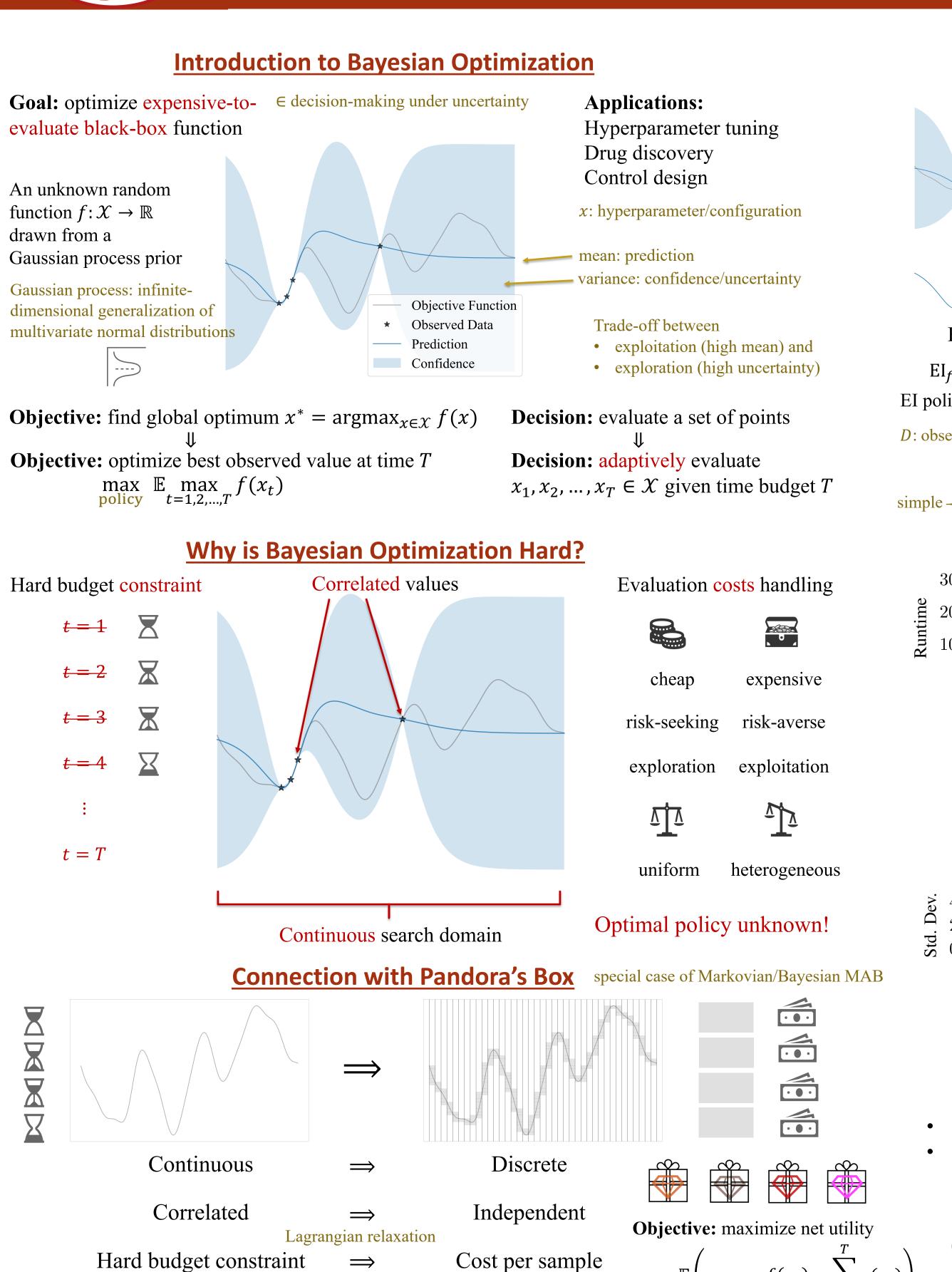


Cost-aware Bayesian Optimization via the Pandora's Box Gittins Index

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extension of [Aminian et al.'24]

How to translate?

Is Gittins index good?

← Optimal policy: Gittins index

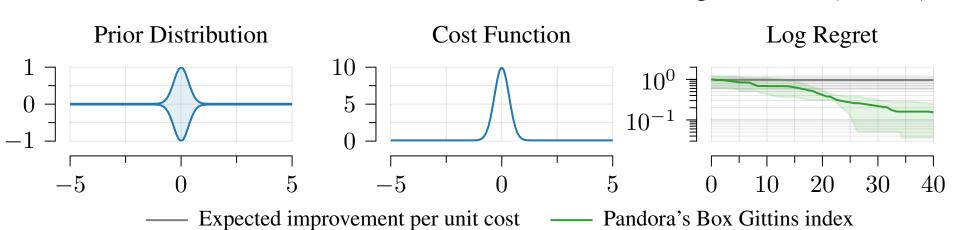
[Weitzman'79]

T: random stopping time

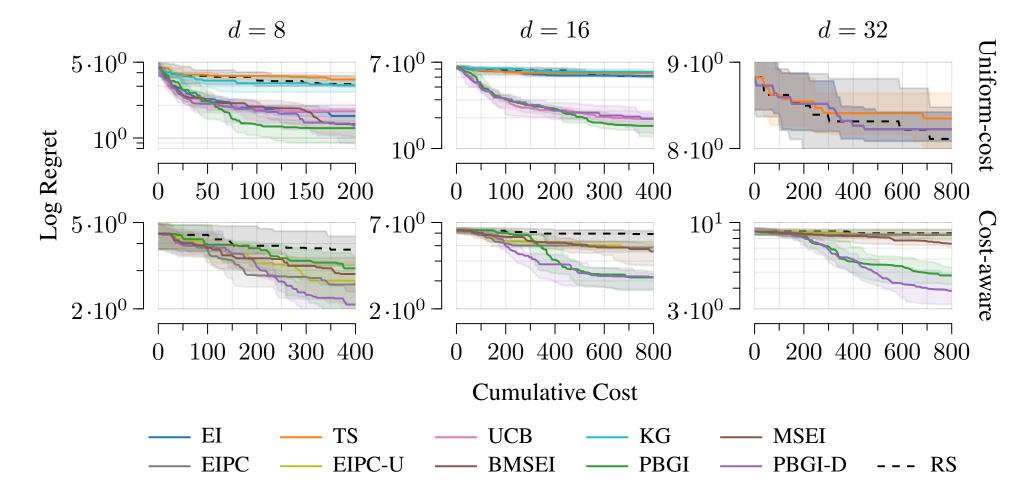
Acquisition Functions Pandora's Box Gittins Index (PBGI) Expected Improvement (EI) g(x): solution to $\mathrm{EI}_{f|D}(x;g(x)) = \lambda^{-1}$ $\operatorname{EI}_{f|D}(x;y) = \mathbb{E}[((f|D)(x) - y)^{+}]$ EI policy: evaluate $\operatorname{argmax}_{x} \operatorname{EI}_{f|D}(x; y_{\text{best}})$ PBGI policy: evaluate $argmax_x g(x)$ λ: cost-per-sample (Lagrange multiplier) D: observed data, y_{best} : current best observed value • Predictive Entropy Search unreliable Other acquisition functions: • Knowledge Gradient (KG) • Upper Confidence Bound (UCB) • Multi-step Lookahead EI (MSEI) • Thompson Sampling (TS) d = 8d = 161,200 **E** 100 0 10 20 30 40 0 20 40 60 80 0 40 80 120 160 **Cumulative Cost** — EI — TS — KG — MSEI PBGI is easy to compute using bisection method! Contour Plot Impact of λ PBGI Expected **PBGI** Log Regret Improvement $\lambda = 10^0$ $\lambda = 10^{-5}$ $- \lambda = 0.001$ $--- \lambda = 0.0001$ $--- \lambda = 0.00001$ 0 50 100 150 200 --- Dynamic λ -3 0**Cumulative Cost** Mean Connection with UCB? Smaller λ , higher exploration **Heterogeneous Costs Baselines:** arbitrarily bad • Given cost function $c: \mathcal{X} \to \mathbb{R}^+$ and budget B

- Replace λ with $\lambda c(x)$ to compute g(x) as PBGI

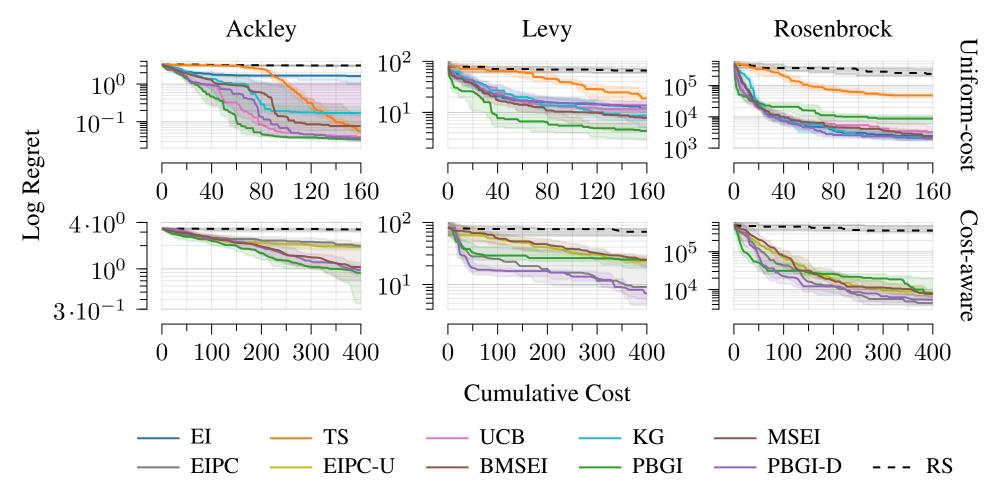
• EI Per Unit Cost (EIPC) • Budgeted MSEI (BMSEI) slow Log Regret



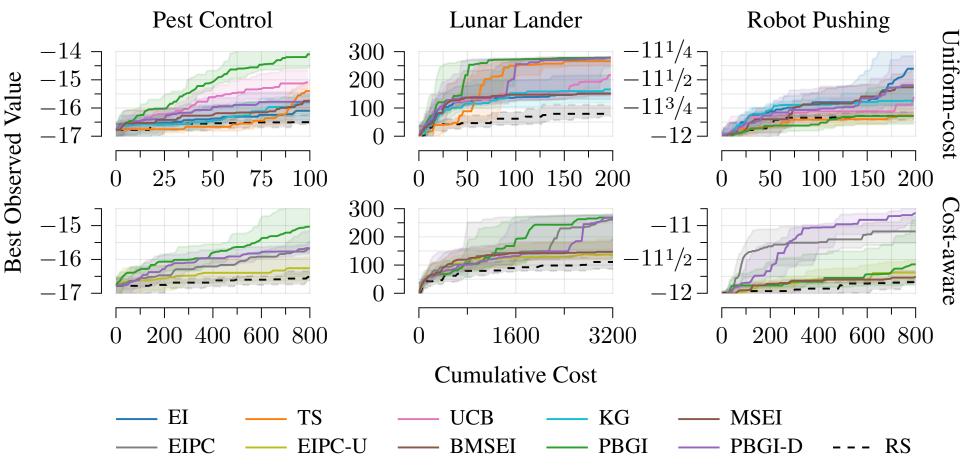
Experiment: Bayesian Regret



Experiment: Synthetic Benchmarks



Experiment: Empirical



Future Work

Extension to complex BO (freeze-thaw, multi-fidelity, function network, etc.) via Gittins variants ("golf" Markovian MAB, optional inspection, etc.)