Partial Fraction

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Consider this integral:

$$\int \frac{x+1}{x^2 - 5x + 6} \mathrm{d}x$$

This integral looks scary, but notice that we can factor the denominator: $x^2 - 5x + 6 = (x - 2)(x - 3)$

Let's first take at look at fraction addition:

$$\frac{A}{B} + \frac{C}{D} = \frac{AD + BC}{BD}$$

Since the integrand is a fraction, and we successfully write the denominator as a product, we should be able to split the fraction into a sum of two fraction.

Assume we have split the fraction like this:

$$\frac{x+1}{(x-2)(x-3)} = \frac{A}{(x-2)} + \frac{B}{(x-3)}$$

Here and A and B are different