

Mixed Integer Linear Programming for Portfolio Optimization

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ABSTRACT

Our team explored the application of a Mixed Integer Linear Programming (MILP) approach to optimize the portfolio of equity derivatives. We have developed an optimization model that seeks to minimize the net costs spent on options over a given period. By utilizing MILP, our approach ensures a minimum exposure of +\$10,000,000 for a given scenario, while minimizing the total premium costs across a time frame of one month.

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1 NET COSTS APPROACH

1.1 Definitions

- The set of options $o \in O$.
- The set of trading dates $d \in D$.

1.2 Decision Variables

For each option $o \in O$:

- $x_o \in \mathbb{Z}^+ :=$ the number of **contracts** to buy.
- $y_o \in \mathbb{Z}^+ :=$ the number of **contracts** to sell.

1.3 Parameters

- | | |
|-----------------------|----------------------------|
| • a_o : Ask Price | • k_o : Strike Price |
| • b_o : Bid Price | • s_o : Underlying Price |
| • A_o : Ask Size | • d_o : Trading Date |
| • B_o : Bid Size | • T_o : Maturity Date |
| • M : Contract Size | • β : Spot Move |

1.3.1 Exposure Function (per Option)

We know that $\text{Min exposure} \geq 10,000,000 \forall d \in D$. Since the next day underlying price is based on spot move, the exposure function per option, E is given by:

$$E(o) = \max(\beta \cdot s_o - k_o, 0) - \max(s_o - k_o, 0)$$

1.3.2 Non-Expired Options

For each trading date $d \in D$: Let $O_d = \{o \in O \mid T_o \geq \text{next_date}(d)\}$, the set of non-expired options.

1.4 Objective Function & Constraints

With this approach, we want to minimize total premium cost over all options:

$$\min \sum_O M \cdot (a_o x_o - b_o y_o)$$

Subject to:

- (i) **Purchase Limits:** $x_o \leq A_o \forall o \in O$
- (ii) **Sales Limits:** $y_o \leq B_o \forall o \in O$
- (iii) **Net Position:** $y_o \leq x_o \forall o \in O$
- (iv) **Expiry:** For any option o where $d_o \geq T_o$, set $x_o = 0, y_o = 0$.
- (v) **Daily Minimum Exposure:**

For each trading date $d \in D$ such that $d + 1 \in D$, our **aggregate exposure** must meet the minimum:

$$M \sum_{o \in O_d} (x_o - y_o) E(o) \geq 10,000,000$$