# Object Calculus II

CS242

Lecture 8

### Review: Record Types

Conceptually an object is a record of fields and methods

```
[ flag = False, value = 42, add(i: Int): Int ]
```

For types we use function types

```
[ flag: Bool, value: Int, add: Int → Int ]
```

# Untyped Object Calculus Syntax

An object is a finite map from field names to methods that produce objects

$$o = [..., l_i = \varsigma(x) b_i, ...]$$

- Here
  - l<sub>i</sub> is a method/field name
  - $\zeta(x)$  b<sub>i</sub> is a method where x is the self object and b<sub>i</sub> is the body
- Operations:
  - Selection:  $o.l_i \rightarrow b_i\{x := o\}$
  - Override:  $o.l_i \le \varsigma(y) b \rightarrow [..., l_i = \varsigma(y) b, ...]$

# Simply Typed Object Calculus

A type has the form

$$X = [..., I_i: Y_i, ...]$$
  $i = 1..n$ 

- The Y<sub>i</sub> could also be X, so types are potentially recursive
- The Y<sub>i</sub> are the return values of the methods
  - All methods take a single argument of type X, so the input type is omitted

### The Question

Why do we need an object calculus at all?

- There is no issue with untyped calculi
  - Object-oriented programs can be encoded in untyped lambda calculus
  - And vice-versa
- The problem is in typed calculi

# Two Features Using Type Recursion

Define A = 
$$[...,l_i: B_i, ...]$$
 i = 1..n

E, 
$$x_i$$
: A  $\vdash$  b<sub>i</sub> : B<sub>i</sub> i = 1..n [Object]  
E  $\vdash$  [..., l<sub>i</sub> =  $\varsigma(x_i)$  b<sub>i</sub>, ...] : A

E 
$$\vdash$$
 a : A  $\vdash$  E, x:A  $\vdash$  b : B<sub>j</sub> [Override]
$$E \vdash a.l_i <= \varsigma(x) \text{ b: A}$$

### What's the Problem?

 When using the lambda calculus with record types, it is difficult to model both the type recursion in object types and the recursion of override simultaneously

#### Because

- Object types depend on the types of fields, which override can change
- Encoding objects in the lambda calculus makes it impossible to treat these separately
  - Need one uniform type system for the lambda calculus that is expressive enough to handle both the encoding of recursive types and the alterations done by override
- This turns out to be difficult and complicated
  - Which makes the resulting type systems difficult to understand and use

# New Stuff

### A Practical Problem

 These issues comes up in all statically typed languages with objectoriented features

- When are an object's methods defined?
- When can override be performed?
- To make both value/object recursion and override work in a statically typed language, these features are often split so that all overrides happen before any computation is done.

# Solution #1: Mainstream Typed OO

- Restrict the definition of methods to a first phase before methods are typed
  - Mechanisms like inheritance, static override, restrictions on modifying superclasses, dynamic update only of fields
  - Guarantees the assembly of the object's type is independent of program evaluation
  - Type checking happens after assembly of the methods and before the program executes

• Examples: C++, Java

# Java Example

```
class Foo{
 public void hello() {
   System.out.println("Hello world!");
class Bar extends Foo {
 public void hello(){
   System.out.println("Hello, user!");
 public void goodbye(){
   System.out.println("Hello, user!");
```

- Class Bar inherits from class Foo
- Inheritance in Java is a static property
  - A class and its parent must be explicitly named
- Method override is completely resolved at compile time
  - Even before type checking!
  - We only need the names of the classes and methods
  - The method in the subclass replaces the overridden method in the parent class
- There are type restrictions
  - A method f must have the same signature as method f in the parent class
  - Just like simply typed object calculus
  - But this can be checked after overriding is resolved

## A More Practical Example

```
abstract class Shape {
  abstract Number calculateArea();
class Triangle extends Shape {
  private final double base;
  private final double height;
  double calculateArea() {
    return (base / 2) * height; }
class Square extends Shape {
  private final double side;
  double calculateArea() {
     return side * side; }
```

- This example shows a more typical use of override
- The base class is abstract, meaning its interface is defined but no implementation is given
- Any method in an abstract base class must have an implementation in any subclass
  - Of course the subclasses can have additional methods and fields, too
- The calculateArea method is overridden in each of the subclasses to give the appropriate implementation for the kind of shape the subclass represents

- C++ has very similar mechanisms for inheritance and override
  - Entirely static

### Solution #2: Functional + OO

- Add object-oriented features to a functional language
  - Add primitive OO features to the lambda calculus
- Let the functional language do most of the work
  - The OO extensions are a thin veneer
  - Record types (or something similar) handles the typing
  - Higher-order functions give other ways to work around OO restrictions
- Every functional language has added an object system
  - Examples: OCaml, Haskell

 Ocaml has a mix of functional, object-oriented and imperative features

- Fundamentally it is a functional language
  - Based on lambda calculus
  - OO features are implemented by translation to lambda calculus
  - Using records and record types
  - Call-by-value

```
let counter =
  object
    val mutable x = 0
    method get = x
    method inc = x <- x + 1
  end;
Type checker: val counter : < get : int, inc : unit >
```

Note that Ocaml is more dynamic that Java and C++
Some new kinds of objects can be computed, not just statically defined
But still statically typed

```
let counter =
  object (s)
  val mutable x = 0
  method get = s#x
  method inc = x <- x + 1
  end;
Type checker: val counter : < get : int, inc : unit >
```

Objects can have a self parameter, but it must be explicitly bound

```
class counter =
  object (s)
  val mutable x = 0
  method get = s#x
  method inc = x <- x + 1
  end;
Type checker: class counter : < get : int, inc : unit >
```

Classes can also be declared at the top level. Unlike immediate objects, classes can be inherited.

```
class counter = ref ...

class counter =
  object (s)
  val mutable x = 0
  method get = s#x
  method inc = x <- x + 1
  method register = pointer <- s
  end;

Type error: Self type cannot escape its class</pre>
```

Self parameters can only be used within the class in which they are bound – the can't "escape" by being stored in global variables, for example, because then standard type checking cannot be guaranteed to give correct results. All other statically typed OO languages (Java, C++, etc.) have the same restrictions on self types.

### Haskell

- A lazy functional language
  - With object-oriented and imperative features that are translated into the functional core
- Haskell takes a different approach to object-oriented features
  - The focus is on general support for overloading

# Overloading: A Digression

- Two kinds of polymorphism are common in programming languages
- Subtyping

Example: if ColorPoint extends Point, then ColorPoint can be used wherever a Point is expected

Parametric polymorphism works for any type

```
Example: cons(a,l): `a -> list `a -> list `a
```

- Overloading is a set of functions with the same name
  - Only works at very specific types
  - Example: A + B
  - A,B could be integers, floats or strings
  - + is overloaded to work at just these three types
  - But three completely different implementations

# Haskell Type Classes

- Type classes are a general method for overloading functions
- Consider: What is the type of the equality function ==?
- If it is overloaded for a fixed set of types (int, bool, float, char) then it is inconvenient that it can't be extended to user-defined types
- A parametric polymorphic definition doesn't make sense
  - ==: `a -> `a -> bool
  - For some types, like function types, there is no sensible definition of ==

## Type Class Example

class Eq a where

Read ``Any type T in the Eq type class must define a function == with signature T -> T -> Bool"

This sounds a lot like an abstract base class!

Really very close to an abstract interface (ala Java)

# Type Class Examples

#### class Eq a where

#### class Num a where

#### instance Eq Int where

#### instance Num Int where

## Type Class Examples

Testing if y is an element of a list:

```
member [] y = False
member (x: xs) y = (x == y) | | member xs y
member : list `a -> `a -> Bool -- the pre-type classes type
```

But member only works if == is defined on the elements of the list With type classes we can enforce this restriction:

```
member :: Eq `a => list `a -> `a -> Bool
```

### Subclasses

#### class Eq where

#### class Eq a => Num a where

"Any instance of the Eq typeclass can also be a member of the Num typeclass if it implements the additional \* and + methods"

Instances can be subclasses of multiple typeclasses

 Again, interfaces in Java, instead of single-inheritance Java classes, are the best analogy

## Summary of Type Classes

- Type classes observe that inheritance/override is a form of overloading
- Unifies traditional ad hoc overloading with OO classes
  - Only two forms of polymorphism, parametric and type classes
  - And they work well together!
  - Compare with the crazy overloading rules in Java and C++
- Cost
  - Very static: Programmer must declare all type classes
  - And explicitly declare which type classes each implementation satisfies

### Solution #3: OO + Functional

Add functional features to an OO language

- Starting from a language with objects and imperative features, add
  - first-class functions
  - parametric polymorphism, if the language is typed
- Every object-oriented language has added first-class functions
  - Examples: Java and C++

### Lambdas in Java

A lambda abstraction in Java is written

```
(arg) -> { function body }
```

- Just like lambda calculus:
  - The function is anonymous (doesn't have a name)
  - Takes a single argument (arg in the scheme above)
- Unlike lambda calculus:
  - The function body can make use of all Java features, include objects and state

### Java Lambda Example

```
-- print out each number in an ArrayList using forEach
numbers.forEach( (n) -> { System.out.println(n); }
-- prints ``Hello?''
mkquestion = (s) -> s + "?";
ask = mkquestion.run(``Hello'')
```

### Parametric Polymorphism in C++

```
template <class T>
 class MyNum {
  private:
   T val;
  public:
    MyNum(T n) : val(n) {}
    T Square() { return val * val; }
};
MyNum<int> MyNum(42);
MyNum<float> MyNum(42.0);
MyNum<Foo> MyNum (Foo); -- type error!
```

- A template parameterizes a block of code on a type
  - Doesn't have to be a class, but often is
- Type checking is done by instantiating the template and then type checking the body with the instance types substituted for the type parameters of the template

# Solution #4: Dynamically Typed

- Give up on static typing
  - Go with the simplicity of dynamically typed languages
- Noticeably more popular in the OO world
  - Because static typing ends up being more complex
- Examples: Python, Javascript
  - These systems are more reminiscent of the untyped object calculus

# Python Classes

```
class Dog:
    def bark(self):
        print("Woof!");

rover = Dog()

rover.bark()

Classes in Python have
    attributes (not shown)
    methods

All pretty conventional!

But not type checking ...
```

### Prototypes

- Prototype-based object systems are found only in dynamically typed languages
- A prototype is a concrete object --- not a class
- In a prototype system, new objects are created by copying a prototype
  - That's all!
  - New subtypes are defined by creating new prototypes that add behavior to a base prototype object

## Javascript Example

```
function Cat(name) {
                                          A = Cat("Sleepy");
 this.name = name;
                                          B = Dog("Grumpy");
                       print(`meow!') }; }
 this.sound = function() {
                                          A.sound();
                                          Meow
function Dog(name) {
 this.name = name;
                                          B.sound();
  this.sound = function() { print(`woof!') }; }
                                          Woof
                                          A. proto = B. proto
                                          A.sound()
                                          Woof
```

# Javascript Example

```
function Cat(name) {
                                             A = Cat("Sleepy");
 this.name = name;
                                             B = Dog("Grumpy");
 this.sound = function() {
                       print(`meow!') }; }
                                             -- Add a new property for cat
function Dog(name) {
                                             A.prototype.fur = "Black";
  this.name = name;
  this.sound = function() { print(`woof!') }; }
                                             -- change the prototype for cats
                                             A.prototype = B.prototype
                                             A.sound()
                                             Woof
```

## Prototypes, Continued

- In a prototype object system, every object has a prototype
- Objects inherit from other objects
  - With null being the initial prototype
  - Any referenced property is searched for in this *prototype chain*
- Since prototypes are implemented by objects, it is possible to
  - Add new properties, both fields and methods
  - Even replace the prototype with a new one
  - All dynamically
- Python has classes and added a prototype system
- Javascript has prototypes and added classes
- Since the languages are very dynamic, possible to implement any object system one wants
  - Classes and prototypes are the popular ones

### Summary

- There has been a convergence of language features over the last decade
  - Mainstream languages have OO, functional, and imperative features
- There is no one best way to combine OO and functional features
  - Common cases all work in all languages
  - But there are different restrictions depending on whether the starting point is a functional language or an object-oriented language
  - Biggest divide is typed vs. untyped