

Hard budget constraint

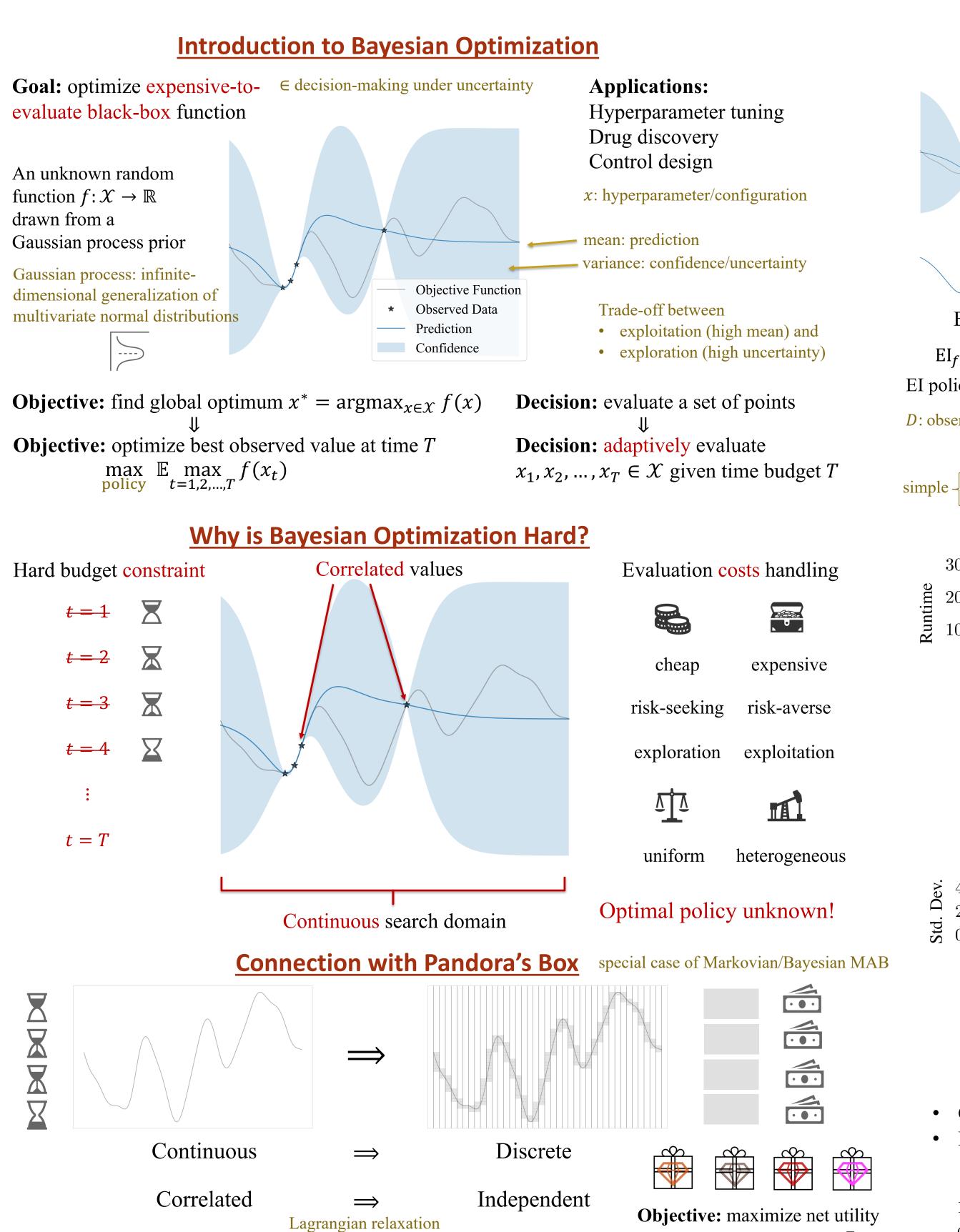
Is Gittins index good?

extension of [Aminian et al.'24]

How to translate?

# Cost-aware Bayesian Optimization via the Pandora's Box Gittins Index

Qian Xie<sup>1</sup>, Raul Astudillo<sup>2</sup>, Peter Frazier<sup>1</sup>, Ziv Scully<sup>1</sup>, Alexander Terenin<sup>1</sup> <sup>1</sup> Cornell University, <sup>2</sup> California Institute of Technology



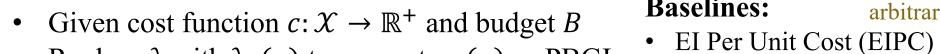
Cost per sample

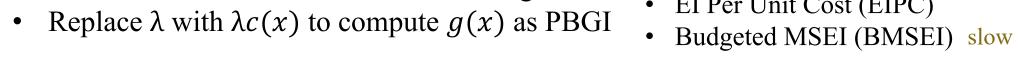
[Weitzman'79]

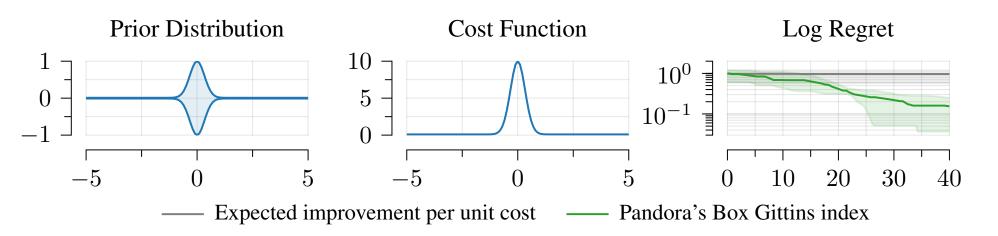
*T*: random stopping time

← Optimal policy: Gittins index

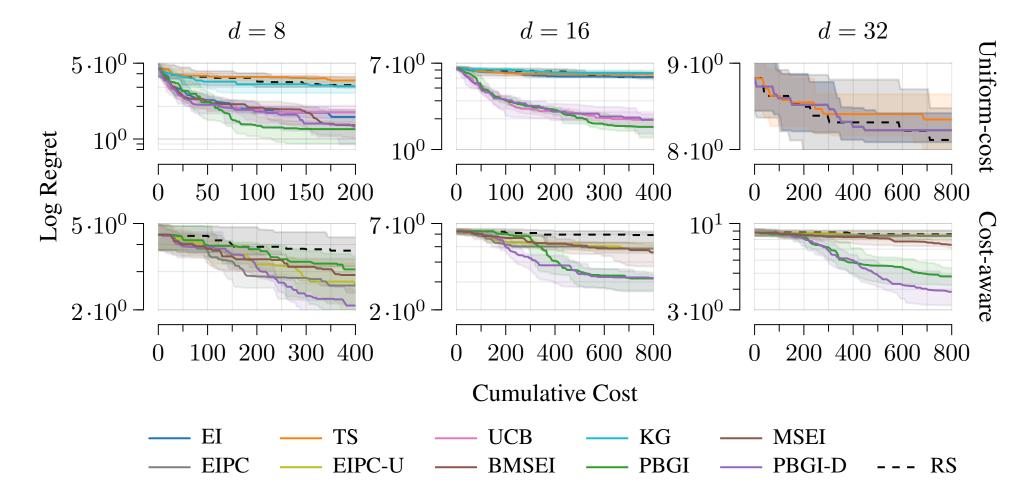
#### **Acquisition Functions** Pandora's Box Gittins Index (PBGI) Expected Improvement (EI) g(x): solution to $\mathrm{EI}_{f|D}(x;g(x)) = \lambda^{-1}$ $\operatorname{EI}_{f|D}(x;y) = \mathbb{E}[((f|D)(x) - y)^{+}]$ EI policy: evaluate $\operatorname{argmax}_{x} \operatorname{EI}_{f|D}(x; y_{\text{best}})$ PBGI policy: evaluate $argmax_x g(x)$ λ: cost-per-sample (Lagrange multiplier) D: observed data, $y_{\text{best}}$ : current best observed value • Predictive Entropy Search unreliable Other acquisition functions: • Knowledge Gradient (KG) • Upper Confidence Bound (UCB) • Multi-step Lookahead EI (MSEI) • Thompson Sampling (TS) d = 8d = 161,200 **E** 100 0 10 20 30 40 0 20 40 60 80 0 40 80 120 160 **Cumulative Cost** — EI — TS — KG — MSEI PBGI is easy to compute using bisection method! Contour Plot Impact of $\lambda$ PBGI Expected **PBGI** Log Regret Improvement $\lambda = 10^0$ $\lambda = 10^{-5}$ $- \lambda = 0.001$ $--- \lambda = 0.0001$ $--- \lambda = 0.00001$ 0 50 100 150 200 --- Dynamic $\lambda$ -3 0**Cumulative Cost** Mean Connection with UCB? Smaller $\lambda$ , higher exploration **Heterogeneous Costs Baselines:** arbitrarily bad



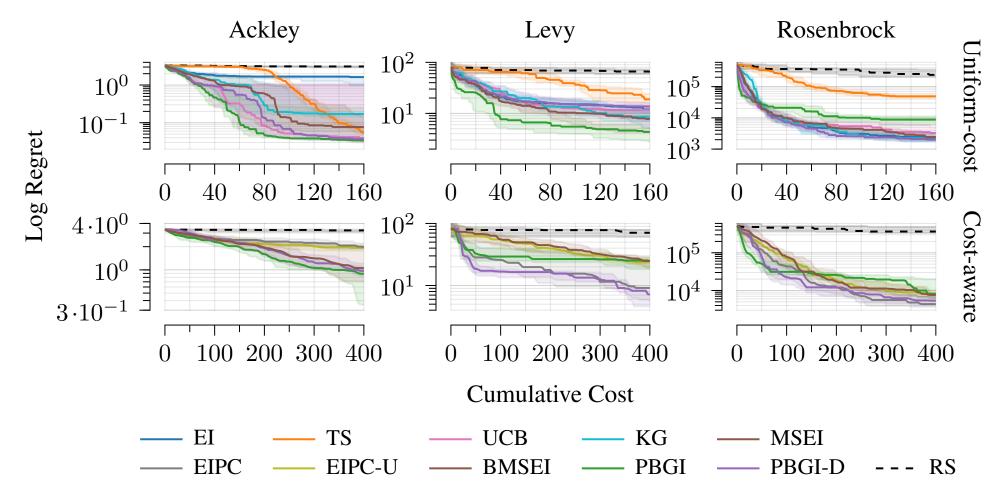




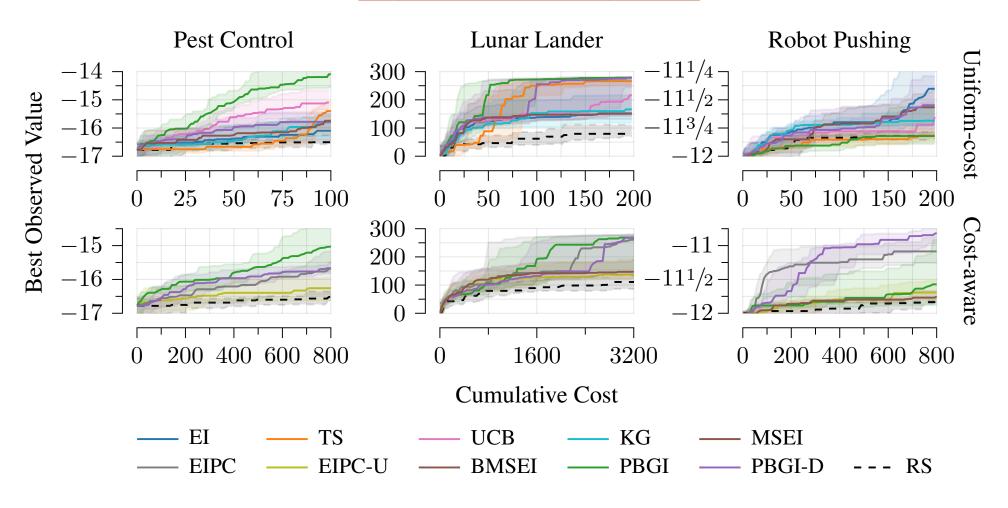
# **Experiment: Bayesian Regret**



## **Experiment: Synthetic Benchmarks**



#### **Experiment: Empirical**



### **Future Work**

Extension to complex BO (freeze-thaw, multi-fidelity, function network, etc.) via Gittins variants ("golf" Markovian MAB, optional inspection, etc.)