircuit@InsertCircuitNoise[
                If[MemberQ[\{0, 5\}, qubit], \{Wait_{0}[t]\}, List/@\{Rx_{qubit}[\pi], Wait_{0}[t]\}, dev]];
```

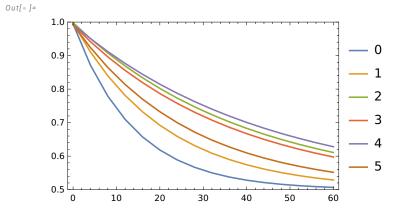
{t, CalcProbOfOutcome[ $\rho$ , qubit, 1]}, {t, 0,  $10^4$ , 1000}

Out[ • ]=

```
In[338]:=
       ListPlot[RelaxationExperiment[SiliconDelft[], #] & /@ Range[0, 5],
        PlotLegends → Range[0, 5], Joined → True,
        ImageSize → 300, AxesLabel → {"τ", "p(0)"}, Frame → True]
Out[ • ]=
       1.00
                                                         — 0
       0.95
                                                          - 1
       0.90
       0.85
                                                          - 2
       0.80
                                                          – 3
       0.75
                                                          - 4
       0.70
                                                          - 5
       0.65
                  2000
                          4000
                                  6000
                                          8000
                                                  10000
    Obtaining T_2: X90 - tau - X180 - tau - X90, tau = 1 \mus
 In[95]:= HahnEchoExperiment[dev_, qubit_, initrep_: 3] := Module[{},
         Table
           (* initialise the qubits to mixed state *)
           SetQuregMatrix[ρ, RandomMixState[7]];
           Table[readInit3[\rho, 5, 4, 3], {initrep}];
           Table[readInit3[\rho, 0, 1, 2], {initrep}];
           ApplyCircuit[\rho, ExtractCircuit@InsertCircuitNoise[
               List/@ \{Rx_{qubit}[\pi/2], Wait_{\theta}[t/2], Rx_{qubit}[\pi], Wait_{\theta}[t/2], Rx_{qubit}[\pi/2]\}, dev]];
           {t, CalcProbOfOutcome[\rho, qubit, If[MemberQ[{5, 0}, qubit], 1, 0]]}, {t, 0, 60, 4}]
 In[96]:= OptionValue[SiliconDelft, T2]
```

 $\langle | 0 \rightarrow 14, 1 \rightarrow 21.1, 2 \rightarrow 40.1, 3 \rightarrow 37.2, 4 \rightarrow 44.7, 5 \rightarrow 26.7 | \rangle$ 

```
In[97]:= ListPlot[HahnEchoExperiment[SiliconDelft[], #] & /@ Range[0, 5],
         PlotLegends \rightarrow Range[0, 5], PlotRange \rightarrow {0.5, 1}, Joined \rightarrow True,
         ImageSize \rightarrow 300, AxesLabel \rightarrow {"\tau", "p(|+))"}, Frame \rightarrow True]
```



# Paper supplement: Bell states

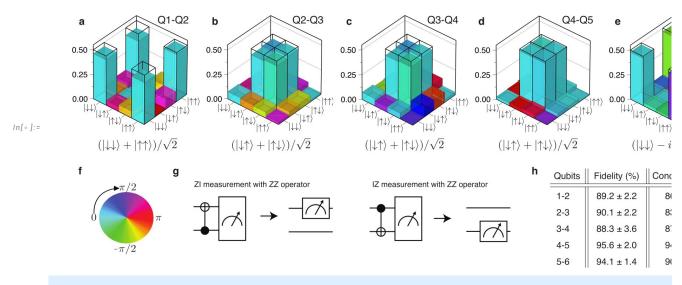
```
ln[98]:= chartstyle[label_] := {ImageSize \rightarrow 200, BarSpacing \rightarrow 0.1\,\),
         ColorFunction → Function [{height}, If [height < 0.1, ColorData["Rainbow"] [10 height],
             ColorData["DeepSeaColors"][(height - 0.9) * 10]], ChartElementFunction \rightarrow "Cube",
         ChartStyle → EdgeForm[Thick], PlotTheme → "Business", Ticks →
           {{{1, "00"}, {2, "01"}, {3, "10"}, {4, "11"}}, {{1, "00"}, {2, "01"}, {3, "10"}, {4, "11"}},
            Automatic}, LabelStyle → Directive[Bold, Black],
          Epilog → Inset[Style[label, Thick, 17], ImageScaled[{.2, .7}]], PlotRange → All
        };
```

The CZ gates' fidelities are unknown. We set it according to the results on the Bell states fidelity.

```
In[99]:= \psi 2 = CreateQureg[2];
       ρ2 = CreateDensityQureg[2];
In[101]:=
       concurence[\rho] := Module[{eigv, \rhom, \rhoms, \rhot, nq, pauliy},
          \rho m = GetQuregMatrix@\rho;
          nq = IntegerPart@Log2@Length@pm;
          \rhoms = MatrixPower[\rhom, 1/2];
          pauliy = CalcCircuitMatrix[Y<sub>#</sub> & /@ Range[0, nq - 1]];
          ρt = pauliy.Conjugate[ρm].pauliy;
          eigv = Reverse@Sort[Chop@Eigenvalues[MatrixPower[ρms.ρt.ρms, 1/2]]];
          Max[0, eigv[1] - Total@eigv[2;;]]
        1
```

```
In[102]:=
         bellcirc\rho = \langle |
               "01" \rightarrow \{Rx_0[\pi/2], Rx_1[-\pi/2], C_0[Z_1], Rx_1[\pi/2]\},
              "12" \rightarrow {Rx<sub>1</sub>[\pi/2], Rx<sub>2</sub>[\pi/2], C<sub>1</sub>[Z<sub>2</sub>], Rx<sub>2</sub>[\pi/2]},
              "23" \rightarrow \{Rx_2[\pi/2], Rx_3[\pi/2], C_2[Z_3], Rx_3[\pi/2]\},
               "34" \rightarrow {Rx<sub>3</sub>[\pi/2], Rx<sub>4</sub>[\pi/2], C<sub>3</sub>[Z<sub>4</sub>], Rx<sub>4</sub>[\pi/2]},
               "45" \rightarrow {Rx<sub>4</sub>[\pi/2], Rx<sub>5</sub>[\pi/2], C<sub>4</sub>[Z<sub>5</sub>], Rx<sub>5</sub>[\pi/2]}|>;
          bellcirc\psi = \langle |
               "01" \rightarrow \{X_0, Rx_0[\pi/2], Rx_1[-\pi/2], C_0[Z_1], Rx_1[\pi/2]\},
              "12" \rightarrow {Rx<sub>0</sub>[\pi/2], Rx<sub>1</sub>[\pi/2], C<sub>0</sub>[Z<sub>1</sub>], Rx<sub>1</sub>[\pi/2]},
               "23" \rightarrow \{Rx_0[\pi/2], Rx_1[\pi/2], C_0[Z_1], Rx_1[\pi/2]\},
               "34" \rightarrow \{Rx_0[\pi/2], Rx_1[\pi/2], C_0[Z_1], Rx_1[\pi/2]\},
               "45" \rightarrow \{X_1, Rx_0[\pi/2], Rx_1[\pi/2], C_0[Z_1], Rx_1[\pi/2]\} > ;
In[104]:=
          bell[code_, opt_, initrep_: 4]:= Module[{qubits, fid, plot, conc, str, out1, out2},
             qubits = ToExpression@StringSplit[code, ""];
             SetQuregMatrix[\rho, IdentityMatrix[2^7]];
             out1 = Table[readInit3[\rho, 5, 4, 3, opt], {initrep}];
             out2 = Table[readInit3[\rho, 0, 1, 2, opt], {initrep}];
             ApplyCircuit[ρ, ExtractCircuit@
                InsertCircuitNoise[Serialize@{bellcircp[code]}, SiliconDelft[Sequence@@opt]]];
             SetQuregMatrix[p2, PartialTrace[p, Sequence @@ Complement[Range[0, 5], qubits], 6]];
             conc = concurence[\rho2] * 100;
             ApplyCircuit[InitZeroState@\psi2, bellcirc\psi[code]];
             fid = CalcFidelity[\rho2, \psi2] * 100;
             str = "Q" <> ToString[1 + qubits[1]] <> "-Q" <> ToString[1 + qubits[2]];
             plot = PlotDensityMatrix[\rho2, \psi2, Sequence @@ chartstyle[str]];
             {str, plot, fid, conc}
```

Reference from the experiment



The simulation

In[105]:=

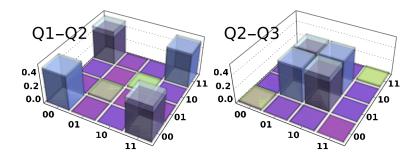
plots = Transpose[bell[#, {}, 4] &/@  $\label{eq:ReplaceList} $$\operatorname{ReplaceList[Sort@Range[0, 5], \{p_{,} a_, b_, q_{,} s_, b_, s_$ TableForm[Transpose@{DecimalForm[#, 4] & /@ plots[3]], DecimalForm[#, 4] & /@ plots[4]]}, TableHeadings → {plots[1], {"Fidelity", "Concurence"}}]

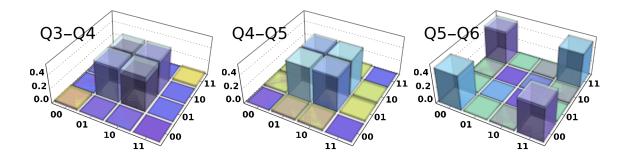
#### Row@plots[2]

Out[•]//TableForm=

	Fidelity	Concurence
Q1-Q2	89.4	79.75
Q2-Q3	90.18	80.42
Q3-Q4	88.69	79.05
Q4-Q5	95.95	94.46
Q5-Q6	94.18	90.43

Out[ • ]=





In[108]:=

$$\begin{split} & \texttt{Export} \Big[ \texttt{plots} \big[ 1, \ \textbf{i} \big] \iff \texttt{".pdf"}, \ \texttt{plots} \big[ 2, \ \textbf{i} \big] \big], \\ & \Big\{ \textbf{i}, \ \texttt{Length@plots} \big[ \texttt{1} \big] \Big\} \Big] \star ) \end{split}$$

```
In[109]:=
      (* average obtained fidelity *)
       Round[#, 0.01] &/@plots[3]
      Mean@%
Out[•]=
      {89.4, 90.18, 88.69, 95.95, 94.18}
Out[•]=
      91.68
```