Homework 6: Continuations

Due date: November 17 (Thursday) at 11:59pm

Overview

This homework consists of two parts:

- 1. Using continuations, implement throw and try_except functions that allow programs to throw and handle exceptions. Then, using the two functions, implement a simple error-detecting calculator.
- 2. Using continuations, implement attempt and assert functions that allow programs to write back-tracking algorithms. Then, using the two functions, implement a simple solver for a Sudoku puzzle.

Some important notes:

• You will use the Racket language, which natively supports continuations. See the instructions below for installing Racket, and read the following guide to Racket before starting the homework.

https://cs242.stanford.edu/materials/assignments/racket-guide.html

For more details on Racket, see https://docs.racket-lang.org/guide/index.html. We highlight a particularly important aspect of Racket that may be confusing at first: be careful about parentheses, they play a significant syntactic role in Racket and you should use them only when they are necessary. The CA's solution is written exclusively with the following built-in syntax or functions of Racket: call/cc, define, lambda, let*, if, cond, else, printf, equal?, not, and, number?, >, +, -, *, /, list, first, second, third, rest, length, and range.

• You should not use any built-in syntax or functions of Racket to throw or handle exceptions. To allow us to automatically enforce this restriction, the words "raise" and "handler" should not appear in any parts of your solution files (prob*.rkt), including comments.

Installing Racket

The particular version of Racket you should use is **Racket Minimal 8.6**. You may either install it on your local machine or work on myth.stanford.edu.

On myth

On the myth machines, you can access the Racket executable by adding the CS 242 directory to your search path. To do this, modify the .bashrc file in your home directory and add this line to the bottom:

export PATH=/afs/ir/class/cs242/tools/racket/bin:\$PATH

Then, restart your shell by either closing and re-SSHing into myth or by running source .bashrc. Verify that you can access Racket by running racket --version, which should print out Welcome to Racket v8.6 [cs]

If you are using a non-default shell on myth, the command to add the CS 242 directory to your path may be different.

Locally

Download the "Minimal Racket" installation file corresponding to your system from the official webpage:

Once you've downloaded Racket, you should have a folder named Racket v8.6 that contains. Rename it to remove the version number, so it's just named Racket. You'll need to add the Racket/bin subdirectory to your \$PATH in order to run Racket from anywhere, just like on Myth. The process varies by system; if you're not sure how, you can follow Section 1.2 of the following installation guide to update the PATH environment variable:

Once complete, verify your Racket installation by running racket --version, which should print Welcome to Racket v8.6 [cs].

How to Use Continuations in Racket

In Racket, we can obtain and pass the current continuation to a function using the call/cc syntax. For example, the expression $(2 + (\text{call/cc } \lambda k. 3 + (\text{resume } k \ 4)))$ written in the language discussed in the lecture can be translated into Racket as follows.

$$\left(+ 2 \left(\text{call/cc } \left(\text{lambda } (k) \left(+ 3 \left(k 4 \right) \right) \right) \right) \right)$$

Here we use different sizes of brackets just to make the expression more readable. Note that $(\operatorname{call/cc} \lambda k. e)$ is translated into Racket as $(\operatorname{call/cc} (\operatorname{lambda} (k) e))$, and (resume k e) as (k e). In this expression, the continuation of the subexpression $(\operatorname{call/cc} \ldots)$ is $(\lambda \square . (+ 2 \square))$, when represented as a lambda abstraction, since the subexpression is in the place of \square in the entire expression $(+ 2 \square)$. What the call/cc syntax inside the expression does is as follows: the call/cc applies its argument $(\operatorname{lambda} (k) (\ldots))$ to the continuation $(\lambda \square . (+ 2 \square))$ of the subexpression (call/cc ...) and then continues evaluation. This leads to the following evaluation steps, where the subexpressions being evaluated at each step are underlined.

$$\begin{pmatrix} + 2 & \left(\frac{\text{call/cc} \left(\text{lambda} (k) + 3 (k 4) \right)}{\text{call/cc} \left(\text{lambda} (k) + 3 (k 4) \right)} \right) \\ \rightarrow & \left(+ 2 & \left(\frac{\text{lambda} (k) + 3 (k 4)}{\text{call} \left(+ 2 \right)} \right) \right) \\ \rightarrow & \left(+ 2 & \left(+ 3 & \left(\frac{(\lambda \square (+ 2 \square))}{\text{call} \left(+ 2 \right)} \right) \right) \right) \\ \rightarrow & \left(+ 2 & 4 \right) \\ \rightarrow & 6 & \end{pmatrix}$$

Note that the second last expression is obtained from the third last one, since 4 is applied to the continuation $(\lambda \square. (+ 2 \square))$ (i.e., the continuation $(\lambda \square. (+ 2 \square))$) is resumed with the value 4). This way we can obtain and pass the current continuation using the call/cc syntax, and resume a continuation k with the evaluation result of e using (k e). In this homework, you will figure out how to use call/cc appropriately to implement exception handling and backtracking algorithms.

Part 1: Exception handling

In the first part of this assignment, you will implement two functions throw and try_except using call/cc (Problem 1), which can serve as a building block for raising and handling exceptions, and then you will implement a simple error-detecting calculator using the two functions (Problem 2).

Problem 1: throw and try_except

The goal of this problem is to implement two functions throw and try_except, which correspond roughly to the raise keyword and the try: ... except: ... statement in Python. For example, throw and try_except should behave as follows.

Example program:

```
Expected print-out:
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That is, (throw msg) should throw (or raise) an exception that carries a message msg. On the other hand, (try_except try_f except_f) should run (try_f) and, if an exception is thrown by (throw msg) during the evaluation of (try_f), it should catch (or handle) the exception and run (except_f msg) immediately after the exception is thrown.

You can assume that throw takes a single string as an argument and try_except takes two functions try_f and except_f as arguments. To simplify the problem, assume that multiple uses of try_except's cannot be nested and continuations cannot be created, stored, or called anywhere except in the definition of throw and try_except. If an exception is thrown by throw outside try_f (i.e., either inside except_f or outside (try_except ...)), you should print out an error message ThrowError and exit to the top-level.

Implement throw and try_except in prob1.rkt using call/cc. You can test your implementation by running racket test/prob1_test.rkt. The expected outputs are provided in the test file. It will be useful to utilize the stack defined in prob1.rkt to store continuations and some arguments of try_except, and the function exit to exit to the top-level. The CA's solution without comments is 20 lines of code.

Hint: One way to implement throw and try_except is as follows. Note that the following description is not complete (just gives you an idea) and there can be other ways to implement them. In try_except which takes arguments try_f and except_f, push the current continuation k and except_f to the stack, call (try_f), and then pop k and except_f from the stack. In throw which takes an argument msg, pop the topmost k and except_f from the stack if the stack is not empty, call (except_f msg), and then resume k with the return value of the call.

Problem 2: Error-detecting calculator

The goal of this problem is to implement a function eval, which takes an arithmetic expression as an argument, and prints out an error message if the expression contains an error of certain types, and prints out the evaluation result otherwise. For example, eval should behave as follows.

Example program:

Expected print-out:

The first line prints out a division-by-zero error, as we have to compute (/ 2 0) while evaluating the given expression. The second line prints out an invalid operator error, as the given expression includes an invalid operator #. The third line prints out the evaluated result, as the given expression makes no errors.

You can assume eval takes a single argument of the following form, where n and s denote a number and a string in Racket, respectively.

```
e ::= n \mid (\texttt{list} \ s \ e \ e)
```

The function eval should detect and print out the two types of errors (and no more): a division-by-zero error, which occurs when an argument to eval contains a division-by-zero computation, and an invalid operator error, which occurs when an argument uses an operator other than "+", "-", "*", and "/". If no errors of the two types are found, eval should print out the evaluated result. You can assume any argument to eval has at most one error.

Implement eval in prob2.rkt using throw and try_except. You can test your implementation by running racket test/prob2_test.rkt. The expected outputs are provided in the test file. The CA's solution without comments is 22 lines of code.

Part 2: Backtracking algorithm

In the second part of this assignment, you will implement two functions attempt and assert using call/cc (Problem 3), which can serve as a building block for writing backtracking algorithms, and then you will implement a simple Sudoku solver using the two functions (Problem 4).

Problem 3: attempt and assert

The goal of this problem is to implement two functions attempt and assert. The function attempt takes a list 1 of choices as an argument and tries out each choice in 1 in order, until every argument of all subsequent asserts becomes true, or until the attempt tries out all the choices listed in 1, whichever happens first. For example, attempt and assert should behave as follows.

Example program:

```
Expected print-out:
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In the first and second lines, the program uses attempt to try out three choices (1, 2, and 3) for the variable x and another three choices (5, 6, and 7) for the variable y. In the fourth line, the program uses assert to describe a condition that needs to be satisfied, namely (* x y) should be equal to 15. From the expected print-out, you can check that the two calls to attempt indeed try out each of their choices one-by-one sequentially, until the condition of the assert becomes true. Note that the two calls to attempt should try their choices exactly in the order shown in the above expected print-out.

You can assume that attempt takes a single non-empty list as an argument and assert takes a single expression that evaluates to a boolean. The expression (attempt 1) should return one of the elements of 1 in the specific order described above. The expression (assert e) should return #t if e evaluates to #t at some point (possibly after trying out some choices), and should return #f if e evaluates to #f for all choices of the prior attempts.

Implement attempt and assert in prob3.rkt using call/cc. You can test your implementation by running racket test/prob3_testN.rkt, where $1 \le N \le 3$. The expected outputs are provided in the test file. It will be useful to utilize the stack defined in prob3.rkt to store continuations and some parts of the argument of attempt. The CA's solution without comments is 18 lines of code.

Problem 4: Sudoku solver

The goal of this problem is to implement a function solve, which solves a given Sudoku puzzle by a simple backtracking algorithm. To explain a Sudoku puzzle, define a *state* as a 9×9 grid partially (or fully) filled with the numbers $1, \dots, 9$. We say a state is *valid* if each number in the state does not appear twice in each

row, each column, and each of the nine 3×3 subgrids. A Sudoku puzzle starts with an initial state, and the objective of the puzzle is to find a valid state that extends the initial state and is fully filled. Such a valid state is a solution of the puzzle.

You can assume that solve takes a single argument state, which represents an initial state of a Sudoku puzzle, and that state has at most one solution. The expression (solve state) should return a solution to state if it exists, and should return #f otherwise. Any state (e.g., an argument or a return value of solve) should be represented as a list of lists in the following way: for example, (list (list 0 3 9) (list 8 0 7)) represents the state where 9 is written at the intersection of row 0 and column 3, and 7 is written at the intersection of row 8 and column 0.

Implement solve in prob4.rkt using attempt and assert. You can test your implementation by running racket test/prob4_testN.rkt, where $1 \le N \le 3$. The expected outputs are provided in the test file. It will be useful to utilize some helper functions defined in prob4.rkt to perform several primitive operations on states. The CA's solution without comments is 16 lines of code. Your solution should run in 15 seconds on the myth cluster for each test/prob4_testN.rkt; the CA's solution runs in < 2 seconds on the myth cluster for each testfile.

Submission

- Edit README.txt to include both your student ID number (the last 8-digit number).
- Generate solution.tar.gz by running python3 src/submit.py,and upload the tarball file to Canvas. Make sure the script gives no errors or warnings.
- Make sure the tarball file consists precisely of: prob{1,2,3,4}.rkt and README.txt.