

# Package ‘IsoplotR’

August 22, 2016

**Title** Statistical Toolbox for Radiometric Geochronology

**Version** 0.8

**Description** An R implementation of Ken Ludwig's popular Isoplot add-in to Microsoft Excel. Currently plots U-Pb data on Wetherill and Tera-Wasserburg concordia diagrams. Calculates concordia and discordia ages. Performs linear regression of measurements with correlated errors using the 'York' approach. Generates Kernel Density Estimates (KDEs) and Cumulative Age Distributions (CADs). Produces Multidimensional Scaling (MDS) configurations and Shepard plots of multi-sample detrital datasets using the Kolmogorov-Smirnov distance as a dissimilarity measure. Calculates  $40\text{A}/39\text{Ar}$  ages, isochrons, and age spectra. Computes weighted means accounting for overdispersion. Calculates U-Th-He (single grain and central) ages, logratio plots and ternary diagrams. Future versions will include functionality for the Rb-Sr, Sm-Nd, Re-Os, fission track and cosmogenic nuclide methods, radial plots and banana diagrams. A graphical user interface is provided as an RStudio Shiny app at <http://isoplotr.london-geochron.com>. Offline access to this interface will be provided at a later point in time.

**Author** Pieter Vermeesch [aut, cre]

**Maintainer** Pieter Vermeesch <p.vermeesch@ucl.ac.uk>

**Depends** R (>= 3.0.0)

**Imports** MASS

**Suggests**

**License** GPL-2

**LazyData** true

**RoxygenNote** 5.0.1

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age	<i>Calculate isotopic ages</i>
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## Description

Calculates U-Pb ages and propagates their analytical uncertainties. Evaluates the equivalence of multiple ( $^{206}\text{Pb}/^{238}\text{U}$ - $^{207}\text{Pb}/^{235}\text{U}$  or  $^{207}\text{Pb}/^{206}\text{Pb}$ - $^{206}\text{Pb}/^{238}\text{U}$ ) compositions, computes the weighted mean isotopic composition and the corresponding concordia age using the method of maximum likelihood, computes the mswd of equivalence and concordance and their respective Chi-squared p-values. Performs linear regression of U-Pb data on Wetherill and Tera-Wasserburg concordia diagrams. Computes the upper and lower intercept ages (for Wetherill) or the lower intercept age and the  $^{207}\text{Pb}/^{206}\text{Pb}$  intercept (for Tera-Wasserburg), taking into account error correlations and decay constant uncertainties.

## Usage

```
age(x, ...)
```

## Default S3 method:

```
age(x, method = "Pb206U238", exterr = TRUE, J = c(NA,
  NA), ...)
```

## S3 method for class 'UPb'

```
age(x, concordia = 1, wetherill = TRUE, exterr = TRUE,
  i = NA, sigdig = 2, ...)
```

## S3 method for class 'detritals'

```
age(x, ...)
```

## S3 method for class 'ArAr'

```
age(x, isochron = FALSE, exterr = TRUE, i = NA,
  sigdig = 2, ...)
```

```
## S3 method for class 'UThHe'
age(x, central = FALSE, i = NA, sigdig = 2, ...)

## S3 method for class 'fissiontracks'
age(x, central = FALSE, i = NA, sigdig = 2,
    exterr = TRUE, ...)
```

## Arguments

x	can be: a scalar containing an isotopic ratio, a two element vector containing an isotopic ratio and its standard error, a four element vector containing Ar40Ar39, s[Ar40Ar39], J, s[J], an six element vector containing U, s[U], Th, s[Th], He and s[He] an eight element vector containing U, s[U], Th, s[Th], He, s[He], Sm and s[Sm], OR an object of class UPb, ArAr or UThHe.
...	optional arguments
method	one of either 'Pb206U238', 'Pb207U235', 'Pb207Pb206', 'Ar40Ar39' or U-Th-He
exterr	propagate the external (decay constant and calibration factor) uncertainties?
J	two element vector with the J-factor and its standard error. This option is only used if method = 'Ar40Ar39'.
concordia	scalar flag indicating whether each U-Pb analysis should be considered separately (concordia=1), a concordia age should be calculated from all U-Pb analyses together (concordia=2), or a discordia line should be fit through all the U-Pb analyses (concordia=2).
wetherill	boolean flag to indicate whether the data should be evaluated in Wetherill (TRUE) or Tera-Wasserburg (FALSE) space. This option is only used when concordia=2
i	(optional) index of a particular aliquot
sigdig	number of significant digits for the uncertainty estimate (only used if concordia=1, isochron=FALSE or central=FALSE).
isochron	Boolean flag indicating whether each Ar-Ar analysis should be considered separately (isochron=FALSE) or an isochron age should be calculated from all Ar-Ar analyses together (isochron=TRUE).
central	Boolean flag indicating whether each U-Th-He analysis should be considered separately (central=FALSE) or a central age should be calculated from all U-Th-He analyses together (central=TRUE).

## Value

if x is a scalar or a vector, returns the age using the geochronometer given by method and its standard error.

if x has class UPb and concordia=1, returns a table with the following columns: 't.75', 'err[t.75]', 't.68', 'err[t.68]', 't.76', 'err[t.76]', 't.conc', 'err[t.conc]', containing the  $^{207}\text{Pb}/^{235}\text{U}$ -age and standard error, the  $^{206}\text{Pb}/^{238}\text{U}$ -age and standard error, the  $^{207}\text{Pb}/^{206}\text{Pb}$ -age and standard error, and the concordia age and standard error, respectively.

if `x` has class `UPb` and `concordia=2`, returns a list with the following items:

**x** a named vector with the (weighted mean) U-Pb composition

**cov** the covariance matrix of the (mean) U-Pb composition

**age** the concordia age (in Ma)

**age.err** the standard error of the concordia age

**mswd** a list with two items (equivalence and concordance) containing the MSWD (Mean of the Squared Weighted Deviates, a.k.a the reduced Chi-squared statistic outside of geochronology) of isotopic equivalence and age concordance, respectively.

**p.value** a list with two items (equivalence and concordance) containing the p-value of the Chi-square test for isotopic equivalence and age concordance, respectively.

if `x` has class `UPb` and `concordia=3`, returns a list with the following items:

**x** a two element vector with the upper and lower intercept ages (if `wetherill==TRUE`) or the lower intercept age and  $^{207}\text{Pb}/^{206}\text{Pb}$  intercept (for Tera-Wasserburg)

**cov** the covariance matrix of the elements in `x`

if `x` has class `ArAr` and `isochron=FALSE`, returns a table of Ar-Ar ages and standard errors.

if `x` has class `ArAr` and `isochron=TRUE`, returns a list with the following items:

**a** the intercept of the straight line fit and its standard error.

**b** the slope of the fit and its standard error.

**y0** the atmospheric  $^{40}\text{Ar}/^{36}\text{Ar}$  ratio and its standard error.

**age** the  $^{40}\text{Ar}/^{39}\text{Ar}$  age and its standard error.

if `x` has class `UThHe` and `central=FALSE`, returns a table of U-Th-He ages and standard errors.

if `x` has class `UThHe` and `central=TRUE`, returns a list with the following items:

**uvw** a three-element list with the weighted mean  $\log[\text{U}/\text{He}]$ ,  $\log[\text{Th}/\text{He}]$  and  $\log[\text{Sm}/\text{He}]$  compositions.

**covmat** a 3x3 covariance matrix for `uvw`

**mswd** the reduced Chi-square value for the  $\log[\text{U}/\text{He}]-\log[\text{Th}/\text{He}]$  compositions.

**p.value** the p-value of concordance between the  $\log[\text{U}/\text{He}]-\log[\text{Th}/\text{He}]$  compositions.

**age** two-element vector with the central age and its standard error.

## Examples

```
data(examples)
print(age(examples$UPb))
print(age(examples$UPb, concordia=1))
print(age(examples$UPb, concordia=2))
```

agespectrum

*Plot a ( $^{40}\text{Ar}/^{39}\text{Ar}$ ) release spectrum***Description**

Produces a plot of boxes whose widths correspond to the cumulative amount of  $^{39}\text{Ar}$  (or any other volume proxy), and whose heights express the analytical uncertainties. Only propagates the analytical uncertainty associated with decay constants and J-factors after computing the plateau composition.

**Usage**

```
agespectrum(x, ...)
```

```
## Default S3 method:
```

```
agespectrum(x, alpha = 0.05, plateau = TRUE,
  plateau.col = rgb(0, 1, 0, 0.5), non.plateau.col = rgb(0, 1, 1, 0.5),
  sigdig = 2, line.col = "red", lwd = 2, title = TRUE, ...)
```

```
## S3 method for class 'ArAr'
```

```
agespectrum(x, alpha = 0.05, plateau = TRUE,
  plateau.col = rgb(0, 1, 0, 0.5), non.plateau.col = rgb(0, 1, 1, 0.5),
  sigdig = 2, exterr = TRUE, line.col = "red", lwd = 2, ...)
```

**Arguments**

x	a three column matrix whose first column gives the amount of $^{39}\text{Ar}$ in each aliquot, and whose second and third columns give the age and its uncertainty. OR an object of class ArAr with format=2
...	optional parameters to the generic plot function
alpha	the confidence limits of the error bars/boxes.
plateau	Boolean flag indicating whether a plateau age should be calculated if plateau=TRUE, the function will compute the weighted mean of the largest succession of steps that yield values passing the Chi-square test for age homogeneity.
plateau.col	the fill colour of the rectangles used to mark the steps belonging to the age plateau.
non.plateau.col	if plateau=TRUE, the steps that do NOT belong to the plateau are given a different colour.
sigdig	the number of significant digits of the numerical values reported in the title of the graphical output (only used if plateau=FALSE).
line.col	colour of the isochron line
lwd	line width
title	add a title to the plot? If FALSE, returns a list with plateau parameters.
exterr	propagate the external (decay constant and calibration factor) uncertainties?

**Value**

if title=FALSE, a list with the following items:

- mean a 2-element vector with the plateau mean and standard error
- mswd the mean square of the weighted deviates of the plateau
- p.value the p-value of a Chi-square test with n-1 degrees of freedom, where n is the number of steps in the plateau.n
- fract the fraction of  $^{39}\text{Ar}$  contained in the plateau

**Examples**

```
data(examples)
agespectrum(examples$ArAr,ylim=c(0,80))
```

---

botev

---

*Compute the optimal kernel bandwidth*


---

**Description**

Uses the diffusion algorithm of Zdravko Botev (2011) to calculate the bandwidth for kernel density estimation

**Usage**

```
botev(x)
```

**Arguments**

x                      a vector of ordinal data

**Value**

a scalar value with the optimal bandwidth

**Author(s)**

Dzdravko Botev

**References**

Botev, Z. I., J. F. Grotowski, and D. P. Kroese. "Kernel density estimation via diffusion." The Annals of Statistics 38.5 (2010): 2916-2957.

**Examples**

```
data(examples)
samp <- examples$DZ[['N1']]
bw <- botev(samp)
print(bw)
```

cad

*Plot continuous data as cumulative age distributions***Description**

Plot a dataset as a Cumulative Age Distribution (CAD), also known as a ‘empirical cumulative distribution function’.

**Usage**

```
cad(x, ...)
```

## Default S3 method:

```
cad(x, pch = NA, verticals = TRUE, xlab = "age [Ma]",
    colmap = "heat.colors", col = "black", ...)
```

## S3 method for class 'detritals'

```
cad(x, pch = NA, verticals = TRUE, xlab = "age [Ma]",
    colmap = "heat.colors", ...)
```

## S3 method for class 'UPb'

```
cad(x, pch = NA, verticals = TRUE, xlab = "age [Ma]",
    col = "black", type = 4, cutoff.76 = 1100, cutoff.disc = c(-15, 5),
    ...)
```

## S3 method for class 'ArAr'

```
cad(x, pch = NA, verticals = TRUE, xlab = "age [Ma]",
    col = "black", ...)
```

## S3 method for class 'UThHe'

```
cad(x, pch = NA, verticals = TRUE, xlab = "age [Ma]",
    col = "black", ...)
```

## S3 method for class 'fissiontracks'

```
cad(x, pch = NA, verticals = TRUE,
    xlab = "age [Ma]", col = "black", ...)
```

**Arguments**

x	a numerical vector OR an object of class UPb or detritals
...	optional arguments to the generic plot function
pch	plot character to mark the beginning of each CAD step
verticals	boolean flag indicating if the horizontal lines of the CAD should be connected by vertical lines
xlab	x-axis label

<code>colmap</code>	an optional string with the name of one of R's built-in colour palettes (e.g., <code>heat.colors</code> , <code>terrain.colors</code> , <code>topo.colors</code> , <code>cm.colors</code> ), which are to be used for plotting data of class <code>detritals</code> .
<code>col</code>	colour to give to single sample datasets (i.e. not of class <code>detritals</code> )
<code>type</code>	scalar indicating whether to plot the $^{207}\text{Pb}/^{235}\text{U}$ age ( <code>type=1</code> ), the $^{206}\text{Pb}/^{238}\text{U}$ age ( <code>type=2</code> ), the $^{207}\text{Pb}/^{206}\text{Pb}$ age ( <code>type=3</code> ), the $^{207}\text{Pb}/^{206}\text{Pb}$ - $^{206}\text{Pb}/^{238}\text{U}$ age ( <code>type=4</code> ), or the (Wetherill) concordia age ( <code>type=5</code> )
<code>cutoff.76</code>	the age (in Ma) below which the $^{206}\text{Pb}/^{238}\text{U}$ and above which the $^{207}\text{Pb}/^{206}\text{Pb}$ age is used. This parameter is only used if <code>type=4</code> .
<code>cutoff.disc</code>	two element vector with the maximum and minimum percentage discordance allowed between the $^{207}\text{Pb}/^{235}\text{U}$ and $^{206}\text{Pb}/^{238}\text{U}$ age (if $^{206}\text{Pb}/^{238}\text{U} < \text{cutoff.76}$ ) or between the $^{206}\text{Pb}/^{238}\text{U}$ and $^{207}\text{Pb}/^{206}\text{Pb}$ age (if $^{206}\text{Pb}/^{238}\text{U} > \text{cutoff.76}$ ). Set <code>cutoff.disc=NA</code> if you do not want to use this filter.

## Examples

```
data(examples)
cad(examples$DZ, verticals=FALSE, pch=20)
```

---

central	<i>Calculate U-Th-He (and fission track) central ages and compositions</i>
---------	--

---

## Description

Computes the geometric mean composition of a set of fission track or U-Th-He data and returns the corresponding age and fitting parameters.

## Usage

```
central(x, ...)

## Default S3 method:
central(x, ...)

## S3 method for class 'UThHe'
central(x, ...)
```

## Arguments

<code>x</code>	an object of class <code>UThHe</code> or <code>fissiontracks</code>
<code>...</code>	optional arguments



**Value**

if `x` has class `UThHe`, returns a list containing the following items:

`uvw` (if the input data table contains `Sm`) or `uv` (if it doesn't): the geometric mean  $\log[U/He]$ ,  $\log[Th/He]$  (,  $\log[Sm/He]$ ) and  $\log[Sm/He]$  composition

`covmat`: the covariance matrix of `uvw` or `uv`

`mswd`: the reduced Chi-square statistic of data concordance, i.e.  $mswd = SS/(2n-2)$  where  $SS$  is the sum of squares of the  $\log[U/He]$ - $\log[Th/He]$  compositions and  $n$  is the number of samples.

`p.value`: the p-value of a Chi-square test with  $n-2$  degrees of freedom

`age`: a two-column vector with the central age and its standard error.

**Examples**

```
data(examples)
print(central(examples$UThHe)$age)
```

---

concordia

*Concordia diagram*


---

**Description**

Plot U-Pb data on Wetherill and Tera-Wasserburg concordia diagrams, calculate concordia ages and compositions, evaluates the equivalence of multiple ( $^{206}Pb/^{238}U$ - $^{207}Pb/^{235}U$  or  $^{207}Pb/^{206}Pb$ - $^{206}Pb/^{238}U$ ) compositions, computes the weighted mean isotopic composition and the corresponding concordia age using the method of maximum likelihood, computes the  $mswd$  of equivalence and concordance and their respective Chi-squared p-values. Performs linear regression and computes the upper and lower intercept ages (for Wetherill) or the lower intercept age and the  $^{207}Pb/^{206}Pb$  intercept (for Tera-Wasserburg), taking into account error correlations and decay constant uncertainties.

**Usage**

```
concordia(x, limits = NULL, alpha = 0.05, wetherill = TRUE,
  show.numbers = FALSE, ellipse.col = rgb(0, 1, 0, 0.5),
  concordia.col = "darksalmon", exterr = TRUE, show.age = 1, sigdig = 2)
```

**Arguments**

<code>x</code>	an object of class <code>UPb</code>
<code>limits</code>	age limits of the concordia line
<code>alpha</code>	confidence cutoff for the error ellipses
<code>wetherill</code>	boolean flag (FALSE for Tera-Wasserburg)
<code>show.numbers</code>	boolean flag (TRUE to show grain numbers)
<code>ellipse.col</code>	background colour of the error ellipses

concordia.col	colour of the concordia line
exterr	show decay constant uncertainty?
show.age	one of either 1: don't show the age 2: calculate the concordia age 3: fit a discordia line
sigdig	number of significant digits for the concordia/discordia age

### Examples

```
data(examples)
concordia(examples$UPb)
```

---

ellipse	<i>Get coordinates of error ellipse for plotting</i>
---------	--

---

### Description

Construct an error ellipse age a given confidence level from its centre and covariance matrix

### Usage

```
ellipse(x, y, covmat, alpha = 0.05)
```

### Arguments

x	x-coordinate (scalar) for the centre of the ellipse
y	y-coordinate (scalar) for the centre of the ellipse
covmat	covariance matrix of the x-y coordinates
alpha	the probability cutoff for the error ellipses

### Value

a [50x2] matrix of plot coordinates

### Examples

```
x = 99; y = 101;
covmat <- matrix(c(1,0.9,0.9,1),nrow=2)
ell <- ellipse(x,y,covmat)
plot(c(90,110),c(90,110),type='l')
polygon(ell,col=rgb(0,1,0,0.5))
points(x,y,pch=21,bg='black')
```

examples

*Example datasets for testing IsoplotR***Description**

U-Pb and detrital zircon datasets

**Details**

examples is a list with two items

UPb: an object of class 'UPb' containing a high precision U-Pb dataset packaged with Ken Ludwig's Isoplot program.

DZ: an object of class 'detrital' containing a detrital zircon U-Pb dataset from Namibia.

ArAr: an object of class 'ArAr' containing a  $^{40}\text{Ar}/^{39}\text{Ar}$  spectrum of Skye basalt produced by Sarah Sherlock (Open University).

UThHe: an object of class 'UThHe' containing a U-Th-Sm-He dataset of Fish Lake apatite produced by Daniel Stockli (UT Austin).

average: an object of class 'other' containing the  $^{206}\text{Pb}/^{238}\text{U}$ -ages and errors of dataset UPb.

KDE: an object of class 'other' containing the  $^{206}\text{Pb}/^{238}\text{U}$ -ages (but not the errors) of dataset UPb.

spectrum: an object of class 'other' containing the  $^{39}\text{Ar}$  abundances,  $^{40}\text{Ar}/^{39}\text{Ar}$ -ages and errors of dataset ArAr.

**Author(s)**

Ken Ludwig and Pieter Vermeesch

**References**

Ludwig, K. R. User's manual for Isoplot 3.00: a geochronological toolkit for Microsoft Excel. No. 4. Kenneth R. Ludwig, 2003.

Vermeesch, Pieter, and Eduardo Garzanti. "Making geological sense of 'Big Data' in sedimentary provenance analysis." *Chemical Geology* 409 (2015): 20-27.

Vermeesch, Pieter. "Three new ways to calculate average (U-Th)/He ages." *Chemical Geology* 249.3 (2008): 339-347.

**Examples**

```
data(examples)
concordia(examples$UPb)
dev.new()
kde(examples$DZ)
```

helioplot

*Visualise U-Th-He data on a logratio plot or ternary diagram***Description**

Plot U-Th(-Sm)-He data on a ( $\log[\text{He/Th}]$  vs.  $\log[\text{U/He}]$ ) logratio plot or U-Th-He ternary diagram

**Usage**

```
helioplot(x, logratio = TRUE, show.central.comp = TRUE,
  show.numbers = FALSE, alpha = 0.05, contour.col = c("white", "red"),
  ellipse.col = rgb(0, 1, 0, 0.5), sigdig = 2, xlim = NA, ylim = NA,
  fact = NA, ...)
```

**Arguments**

<code>x</code>	an object of class UThHe
<code>logratio</code>	Boolean flag indicating whether the data should be shown on bivariate $\log[\text{He/Th}]$ vs. $\log[\text{U/He}]$ diagramme, or a U-Th-He ternary diagramme.
<code>show.central.comp</code>	show the geometric mean composition as a white ellipse?
<code>show.numbers</code>	show the grain numbers inside the error ellipses?
<code>alpha</code>	confidence cutoff for the error ellipses
<code>contour.col</code>	two-element vector with the fill colours to be assigned to the minimum and maximum age contour
<code>ellipse.col</code>	background colour of the error ellipses
<code>sigdig</code>	number of significant digits for the central age
<code>xlim</code>	optional limits of the x-axis ( $\log[\text{U/He}]$ ) of the logratio plot. If <code>xlim=NA</code> , the axis limits are determined automatically.
<code>ylim</code>	optional limits of the y-axis ( $\log[\text{Th/He}]$ ) of the logratio plot. If <code>ylim=NA</code> , the axis limits are determined automatically.
<code>fact</code>	three element vector with the scaling factors of the ternary diagram if <code>fact=NA</code> , these will be determined automatically
<code>...</code>	optional arguments to the generic plot function

**Examples**

```
data(examples)
helioplot(examples$UThHe)
dev.new()
helioplot(examples$UThHe, logratio=FALSE)
```

---

iratio	<i>Isotopic ratios</i>
--------	------------------------

---

## Description

Gets or sets natural isotopic ratios.

## Usage

```
iratio(ratio, x = NULL, e = NULL)
```

## Arguments

ratio	one of either 'U238U235', 'Ar40Ar36', 'Ar38Ar36', 'Rb85Rb87', 'Sr88Sr86', 'Sr87Sr86', 'Sr84Sr86', 'Re185Re187', 'Os184Os192', 'Os186Os192', 'Os187Os192', 'Os188Os192', 'Os189Os192'
x	new value for ratio
e	new value for its standard error

## Value

if x=e=NULL, returns a two-item vector containing the mean value of the requested ratio and its standard error, respectively.

## References

- Ar: Lee, Jee-Yon, et al. "A redetermination of the isotopic abundances of atmospheric Ar." *Geochimica et Cosmochimica Acta* 70.17 (2006): 4507-4512.
- Rb: Catanzaro, E. J., et al. "Absolute isotopic abundance ratio and atomic weight of terrestrial rubidium." *J. Res. Natl. Bur. Stand. A* 73 (1969): 511-516.
- Sr: Moore, L. J., et al. "Absolute isotopic abundance ratios and atomic weight of a reference sample of strontium." *J. Res. Natl. Bur. Stand.* 87.1 (1982): 1-8.
- Sm: Chang, Tsing-Lien, et al. "Absolute isotopic composition and atomic weight of samarium." *International Journal of Mass Spectrometry* 218.2 (2002): 167-172.
- Re: Gramlich, John W., et al. "Absolute isotopic abundance ratio and atomic weight of a reference sample of rhenium." *J. Res. Natl. Bur. Stand. A* 77 (1973): 691-698.
- Os: Voelkening, Joachim, Thomas Walczyk, and Klaus G. Heumann. "Osmium isotope ratio determinations by negative thermal ionization mass spectrometry." *Int. J. Mass Spect. Ion Proc.* 105.2 (1991): 147-159.
- U: Hiess, Joe, et al. "<sup>238</sup>U/<sup>235</sup>U systematics in terrestrial uranium-bearing minerals." *Science* 335.6076 (2012): 1610-1614.

## Examples

```
# returns the 238U/235U ratio of Hiess et al. (2012):
print(iratio('U238U235'))
# use the 238U/235U ratio of Steiger and Jaeger (1977):
iratio('U238U235',138.88,0)
print(iratio('U238U235'))
```

---

isochron

*Calculate and plot isochrons*


---

## Description

Plots cogenetic  $^{40}\text{Ar}/^{39}\text{Ar}$  data as X-Y scatterplots, fits an isochron curve through them using the `yorkfit` function, and computes the corresponding isochron age, including decay constant uncertainties.

## Usage

```
isochron(x, ...)

## Default S3 method:
isochron(x, xlim = NA, ylim = NA, alpha = 0.05,
         sigdig = 2, show.numbers = FALSE, ellipse.col = rgb(0, 1, 0, 0.5),
         line.col = "red", lwd = 2, title = TRUE, ...)

## S3 method for class 'ArAr'
isochron(x, xlim = NA, ylim = NA, alpha = 0.05,
         sigdig = sigdig, show.numbers = FALSE, ellipse.col = rgb(0, 1, 0, 0.5),
         inverse = TRUE, line.col = "red", lwd = 2, plot = TRUE, ...)
```

## Arguments

<code>x</code>	EITHER a list or a matrix with the following vectors: <code>X</code> : the x-variable <code>Y</code> : the y-variable <code>sX</code> : the standard error of X <code>sY</code> : the standard error of Y <code>rXY</code> : the correlation coefficient of X and Y OR an object of class <code>ArAr</code>
<code>...</code>	optional arguments
<code>xlim</code>	2-element vector with the plot limits of the x-axis
<code>ylim</code>	2-element vector with the plot limits of the y-axis
<code>alpha</code>	confidence cutoff for the error ellipses
<code>sigdig</code>	the number of significant digits of the numerical values reported in the title of the graphical output

show.numbers	boolean flag (TRUE to show grain numbers)
ellipse.col	background colour of the error ellipses
line.col	colour of the isochron line
lwd	line width
title	add a title to the plot?
inverse	if TRUE, plots $^{36}\text{Ar}/^{40}\text{Ar}$ vs. $^{39}\text{Ar}/^{40}\text{Ar}$ . If FALSE, plots $^{40}\text{Ar}/^{36}\text{Ar}$ vs. $^{39}\text{Ar}/^{36}\text{Ar}$ .
plot	if FALSE, suppresses the graphical output

### Value

if plot=FALSE, returns a list with the following items:

a: the intercept of the straight line fit and its standard error

b: the slope of the fit and its standard error

y0: the atmospheric  $^{40}\text{Ar}/^{36}\text{Ar}$  ratio and its standard error

age: the  $^{40}\text{Ar}/^{39}\text{Ar}$  age and its standard error

### Examples

```
data(examples)
isochron(examples$ArAr)
```

---

kde	<i>Create (a) kernel density estimate(s)</i>
-----	--

---

### Description

Creates one or more kernel density estimates using a combination of the Botev (2010) bandwidth selector and the Abramson (1982) adaptive kernel bandwidth modifier.

### Usage

```
kde(x, ...)
```

## Default S3 method:

```
kde(x, from = NA, to = NA, bw = NA, adaptive = TRUE,
    log = FALSE, n = 512, plot = TRUE, pch = NA, xlab = "age [Ma]",
    ylab = "", kde.col = rgb(1, 0, 1, 0.6), hist.col = rgb(0, 1, 0, 0.2),
    show.hist = TRUE, bty = "n", binwidth = NA, ncol = NA, ...)
```

## S3 method for class 'UPb'

```
kde(x, from = NA, to = NA, bw = NA, adaptive = TRUE,
    log = FALSE, n = 512, plot = TRUE, pch = NA, xlab = "age [Ma]",
    ylab = "", kde.col = rgb(1, 0, 1, 0.6), hist.col = rgb(0, 1, 0, 0.2),
    show.hist = TRUE, bty = "n", binwidth = NA, ncol = NA, type = 4,
```

```

cutoff.76 = 1100, cutoff.disc = c(-15, 5), ...)

## S3 method for class 'detritals'
kde(x, from = NA, to = NA, bw = NA, adaptive = TRUE,
    log = FALSE, n = 512, plot = TRUE, pch = NA, xlab = "age [Ma]",
    ylab = "", kde.col = rgb(1, 0, 1, 0.6), hist.col = rgb(0, 1, 0, 0.2),
    show.hist = TRUE, bty = "n", binwidth = NA, ncol = NA,
    samebandwidth = TRUE, normalise = TRUE, ...)

## S3 method for class 'ArAr'
kde(x, from = NA, to = NA, bw = NA, adaptive = TRUE,
    log = FALSE, n = 512, plot = TRUE, pch = NA, xlab = "age [Ma]",
    ylab = "", kde.col = rgb(1, 0, 1, 0.6), hist.col = rgb(0, 1, 0, 0.2),
    show.hist = TRUE, bty = "n", binwidth = NA, ncol = NA, ...)

## S3 method for class 'UThHe'
kde(x, from = NA, to = NA, bw = NA, adaptive = TRUE,
    log = FALSE, n = 512, plot = TRUE, pch = NA, xlab = "age [Ma]",
    ylab = "", kde.col = rgb(1, 0, 1, 0.6), hist.col = rgb(0, 1, 0, 0.2),
    show.hist = TRUE, bty = "n", binwidth = NA, ncol = NA, ...)

## S3 method for class 'fissiontracks'
kde(x, from = NA, to = NA, bw = NA,
    adaptive = TRUE, log = FALSE, n = 512, plot = TRUE, pch = NA,
    xlab = "age [Ma]", ylab = "", kde.col = rgb(1, 0, 1, 0.6),
    hist.col = rgb(0, 1, 0, 0.2), show.hist = TRUE, bty = "n",
    binwidth = NA, ncol = NA, ...)

```

## Arguments

<code>x</code>	a vector of numbers or an object of class UPb, ArAr or detrital
<code>...</code>	optional arguments to be passed on to density
<code>from</code>	minimum age of the time axis. If NULL, this is set automatically
<code>to</code>	maximum age of the time axis. If NULL, this is set automatically
<code>bw</code>	the bandwidth of the KDE. If NULL, bw will be calculated automatically using <code>botev()</code>
<code>adaptive</code>	boolean flag controlling if the adaptive KDE modifier of Abramson (1982) is used
<code>log</code>	transform the ages to a log scale if TRUE
<code>n</code>	horizontal resolution of the density estimate
<code>plot</code>	show the KDE as a plot
<code>pch</code>	the symbol used to show the samples. May be a vector. Set <code>pch = NA</code> to turn them off.
<code>xlab</code>	the label of the x-axis
<code>ylab</code>	the label of the y-axis



<code>kde.col</code>	the fill colour of the KDE specified as a four element vector of <code>r</code> , <code>g</code> , <code>b</code> , <code>alpha</code> values
<code>hist.col</code>	the fill colour of the histogram specified as a four element vector of <code>r</code> , <code>g</code> , <code>b</code> , <code>alpha</code> values
<code>show.hist</code>	boolean flag indicating whether a histogram should be added to the KDE
<code>bty</code>	change to "o", "l", "7", "c", "u", or "]" if you want to draw a box around the plot
<code>binwidth</code>	scalar width of the histogram bins, in Myr if <code>x\$log==FALSE</code> , or as a fractional value if <code>x\$log==TRUE</code> . Sturges' Rule is used if <code>binwidth==NA</code>
<code>ncol</code>	scalar value indicating the number of columns over which the KDEs should be divided. This option is only used if <code>x</code> is of class <code>detritals</code> .
<code>type</code>	scalar indicating whether to plot the $^{207}\text{Pb}/^{235}\text{U}$ age ( <code>type=1</code> ), the $^{206}\text{Pb}/^{238}\text{U}$ age ( <code>type=2</code> ), the $^{207}\text{Pb}/^{206}\text{Pb}$ age ( <code>type=3</code> ), the $^{207}\text{Pb}/^{206}\text{Pb}$ - $^{206}\text{Pb}/^{238}\text{U}$ age ( <code>type=4</code> ), or the (Wetherill) concordia age ( <code>type=5</code> )
<code>cutoff.76</code>	the age (in Ma) below which the $^{206}\text{Pb}/^{238}\text{U}$ and above which the $^{207}\text{Pb}/^{206}\text{Pb}$ age is used. This parameter is only used if <code>type=4</code> .
<code>cutoff.disc</code>	two element vector with the maximum and minimum percentage discordance allowed between the $^{207}\text{Pb}/^{235}\text{U}$ and $^{206}\text{Pb}/^{238}\text{U}$ age (if $^{206}\text{Pb}/^{238}\text{U} < \text{cutoff.76}$ ) or between the $^{206}\text{Pb}/^{238}\text{U}$ and $^{207}\text{Pb}/^{206}\text{Pb}$ age (if $^{206}\text{Pb}/^{238}\text{U} > \text{cutoff.76}$ ). Set <code>cutoff.disc=NA</code> if you do not want to use this filter.
<code>samebandwidth</code>	boolean flag indicating whether the same bandwidth should be used for all samples. If <code>samebandwidth = TRUE</code> and <code>bw = NULL</code> , then the function will use the median bandwidth of all the samples.
<code>normalise</code>	boolean flag indicating whether or not the KDEs should all integrate to the same value.

## Value

if `plot==TRUE`, returns an object of class `KDE`, i.e. a list containing the following items:

**x** horizontal plot coordinates  
**y** vertical plot coordinates  
**bw** the base bandwidth of the density estimate  
**ages** the data values from the input to the KDE function

or, if `class(x)=='detritals'`, an object of class `KDEs`, i.e. a list containing the following items:

**kdes** a named list with objects of class `KDE`  
**from** the beginning of the common time scale  
**to** the end of the common time scale  
**themax** the maximum probability density of all the KDEs  
**xlabel** the x-axis label to be used by `plot.KDEs`

**Examples**

```
data(examples)
kde(examples$DZ[['N1']],kernel="epanechnikov")
kde(examples$DZ,from=0,to=3000)
```

lambda

*Decay constants***Description**

Gets or sets the decay constants of radioactive isotopes

**Usage**

```
lambda(nuclide, x = NULL, e = NULL)
```

**Arguments**

nuclide	the nuclide name
x	new value for the decay constant
e	new value for the decay constant uncertainty

**Value**

if x==e==NULL, returns a two-item vector containing the decay constant [in Ma<sup>-1</sup>] and its standard error, respectively.

**References**

U: Jaffey, A. H., et al. "Precision measurement of half-lives and specific activities of U235 and U238." *Physical Review C* 4.5 (1971): 1889.

Th: Le Roux, L. J., and L. E. Glendenin. "Half-life of 232Th. "Proceedings of the National Meeting on Nuclear Energy, Pretoria, South Africa. 1963.

Sm: Lugmair, G. W., and K. Marti. "Lunar initial 143Nd/144Nd: differential evolution of the lunar crust and mantle." *Earth and Planetary Science Letters* 39.3 (1978): 349-357.

Ar: Renne, Paul R., et al. "Response to the comment by WH Schwarz et al. on "Joint determination of 40K decay constants and 40Ar\*/40K for the Fish Canyon sanidine standard, and improved accuracy for 40 Ar/39 Ar geochronology" by PR Renne et al.(2010)." *Geochimica et Cosmochimica Acta* 75.17 (2011): 5097-5100.

**Examples**

```
print(lambda('U238'))
# use the decay constant of Kovarik and Adams (1932)
lambda('U238',0.0001537,0.0000068)
print(lambda('U238'))
```

---

mds
*Multidimensional Scaling*

---

**Description**

Performs classical or nonmetric Multidimensional Scaling analysis

**Usage**

```
mds(x, ...)

## Default S3 method:
mds(x, classical = FALSE, plot = TRUE, shepard = FALSE,
     nnlines = FALSE, pch = 21, pos = NULL, cex.symbols = 2.5,
     col = "black", bg = "white", xlab = "", ylab = "", ...)

## S3 method for class 'detritals'
mds(x, classical = FALSE, plot = TRUE,
     shepard = FALSE, nnlines = FALSE, pch = 21, pos = NULL,
     cex.symbols = 2.5, col = "black", bg = "white", xlab = "",
     ylab = "", ...)
```

**Arguments**

x	a dissimilarity matrix OR an object of class detrital
...	optional arguments to the generic plot function
classical	boolean flag indicating whether classical (TRUE) or nonmetric (FALSE) MDS should be used
plot	show the MDS configuration (if shepard=FALSE) or Shepard plot (if shepard=TRUE) on a graphical device
shepard	Boolean flag indicating whether the graphical output should show the MDS configuration (shepard=FALSE) or a Shepard plot with the 'stress' value. This argument is only used if plot=TRUE.
nnlines	if TRUE, draws nearest neighbour lines
pch	plot character (see ?plot for details). May be a vector.
pos	a position specifier for the labels (if pch != NA). Values of 1, 2, 3 and 4 indicate positions below, to the left of, above and to the right of the MDS coordinates, respectively.
cex.symbols	a numerical value giving the amount by which plotting symbols should be magnified relative to the default
col	plot colour (may be a vector)
bg	background colour (may be a vector)
xlab	a string with the label of the x axis
ylab	a string with the label of the y axis

**Value**

if plot=FALSE, returns an object of class MDS, i.e. a list containing the following items:

- points: a two column vector of the fitted configuration
- classical: a boolean flag indicating whether the MDS configuration was obtained by classical (TRUE) or nonmetric (FALSE) MDS.
- diss: the dissimilarity matrix used for the MDS analysis
- stress: (only if classical=TRUE) the final stress achieved (in percent)

**Examples**

```
data(examples)
# Parameters 'xaxt' and 'yaxt' control if the axis is plotted at all.
mds(examples$DZ, nnlines=TRUE, cex=5, xaxt='n', yaxt='n')
dev.new()
mds(examples$DZ, shepard=TRUE)
```

---

radialplot

---

*Visualise heteroscedastic data on a radial plot*


---

**Description**

Implementation of a graphical device developed by Rex Galbraith to display several estimates of the same quantity that have different standard errors.

**Usage**

```
radialplot(x, ...)
```

## Default S3 method:

```
radialplot(x, from = NA, to = NA, t0 = NA,
  transformation = "log", sigdig = 2, show.numbers = FALSE, pch = 21,
  bg = "white", ...)
```

## S3 method for class 'fissiontracks'

```
radialplot(x, from = NA, to = NA, t0 = NA,
  transformation = "arcsin", sigdig = 2, show.numbers = FALSE, pch = 21,
  bg = "white", ...)
```

## S3 method for class 'UPb'

```
radialplot(x, from = NA, to = NA, t0 = NA,
  transformation = "log", type = 4, cutoff.76 = 1100,
  cutoff.disc = c(-15, 5), sigdig = 2, show.numbers = FALSE, pch = 21,
  bg = "white", ...)
```

## S3 method for class 'ArAr'

```
radialplot(x, from = NA, to = NA, t0 = NA,
```

```

transformation = "log", sigdig = 2, show.numbers = FALSE, pch = 21,
bg = "white", ...)

## S3 method for class 'UThHe'
radialplot(x, from = NA, to = NA, t0 = NA,
  transformation = "log", sigdig = 2, show.numbers = FALSE, pch = 21,
  bg = "white", ...)

```

## Arguments

x	Either an nx2 matrix of (transformed) values z and their standard errors s OR and object of class fissiontracks, UThHe, ArAr, or UPb
...	additional arguments to the generic points function
from	minimum age limit of the radial scale
to	maximum age limit of the radial scale
t0	central value
transformation	one of either log, linear or (if x has class fissiontracks)
sigdig	the number of significant digits of the numerical values reported in the title of the graphical output.
show.numbers	boolean flag (TRUE to show grain numbers)
pch	plot character (default is a filled circle)
bg	background colour of the plot character
type	scalar indicating whether to plot the $^{207}\text{Pb}/^{235}\text{U}$ age (type=1), the $^{206}\text{Pb}/^{238}\text{U}$ age (type=2), the $^{207}\text{Pb}/^{206}\text{Pb}$ age (type=3), the $^{207}\text{Pb}/^{206}\text{Pb}$ - $^{206}\text{Pb}/^{238}\text{U}$ age (type=4), or the (Wetherill) concordia age (type=5)
cutoff.76	the age (in Ma) below which the $^{206}\text{Pb}/^{238}\text{U}$ and above which the $^{207}\text{Pb}/^{206}\text{Pb}$ age is used. This parameter is only used if type=4.
cutoff.disc	two element vector with the maximum and minimum percentage discordance allowed between the $^{207}\text{Pb}/^{235}\text{U}$ and $^{206}\text{Pb}/^{238}\text{U}$ age (if $^{206}\text{Pb}/^{238}\text{U} < \text{cutoff.76}$ ) or between the $^{206}\text{Pb}/^{238}\text{U}$ and $^{207}\text{Pb}/^{206}\text{Pb}$ age (if $^{206}\text{Pb}/^{238}\text{U} > \text{cutoff.76}$ ). Set cutoff.disc=NA if you do not want to use this filter.

## Examples

```

data(examples)
radialplot(examples$FT)

```

---

read.data	<i>Read geochronology data</i>
-----------	--------------------------------

---

## Description

Cast a .csv file or a matrix into one of IsoplotR's data classes

## Usage

```
read.data(x, ...)

## Default S3 method:
read.data(x, method = "U-Pb", format = 1, ...)

## S3 method for class 'matrix'
read.data(x, method = "U-Pb", format = 1, ...)
```

## Arguments

x	a file name (.csv format) or matrix
...	optional arguments to the read.csv function
method	one of 'U-Pb', 'Ar-Ar', 'Rb-Sr', 'Sm-Nd', 'Re-Os', 'U-Th-He', 'fission tracks', 'cosmogenic nuclides' or 'other'
format	formatting option, depends on the value of method. If method = 'U-Pb', then format is one of either: 1: 7/6, s[7/6], 6/8, s[6/8], 7/5, s[7/5] If method = 'Ar-Ar', then format is one of either: 1: 39/40, s[39/40], 36/40, s[36/40], 39/36, s[39/36] 2: 39, 39/40, s[39/40], 36/40, s[36/40], 39/36, s[39/36]

## Value

an object of class 'UPb', 'ArAr', 'RbSr', 'SmNd', 'ReOs', 'UThHe', 'fission', 'cosmogenics', or 'other'

## Examples

```
# load one of the built-in .csv files:
data(examples)
concordia(examples$UPb)
```

---

settings	<i>Load settings to and from json</i>
----------	---------------------------------------

---

**Description**

Get and set preferred values for decay constants and isotopic abundances from and to a .json file format

**Usage**

```
settings(fname = NULL)
```

**Arguments**

fname                      the path of a .json file

**Value**

if fname==NULL, returns a .json string

**Examples**

```
json <- system.file("defaults.json",package="IsoplotR")
settings(json)
print(settings())
```

---

weightedmean	<i>Calculate the weighted mean age</i>
--------------	--

---

**Description**

Models the data as a Normal distribution with two sources of variance. Estimates the mean and 'overdispersion' using the method of Maximum Likelihood. Computes the MSWD of a Normal fit without overdispersion. Implements Chauvenet's Criterion to detect and reject outliers. Only propagates the analytical uncertainty associated with decay constants and J-factors after computing the weighted mean isotopic composition.

**Usage**

```
weightedmean(x, ...)

## Default S3 method:
weightedmean(x, detect.outliers = TRUE, plot = TRUE,
  rect.col = rgb(0, 1, 0, 0.5), outlier.col = rgb(0, 1, 1, 0.5),
  sigdig = 2, alpha = 0.05, ...)
```

```

## S3 method for class 'UPb'
weightedmean(x, detect.outliers = TRUE, plot = TRUE,
  rect.col = rgb(0, 1, 0, 0.5), outlier.col = rgb(0, 1, 1, 0.5),
  sigdig = 2, type = 4, cutoff.76 = 1100, cutoff.disc = c(-15, 5),
  alpha = 0.05, exterr = TRUE, ...)

## S3 method for class 'ArAr'
weightedmean(x, detect.outliers = TRUE, plot = TRUE,
  rect.col = rgb(0, 1, 0, 0.5), outlier.col = rgb(0, 1, 1, 0.5),
  sigdig = 2, alpha = 0.05, exterr = TRUE, ...)

## S3 method for class 'UThHe'
weightedmean(x, detect.outliers = TRUE, plot = TRUE,
  rect.col = rgb(0, 1, 0, 0.5), outlier.col = rgb(0, 1, 1, 0.5),
  sigdig = 2, alpha = 0.05, exterr = TRUE, ...)

## S3 method for class 'fissiontracks'
weightedmean(x, detect.outliers = TRUE, plot = TRUE,
  rect.col = rgb(0, 1, 0, 0.5), outlier.col = rgb(0, 1, 1, 0.5),
  sigdig = 2, alpha = 0.05, exterr = TRUE, ...)

```

## Arguments

x	a two column matrix of values (first column) and their standard errors (second column) OR an object of class UPb OR an object of class ArAr
...	optional arguments
detect.outliers	Boolean flag indicating whether outliers should be detected and rejected using Chauvenet's Criterion.
plot	Boolean flag indicating whether the function should produce graphical output or return numerical values to the user.
rect.col	the fill colour of the rectangles used to show the measurements or age estimates.
outlier.col	if detect.outliers=TRUE, the outliers are given a different colour.
sigdig	the number of significant digits of the numerical values reported in the title of the graphical output.
alpha	the confidence limits of the error bars/rectangles.
type	scalar indicating whether to plot the $^{207}\text{Pb}/^{235}\text{U}$ age (type=1), the $^{206}\text{Pb}/^{238}\text{U}$ age (type=2), the $^{207}\text{Pb}/^{206}\text{Pb}$ age (type=3), the $^{207}\text{Pb}/^{206}\text{Pb}$ - $^{206}\text{Pb}/^{238}\text{U}$ age (type=4), or the (Wetherill) concordia age (type=5)
cutoff.76	the age (in Ma) below which the $^{206}\text{Pb}/^{238}\text{U}$ and above which the $^{207}\text{Pb}/^{206}\text{Pb}$ age is used. This parameter is only used if type=4.
cutoff.disc	two element vector with the maximum and minimum percentage discordance allowed between the $^{207}\text{Pb}/^{235}\text{U}$ and $^{206}\text{Pb}/^{238}\text{U}$ age (if $^{206}\text{Pb}/^{238}\text{U} < \text{cutoff.76}$ ) or between the $^{206}\text{Pb}/^{238}\text{U}$ and $^{207}\text{Pb}/^{206}\text{Pb}$ age (if $^{206}\text{Pb}/^{238}\text{U} > \text{cutoff.76}$ ). Set cutoff.disc=NA if you do not want to use this filter.
exterr	propagate decay constant uncertainty?



**Value**

if PLOT=FALSE, returns a list with the following items:

mean: a two element vector with the weighted mean and its standard error.

disp: a two element vector with the (over)dispersion and its standard error.

mswd: the Mean Square of the Weighted Deviates (a.k.a. 'reduced Chi-square' statistic)

p.value: the p-value of a Chi-square test with n-1 degrees of freedom, testing the null hypothesis that the underlying population is not overdispersed.

valid: vector of Boolean flags indicating which steps are included into the weighted mean calculation

**Examples**

```
ages <- c(251.9,251.59,251.47,251.35,251.1,251.04,250.79,250.73,251.22,228.43)
errs <- c(0.28,0.28,0.63,0.34,0.28,0.63,0.28,0.4,0.28,0.33)
weightedmean(cbind(ages,errs))
#data(examples)
#weightedmean(examples$ArAr)
```

---

yorkfit

---

*Linear regression of X,Y-variables with correlated errors*


---

**Description**

Implements the unified regression algorithm of York et al. (2004) which, although based on least squares, yields results that are consistent with maximum likelihood estimates of Ludwig and Titterton (1994)

**Usage**

```
yorkfit(X, Y, sX, sY, rXY)
```

**Arguments**

X	vector of measurements
Y	vector of measurements
sX	standard errors of X
sY	standard errors of Y
rXY	correlation coefficients between X and Y

**Value**

a two element list of vectors containing

**a** the intercept of the straight line fit and its standard error

**b** the slope of the fit and its standard error

## References

Ludwig, K. R., and D. M. Titterton. "Calculation of  $^{230}\text{Th}/^{232}\text{Th}$  isochrons, ages, and errors." *Geochimica et Cosmochimica Acta* 58.22 (1994): 5031-5042.

York, Derek, et al. "Unified equations for the slope, intercept, and standard errors of the best straight line." *American Journal of Physics* 72.3 (2004): 367-375.

## Examples

```
X <- c(1.550,12.395,20.445,20.435,20.610,24.900,
      28.530,50.540,51.595,86.51,106.40,157.35)
Y <- c(.7268,.7849,.8200,.8156,.8160,.8322,
      .8642,.9584,.9617,1.135,1.230,1.490)
n <- length(X)
sX <- X*0.01
sY <- Y*0.005
rXY <- rep(0.8,n)
fit <- yorkfit(X,Y,sX,sY,rXY)
covmat <- matrix(0,2,2)
plot(range(X),fit$a[1]+fit$b[1]*range(X),type='l',ylim=range(Y))
for (i in 1:n){
  covmat[1,1] <- sX[i]^2
  covmat[2,2] <- sY[i]^2
  covmat[1,2] <- rXY[i]*sX[i]*sY[i]
  covmat[2,1] <- covmat[1,2]
  ell <- ellipse(X[i],Y[i],covmat,alpha=0.05)
  polygon(ell)
}
```

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