

Gittins Indices for Bayesian Optimization: Insights from Pandora's Box

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Joint work with Raul Astudillo, Peter Frazier, Ziv Scully, and Alexander Terenin

ECGI'24

Bayesian Optimization

Goal: optimize expensive-to-evaluate black-box function

∈ decision-making under uncertainty

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Applications:

Hyperparameter tuning

Drug discovery

Control design

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∈ decision-making under uncertainty

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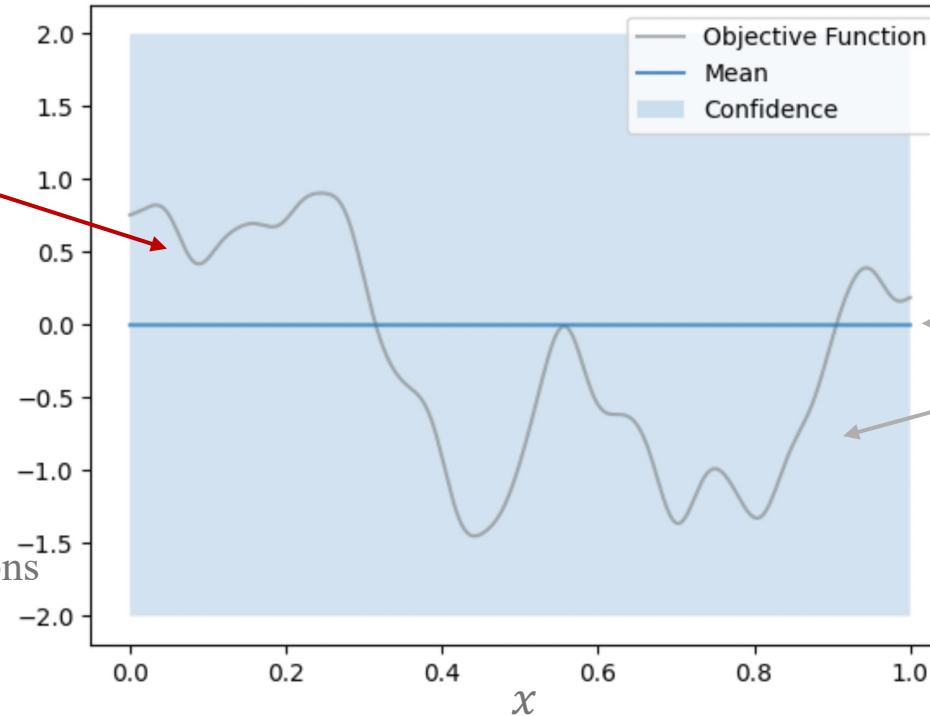
Control design

Bayesian Optimization

Goal: optimize expensive-to-evaluate **black-box** function

An **unknown random** function $f: \mathcal{X} \rightarrow \mathbb{R}$ drawn from a Gaussian process prior

Gaussian process: infinite-dimensional generalization of multivariate normal distributions



Applications:

Hyperparameter tuning
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x : hyperparameter/configuration

mean: prediction

variance: confidence/uncertainty

Bayesian Optimization

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Gaussian process: infinite-dimensional generalization of multivariate normal distributions

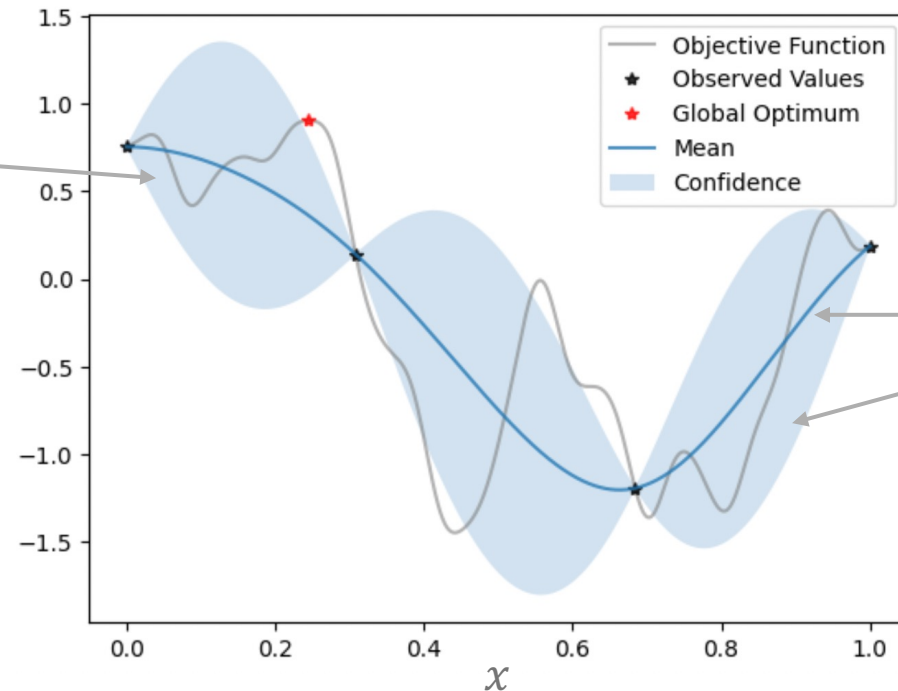
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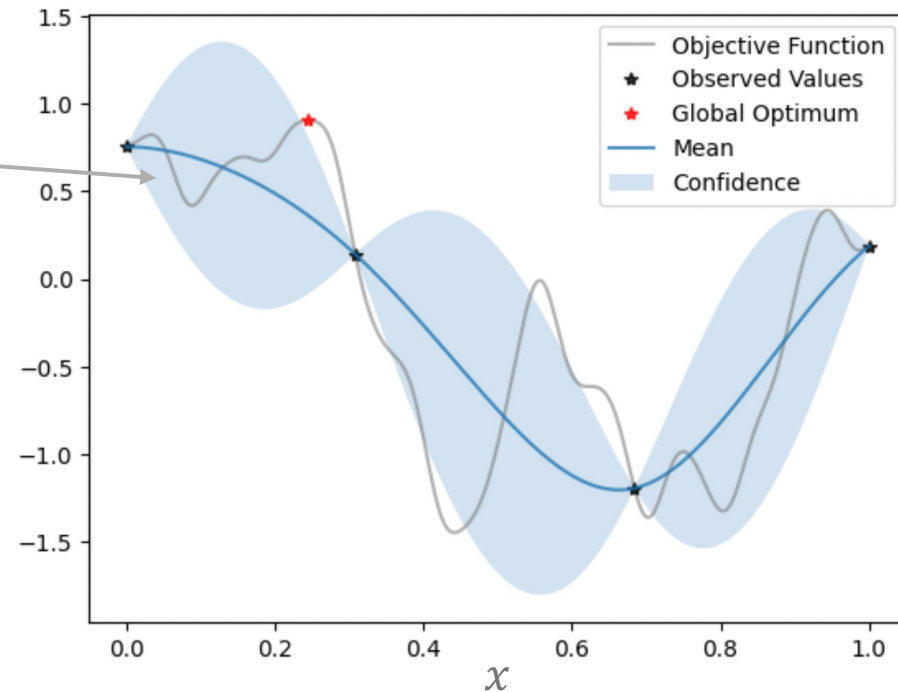
Objective: find global optimum $x^* = \operatorname{argmax}_{x \in \mathcal{X}} f(x)$

Decision: evaluate a set of points

Bayesian Optimization

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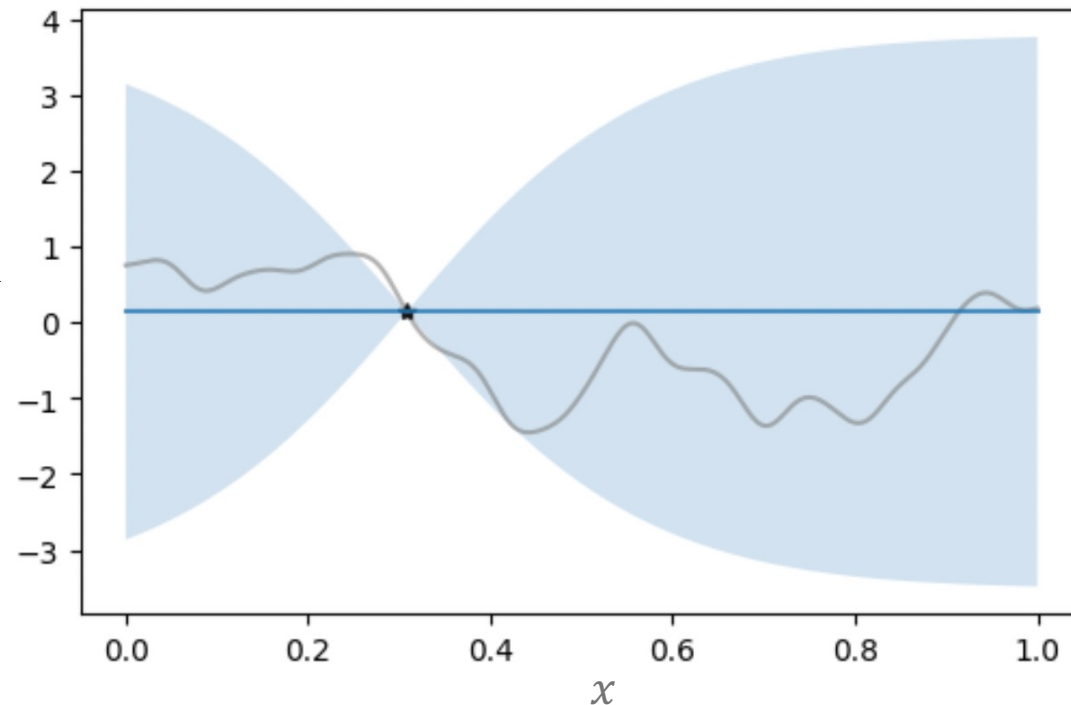
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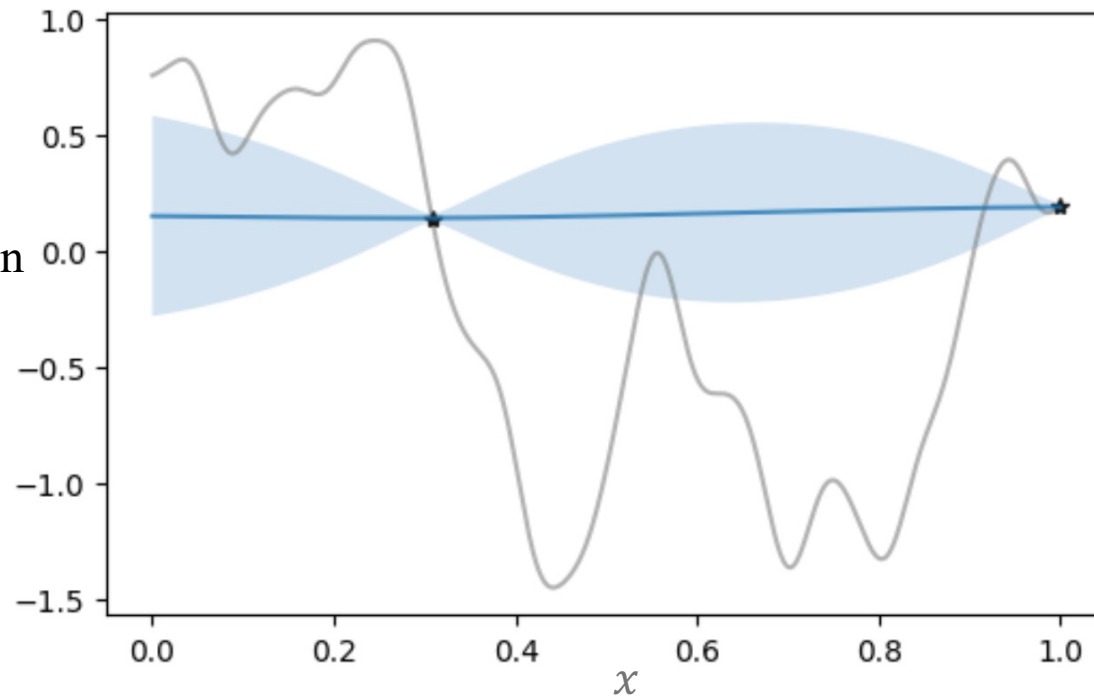
adaptively

Decision: evaluate a set of points

Bayesian Optimization

Goal: optimize **expensive-to-evaluate** black-box function

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Applications:

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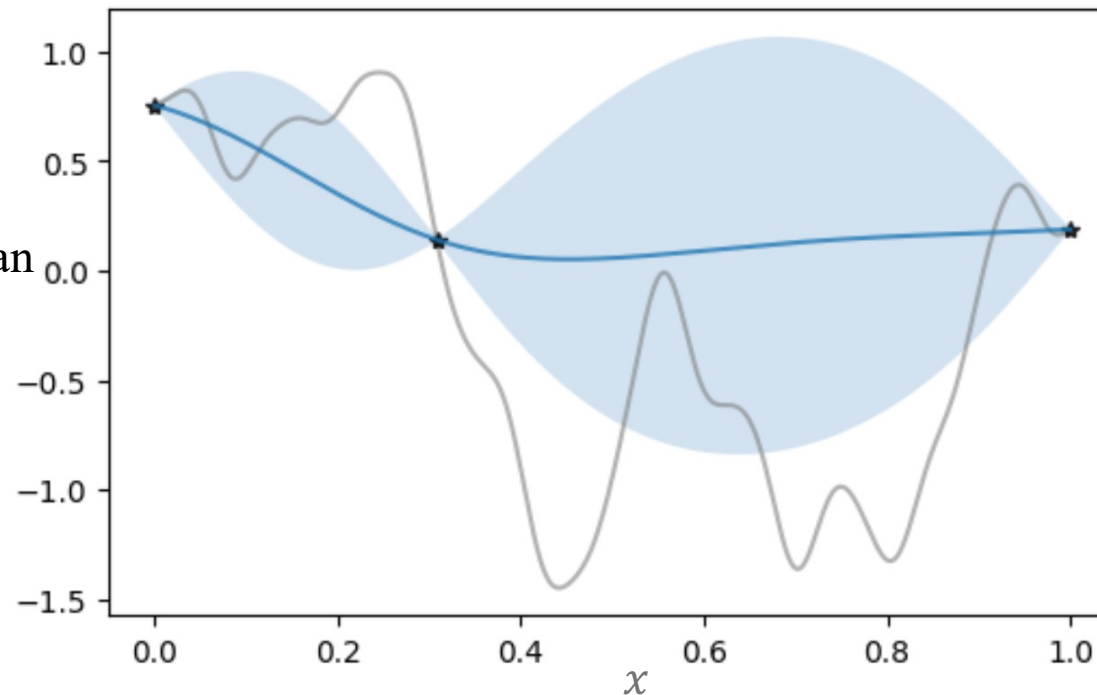
x : hyperparameter/configuration

Decision: evaluate a set of points **adaptively**

Bayesian Optimization

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x : hyperparameter/configuration

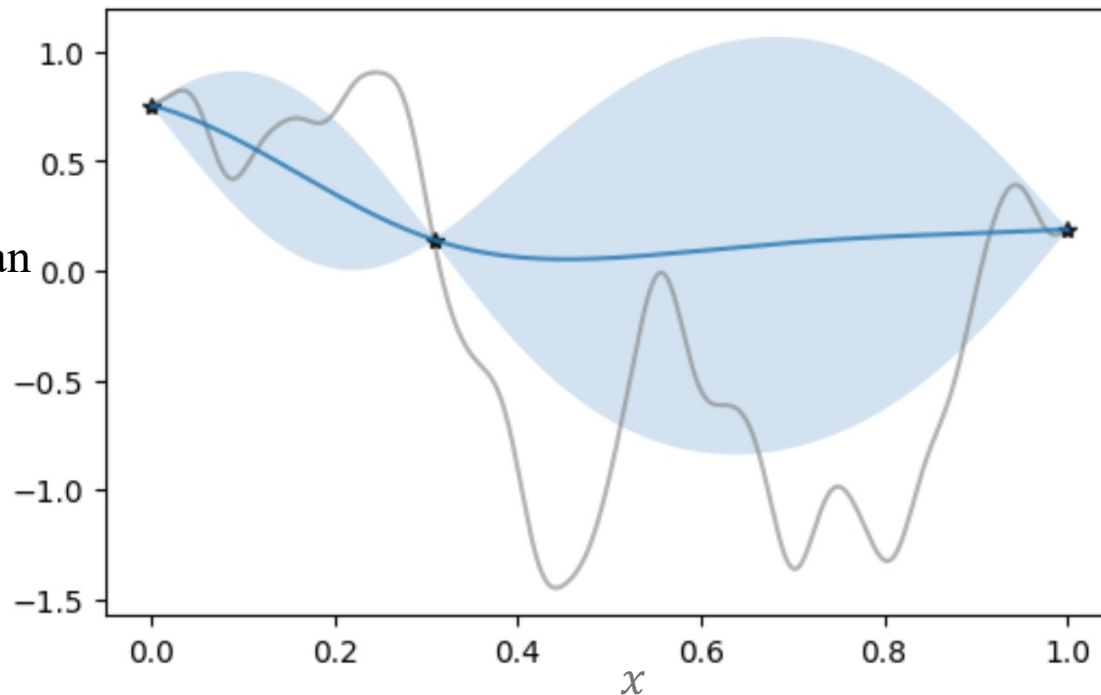
adaptively

Decision: evaluate a set of points

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Applications:

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x : hyperparameter/configuration

Decision: **adaptively** evaluate a set of points

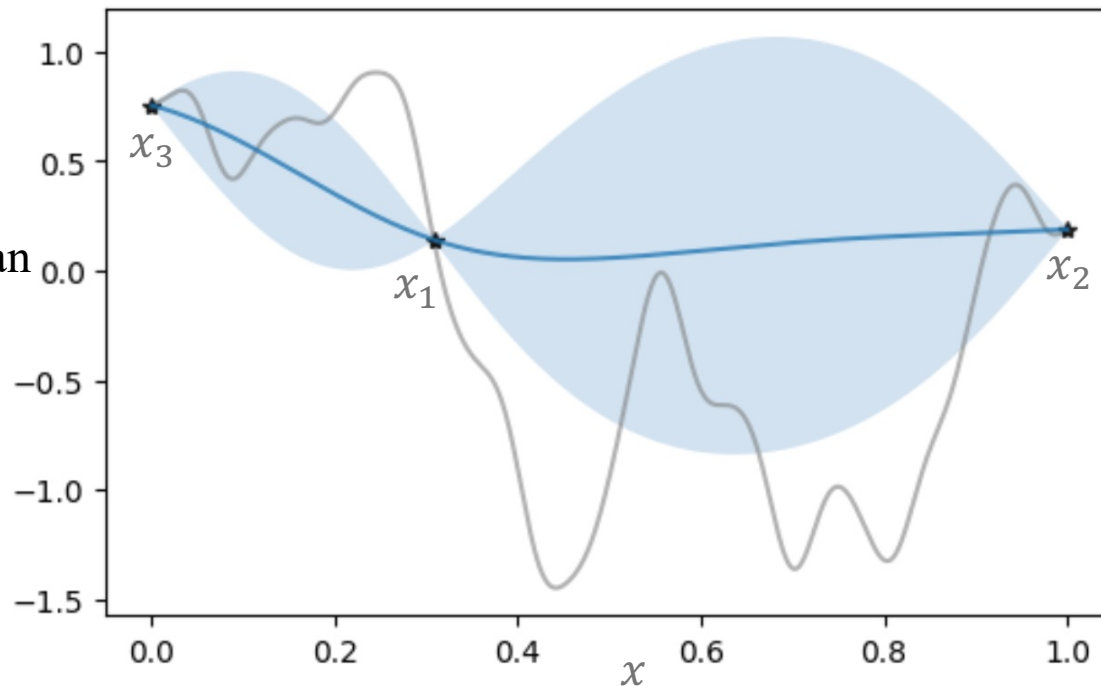
$x_1, x_2, \dots, x_T \in \mathcal{X}$

T : time budget

Bayesian Optimization

Goal: optimize **expensive-to-evaluate** black-box function

An unknown random function $f: \mathcal{X} \rightarrow \mathbb{R}$ drawn from a Gaussian process prior



Applications:

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x : hyperparameter/configuration

Objective: optimize best observed value at time T

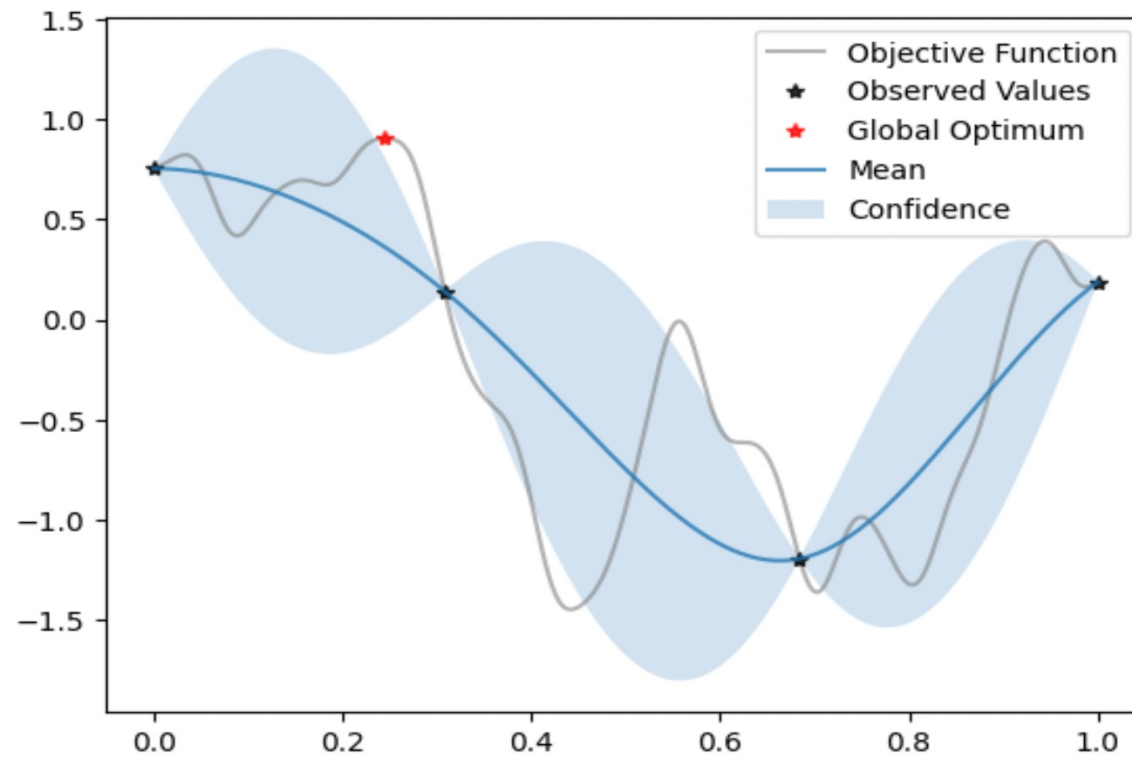
Decision: **adaptively** evaluate a set of points

$$\sup_{\text{policy}} \mathbb{E} \max_{t=1,2,\dots,T} f(x_t)$$

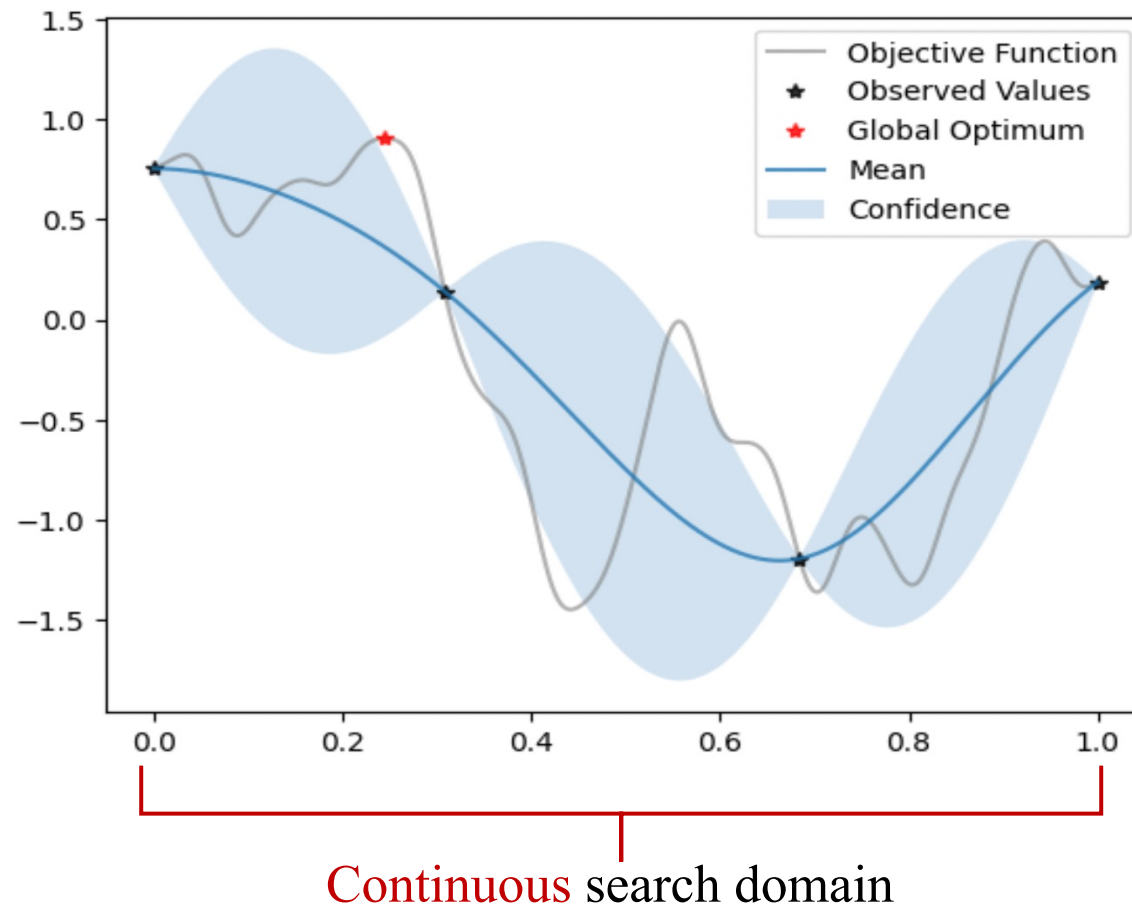
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T : time budget

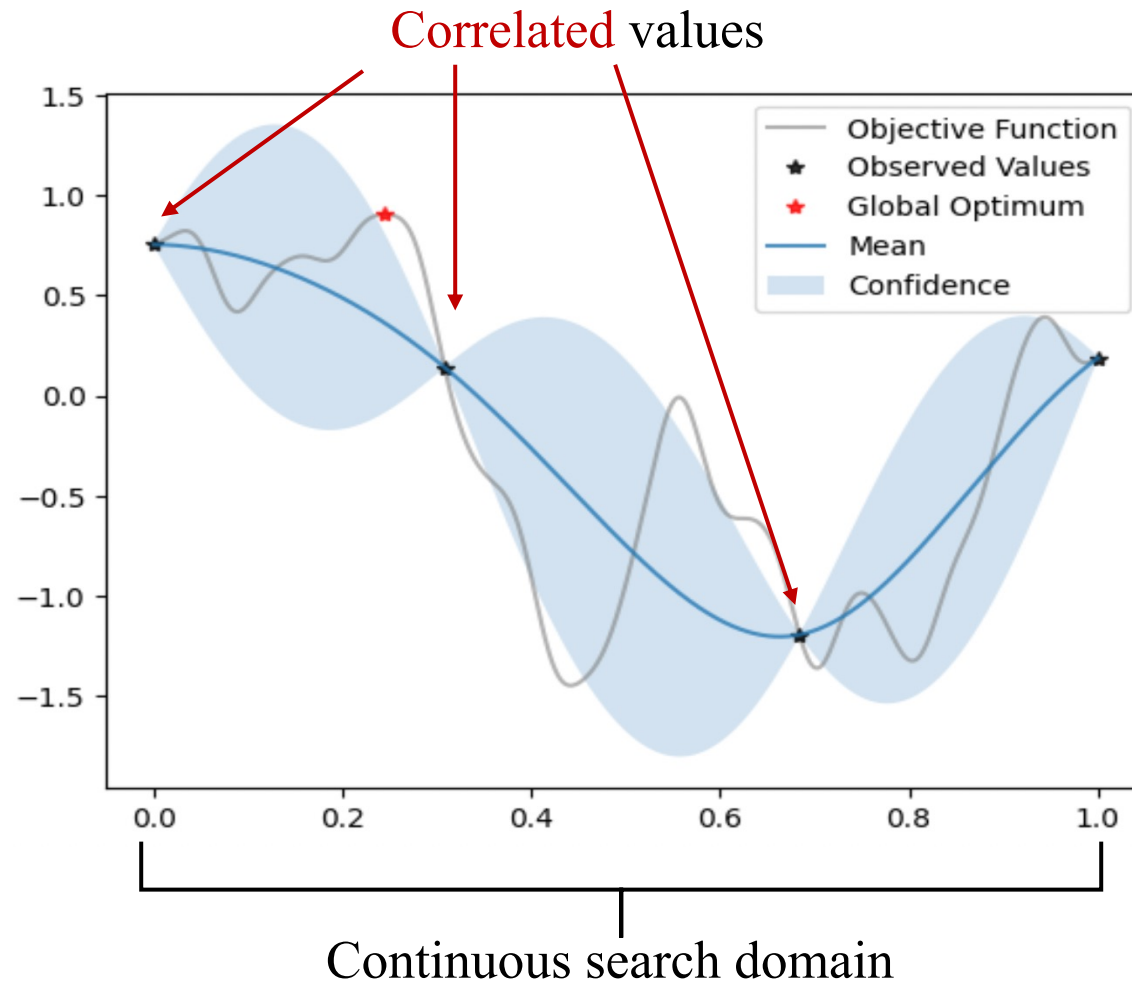
Why is it hard?



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Why is it hard?

Hard budget **constraint**

~~$t=1$~~



~~$t=2$~~



~~$t=3$~~

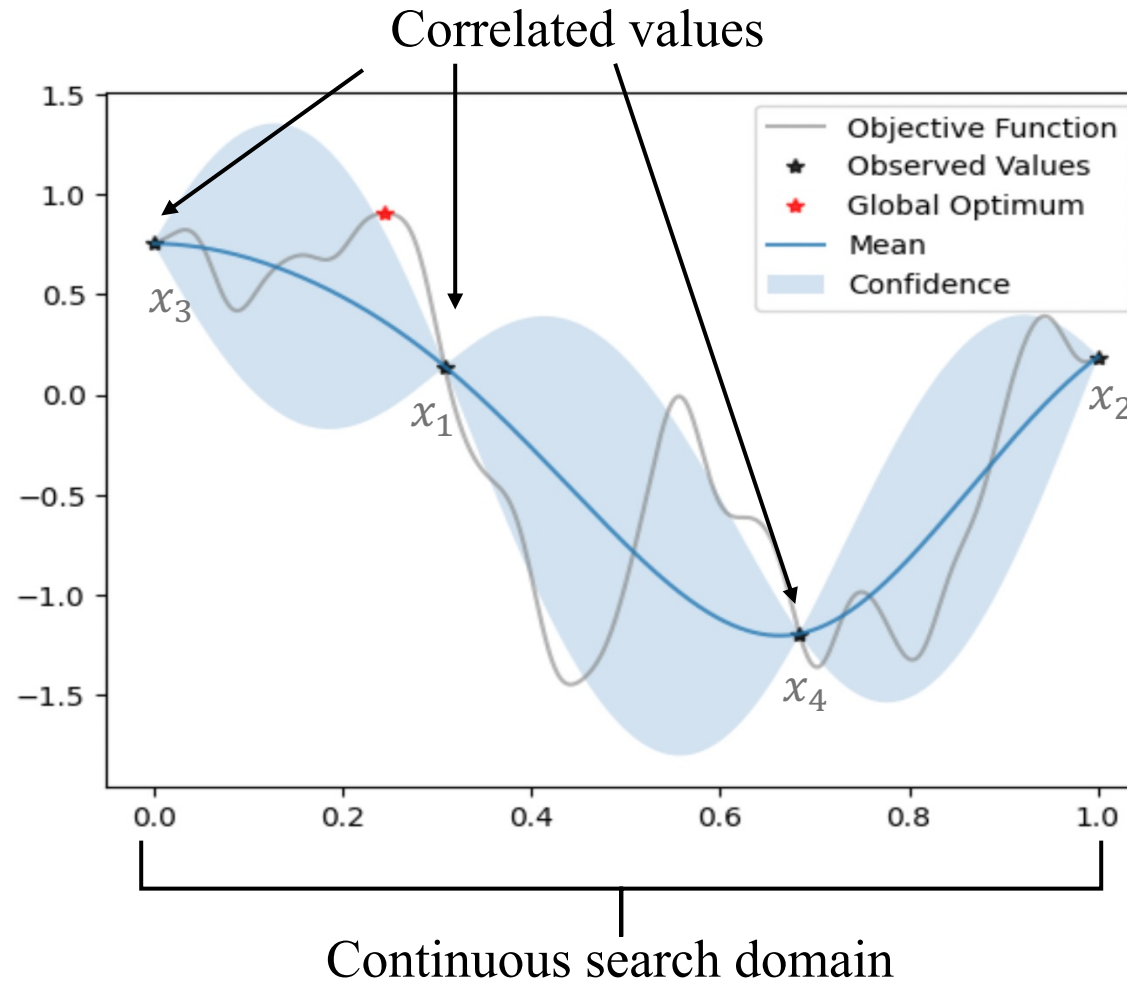


~~$t=4$~~







\vdots

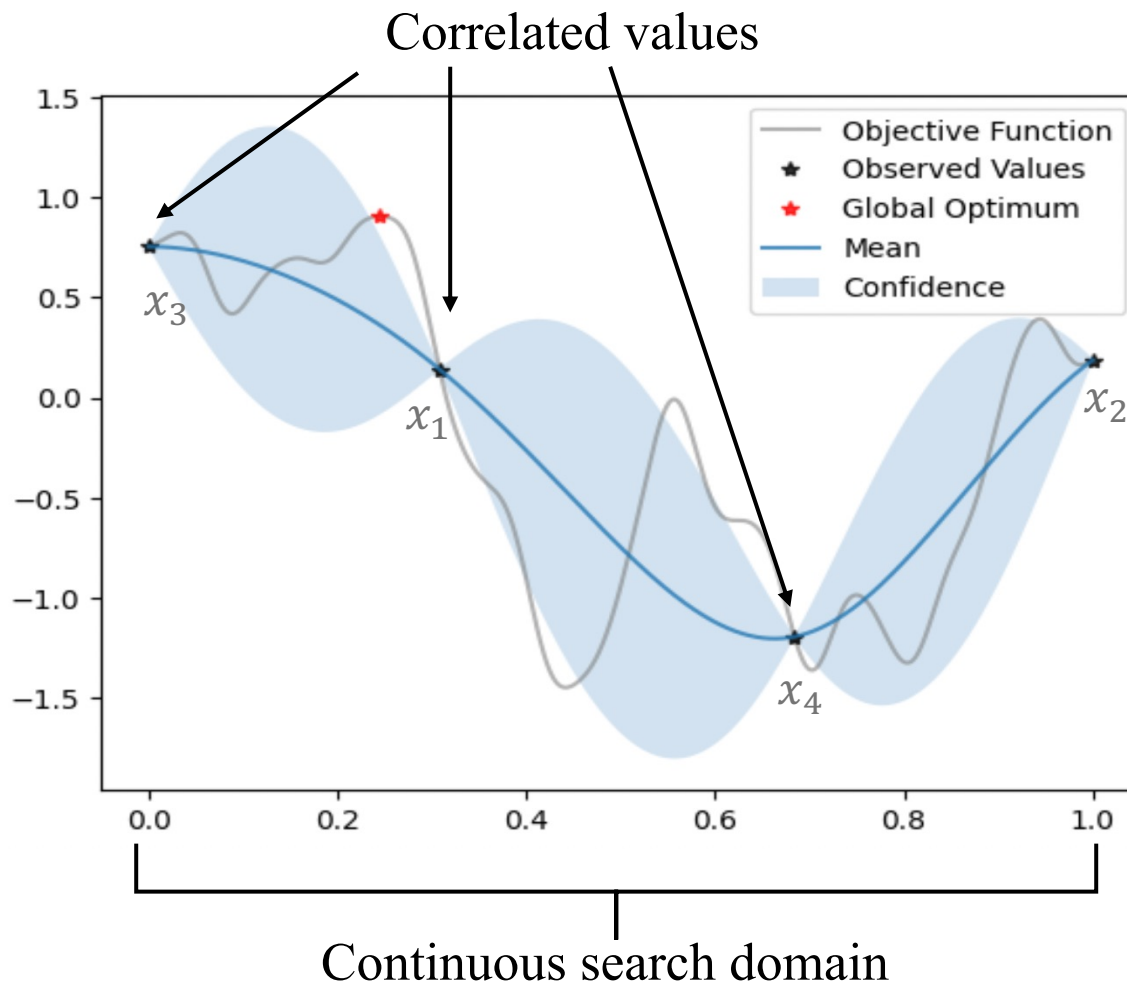
$t = T$



Why is it hard?

Hard budget constraint

$t=1$ 
 $t=2$ 
 $t=3$ 
 $t=4$ 
 \vdots
 $t=T$



Evaluation **costs** handling



cheap

risk-seeking

exploration







expensive

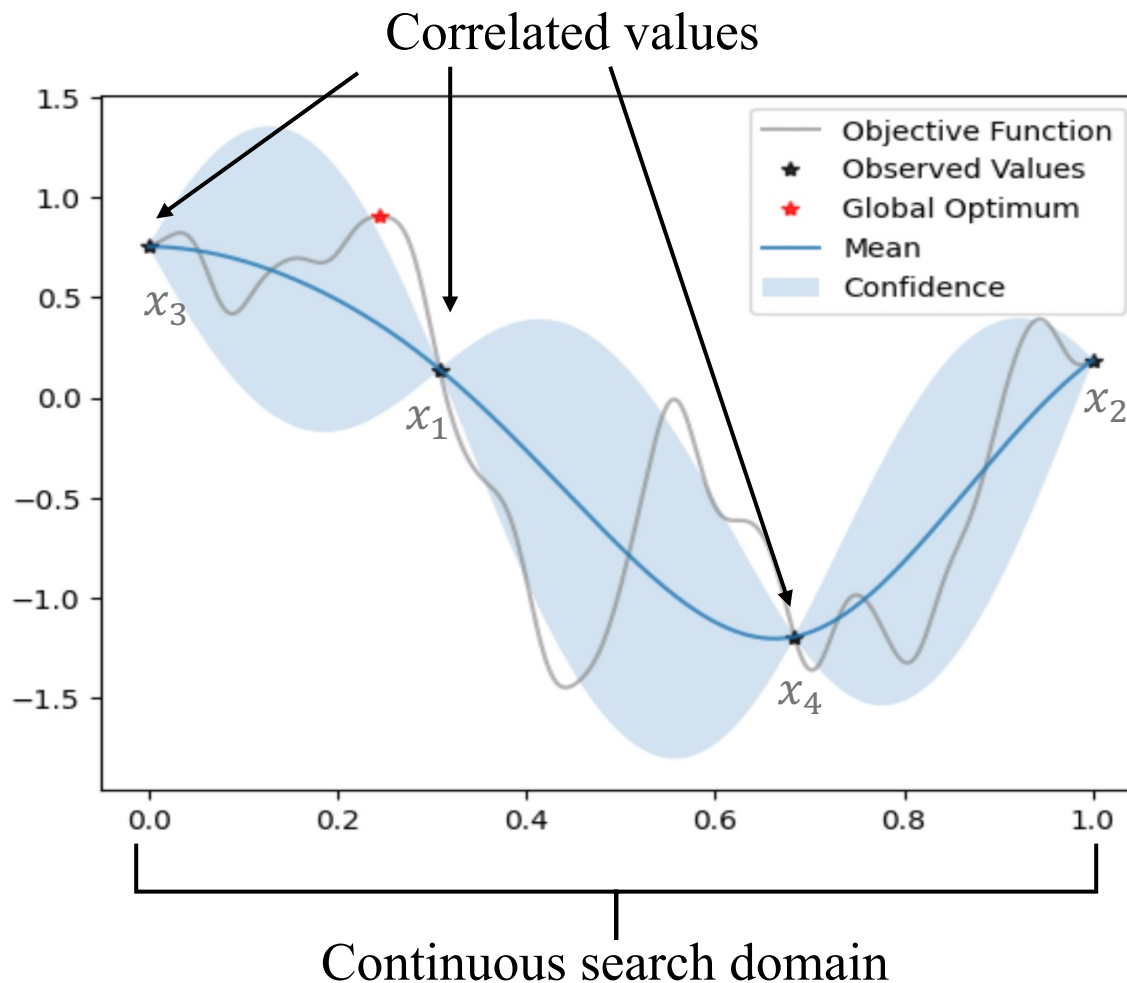
risk-averse

exploitation

Why is it hard?

Hard budget constraint

$t=1$ 
 $t=2$ 
 $t=3$ 
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 $t=T$



Evaluation **costs** handling



cheap

risk-seeking

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uniform



expensive

risk-averse





exploitation

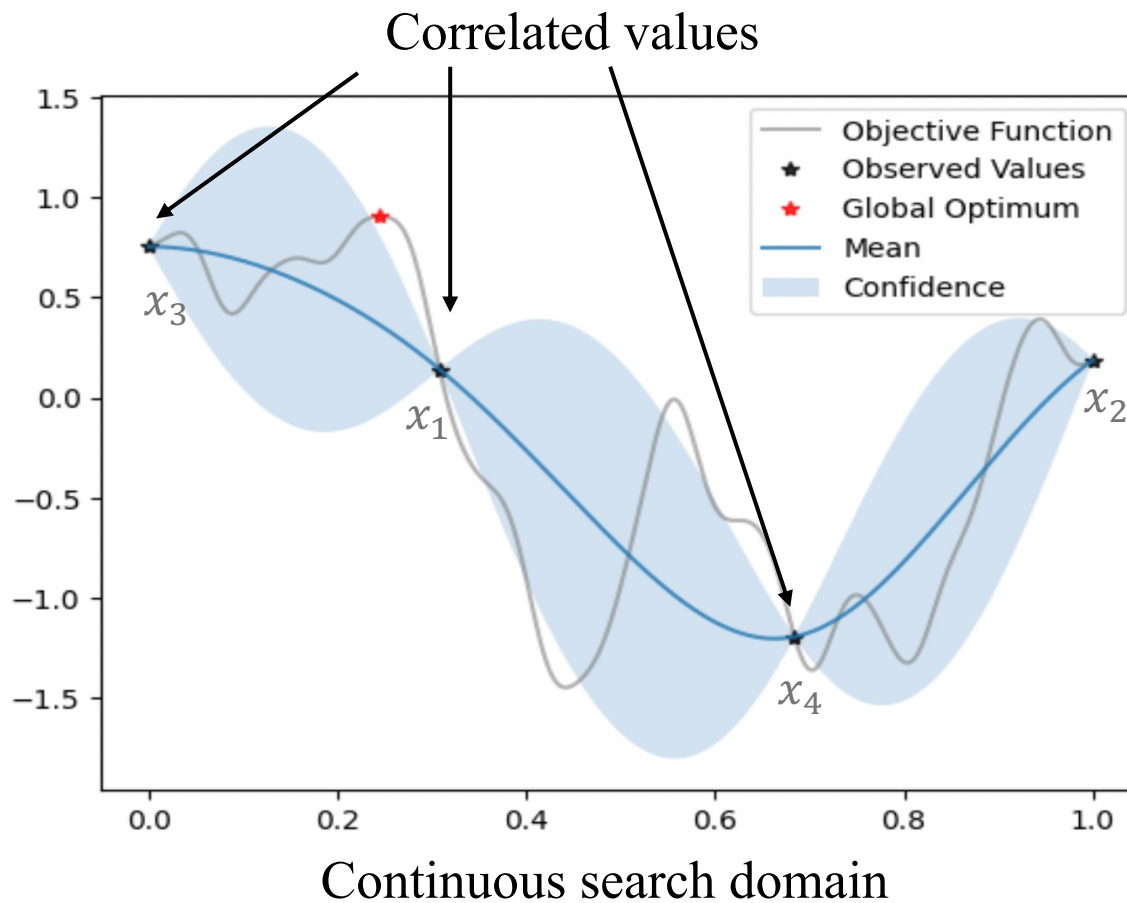


heterogeneous

Why is it hard?

Hard budget constraint

$t=1$ 
 $t=2$ 
 $t=3$ 
 $t=4$ 
 \vdots
 $t=T$



Evaluation costs handling



cheap

risk-seeking

exploration



uniform



expensive

risk-averse

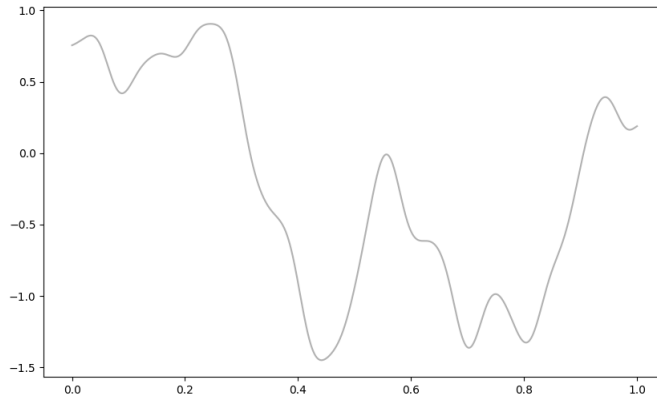
exploitation



heterogeneous

⇒ Optimal policy unknown!

Bayesian Optimization

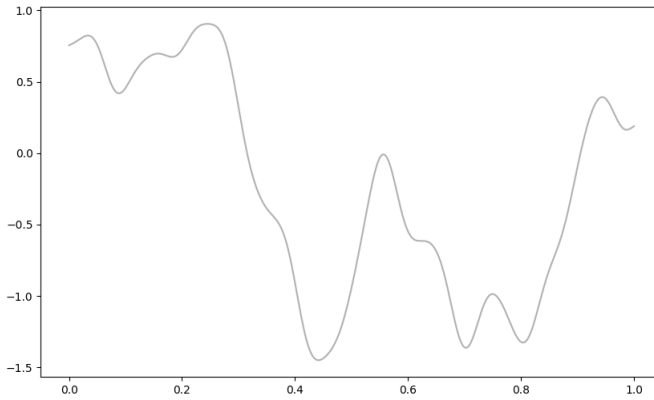


Continuous

Correlated

Hard budget constraint

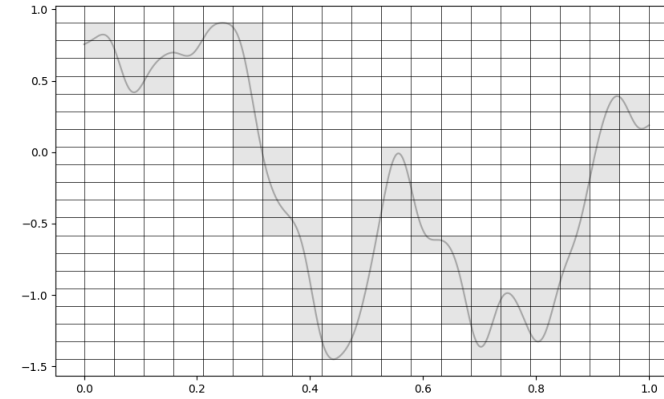
Bayesian Optimization



Continuous

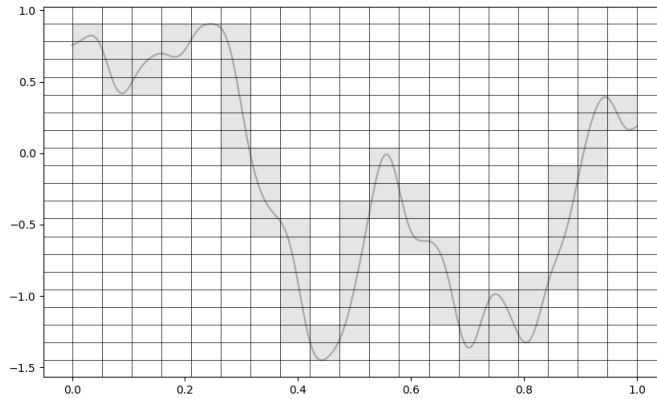
Correlated

Hard budget constraint



Discrete

Bayesian Optimization



Continuous

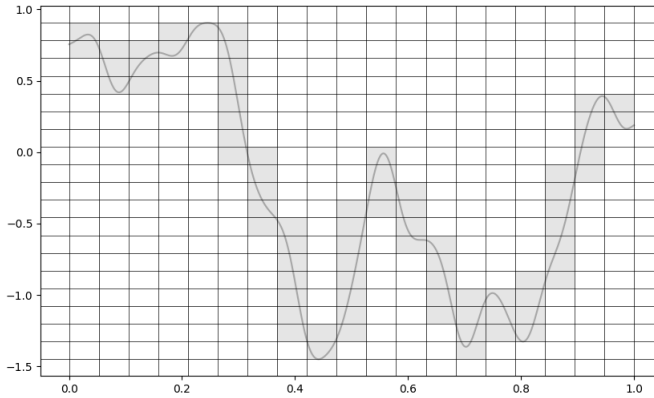


Discrete

Correlated

Hard budget constraint

Bayesian Optimization



Continuous



Discrete

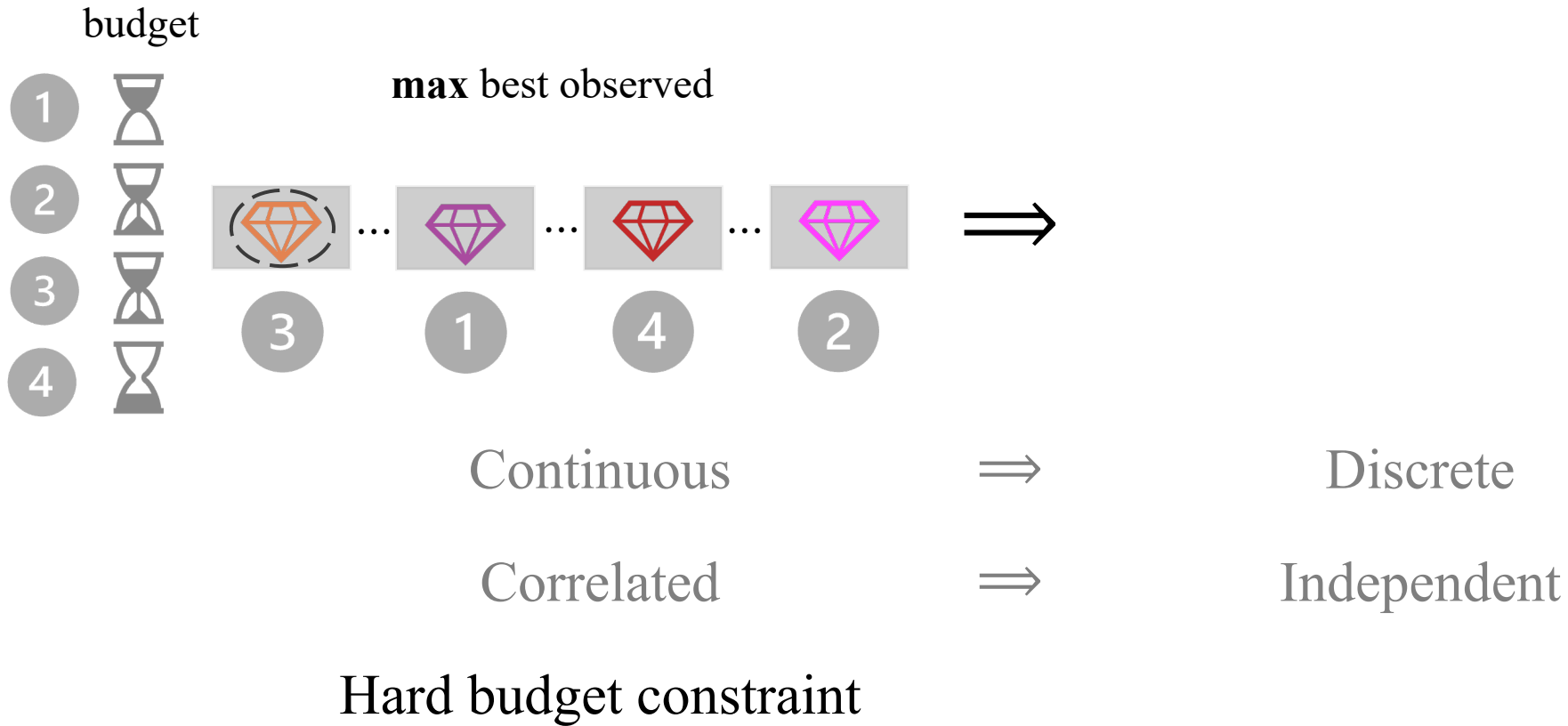
Correlated



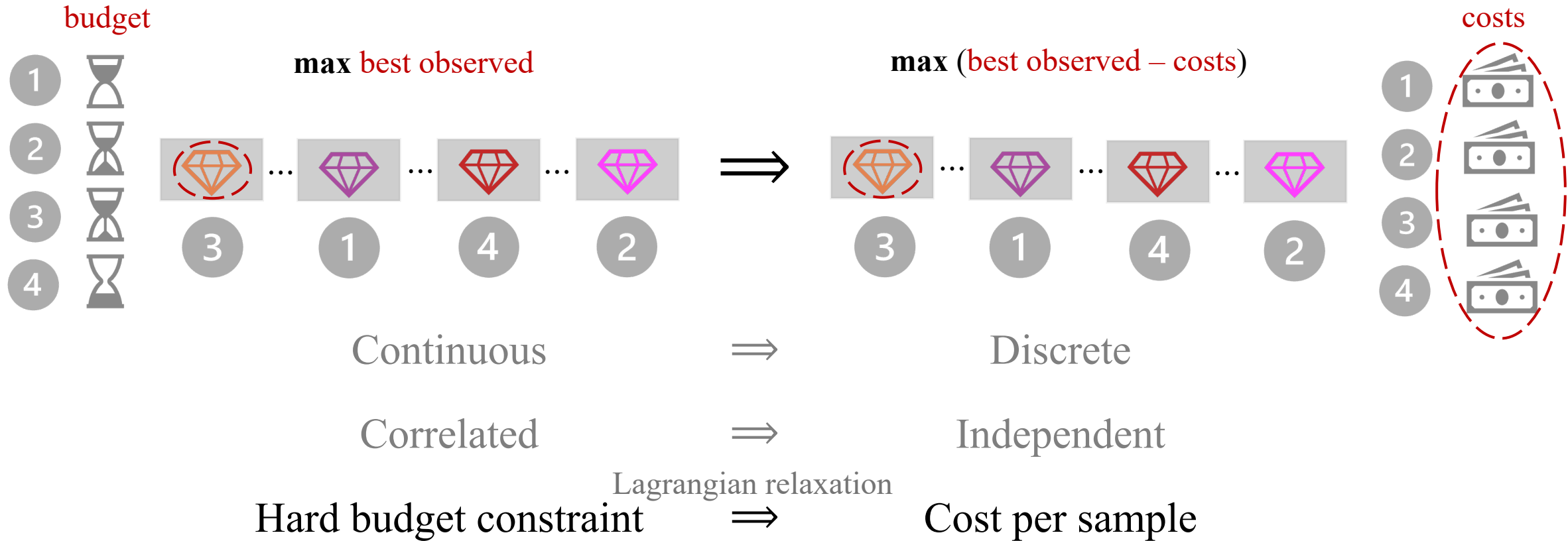
Independent

Hard budget constraint

Bayesian Optimization

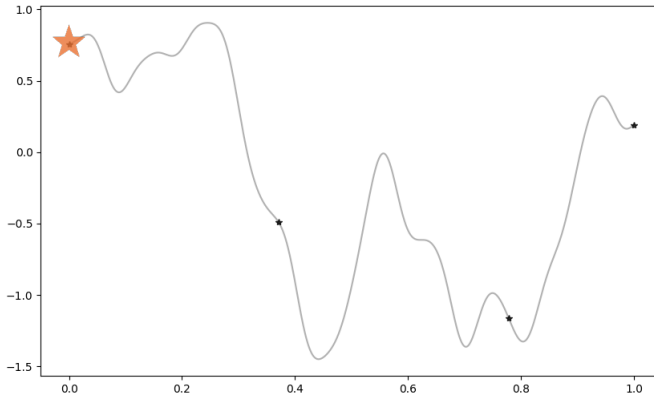


Bayesian Optimization

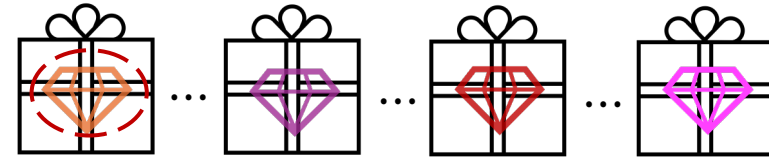


Bayesian Optimization \Rightarrow Pandora's Box

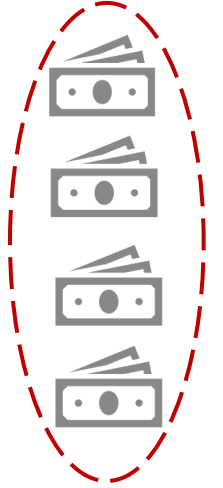
[Weitzman'79]



Continuous



Discrete



Correlated



Independent

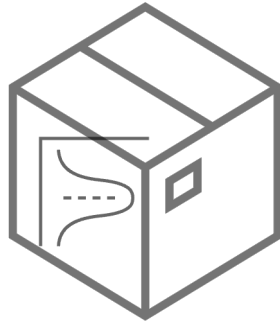
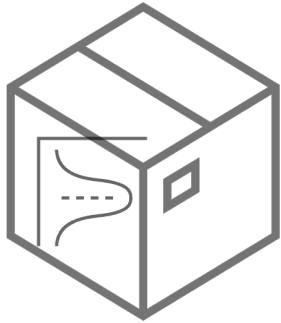
Hard budget constraint



Cost per sample

Pandora's Box

$t = 0$

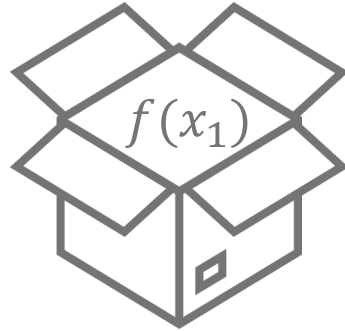
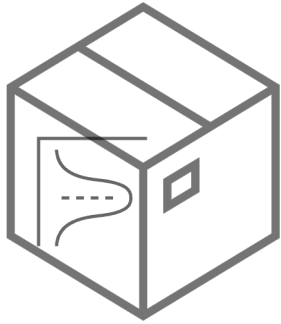


Objective: maximize net utility

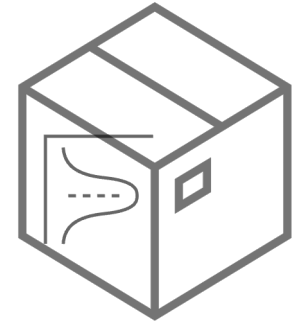
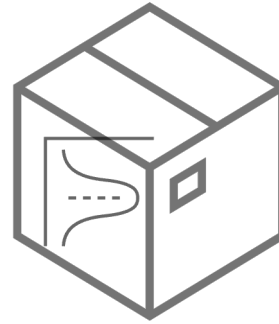
Decision: adaptively evaluate a set of points

Pandora's Box

$t = 1$



$c(x_1)$

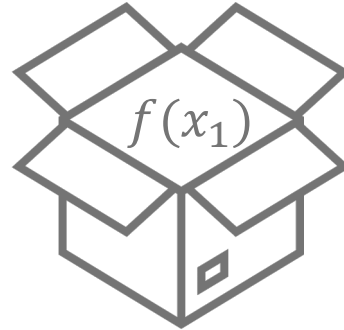
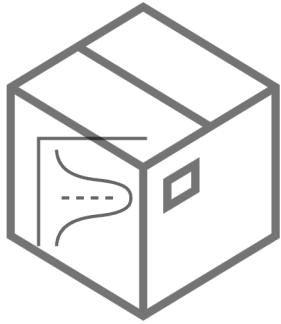


Objective: maximize net utility

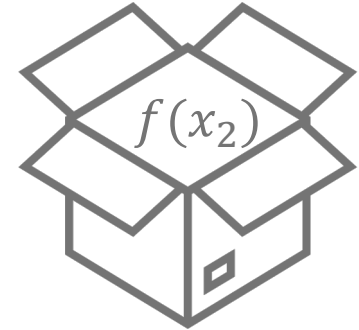
Decision: adaptively evaluate a set of points

Pandora's Box

$t = 2$



$c(x_1)$



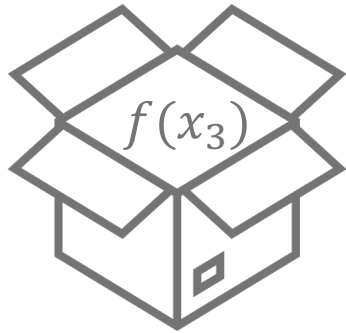
$c(x_2)$

Objective: maximize net utility

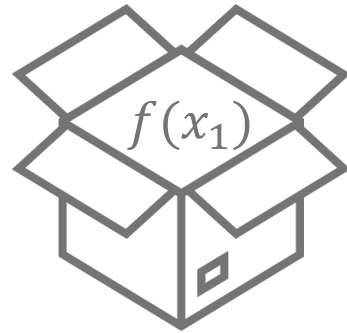
Decision: adaptively evaluate a set of points

Pandora's Box

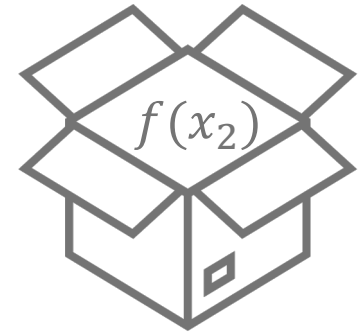
$t = 3$



$c(x_3)$



$c(x_1)$



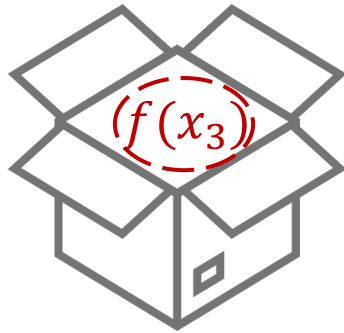
$c(x_2)$

Objective: maximize net utility

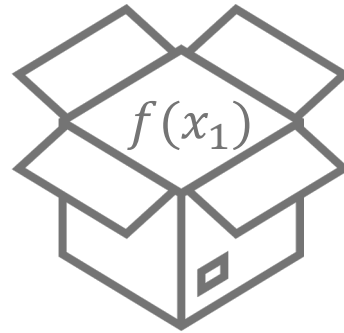
Decision: adaptively evaluate a set of points

Pandora's Box

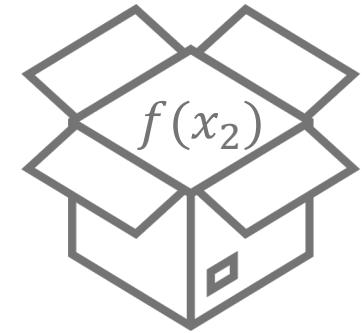
$t = 3$



$c(x_3)$



$c(x_1)$



$c(x_2)$

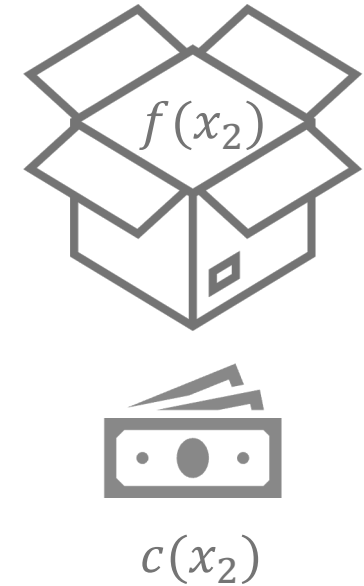
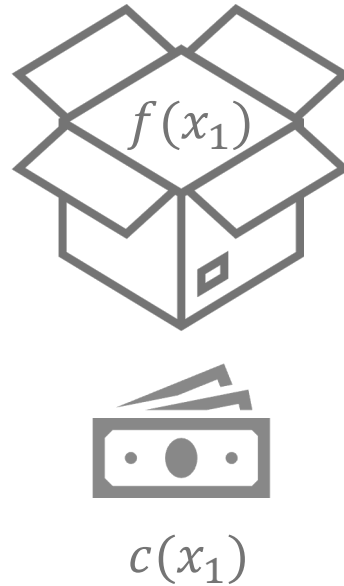
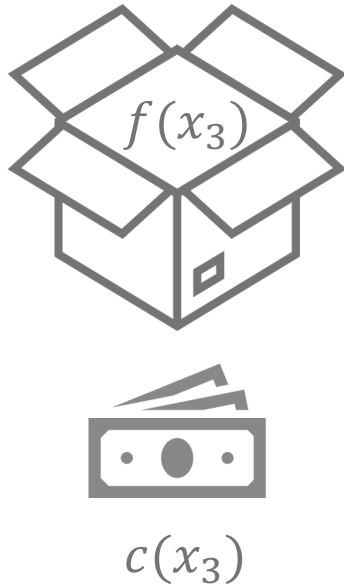
Objective: maximize **net utility**

Decision: adaptively evaluate a set of points

max (best observed value – total costs)

Pandora's Box

$t = 3$



Objective: maximize **net utility**

$$\sup_{\text{policy}} \mathbb{E} \left(\max_{t=1,2,\dots,T} f(x_t) - \sum_{t=1}^T c(x_t) \right)$$

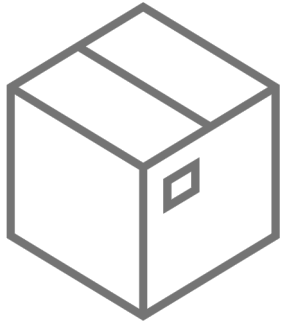
Decision: adaptively evaluate a set of points

$$x_1, x_2, \dots, x_T \in \mathcal{X}$$

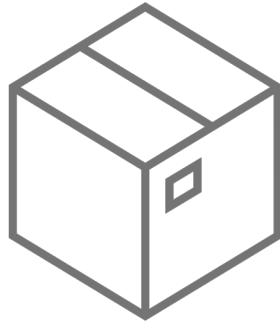
\mathcal{X} : discrete

T : random stopping time

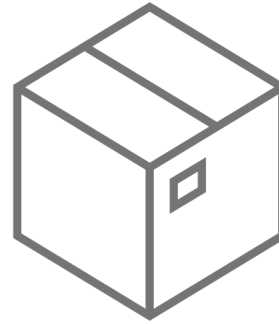
Greedy policy can fail [Singla'18]



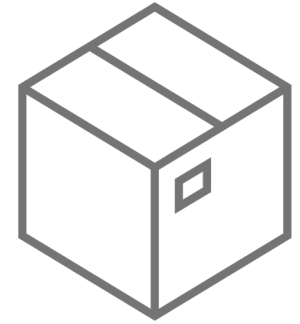
$$\begin{aligned} f(1) &= 200 \text{ w.p. } 1 \\ c(1) &= 198 \end{aligned}$$



...



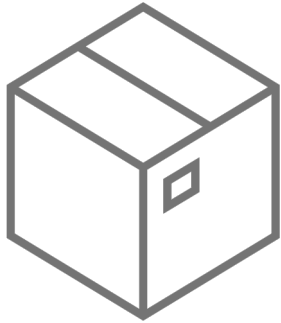
...



$$f(x) = \begin{cases} 200 & \text{w.p. } 0.01 \\ 0 & \text{otherwise} \end{cases}, c(x) = 1, x \in \{2, 3, \dots, 1000\}$$

Greedy policy can fail [Singla'18]

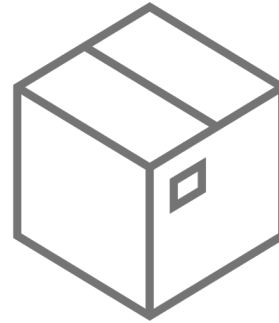
Greedy policy



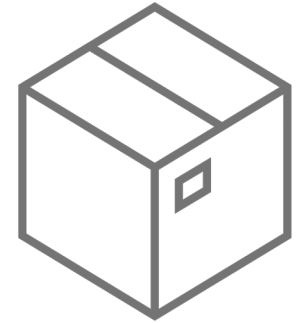
$$\begin{aligned} f(1) &= 200 \text{ w.p. } 1 \\ c(1) &= 198 \end{aligned}$$



...



...



$$f(x) = \begin{cases} 200 & \text{w.p. } 0.01 \\ 0 & \text{otherwise} \end{cases}, c(x) = 1, x \in \{2, 3, \dots, 1000\}$$

Inspection rule: $\operatorname{argmax}_x (\operatorname{El}_f(x; y_{\text{best}}) - c(x))$ **Stopping rule:** $\operatorname{El}_f(x; y_{\text{best}}) \leq c(x), \forall x \in \mathcal{X}$
expected improvement - cost expected improvement \leq cost

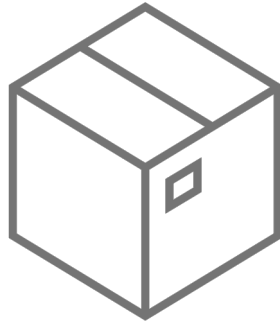
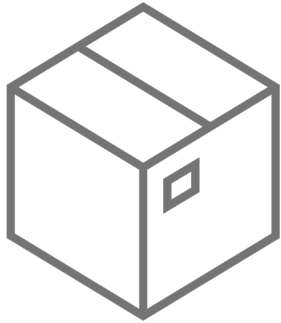
y_{best} : current best observed value

$$\operatorname{El}_f(x; y) = \mathbb{E}[(f(x) - y)^+]$$

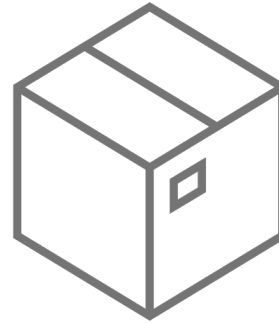
Greedy policy can fail [Singla'18]

$t = 0$

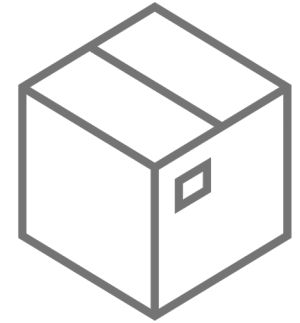
$y_{\text{best}} = 0$



...



...



$$\begin{aligned} f(1) &= 200 \text{ w.p. } 1 \\ c(1) &= 198 \end{aligned}$$

$$\begin{aligned} \text{EI}_f(1; 0) - c(1) \\ &= 200 - 198 = 2 \end{aligned}$$

$$f(x) = \begin{cases} 200 & \text{w.p. } 0.01 \\ 0 & \text{otherwise} \end{cases}, c(x) = 1, x \in \{2, 3, \dots, 1000\}$$

$$\begin{aligned} \text{EI}_f(x; 0) - c(x) \\ &= 2 - 1 = 1 \end{aligned}$$

Inspection rule: $\operatorname{argmax}_x (\text{EI}_f(x; y_{\text{best}}) - c(x))$ **Stopping rule:** $\text{EI}_f(x; y_{\text{best}}) \leq c(x), \forall x \in \mathcal{X}$

$$\text{EI}_f(x; y) = \mathbb{E}[(f(x) - y)^+]$$

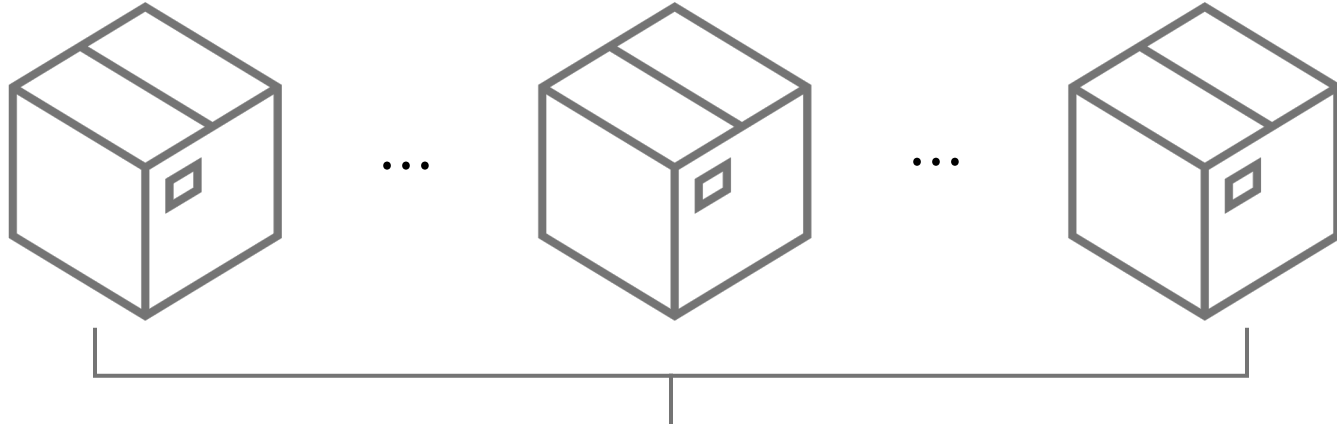
Greedy policy can fail [Singla'18]

$t = 1$

$y_{\text{best}} = 200$



$$\begin{aligned} f(1) &= 200 \text{ w.p. } 1 \\ c(1) &= 198 \end{aligned}$$



$$f(x) = \begin{cases} 200 & \text{w.p. } 0.01 \\ 0 & \text{otherwise} \end{cases}, c(x) = 1, x \in \{2, 3, \dots, 1000\}$$

$$\begin{aligned} & \text{EI}_f(x; 200) - c(x) \\ &= 0 - 1 = -1 < 0 \end{aligned}$$

Inspection rule: $\operatorname{argmax}_x (\text{EI}_f(x; y_{\text{best}}) - c(x))$ **Stopping rule:** $\text{EI}_f(x; y_{\text{best}}) \leq c(x), \forall x \in \mathcal{X}$

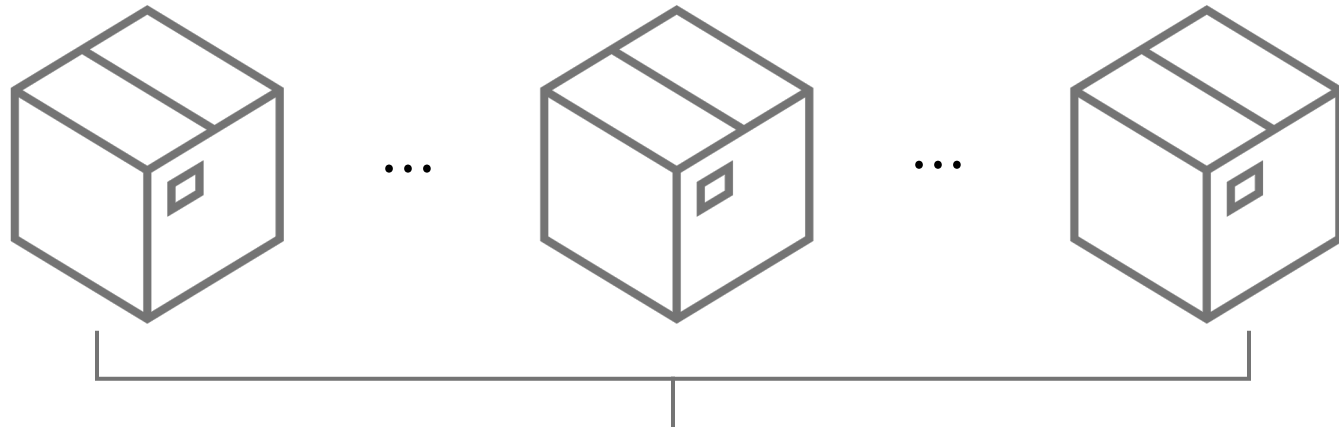
$$\text{EI}_f(x; y) = \mathbb{E}[(f(x) - y)^+]$$

Greedy policy can fail [Singla'18]

$t = 1$



$$\begin{aligned} f(1) &= 200 \text{ w.p. } 1 \\ c(1) &= 198 \end{aligned}$$



$$f(x) = \begin{cases} 200 & \text{w.p. } 0.01 \\ 0 & \text{otherwise} \end{cases}, c(x) = 1, x \in \{2, 3, \dots, 1000\}$$

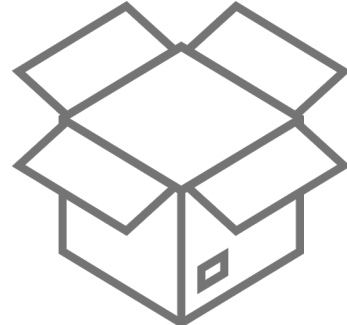
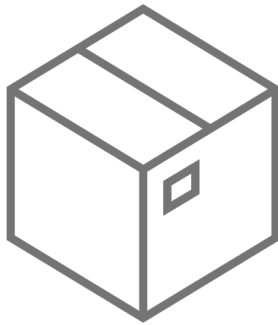
Inspection rule: $\operatorname{argmax}_x (\operatorname{El}_f(x; y_{\text{best}}) - c(x))$ **Stopping rule:** $\operatorname{El}_f(x; y_{\text{best}}) \leq c(x), \forall x \in \mathcal{X}$

Expected utility: $\mathbb{E}[\text{Greedy}] = 200 - 198 = 2$

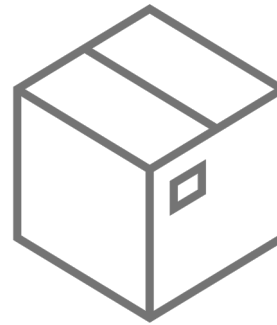
Greedy policy can fail [Singla'18]

$t \approx 100$

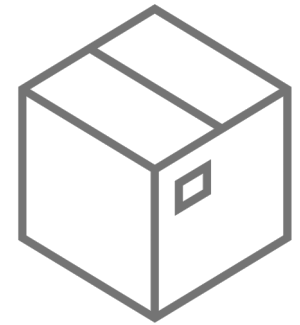
$y_{\text{best}} = 200$



...



...



$$\begin{aligned} f(1) &= 200 \text{ w.p. } 1 \\ c(1) &= 198 \end{aligned}$$

$$f(x) = \begin{cases} 200 & \text{w.p. } 0.01 \\ 0 & \text{otherwise} \end{cases}, c(x) = 1, x \in \{2, 3, \dots, 1000\}$$

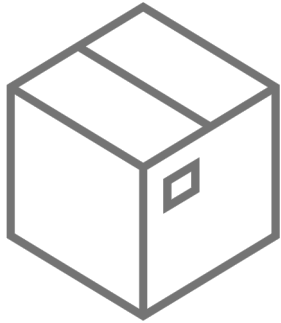
Inspection rule: $x \in \{2, 3, \dots, 1000\}$

Stopping rule: $y_{\text{best}} = 200$

Expected utility: $\mathbb{E}[\text{Optimal}] = 200 - 100 * 1 = 100$

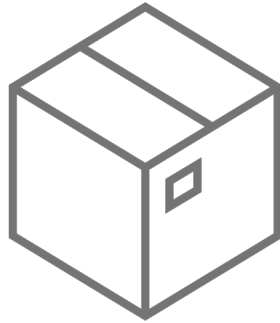
Optimal policy: Gittins policy

Gittins policy

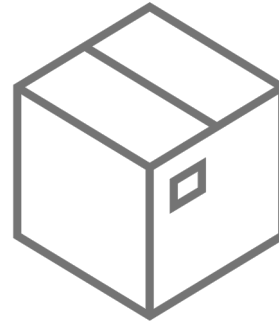


$$f(1) = 200 \text{ w. p. } 1$$

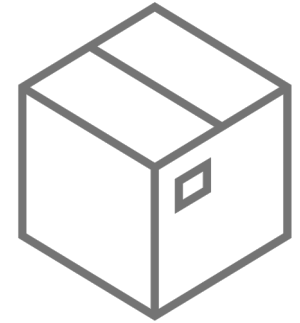
$$c(1) = 198$$



...



...



$$f(x) = \begin{cases} 200 & \text{w. p. } 0.01 \\ 0 & \text{otherwise} \end{cases}, c(x) = 1, x \in \{2, 3, \dots, 1000\}$$

Inspection rule: $\operatorname{argmax}_x \alpha^*(x)$ s.t. $\operatorname{El}_f(x; \alpha^*(x)) = c(x)$ **Stopping rule:** $\alpha^*(x) \leq y_{\text{best}}, \forall x \in \mathcal{X}$

solution to expected improvement = cost

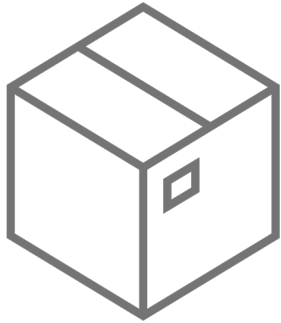
Gittins index \leq current best

y_{best} : current best observed value

$$\operatorname{El}_f(x; y) = \mathbb{E}[(f(x) - y)^+]$$

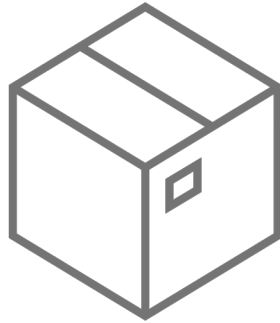
Optimal policy: Gittins policy

$t = 0$

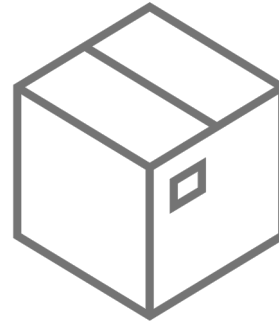


$$f(1) = 200 \text{ w.p. } 1$$
$$c(1) = 198$$

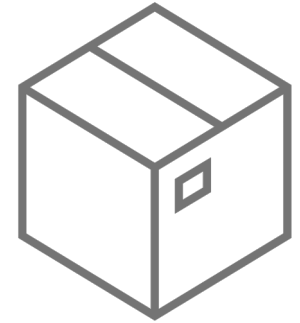
$$\alpha^*(1) = 2$$



...



...



$$f(x) = \begin{cases} 200 & \text{w.p. } 0.01 \\ 0 & \text{otherwise} \end{cases}, c(x) = 1, x \in \{2, 3, \dots, 1000\}$$

$$\alpha^*(x) = 100$$

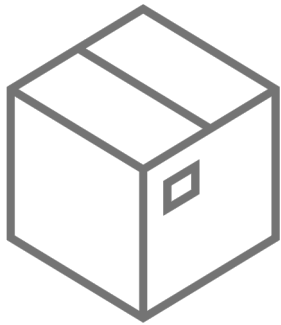
Inspection rule: $\operatorname{argmax}_x \alpha^*(x)$ s.t. $\operatorname{El}_f(x; \alpha^*(x)) = c(x)$ **Stopping rule:** $\alpha^*(x) \leq y_{\text{best}}, \forall x \in \mathcal{X}$

$$\operatorname{El}_f(x; y) = \mathbb{E}[(f(x) - y)^+]$$

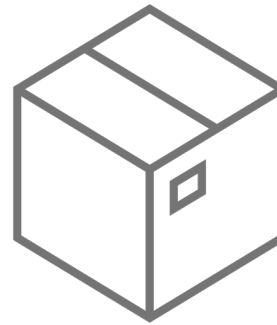
Optimal policy: Gittins policy

$t = 1$

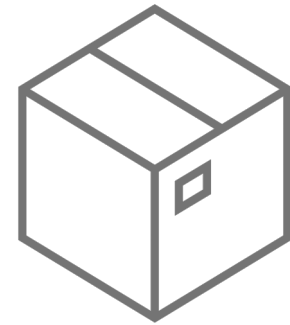
$y_{\text{best}} = 200 \text{ or } 0$



...



...



$$f(1) = 200 \text{ w.p. } 1$$

$$c(1) = 198$$

$$\alpha^*(1) = 2$$

$$f(x) = \begin{cases} 200 & \text{w.p. } 0.01 \\ 0 & \text{otherwise} \end{cases}, c(x) = 1, x \in \{2, 3, \dots, 1000\}$$

$$\alpha^*(x) = 100$$

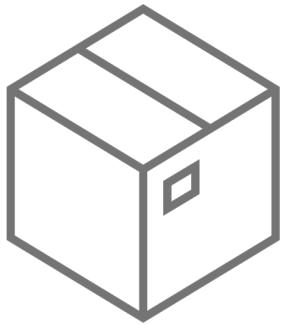
Inspection rule: $\operatorname{argmax}_x \alpha^*(x)$ s.t. $\operatorname{El}_f(x; \alpha^*(x)) = c(x)$ **Stopping rule:** $\alpha^*(x) \leq y_{\text{best}}, \forall x \in \mathcal{X}$

$$\operatorname{El}_f(x; y) = \mathbb{E}[(f(x) - y)^+]$$

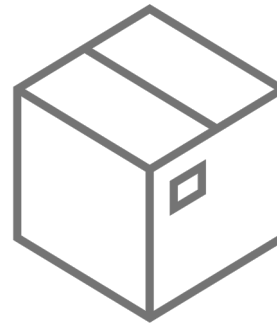
Optimal policy: Gittins policy

$t \approx 100$

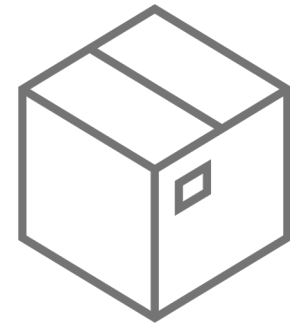
$y_{\text{best}} = 200$



...



...



$$f(1) = 200 \text{ w.p. } 1$$

$$c(1) = 198$$

$$\alpha^*(1) = 2$$

$$f(x) = \begin{cases} 200 & \text{w.p. } 0.01 \\ 0 & \text{otherwise} \end{cases}, c(x) = 1, x \in \{2, 3, \dots, 1000\}$$

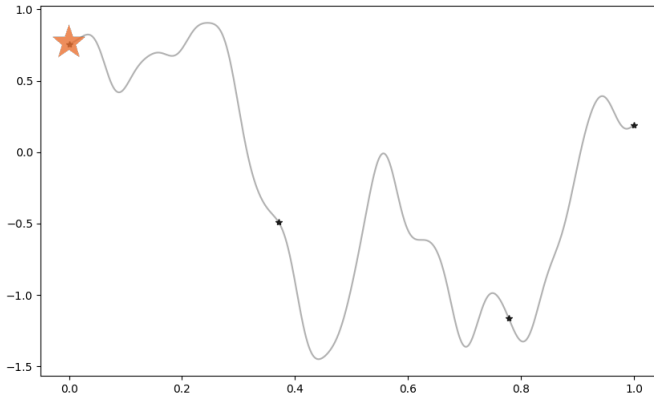
$$\alpha^*(x) = 100$$

Inspection rule: $\operatorname{argmax}_x \alpha^*(x)$ s.t. $\mathbb{E}_f(x; \alpha^*(x)) = c(x)$ **Stopping rule:** $\alpha^*(x) \leq y_{\text{best}}, \forall x \in \mathcal{X}$

Expected utility: $\mathbb{E}[\text{Gittins}] = 200 - 100 * 1 = 100$

Bayesian Optimization \Rightarrow Pandora's Box

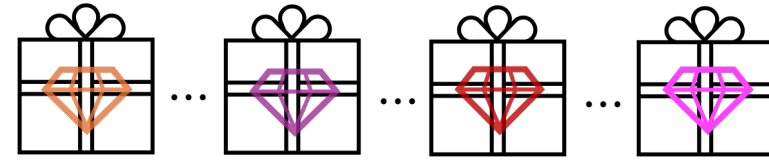
Special case of Markovian/
Bayesian multi-armed bandits



Continuous

Correlated

Hard budget constraint



Discrete



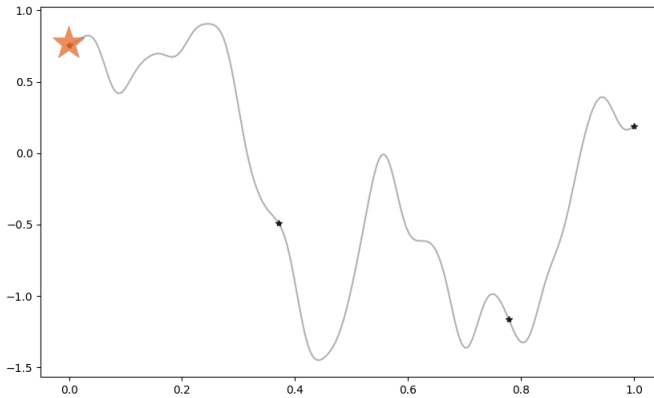
Independent



Cost per sample

Optimal policy: Gittins index [Weitzman'79]

Bayesian Optimization \Rightarrow Pandora's Box

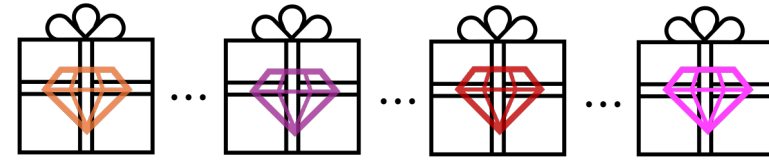
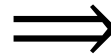


Continuous

Correlated

Hard budget constraint

Is Gittins index good?



Discrete

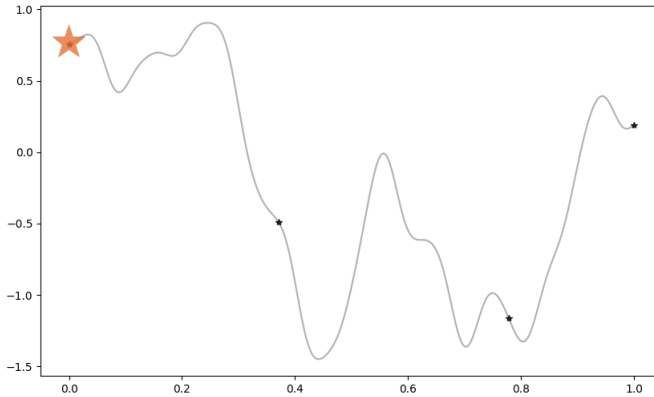
Independent

Cost per sample

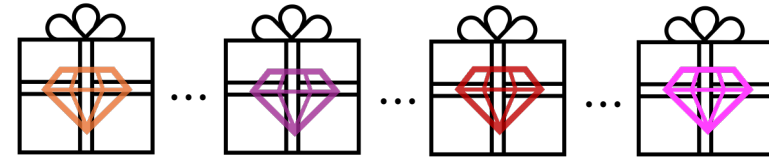
Optimal policy: Gittins index



Bayesian Optimization \Rightarrow Pandora's Box



Continuous



Discrete

Correlated



Independent

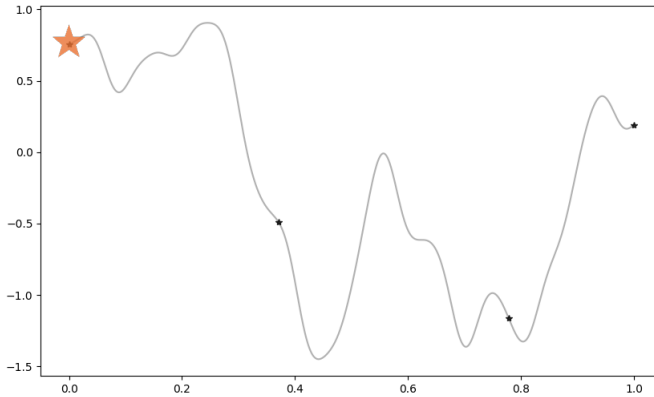
Hard budget constraint



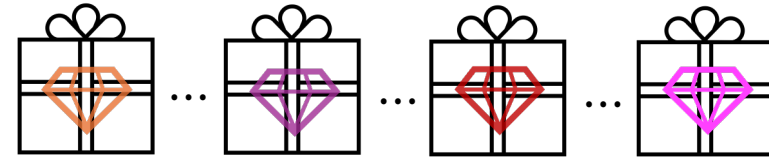
Cost per sample

Is Gittins index good? How to translate? \Leftarrow Optimal policy: Gittins index

Bayesian Optimization \Rightarrow Pandora's Box



Continuous



Discrete

Correlated



Independent

Hard budget constraint



Cost per sample

Is Gittins index good?

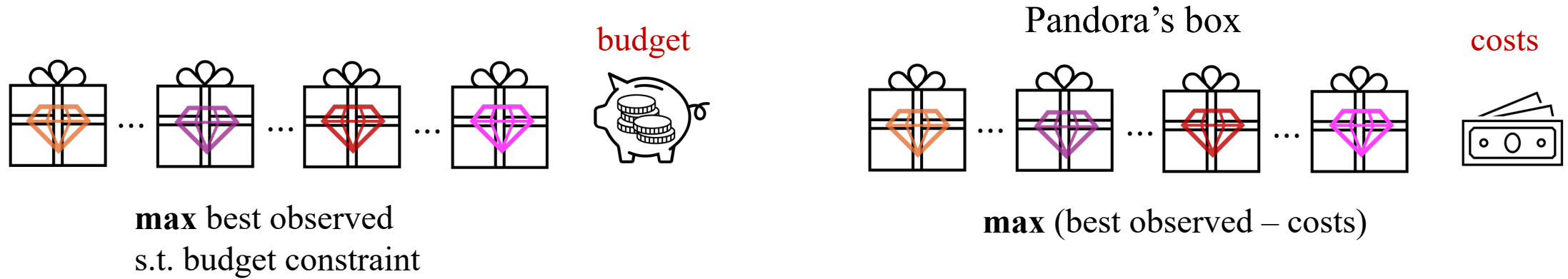
How to translate?



Optimal policy: Gittins index

Our contributions!

How to translate?



Expected budget constraint



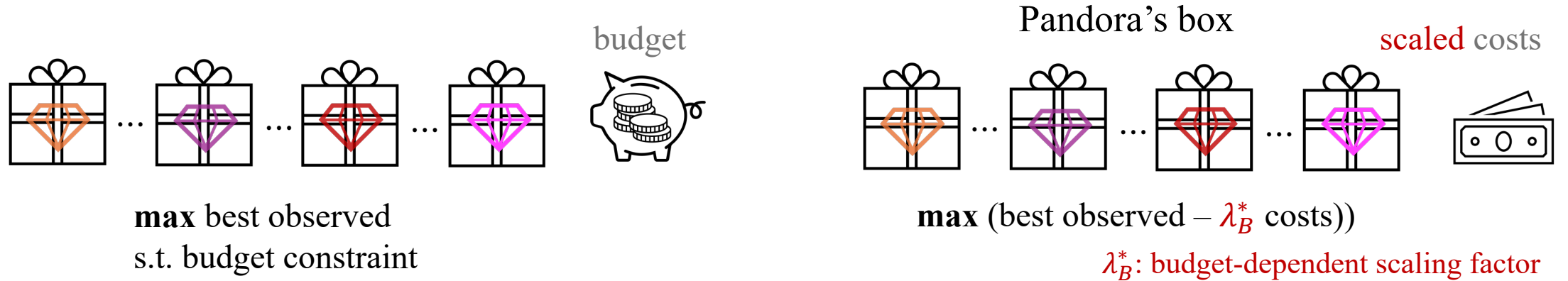
Cost per sample

Optimal policy?



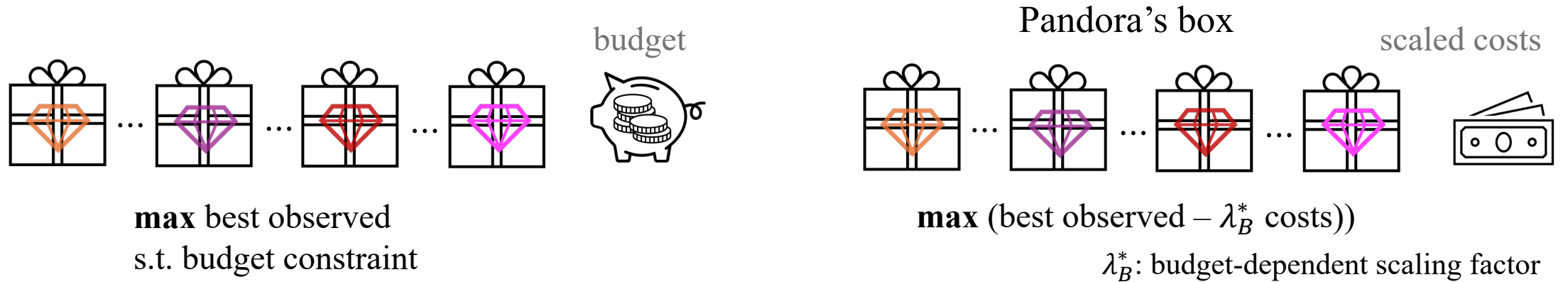
Optimal policy: Gittins index

Expected budget constraint \Leftrightarrow Cost per sample



Optimal policy: Gittins solution to Pandora's box with scaled costs \Leftrightarrow Optimal policy: Gittins index

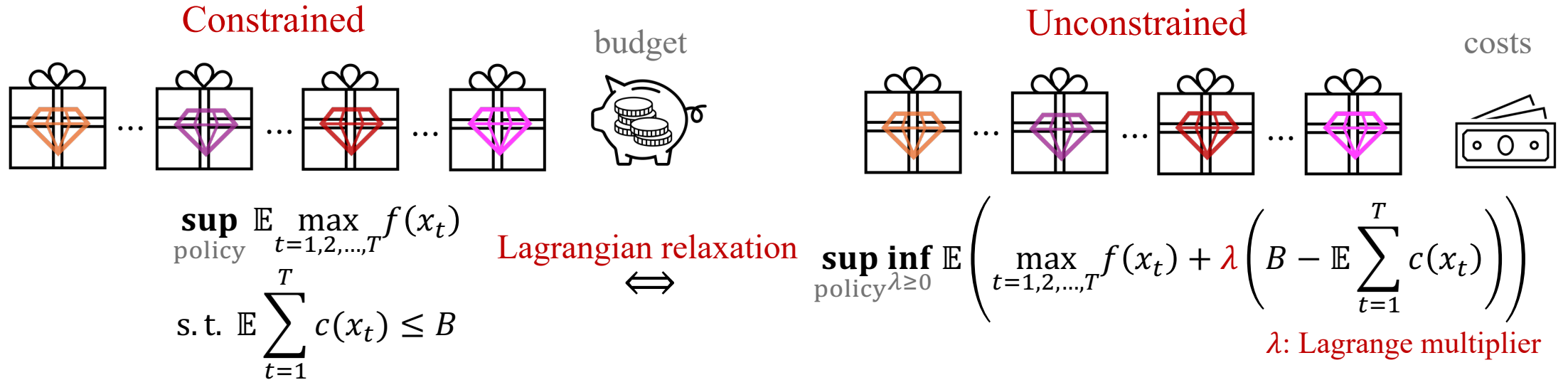
Expected budget constraint \Leftrightarrow Cost per sample



Reward distribution	Reference
finite support	[Aminian et al.'24]
general support	our work

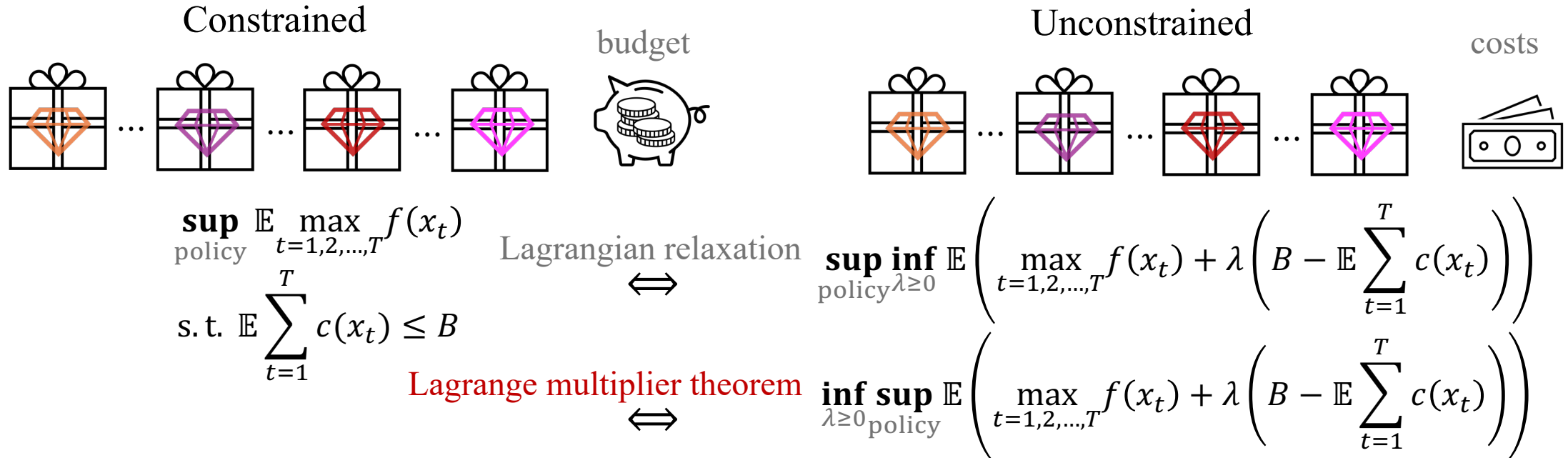
Optimal policy: Gittins solution to Pandora's box with scaled costs \Leftarrow Optimal policy: Gittins index

Expected budget constraint \Leftrightarrow Cost per sample



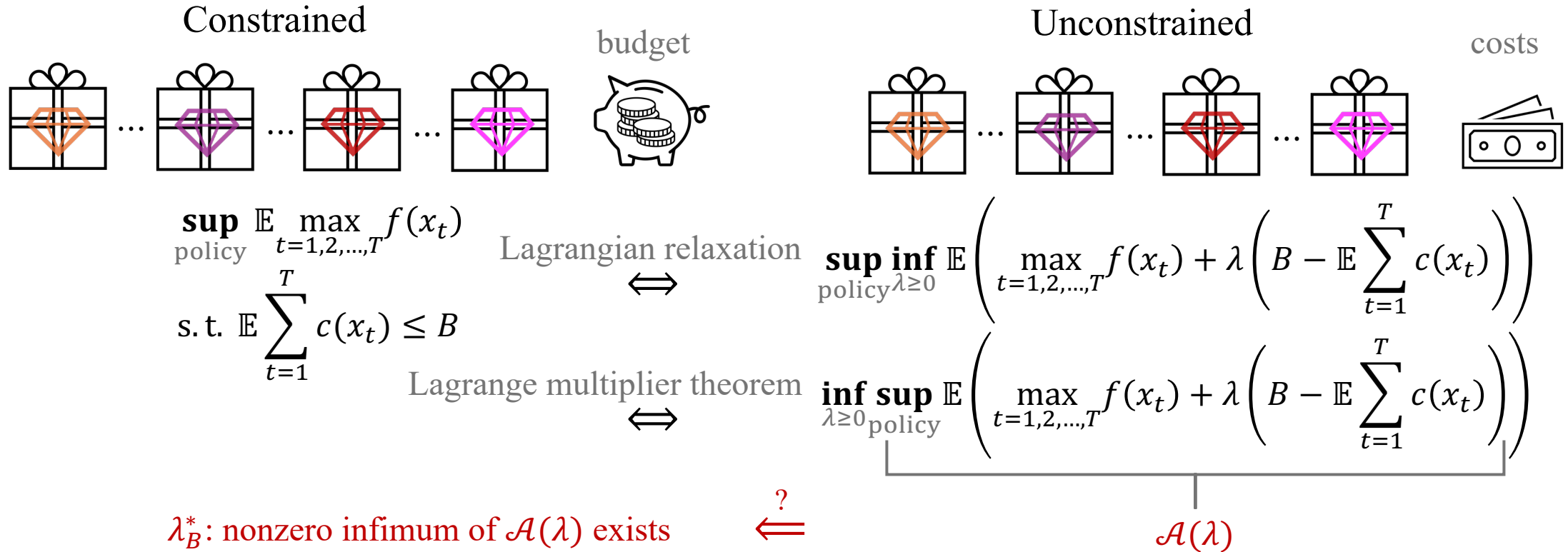
Optimal policy: Gittins solution to \Leftarrow Optimal policy: Gittins index
 Pandora's box with scaled costs
 Extension to [Aminian et al.'24]

Expected budget constraint \Leftrightarrow Cost per sample



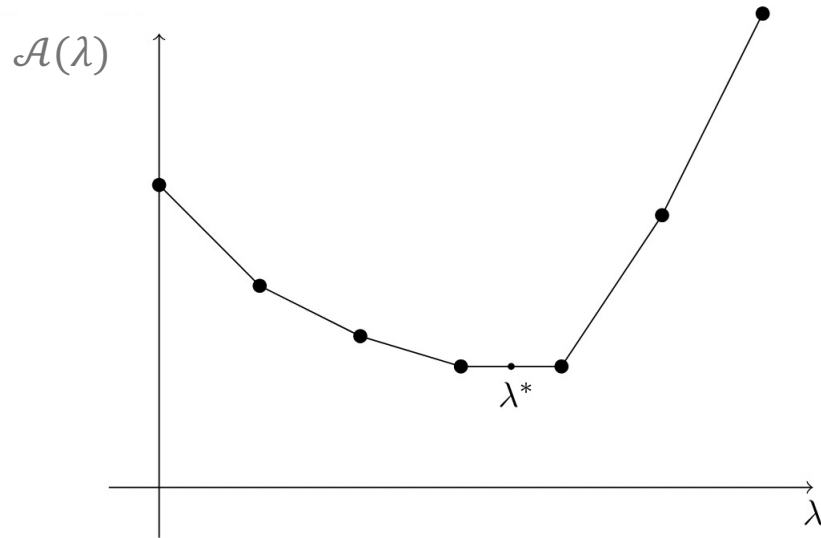
Optimal policy: Gittins solution to \Leftarrow Optimal policy: Gittins index
 Pandora's box with scaled costs
 Extension to [Aminian et al.'24]

Expected budget constraint \Leftrightarrow Cost per sample

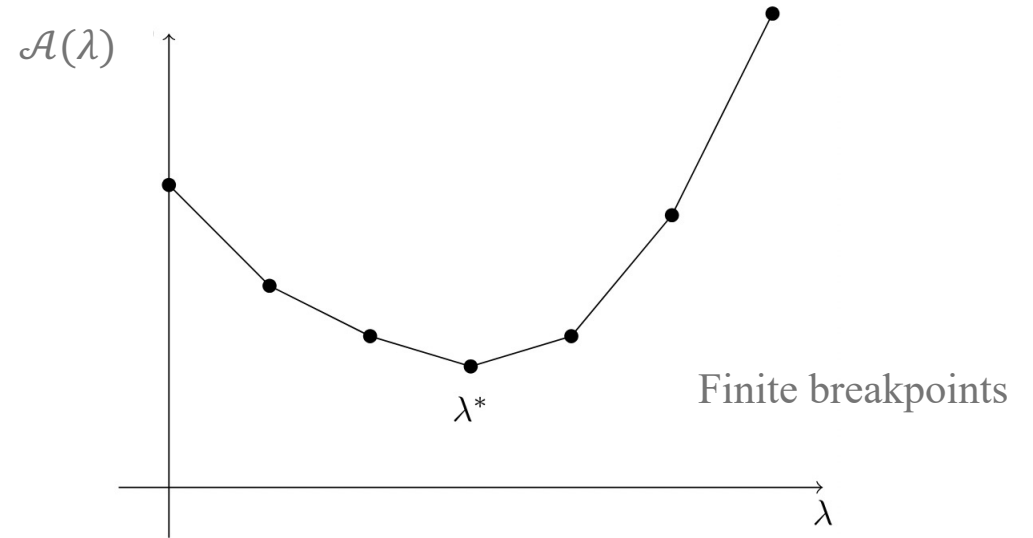


Optimal policy: Gittins solution to \Leftarrow Optimal policy: Gittins index
 Pandora's box with scaled costs
 Extension to [Aminian et al.'24]

Expected budget constraint \Leftrightarrow Cost per sample



(a) Degenerate case, differentiable at λ^* .



(b) Non-degenerate case, breakpoint at λ^* .

$$\inf_{\lambda \geq 0} \sup_{\text{policy}} \mathbb{E} \left(\max_{t=1,2,\dots,T} f(x_t) + \lambda \left(B - \mathbb{E} \sum_{t=1}^T c(x_t) \right) \right)$$

Envelope Theorem

λ_B^* : nonzero infimum of $\mathcal{A}(\lambda)$ exists

\Leftrightarrow

$\mathcal{A}(\lambda)$: **convex (possibly non-differentiable) in λ**

Optimal policy: Gittins solution to

\Leftrightarrow

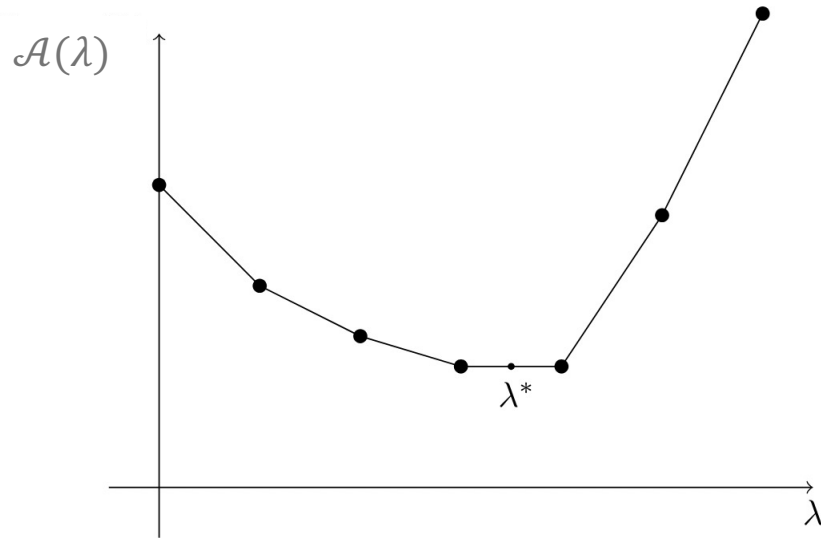
Optimal policy: Gittins index

Pandora's box with scaled costs

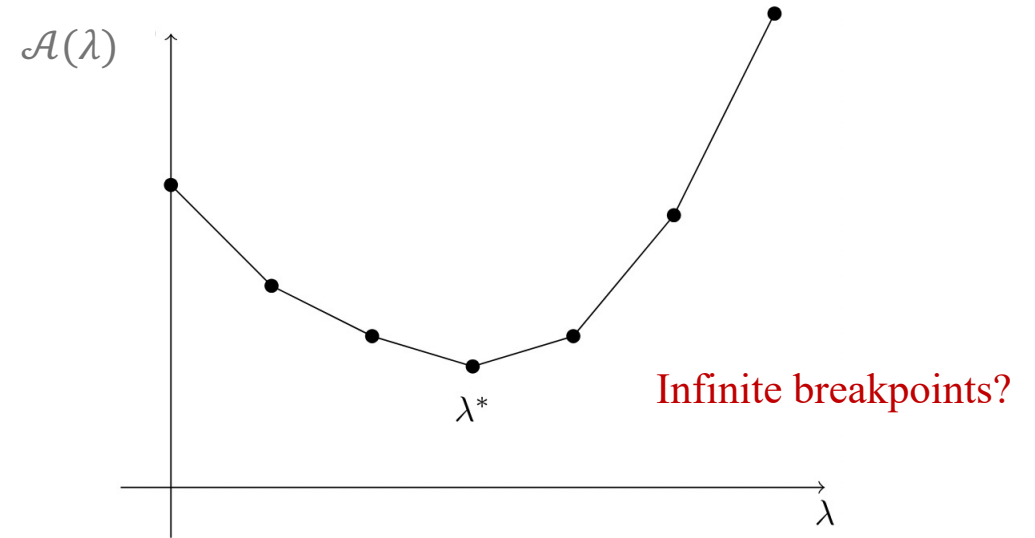
Extension to [Aminian et al.'24]

Figure from [Aminian et al.'24]

Expected budget constraint \Leftrightarrow Cost per sample



(a) Degenerate case, differentiable at λ^* .



(b) Non-degenerate case, breakpoint at λ^* .

$$\inf_{\lambda \geq 0} \sup_{\text{policy}} \mathbb{E} \left(\max_{t=1,2,\dots,T} f(x_t) + \lambda \left(B - \mathbb{E} \sum_{t=1}^T c(x_t) \right) \right)$$

λ_B^* : nonzero infimum of $\mathcal{A}(\lambda)$ exists

\Leftrightarrow

$\mathcal{A}(\lambda)$: convex (possibly non-differentiable) in λ

Optimal policy: Gittins solution to
Pandora's box with scaled costs

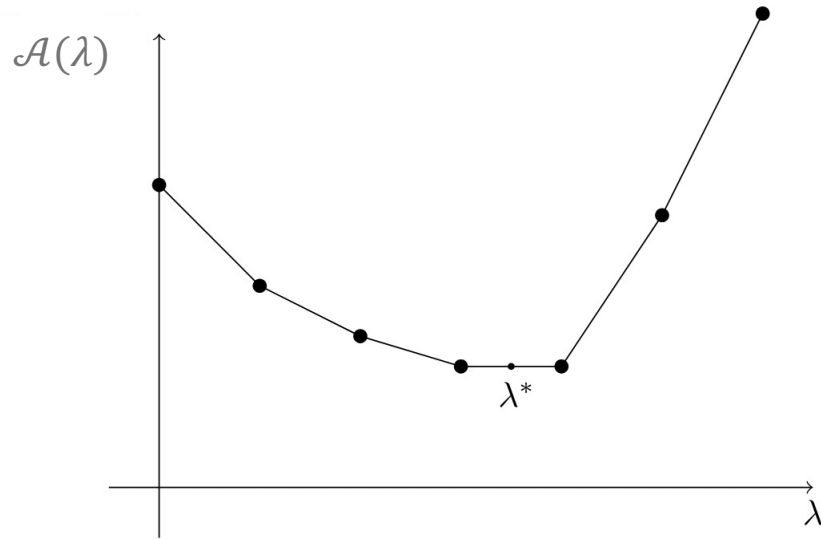
\Leftrightarrow

Optimal policy: Gittins index

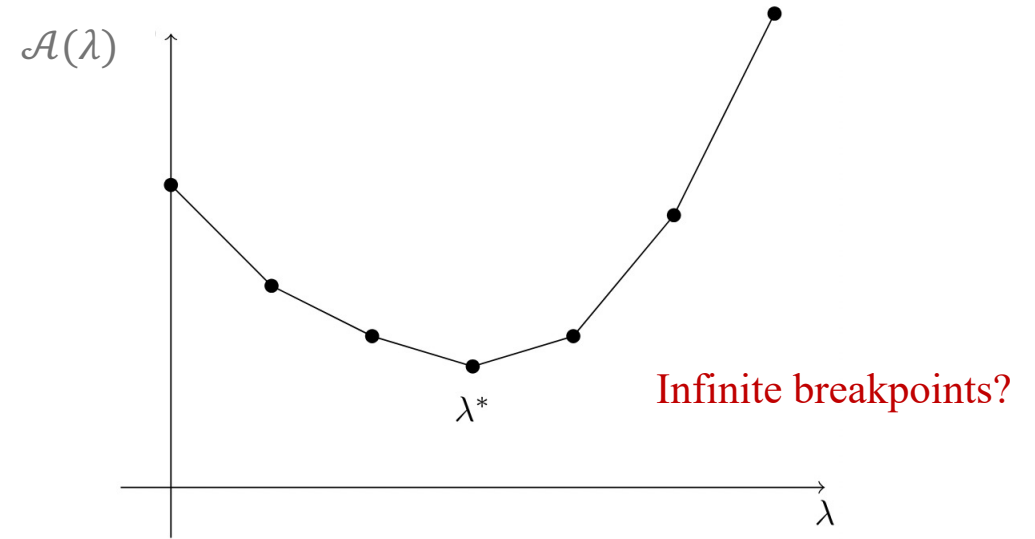
Extension to [Aminian et al.'24]

Figure from [Aminian et al.'24]

Expected budget constraint \Leftrightarrow Cost per sample



(a) Degenerate case, differentiable at λ^* .



(b) Non-degenerate case, breakpoint at λ^* .

$$\inf_{\lambda \geq 0} \sup_{\text{policy}} \mathbb{E} \left(\max_{t=1,2,\dots,T} f(x_t) + \lambda \left(B - \mathbb{E} \sum_{t=1}^T c(x_t) \right) \right)$$

sharp Envelope Theorem

λ_B^* : nonzero infimum of $\mathcal{A}(\lambda)$ exists

\Leftrightarrow

$\mathcal{A}(\lambda)$: convex (possibly non-differentiable) in λ

Optimal policy: Gittins solution to

\Leftrightarrow

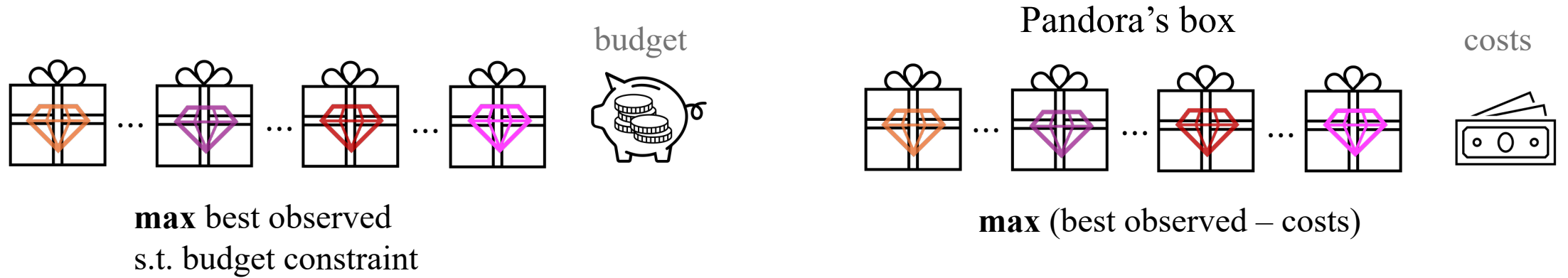
Optimal policy: Gittins index

Pandora's box with scaled costs

Extension to [Aminian et al.'24]

Figure from [Aminian et al.'24]

How to translate?



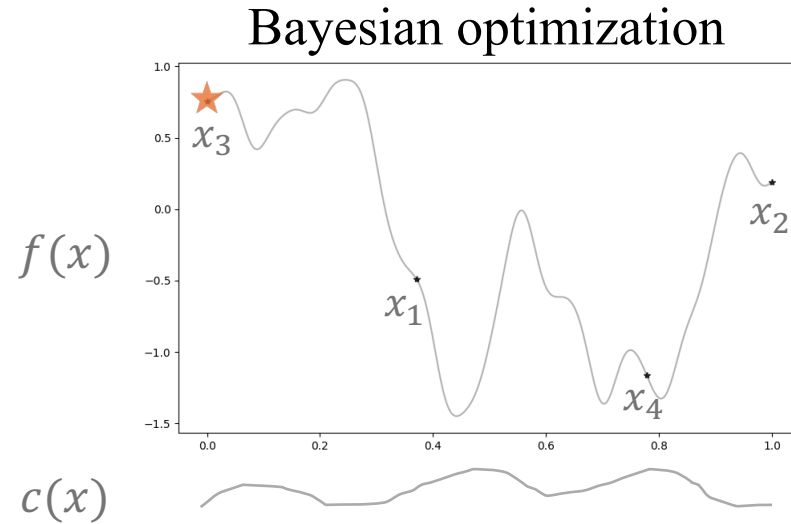
Hard budget constraint

\Leftarrow

Cost per sample

$$\operatorname{argmax}_x \alpha^*(x) \text{ s.t. } \operatorname{El}_f(x; \alpha^*(x)) = \lambda_B^* c(x) \Leftarrow \operatorname{argmax}_x \alpha^*(x) \text{ s.t. } \operatorname{El}_f(x; \alpha^*(x)) = c(x)$$

How to translate?

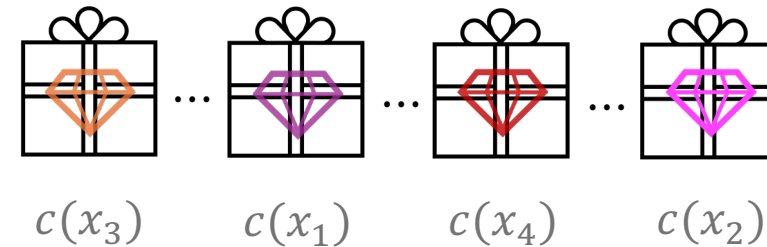


Continuous

Correlated

Hard budget constraint

Budget-constrained
Pandora's box



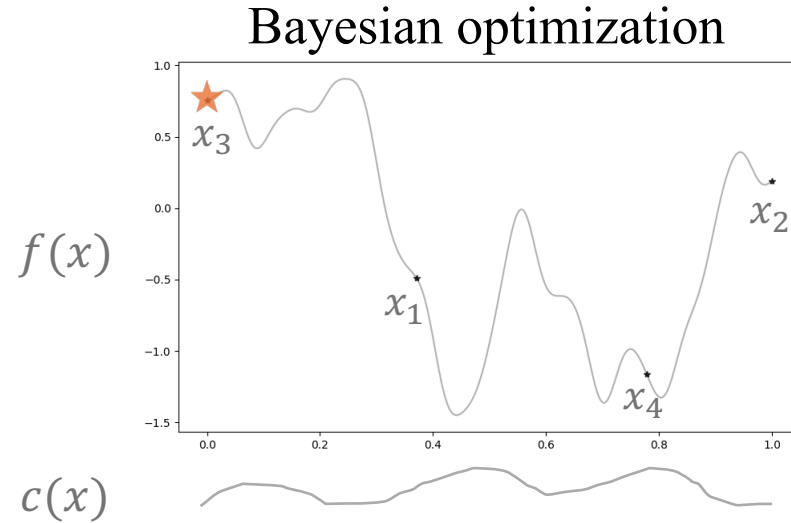
Discrete

Independent

Cost per sample

How to incorporate Gaussian process? \Leftarrow Optimal policy: Gittins solution to Pandora's box with scaled costs

How to translate?

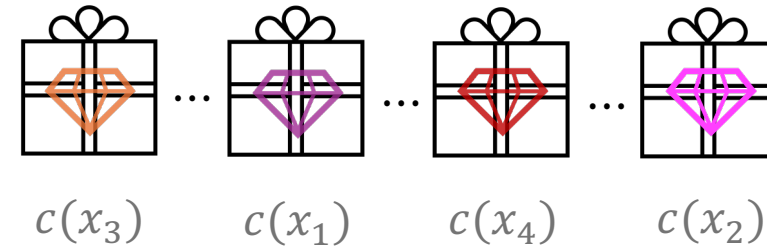


Continuous

Correlated

Hard budget constraint

Budget-constrained
Pandora's box



Discrete

Independent

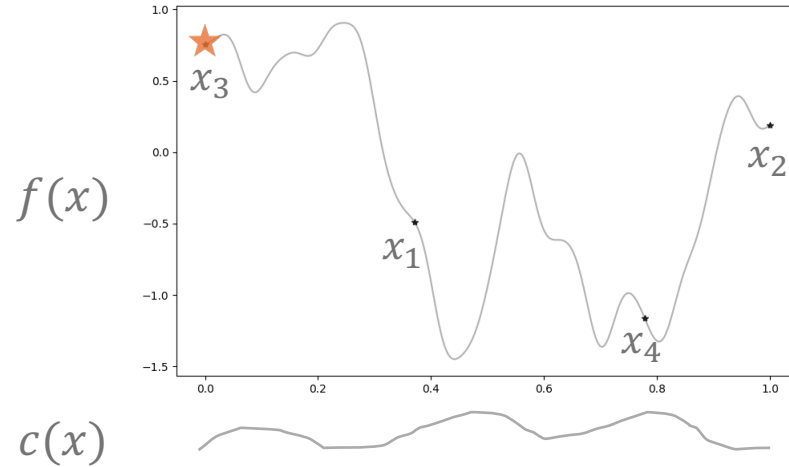
Cost per sample

$$\operatorname{argmax}_x \alpha^*(x) \text{ s.t. } \operatorname{EI}_{f|D}(x; \alpha^*(x)) = \lambda_B^* c(x) \iff \operatorname{argmax}_x \alpha^*(x) \text{ s.t. } \operatorname{EI}_f(x; \alpha^*(x)) = \lambda_B^* c(x)$$

D : observed data

How to translate?

Bayesian optimization

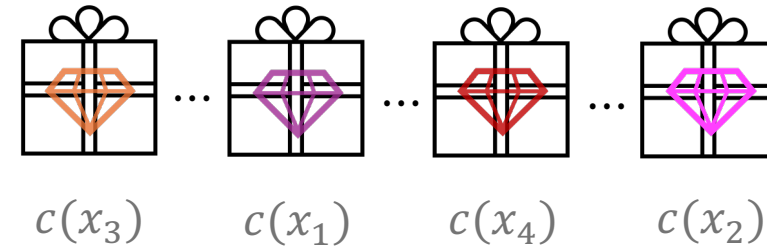


Continuous

Correlated

Hard budget constraint

Budget-constrained
Pandora's box



Discrete

Independent

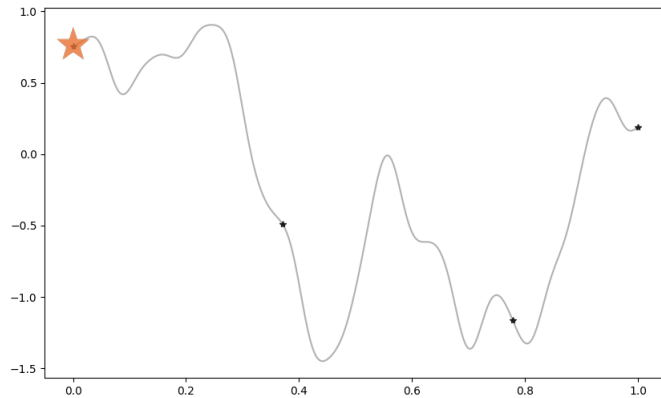
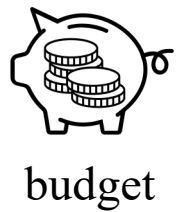
Cost per sample

$$\operatorname{argmax}_x \alpha^*(x) \text{ s.t. } \underbrace{\operatorname{EI}_{f|D}(x; \alpha^*(x))}_{\text{popular one-step heuristic: EI policy}} = \lambda_B^* c(x) \iff \operatorname{argmax}_x \alpha^*(x) \text{ s.t. } \operatorname{EI}_f(x; \alpha^*(x)) = \lambda_B^* c(x)$$

popular one-step
heuristic: EI policy

Our Contributions

- How to translate?
- Is Pandora's Box Gittins index (PBGI) good?



?

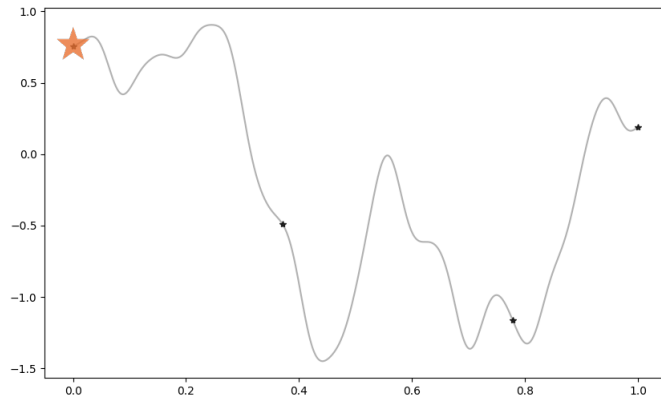


Pandora's Box Gittins index



Our Contributions

- Develop **PBGI policy** for cost-aware Bayesian optimization
- Is Pandora's Box Gittins index (PBGI) good?



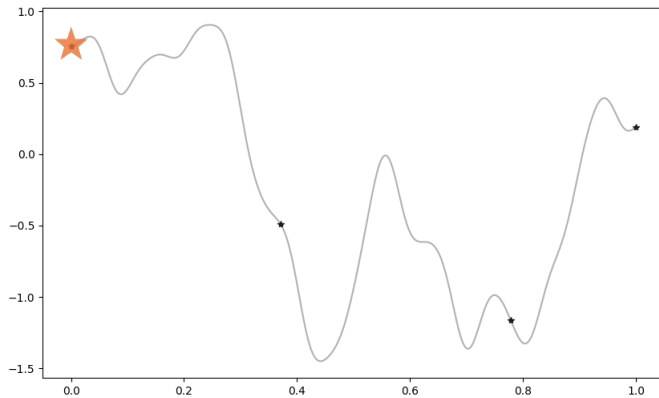
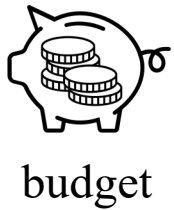
Our work



⇐ Pandora's Box Gittins index

Our Contributions

- Develop PBGI policy for Bayesian optimization
- Show **performance** against baselines on synthetic & empirical experiments

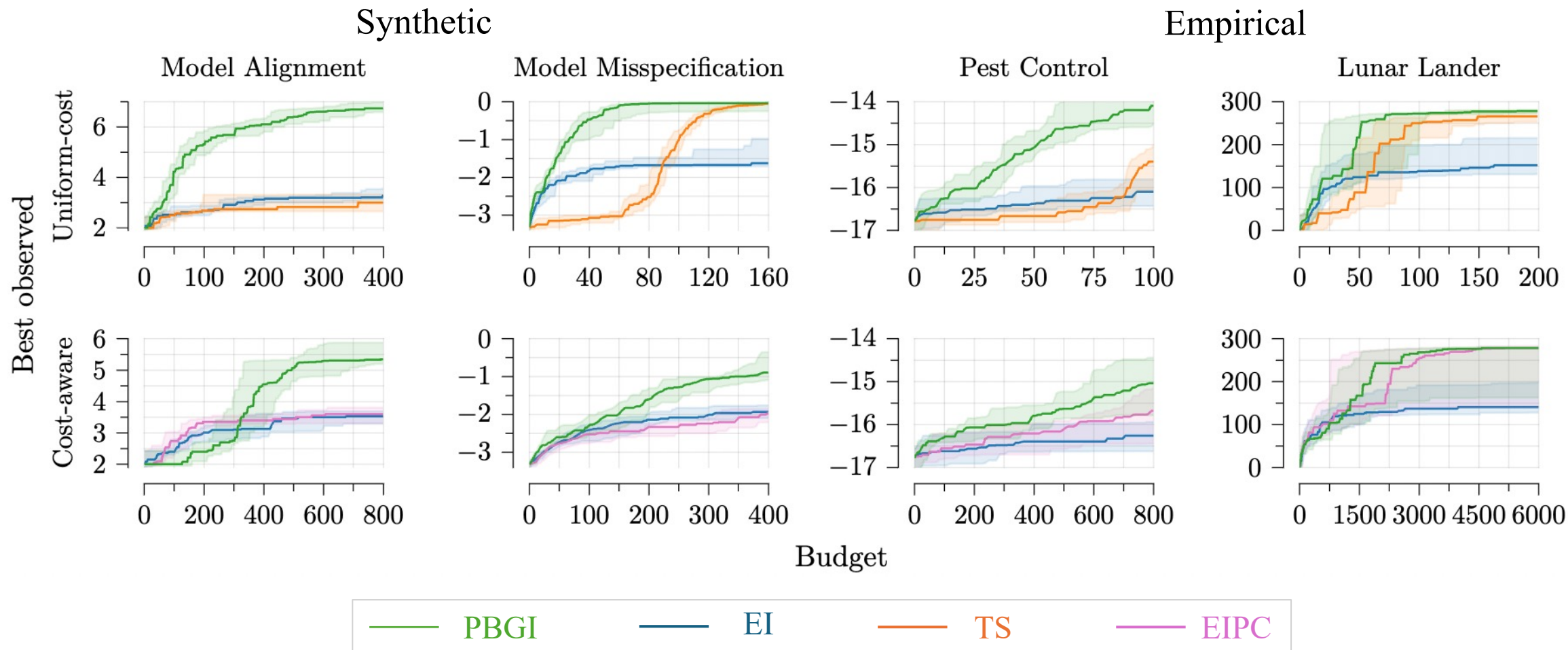


Our work



\Leftarrow Pandora's Box Gittins index

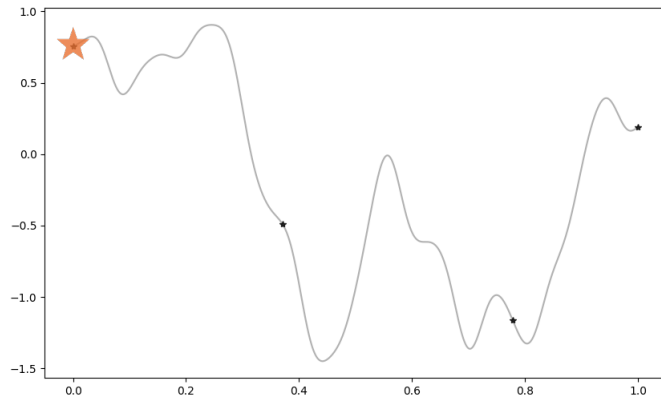
Experiment Results: PBGI vs Baselines



Check our preprint on arXiv!

Conclusions

- Propose **easy-to-compute** PBGI policy for Bayesian optimization



Our work



Pandora's Box Gittins index

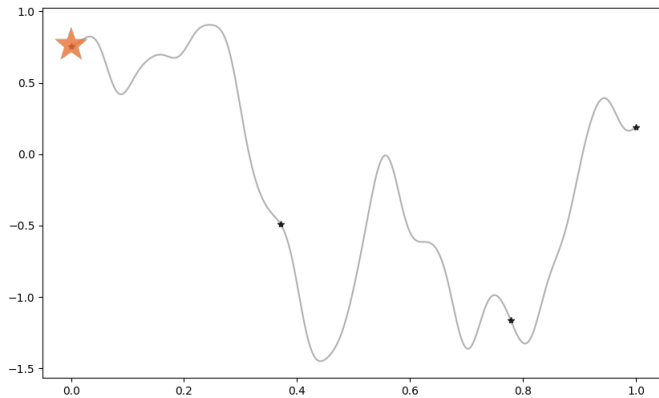
Check our preprint on arXiv!

Conclusions

- Propose easy-to-compute PBGI policy for Bayesian optimization
- Show the **effectiveness of PBGI** on synthetic & empirical experiments



budget



Our work

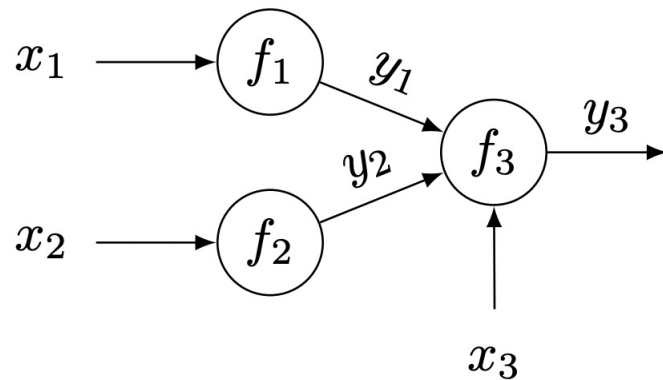


Pandora's Box Gittins index

Check our preprint on arXiv!

Conclusions

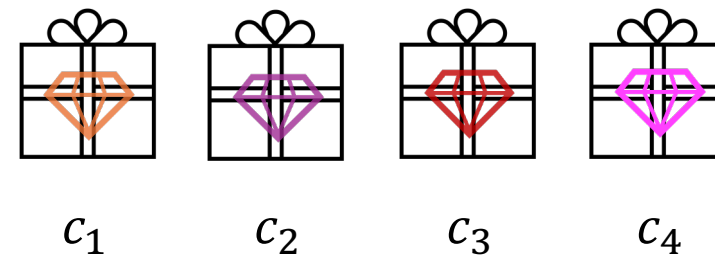
- Propose easy-to-compute PBGI policy for Bayesian optimization
- Show the effectiveness of PBGI on synthetic & empirical experiments
- Open door for **more-complex BO** (freeze-thaw, multi-fidelity, function network, etc.) via Gittins variants (“golf” Markovian MAB, optional inspection, etc.)



?



Pandora's Box Gittins index



Check our preprint on arXiv!