

# PyCUP--0.1.0 documentation

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Overview

Who uses PyCUP?

Open-access package

Install

Dependencies

Project structure

Tutorial

Importing the package and other dependencies

Defining an/a objective function/likelihood function

Defining the parameter upper & lower boundaries

Enjoy our algorithms

Save & Load the results

Raw results

Processed uncertainty analysis results

Parameter sensitivity analysis

Parameter uncertainty analysis

Calculate the P factor and R factor

Plot your results

Plot the 2D sample space

Plot the 3D sample space

Plot the 2D fitness space

Plot the 3D fitness space

Plot the optimization curve(s)

Plot the 2D Pareto front

Plot the 3D Pareto front surface

Plot the 2D multi-objective fitness space

Plot the 3D multi-objective fitness space

Plot the posterior distribution

Plot the 3D posterior distributions

Plot the 3D bar plots of normalized weights

Plot the uncertainty band

Plot a radar plot for sensitivity analysis results

The common parameter list of the plotting functions

Advanced utilizations

Elite opposition based strategy

Multi-processing algorithms

Multi-variable calibration (only available for single-objective algorithms in the current version)

How to apply our algorithms to modeling softwares?--Customize your objective function.

Validation and prediction

Saving the archive/record and resuming

Author's gift -- for some problems that you may meet when calibrating a model with executable.

Potential problem of multi-site or multi-event calibration

Examples

Example 1: using GWO to calibrate a testing function

Example 2: comparison between GLUE and swarm optimization algorithm

Example 3: using PSO to calibrate an SVR model

## Overview

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pycup is a python package for parameter optimization and uncertainty analysis of different kinds of models, such as machine learning models, hydrological models, and water quality models. Version 0.1.0 is the very first version of this package, and it will be improved continuously. Eleven swarm optimization algorithms (8 single-objective algorithms and 3 multi-objective algorithms) and GLUE (Generalized Likelihood Uncertainty Estimation) have been encapsulated in this version. When applying swarm optimization algorithms, this package considers parameter uncertainty instead of only obtaining the parameter with the best simulation performance in the calibration stage. Also, several improvements, including elite opposition theory and Latin hypercube sampling, have been integrated into those algorithms.

## Who uses PyCUP?

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Engineers, modelers, and researchers who are constructing models (especially hydrological models, hydraulic models, and water quality models) and want to quantify the parameter uncertainty. The functions of the package are especially compatible with environmental models, although it can also be used in other realms.

## Open-access package

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pycup is a free python package. Users can redistribute it and/or modify it under the terms of the license. We welcome contributions from the community. Also, we welcome feedbacks for any potential errors in the package.

## Install

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Please visit [pypi.org](https://pypi.org) to download the .whl file, or simply install it using:

```
pip install pycup
```

## Dependencies

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1. python > 3.0
2. numpy
3. scipy
4. matplotlib
5. pyDOE
6. statsmodels
7. multiprocessing
8. Anaconda 3 environment is strongly recommended

## Project structure

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## 1. Algorithms

<b>Module name</b>	<b>Description</b>
GLUE.py	Includes generalized likelihood uncertainty estimation method (1992) and its multi-processing version.
SSA.py	Includes sparrow search algorithm (2020) and its multi-processing version.
GWO.py	Includes gray wolf optimization algorithm (2014) and its multi-processing version.
MFO.py	Includes moth-flame optimization algorithm (2015) and its multi-processing version.
PSO.py	Includes particle swarm optimization (1995) and its multi-processing version.
SCA.py	Includes sine cosine algorithm (2016) and its multi-processing version.
SOA.py	Includes seagull optimization algorithm (2019) and its multi-processing version.
TSA.py	Includes tunicate swarm algorithm (2020) and its multi-processing version.
WOA.py	Includes whale optimization algorithm (2016) and its multi-processing version.
MOPSO.py	Multi-objective PSO and its multi-processing version based on non-dominated sort and archive.
MODE.py	Multi-objective differential evolution algorithm (2007) and its multi-processing version.
NSGA2.py	Non-dominated sorting genetic algorithm (2000) and its multi-processing version.

## 2. Calculation Auxiliaries & Post-processing

<b>Module name</b>	<b>Description</b>
evaluation_metrics.py	Includes several popular evaluation metrics such NSE, MAE, RMSE.
sampling.py	Includes the function for Latin hypercube sampling for population initialization.
plot.py	Includes functions for plotting posterior distributions, 95PPU bands, fitness curves, and sample spaces.

Module name	Description
uncertainty_analysis_fun.py	Includes functions for calculating the posterior distribution, uncertainty bands, and uncertainty evaluation metrics such as P factor and R factor.
utilize.py	Includes validator and predictor objects for validation and prediction related utilizations.

### 3. Others

Module name	Description
multi_jobs.py	Functions for parallel calculations.
progress_bar.py	Functions for showing a progress bar.
test_functions.py	CEC and author-defined testing functions.
save.py	Contains RawResult and OptResult saver objects.
utilize.py	Validator and Predictor object for validation and prediction.
template.py	Template functions for advanced utilization of pycup.

## Tutorial

### Importing the package and other dependencies

```
import pycup as cp
import numpy as np
```

### Defining an/a objective function/likelihood function

To use the optimization algorithms, firstly you should have an objective function (the optimization target). The function should have an X parameter, which is a numpy 1D array that contains all the parameters that you want to optimize. The function should contain 2 return values including the fitness value and the result 2D array.

$$fitness = \sum x_i^2$$

```
def uni_fun1(x):
    # X for example np.array([1,2,3,...,30])
    fitness = np.sum(np.power(x,2)) + 1 # example: 1.2
    result = fitness.reshape(1,-1) # example ([1.2,])

    return fitness,result
```

# Defining the parameter upper & lower boundaries

The upper and lower boundaries should be 1D numpy array.

```
lb = -100 * np.ones(30)
ub = 100 * np.ones(30)
```

## Enjoy our algorithms

The pop denotes the population size in each iteration, dim is the dimension of the parameter space (30 in this example), lb is the lower bound, ub is the upper bound, Max\_iter is the number of optimization iterations. The raw(optimization) data results (RawResult.rst) will be saved in your project folder. If you only want the best result and do not consider the parameter uncertainty, that is all you need.

```
cp.SSA.run(pop = 1000, dim = 30, lb = lb, ub = ub, MaxIter = 30, fun = uni_fun1)
```

For multi-objective optimization using MOPSO, the required arguments are slightly different:

```
import pycup as cp
import numpy as np

def mo_fun1(x):
    y1 = 1 - np.exp(-np.sum((x-1/np.sqrt(3))**2))
    y2 = 1 - np.exp(-np.sum((x+1/np.sqrt(3))**2))
    y3 = 1 - np.exp(np.sum((x**2 + np.sqrt(2))))
    fitness = np.array([y1,y2,y3]).reshape(1,-1)
    result = fitness
    return fitness,result

lb = np.array([-2, -2, -2])
ub = np.array([2, 2, 2])
cp.MOPSO.run(pop=100, dim=3, lb=lb, ub = ub, MaxIter=20,n_obj=3,nAr=300,M=50,
             fun=mo_fun1)
```

## Save & Load the results

The results are automatically saved in two binary files, which are "RawResult.rst" and "ProcResult.rst". Those files are located in your python project root folder. Also, users can define their specific result path and format.

### Raw results

Users can load the binary raw result file using the "RawResultSaver" object in the module "pycup.save". The returned value is a saver object that contains different unprocessed data including the historical samples generated by the algorithm. Users can also plot the sample spaces or fitness spaces directly using the functions in "pycup.plot" and this saver object (this will be introduced later). To load the raw result with default path and format:

```
from pycup import save

raw_res = save.RawDataSaver.load(r"RawResult.rst")
```

To define and load a raw result file:

```
from pycup import save
import pycup as cp
import numpy as np

def uni_fun1(x):
    # x for example np.array([1,2,3,...,30])
    fitness = np.sum(np.power(x,2)) + 1 # example: 1.2
    result = fitness.reshape(1,-1) # example ([1.2,])

    return fitness,result

lb = -100 * np.ones(30)
ub = 100 * np.ones(30)
save.raw_path = r"D:\example01.txt"
cp.SSA.run(pop = 1000, dim = 30, lb = lb, ub = ub, MaxIter = 30, fun = uni_fun1)
raw_res = save.RawDataSaver.load(r"D:\example01.txt")
```

A raw result saver object includes the following attributes:

Attribute name	Description	Data Type	Format/Shape
.historical_samples	The historical parameter samples generated by the algorithm.	numpy array	(iterations, pop, dim) for swarm opt algorithms; (iterations, dim) for GLUE
.historical_fitness	The fitness/likelihood function values of the corresponding samples.	numpy array	(iterations, pop, 1) for swarm opt algorithms; (iterations, 1) for GLUE
.historical_results	The simulation/calculation results of the corresponding samples.	numpy array	(iterations, pop, len(res)) for swarm opt algorithms; (iterations, len(res)) for GLUE
.GbestScore	The fitness value of the best sample found by the algorithm.	float	-
.GbestPosition	The best parameter sample found by the algorithm.	numpy array	(dim)
.Curve (GLUE doesn't have)	The optimization curve	numpy array	(iterations,)
.pareto_samples (only for MOPSO)	Samples of the Pareto optimal result set.	numpy array	(num. Pareto results, dim)
.pareto_fitness (only for MOPSO)	Fitness of the Pareto optimal result set.	numpy array	((num. Pareto results, 1)

Attribute name	Description	Data Type	Format/Shape
.pareto_results (only for MOPSO)	Pareto optimal result set.	numpy array	(num. Pareto results, pop, len(res))

Users can extract the data from the raw result saver object by:

```
import pycup as cp

raw_res = cp.save.RawDataSaver.load(r"RawResult.rst")
hs = raw_res.historical_samples
print(hs)
```

## Processed uncertainty analysis results

Users can load the binary optimization result file using the "ProcResultSaver" object in the module "pycup.save". The returned value is a saver object that contains different processed data including the historical results, posterior distributions, and uncertainty bands. Users can also plot the posterior distributions or uncertainty bands directly using the functions in "pycup.plot" and this saver object (this will be introduced later). To load the processed optimization results:

```
import pycup as cp

opt_res = cp.save.ProcResultSaver.load(r"ProcResult.rst")
```

To define and load an opt result file:

```
from pycup import save

save.proc_path = r"D:\example02.txt"
opt_res = save.ProcResultSaver.load(r"D:\example02.txt")
```

An optimization result saver contains the following attributes:

Attribute name	Sub attribute	Description	Data type	Format/shape
.historical_results	.historical_samples	The concatenated historical samples.	numpy array	(iterations * pop, dim) for swarm opt; (iterations, dim) for GLUE
	.historical_fitness	The concatenated historical fitness values.	numpy array	(iterations * pop, 1) for swarm opt; (iterations, 1) for GLUE

Attribute name	Sub attribute	Description	Data type	Format/shape
	.histroical_results	The concatenated historical simulation results.	numpy array	(iterations * pop, len(result)) for swarm opt; (iterations, len(result)) for GLUE
.best_result	.best_sample	The sample with the best fitness value.	numpy .array	(, dim)
	.best_fitness	The best fitness value.	float	-
	.best_result	The simulation result calculated using the best parameter sample.	numpy array	(1, len(result))
.behaviour_results	.behaviour_samples	The selected samples according the user defined threshold value. Typically, a sample with a fitness value lower (better) than the threshold is defined as a behaviour sample.	numpy array	(n_behaviour, dim)
	.behaviour_fitness	The fitness of selected behaviour samples.	numpy array	(n_behaviour, )
	.behaviour_results	The results of selected behaviour samples.	numpy array	(n_behaviour, len(result))
	.normalized_weight	The normalized likelihood weights of selected behaviour samples.	numpy array	(n_behaviour, )
.posterior_results	.sorted_sample_val	The sorted behaviour samples according to the sample value.	numpy array	(n_behaviour, dim)
	.cum_sample	The accumulative weights of sorted samples.	numpy array	(n_behaviour, dim)

Attribute name	Sub attribute	Description	Data type	Format/shape
.uncertain_results	.result_sort	The sorted results of selected behaviour samples according to the magnitude of the result value at each step. (for time series sim.)	numpy array	(n_behaviour, len(result))
	.cum_weight	The accumulative weights of sorted results at each step.	numpy array	(n_behaviour, dim)
	.ppu_line_lower	The lower boundary of the user defined confidence level (typically 95PPU)	numpy array	(, len(result))
	.ppu_line_upper	The upper boundary of the user defined confidence level (typically 95PPU)	numpy array	(, len(result))
	.line_min	The minimum values of the simulated	numpy array	(, len(result))
	.line_max	The maximum values of the simulated results of all the behaviour samples.	numpy array	(, len(result))
.pareto_result (only for MOPSO)	.pareto_samples	Samples of the Pareto optimal result set.	numpy array	(num. Pareto results, dim)
	.pareto_fitness	Fitness of the Pareto optimal result set.	numpy array	((num. Pareto results, 1)
	.pareto_results	Pareto optimal result set.	numpy array	(num. Pareto results, pop, len(res))

Users can extract and print the data from the opt result saver object by:

```
import pycup as cp

opt_res = cp.save.ProcResultsSaver.load(r"ProcResult.rst")
ppu_l = opt_res.uncertain_results.ppu_line_lower
print(ppu_l)
```

## Parameter sensitivity analysis

For parameter sensitivity analysis, use the sensitivity\_analysis function in uncertainty\_analysis\_fun module.

```
import pycup as cp
import pycup.uncertainty_analysis_fun as u_fun

raw_res = cp.save.RawDataSaver.load(r"RawResult.rst")
u_fun.sensitivity_analysis(raw_res)
```

For MOPSO, users should provide a single objective function index for sensitivity analysis (the shape of the fitness value is (pop\_size, n\_obj), but the multi-linear regression method only accept an unidimensional target). Users can specify the obj\_fun index by using the argument "objfun\_id" of sensitivity\_analysis function (the default index is 0):

```
import pycup as cp
import pycup.uncertainty_analysis_fun as u_fun

raw_res = cp.save.RawDataSaver.load(r"RawResult.rst")
u_fun.sensitivity_analysis(raw_res,objfun_id=1)
```

## Parameter uncertainty analysis

If you want to analyze the parameter uncertainty, use the likelihood\_uncertainty function in uncertainty\_analysis\_fun module. The result will be automatically saved in "ProcResult.rst" in your python project folder.

```
import pycup as cp
import pycup.uncertainty_analysis_fun as u_fun

raw_res = cp.save.RawDataSaver.load(r"RawResult.rst")
u_fun.likelihood_uncertainty(raw_res,threshold=0.5,ppu=0.95)
```

For MOPSO and GLUE with a multi-objective target function, use the function likelihood\_uncertaintyMO.

```
raw_res = cp.save.RawDataSaver.load(r"RawResult.rst")
u_fun.likelihood_uncertaintyMO(raw_res,n_obj=2,thresholds=[0.5,0.2],ppu=0.95,obj_weights=[0.5,0.5])
```

## Calculate the P factor and R factor

P factor and R factor are the most popular metrics for uncertainty evaluation. When calculating a P factor, you will need an observation data array. Users can call the "calc\_p\_factor" function in "uncertainty\_analysis\_fun" module to calculate the P factor.

```
import pycup.uncertainty_analysis_fun as u_fun
from pycup import save
import numpy as np
```

```

# assume that you have an observation data like this
obs_timestep = np.array([1,2,3,4,5,6,7])
obs_data = np.array([0.5,1.0,2.0,34.0,23.0,15.5,0.0])

# load your result and get the lower and upper ppu lines
opt_res = save.ProcResultsaver.load(r"ProcResult.rst")
ppu_l = opt_res.uncertain_results.ppu_line_lower
ppu_u = opt_res.uncertain_results.ppu_line_upper

# calculate the P factor
p = u_fun.calc_p_factor(upper=ppu_u, lower=ppu_l, obs_x=obs_timestep,
obs_y=obs_data)
print(p)

```

You can calculate the R factor using the function "calc\_r\_factor" in "uncertainty\_analysis\_fun" module.

```

import pycup.uncertainty_analysis_fun as u_fun
from pycup import save
import numpy as np

# load your result and get the lower ppu, upper ppu, max, and min lines
opt_res = save.ProcResultsaver.load(r"ProcResult.rst")
ppu_l = opt_res.uncertain_results.ppu_line_lower
ppu_u = opt_res.uncertain_results.ppu_line_upper

# your observation data (assume np.arange(100) here)
obs = np.arange(100)
# calculate the R factor
r = u_fun.calc_r_factor(upper=ppu_u, lower=ppu_l, obs=obs)
print(r)

```

## Plot your results

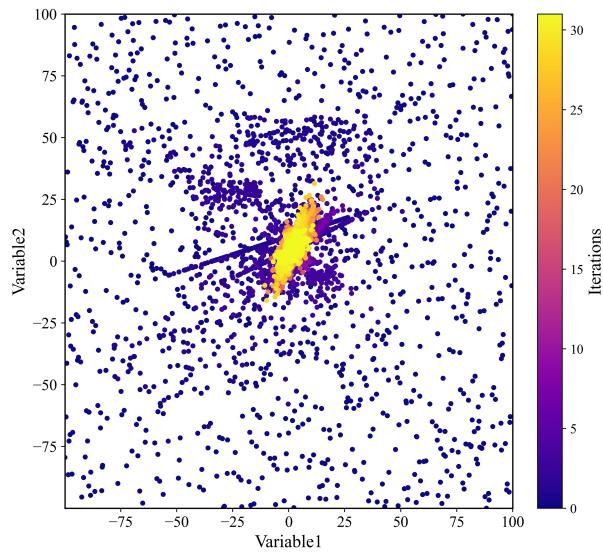
### Plot the 2D sample space

```

from pycup import save, plot

opt_res = save.RawDataSaver.load(r"RawResult.rst")
plot.plot_2d_sample_space(opt_res, variable_id1=0, variable_id2=1, obj_path="sample_space.jpg")

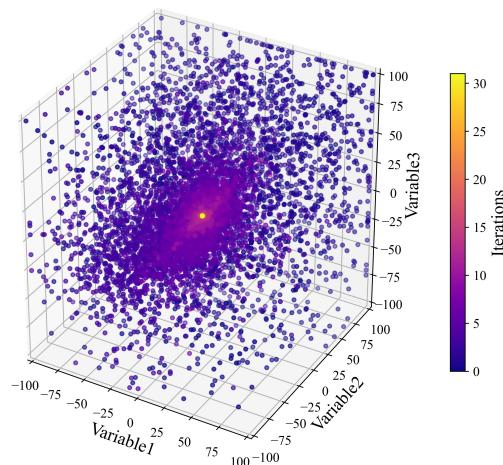
```



## Plot the 3D sample space

```
from pycup import save, plot

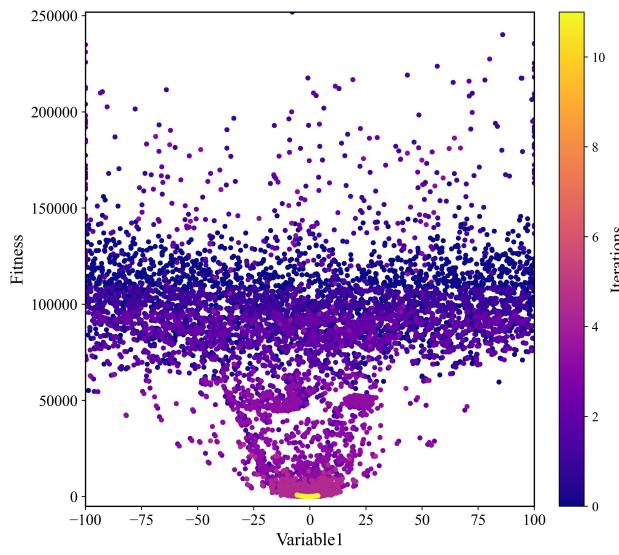
opt_res = save.RawDataSaver.load(r"RawResult.rst")
plot.plot_3d_sample_space(opt_res, variable_id1=0, variable_id2=1, variable_id3=2, o
bj_path="sample_space.jpg")
```



## Plot the 2D fitness space

```
from pycup import save, plot

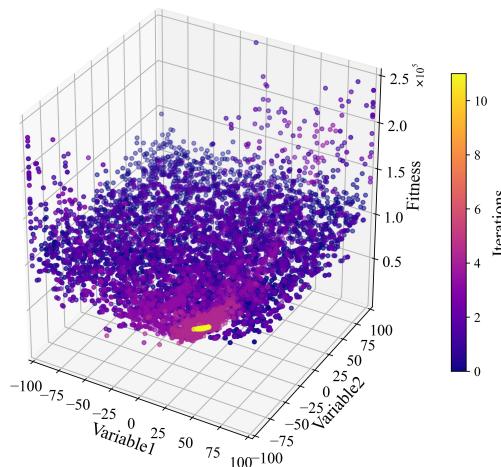
opt_res = save.RawDataSaver.load(r"RawResult.rst")
plot.plot_2d_fitness_space(opt_res, variable_id=1, y_lim=(0,))
```



## Plot the 3D fitness space

```
from pycup import save, plot

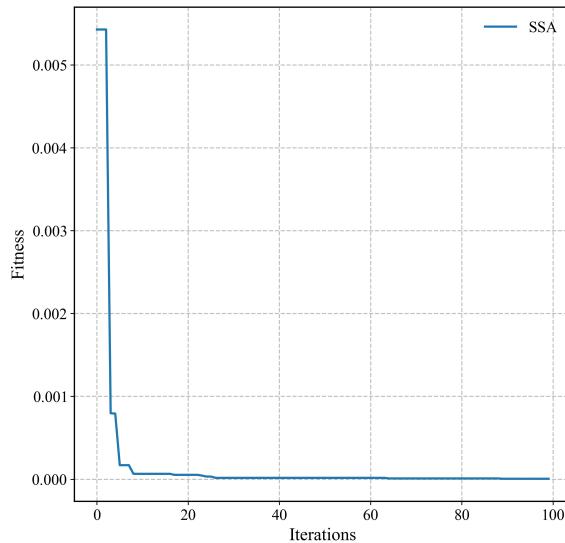
opt_res = save.RawDataSaver.load(r"RawResult.rst")
plot.plot_3d_fitness_space(opt_res, variable_id1=1, variable_id2=2, obj_path="sample_space.jpg")
```



## Plot the optimization curve(s)

```
from pycup import save, plot

raw_res1 = save.RawDataSaver.load(r"RawResult.rst")
plot.plot_opt_curves(raw_res1, slim=False, frameon=False, legendlabels=["SSA"], obj_path="opt_curves.jpg")
```

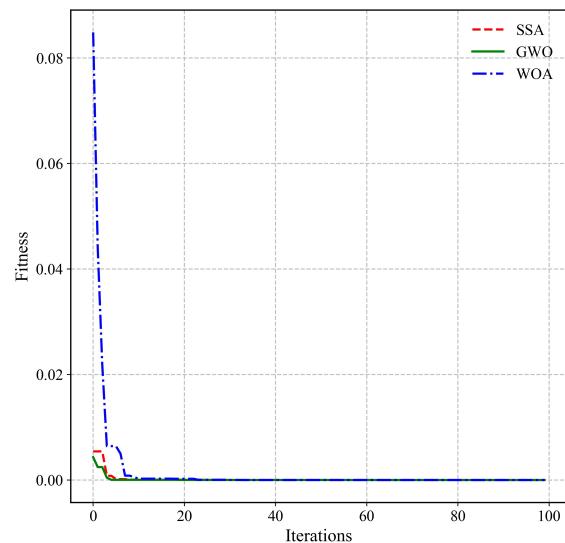


Or you can plot several optimization curves at the same time:

```
from pycup import save, plot

raw_res1 = save.RawDataSaver.load(r"RawResult1.rst")
raw_res2 = save.RawDataSaver.load(r"RawResult2.rst")
raw_res3 = save.RawDataSaver.load(r"RawResult3.rst")
raw_res = [raw_res1, raw_res2, raw_res3]

plot.plot_opt_curves(raw_res, slim=False, frameon=False, legendlabels=
["SSA", "GWO", "WOA"], linestyle=["--", "-.", "-"], colors=
["r", "g", "b"], obj_path="opt_curves.jpg")
```



## Plot the 2D Pareto front

```
import pycup as cp
import numpy as np
from pycup import plot, save

def mo_fun1(X):
    y1 = 1 - np.exp(-np.sum((X-1)/np.sqrt(3))**2)
    y2 = 1 - np.exp(-np.sum((X+1)/np.sqrt(3))**2)
    fitness = np.array([y1,y2]).reshape(1,-1)
```

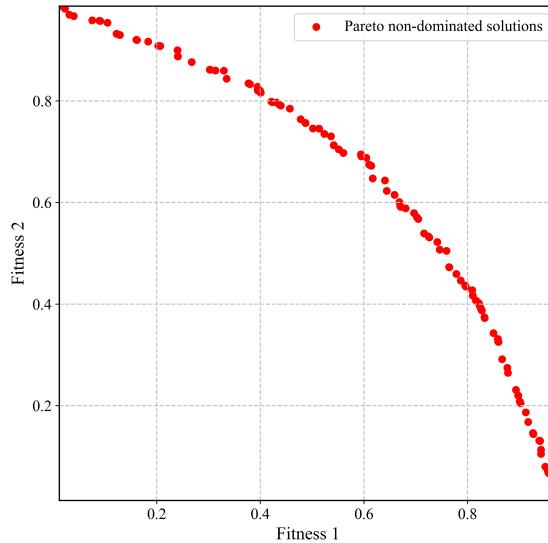
```

        result = fitness
        return fitness,result

lb = np.array([-2, -2, -2])
ub = np.array([2, 2, 2])
cp.MOPSO.run(pop=100, dim=3, lb=lb, ub = ub, MaxIter=20,n_obj=2,nAr=300,M=50,
             fun=mo_fun1)

path = "RawResult.rst"
saver = save.RawDataSaver.load(path)
plot.plot_2d_pareto_front(saver,objfunid1=0,objfunid2=1,obj_path="pareto2d.pdf")

```



## Plot the 3D Pareto front surface

```

import pycup as cp
import numpy as np

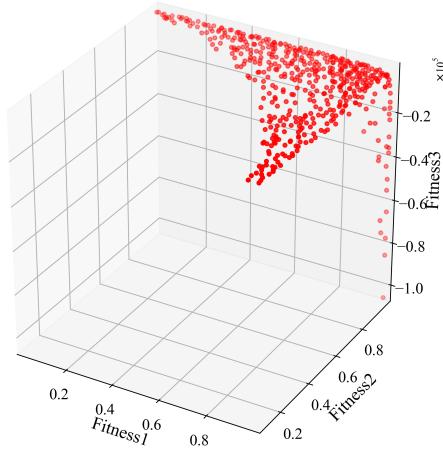
def mo_fun1(x):
    y1 = 1 - np.exp(-np.sum((x-1/np.sqrt(3))**2))
    y2 = 1 - np.exp(-np.sum((x+1/np.sqrt(3))**2))
    y3 = 1 - np.exp(np.sum((x**2 + np.sqrt(2))))
    fitness = np.array([y1,y2,y3]).reshape(1,-1)
    result = fitness
    return fitness,result

lb = np.array([-2, -2, -2])
ub = np.array([2, 2, 2])
cp.MOPSO.run(pop=100, dim=3, lb=lb, ub = ub, MaxIter=20,n_obj=3,nAr=300,M=50,
             fun=mo_fun1)

from pycup import plot,save

path = "RawResult.rst"
saver = save.RawDataSaver.load(path)
plot.plot_3d_pareto_front(saver,objfunid1=0,objfunid2=1,objfunid3=2,obj_path="pa
reto3d.pdf")

```



## Plot the 2D multi-objective fitness space

This function is to plot the searching history from the aspect of fitness for the multi-objective functions. By plotting this, users can see that the population is getting close to the Pareto front.

```

import pycup as cp
import numpy as np

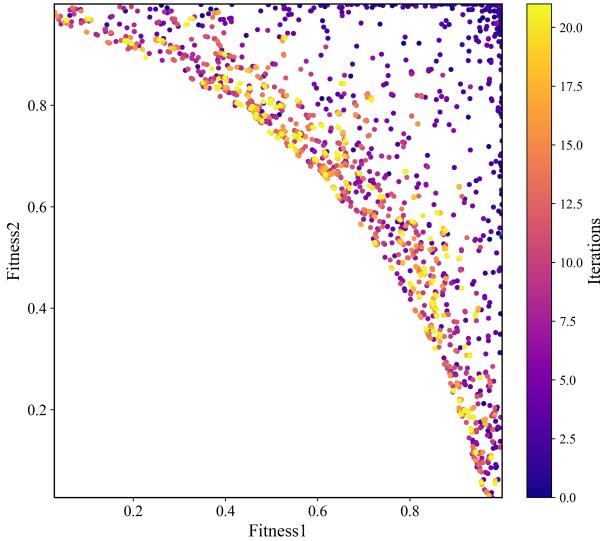
def mo_fun1(x):
    y1 = 1 - np.exp(-np.sum((x-1/np.sqrt(3))**2))
    y2 = 1 - np.exp(-np.sum((x+1/np.sqrt(3))**2))
    fitness = np.array([y1,y2]).reshape(1,-1)
    result = fitness
    return fitness,result

lb = np.array([-2, -2, -2])
ub = np.array([2, 2, 2])
cp.MOPSO.run(pop=100, dim=3, lb=lb, ub = ub, MaxIter=20,n_obj=2,nAr=300,M=50,
             fun=mo_fun1)

from pycup import plot,save

path = "RawResult.rst"
saver = save.RawDataSaver.load(path)
plot.plot_2d_mo_fitness_space(saver,objfunid1=0,objfunid2=1)

```



## Plot the 3D multi-objective fitness space

```

import pycup as cp
import numpy as np

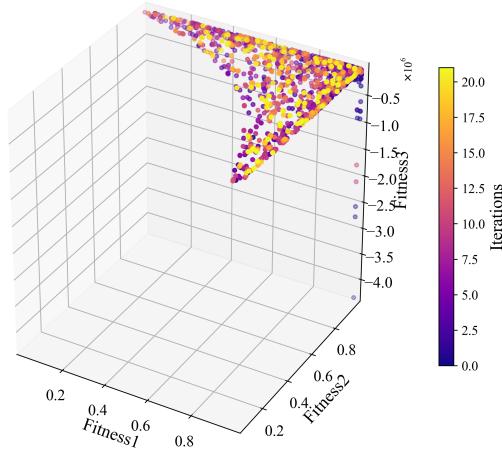
def mo_fun1(x):
    y1 = 1 - np.exp(-np.sum((x-1/np.sqrt(3))**2))
    y2 = 1 - np.exp(-np.sum((x+1/np.sqrt(3))**2))
    y3 = 1 - np.exp(np.sum((x**2 + np.sqrt(2))))
    fitness = np.array([y1,y2,y3]).reshape(1,-1)
    result = fitness
    return fitness,result

lb = np.array([-2, -2, -2])
ub = np.array([2, 2, 2])
cp.MOPSO.run(pop=100, dim=3, lb=lb, ub = ub, MaxIter=20,n_obj=3,nAr=300,M=50,
             fun=mo_fun1)

from pycup import plot,save

path = "RawResult.rst"
saver = save.RawDataSaver.load(path)
plot.plot_3d_mo_fitness_space(saver,objfunid1=0,objfunid2=1,objfunid3=2)

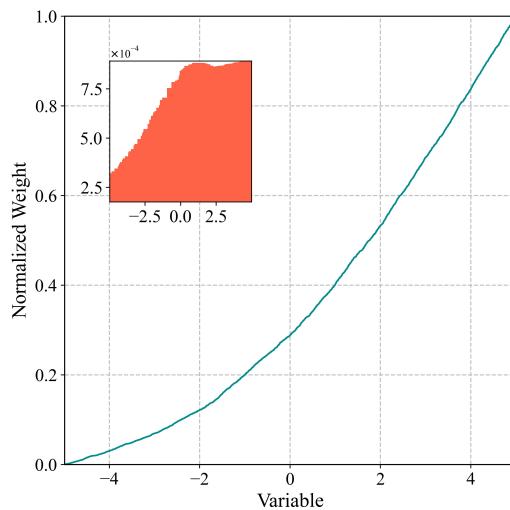
```



## Plot the posterior distribution

```
from pycup import save, plot

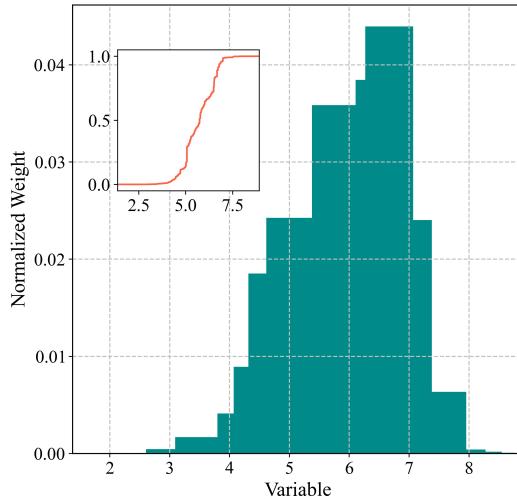
opt_res = save.ProcResultsaver.load(r"ProcResult.rst")
plot.plot_posterior_distribution(opt_res, variable_id=1, obj_path="dis.jpg")
```



You can reverse your main plot and the subplot by setting the "reverse" parameter equal to True.

```
from pycup import save, plot

opt_res = save.ProcResultsaver.load(r"ProcResult.rst")
plot.plot_posterior_distribution(opt_res, variable_id=1, obj_path="dis.jpg", reverse=True)
```

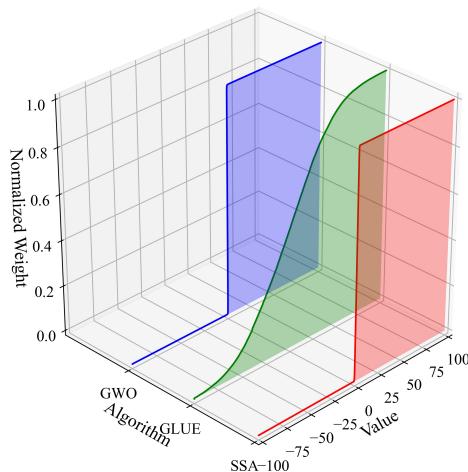


## Plot the 3D posterior distributions

This function is for users to make a comparison between the posterior distributions obtained from different algorithms.

```
from pycup import save, plot

res1 = save.ProcResultSaver.load(r"ProcResult1.rst")
res2 = save.ProcResultSaver.load(r"ProcResult2.rst")
res3 = save.ProcResultSaver.load(r"ProcResult3.rst")
r_list = [res1, res2, res3]
plot.plot_3d_posterior_distributions(r_list, variable_id=0, obj_path="dis3d.jpg", y
_ticklabels=["SSA", "GLUE", "GWO"])
```



## Plot the 3D bar plots of normalized weights

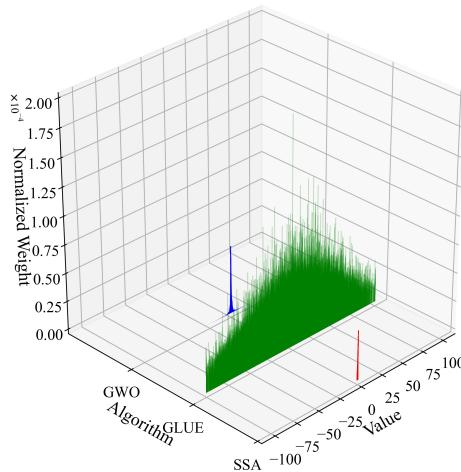
This function is for users to make a comparison between the normalized weights obtained from different algorithms.

```

from pycup import save, plot

res1 = save.ProcResultSaver.load(r"ProcResult1.rst")
res2 = save.ProcResultSaver.load(r"ProcResult2.rst")
res3 = save.ProcResultSaver.load(r"ProcResult3.rst")
r_list = [res1, res2, res3]
plot.plot_3d_posterior_bars(r_list, variable_id=0, obj_path="dis3d.jpg", y_ticklabels=[["SSA", "GLUE", "GWO"]])

```



## Plot the uncertainty band

```

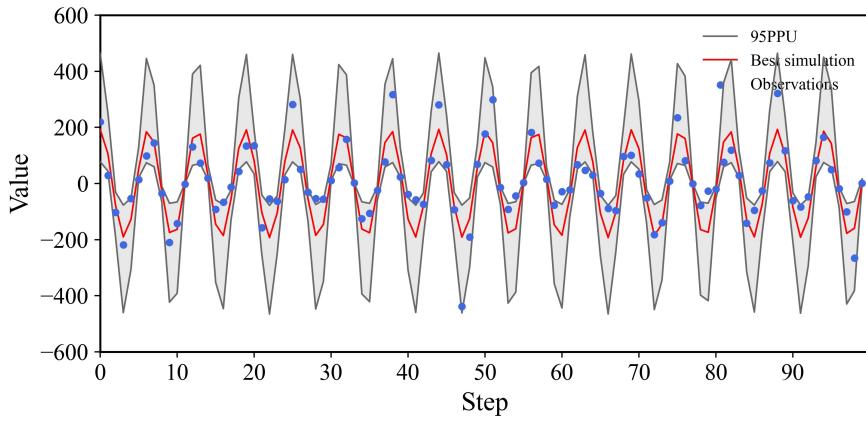
from pycup import save, plot
import numpy as np
import random

# load the result
opt_res = save.ProcResultSaver.load(r"ProcResult.rst")

# simulate an observation data array (in this example)
t = np.arange(0, 100)
res = []
for i in t:
    obs = np.sin(i) * (2.1 + np.random.randn()) + np.cos(i) * (5.2 +
    np.random.randn()) ** 3 + random.random()
    res.append(obs)

# plot the uncertainty band
plot.plot_uncertainty_band(opt_res, t, res, ylim=(-600, 600),
                           ticklocs=np.arange(0, 100, 10), legendloc=1)

```



To specify a time axis, users can use the function "get\_time\_labels" in the plot module.

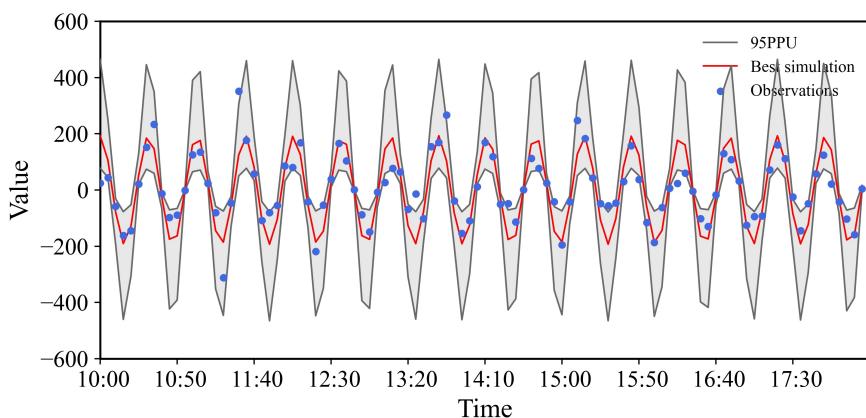
```
from pycup import save, plot
import numpy as np

# Load the result
opt_res = save.ProcResultSaver.load(r"ProcResult.rst")

# simulate an observation data array (in this example)
t = np.arange(0,100)
res = []
for i in t:
    obs = np.sin(i) * (2.1 + np.random.randn()) + np.cos(i) * (5.2 +
np.random.randn()) ** 3 + random.random()
    res.append(obs)

# customize your time tick label
xticks = plot.get_time_labels("2021-12-01
10:00:00",100,showY=False,showdate=False,shows=False)[::10]

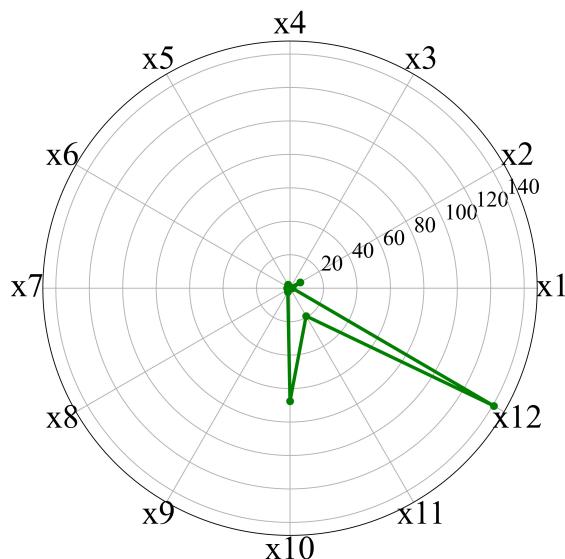
# plot the uncertainty band
plot.plot_uncertainty_band(opt_res,t,res,ylim=
(-600,600),ticklocs=np.arange(0,100,10),xticks=xticks,x_label="Time",legendloc=1
,obj_path="band.jpg")
```



## Plot a radar plot for sensitivity analysis results

Plot a radar plot for t-stats of the parameter sensitivity (based on multi-linear regression method).

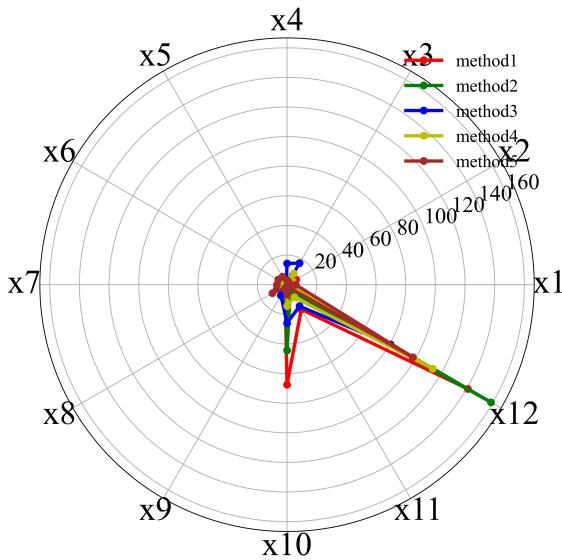
```
from pycup import save
import pycup as cp
# Load the raw optimization result saver, the
r1 = cp.save.RawDataSaver.load("RawResult.rst")
# plot: 0 -> plot the t-stats, 1 -> plot the p-values
cp.plot.plot_radar_sensitivity(r1,objfun_id=0,plot=0,linewidth=3,parameter_labels
s=["x1", "x2", "x3", "x4", "x5", "x6", "x7", "x8", "x9", "x10", "x11", "x12"])
```



Plot a radar plot for several sensitivity analysis results of different algorithms.

```
from pycup import save
import pycup as cp

r1 = cp.save.RawDataSaver.load("RawResultGLUE.rst")
r2 = cp.save.RawDataSaver.load("RawResultPSO.rst")
r3 = cp.save.RawDataSaver.load("RawResultSSA.rst")
r4 = cp.save.RawDataSaver.load("RawResultGWO.rst")
r5 = cp.save.RawDataSaver.load("RawResultNSGA2.rst")
cp.plot.plot_radar_sensitivity([r1, r2, r3, r4, r5], 0, 0, linewidth=3,
frameon=False,
parameter_labels=
["x1", "x2", "x3", "x4", "x5", "x6", "x7", "x8", "x9", "x10", "x11", "x12"],
legend_labels=
["method1", "method2", "method3", "method4", "method5"])
```



## The common parameter list of the plotting functions

Parameter name	Description	Data type/Format	Default value
raw_saver/proc_saver	The raw result saver/optimization result saver object generated by the saver.load() method.	object	N/A (required)
variable_id/variable_id1/variable_id2	The index of the parameter that you want to be plotted.	int	N/A (required)
obj_path	The target file path that you want to save the plot.	str	Varies according to the function.
figsize	The size of the canvas.	tuple	(8, 8); (8, 4) for the uncertainty band function.
dpi	The resolution of the figure.	int	400
title	The title of the plot.	str	" "
lbl_fontsize	The font size of axis labels.	int/float	16
marker	The type of the marker in a scatter plot.	str	"."
markersize	The size of the marker in a scatter plot.	int/float	50
x_label/y_label/z_label	The x/y/z axis label.	str	Varies according to the function.
tick_fontsize	The font size of tick labels.	int/float	14
tick_dir	The direction of ticks.	str ("in" or "out")	"out"
framewidth	The line width of the frame of the graph.	int/float	1.2

Parameter name	Description	Data type/Format	Default value
cmap	The color map of the scatter plot rendered by the iteration values. Please see the matplotlib.cmap for more options.	str	"plasma"
single_c	The color of the dots in a scatter plot when the iteration values are not available (e.g. GLUE).	str	"b"/"blue"
cbar_ttl	The title of the color bar.	str	"Iterations"
cbar_ttl_size	The font size of the color bar title.	int/float	16
cbar_lbl_size	The font size of the color bar tick labels.	int/float	12
cbar_frac	The size of the color bar.	float	0.05/0.03
cbar_pad	The gap between the color bar and your graph	float	0.05
x_lim/y_lim/z_lim	The lower and upper bound of the axes that you want to show.	tuple for example (-100,100)	()
slim	When this param is True, the program will automatically detect your x_lim/y_lim/z_lim	bool	True
tight	When this param is True, the program will automatically remove the redundant white edges.	bool	True; False for the uncertainty band function.
show	When this param is True, the graph will be shown in your IDE. (plt.show())	bool	True
view_init (only for 3D plot functions)	The visual angle.	tuple (elev, azim)	()
pad (only for uncertainty band plotting function)	The magnitude of your frame.	tuple	(0.1,0.15,0.9,0.85)
xtick_rotation/xtick_rotation (only for uncertainty band plotting function)	Rotate your tick labels.	int/float	0
bestlinewidth/bandlinewidth (only for the uncertainty band plotting function)	Line width.	int/float	1
legendloc (only for the uncertainty band plotting function)	The location of your legend in your graph.	int (0~8)	0
frameon (only for the uncertainty band plotting function)	The switch of your legend frame.	bool	False

Parameter name	Description	Data type/Format	Default value
subon (only for the uncertainty band plotting function)	The switch of your subplot.	bool	True
barwidth (only for the uncertainty band plotting function)	The bar width of the bar plot.	float/int	0.8
grid/subgrid (only for the posterior distribution plotting function)	The switch of grid lines in the plot/subplot.	bool	True
gridwidth/subgridwidth (only for the posterior distribution plotting function)	The width of grid lines in the plot/subplot.	int/float	1.0
color/subcolor (only for the posterior distribution plotting function)	The color of bars/lines in the plot.	str	"darkcyan"/"tomato"
reverse (only for the posterior distribution plotting function)	To reverse the order of your plot and subplot.	bool	False
subloc (only for the posterior distribution plotting function)	The location of the subplot.	int (0~8)	0 (top right)
gap, subgap, subsizex, subsizey, subframewidth (only the for posterior distribution plotting function)	graph property modification parameters.	float < 1.0	Varies according to the parameter.
idx	slice positions	a list/tuple of 2 elements	None

## Advanced utilizations

### Elite opposition based strategy

Elite opposition is a search technique to make the algorithm more convergent. Use SSA as an example to open the elite opposition function, set the global variable "EliteOppoSwitch" equal to True. Users can set the ratio of individuals that execute the elite opposition operation using the module variable named "OppoFactor". The default value of it is 0.1, which denotes that the top 10% of total individuals (elite samples) will execute the elite opposition operation, in other words, 10% more calculations will be appended to each iteration.

```
import pycup as cp
import numpy as np

lb = -100 * np.ones(30)
ub = 100 * np.ones(30)

cp.SSA.EliteOpposwitch = True
cp.SSA.OppoFactor = 0.05
cp.SSA.run(pop=3000, dim=30, lb=lb, ub = ub,
MaxIter=10, fun=cp.test_functions.uni_fun6)
```

Not all the algorithms support the elite opposition based learning in the current version.

Algorithms	Support elite opposition in pycup?
GLUE	False
SSA	True
GWO	True
MFO	True
PSO	True
SCA	True
SOA	True
TSA	True
WOA	True
MOPSO	True
MODE	False
NSGA2	False

## Multi-processing algorithms

Each algorithm that we collected has its multi-processing version. Users can call a multi-processing function using:

```
import numpy as np
from pycup import SSA
from pycup import test_functions

# When using a multi-processing version, please always add the "if __name__ ==
 "__main__":
if __name__ == "__main__":
    lb = -100 * np.ones(2)
    ub = 100 * np.ones(2)
    SSA.runMP(1000, 2, lb, ub, 30, test_functions.ts_fun2,n_jobs=5)
```

Please note, for simple testing functions, the multiprocessing version would not improve the speed of the algorithm, that is because the opening and closing operations of processes are time-consuming. However, when your objective function contains a long computational blocking (e.g. a hydraulic model), the multi-processing function will be a powerful tool.

If you want to develop an executable program (.exe) based on our package, please always call the "freeze\_support" function in multiprocessing.

```

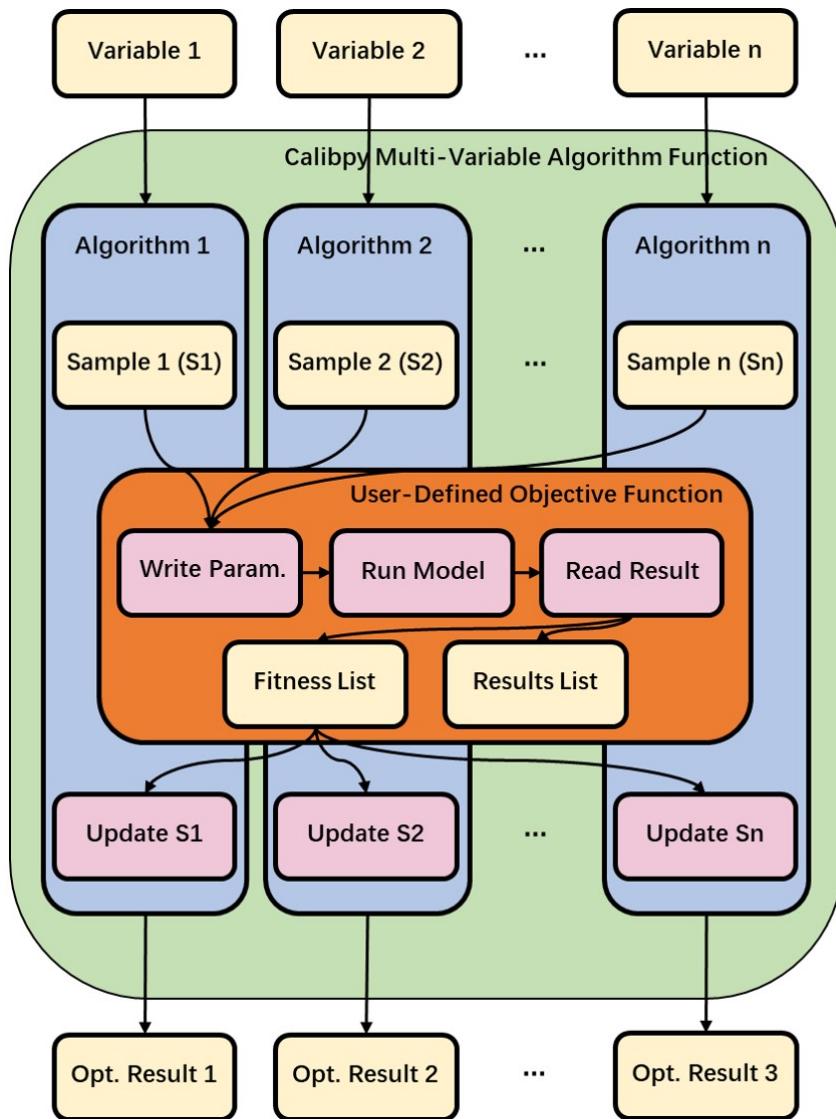
import numpy as np
from pycup import SSA
import multiprocessing as mp
from pycup import test_functions

if __name__ == "__main__":
    mp.freeze_support()
    lb = -100 * np.ones(2)
    ub = 100 * np.ones(2)
    SSA.runMP(1000, 2, lb, ub, 30, test_functions.ts_fun2,n_jobs=5)

```

## Multi-variable calibration (only available for single-objective algorithms in the current version)

Sometimes we would have several independent variables that we want to calibrate simultaneously in a model, thus, the problem becomes to a multi-variable optimization problem. For instance, in water quality simulation, sometimes we would treat the chemical oxygen demand (COD, concentration in mg/L) and the total nitrogen (TN, concentration in mg/L) as two independent variables. Then, the decay rates of these two variables are two independent parameters that need different metrics to evaluate their estimation accuracies. In pycup, we provide multi-variable version of all the algorithms for this type of problems. The user defined objective function should return a fitness list that contains the evaluation metrics of all the variables, as well as a result list that contains the estimation results of all the variables. The optimization algorithm is carried out separately for each variable, however, since your model can calculate those variables simultaneously, you do not need to run your model for twice or more to calibrate the variables separately. The following flowchart may help for understanding the mechanism of this process.



To use the multi-variable calibration function:

```

import pycup as cp
import numpy as np
"""

2 variables
For this function, we actually have two numerical models, therefore, the
calibration
duration will not be reduced. However, for a real world model, typically, x1 and
x2
are calculated at the same time in a simulation program.
"""

def mv_fun1(xs):
    x1 = xs[0]
    fitness1 = 4*x1[0]**2 - 2.1*x1[0]**4 + (x1[0]**6)/3 + x1[0] * x1[1] -
    4*x1[1]**2 + 4*x1[1]**4 + 2
    result1 = fitness1.reshape(1, -1)

    x2 = xs[1]
    fitness2 = (x2[1] - (5.1/(4*np.pi**2))*x2[0]**2 + (5/np.pi)*x2[0] - 6)**2 +
    10*(1-1/(8*np.pi)*np.cos(x2[0])) + 10
    result2 = fitness2.reshape(1, -1)

    fitness = [fitness1,fitness2]
    results = [result1,result2]

```

```

    return fitness,results

# define the lb and ub for variable x1
lb1 = -5 * np.ones(2)
ub1 = 5 * np.ones(2)
# define the lb and ub for variable x2
lb2 = -5 * np.ones(2)
ub2 = 5 * np.ones(2)
lbs = [lb1,lb2]
ubs = [ub1,ub2]
cp.WOA.EliteOpposwitch = True
"""
Define the result paths (optional). If not defined, the results will be saved
in the root folder of the project as "RawResult_Var1.rst", "RawResult_Var2.rst"
and "OptResult_Var1.rst", "OptResult_Var2.rst"
"""
cp.save.proc_pathMV = ["v1.rst", "v2.rst"]
cp.save.raw_pathMV = ["v1raw.rst", "v2raw.rst"]
# params: pop, dim list, lb list, ub list, iterations,threshold list, ppu list,
obj
cp.WOA.run_MV(300,[2,2],lbs,ubs,10,mv_fun1)

```

To run a multi-processing version of this:

```

if __name__ == "__main__":
    cp.WOA.runMP_MV(300,[2,2],lbs,ubs,10,cp.test_functions.mv_fun1,n_jobs=5)

```

For a real world model (take a water quality as the example), the template(pseudo) code would be:

```

import pycup as cp
from pycup.evaluation_metrics import MAE
import numpy as np
import os

def write_param(param_file_path, COD_param, TN_param):
    ...
    ...

def read_result(res_file_path):
    ...
    return COD_timeseries, TN_timeseries

def run_model(f_model, f_sim):
    cmd = f_model + " " + f_sim
    ret = os.system(cmd)
    return ret

# assume a water quality model for COD and TN simulation
# obs -> observation data
def
obj(x_list,model_exe_path,project_file_path,param_file_path,res_file_path,obs):
    COD_param = x_list[0]

```

```

TN_param = X_list[1]
write_param(param_file_path, COD_param, TN_param)
run_model(model_exe_path, project_file_path)
COD_timeseries, TN_timeseries = read_result(res_file_path)
obs_COD = obs[0]
obs_TN = obs[1]
fitness_COD = MAE(obs_COD, COD_timeseries)
fitness_TN = MAE(obs_TN, TN_timeseries)

# shape requirement
COD_timeseries = COD_timeseries.reshape(1, -1)
TN_timeseries = TN_timeseries.reshape(1, -1)

fitness = [fitness_COD, fitness_TN]
result = [COD_timeseries, TN_timeseries]

return fitness, results

if __name__ == "__main__":
    model_exe_path = ...
    project_file_path = ...
    param_file_path = ...
    res_file_path = ...
    obs = np.array([.....])

    lb_COD_decay = np.array([0])
    ub_COD_decay = np.array([10])

    lb_TN_decay = np.array([0])
    ub_TN_decay = np.array([5])

    lbs = [lb_COD_decay, lb_TN_decay]
    ubs = [ub_COD_decay, ub_TN_decay]

    WOA.EliteOpposwitch = True

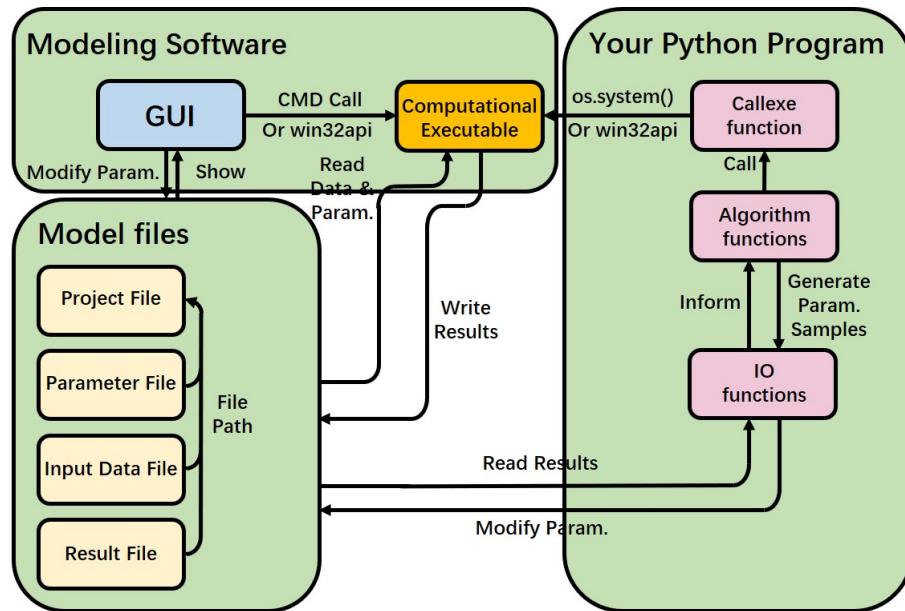
    cp.WOA.runMP_MV(300, [1,1], lbs, ubs, 10, obj, n_jobs=5, args =
(model_exe_path, project_file_path, param_file_path, res_file_path, obs))

```

## How to apply our algorithms to modeling softwares?--Customize your objective function.

In the practical situation, some models might have been compiled as executable software with a GUI (user interface). However, these softwares generally have a core computational engine, which is an executable (.exe) in the installation folder (typically, the "bin" folder). For instance, the SWMM (swmm5.exe, or one can also use pyswmm [<https://pypi.org/project/pyswmm/>] to control it), VIC, BTOPMC (YHyM132.exe), Flo2D (FLOPRO.exe), and DHI MIKE 11 (mike11.exe). The GUI usually act as an auxiliary tool for the users to construct/modify their models/parameters. After the model construction stage, the GUI is not necessary anymore, although users can press the button "run" in the GUI to execute their simulations. When pressing the "run" button, the GUI is actually calling the computational executable and sending it the message about the current simulation project file. However, this action can also be done automatically by your "CMD" shell command/python (os.system(cmd)). Users can write several functions using python to automatically modify the parameter, run the simulation, read the result, calculate the

performance metrics, and then repeat these processes. Combining with the optimization algorithms, users can actively modify the parameters to obtain a better modeling performance. Here is a conceptual graph that demonstrates the relationships between the modeling software, your model files, and your auto-calibration python program:



To develop an auto-calibration program using pycup, basically, you should know:

1. How to read and write (this is more important) your model's parameter file.
2. How to call your model executable using the command line (CMD).
3. How to read your simulation results.

Then, you will need to define your objective function, which is capable of the above-mentioned bullets.

The following codes contain some template functions, which are necessary for the auto-calibration program. These template codes may help you with understanding and developing your auto-calibration program. The objective function in the template receives the parameter sample generated by our algorithms and returns the fitness value as well as the simulation results. **It writes the parameters into their corresponding parameter files, executes the computational executable, reads the result, and calculates the fitness value.** This function may need extra function parameters such as model parameter file path, simulation file path, and executable path. Users can simply put these things into the tuple parameter "args" of the algorithm function. Then, the parameters will be sent to your objective function using the \*args method. Please carefully read the following codes.

```

import os
import pycup.evaluation_metrics
import multiprocessing as mp
import calipy as cp
import pycup.uncertainty_analysis_fun as ufun

# very important
def template_obj_fun(x, execute, fsim, fparam, fres, obs):
    """
    This is a template objective function for single process algorithms.
    :param x: your sample
    :param execute: your model executable file

```

```

:param fsim: your simulation project file, typically, you can directly call
your      model using cmd => executable_file_path simulation_project_file_path
:param fparam: your parameter file path
:param fres: your result file path
:param obs: your observation data array
:return: the fitness/liklihood function value, the result array

NOTE:
x is generated by the algorithm,
execute, dir_proj, fnsim,fnparam, fnres,obs,n_jobs, these parameters should
be
provided by the "args" parameter of the algorithm function.

e.g.
cp.SSA.SSA(..., args=(execute, dir_proj, fnsim,fnparam, fnres,obs,n_jobs))
"""

write_param(x,fparam)
callexe(execute,fsim)
res = read_result(fres)
nse = pycup.evaluation_metrics.OneMinusNSE(obs,res)
return nse,res

# very important
def template_obj_fun_mp(x, execute, dir_proj, fnsim,fnparam, fnres,obs,n_jobs):
"""
This is a template objective function for multi-processing algorithms.
:param x: the parameter array
:param execute: the path of your modeling software executable, it should be
the      "core" of your model, in other words, the executable for
calculation. (NOT THE GUI-      USER INTERFACE EXECUTABLE)
:param dir_proj: the folder of your simulation project r'hydro_simulation' in
this      template
:param fnparam: the name/relative path (not the abs path) of your parameter
file      (e.g. "para.txt")
:param fnres: the name/relative path (not the abs  path) of your result file
(e.g.      "result.res")
:param obs: the observation data array
:param n_jobs: number of threads (processes)
:return:

NOTE:
x is generated by the algorithm,
execute, dir_proj, fnsim,fnparam, fnres,obs,n_jobs, these parameters should
be
provided by the "args" parameter of the algorithm function.

e.g.
cp.SSA.SSA_MP(...,args=(execute, dir_proj, fnsim,fnparam, fnres,obs,n_jobs))
"""

process_id = mp.current_process().name.split("-")[-1]
"""

Allocate the folder id for parallel simulations.

```

```
Users can create several folders to simulate parallelly in case of potential
conflicts between different simulations. By doing this, the
program can write the param and read the result separately according to the
process-id.
```

```
For example:
```

```
If you have 4 processes (n_jobs = 4), you can copy your simulation
project into 4
seperate folders and renamed them:
```

```
r'hydro_simulation\\process1\\'
r'hydro_simulation\\process2\\'
r'hydro_simulation\\process3\\'
r'hydro_simulation\\process4\\'
```

```
when optimizing, if the process-id is 0013,
then, its corresponding folder id will be  $13 \% 4 = 1 + 1 = 2$ 
the params and results will be written in r'hydro_simulation\\process2\\'
"""

```

```
folder_id = int(process_id) % n_jobs + 1
process_folder = dir_proj + r"\\"+process{}\".format(folder_id)
```

```
f_param = process_folder + fnparam
write_param(x, f_param)
```

```
f_sim = process_folder + fnsim
callexe(execute,f_sim)
```

```
f_res = process_folder + fnres
res = read_result(f_res)
```

```
nse = pycup.evaluation_metrics.NSE(obs, res)
return nse, res
```

```
def callexe(f_model, f_sim):
```

```
"""

```

```
Call the model executable using this function.
Sometimes the process will return a code to show whether the
simulation is successfully completed or not.
```

```
Our program assumes that your model is good and does not have
fatal error.
"""

```

```
cmd = f_model + " " + f_sim
ret = os.system(cmd)
```

```
return ret
```

```
def write_param(param,fparam):
```

```
# Write your parameters into your parameter file.
pass
```

```
def read_result(fres):
```

```

"""
...
fres => res
"""

result = np.array(res).reshape(1,-1)
return result


if __name__ == "__main__":
    # define lb and ub, other settings
    lb = np.array([0,0,0,0,-5])
    ub = np.array([10,20,10,10,5])
    cp.SSA.EliteOpposwitch = True
    cp.SSA.OppoFactor = 0.05

    # define extra objective function parameters
    executable = r"D:\hydrological_model.exe"
    dir_proj = r"D:\hydrological_simulation"
    fnsim = r"simulation.txt"
    fnparam = r"params\hdparam.txt"
    fnres = r"results\res.txt"

    # read the calibration data
    with open(r"obsdata.txt",r) as f:
        obs = f.readlines()
    obs_array = np.array(obs)

    """
The algorithm function will call your objective function and send your extra
parameters through the *args method

then you have:
template_obj_fun_mp(x,executable,dir_proj,fnsim,fnparam,fnres,obs_array)
which is what you have defined.
"""

cp.SSA.runMP(pop=300, dim=5, lb=lb, ub = ub, MaxIter=30,
fun=template_obj_fun_mp,n_jobs=5,args=
(executable,dir_proj,fnsim,fnparam,fnres,obs_array))
raw_res = cp.save.RawDataSaver.load("RawResult.rst")
ufun.likelihood_uncertainty(raw_res,threshold=0.2,ppu=95)

```

## Validation and prediction

In practical situations, models, especially hydrological models usually need a validation period, the new observation data will be used to calculate evaluation metric values to determine whether the model is acceptable or not. After validation, the model can be used to predict a future scenario. Users can do the validation or prediction using our EnsembleValidator/Validator and Ensemble/Predictor objects combining with an user-defined objective function for validation. The differences between EnsembleValidator and Validator, as well as Ensemble and Predictor are that the "ensemble" ones execute the objective function for all the behavioral results obtained from uncertainty analysis, while the not "ensemble" ones only execute the objective function for the best solution/pareto-solutions obtained from calibration process. In other words, the "ensemble"

ones are designed for simulations considering parameter uncertainty, while the not "ensemble" ones are designed for certain simulations.

To be noticed, the objective function of a validation process should return the fitness value and the modelling result, whereas a prediction process should only return the modelling result.

In the validation period considering uncertainty, the 95ppu band will be calculated again. The "run" and "runMP" method of the validator object will return a validation result saver object, which contains the fitness value of all samples, results, PPU upper, PPU lower, Line max, Line min. To use the Validator for model validation:

```
from pycup import save, utilize, evaluation_metrics
import random
import numpy as np
from pycup import utilize
"""

Assume that this is the validation function.

The objective function for validation is similar to the one provided
in the template. For the validation of a real model, you should
substitute it with a function that feeds the validation input data
to the model. Also, the simulation period or other settings should be
correctly set.
"""

def obj_fun(x):
    import random
    t = np.arange(100)
    obs = np.sin(t) * 2.1 + np.tan(t) * 5.2**3 + random.random()
    res = np.sin(t) * x[0] + np.tan(t) * x[1]**3
    fitness = evaluation_metrics.OneMinusNSE(obs, res)
    result = res.reshape(1, -1)
    return fitness, result

# Load an opt/uncertainty analysis result with behaviour samples
res = save.ProcResultSaver.load(r"ProcResult.rst")
vldt = utilize.Ensemblevalidator(res, 95, obj_fun, n_obj=1, rstpath =
"ValidationResult.rst", args=())
saver = vldt.run()

#for a multi processing version
#saver = vldt.runMP(n_jobs=5)
```

In the validation stage that only considers best solutions:

```
from pycup import save, utilize, evaluation_metrics
import random
import numpy as np
"""

Assume that this is the validation function.

The objective function for validation is similar to the one provided
in the template. For the validation of a real model, you should
substitute it with a function that feeds the validation input data
to the model. Also, the simulation period or other settings should be
```

```

correctly set.

def obj_fun(x):
    import random
    t = np.arange(100)
    obs = np.sin(t) * 2.1 + np.tan(t) * 5.2**3 + random.random()
    res = np.sin(t) * x[0] + np.tan(t) * x[1]**3
    fitness = evaluation_metrics.OneMinusNSE(obs, res)
    result = res.reshape(1, -1) #important
    return fitness, result

# Load an opt/uncertainty analysis result with behaviour samples
res = save.RawDataSaver.load(r"RawResult.rst")
vldt = utilize.validator(res,obj_fun,n_obj=1, rstpath = "ValidationResult.rst",
args=())
saver = vldt.run()

#for a multi processing version
#saver = vldt.runMP(n_jobs=5)

```

Users can load the validation results using the "load" method of the result saver object.

```

from pycup import save

vldt_res = save.ValidationResultsSaver.load("ValidationResult.rst")
print(vldt_res.ppu_upper)           #only available for ensemble validation
print(vldt_res.ppu_lower)           #only available for ensemble validation
print(vldt_res.fitness)
print(vldt_res.results)
print(vldt_res.line_max)           #only available for ensemble validation
print(vldt_res.line_min)           #only available for ensemble validation
print(vldt_res.best_result)         #equivalent to vldt_res.results for non-
ensemble                           validation
print(vldt_res.median_prediction)   #only available for ensemble validation

```

To make a prediction using your behavioral samples:

```

from pycup import save, utilize,evaluation_metrics,utilize
import numpy as np

def obj_fun(x):
    t = np.arange(100)
    res = np.sin(t) * x[0] + np.tan(t) * x[1]**3
    result = res.reshape(1, -1) #important
    return result

res = save.ProcResultSaver.load(r"ProcResult.rst")
pred = utilize.EnsemblePredictor(res,95,obj_fun, rstpath = "PredResult.rst",
args=())
pred.run()

```

To make a prediction using your best/pareto solution(s):

```

from pycup import save, utilize, evaluation_metrics, utilize
import numpy as np

def obj_fun(x):
    t = np.arange(100)
    res = np.sin(t) * x[0] + np.tan(t) * x[1]**3
    result = res.reshape(1, -1) #important
    return result

res = save.RawDataSaver.load(r"RawResult.rst")
pred = utilize.Predictor(res,obj_fun,rstpath = "PredResult.rst", args=())
pred.run()

```

To load the prediction results:

```

from pycup import save
pred_res = save.PredResultsSaver.load("PredResult.rst")
print(pred_res.result)
print(pred_res.ppu_upper)           #only available for ensemble prediction
print(pred_res.ppu_lower)           #only available for ensemble prediction
print(pred_res.line_max)            #only available for ensemble prediction
print(pred_res.line_min)            #only available for ensemble prediction
print(pred_res.median_prediction)   #only available for ensemble prediction

```

## Saving the archive/record and resuming

In case of any interruptions, the optimization information will be automatically saved in a "Record.rcd" file during the optimization process at the end of each iteration. Users can load the "Record.rcd" file to resume their optimization process. Take GLUE calibration as an example:

```

cp.GLUE.run(n = 1000, dim = 30, lb = lb, ub = ub, fun =
uni_fun1,RecordPath="Record.rcd")

```

Users can also define the record saving path by modifying the variable in module "pycup.save"

```

from pycup import save
save.record_path = "D:\\Record.rcd"

```

## Author's gift -- for some problems that you may meet when calibrating a model with executable.

For some modeling softwares, the automatic execution of the executables may needs the Administrator's privileges for Windows system environment, otherwise there will always have a problem of pop-up windows that requiring you to confirm the Administrator's privileges. To solve this kind of problems, you can run your IDE (for example, PyCharm) with Administrator's privileges. Or you can run the CMD with Administrator's privileges and directly execute your script by:

```

python xxxx.py

```

Still for some modeling softwares with executables, there may be some other kinds of pop-up windows generated by the modeling software that requires you to confirm some information about the simulation process. Take the MIKE 11 ad (a water quality model) as an example, there may be a warning window for high courant number in simulation process, you can simply write a function for closing these windows using Windows API. For example:

```
import win32gui
import win32con
import multiprocessing as mp
import bnuMIKE11.callMIKE as cmike # this is a library developed by the author,
ignore it

def close_courant_wd():
    """
        this function can find the window that you want according to the handle of
        it
        For different pop-up windows, the handles will be vary. You can get the
        handle of
        a window using some auxiliary softwares (e.g. WinSpy).
    """
    courant_wd = win32gui.FindWindow("#32770", "AD Courant number warning")
    # the following sentence click messages to click the "No" option to close the
    window
    # and continue the simulation
    bu = win32gui.FindWindowEx(courant_wd, None, 'Button', "否(&N)")
    win32gui.SendMessage(bu, win32con.WM_LBUTTONDOWN, win32con.MK_LBUTTON, 0)
    win32gui.SendMessage(bu, win32con.WM_LBUTTONUP, win32con.MK_LBUTTON, 0)
    return courant_wd, bu

def listener():
    """
        This is a listener that continuously detect the pop-up window
    """
    flag = 0
    while True:
        try:
            cw, bu = close_courant_wd()
        except:
            cw, bu = 0, 0
        if cw != 0 and bu != 0:
            flag += 1
        if flag >= 2:
            break
        else:
            time.sleep(1)
    return

def run_wq_coupling(proj_dir):
    # creat a Process that runs the listener function
    lis_proc = mp.Process(target=listener)
    lis_proc.start()
    # This sentence call the MIKE11 computational executable
    ret = cmike.callexe(r"Z:\DHI\bin\x64\mike11.exe", proj_dir +
r"\tonghuihe.sim11")
```

```

# When the simulation process has finished, terminate and close the process
of Listener
lis_proc.terminate()
lis_proc.join()
lis_proc.close()
return 0

```

Here I also give an effective executable calling function that would be commonly used based on the Windows API:

```

import win32api
import win32event
import win32process
import win32con
from win32com.shell.shell import ShellExecuteEx
from win32com.shell import shellcon

def callexe(f_model, f_sim):

    #ret = win32api.ShellExecute(0, "open", f_model, f_sim, '', 1)
    process_info = ShellExecuteEx(nShow=win32con.SW_HIDE,
                                fMask=shellcon.SEE_MASK_NOCLOSEPROCESS,
                                lpVerb='runas',
                                lpFile=f_model,
                                lpParameters=f_sim)
    win32event.WaitForSingleObject(process_info['hProcess'], -1)

    ret = win32process.GetExitCodeProcess(process_info['hProcess'])
    #cmd = f_model + " " + f_sim
    #ret = os.system(cmd)

    return ret

```

## Potential problem of multi-site or multi-event calibration

For environmental models, sometimes you would need to save and analysis the results from different sites or in different events (e.g., different rainfall events). This situation is not completely supported in this version of the package. However, there are some alternative ways to do this:

1. (RECOMMENDED) concatenate the these results in the objective function to make sure that the returned result is a numpy 2D array with a shape of (1, total data length). This will not affect the following uncertainty analysis. When you are plotting your uncertainty band results (pycup.plot.plot\_uncertainty\_band), you can use the argument "idx" (a tuple of the starting index and the ending index) to extract the corresponding simulation data.
2. return the simulation results in a 3D numpy array, then use the argument "st\_id" of likelihood\_uncertainty to perform the uncertainty analysis based on a specific site/event. However, the validation and prediction functions do not support operations like this.

## Examples

### Example 1: using GWO to calibrate a testing function

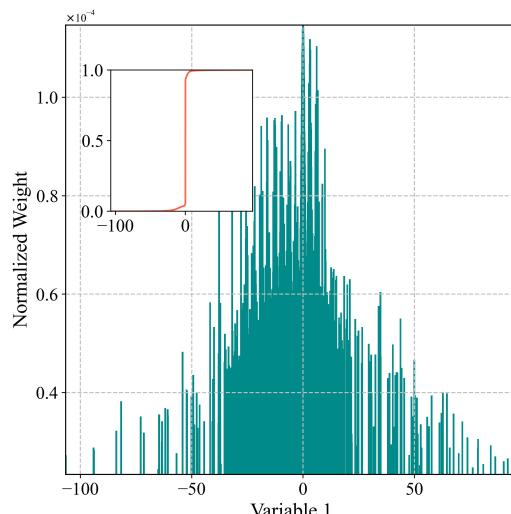
```
import pycup as cp
import numpy as np
from pycup import GWO
import pycup.uncertainty_analysis_fun as ufun

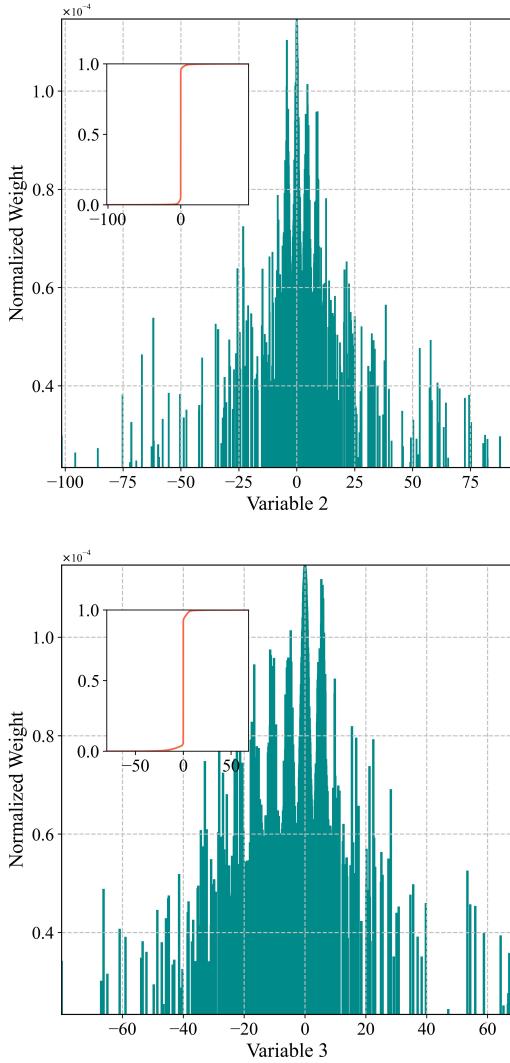
#####
##fmin = 1, dim = 3, range = [-600,600], minX = [0,0,0]
def mul_fun3(x):
    a = np.sum(np.power(x,2))/4000
    b = np.prod([np.cos(x[i]/np.sqrt(i)) for i in range(len(x))])
    fitness = a - b + 1 + 1
    result = fitness.reshape(1, -1)
    return fitness, result
####

if __name__ == "__main__":
    lb = -600 * np.ones(3)
    ub = 600 * np.ones(3)
    GWO.EliteOpposwitch = True
    GWO.OppoFactor = 0.05

    GWO.run(pop=100, dim=3, lb=lb, ub=ub, MaxIter=100,
fun=cp.test_functions.mul_fun3)

    raw_res = cp.save.RawDataSaver.load(r"RawResult.rst")
    cp.plot.plot_opt_curves(raw_res)
    ufun.likelihood_uncertainty(raw_res, 10, 95)
    opt_res = cp.save.ProcResultSaver.load(r"ProcResult.rst")
    cp.plot.plot_posterior_distribution(opt_res, variable_id=0,
x_label="Variable 1", obj_path="dis0.jpg", reverse=True)
    cp.plot.plot_posterior_distribution(opt_res, variable_id=1,
x_label="Variable 2", obj_path="dis1.jpg", reverse=True)
    cp.plot.plot_posterior_distribution(opt_res, variable_id=2,
x_label="Variable 3", obj_path="dis2.jpg", reverse=True)
```





## Example 2: comparison between GLUE and swarm optimization algorithm

```

import pycup as cp
import numpy as np
from pycup import GWO,GLUE

if __name__ == "__main__":
    lb = -600 * np.ones(3)
    ub = 600 * np.ones(3)
    GWO.EliteOppoSwitch = True
    GWO.OppoFactor = 0.05
    cp.save.raw_path = r"RawGWOResult.rst"
    GWO.run(pop=100, dim=3, lb=lb, ub=ub,
MaxIter=50, fun=cp.test_functions.mul_fun3)
    raw_res = cp.save.RawDataSaver.load(r"RawGWOResult.rst")

    cp.plot.plot_2d_sample_space(raw_res,obj_path="sampleGWO.jpg",variable_id1=0,va
riable_id2=1)
    cp.plot.plot_3d_fitness_space(raw_res, obj_path="fitnessGWO.jpg",
variable_id1=0, variable_id2=1)
    cp.save.raw_path = r"RawGLUEResult.rst"

```

```

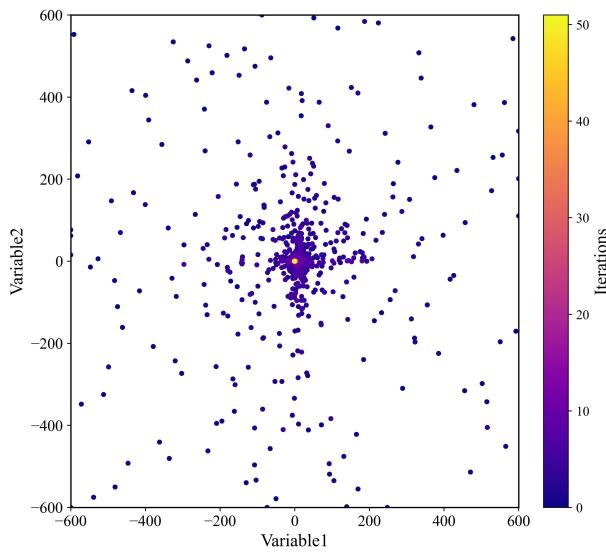
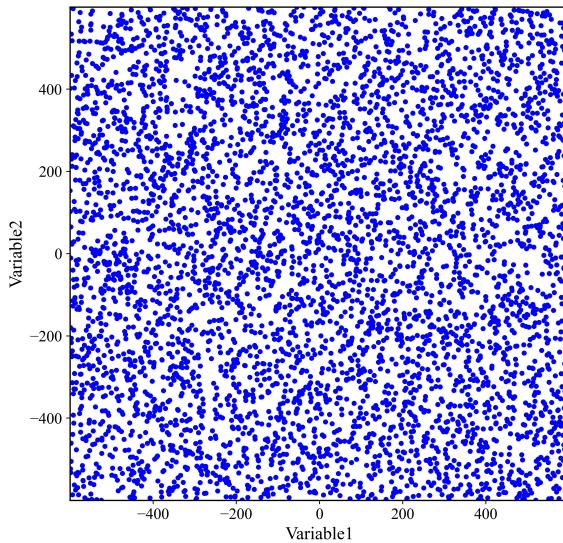
GLUE.runMP(5000, dim=3, lb=lb,
ub=ub, fun=cp.test_functions.mul_fun3,n_jobs=5)

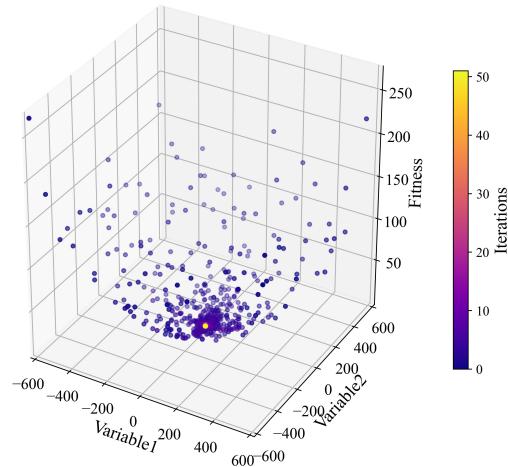
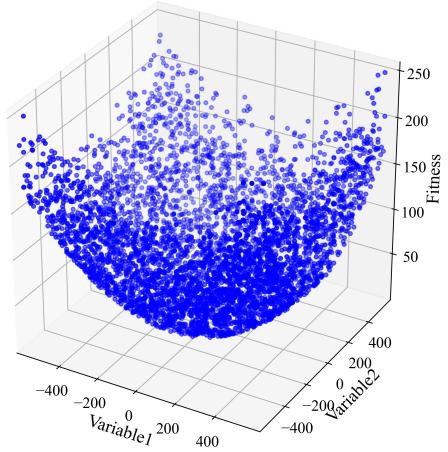
raw_res2 = cp.save.RawDataSaver.load(r"RawGLUEResult.rst")

cp.plot.plot_2d_sample_space(raw_res2,obj_path="sampleGLUE.jpg",variable_id1=0,
variable_id2=1)

cp.plot.plot_3d_fitness_space(raw_res2, obj_path="fitnessGLUE.jpg",
variable_id1=0, variable_id2=1)

```





### Example 3: using PSO to calibrate an SVR model

```

from sklearn.preprocessing import StandardScaler
from sklearn.datasets import load_boston
from sklearn.model_selection import train_test_split
import numpy as np
from sklearn.svm import SVR
import pycup as cp
from sklearn.metrics import r2_score
from pycup import save,plot
import pycup.uncertainty_analysis_fun as ufun

# define an objective function
def obj_fun(x,train_x,train_y,test_x,test_y,ss_y):
    C = x[0]
    gamma = x[1]
    rbf_svr = SVR(kernel='rbf',C=C,gamma=gamma)
    rbf_svr.fit(train_x, train_y.ravel())
    rbf_svr_predict = rbf_svr.predict(test_x)
    r_test_y = ss_y.inverse_transform(test_y)
    r_pred_y = ss_y.inverse_transform(rbf_svr_predict)

    # use 2-r2 as the likihood function
    # (in case of r2~1.0 then num/0 during uncertainty analysis)
    fitness = 2 - r2_score(r_test_y,r_pred_y)
    result = r_pred_y.reshape(1,-1)
    return fitness,result

```

```

if __name__ == "__main__":
    boston_data = load_boston()
    # SVR model for the Boston house price regression problem
    # print(boston_data.DESCR)
    x = boston_data.data
    y = boston_data.target
    # split the data set 70% training (fit), 30% validation (optimizing the
    # hyper-parameters)
    x_train, x_test, y_train, y_test = train_test_split(x, y, test_size=0.3,
random_state=7)
    # Standardization
    ss_x = StandardScaler()
    ss_y = StandardScaler()
    x_train = ss_x.fit_transform(x_train)
    x_test = ss_x.transform(x_test)
    y_train = ss_y.fit_transform(y_train.reshape(-1, 1))
    y_test = ss_y.transform(y_test.reshape(-1, 1))

    # set the result saving path
    cp.save.proc_path = "proc_svr.rst"
    cp.save.raw_path = "raw_svr.rst"

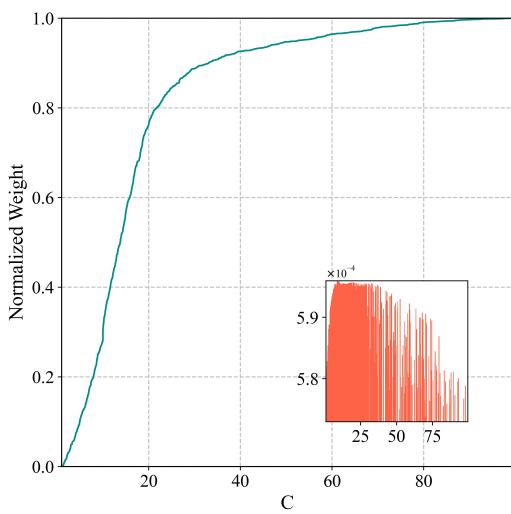
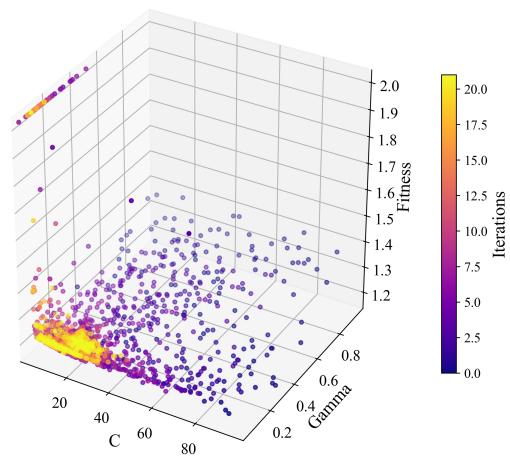
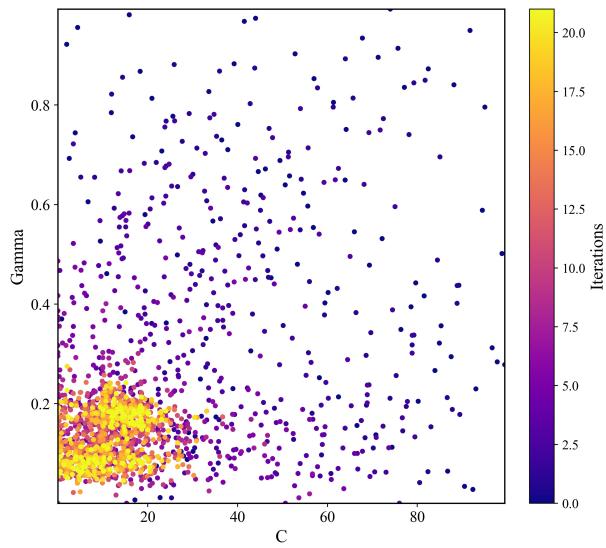
    # define the lower and upper searching boundary
    lb = np.array([0.000001,0.000001])
    ub = np.array([100.0,1.0])

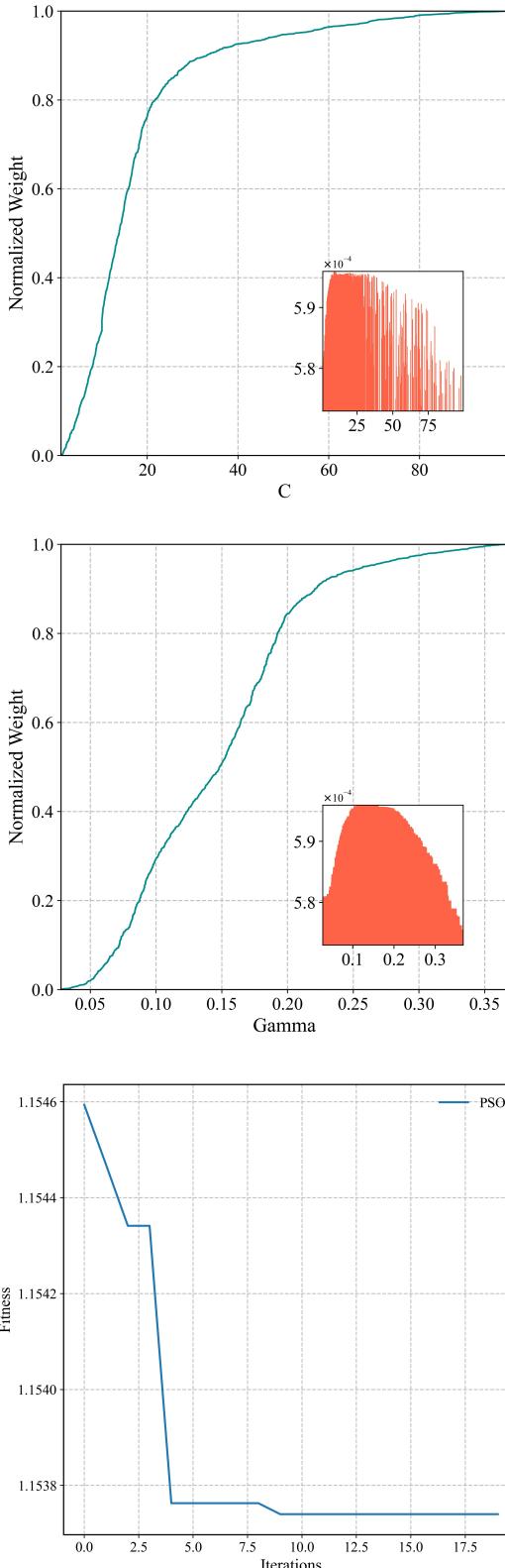
    # algorithm settings
    cp.PSO.EliteOpposwitch = True

    # run the PSO
    cp.PSO.run(pop=100, dim=2, lb=lb, ub = ub, MaxIter=20, fun=obj_fun,
args=(x_train,y_train,x_test,y_test,ss_y))

    # Load the results
    raw_res = save.RawDataSaver.load(r"raw_svr.rst")
    # uncertainty analysis
    ufun.likelihood_uncertainty(raw_res,1.2,95)
    # plot
    plot.plot_2d_sample_space(raw_res, variable_id1=0,
variable_id2=1,x_label="C",y_label="Gamma", obj_path="sample2dSVR.jpg")
    plot.plot_3d_fitness_space(raw_res, variable_id1=0,
variable_id2=1,x_label="C",y_label="Gamma", obj_path="sample3dSVR.jpg")
    opt_res = save.ProcResultSaver.load(r"proc_svr.rst")
    plot.plot_posterior_distribution(opt_res, variable_id=0,x_label="C",
obj_path="disc.jpg", reverse=False, barwidth=0.05, subloc=8)
    plot.plot_posterior_distribution(opt_res, variable_id=1,x_label="Gamma",
obj_path="disGamma.jpg", reverse=False, barwidth=0.05, subloc=8)
    plot.plot_opt_curves(raw_res, slim=False, frameon=False, legendlabels=
["PSO"], obj_path="curveSVR.jpg")

```

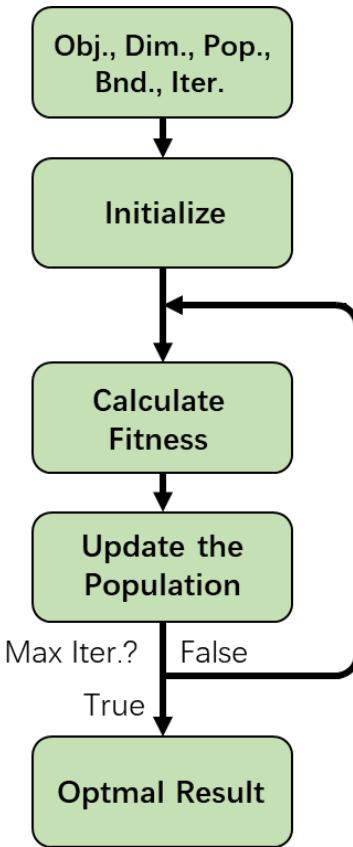




## Theoretical foundations

### Algorithms

All the swarm-optimization algorithms have a similar work flow as shown in the following figure. Firstly, the objective function, dimension (num. parameters), population size, searching boundary, and maximum iterations should be defined. Then, the population is initialized using a random sampling technique. After that, each individual in the population will be used to calculate the objective function value (fitness). Subsequently, the population will be updated according to the mechanism of a specific algorithm.



In pycup, we made some improvements/modifications on the algorithms, the modified work flow as follows:

For the random sampling strategy, our algorithm utilize the Latin hypercube sampling (LHS) instead of using a simple random grab sampling. When updating the population, we provide options for elite opposition strategy. Conventionally, a swarm-optimization algorithm only return the best result. In pycup, you not only can use the conventional function of the algorithm, but also can get the uncertainty analysis result.

Relevant articles for the principles of the algorithms are concluded in the following table:

Algorithm	Reference
GLUE	Keith and Andrew 1992
SSA	Xue and Shen 2020
GWO	Mirjalili et al. 2014
MFO	Mirjalili 2015
PSO	Kennedy and Eberhart 1995
SCA	Mirjalili 2016
SOA	Dhiman and Kumar 2019
TSA	Kaur et al. 2020
WOA	Mirjalili and Lewis 2016
MOPSO	Coello Coello and Lechuga 2002
MODE	Reddy, M. and Kumar, D. 2007

Algorithm	Reference
NSGA2	Deb, K. et al. 2002

## Elite opposition strategy

Opposition-Based Learning (OBL) is an optimization strategy used to improve the diversity of optimization algorithm and enhance its generated solutions. Tizhoosh (2005) proposed the Elite opposition-based learning based on the OBL theory. Several studies have verified that the OBL and EOBL can obtain a solutions that close to global optimal solution with a higher probability. EOBL strategy relies on the elite individual to lead the population towards the global solution. For an elite individual, the opposition point of it can be calculated as:

$$\check{x}_{i,j} = S \times (da_j + db_j) - x_{i,j}$$

where, S is a random number in [0,1], da and db are the dynamic minimum and maximum boundary of the elite solution set,  $x_{i,j}$  is the elite individual. For more details about the EOBL, users can see Sihwail et al. (2020).

## Sensitivity analysis

In pycup, the sensitivity analysis is carried out using a multiple linear regression method. The sensitivity of parameters can be obtained according to the t-test statistics. The multiple-linear regression and t-test is relying on statsmodels.api. Users can visit statsmodels.api's website at <https://github.com/statsmodels/statsmodels> for more information.

## Uncertainty analysis

The uncertainty analysis method used in this package is same as the one in GLUE. In this method, a likelihood function should be firstly defined. For swarm optimization algorithms, the reciprocal value of the objective function is used as the likelihood function. Use the one minus Nash-Sutcliffe efficiency coefficient as an example (the algorithm is to minimize the value), then we have:

$$Obj = 1 - NSE$$

$$L_y(\theta|Y) = 1/Obj$$

Subsequently, the behavioral solution set is obtained according to the historical searching results and the user-defined threshold value. The posterior distribution and uncertainty band is calculated using the following equations:

$$L_p[\theta|Y] = CL_y[\theta|Y]L_0[\theta]$$

$$P_t(Z_t < z) = \sum_{i=1}^m L_p[\theta_i | Z_{ti} < z]$$

where C is a coefficient that makes the summation of  $L_p[\Theta|Y]$  equal to 1;  $L_0[\Theta]$  is the prior distribution weight, in this package the prior distribution is assumed as a uniform distribution (same as relevant studies);  $L_y[\Theta|Y]$  is the calculated likelihood value;  $P_t(Z_t < z)$  is the cumulative probability that the prediction target value is lower than the given z value;  $L_p[\Theta_i]$  is the

normalized weight.

Generally, current studies use P-factor and R-factor as the uncertainty evaluation metrics. P-factor is the proportion of measured data bracketed by the 95PPU band. R-factor is a value of the average distance between the upper and lower 95PPU and is expressed as the value of the average 95PPU thickness divided by the standard deviation of the observations. The equations for r-factor as follows:

$$\bar{d} = \frac{1}{n} \sum_{i=1}^n (y_{i,97.5\%}^M - y_{i,92.5\%}^M)$$

$$r - \text{factor} = \frac{\bar{d}}{\sigma_{obs}}$$

## References

---

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