### **Model-based Reasoning**

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#### **Introduction**

- Description of the Field
- Motivations for development
- · Relevance of the Field
- Objectives
- Overview
- Models Background
- Recommended Text:
  "Qualitative Reasoning"
  Ben Kuipers, MIT Press 1994
  £40 if you are really interested!

#### **Model-based Reasoning**

- Qualitative Reasoning
  - Symbollic, using no numbers
  - Structural though incomplete
  - Synonyms: Naive physics, Qualitative modelling, Qualitative simulation, Commonsense reasoning, Deep knowledge.
- · Developments
  - Use of any models in the domain reasoning process
  - Numerical, Interval, Semi-quantitative, Fuzzy, Qualitative, Rule-based, Procedural

#### **Systems**

- Natural Systems
  - Physical: Fluid behaviour, Chemical reactions
  - Biological: Drug uptake, Cardiac performance, Renal operation, Photosynthesis
  - Ecological
- · Artificial Systems
  - Physical: Electrical circuits,
     Mechanical systems, Chemical plant
  - Economic: Housing markets, Organisations

#### **Motivations**

- · Problems with RBS
  - Reasoning from First Principles
  - Dangers with "nearest approximation"
- Modellers requirements
- Second Generation Expert Systems
  - Use deep knowledge
  - Provide explanations of reasoning process
- · Commonsense reasoning
  - Capture how humans reason
  - Enable use of appropriate causality
- · Model reuse
  - Improved ease of ES maintenance

## Is MBR relevant? (1)

- Domains of Application
  - Modelling of ecological systems
  - Diagnosis of industrial plant
  - Training of process operators
  - Control of process plant
- · Industrial Investment
  - Number of large collaborative projects involving industry (e.g. Unilever, Siemens, BG) and academia
- Eye to the future
  - Industrial rollout
  - Focus on the essence of 'Modelling'
- · Development methods
  - KADS Expert Systems development
  - ARTIST, PRIDE Model-based Diagnosis

#### Is MBR relevant (2)

- · Communication infrastructure
  - European Monet
  - National R&R (UK), MQD (France)
- Commercialisation
  - Tiger Diagnosis of Gas Turbines
  - FLAME (Autosteve) FMEA and Diagnosis of car electrics

### **Objectives**

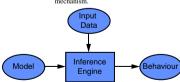
- · Understand basis of QR and MBR
- · Awareness of modelling perspectives
- Understanding of QR ontologies
- Detailed knowledge of constraint approaches - development and application
- · Awareness of domains of application
- Awareness of issues in model construction
- (Understanding of spatial models)

#### Overview

- · Background and Basics
  - Ontologies, Quantity spaces,
     Qualitative arithmetic, Operations,
     Causality.
- · Major methods of QR
  - Devices, Processes and Constraints
  - Focus on constraint based and developments
- · Reasoning Domains
  - Explanation, Diagnosis, Training, Prediction, Spatial reasoning, Kinematics
- Modelling Methodologies
  - Teleological, Behavioural,
     Multimodelling, Multiple models

#### What is a Model?

- · Assume knowledge
  - · You've all come across them.
- Physical
  - E.g. Doorlock mechanism
- Mathematical
  - Declarative Structure
    - · Representation
      - Executable but distinct from inference mechanism.



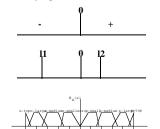
- Prediction:
  - What value will it have?
- Explanation
  - Why did it happen that way?
  - Facilitates understanding of system

# **Basic Principles of QR**

- · Terminology and Concepts
  - new(ish) field: proliferation of terms
  - underlying concepts basis for all QR
- Symbollically represents the important (qualitative) distinctions in a system
  - increasing, steady, decreasing
  - high, medium, low
- · Scales of Measurement
  - nominal, ordinal, interval, ratio
- · Qualitative versus Quantitative?

# **Qualitative Reasoning**

- · Components of a Qualitative Model
  - Ontology (a way of looking at the world)
  - Variables (things that change)
  - Quantity space (values variables take)
  - Relations (what variables do to each other)
- · Quantity Spaces



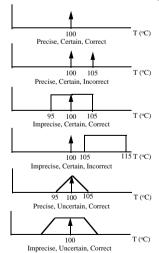
#### **Qualitative Relations**

#### · Behavioural Abstraction



- Incompleteness
  - Not the same as "Uncertainty"
    - · but is related to "Precision"
  - Known model structure (assumed)
  - Imprecise knowledge of system functional relations
- · Operators
  - ADD, MULT, DERIV

## **Precision and Uncertainty**



## **Arithmetic Operations**

#### • Sign Algebra

MULT

| 8 | + | 0 | - |
|---|---|---|---|
| + | + | 0 | _ |
| 0 | 0 | 0 | 0 |
| _ | _ | 0 | + |

DIV

| 0 | + | 0 | _ |
|---|---|---|---|
| + | + | X | _ |
| 0 | 0 | X | 0 |
| _ | _ | X | + |

# **Aritmetic Operations (2)**

ADD

| $\oplus$ | + | 0 | _ |
|----------|---|---|---|
| +        | + | + | ? |
| 0        | + | 0 | _ |
| _        | ? | _ | _ |

|     | Φ | + | 0 | - |
|-----|---|---|---|---|
| SUB | + | ? | + | + |
| зов | 0 | _ | 0 | + |
|     | _ | _ | _ | ? |

# **Arithmetic Operations (3)**

$$A = B - C$$

where B & C both have value [+], A will be undefined

- Disambiguation
  - may be possible from other information
  - A = [+] if B > C
  - A = [0] if B = C
  - A = [-] if B < C
- Functional Relations
  - $Y = \mathbf{M} + (X)$
  - $Y = \mathbf{M} (X)$

## **Qualitative Vectors**

- Convenient representation of state and behaviour
- Consists of Magnitude and first *n* derivatives of a variable:

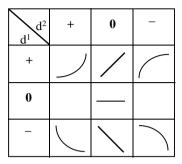
 $x \rightarrow d^0$  (zeroth derivative)  $x' \rightarrow d^1$  (first derivative)  $x'' \rightarrow d^2$  (second derivative)

. . .

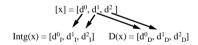
$$[x] = (d^0, d^1, d^2 \dots)$$

• Usually need at least two elements in a vector (three is better because curve shapes can be seen).

## **Qualitative Vectors (2)**



### **Qualitative Calculus**



For Integration:

$$d^0_I = d^0 + d^1 = d^1_I + d^2_I$$
  
(by Taylor's Theorem)

For Differentiation:

d<sup>2</sup><sub>D</sub>: depends on what is known of the original function (or system in which it appears)

# **Model Types**

- Static (Equilibrium)
  - algebraic equations only

$$[A] = [B] + [C]$$

$$[X] = M + ([Y])$$

$$M = U * V$$

- Dynamic
  - contains derivatives,
  - requires integration

$$x' = k.x$$

$$y = \int x dt$$

- may also have algebraic parts
- NB: Dynamic is not the same as time varying!!!

# Model Types (2)

- Continuous
  - no gaps in quantity space
  - no jumps allowed
  - focus of QR (mainly)



- Discontinuous/Discrete
  - finite number of gaps in quantity space
  - jumps can occur



#### **Behaviour Types**

- Results of Simulation/Inference are known as **ENVISIONMENTS**
- TOTAL ENVISIONMENT
  - All possible behaviours for all possible inputs
- COMPLETE ENVISIONMENT
  - All possible behaviours for a specific input
- ATTAINABLE ENVISIONMENT
  - All behaviours from a specified initial value and input ~ with a fixed quantity space
- PARTIAL ENVISIONMENT
  - All behaviours from a specified initial value and input ~ with landmark generation

# **Behaviour Types (2)**

- Envisionments are represented as a graph or a tree
- BEHAVIOUR
  - Single path through an envisionment graph or behaviour tree
- HISTORY
  - Behaviour of a single variable removed from its envisioned context.

## **Ontology**

- A way of representing what there is in the world (closed)
- Two (main) perspectives:
  - Functional: focuses on purpose (design)
  - Behavioural: focuses on operation
- Three Behavioural Ontologies:
  - Devices (Components): pipes, tanks valves
  - Processes: heating, reacting, decomposing
  - Constraints: relations between variables