Table 1: Comparison of DPR, BM-25, LLM Reranking and GPR-LLM (RBF kernel,  $\epsilon=0.1$ ) with all-MiniLM-L6-v2 encoder across four datasets (TravelDest, POINTREC, Yelp Restaurant, TripAdvisor Hotel) at varying budget of LLM labels. Metrics reported are Precision@10, NDCG@10, Precision@30, and NDCG@30; bold values indicate the best-performing method per column. Statistically significant improvements over the best-performing baseline (paired t-test, p < 0.05) are indicated by an underline.

Budget	Method	P@10	Trave NDCG@10	P@30	NDCG@30	P@10	POIN NDCG@10	TREC P@30		P@10	Yelp Re NDCG@10			P@10	TripAdv NDCG@10		
N/A	DPR BM25	$0.360 \\ 0.234$	0.366 0.238	$0.314 \\ 0.237$	$0.332 \\ 0.239$	$  \begin{array}{c} 0.164 \\ 0.025 \end{array}  $	$0.179 \\ 0.032$	$0.104 \\ 0.025$	$0.182 \\ 0.038$	0.346	$0.362 \\ 0.327$	$0.282 \\ 0.236$	$0.331 \\ 0.283$	$  \begin{array}{c} 0.231 \\ 0.205 \end{array}  $	$0.297 \\ 0.257$	$0.166 \\ 0.153$	0.365 0.325
25	LLM Reranking GPR-LLM	0.294 <b>0.376</b>	0.309 <b>0.401</b>	0.238 <b>0.340</b>	0.219 <b>0.364</b>	0.175 0.157	0.206 0.200	$0.106 \\ 0.108$	0.158 $0.177$	$\begin{vmatrix} 0.324 \\ 0.360 \end{vmatrix}$	0.374 <b>0.402</b>	0.237 $0.273$	0.260 <b>0.340</b>	$  {0.251} \atop {f 0.282}$	0.349 <b>0.382</b>	0.178 $0.182$	0.332 <b>0.426</b>
50	LLM Reranking GPR-LLM	0.356 <b>0.432</b>	0.371 <b>0.445</b>	0.248 $0.362$	0.281 <b>0.389</b>	0.196 0.236	0.234 <b>0.262</b>	$0.105 \\ 0.113$	0.208 <b>0.222</b>	$  {0.386}\atop {f 0.408}$	0.426 <b>0.451</b>	0.254 $0.304$	0.332 <b>0.377</b>	0.289 $0.324$	0.397 <b>0.439</b>	0.169 <b>0.197</b>	0.417 <b>0.482</b>
100	LLM Reranking GPR-LLM	0.398 <b>0.448</b>	$0.406 \\ \underline{0.472}$	0.296	0.328 $0.412$	$  egin{array}{c} 0.225 \ {f 0.246} \ \end{array}  $	0.255 <b>0.269</b>	$0.124 \\ 0.130$	0.231 <b>0.239</b>	$\begin{vmatrix} 0.418 \\ 0.444 \end{vmatrix}$	0.459 <b>0.487</b>	$\begin{array}{c} 0.298 \\ 0.334 \end{array}$	0.379 <b>0.413</b>	$\begin{vmatrix} 0.322 \\ {f 0.358} \end{vmatrix}$	0.438 $0.481$	$0.189 \\ 0.218$	0.472 <b>0.529</b>

Table 2: Comparison of DPR, BM-25, LLM Reranking and GPR-LLM (RBF kernel,  $\epsilon=0.1$ ) with msmarco-distilbert-base-tas-b encoder across four datasets (TravelDest, POINTREC, Yelp Restaurant, TripAdvisor Hotel) at varying budget of LLM labels. Metrics reported are Precision@10, NDCG@10, Precision@30, and NDCG@30; bold values indicate the best-performing method per column. Statistically significant improvements over the best-performing baseline (paired t-test, p < 0.05) are indicated by an underline.

Budget	Method	P@10	Trave NDCG@10	P@30	NDCG@30	P@10		TREC P@30		P@10	Yelp Re NDCG@10			P@10	TripAdvi NDCG@10		
N/A	DPR BM25	$0.358 \\ 0.234$	0.365 0.238	$0.318 \\ 0.237$	0.333 0.239	$0.143 \\ 0.025$	0.161 0.032	$0.094 \\ 0.025$	0.165 0.038	0.363	$0.385 \\ 0.327$	$0.294 \\ 0.236$	$0.351 \\ 0.283$	0.224	$0.275 \\ 0.257$	$0.165 \\ 0.153$	0.349 0.325
25	LLM Reranking GPR-LLM	0.344 <b>0.370</b>	0.379 <b>0.402</b>	0.313 $0.325$	0.339 <b>0.356</b>	0.154 <b>0.159</b>	0.188 $0.192$	0.094 <b>0.098</b>	0.178 <b>0.183</b>	0.340 <b>0.359</b>	0.382 <b>0.397</b>	0.289 0.272	0.355 0.343	0.227 $0.286$	0.302 <b>0.378</b>	0.165 <b>0.177</b>	0.369 <b>0.419</b>
50	LLM Reranking GPR-LLM	0.380	0.419 <b>0.453</b>	0.298	0.339 <b>0.386</b>	0.171 <b>0.176</b>	0.215 <b>0.217</b>	0.098 <b>0.103</b>	0.193 <b>0.197</b>	$  {0.368} \atop {\bf 0.376}$	0.410 <b>0.414</b>	$0.282 \\ 0.286$	0.355 <b>0.361</b>	$0.251 \\ 0.325$	0.336 <b>0.423</b>	0.166	0.389 <b>0.470</b>
100	LLM Reranking GPR-LLM	0.428 <b>0.444</b>	0.467 <b>0.479</b>	0.323 $0.344$	0.371 <b>0.389</b>	0.214 $0.215$	0.245 <b>0.246</b>	0.102 $0.121$	0.200 <b>0.227</b>	$\begin{vmatrix} 0.391 \\ 0.430 \end{vmatrix}$	0.432 $0.472$	0.285	0.366 <b>0.398</b>	0.273 0.360	0.366 <b>0.476</b>	0.170	0.408 <b>0.535</b>

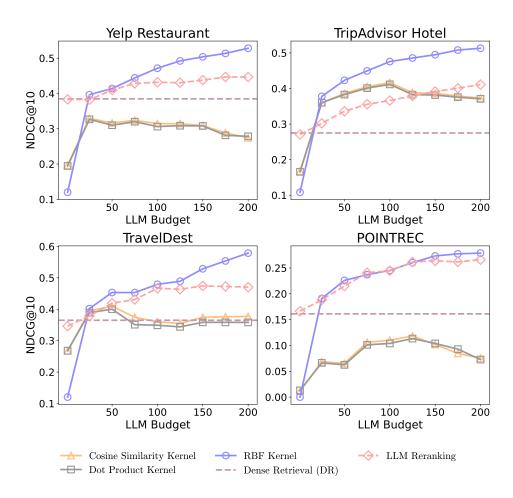


Figure 1: Performance comparison of different kernel functions with Greedy Sampling ( $\epsilon = 0$ ) under varying number of passages with LLM judgments (budget of LLM labels) with TAS-B embedding.

Table 3: Per-query time complexity and latency for different retrieval methods. Let N be the number of passages, D the embedding dimension, R the LLM budget, and  $C_{\text{LLM}}$  the cost of a single LLM scoring call. For GPR, the time complexity includes: kernel matrix computation  $\mathcal{O}(R^2D)$ , matrix inversion  $\mathcal{O}(R^3)$ , and inference over N passages  $\mathcal{O}(NRD)$ . We report empirical per-query latency (in seconds) under the following setup: R = 50, N = 100,000, using MinilM embeddings. Latency values include 95% confidence intervals in [-].

System specifications: CPU—Intel(R) Core(TM) i7-14700HX; GPU—NVIDIA GeForce RTX 4070 Laptop GPU; average CPU utilization during measurement: ∼5%.

Method	Per-query Complexity	Latency (sec)
DPR LLM Rerank		0.165 [0.161, 0.168] 0.678 [0.671, 0.685]
GPR-LLM	$O(ND + R \cdot C_{\text{LLM}} + R^2D + R^3 + NRD)$	Dot Product: 0.782 [0.769, 0.795] Cosine Similarity: 0.774 [0.762, 0.787] RBF Kernel: 0.754 [0.730, 0.780]