

TASK 1:

```
Task 1: Deriving the Private Key

p = F7E75FDC469067FFDC4E847C51F452DF
q = E85CED54AF57E53E092113E62F436F4F

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n = E103ABD94892E3E74AFD724BF28E78366D9676BCCC70118BD0AA1968DBB143D1
phi(n) = E103ABD94892E3E74AFD724BF28E78348D52298BD687C44DEB3A81065A7981A4
Private key d = 3587A24598E5F2A21DB007D89D18CC50ABA5075BA19A33890FE7C28A9B496AEB
qasim@ubuntu: ~/Downloads/Labsetup$
```

```
1 #include <stdio.h>
2 #include <openssl/bn.h>
3 void printBN(char *msg, BIGNUM *a) {
       char *num str = BN bn2hex(a);
5
       printf("%s %s\n", msg, num str);
       OPENSSL free(num str);
6
7 }
8 int main() |
9
       BN CTX *ctx = BN CTX new();
1Θ
       BIGNUM *p = BN new(), *q = BN new(), *n = BN new(), *e = BN new(), *phi = BN new();
       BIGNUM *p_1 = BN_new(), *q_1 = BN_new(), *d = BN_new()
11
       BN hex2bn(&p, "F7E75FDC469067FFDC4E847C51F452DF");
BN hex2bn(&q, "E85CED54AF57E53E092113E62F436F4F");
BN hex2bn(&e, "0D88C3");
12
13
14
15
       BN mul(n, p, q, ctx); printBN("n = ", n);
       BN_sub(p_1, p, BN_value_one());
16
17
       BN_sub(q_1, q, BN_value_one());
18
       BN mul(phi, p 1, q 1, ctx); printBN("phi(n) = ", phi);
       BN_mod_inverse(d, e, phi, ctx); printBN("Private key d = ", d);
19
20 🔢
```

TASK 2:

```
Task 2: Encrypting a Message

qasim@ubuntu: ~/Downloads/Labsetup

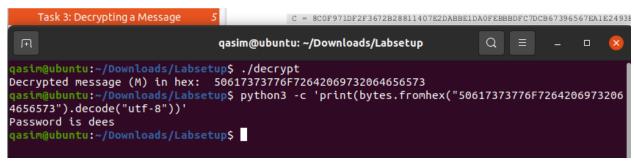
qasim@ubuntu: ~/Downloads/Labsetup$ gcc encrypt.c -o encrypt -lcrypto
qasim@ubuntu: ~/Downloads/Labsetup$ ./encrypt
encryption of message = 6FB078DA550B2650832661E14F4F8D2CFAEF475A0DF3A75CACDC5DE5CFC5FADC
decryption of message = 4120746F702073656372657421
qasim@ubuntu: ~/Downloads/Labsetup$ python3 -c 'print("A top secret!".encode("utf-8").hex())'
4120746f702073656372657421
qasim@ubuntu: ~/Downloads/Labsetup$

1 #include <stdio.h>
2 #include <openssl/bn.h>
3 #define NBITS 256
4 |
5 yoid printBNhex(char *msq. BIGNIM * a)
```

```
5 void printBNhex(char *msg, BIGNUM * a)
6 {
 7
            /* Use BN bn2hex(a) for hex string*/
 8
            char * number_str = BN_bn2hex(a);
            printf("%s %s\n", msg, number str);
 9
            OPENSSL free(number_str);
10
11 }
12 int main ()
13 {
14
            BN CTX *ctx = BN CTX new();
15
            BIGNUM *e = BN new();
            BIGNUM *n = BN new();
16
            BIGNUM *M = BN new();
17
            BIGNUM *c = BN new();
18
19
            BIGNUM *d = BN new();
20
            BN_hex2bn(&n, "DCBFFE3E51F62E09CE7032E2677A78946A849DC4CDDE3A4D0CB81629242FB1A5");
            BN_hex2bn(&e, "010001");
BN_hex2bn(&M, "4120746f702073656372657421");
BN_hex2bn(&d, "74D806F9F3A62BAE331FFE3F0A68AFE35B3D2E4794148AACBC26AA381CD7D30D");
21
22
23
24
            BN mod exp(c, M, e, n, ctx);
25
            printBNhex("encryption of message = ", c);
26
            BN mod exp(M, c, d, n, ctx);
27
            printBNhex("decryption of message = ", M);
28
29 }
```

]

TASK 3:



```
decrypt.c
    Open
                       ſŦ
                                                                        ~/Downloads/Labsetup
 1 #include <stdio.h>
 2 #include <openssl/bn.h>
 3 void printBN(char *msg, BIGNUM *a) {
 4 char *number str = BN bn2hex(a);
 5
       printf("%s %s\n", msg, number str);
 6
       OPENSSL_free(number_str);
 7 }
 8 int main() {
 9
       BN CTX *ctx = BN CTX new();
       BIGNUM *n = BN new();
10
       BIGNUM *d = BN new();
11
       BIGNUM *C = BN new();
12
13
       BIGNUM *M = BN new();
       BN_hex2bn(&n, "DCBFFE3E51F62E09CE7032E2677A78946A849DC4CDDE3A4D0CB81629242FB1A5");
14
       BN_hex2bn(&d, "74D806F9F3A62BAE331FFE3F0A68AFE35B3D2E4794148AACBC26AA381CD7D30D"); BN_hex2bn(&C, "8C0F971DF2F3672B28811407E2DABBE1DA0FEBBBDFC7DCB67396567EA1E2493F");
15
16
17
       BN mod exp(M, C, d, n, ctx);
18
       printBN("Decrypted message (M) in hex: ", M);
19 }
```

TASK 4:

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Task 4: Signing a Message

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```

```
1 #include <stdio.h>
 2 #include <openssl/bn.h>
 3 #define NBITS 256
 5 void printBNhex(char *msg, BIGNUM * a){
      char *number_str = BN_bn2hex(a);
 7
       printf("%s %s\n", msg, number_str);
 8
       OPENSSL free(number str);
 9 }
10
11 int main ()
      BN CTX *ctx = BN CTX new();
12
       BIGNUM *e = BN new();
13
      BIGNUM *n = BN new();
14
      BIGNUM *M1 = \overline{BN} new();
15
      BIGNUM *M2 = BN new():
16
17
      BIGNUM *c1 = BN new();
      BIGNUM *c2 = BN new();
18
19
      BIGNUM *d = BN new();
20
       BN_hex2bn(&n, "DCBFFE3E51F62E09CE7032E2677A78946A849DC4CDDE3A4D0CB81629242FB1A5");
21
22
       BN hex2bn(&e, "010001");
       BN_hex2bn(&M1, "49206F776520796F752024323030302E");
23
       BN_hex2bn(&M2, "49206F776520796F752024333030302E");
24
25
       BN hex2bn(&d, "74D806F9F3A62BAE331FFE3F0A68AFE35B3D2E4794148AACBC26AA381CD7D30D");
26
27
       // Encrypting $2000
28
       BN mod exp(cl, Ml, d, n, ctx);
29
       printBNhex("Encryption of message \"$2000.\" = ", c1);
30
31
       // Encrypting $3000
32
       BN mod exp(c2, M2, d, n, ctx);
       printBNhex("Encryption of message \"$3000.\" = ", c2);
33
34
35
```

TASK 5:

```
Task 5: Verifying a Signature

qasim@ubuntu: ~/Downloads/Labsetup

qasim@ubuntu: ~/Downloads/Labsetup$ gcc verify.c -o verify -lcrypto
qasim@ubuntu: ~/Downloads/Labsetup$ ./verify

Decrypted message hex = 4C61756E63682061206D697373696C652E

Expected message hex = 4C61756E63682061206D697373696C652E

Signature is valid.
qasim@ubuntu: ~/Downloads/Labsetup$
```

```
1 #include <stdio.h>
2 #include <openssl/bn.h>
3 #include <string.h>
4 #define NBITS 256
5 void printBNhex(char *msg, BIGNUM *a) {
      char *number str = BN bn2hex(a);
7
      printf("%s %s\n", msg, number_str);
8
      OPENSSL free(number str);
9 }
10 void convertMessageToHex(const char *msg, BIGNUM *msg bn) {
11
12
      size t len = strlen(msg);
13
      char hex str[len * 2 + 1];
14
      for (size t i = 0; i < len; i++) {</pre>
           sprintf(&hex str[i * 2], "%02x", (unsigned char)msg[i]);
15
16
17
      hex str[len * 2] = ' \setminus 0';
18
      BN hex2bn(&msg bn, hex str);
19 }
20 int main() {
21
      BN CTX *ctx = BN CTX new();
22
23
      BIGNUM *e = BN new();
24
      BIGNUM *n = BN new();
25
      BIGNUM *S = BN new();
26
      BIGNUM *m = BN new();
27
      BIGNUM *expected msg = BN new();
28
      BN hex2bn(&n, "AE1CD4DC432798D933779FBD46C6E1247F0CF1233595113AA51B450F18116115");
      BN hex2bn(&e, "010001");
29
      BN hex2bn(&S, "643D6F34902D9C7EC90CB0B2BCA36C47FA37165C0005CAB026C0542CBDB6802F");
30
31
      BN mod exp(m, S, e, n, ctx);
      printBNhex("Decrypted message hex = ", m);
32
      convertMessageToHex("Launch a missile.", expected msg);
33
      printBNhex("Expected message hex = ", expected_msg);
34
35
      if (BN cmp(m, expected msg) == 0) {
36
          printf("Signature is valid.\n");
37
      } else {
38
           printf("Signature is invalid.\n");
39
40 }
```

TASK 6:

1. Certificate Retrieval: Retrieved Facebook's certificates using openssl s_client and saved them as c0.pem and c1.pem.

```
qasim@ubuntu: ~/Downloads/Labsetup
qasim@ubuntu:~/Downloads/Labsetup$ openssl s_client -connect www.facebook.com:443 -showcerts
CONNECTED(00000003)
depth=2 C = US, O = DigiCert Inc, OU = www.digicert.com, CN = DigiCert High Assurance EV Root CA
verify return:1
depth=1 C = US, O = DigiCert Inc, OU = www.digicert.com, CN = DigiCert SHA2 High Assurance Server C
verify return:1
depth=0 C = US, ST = California, L = Menlo Park, O = "Meta Platforms, Inc.", CN = *.facebook.com
verify return:1
Certificate chain
0 s:C = US, ST = California, L = Menlo Park, 0 = "Meta Platforms, Inc.", CN = *.facebook.com
 i:C = US, O = DigiCert Inc, OU = www.digicert.com, CN = DigiCert SHA2 High Assurance Server CA
 ----BEGIN CERTIFICATE---
MIIGmDCCBYCgAwIBAgIQDSXR7+FsuhxCLMjTrFaCODANBgkqhkiG9w0BAQsFADBw
MQswCQYDVQQGEwJVUZEVMBMGA1UEChMMRGlnaUNlcnQgSW5jMRkwFwYDVQQLExB3
qasim@ubuntu:~/Downloads/Labsetup$ nano c0.pem
qasim@ubuntu:~/Downloads/Labsetup$ nano c1.pem
gasim@ubuntu:~/Downloads/Labsetup$
```

2. Public Key Extraction: Extracted the public key (n,e) from the issuer's certificate.

```
sim@ubuntu:~/Downloads/Labsetup$ openssl x509 -in c1.pem -noout -modulus | openssl md5
(stdin)= 5398db7538f69b1c77092935f13281bc
qasim@ubuntu:~/Downloads/Labsetup$ openssl x509 -in c1.pem -text -noout
Certificate:
   Data:
        Version: 3 (0x2)
        Serial Number:
            04:e1:e7:a4:dc:5c:f2:f3:6d:c0:2b:42:b8:5d:15:9f
        Signature Algorithm: sha256WithRSAEncryption
        Issuer: C = US, O = DigiCert Inc, OU = www.digicert.com, CN = DigiCert High Assurance EV Ro
ot CA
        Validity
            Not Before: Oct 22 12:00:00 2013 GMT
            Not After: Oct 22 12:00:00 2028 GMT
        Subject: C = US, O = DigiCert Inc, OU = www.digicert.com, CN = DigiCert SHA2 High Assurance
Server CA
        Subject Public Key Info:
            Public Key Algorithm: rsaEncryption
                RSA Public-Key: (2048 bit)
```

3. Signature Extraction: Extracted and formatted the signature from the server's certificate using openssl x509.

```
qasim@ubuntu:~/Downloads/Labsetup$ openssl x509 -in c0.pem -text -noout
Certificate:
    Data:
        Version: 3 (0x2)
        Serial Number:
            0d:25:d1:ef:e1:6c:ba:1c:42:2c:c8:d3:ac:56:82:38
            Signature Algorithm: sha256WithRSAEncryption
            Issuer: C = US, 0 = DigiCert Inc, 0U = www.digicert.com, CN = DigiCert SHA2 High Assurance
Server CA
        Validity
            Not Before: Jul 22 00:00:00 2024 GMT
            Not After : Oct 20 23:59:59 2024 GMT
            Subject: C = US, ST = California, L = Menlo Park, O = "Meta Platforms, Inc.", CN = *.facebook.com
```

4. Body Extraction: Used openssl asn1parse to extract the certificate body and saved it as c0 body.bin.

```
Downloads/Labsetup$ cat c0.pem | grep "Signature" | awk '{print $2}' | tr -d ':
signature.hex
asim@ubuntu:~/Downloads/Labsetup$ openssl asn1parse -in c0.pem -out c0_body.bin
   0:d=0 hl=4 l=1688 cons: SEQUENCE
   4:d=1 hl=4 l=1408 cons: SEQUENCE
                   3 cons: cont [ 0 ]
   8:d=2
         hl=2 l=
  10:d=3 hl=2 l=
                   1 prim: INTEGER
                                             :02
  13:d=2 hl=2 l= 16 prim: INTEGER
                                             :0D25D1EFE16CBA1C422CC8D3AC568238
  31:d=2 hl=2 l= 13 cons: SEQUENCE
  33:d=3 hl=2 l=
                  9 prim: OBJECT
                                             :sha256WithRSAEncryption
  44:d=3
          hl=2 l=
                   0 prim: NULL
  46:d=2
          hl=2 l= 112 cons: SEQUENCE
  48:d=3 hl=2 l= 11 cons: SET
  50:d=4 hl=2 l=
                   9 cons: SEQUENCE
                                             :countryName
  52:d=5 hl=2 l=
                   3 prim: OBJECT
  57:d=5
          hl=2 l=
                   2 prim: PRINTABLESTRING
  61:d=3 hl=2 l=
                   21 cons: SET
  63:d=4 hl=2 l=
                  19 cons: SEQUENCE
  65:d=5 hl=2 l=
                                             :organizationName
                  3 prim: OBJECT
```

5. Hashing: Computed the SHA-256 hash of c0 body.bin to prepare for signature verification.

```
qasim@ubuntu:~/Downloads/Labsetup$ sha256sum c0_body.bin > hash.txt
qasim@ubuntu:~/Downloads/Labsetup$
```

6. Signature Verification: Verified the signature using the extracted public key and noted the differences in hashes during verification.