Probability scoring for spelling correction

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This paper describes a new program, CORRECT, which takes words rejected by the Unix® SPELL program, proposes a list of candidate corrections, and sorts them by probability score. The probability scores are the novel contribution of this work. They are based on a noisy channel model. It is assumed that the typist knows what words he or she wants to type but some noise is added on the way to the keyboard (in the form of typos and spelling errors). Using a classic Bayesian argument of the kind that is popular in recognition applications, especially speech recognition (Jelinek, 1985), one can often recover the intended correction, c, from a typo, t, by finding the correction c that maximizes Pr(c) Pr(t | c). The first factor, Pr(c), is a prior model of word probabilities; the second factor, Pr(t | c), is a model of the noisy channel that accounts for spelling transformations on letter sequences (insertions, deletions, substitutions and reversals). Both sets of probabilities were estimated using data collected from the Associated Press (AP) newswire over 1988 and 1989 as a training set. The AP generates about 1 million words and 500 typos per week.

In evaluating the program, we found that human judges were extremely reluctant to cast a vote given only the information available to the program, and that they were much more comfortable when they could see a concordance line or two. The second half of this paper discusses some very simple methods of modeling the context using *n*-gram statistics. Although *n*-gram methods are much too simple (compared with much more sophisticated methods used in artificial intelligence and natural language processing), we have found that even these very simple methods illustrate some very interesting estimation problems that will almost certainly come up when we consider more sophisticated models of contexts. The problem is how to estimate the probability of a context that we have not seen. We compare several estimation techniques and find that some are useless. Fortunately, we have found that the Good-Turing method provides an estimate of contextual probabilities that produces a significant improvement in program performance. Context is helpful in this application, but only if it is estimated very carefully.

At this point, we have a number of different knowledge sources—the prior, the channel and the context—and there will certainly be more in the future. In general, performance will be improved as more and more knowledge sources are added to the system, as long as each additional knowledge source provides some new (independent) information. As we shall see, it is important to think more carefully about combination rules, especially when there are a large number of different knowledge sources.

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1. The problem

The CORRECT program reads a list of misspelled words from the input stream (stdin) and prints a set of candidate corrections for each word on the output stream (stdout). CORRECT also produces a probability estimate along with each candidate correction (unless there is only one candi-

date correction). These probabilities distinguish CORRECT from previous spelling correctors. The problem of finding just the right way to estimate these probabilities from the various available sources of knowledge poses a technical challenge for both statistics and artificial intelligence. In this paper we have only dealt with a few of the more obvious possibilities.

Table 1. Examples of output of CORRECT

Туро	Corrections (%)
detered	deterred (100) metered (0) petered (0)
laywer	lawyer (100) layer (0) lawer (0)
negotations	negotiations
notcampaigning	???*
progession	progression (94) procession (4) profession (2)
ususally	usually
winky	windy (69) wink (20) winks (7) kinky (2)
·	wonky (1) pinky (1) dinky (0) winy (0)
	inky (0)

^{*???} indicates that no correction was found.

Table 1 presents some sample output produced by the Unix® command, 'spell paper | correct', where *paper* is a text file containing the misspelled words in column 1.

2. Proposing candidate corrections

The first stage of CORRECT searches a wordlist to find candidate corrections that differ from the input typos by a single insertion, deletion, substitution or reversal. The wordlist was collected from five sources, the AP newswire, the Unix® SPELL program, the Cobuild dictionary (Sinclair et al, 1987), the Collins Dictionary of the English Language (Hanks et al, 1979), and Roget's International Thesaurus (Chapman, 1977). This first stage produces the output shown in Table 2, given the input typo, 'acress'.

The candidate 'actress', for example, can be mistyped as 'acress' by deleting the 't' at position 2. The symbols @ and # represent nulls. (The transformations are named from the point of view of the correct word, not the typo.) The typo, 'acress', can arise from 'acres' by insertion of 's' after either the fourth or the fifth letter, so 'acres' appears twice in the table as a candidate correction. This unusually

Table 2. Example of candidate corrections

Туро	Correction	Transformation				
acress	actress	<u>@</u>	t	2	deletion	
acress	cress	a	#	0	insertion	
acress	caress	ac	ca	0	reversal	
acress	access	r	c	2	substitution	
acress	across	e	o	3	substitution	
acress	acres	S	#	4	insertion	
acress	acres	S	#	5	insertion	

§For the purposes of this experiment, a typo is a lower-case word rejected by the Unix® SPELL program.

Table 3. An example from the deletion table

Corre	ction
t	4
a	3
e	2
r	1
g	0
	a e r

difficult example was selected to illustrate the four transformations; most examples do not have so many high-scoring possibilities.

In principle, one could implement the transformations very straightforwardly by trying all the possibilities. The insertion operation is actually implemented this way. It requires n dictionary accesses to see if the nth letter in the typo may have been inserted. Unfortunately, the deletion operation is much more expensive; there are 26 letters that might have been deleted in n+1 positions. In order to reduce the number of dictionary accesses, the system makes use of a precomputed table as shown in Table 3. This table maps words missing a letter to corrections. With this table, the system can check for deletions in one table look-up. The table is also useful for checking for substitutions and reversals. Of course, there is a cost in space. The deletion table has about a million entries, approximately ten times as many as the dictionary. The deletion table is stored using heuristic hashing methods very similar to those in SPELL (McIlroy, 1982).

3. Scoring

Two versions of CORRECT have been studied: one with context and the other without context. We discuss the simpler no-context version first.

Each candidate correction is scored by the Bayesian combination rule $Pr(c) Pr(t \mid c)$, and then normalized by the sum of the scores for all proposed candidates. Care must be taken in estimating the prior because of sparse data problems. It is possible (and even likely) that a proposed correction might not have appeared in the training set. Some methods of estimating the prior would produce undesirable results in this case. For example, the maximum likelihood estimate (MLE) would estimate Pr(c) = 0 and, consequently, many candidate corrections would be rejected just because they did not happen to appear in the training set (the 1988 AP corpus). We will encounter even more severe forms of the sparse data problem when we consider context.

We will consider three estimation methods that deal with the sparse data problems in three different ways. All

of these methods attempt to estimate a set of probabilities, p, from observed frequencies, r. It is assumed that the observed frequencies are generated by a binomial process with N total observations. The estimation methods generate an adjusted frequency r^* , where r^* is a function of r. Once r^* has been determined, then p is estimated as $p \approx r^*/N^*$. $N^* = \Sigma r^*N_r$ where N_r is the frequency r,\dagger assuring that the estimated probabilities add to one. The maximum likelihood estimator sets $r^* = r$. The MLE is particularly poor when r = 0, since the true probabilities are probability greater than 0 in this case.

Following Box and Tiao (1973), we can assume an uninformative prior and reach a posterior distribution for p. Using the expectation of this distribution amounts to using $r^* = r + 0.5$. We call this the expected likelihood estimate (ELE). The third method is the Good-Turing (GT) method (Good, 1953). This method sets $r^* = (r+1)N_{r+1}/N_r$. Unlike the MLE, both ELE and GT estimates assign non-zero probabilities, even when r = 0. This is probably a desirable property.

The prior, Pr(c), estimated by the ELE, is (freq(c) + 0.5)/(N + V/2), where freq(c) is the number of times that the proposed correction c appears in the 1988 AP corpus (N = 44 million words, and the vocabulary size, V, is 112 964). Although we have discussed problems with the ELE elsewhere (Gale and Church, 1989), it will be used here.

The channel probabilities $Pr(t \mid c)$, are computed from four confusion matrices (presented in Appendix A so as to encourage replication of this work): (1) del[x, y], the number of times that the characters 'xy' (in the correct word) were typed as 'x' in the training set; (2) add[x, y], the number of times that 'x' was typed as 'xy'; (3) sub[x, y], the number of times that 'y' was typed as 'x', and (4) rev[x, y], the number of times that 'xy' was typed as 'yx'. As the following formula shows, these four confusion matrices are normalized by chars[x, y] and chars[x], the number of times that 'xy' and 'x' appeared in the training set, respectively. These matrices are not included in the appendix since they can be easily replicated.

$$Pr(t \mid c) \approx \begin{cases} \operatorname{del}[c_{p-1}, c_p] / \operatorname{chars}[c_{p-1}, c_p] & \text{if deletion} \\ \operatorname{add}[c_{p-1}, t_p] / \operatorname{chars}[c_{p-1}] & \text{if insertion} \\ \operatorname{sub}[t_p, c_p] / \operatorname{chars}[c_p] & \text{if substitution} \\ \operatorname{rev}[c_p, c_{p+1}] / \operatorname{chars}[c_p, c_{p+1}] & \text{if reversal} \end{cases}$$

In this formula, c_p is the pth character of the proposed correction, c. Likewise, t_p is the pth character of the typo, t. The confusion matrices are computed with a bootstrapping procedure. Initially assume a uniform distribution over the possible confusions. Then run the program over the training set to find corrections for the words that

Table 4. Example of rating candidate corrections without context

cor	%	Raw score	freq(cor)	Pr(typo cor)
actress	37	0.157	1343	55./470 000
cress	0	0.000	0	46./32 000 000
caress	0	0.000	4	.95/580 000
access	0	0.000	2280	.98/4 700 000
across	18	0.077	8436	93./10 000 000
acres	21	0.092	2879	417./13 000 000
acres	23	0.098	2879	205./6 000 000

SPELL rejects. Use these corrections to update the confusion matrices, and iterate. The probabilities are estimated using the Good-Turing method (Good, 1953), with the cells of the matrices as the typos.

Returning to the 'acress' example, the seven proposed transformations are scored by multiplying the prior probability (which is proportional to 0.5 + column 4 in Table 4) and the channel probability (column 5) to form a raw score (column 3), which are normalized to produce probabilities (column 2). The final results are: 'acres' (45%), 'actress' (37%), 'across' (18%), 'access' (0%), 'cress' (0%). This example is very hard; in fact, the second choice is probably right, as can be seen from the context:

... was called a 'stellar and versatile *acress* whose combination of sass and glamour has defined her

The program would need a much better prior model in order to handle this case. When we consider context, we will show how the program can take advantage of the fact that 'actress' is more likely than 'acres' in the context of 'whose'.

4. Evaluation

Many typos such as 'absorbant' have just one candidate correction, but others such as 'adusted' have multiple corrections. Table 5 shows examples of typos with less than ten candidate corrections. The candidate corrections are ordered by likelihood. Most typos have relatively few candidate corrections. Table 6 shows the number of typos† broken down by the number of corrections in seven month-long samples of the AP newswire. In March, for example, there were 720 typos with 0 corrections, 1120 typos with 1 correction, 269 with 2 corrections, etc. The final column shows that there is a general trend for fewer choices, though the 0-choice case is special. (The system was trained on the AP wire from February 1988; the results below were computed from the AP wire during the period from March through Septermber 1989.)

We decided to look at the 2-candidate case in more detail in order to test how often the top-scoring candidate

Table 5. Examples of typos with various numbers of candidate corrections

No. of corrections	Туро	Corrections
0	admininistration	
1	absorbant	absorbent
2	adusted	adjusted, dusted
3	ambitios	ambitious, ambitions, ambition
4	compatability	compatibility, compactability, comparability, computability
5	afte	after, fate, aft, ate, ante
6	dialy	daily, diary, dials, dial, dimly, dilly
7	poice	police, price, voice, poise, pice, ponce, poire
8	piots	pilots, pivots, riots, plots, pits, pots, pints, pious
9	spash	splash, smash, slash, spasm, stash, swash, sash, pash, spas

Table 6. Number of typos by month and number of candidate corrections

No. of typos	March	April	May	June	July	Aug	Sept	Total
0	720	604	542	606	492	465	508	3937
1	1120	997	1037	1007	958	944	930	6993
2	269	224	209	223	199	224	214	1562
3	109	92	89	101	79	87	82	639
4	58	57	62	45	43	59	43	367
5	54	41	20	26	28	24	28	221
6	35	22	19	19	22	17	23	157
7	20	11	13	7	11	15	17	94
8	19	14	14	5	7	7	16	82
9	15	11	6	11	10	8	16	77
10+	154	97	79	75	53	77	78	613
Total	2573	2170	2090	2125	1902	1927	1955	14742

agreed with a panel of three judges. The judges were given 564 triples and a few concordance lines:

absurb absorb absurd

527595: financial community. *E* *S* "It is absurb and probably obscene for any person so engaged to und

actuall actual actually

3603767: le in determining whether the defendant actuall will die. *E* *S* In the 1985 decision, the justic

741671: was Pearl Harbor Day. *E* *S* The day actuall is Dec. 7. *E* *S* Bush said the extradition Wednes

The first word of the triple was a SPELL reject; the other two were the candidates, sorted by alphabetical order. The judges were given a five-way forced choice. They could circle any one of the three words, if they thought that was what the author had intended. Alternatively, if they thought that the author had intended something else, they could write down 'other'. Finally, if they weren't sure, they

could write "?". The distribution of responses is shown in Table 7. It should be clear from the table above that SPELL is rejecting too many words. In almost 20% of the triples, CORRECT was given a non-problem to correct:

acquirees acquirers acquires

1434654: be acquirers, as they have been, than acquirees. *E* *S* If the industrials had attracted bids th

Table 7. Distribution of judges' responses

	Judge 1	Judge 2	Judge 3
Choice 0 (SPELL error)	99	124	93
Choice 1	188	176	167
Choice 2	175	159	151
Other	28	26	30
?	74	79	123
Total	564	564	564

Since we were mostly concerned with evaluating the scoring function, we did not want to be distracted with errors in SPELL and other problems that are beyond the scope of this paper. Therefore, we decided to consider only those cases where at least two judges circled one of the two candidates, and they agreed with each other. This left 332 triples.

Table 8 shows that this version of CORRECT agrees with the majority of the judges in 87% of the 332 cases of interest. In order to help calibrate this result, three inferior methods are also evaluated. The *channel-only* method selects the candidate with the larger channel probability $Pr(t \mid c)$. The *prior-only* method selects the candidate with the larger prior Pr(c). Finally, the *chance* method selects the first candidate. As Table 8 shows, CORRECT is significantly better than the three alternative methods. The table also evaluates the three judges.† The table shows that the judges significantly outperform CORRECT, indicating that there is room for improvement. All three judges found the task more difficult and more time-consuming than they had expected. Each judge spent about half a day grading the 564 triples.

We were also interested in testing whether the score predicted accuracy. Consider, for example, a group of typos whose average score was 80%. Perfect accuracy would be achieved if exactly 80% of this group agreed with the majority opinion of the judges. Figure 1 shows a test of this concept, although our data are scanty for this purpose. The horizontal axis shows the score from CORRECT averaged over a group of 20 typos. The vertical axis shows the fraction of this group that were right (agreed with the majority opinion of the judges). The diagonal line indicates perfection. The curved lines above and below the

Table 8. Performance without context

Method	Discrimination	(%)
CORRECT	286/329	87 ± 1.9 §
channel-only	263/329	80 ± 2.2
prior-only	247/329	75 ± 2.4
chance	172/329	52 ± 2.8
Judge 1	271/273	99 ± 0.5
Judge 2	271/275	99 ± 0.7
Judge 3	271/281	$\frac{-}{96 \pm 1.1}$
Judge 5	271/281	90 ± 1.1

§The standard deviations are calculated assuming a binomial distribution of d drawings with probability n/d, where n is the numerator and d is the denominator shown in column 2. The calculation is $100\sqrt{n(d-n)/d^3}$.

†Judges were only scored on triples for which they selected '1' or '2', and for which the other two judges agreed on '1' or '2'. A triple was scored 'correct' for one judge if that judge agreed with the other two and 'incorrect' if that judge disagreed with the other two.

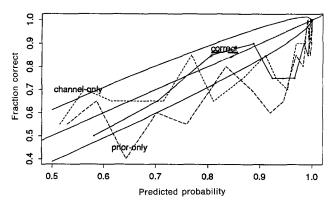


Fig. 1. The fraction actually correct is plotted against the predicted score. The prior-only model is shown with long dashes, the channel-only model with short dashes, and CORRECT with a solid line. The straight line is ideal performance, and the curved lines show one-standard-deviation limits. CORRECT is outside the one-standard-deviation limits about as much as could be expected by chance, while the two partial models are less accurate.

perfection line show one-standard-deviation limits for estimating probabilities from samples of 20.

All three of the methods shown are over-confident when their prediction is between 90% and 99%. The channel-only method is over-confident over the wider range from about 80% to 99%, while the prior-only method is over-confident over most of the range. The observations on CORRECT are outside of the one-standard-deviation limits about as much as would be called for by chance, while each of the other two methods has more points outside than would result just by chance. We conclude that the scores from CORRECT predict accuracy fairly well; scores from the other two methods are more problematic.

5. Contextual constraints

We have already pointed out that the human judges were extremely reluctant to cast a vote without more information, and that they were much more comfortable when they could see a concordance line or two. This suggests that contextual clues might help improve performance. However, it is important to estimate the context carefully; we have found that poor measures of context are worse than none.

In this work, we use a simple n-gram model of context, $Pr(l \mid c) Pr(r \mid c)$, where l is the word to the left of the typo, and r is the word to the right. Although n-gram methods are much too simple (compared with much more sophisticated methods used in artificial intelligence and natural language processing), even these simple n-gram methods illustrate the problem that poor estimates of contextual probabilities are worse than none. The same estimation issue is probably even more critical when more sophisticated artificial intelligence models of context are used.

Table 9. Poor estimates of context offer little or no help

	chance	MLE	ELE
wrong	164.5	15	169
uninformative	0	136	4
right	164.5	178	156

Table 10. A careful measure of context helps

	chance	GT
wrong	164.5	45
uninformative	0	4
right	164.5	280

Table 9 shows two inferior methods of estimating $Pr(l \mid c)$ $Pr(r \mid c)$. The MLE method is uninformative in nearly half of the cases because either $Pr(l \mid c)$ or $Pr(r \mid c)$ is zero.* Simple attempts to 'fix' these zeros can be disasterous; the ELE, for example, badly overestimates the probability of a bigram that has not been seen in the training set, and consequently, it is wrong more often than it is right.

A more sophisticated method of 'fixing' the zeros based on the Good-Turing (GT) estimate is discussed in Church and Gale (1991). Table 10 shows that this method performs significantly better than chance.

How do we combine this contextual evidence with the other knowledge sources? Recall that we previously scored candidate corrections with Pr(c) $Pr(t \mid c)$. We now enhance this formula to include contextual factors: Pr(c) Pr(c)

*The MLE statistics suggest that a trigram model such as Mays et al (1990) might not work much better than the simple bigram model that we have been using. The trigram model might help for the 15 cases where the bigram context is misleading, but it probably will not help for the much larger set of 136 cases where the bigram context is uninformative, since the trigrams will also be uninformative in these cases.

†The GT method changes the program's preference in 25 of the 329 cases; 17 of the changes are right and 8 of them are wrong. The probability of 17 or more right out of 25, assuming equal probability of two alternatives, is 0.04. Thus, we conclude that the improvement is significant.

‡A log transform is used here because the factors are combined by a multiplicative rule.

text, $t \mid c$). If we assume that the context is determined by the adjacent words, l and r, and that these factors are independent with each other and with the typo, then we can use the formula: $Pr(c) Pr(t \mid c) Pr(l \mid c) Pr(r \mid c)$.

Table 11 shows the results when the three estimates of context are combined with the previous version of CORRECT. We find, as we expected, that GT estimates of context provide a significant improvement over ignoring the context.† Adding the GT estimate of context improves performance from 87% to 90%. In contrast, poor estimates of context, such as ELE, actually *degrade* performance significantly. It is better to ignore context than to use it badly.

6. Combining multiple knowledge sources

Four knowledge sources have been discussed: the prior; the channel probability; the left context; and the right context. Ideally, we would hope that each of these knowledge sources is contributing new (independent) information. Figure 2 shows that this is so. There is a scatter plot for each pair of the four factors. The plot shows the logarithm; of the score assigned by one of the factors to the correct word (as determined by our panel of judges). Note that none of the scatter plots shows a strong correlation.

Table 12 shows the pairwise correlations. Note that most of the correlations are quite small, although there is a modest correlation between the prior probability and the left and right contextual probabilities. As mentioned above, this lack of correlation is encouraging, because it suggests that each knowledge source is contributing new information, which will (hopefully) improve performance.

Table 13 shows that performance is generally improved with each additional knowledge source. That is, each of the knowledge sources by itself performs better than chance, pairs of knowledge sources perform better still, triples are better yet, and all four perform best of all. However, we cannot say that the four-way combination is significantly better than all three-way combinations because our experiment is too small. We conclude that it is worth seeking additional factors.

The fourth column shows the mean of the scores for the correct words. Note that scores are highly correlated with empirically observed performance, as we would hope.

Table 11. Context is misleading unless carefully measured

	no context	+MLE context	+ELE context	+GT context
wrong	43	11	61	34
uninformative	0	136	0	0
right	286	182	268	295

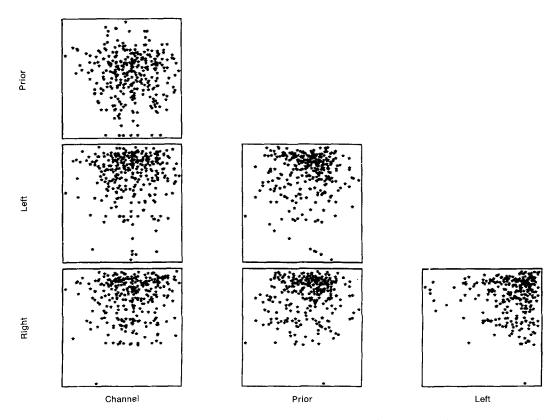


Fig. 2. Each panel shows a scatter plot comparing two of our knowledge sources. The logarithms of the scores assigned by the individual factors to the correct word are plotted. The plots show that each pair of factors are nearly independent.

Table 12. Correlations of logarithms of scores from individual knowledge sources

	channel	prior	left	right
channel	1.00	-0.05	-0.00	0.07
prior	-0.05	1.00	0.15	0.22
left	-0.00	0.15	1.00	0.11
right	0.07	0.22	0.11	1.00

Many other factors can be defined. One might first parse the input (Hindle, 1983; Seneff, 1989) and then look at words in particular syntactic constructions. For example, there are interesting constraints between verbs and objects which are not always modeled very well by simple *n*-gram methods. Of course, we should also consider extending the context to trigrams, which has been useful in speech recognition (Jelinek, 1985), and could be useful here.* However, since zero is the most common bigram frequency already, trigrams will not help in about half of the cases. Parts of speech (Church, 1989; Elbeze and Deroualt, 1990) of the adjacent words should also be

investigated. Thesaurus distances have proved useful in information retrieval applications (Salton, 1989), and could provide additional information here. Morphological decomposition might also be worth investigating.

As more factors are added, we believe the methods for combination need to be studied more closely. Each of our individual factors is over-confident, so it would be reasonable to shrink each likelihood ratio towards 1 before multiplying. The least over-confident sources of evidence would then be given greater weight. It would also be reasonable to shrink individually poorly measured factors.

7. Conclusions

There have been a number of spelling correction programs in the past such as Kucera (1988) that generated a list of candidates by looking for insertions, deletions, substitutions and reversals, much as we have been doing here. Our contribution is the emphasis on scoring. McIlroy, the author of the Unix® SPELL program (1982), intentionally focused on the spelling detection problem, and argued (private communication) that spelling correction was a bad idea so long as the corrector could not separate the plausible candidates from the implausible ones. He felt that it was probably more distracting than helpful to bury

^{*}Mays et al (1990) have used a trigram model for spelling correction. It would be interesting to know how much the extra context improves performance.

Table 13. Performance increases with number of knowledge sources

No. of KBS	model	performance	mean score
1	channel	80	75
1	prior	76	73
1	left	78	77
1	right	77	74
2	channel + prior	87	84
2	channel + left	87	85
2	channel + right	88	85
2	prior + left	83	82
2	prior + right	80	79
2	left + right	86	84
3	channel + prior + left	90	88
3	channel + prior + right	88	87
3	channel + left + right	90	89
3	prior + left + right	86	85
4	channel + prior + left + right	90	89

the user under a long list of mostly implausible candidates. In this work, we have attempted to show that it is possible to sort the candidates by a likelihood function that agrees well enough with human judges to be helpful.

Furthermore, we have studied the problem of adding contextual information. We have looked at just a few of the more obvious approaches. We have considered only the two words adjacent to the typo, and have tried to estimate probabilities of the proposed corrections conditional on these adjacent words. Using the simplest estimators that one might think of, the maximum likelihood and expected likelihood estimates, actually degrades performance. Fortunately, if the context is estimated very carefully with Good-Turing methods, then context does improve performance, as one would hope it should.

We noticed that the human judges were extremely reluctant to cast a vote given only the information available to the program, and that they were much more comfortable when they could see a concordance line or two. Furthermore, the judges all exceeded the program's performance. Apparently the judges are using additional contextual factors. It might be worth looking at a number of possibilities such as parse trees, word trigrams, part of speech n-grams, thesaurus relations, and morphological structures. Many of these possibilities have proved useful in other applications, and may also improve performance in this application, though it may not be easy to make the case given the estimation issues. Researchers in both artificial intelligence and statistics should take it as a challenge to show how their methodologies can be used to help raise performance up to the level of human performance.

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Appendix: Confusion Matrices

X		del[X, Y] = Deletion of 'Y' after 'X' Y (Deleted Letter)																								
	a	b	c	d	e	f	g	h	i	j	k	ì	m	n	o	p	q	r	s	t	u	v	w	x	у	Z
a	0	7	58	21	3	5	18	8	61	0	4	43	5	53	0	9	0	98	28	53	62	1	0	0	2	0
b	2	2	1	0	22	0	0	0	183	0	0	26	0	0	2	0	0	6	17	0	6	1	0	0	0	0
c	37	0	70	0	63	0	0	24	320	0	9	17	0	0	33	0	0	46	6	54	17	0	0	0	1	0
d	12	0	7	25	45	0	10	0	62	1	1	8	4	3	3	0	0	11	1	0	3	2	0	0	6	0
e	80	1	50	74	89	3	1	1	6	0	0	32	9	76	19	9	1	237	223	34	8	2	1	7	1	0
f	4	0	0	0	13	46	0	0	79	0	0	12	0	0	4	0	0	11	0	8	1	0	0	0	1	0
g	25	0	0	2	83	1	37	25	39	0	0	3	0	29	4	0	0	52	7	1	22	0	0	0	1	0
h	15	12	1	3	20	0	0	25	24	0	0	7	1	9	22	0	0	15	1	26	0	0	1	0	1	0
i	26	1	60	26	23	1	9	0	1	0	0	38	14	82	41	7	0	16	71	64	1	1	0	0	1	7
j	0	0	0	0	1	0	0	0	0	0	0	0	0	1	1	0	0	0	0	0	1	0	0	0	0	0
k	4	0	0	1	15	1	8	1	5	0	1	3	0	17	0	0	0	1	5	0	0	0	1	0	0	0
1	24	0	1	6	48	0	0	0	217	0	0	211	2	0	29	0	0	2	12	7	3	2	0	0	11	0
m	15	10	0	0	33	0	0	1	42	0	0	0	180	7	7	31	0	0	9	0	4	0	0	0	0	0
n	21	0	42	71	68	1	160	0	191	0	0	0	17	144	21	0	0	0	127	87	43	1	1	0	2	0
o	11	4	3	6	8	0	5	0	4	1	0	13	9	70	26	20	0	98	20	13	47	2	5	0	1	0
p	25	0	0	0	22	0	0	12	15	0	0	28	1	0	30	93	0	58	1	18	2	0	0	0	0	0
q	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	18	0	0	0	0	0
r	63	4	12	19	188	0	11	5	132	0	3	33	7	157	21	2	0	277	103	68	0	10	1	0	27	0
s	16	0	27	0	74	1	0	18	231	0	0	2	1	0	30	30	0	4	265	124	21	0	0	0	1	0
t	24	1	2	0	76	1	7	49	427	0	0	31	3	3	11	1	0	203	5	137	14	0	4	0	2	0
u	26	6	9	10	15	0	1	0	28	0	0	39	2	111	1	0	0	129	31	66	0	0	0	0	1	0
V	9	0	0	0	58	0	0	0	31	0	0	0	0	0	2	0	0	1	0	0	0	0	0	0	1	0
W	40	0	0	1	11	1	0	11	15	0	0	1	0	2	2	0	0	2	24	0	0	0	0	0	0	0
X	1	0	17	0	3	0	0	1	0	0	0	0	0	0	0	6	0	0	0	5	0	0	0	0	1	0
у	2	1	34	0	2	0	1	0	1	0	0	1	2	1	1	1	0	0	17	1	0	0	1	0	0	0
Z	1	0	0	0	2	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2
(a)	20	14	41	31	20	20	7	6	20	3	6	22	16	5	5	17	0	28	26	6	2	1	24	0	0	2

X									a	dd[X		= Inse				er 'X	('									
	a	b	С	d	e	f	g	h	i	j	k	1	m	n	0	p	q	r	S	t	u	v	w	x	y	Z
a	15	1	14	7	10	0	1	1	33	1	4	31	2	39	12	4	3	28	134	7	28	0	1	1	4	1
b	3	11	0	0	7	0	1	0	50	0	0	15	0	1	1	0	0	5	16	0	0	3	0	0	0	0
c	19	0	54	1	13	0	0	18	50	0	3	1	1	1	7	1	0	7	25	7	8	4	0	1	0	0
d	18	0	3	17	14	2	0	0	9	0	0	6	1	9	13	0	0	6	119	0	0	0	0	0	5	0
e	39	2	8	76	147	2	0	1	4	0	3	4	6	27	5	1	0	83	417	6	4	1	10	2	8	0
c	1	Λ	Λ	0	2	27	1	Λ	12	Λ	Λ	10	Λ	Λ	Λ	Λ	Λ	5	22	Λ	1	Λ	Λ	Λ	1	Λ

	tinued	.)								;	_		= Inse			('aft	er '	X'								
X												Y (Ins	erted	Lette	r)											
	a	b	c	d	e	f	g	h	i	j	k	1	m	n	0	p	q	r	S	t	u	v	W	X	у	Z
h	4	1	0	1	24	0	10	18	17	2	0	1	0	1	4	0	0	16	24	22	1	0	5	0	3	0
i	10	3	13	13	25	0	1	1	69	2	1	17	11	33	27	1	0	9	30	29	11	0	0	1	0	1
j	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0
k	2	4	0	1	9	0	0	1	1	0	1	1	0	0	2	1	0	0	95	0	1	0	0	0	4	0
1	3	1	0	1	38	0	0	0	79	0	2	128	1	0	7	0	0	0	97	7	3	1	0	0	2	0
m	11	1	1	0	17	0	0	1	6	0	1	0	102	44	7	2	0	0	47	1	2	0	1	0	0	0
n	15	5	7	13	52	4	17	0	34	0	1	1	26	99	12	0	0	2	156	53	1	1	0	0	1	0
o	14	1	1	3	7	2	1	0	28	1	0	6	3	13	64	30	0	16	59	4	19	1	0	0	1	1
p	23	0	1	1	10	0	0	20	3	0	0	2	0	0	26	70	0	29	52	9	1	1	1	0	0	0
q	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0
r	15	2	1	0	89	1	1	2	64	0	0	5	9	7	10	0	0	132	273	29	7	0	1	0	10	0
s	13	1	7	20	41	0	1	50	101	0	2	2	10	7	3	1	0	1	205	49	7	0	1	0	7	0
t	39	0	0	3	65	1	10	24	59	1	0	6	3	1	23	1	0	54	264	183	11	0	5	0	6	0
u	15	0	3	0	9	0	0	1	24	1	1	3	3	9	1	3	0	49	19	27	26	0	0	2	3	0
V	0	2	0	0	36	0	0	0	10	0	0	1	0	1	0	1	0	0	0	0	1	5	1	0	0	0
\mathbf{w}	0	0	0	1	10	0	0	1	1	0	1	1	0	2	0	0	1	1	8	0	2	0	4	0	0	0
X	0	0	18	0	1	0	0	6	1	0	0	0	1	0	3	0	0	0	2	0	0	0	0	1	0	0
у	5	1	2	0	3	0	0	0	2	0	0	1	1	6	0	0	0	1	33	1	13	0	1	0	2	0
Z	2	0	0	0	5	1	0	0	6	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2	4
<u>@</u>	46	8	9	8	26	11	14	3	5	1	17	5	6	2	2	10	0	6	23	2	11	1	2	1	1	2

						su	sub[X, Y] = Substitution of 'X' (incorrect) for 'Y' (correct) Y (correct)																			
X													(cori	ect)												
	a	b	_ c	d _	e	f —	g	h	i	j	k	l 	m	n	0	p	q	r	s	t	u	v	w	Х	У	Z
a	0	0	7	1	342	0	0	2	118	0	1	0	0	3	76	0	0	1	35	9	9	0	1	0	5	0
b	0	0	9	9	2	2	3	1	0	0	0	5	11	5	0	10	0	0	2	1	0	0	8	0	0	0
c	6	5	0	16	0	9	5	0	0	0	1	0	7	9	1	10	2	5	39	40	1	3	7	1	1	0
d	1	10	13	0	12	0	5	5	0	0	2	3	7	3	0	1	0	43	30	22	0	0	4	0	2	0
e	388	0	3	11	0	2	2	0	89	0	0	3	0	5	93	0	0	14	12	6	15	0	1	0	18	0
f	0	15	0	3	1	0	5	2	0	0	0	3	4	1	0	0	0	6	4	12	0	0	2	0	0	0
g	4	1	11	11	9	2	0	0	0	1	1	3	0	0	2	1	3	5	13	21	0	0	1	0	3	0
h	1	8	0	3	0	0	0	0	0	0	2	0	12	14	2	3	0	3	1	11	0	0	2	0	0	0
i	103	0	0	0	146	0	1	0	0	0	0	6	0	0	49	0	0	0	2	1	47	0	2	1	15	0
j	0	1	1	9	0	0	l	0	0	0	0	2	1	0	0	0	0	0	5	0	0	0	0	0	0	0
k	1	2	8	4	1	1	2	5	0	0	0	0	5	0	2	0	0	0	6	0	0	0	4	0	0	3
1	2	10	1	4	0	4	5	6	13	0	1	0	0	14	2	5	0	11	10	2	0	0	0	0	0	0
m	1	3	7	8	0	2	0	6	0	0	4	4	0	180	0	6	0	0	9	15	13	3	2	2	3	0
n	2	7	6	5	3	0	1	19	1	0	4	35	78	0	0	7	0	28	5	7	0	0	1	2	0	2
o	91	1	1	3	116	0	0	0	25	0	2	0	0	0	0	14	0	2	4	14	39	0	0	0	18	0
p	0	11	1	2	0	6	5	. 0	2	9	0	2	7	6	15	0	0	1	3	6	0	4	1	0	0	0
q	0	0	1	0	0	0	27	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
r	0	14	0	30	12	2	2	8	2	0	5	8	4	20	1	14	0	0	12	22	4	0	0	1	0	0
s	11	8	27	33	35	4	0	1	0	1	0	27	0	6	1	7	0	14	0	15	0	0	5	3	20	1
t	3	4	9	42	7	5	19	5	0	1	0	14	9	5	5	6	0	11	37	0	0	2	19	0	7	6
u	20	0	0	0	44	0	0	0	64	0	0	0	0	2	43	0	0	4	0	0	0	0	2	0	8	0
v	0	0	7	0	0	3	0	0	0	0	0	1	0	0	1	0	0	0	8	3	0	0	0	0	0	0
w	2	2	1	0	1	0	0	2	0	0	1	0	0	0	0	7	0	6	3	3	1	0	0	0	0	0
X	0	0	0	2	0	0	0	0	0	0	0	0	0	0	0	0	0	0	9	0	0	0	0	0	0	0
y	0	0	2	0	15	0	1	7	15	0	0	0	2	0	6	1	0	7	36	8	5	0	0	1	0	0
Z	0	0	0	7	0	0	0	0	0	0	0	7	5	0	0	0	0	2	21	3	0	0	0	0	3	.0

reviX	VI	= Reversal	l of	'XV'
IEVIA.	11	= $neversa$		A 1

\mathbf{X}														Y												
	a	b	c	d	e	f	g	h	i	j	k	1	m	n	o	p	q	r	s	t	u	V	W	X	y	Z
a	0	0	2	1	1	0	0	0	19	0	1	14	4	25	10	3	0	27	3	5	31	0	0	0	0	0
b	0	0	0	0	2	0	0	0	0	0	0	1	1	0	2	0	0	0	2	0	0	0	0	0	0	0
С	0	0	0	0	1	0	0	1	85	0	0	15	0	0	13	0	0	0	3	0	7	0	0	0	0	0
d	0	0	0	0	0	0	0	0	7	0	0	0	0	0	0	0	0	1	0	0	2	0	0	0	0	0
e	1	0	4	5	0	0	0	0	60	0	0	21	6	16	11	2	0	29	5	0	85	0	0	0	2	0
f	0	0	0	0	0	0	0	0	12	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0
g	4	0	0	0	2	0	0	0	0	0	0	1	0	15	0	0	0	3	0	0	3	0	0	0	0	0
h	12	0	0	0	15	0	0	0	0	0	0	0	0	0	0	0	0	0	0	10	0	0	0	0	0	0
i	15	8	31	3	66	1	3	0	0	0	0	9	0	5	11	0	1	13	42	35	0	6	0	0	0	3
j	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
k	0	0	0	0	2	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
1	11	0	0	12	20	0	1	0	4	0	0	0	0	0	1	3	0	0	1	1	3	9	0	0	7	0
m	9	0	0	0	20	0	0	0	0	0	0	0	0	2	0	0	0	0	0	0	4	0	0	0	0	0
n	15	0	6	2	12	0	8	0	1	0	0	0	3	0	0	0	0	0	6	4	0	0	0	0	0	0
O	5	0	2	0	4	0	0	0	5	0	0	1	0	5	0	1	0	11	1	1	0	0	7	1	0	0
p	17	0	0	0	4	0	0	1	0	0	0	0	0	0	1	0	0	5	3	6	0	0	0	0	0	0
q	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
r	12	0	0	0	24	0	3	0	14	0	2	2	0	7	30	1	0	0	0	2	10	0	0	0	2	0
S	4	0	0	0	9	0	0	5	15	0	0	5	2	0	1	22	0	0	0	1	3	0	0	0	16	0
t	4	0	3	0	4	0	0	21	49	0	0	4	0	0	3	0	0	5	0	0	11	0	2	0	0	0
u	22	0	5	1	I	0	2	0	2	0	0	2	1	0	20	2	0	11	11	2	0	0	0	0	0	0
V	0	0	0	0	1	0	0	0	4	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
W	0	0	0	0	0	0	0	4	0	0	0	0	1	1	1	0	0	0	0	0	0	0	0	0	8	0
X	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0
У	0	1	2	0	0	0	1	0	0	0	0	3	0	0	0	2	0	1	10	0	0	0	0	0	0	0
Z	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0