­­­­Title: Raspberry Pi 2B+ runs FFT on GPU and CPU, energy and power comparison

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# GPU part:

Library name: GPU\_FFT

Written by: Andrew Holme

## Library description:

Reference:

ACCELERATING FOURIER TRANSFORMS USING THE GPU

<https://www.raspberrypi.org/blog/accelerating-fourier-transforms-using-the-gpu/>

General purpose code for the VideoCore IV graphics processing unit(GPU) in the BCM2835. To create an accelerated Fast Fourier Transform library. Taking the Fourier transform of a function yields its frequency spectrum (i.e. the pure harmonic functions which can be added together to reconstruct the original function).

GPU\_FFT is an FFT library for the Raspberry Pi which exploits the BCM2835 SoC V3D hardware to deliver ten times the performance that is possible on the 700 MHz ARM. Kernels are provided for all power-of-2 FFT lengths from 256 to 131,072 points inclusive.

GPU\_FFT uses single-precision floating point for data and twiddle factors, so it does not compete on accuracy with double-precision libraries; however, the relative root-mean-square (rms) error for a 2048-point transform is less than one part per million, which is not bad.

The library runs on dedicated 3D hardware in the BCM2835 SoC, and communication between ARM and GPU adds 100µs of latency which is much longer than the shortest transform takes to compute! To overcome this, batches of transforms can be executed with a single call. Typical per-transform runtimes in microseconds are:

|  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- |
| Points | batch=1 | batch=10 | batch=50 | FFTW | Speedup |
| 256 | 112 | 22 | 16 | 92 | 5.8x |
| 512 | 125 | 37 | 26 | 217 | 8.3x |
| 1024 | 136 | 54 | 45 | 482 | 10.7x |
| 2048 | 180 | 107 | 93 | 952 | 10.2x |
| 4096 | 298 | 256 | 240 | 3002 | 12.5x |
| 8192 | 689 | 624 | 608 | 5082 | 8.4x |
| 16384 | 1274 | 1167 | 1131 | 12005 | 10.6x |
| 32768 | 3397 | 3225 | 3196 | 31211 | 9.8x |
| 65536 | 6978 | 6703 | 6674 | 82769 | 12.4x |
| 131072 | 16734 | 16110 | 16171 | 183731 | 11.4x |

## ­Library usage:

Being able to perform lots of Fourier transforms quickly is useful for all sorts of audio and radio applications including, unsurprisingly, GPS. Ham radio enthusiasts will also find Andrew’s work very useful.

Last October, Eben attended the Radio Society of Great Britain (RSGB) Convention, where radio amateurs told him they wanted a speedy fast Fourier transform (FFT) library to do Software Defined Radio (SDR) projects on the Pi.

## Library operate:

To get GPU\_FFT enter the following at the command prompt:

sudo rpi-update && sudo reboot

To build and run the example program:

directory:

cd /opt/vc/src/hello\_pi/hello\_fft

make

sudo mknod char\_dev c 100 0

sudo ./hello\_fft.bin

API documentation can be found in the hello\_fft folder.

File: hello\_fft usage:

$ sudo ./hello\_fft.bin

Usage: hello\_fft.bin log2\_N [jobs [loops]]

log2\_N = log2(FFT\_length), log2\_N = 8...22

jobs = transforms per batch, jobs>0, default 1

loops = number of test repeats, loops>0, default 1

e.g.

$ sudo ./hello\_fft.bin 8

rel\_rms\_err = 3.3e-07, usecs = 45, k = 0

$ sudo ./hello\_fft.bin 22

rel\_rms\_err = 1.5e-06, usecs = 782379, k = 0

$ sudo ./hello\_fft.bin 8 2 2

rel\_rms\_err = 3.1e-07, usecs = 33, k = 0

rel\_rms\_err = 3.1e-07, usecs = 23, k = 1

## Library details:

Reference: gpu\_fft.txt from the library hello\_fft

BCM2835 "GPU\_FFT" release 3.0 by Andrew Holme, 2015.

GPU\_FFT is an FFT library for the Raspberry Pi which exploits the BCM2835 SoC

3D hardware to deliver ten times more data throughput than is possible on the

700 MHz ARM of the Pi 1. Kernels are provided for all power-of-2 FFT lengths

between 256 and 4,194,304 points inclusive. A transpose function, which also

uses the 3D hardware, is provided to support 2-dimensional transforms.

\*\*\* Accuracy \*\*\*

GPU\_FFT uses single-precision floats for data and twiddle factors. The output

is not scaled. The relative root-mean-square (rms) error in parts-per-million

(ppm) for different transform lengths (N) is typically:

log2(N) | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15

ppm rms | 0.33 | 0.46 | 0.52 | 0.59 | 0.78 | 0.83 | 0.92 | 0.98

log2(N) | 16 | 17 | 18 | 19 | 20 | 21 | 22

ppm rms | 1.0 | 1.3 | 1.3 | 1.4 | 1.5 | 1.5 | 1.5

Accuracy has improved significantly over previous releases at the expense of a

small (2%) performance hit; however, FFTW is still one order of magnitude more

accurate than GPU\_FFT.

\*\*\* Throughput \*\*\*

GPU\_FFT 1.0 had to be invoked through a "mailbox" which added a 100us overhead

on every call. To mitigate this, batches of transforms could be submitted via

a single call. GPU\_FFT now avoids this 100us overhead by poking GPU registers

directly from the ARM if total batch runtime will be short; but still uses the

mailbox for longer jobs to avoid busy waiting at 100% CPU for too long.

Typical per-transform runtimes for batch sizes of 1 and 10; and comparative

figures for FFTW (FFTW\_MEASURE mode) on a Pi 1 with L2 cache enabled are:

log2(N) | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15

1 | 0.033 | 0.049 | 0.070 | 0.12 | 0.25 | 0.61 | 1.2 | 3.5

10 | 0.017 | 0.029 | 0.049 | 0.11 | 0.27 | 0.66 | 1.2 | 3.3

FFTW | 0.092 | 0.22 | 0.48 | 0.95 | 3.0 | 5.1 | 12 | 31

log2(N) | 16 | 17 | 18 | 19 | 20 | 21 | 22 All times in

1 | 7.0 | 17 | 43 | 97 | 194 | 388 | 786 milliseconds

FFTW | 83 | 180 | 560 | 670 | 1600 | 3400 | 8800 2 sig. figs.

\*\*\* API functions \*\*\*

gpu\_fft\_prepare() Call once to allocate memory and initialise data

structures. Returns 0 for success.

gpu\_fft\_execute() Call one or more times to execute a previously

prepared FFT batch. Returns 0 for success.

gpu\_fft\_release() Call once to release resources after use.

GPU memory is permanently lost if not freed.

\*\*\* Parameters \*\*\*

int mb Mailbox file descriptor obtained by calling mbox\_open()

int log2\_N log2(FFT length) = 8 to 22

int direction FFT direction: GPU\_FFT\_FWD for forward FFT

GPU\_FFT\_REV for inverse FFT

int jobs Number of transforms in batch = 1 or more

GPU\_FFT \*\* Output parameter from prepare: control structure.

GPU\_FFT \* Input parameter to execute and release

\*\*\* Data format \*\*\*

Complex data arrays are stored as alternate real and imaginary parts:

struct GPU\_FFT\_COMPLEX {

float re, im;

};

The GPU\_FFT struct created by gpu\_fft\_prepare() contains pointers to the input

and output arrays:

struct GPU\_FFT {

struct GPU\_FFT\_COMPLEX \*in, \*out;

When executing a batch of transforms, buffer pointers are obtained as follows:

struct GPU\_FFT \*fft = gpu\_fft\_prepare( ... , jobs);

for (int j=0; j<jobs; j++) {

struct GPU\_FFT\_COMPLEX \*in = fft->in + j\*fft->step;

struct GPU\_FFT\_COMPLEX \*out = fft->out + j\*fft->step;

GPU\_FFT.step is greater than FFT length because a guard space is left between

buffers for caching and alignment reasons.

GPU\_FFT performs multiple passes between ping-pong buffers. The final output

lands in the same buffer as input after an even number of passes. Transforms

where log2\_N=12...16 use an odd number of passes and the final result is left

out-of-place. The input data is never preserved.

GPU\_FFT and Open GL will run concurrently on Pi 1 if GPU\_FFT is configured not

to use VC4 L2 cache by zeroing a define in file gpu\_fft\_base.c as follows:

#define GPU\_FFT\_USE\_VC4\_L2\_CACHE 0 // Pi 1 only: cached=1; direct=0

Overall performance will probably be higher if GPU\_FFT and Open GL take turns

at using the 3D hardware. Since eglSwapBuffers() returns immediately without

waiting for rendering, call glFlush() and glFinish() afterwards as follows:

## Library results:

pi@raspberrypi:/opt/vc/src/hello\_pi/hello\_fft $ sudo ./hello\_fft.bin 8 1 1

rel\_rms\_err = 3.3e-07, usecs = 44, k = 0

pi@raspberrypi:/opt/vc/src/hello\_pi/hello\_fft $ sudo ./hello\_fft.bin 8 2 1

rel\_rms\_err = 3.1e-07, usecs = 30, k = 0

pi@raspberrypi:/opt/vc/src/hello\_pi/hello\_fft $ sudo ./hello\_fft.bin 8 4 1

rel\_rms\_err = 2.8e-07, usecs = 22, k = 0

pi@raspberrypi:/opt/vc/src/hello\_pi/hello\_fft $ sudo ./hello\_fft.bin 8 8 1

rel\_rms\_err = 2.7e-07, usecs = 19, k = 0

pi@raspberrypi:/opt/vc/src/hello\_pi/hello\_fft $ sudo ./hello\_fft.bin 8 16 1

rel\_rms\_err = 2.6e-07, usecs = 28, k = 0

pi@raspberrypi:/opt/vc/src/hello\_pi/hello\_fft $ sudo ./hello\_fft.bin 8 32 1

rel\_rms\_err = 2.6e-07, usecs = 17, k = 0

pi@raspberrypi:/opt/vc/src/hello\_pi/hello\_fft $ sudo ./hello\_fft.bin 8 64 1

rel\_rms\_err = 2.5e-07, usecs = 16, k = 0

pi@raspberrypi:/opt/vc/src/hello\_pi/hello\_fft $ sudo ./hello\_fft.bin 8 16 1

rel\_rms\_err = 2.6e-07, usecs = 17, k = 0

pi@raspberrypi:/opt/vc/src/hello\_pi/hello\_fft $ sudo ./hello\_fft.bin 8 128 1

rel\_rms\_err = 0.062, usecs = 17, k = 0

pi@raspberrypi:/opt/vc/src/hello\_pi/hello\_fft $ sudo ./hello\_fft.bin 8 256 1

rel\_rms\_err = 0.062, usecs = 16, k = 0

pi@raspberrypi:/opt/vc/src/hello\_pi/hello\_fft $ sudo ./hello\_fft.bin 8 512 1

rel\_rms\_err = 0.71, usecs = 15, k = 0

pi@raspberrypi:/opt/vc/src/hello\_pi/hello\_fft $ sudo ./hello\_fft.bin 8 1024 1

rel\_rms\_err = 0.94, usecs = 15, k = 0

pi@raspberrypi:/opt/vc/src/hello\_pi/hello\_fft $ sudo ./hello\_fft.bin 8 2048 1

rel\_rms\_err = 1, usecs = 15, k = 0

pi@raspberrypi:/opt/vc/src/hello\_pi/hello\_fft $ sudo ./hello\_fft.bin 8 4096 1

rel\_rms\_err = 1.1, usecs = 15, k = 0

pi@raspberrypi:/opt/vc/src/hello\_pi/hello\_fft $ sudo ./hello\_fft.bin 8 8192 1

rel\_rms\_err = 1.1, usecs = 15, k = 0

pi@raspberrypi:/opt/vc/src/hello\_pi/hello\_fft $ sudo ./hello\_fft.bin 8 1 4

rel\_rms\_err = 3.3e-07, usecs = 44, k = 0

rel\_rms\_err = 3.3e-07, usecs = 31, k = 1

rel\_rms\_err = 3.3e-07, usecs = 31, k = 2

rel\_rms\_err = 3.3e-07, usecs = 31, k = 3

pi@raspberrypi:/opt/vc/src/hello\_pi/hello\_fft $ sudo ./hello\_fft.bin 8 1 8

rel\_rms\_err = 3.3e-07, usecs = 51, k = 0

rel\_rms\_err = 3.3e-07, usecs = 31, k = 1

rel\_rms\_err = 3.3e-07, usecs = 32, k = 2

rel\_rms\_err = 3.3e-07, usecs = 32, k = 3

rel\_rms\_err = 3.3e-07, usecs = 32, k = 4

rel\_rms\_err = 3.3e-07, usecs = 33, k = 5

rel\_rms\_err = 3.3e-07, usecs = 31, k = 6

rel\_rms\_err = 3.3e-07, usecs = 31, k = 7

pi@raspberrypi:/opt/vc/src/hello\_pi/hello\_fft $ sudo ./hello\_fft.bin 8 1 16

rel\_rms\_err = 3.3e-07, usecs = 43, k = 0

rel\_rms\_err = 3.3e-07, usecs = 31, k = 1

rel\_rms\_err = 3.3e-07, usecs = 32, k = 2

rel\_rms\_err = 3.3e-07, usecs = 31, k = 3

rel\_rms\_err = 3.3e-07, usecs = 32, k = 4

rel\_rms\_err = 3.3e-07, usecs = 33, k = 5

rel\_rms\_err = 3.3e-07, usecs = 32, k = 6

rel\_rms\_err = 3.3e-07, usecs = 31, k = 7

rel\_rms\_err = 3.3e-07, usecs = 30, k = 8

rel\_rms\_err = 3.3e-07, usecs = 30, k = 9

rel\_rms\_err = 3.3e-07, usecs = 30, k = 10

rel\_rms\_err = 3.3e-07, usecs = 30, k = 11

rel\_rms\_err = 3.3e-07, usecs = 29, k = 12

rel\_rms\_err = 3.3e-07, usecs = 31, k = 13

rel\_rms\_err = 3.3e-07, usecs = 30, k = 14

rel\_rms\_err = 3.3e-07, usecs = 31, k = 15

pi@raspberrypi:/opt/vc/src/hello\_pi/hello\_fft $ sudo ./hello\_fft.bin 8 1 32

rel\_rms\_err = 3.3e-07, usecs = 46, k = 0

rel\_rms\_err = 3.3e-07, usecs = 31, k = 1

rel\_rms\_err = 3.3e-07, usecs = 32, k = 2

rel\_rms\_err = 3.3e-07, usecs = 31, k = 3

rel\_rms\_err = 3.3e-07, usecs = 32, k = 4

rel\_rms\_err = 3.3e-07, usecs = 31, k = 5

rel\_rms\_err = 3.3e-07, usecs = 32, k = 6

rel\_rms\_err = 3.3e-07, usecs = 30, k = 7

rel\_rms\_err = 3.3e-07, usecs = 31, k = 8

rel\_rms\_err = 3.3e-07, usecs = 29, k = 9

rel\_rms\_err = 3.3e-07, usecs = 29, k = 10

rel\_rms\_err = 3.3e-07, usecs = 29, k = 11

rel\_rms\_err = 3.3e-07, usecs = 29, k = 12

rel\_rms\_err = 3.3e-07, usecs = 30, k = 13

rel\_rms\_err = 3.3e-07, usecs = 32, k = 14

rel\_rms\_err = 3.3e-07, usecs = 31, k = 15

rel\_rms\_err = 3.3e-07, usecs = 30, k = 16

rel\_rms\_err = 3.3e-07, usecs = 30, k = 17

rel\_rms\_err = 3.3e-07, usecs = 30, k = 18

rel\_rms\_err = 3.3e-07, usecs = 29, k = 19

rel\_rms\_err = 3.3e-07, usecs = 30, k = 20

rel\_rms\_err = 3.3e-07, usecs = 30, k = 21

rel\_rms\_err = 3.3e-07, usecs = 29, k = 22

rel\_rms\_err = 3.3e-07, usecs = 29, k = 23

rel\_rms\_err = 3.3e-07, usecs = 29, k = 24

rel\_rms\_err = 3.3e-07, usecs = 29, k = 25

rel\_rms\_err = 3.3e-07, usecs = 30, k = 26

rel\_rms\_err = 3.3e-07, usecs = 29, k = 27

rel\_rms\_err = 3.3e-07, usecs = 29, k = 28

rel\_rms\_err = 3.3e-07, usecs = 29, k = 29

rel\_rms\_err = 3.3e-07, usecs = 29, k = 30

rel\_rms\_err = 3.3e-07, usecs = 31, k = 31

pi@raspberrypi:/opt/vc/src/hello\_pi/hello\_fft $ sudo ./hello\_fft.bin 22 1 1

rel\_rms\_err = 1.5e-06, usecs = 781473, k = 0

pi@raspberrypi:/opt/vc/src/hello\_pi/hello\_fft $ sudo ./hello\_fft.bin 22 2 1

rel\_rms\_err = 1.5e-06, usecs = 783190, k = 0

pi@raspberrypi:/opt/vc/src/hello\_pi/hello\_fft $ sudo ./hello\_fft.bin 22 4 1

Out of memory. Try a smaller batch or increase GPU memory.

pi@raspberrypi:/opt/vc/src/hello\_pi/hello\_fft $ sudo ./hello\_fft.bin 22 8 1

Out of memory. Try a smaller batch or increase GPU memory.

pi@raspberrypi:/opt/vc/src/hello\_pi/hello\_fft $ sudo ./hello\_fft.bin 22 2 2

rel\_rms\_err = 1.5e-06, usecs = 785348, k = 0

rel\_rms\_err = 1.5e-06, usecs = 781543, k = 1

pi@raspberrypi:/opt/vc/src/hello\_pi/hello\_fft $ sudo ./hello\_fft.bin 22 2 4

rel\_rms\_err = 1.5e-06, usecs = 781577, k = 0

rel\_rms\_err = 1.5e-06, usecs = 778754, k = 1

rel\_rms\_err = 1.5e-06, usecs = 778890, k = 2

rel\_rms\_err = 1.5e-06, usecs = 778164, k = 3

$ cd /opt/vc/src/hello\_pi/hello\_fft

$ sudo perf\_3.16 stat -d ./hello\_fft.bin 21 4

rel\_rms\_err = 1.5e-06, usecs = 384048, k = 0

Performance counter stats for './hello\_fft.bin 21 4':

16611.682000 task-clock (msec) # 0.884 CPUs utilized

331 context-switches # 0.020 K/sec

0 cpu-migrations # 0.000 K/sec

16,477 page-faults # 0.992 K/sec

11,577,399,763 cycles # 0.697 GHz [37.56%]

1,285,911,727 stalled-cycles-frontend # 11.11% frontend cycles idle [37.54%]

11,624,766 stalled-cycles-backend # 0.10% backend cycles idle [37.36%]

3,590,951,918 instructions # 0.31 insns per cycle

# 0.36 stalled cycles per insn [24.99%]

491,596,173 branches # 29.593 M/sec [25.14%]

12,319,210 branch-misses # 2.51% of all branches [25.08%]

27,138,104 L1-dcache-loads # 1.634 M/sec [25.06%]

697,059 L1-dcache-load-misses # 2.57% of all L1-dcache hits [25.08%]

<not supported> LLC-loads

<not supported> LLC-load-misses

18.790153624 seconds time elapsed

$ cd ~/QH\_directory/userland/host\_applications/linux/apps/hello\_pi/hello\_fft

$ sudo perf\_3.16 stat -d ./hello\_fft.bin 20 10

rel\_rms\_err = 1.4e-06, usecs = 192471, k = 0

Performance counter stats for './hello\_fft.bin 20 10':

20842.337000 task-clock (msec) # 0.812 CPUs utilized

599 context-switches # 0.029 K/sec

0 cpu-migrations # 0.000 K/sec

20,571 page-faults # 0.987 K/sec

14,530,940,586 cycles # 0.697 GHz [37.67%]

1,611,996,079 stalled-cycles-frontend # 11.09% frontend cycles idle [37.42%]

14,560,086 stalled-cycles-backend # 0.10% backend cycles idle [37.28%]

4,522,659,463 instructions # 0.31 insns per cycle

# 0.36 stalled cycles per insn [24.94%]

615,849,834 branches # 29.548 M/sec [25.04%]

14,833,907 branch-misses # 2.41% of all branches [25.11%]

32,706,289 L1-dcache-loads # 1.569 M/sec [25.19%]

1,152,936 L1-dcache-load-misses # 3.53% of all L1-dcache hits [25.16%]

<not supported> LLC-loads

<not supported> LLC-load-misses

25.663854775 seconds time elapsed

$ sudo perf\_3.16 stat -d ./hello\_fft.bin 20 1

rel\_rms\_err = 1.5e-06, usecs = 191712, k = 0

Performance counter stats for './hello\_fft.bin 20 1':

2073.859000 task-clock (msec) # 0.895 CPUs utilized

45 context-switches # 0.022 K/sec

0 cpu-migrations # 0.000 K/sec

2,138 page-faults # 0.001 M/sec

1,445,726,218 cycles # 0.697 GHz [37.45%]

168,054,051 stalled-cycles-frontend # 11.62% frontend cycles idle [37.85%]

2,340,102 stalled-cycles-backend # 0.16% backend cycles idle [38.15%]

439,204,097 instructions # 0.30 insns per cycle

# 0.38 stalled cycles per insn [25.45%]

60,354,270 branches # 29.102 M/sec [25.31%]

1,630,240 branch-misses # 2.70% of all branches [25.16%]

4,900,540 L1-dcache-loads # 2.363 M/sec [25.60%]

155,059 L1-dcache-load-misses # 3.16% of all L1-dcache hits [25.15%]

<not supported> LLC-loads

<not supported> LLC-load-misses

2.316615205 seconds time elapsed

$ sudo perf\_3.16 stat -d ./hello\_fft.bin 20 10 1

rel\_rms\_err = 1.4e-06, usecs = 192392, k = 0

Performance counter stats for './hello\_fft.bin 20 10 1':

20795.216000 task-clock (msec) # 0.820 CPUs utilized

622 context-switches # 0.030 K/sec

0 cpu-migrations # 0.000 K/sec

20,571 page-faults # 0.989 K/sec

14,462,479,493 cycles # 0.695 GHz [37.65%]

1,591,452,238 stalled-cycles-frontend # 11.00% frontend cycles idle [37.42%]

14,030,599 stalled-cycles-backend # 0.10% backend cycles idle [37.63%]

4,527,389,098 instructions # 0.31 insns per cycle

# 0.35 stalled cycles per insn [25.28%]

618,832,550 branches # 29.758 M/sec [25.06%]

14,727,795 branch-misses # 2.38% of all branches [24.83%]

36,632,522 L1-dcache-loads # 1.762 M/sec [24.99%]

997,478 L1-dcache-load-misses # 2.72% of all L1-dcache hits [25.00%]

<not supported> LLC-loads

<not supported> LLC-load-misses

25.369885801 seconds time elapsed

$ sudo perf\_3.16 stat -d ./hello\_fft.bin 20 10 2

rel\_rms\_err = 1.4e-06, usecs = 193745, k = 0

rel\_rms\_err = 1.4e-06, usecs = 194533, k = 1

Performance counter stats for './hello\_fft.bin 20 10 2':

41489.336000 task-clock (msec) # 0.813 CPUs utilized

1,241 context-switches # 0.030 K/sec

0 cpu-migrations # 0.000 K/sec

20,567 page-faults # 0.496 K/sec

28,924,373,678 cycles # 0.697 GHz [37.64%]

3,146,747,530 stalled-cycles-frontend # 10.88% frontend cycles idle [37.61%]

27,314,821 stalled-cycles-backend # 0.09% backend cycles idle [37.43%]

9,032,409,981 instructions # 0.31 insns per cycle

# 0.35 stalled cycles per insn [24.85%]

1,234,499,221 branches # 29.755 M/sec [24.84%]

29,373,667 branch-misses # 2.38% of all branches [25.05%]

59,944,125 L1-dcache-loads # 1.445 M/sec [25.11%]

2,015,937 L1-dcache-load-misses # 3.36% of all L1-dcache hits [25.19%]

<not supported> LLC-loads

<not supported> LLC-load-misses

51.033239728 seconds time elapsed

pi@raspberrypi:~/QH\_directory/userland/host\_applications/linux/apps/hello\_pi/hello\_fft $ sudo perf\_3.16 stat -d ./hello\_fft.bin 20 1

rel\_rms\_err = 1.5e-06, usecs = 191971, k = 0

Performance counter stats for './hello\_fft.bin 20 1':

2064.348000 task-clock (msec) # 0.733 CPUs utilized

97 context-switches # 0.047 K/sec

0 cpu-migrations # 0.000 K/sec

2,139 page-faults # 0.001 M/sec

1,434,184,235 cycles # 0.695 GHz [37.63%]

172,340,145 stalled-cycles-frontend # 12.02% frontend cycles idle [38.27%]

2,299,751 stalled-cycles-backend # 0.16% backend cycles idle [37.83%]

433,672,117 instructions # 0.30 insns per cycle

# 0.40 stalled cycles per insn [25.32%]

59,474,670 branches # 28.810 M/sec [25.38%]

1,597,489 branch-misses # 2.69% of all branches [25.16%]

2,826,475 L1-dcache-loads # 1.369 M/sec [25.21%]

100,975 L1-dcache-load-misses # 3.57% of all L1-dcache hits [25.07%]

<not supported> LLC-loads

<not supported> LLC-load-misses

2.817823205 seconds time elapsed

pi@raspberrypi:~/QH\_directory/userland/host\_applications/linux/apps/hello\_pi/hello\_fft $ sudo perf\_3.16 stat -d ./hello\_fft.bin 21 1

rel\_rms\_err = 1.5e-06, usecs = 385656, k = 0

Performance counter stats for './hello\_fft.bin 21 1':

4087.019000 task-clock (msec) # 0.796 CPUs utilized

125 context-switches # 0.031 K/sec

0 cpu-migrations # 0.000 K/sec

4,188 page-faults # 0.001 M/sec

2,829,402,817 cycles # 0.692 GHz [37.27%]

307,584,517 stalled-cycles-frontend # 10.87% frontend cycles idle [37.38%]

3,192,126 stalled-cycles-backend # 0.11% backend cycles idle [37.79%]

894,395,400 instructions # 0.32 insns per cycle

# 0.34 stalled cycles per insn [25.04%]

121,646,131 branches # 29.764 M/sec [24.90%]

3,196,376 branch-misses # 2.63% of all branches [25.66%]

4,984,933 L1-dcache-loads # 1.220 M/sec [25.60%]

136,897 L1-dcache-load-misses # 2.75% of all L1-dcache hits [24.81%]

<not supported> LLC-loads

<not supported> LLC-load-misses

5.136850680 seconds time elapsed

pi@raspberrypi:~/QH\_directory/userland/host\_applications/linux/apps/hello\_pi/hello\_fft $ sudo perf\_3.16 stat -d ./hello\_fft.bin 22 1

rel\_rms\_err = 1.5e-06, usecs = 816007, k = 0

Performance counter stats for './hello\_fft.bin 22 1':

8195.111000 task-clock (msec) # 0.740 CPUs utilized

325 context-switches # 0.040 K/sec

0 cpu-migrations # 0.000 K/sec

8,290 page-faults # 0.001 M/sec

5,682,711,188 cycles # 0.693 GHz [37.49%]

623,837,550 stalled-cycles-frontend # 10.98% frontend cycles idle [37.61%]

5,347,961 stalled-cycles-backend # 0.09% backend cycles idle [37.66%]

1,778,767,421 instructions # 0.31 insns per cycle

# 0.35 stalled cycles per insn [25.04%]

243,544,562 branches # 29.718 M/sec [25.07%]

6,518,812 branch-misses # 2.68% of all branches [25.06%]

11,374,739 L1-dcache-loads # 1.388 M/sec [24.88%]

353,800 L1-dcache-load-misses # 3.11% of all L1-dcache hits [25.13%]

<not supported> LLC-loads

<not supported> LLC-load-misses

11.069579943 seconds time elapsed

pi@raspberrypi:~/QH\_directory/userland/host\_applications/linux/apps/hello\_pi/hello\_fft $ sudo perf\_3.16 stat -d ./hello\_fft.bin 22 2

rel\_rms\_err = 1.5e-06, usecs = 780728, k = 0

Performance counter stats for './hello\_fft.bin 22 2':

16371.392000 task-clock (msec) # 0.777 CPUs utilized

545 context-switches # 0.033 K/sec

0 cpu-migrations # 0.000 K/sec

16,477 page-faults # 0.001 M/sec

11,410,947,128 cycles # 0.697 GHz [37.61%]

1,212,675,629 stalled-cycles-frontend # 10.63% frontend cycles idle [37.48%]

9,727,120 stalled-cycles-backend # 0.09% backend cycles idle [37.46%]

3,567,023,001 instructions # 0.31 insns per cycle

# 0.34 stalled cycles per insn [25.31%]

487,332,922 branches # 29.767 M/sec [25.12%]

12,476,017 branch-misses # 2.56% of all branches [24.87%]

20,425,838 L1-dcache-loads # 1.248 M/sec [24.96%]

839,717 L1-dcache-load-misses # 4.11% of all L1-dcache hits [25.03%]

<not supported> LLC-loads

<not supported> LLC-load-misses

21.075656071 seconds time elapsed

pi@raspberrypi:~/QH\_directory/userland/host\_applications/linux/apps/hello\_pi/hello\_fft $ sudo perf\_3.16 stat -d ./hello\_fft.bin 22 4

Out of memory. Try a smaller batch or increase GPU memory.

Performance counter stats for './hello\_fft.bin 22 4':

14.344000 task-clock (msec) # 0.357 CPUs utilized

5 context-switches # 0.349 K/sec

0 cpu-migrations # 0.000 K/sec

81 page-faults # 0.006 M/sec

3,348,372 cycles # 0.233 GHz

5,342,282 stalled-cycles-frontend # 159.55% frontend cycles idle

360,832 stalled-cycles-backend # 10.78% backend cycles idle

<not counted> instructions

<not counted> branches

<not counted> branch-misses

<not counted> L1-dcache-loads

<not counted> L1-dcache-load-misses

<not supported> LLC-loads

<not supported> LLC-load-misses

0.040231574 seconds time elapsed

pi@raspberrypi:~/QH\_directory/userland/host\_applications/linux/apps/hello\_pi/hello\_fft $ sudo perf\_3.16 stat -d ./hello\_fft.bin 23 1

log2\_N=23 not supported. Try between 8 and 22.

Performance counter stats for './hello\_fft.bin 23 1':

9.527000 task-clock (msec) # 0.629 CPUs utilized

3 context-switches # 0.315 K/sec

0 cpu-migrations # 0.000 K/sec

72 page-faults # 0.008 M/sec

3,298,003 cycles # 0.346 GHz

3,616,153 stalled-cycles-frontend # 109.65% frontend cycles idle

294,918 stalled-cycles-backend # 8.94% backend cycles idle

<not counted> instructions

<not counted> branches

<not counted> branch-misses

<not counted> L1-dcache-loads

<not counted> L1-dcache-load-misses

<not supported> LLC-loads

<not supported> LLC-load-misses

0.015135840 seconds time elapsed

$ sudo perf\_3.16 stat -d ./hello\_fft.bin 8 10 2

rel\_rms\_err = 2.7e-07, usecs = 20, k = 0

rel\_rms\_err = 2.7e-07, usecs = 18, k = 1

Performance counter stats for './hello\_fft.bin 8 10 2':

35.376000 task-clock (msec) # 0.814 CPUs utilized

11 context-switches # 0.311 K/sec

0 cpu-migrations # 0.000 K/sec

97 page-faults # 0.003 M/sec

1,315,035 cycles # 0.037 GHz

4,507,197 stalled-cycles-frontend # 342.74% frontend cycles idle

441,497 stalled-cycles-backend # 33.57% backend cycles idle

4,967,122 instructions # 3.78 insns per cycle

# 0.91 stalled cycles per insn [59.55%]

942,058 branches # 26.630 M/sec [39.51%]

40,161 branch-misses # 4.26% of all branches [16.84%]

<not counted> L1-dcache-loads

<not counted> L1-dcache-load-misses

<not supported> LLC-loads

<not supported> LLC-load-misses

0.043437430 seconds time elapsed

$ sudo perf\_3.16 stat -d ./hello\_fft.bin 8 1 2

rel\_rms\_err = 3.3e-07, usecs = 53, k = 0

rel\_rms\_err = 3.3e-07, usecs = 34, k = 1

Performance counter stats for './hello\_fft.bin 8 1 2':

25.234000 task-clock (msec) # 0.741 CPUs utilized

17 context-switches # 0.674 K/sec

0 cpu-migrations # 0.000 K/sec

91 page-faults # 0.004 M/sec

3,416,788 cycles # 0.135 GHz

5,496,335 stalled-cycles-frontend # 160.86% frontend cycles idle

459,694 stalled-cycles-backend # 13.45% backend cycles idle

4,608,842 instructions # 1.35 insns per cycle

# 1.19 stalled cycles per insn [42.36%]

787,847 branches # 31.222 M/sec [18.20%]

<not counted> branch-misses

<not counted> L1-dcache-loads

<not counted> L1-dcache-load-misses

<not supported> LLC-loads

<not supported> LLC-load-misses

0.034069553 seconds time elapsed

$ sudo perf\_3.16 stat -d ./hello\_fft.bin 8 50 2

rel\_rms\_err = 2.5e-07, usecs = 18, k = 0

rel\_rms\_err = 2.5e-07, usecs = 18, k = 1

Performance counter stats for './hello\_fft.bin 8 50 2':

85.593000 task-clock (msec) # 0.905 CPUs utilized

13 context-switches # 0.152 K/sec

0 cpu-migrations # 0.000 K/sec

141 page-faults # 0.002 M/sec

59,446,895 cycles # 0.695 GHz [33.73%]

18,211,275 stalled-cycles-frontend # 30.63% frontend cycles idle [44.18%]

447,559 stalled-cycles-backend # 0.75% backend cycles idle

9,224,249 instructions # 0.16 insns per cycle

# 1.97 stalled cycles per insn [43.85%]

1,173,759 branches # 13.713 M/sec [33.63%]

72,115 branch-misses # 6.14% of all branches [28.20%]

82,373 L1-dcache-loads # 0.962 M/sec [27.02%]

58,372 L1-dcache-load-misses # 70.86% of all L1-dcache hits [26.00%]

<not supported> LLC-loads

<not supported> LLC-load-misses

0.094569758 seconds time elapsed

## Conclusion:

Rel\_rms\_err, time,

Bigger job size, bigger rel\_rms\_err.

More batches, less rel\_rms\_err.

More batches, less compute time for each task.

## FFT

# CPU part:

Numpy

Measure python 2.7

## Reference: [A guide to analyzing Python performance](https://www.huyng.com/posts/python-performance-analysis)

By: Huy Nguyen

<https://www.huyng.com/posts/python-performance-analysis>   
(Link is no longer useful)  
<http://zqpythonic.qiniucdn.com/data/20170602154836/index.html>

### Coarse grain timing with time

Let’s begin by using a quick and dirty method of timing our code: the good old unix utility time.

$ time python yourprogram.py

real 0m1.028s

user 0m0.001s

sys 0m0.003s

The meaning between the three output measurements are detailed in this [stackoverflow article](http://stackoverflow.com/questions/556405/what-do-real-user-and-sys-mean-in-the-output-of-time1), but in short

* real - refers to the actual elasped time
* user - refers to the amount of cpu time spent outside of kernel
* sys - refers to the amount of cpu time spent inside kernel specific functions

You can get a sense of how many cpu cycles your program used up regardless of other programs running on the system by adding together the sys and user times.

If the sum of sys and user times is much less than real time, then you can guess that most your program’s performance issues are most likely related to IO waits.

### Fine grain timing with a timing context manager

Our next technique involves direct instrumentation of the code to get access to finer grain timing information. Here’s a small snippet I’ve found invaluable for making ad-hoc timing measurements:

timer.py

import time

class Timer(object):

def \_\_init\_\_(self, verbose=False):

self.verbose = verbose

def \_\_enter\_\_(self):

self.start = time.time()

return self

def \_\_exit\_\_(self, \*args):

self.end = time.time()

self.secs = self.end - self.start

self.msecs = self.secs \* 1000 # millisecs

if self.verbose:

print 'elapsed time: %f ms' % self.msecs

In order to use it, wrap blocks of code that you want to time with Python’s withkeyword and this Timer context manager. It will take care of starting the timer when your code block begins execution and stopping the timer when your code block ends.

Here’s an example use of the snippet:

from timer import Timer

from redis import Redis

rdb = Redis()

with Timer() as t:

rdb.lpush("foo", "bar")

print "=> elasped lpush: %s s" % t.secs

with Timer() as t:

rdb.lpop("foo")

print "=> elasped lpop: %s s" % t.secs

I’ll often log the outputs of these timers to a file in order to see how my program’s performance evolves over time.

## Perf measure results:

e.g. perf measure the test demo:

$ sudo perf\_3.16 stat -d python2.7 test1.py

hello

a sum of 1 to 9 is: 45

b list of array is: [0, 1, 2, 3, 4, 5, 6, 7, 8, 9]

0.00572299957275

Performance counter stats for 'python2.7 test1.py':

220.890000 task-clock (msec) # 0.946 CPUs utilized

13 context-switches # 0.059 K/sec

0 cpu-migrations # 0.000 K/sec

527 page-faults # 0.002 M/sec

153,804,192 cycles # 0.696 GHz [36.35%]

59,483,571 stalled-cycles-frontend # 38.67% frontend cycles idle [34.87%]

1,980,583 stalled-cycles-backend # 1.29% backend cycles idle [44.04%]

25,577,199 instructions # 0.17 insns per cycle

# 2.33 stalled cycles per insn [31.79%]

4,450,862 branches # 20.150 M/sec [28.31%]

481,440 branch-misses # 10.82% of all branches [26.68%]

1,475,384 L1-dcache-loads # 6.679 M/sec [27.85%]

263,682 L1-dcache-load-misses # 17.87% of all L1-dcache hits [26.46%]

<not supported> LLC-loads

<not supported> LLC-load-misses

0.233527929 seconds time elapsed

TEST script file scipy\_fftpack.py on the RPi

pi@raspberrypi:~/QH\_directory/Parallel-programming/PI/scipy $ sudo perf\_3.16 stat -d ./scipy\_fftpack.py 1048576

This is the name of the script: ./scipy\_fftpack.py

The jobsize for the FFT is: 1048576

double float array 'a' datatype: float64

single float array 'b' datatype: float32

output of FFT single float complex array 'c' datatype: complex64

Time elapsed (Without user input): 2.16360902786

Performance counter stats for './scipy\_fftpack.py 1048576':

3849.696000 task-clock (msec) # 0.993 CPUs utilized

79 context-switches # 0.021 K/sec

0 cpu-migrations # 0.000 K/sec

12,678 page-faults # 0.003 M/sec

2,668,172,027 cycles # 0.693 GHz [37.63%]

425,384,314 stalled-cycles-frontend # 15.94% frontend cycles idle [37.86%]

29,981,361 stalled-cycles-backend # 1.12% backend cycles idle [38.04%]

465,243,453 instructions # 0.17 insns per cycle

# 0.91 stalled cycles per insn [25.02%]

57,365,641 branches # 14.901 M/sec [25.21%]

4,233,199 branch-misses # 7.38% of all branches [25.17%]

20,450,279 L1-dcache-loads # 5.312 M/sec [25.03%]

5,221,311 L1-dcache-load-misses # 25.53% of all L1-dcache hits [24.87%]

<not supported> LLC-loads

<not supported> LLC-load-misses

3.875131052 seconds time elapsed

pi@raspberrypi:~/QH\_directory/Parallel-programming/PI/scipy $ sudo perf\_3.16 stat -d ./scipy\_fftpack.py 2097152

This is the name of the script: ./scipy\_fftpack.py

The jobsize for the FFT is: 2097152

double float array 'a' datatype: float64

single float array 'b' datatype: float32

output of FFT single float complex array 'c' datatype: complex64

Time elapsed (Without user input): 5.01232290268

Performance counter stats for './scipy\_fftpack.py 2097152':

6137.023000 task-clock (msec) # 0.814 CPUs utilized

245 context-switches # 0.040 K/sec

0 cpu-migrations # 0.000 K/sec

22,915 page-faults # 0.004 M/sec

4,272,503,310 cycles # 0.696 GHz [37.76%]

504,622,330 stalled-cycles-frontend # 11.81% frontend cycles idle [37.73%]

45,855,098 stalled-cycles-backend # 1.07% backend cycles idle [37.58%]

722,607,232 instructions # 0.17 insns per cycle

# 0.70 stalled cycles per insn [24.88%]

80,908,590 branches # 13.184 M/sec [25.11%]

5,720,158 branch-misses # 7.07% of all branches [25.06%]

37,530,056 L1-dcache-loads # 6.115 M/sec [25.29%]

8,733,112 L1-dcache-load-misses # 23.27% of all L1-dcache hits [24.94%]

<not supported> LLC-loads

<not supported> LLC-load-misses

7.538532244 seconds time elapsed

pi@raspberrypi:~/QH\_directory/Parallel-programming/PI/scipy $ sudo perf\_3.16 stat -d ./scipy\_fftpack.py 4194304

This is the name of the script: ./scipy\_fftpack.py

The jobsize for the FFT is: 4194304

double float array 'a' datatype: float64

single float array 'b' datatype: float32

output of FFT single float complex array 'c' datatype: complex64

Time elapsed (Without user input): 12.4275429249

Performance counter stats for './scipy\_fftpack.py 4194304':

11430.988000 task-clock (msec) # 0.791 CPUs utilized

468 context-switches # 0.041 K/sec

0 cpu-migrations # 0.000 K/sec

43,398 page-faults # 0.004 M/sec

7,959,804,965 cycles # 0.696 GHz [37.66%]

643,866,991 stalled-cycles-frontend # 8.09% frontend cycles idle [37.80%]

81,870,766 stalled-cycles-backend # 1.03% backend cycles idle [37.44%]

1,247,220,994 instructions # 0.16 insns per cycle

# 0.52 stalled cycles per insn [24.83%]

125,266,636 branches # 10.959 M/sec [25.17%]

7,200,627 branch-misses # 5.75% of all branches [25.23%]

63,336,063 L1-dcache-loads # 5.541 M/sec [24.94%]

15,605,235 L1-dcache-load-misses # 24.64% of all L1-dcache hits [24.94%]

<not supported> LLC-loads

<not supported> LLC-load-misses

14.448295478 seconds time elapsed

pi@raspberrypi:~/QH\_directory/Parallel-programming/PI/scipy $ sudo perf\_3.16 stat -d ./scipy\_fftpack.py 8388608

This is the name of the script: ./scipy\_fftpack.py

The jobsize for the FFT is: 8388608

double float array 'a' datatype: float64

single float array 'b' datatype: float32

output of FFT single float complex array 'c' datatype: complex64

Time elapsed (Without user input): 30.5332231522

Performance counter stats for './scipy\_fftpack.py 8388608':

22532.759000 task-clock (msec) # 0.670 CPUs utilized

3,929 context-switches # 0.174 K/sec

0 cpu-migrations # 0.000 K/sec

107,385 page-faults # 0.005 M/sec

15,661,751,178 cycles # 0.695 GHz [37.10%]

1,061,623,576 stalled-cycles-frontend # 6.78% frontend cycles idle [37.54%]

158,905,796 stalled-cycles-backend # 1.01% backend cycles idle [37.75%]

2,265,053,870 instructions # 0.14 insns per cycle

# 0.47 stalled cycles per insn [24.95%]

202,248,048 branches # 8.976 M/sec [25.10%]

11,359,288 branch-misses # 5.62% of all branches [25.37%]

162,457,493 L1-dcache-loads # 7.210 M/sec [24.86%]

33,874,080 L1-dcache-load-misses # 20.85% of all L1-dcache hits [24.60%]

<not supported> LLC-loads

<not supported> LLC-load-misses

33.647943532 seconds time elapsed

pi@raspberrypi:~/QH\_directory/Parallel-programming/PI/scipy $ sudo perf\_3.16 stat -d ./scipy\_fftpack.py 16777216

This is the name of the script: ./scipy\_fftpack.py

The jobsize for the FFT is: 16777216

Traceback (most recent call last):

File "./scipy\_fftpack.py", line 22, in <module>

a = np.linspace(1., 4., jobsize)

File "/usr/lib/python2.7/dist-packages/numpy/core/function\_base.py", line 88, in linspace

y = \_nx.arange(0, num) \* step + start

MemoryError

Performance counter stats for './scipy\_fftpack.py 16777216':

4865.617000 task-clock (msec) # 0.432 CPUs utilized

1,936 context-switches # 0.398 K/sec

0 cpu-migrations # 0.000 K/sec

55,164 page-faults # 0.011 M/sec

3,372,902,713 cycles # 0.693 GHz [37.12%]

691,182,390 stalled-cycles-frontend # 20.49% frontend cycles idle [38.91%]

88,316,197 stalled-cycles-backend # 2.62% backend cycles idle [38.42%]

797,049,833 instructions # 0.24 insns per cycle

# 0.87 stalled cycles per insn [24.30%]

115,369,328 branches # 23.711 M/sec [25.73%]

7,260,701 branch-misses # 6.29% of all branches [25.33%]

92,582,694 L1-dcache-loads # 19.028 M/sec [23.65%]

18,733,338 L1-dcache-load-misses # 20.23% of all L1-dcache hits [24.54%]

<not supported> LLC-loads

<not supported> LLC-load-misses

11.257579058 seconds time elapsed

Modified script for less print out message

pi@raspberrypi:~/QH\_directory/Parallel-programming/PI/scipy $ sudo perf\_3.16 stat -d ./scipy\_fftpack.py 256

The jobsize for the scipy-FFT is: 256

Time elapsed: 0.00441002845764

Performance counter stats for './scipy\_fftpack.py 256':

1694.041000 task-clock (msec) # 0.887 CPUs utilized

47 context-switches # 0.028 K/sec

0 cpu-migrations # 0.000 K/sec

2,193 page-faults # 0.001 M/sec

1,178,936,251 cycles # 0.696 GHz [36.41%]

381,368,964 stalled-cycles-frontend # 32.35% frontend cycles idle [37.89%]

11,542,098 stalled-cycles-backend # 0.98% backend cycles idle [37.50%]

218,446,742 instructions # 0.19 insns per cycle

# 1.75 stalled cycles per insn [24.99%]

42,590,805 branches # 25.142 M/sec [25.62%]

4,178,138 branch-misses # 9.81% of all branches [25.95%]

13,563,842 L1-dcache-loads # 8.007 M/sec [25.35%]

1,887,498 L1-dcache-load-misses # 13.92% of all L1-dcache hits [24.72%]

<not supported> LLC-loads

<not supported> LLC-load-misses

1.908827627 seconds time elapsed

pi@raspberrypi:~/QH\_directory/Parallel-programming/PI/scipy $ sudo perf\_3.16 stat -d ./scipy\_fftpack.py 512

The jobsize for the scipy-FFT is: 512

Time elapsed: 0.00367498397827

Performance counter stats for './scipy\_fftpack.py 512':

1687.118000 task-clock (msec) # 0.994 CPUs utilized

35 context-switches # 0.021 K/sec

0 cpu-migrations # 0.000 K/sec

2,194 page-faults # 0.001 M/sec

1,174,492,494 cycles # 0.696 GHz [37.96%]

372,397,564 stalled-cycles-frontend # 31.71% frontend cycles idle [37.48%]

11,262,778 stalled-cycles-backend # 0.96% backend cycles idle [37.50%]

203,400,639 instructions # 0.17 insns per cycle

# 1.83 stalled cycles per insn [25.58%]

40,761,200 branches # 24.160 M/sec [25.40%]

3,985,902 branch-misses # 9.78% of all branches [25.25%]

9,709,970 L1-dcache-loads # 5.755 M/sec [25.55%]

1,734,205 L1-dcache-load-misses # 17.86% of all L1-dcache hits [25.37%]

<not supported> LLC-loads

<not supported> LLC-load-misses

1.697836991 seconds time elapsed

pi@raspberrypi:~/QH\_directory/Parallel-programming/PI/scipy $ sudo perf\_3.16 stat -d ./scipy\_fftpack.py 1024

The jobsize for the scipy-FFT is: 1024

Time elapsed: 0.00434184074402

Performance counter stats for './scipy\_fftpack.py 1024':

1697.404000 task-clock (msec) # 0.835 CPUs utilized

71 context-switches # 0.042 K/sec

0 cpu-migrations # 0.000 K/sec

2,200 page-faults # 0.001 M/sec

1,175,073,087 cycles # 0.692 GHz [38.34%]

377,560,617 stalled-cycles-frontend # 32.13% frontend cycles idle [38.16%]

11,579,072 stalled-cycles-backend # 0.99% backend cycles idle [37.62%]

207,091,603 instructions # 0.18 insns per cycle

# 1.82 stalled cycles per insn [25.93%]

40,474,843 branches # 23.845 M/sec [25.86%]

3,829,836 branch-misses # 9.46% of all branches [25.09%]

9,051,848 L1-dcache-loads # 5.333 M/sec [24.66%]

1,637,583 L1-dcache-load-misses # 18.09% of all L1-dcache hits [25.56%]

<not supported> LLC-loads

<not supported> LLC-load-misses

2.033295239 seconds time elapsed

pi@raspberrypi:~/QH\_directory/Parallel-programming/PI/scipy $ sudo perf\_3.16 stat -d ./scipy\_fftpack.py 2048

The jobsize for the scipy-FFT is: 2048

Time elapsed: 0.00499701499939

Performance counter stats for './scipy\_fftpack.py 2048':

1677.842000 task-clock (msec) # 0.993 CPUs utilized

34 context-switches # 0.020 K/sec

0 cpu-migrations # 0.000 K/sec

2,211 page-faults # 0.001 M/sec

1,168,330,752 cycles # 0.696 GHz [37.18%]

396,781,019 stalled-cycles-frontend # 33.96% frontend cycles idle [37.17%]

12,414,814 stalled-cycles-backend # 1.06% backend cycles idle [37.94%]

232,662,742 instructions # 0.20 insns per cycle

# 1.71 stalled cycles per insn [25.54%]

45,368,099 branches # 27.040 M/sec [25.36%]

4,292,784 branch-misses # 9.46% of all branches [25.58%]

10,044,964 L1-dcache-loads # 5.987 M/sec [25.44%]

1,648,055 L1-dcache-load-misses # 16.41% of all L1-dcache hits [25.26%]

<not supported> LLC-loads

<not supported> LLC-load-misses

1.689309091 seconds time elapsed

pi@raspberrypi:~/QH\_directory/Parallel-programming/PI/scipy $ sudo perf\_3.16 stat -d ./scipy\_fftpack.py 4096

The jobsize for the scipy-FFT is: 4096

Time elapsed: 0.00750398635864

Performance counter stats for './scipy\_fftpack.py 4096':

1704.142000 task-clock (msec) # 0.889 CPUs utilized

55 context-switches # 0.032 K/sec

0 cpu-migrations # 0.000 K/sec

2,228 page-faults # 0.001 M/sec

1,185,695,922 cycles # 0.696 GHz [37.50%]

402,048,211 stalled-cycles-frontend # 33.91% frontend cycles idle [37.52%]

13,035,761 stalled-cycles-backend # 1.10% backend cycles idle [37.82%]

245,609,269 instructions # 0.21 insns per cycle

# 1.64 stalled cycles per insn [26.14%]

44,776,635 branches # 26.275 M/sec [25.15%]

4,291,688 branch-misses # 9.58% of all branches [24.63%]

7,512,214 L1-dcache-loads # 4.408 M/sec [25.04%]

1,650,700 L1-dcache-load-misses # 21.97% of all L1-dcache hits [25.28%]

<not supported> LLC-loads

<not supported> LLC-load-misses

1.917500538 seconds time elapsed

pi@raspberrypi:~/QH\_directory/Parallel-programming/PI/scipy $ sudo perf\_3.16 stat -d ./scipy\_fftpack.py 8192

\The jobsize for the scipy-FFT is: 8192

Time elapsed: 0.0128231048584

Performance counter stats for './scipy\_fftpack.py 8192':

1689.532000 task-clock (msec) # 0.994 CPUs utilized

29 context-switches # 0.017 K/sec

0 cpu-migrations # 0.000 K/sec

2,255 page-faults # 0.001 M/sec

1,166,694,698 cycles # 0.691 GHz [37.49%]

364,940,862 stalled-cycles-frontend # 31.28% frontend cycles idle [37.99%]

10,782,326 stalled-cycles-backend # 0.92% backend cycles idle [38.18%]

211,833,870 instructions # 0.18 insns per cycle

# 1.72 stalled cycles per insn [25.02%]

40,022,050 branches # 23.688 M/sec [25.56%]

3,907,572 branch-misses # 9.76% of all branches [25.44%]

9,267,612 L1-dcache-loads # 5.485 M/sec [25.23%]

1,983,520 L1-dcache-load-misses # 21.40% of all L1-dcache hits [24.99%]

<not supported> LLC-loads

<not supported> LLC-load-misses

1.698884987 seconds time elapsed

pi@raspberrypi:~/QH\_directory/Parallel-programming/PI/scipy $ sudo perf\_3.16 stat -d ./scipy\_fftpack.py 16384

The jobsize for the scipy-FFT is: 16384

Time elapsed: 0.0225789546967

Performance counter stats for './scipy\_fftpack.py 16384':

1716.049000 task-clock (msec) # 0.994 CPUs utilized

34 context-switches # 0.020 K/sec

0 cpu-migrations # 0.000 K/sec

2,309 page-faults # 0.001 M/sec

1,169,098,238 cycles # 0.681 GHz [37.68%]

380,293,245 stalled-cycles-frontend # 32.53% frontend cycles idle [37.96%]

10,803,502 stalled-cycles-backend # 0.92% backend cycles idle [38.54%]

214,737,979 instructions # 0.18 insns per cycle

# 1.77 stalled cycles per insn [25.70%]

40,206,566 branches # 23.430 M/sec [25.36%]

3,799,170 branch-misses # 9.45% of all branches [24.78%]

10,070,756 L1-dcache-loads # 5.869 M/sec [25.26%]

1,719,486 L1-dcache-load-misses # 17.07% of all L1-dcache hits [24.91%]

<not supported> LLC-loads

<not supported> LLC-load-misses

1.726583678 seconds time elapsed

pi@raspberrypi:~/QH\_directory/Parallel-programming/PI/scipy $ sudo perf\_3.16 stat -d ./scipy\_fftpack.py 32768

The jobsize for the scipy-FFT is: 32768

Time elapsed: 0.0483119487762

Performance counter stats for './scipy\_fftpack.py 32768':

1801.709000 task-clock (msec) # 0.995 CPUs utilized

31 context-switches # 0.017 K/sec

0 cpu-migrations # 0.000 K/sec

2,488 page-faults # 0.001 M/sec

1,224,249,914 cycles # 0.679 GHz [37.70%]

394,532,201 stalled-cycles-frontend # 32.23% frontend cycles idle [38.07%]

14,138,171 stalled-cycles-backend # 1.15% backend cycles idle [38.34%]

237,681,900 instructions # 0.19 insns per cycle

# 1.66 stalled cycles per insn [25.60%]

42,605,437 branches # 23.647 M/sec [25.55%]

4,103,825 branch-misses # 9.63% of all branches [25.04%]

9,771,858 L1-dcache-loads # 5.424 M/sec [24.47%]

1,678,104 L1-dcache-load-misses # 17.17% of all L1-dcache hits [25.13%]

<not supported> LLC-loads

<not supported> LLC-load-misses

1.810596738 seconds time elapsed

pi@raspberrypi:~/QH\_directory/Parallel-programming/PI/scipy $ sudo perf\_3.16 stat -d ./scipy\_fftpack.py 65536

The jobsize for the scipy-FFT is: 65536

Time elapsed: 0.103672981262

Performance counter stats for './scipy\_fftpack.py 65536':

1784.527000 task-clock (msec) # 0.992 CPUs utilized

39 context-switches # 0.022 K/sec

0 cpu-migrations # 0.000 K/sec

2,844 page-faults # 0.002 M/sec

1,225,998,688 cycles # 0.687 GHz [37.88%]

370,364,139 stalled-cycles-frontend # 30.21% frontend cycles idle [37.79%]

11,783,863 stalled-cycles-backend # 0.96% backend cycles idle [38.04%]

232,059,873 instructions # 0.19 insns per cycle

# 1.60 stalled cycles per insn [25.27%]

41,728,222 branches # 23.383 M/sec [24.73%]

3,747,428 branch-misses # 8.98% of all branches [25.20%]

11,297,730 L1-dcache-loads # 6.331 M/sec [25.61%]

2,000,838 L1-dcache-load-misses # 17.71% of all L1-dcache hits [25.56%]

<not supported> LLC-loads

<not supported> LLC-load-misses

1.799354865 seconds time elapsed

pi@raspberrypi:~/QH\_directory/Parallel-programming/PI/scipy $ sudo perf\_3.16 stat -d ./scipy\_fftpack.py 131072

The jobsize for the scipy-FFT is: 131072

Time elapsed: 0.225043058395

Performance counter stats for './scipy\_fftpack.py 131072':

1933.726000 task-clock (msec) # 0.993 CPUs utilized

39 context-switches # 0.020 K/sec

0 cpu-migrations # 0.000 K/sec

3,499 page-faults # 0.002 M/sec

1,329,364,095 cycles # 0.687 GHz [37.50%]

388,247,741 stalled-cycles-frontend # 29.21% frontend cycles idle [37.75%]

13,069,847 stalled-cycles-backend # 0.98% backend cycles idle [38.01%]

255,323,503 instructions # 0.19 insns per cycle

# 1.52 stalled cycles per insn [25.38%]

38,729,607 branches # 20.028 M/sec [24.90%]

3,700,986 branch-misses # 9.56% of all branches [25.46%]

10,533,044 L1-dcache-loads # 5.447 M/sec [25.35%]

2,242,423 L1-dcache-load-misses # 21.29% of all L1-dcache hits [25.23%]

<not supported> LLC-loads

<not supported> LLC-load-misses

1.947514208 seconds time elapsed

pi@raspberrypi:~/QH\_directory/Parallel-programming/PI/scipy $ sudo perf\_3.16 stat -d ./scipy\_fftpack.py 262144

The jobsize for the scipy-FFT is: 262144

Time elapsed: 0.490144014359

Performance counter stats for './scipy\_fftpack.py 262144':

2180.217000 task-clock (msec) # 0.993 CPUs utilized

43 context-switches # 0.020 K/sec

0 cpu-migrations # 0.000 K/sec

4,780 page-faults # 0.002 M/sec

1,502,323,830 cycles # 0.689 GHz [37.25%]

384,931,491 stalled-cycles-frontend # 25.62% frontend cycles idle [37.62%]

15,525,945 stalled-cycles-backend # 1.03% backend cycles idle [38.03%]

257,320,961 instructions # 0.17 insns per cycle

# 1.50 stalled cycles per insn [25.22%]

41,457,881 branches # 19.015 M/sec [24.82%]

3,671,001 branch-misses # 8.85% of all branches [25.67%]

12,608,993 L1-dcache-loads # 5.783 M/sec [25.50%]

2,536,265 L1-dcache-load-misses # 20.11% of all L1-dcache hits [24.83%]

<not supported> LLC-loads

<not supported> LLC-load-misses

2.196506425 seconds time elapsed

pi@raspberrypi:~/QH\_directory/Parallel-programming/PI/scipy $ sudo perf\_3.16 stat -d ./scipy\_fftpack.py 524288

The jobsize for the scipy-FFT is: 524288

Time elapsed: 0.999449968338

Performance counter stats for './scipy\_fftpack.py 524288':

2679.947000 task-clock (msec) # 0.995 CPUs utilized

45 context-switches # 0.017 K/sec

0 cpu-migrations # 0.000 K/sec

7,336 page-faults # 0.003 M/sec

1,836,739,254 cycles # 0.685 GHz [37.75%]

417,664,859 stalled-cycles-frontend # 22.74% frontend cycles idle [37.94%]

21,653,443 stalled-cycles-backend # 1.18% backend cycles idle [38.12%]

353,213,784 instructions # 0.19 insns per cycle

# 1.18 stalled cycles per insn [25.40%]

55,436,854 branches # 20.686 M/sec [25.31%]

4,820,102 branch-misses # 8.69% of all branches [24.96%]

17,734,920 L1-dcache-loads # 6.618 M/sec [24.60%]

3,272,221 L1-dcache-load-misses # 18.45% of all L1-dcache hits [25.07%]

<not supported> LLC-loads

<not supported> LLC-load-misses

2.692897874 seconds time elapsed

pi@raspberrypi:~/QH\_directory/Parallel-programming/PI/scipy $ sudo perf\_3.16 stat -d ./scipy\_fftpack.py 1048576

The jobsize for the scipy-FFT is: 1048576

Time elapsed: 2.44907593727

Performance counter stats for './scipy\_fftpack.py 1048576':

3896.361000 task-clock (msec) # 0.840 CPUs utilized

142 context-switches # 0.036 K/sec

0 cpu-migrations # 0.000 K/sec

12,460 page-faults # 0.003 M/sec

2,711,643,789 cycles # 0.696 GHz [37.23%]

449,084,232 stalled-cycles-frontend # 16.56% frontend cycles idle [37.58%]

30,364,335 stalled-cycles-backend # 1.12% backend cycles idle [37.91%]

473,494,905 instructions # 0.17 insns per cycle

# 0.95 stalled cycles per insn [25.39%]

60,128,872 branches # 15.432 M/sec [25.18%]

4,856,233 branch-misses # 8.08% of all branches [24.78%]

24,900,430 L1-dcache-loads # 6.391 M/sec [24.81%]

5,112,107 L1-dcache-load-misses # 20.53% of all L1-dcache hits [25.28%]

<not supported> LLC-loads

<not supported> LLC-load-misses

4.636521136 seconds time elapsed

pi@raspberrypi:~/QH\_directory/Parallel-programming/PI/scipy $ sudo perf\_3.16 stat -d ./scipy\_fftpack.py 2097152

The jobsize for the scipy-FFT is: 2097152

Time elapsed: 5.05225992203

Performance counter stats for './scipy\_fftpack.py 2097152':

6225.630000 task-clock (msec) # 0.919 CPUs utilized

166 context-switches # 0.027 K/sec

0 cpu-migrations # 0.000 K/sec

22,700 page-faults # 0.004 M/sec

4,334,856,577 cycles # 0.696 GHz [37.22%]

498,388,066 stalled-cycles-frontend # 11.50% frontend cycles idle [38.03%]

45,047,106 stalled-cycles-backend # 1.04% backend cycles idle [37.96%]

693,384,108 instructions # 0.16 insns per cycle

# 0.72 stalled cycles per insn [25.20%]

79,158,623 branches # 12.715 M/sec [24.92%]

5,440,378 branch-misses # 6.87% of all branches [24.91%]

43,420,033 L1-dcache-loads # 6.974 M/sec [24.79%]

9,906,845 L1-dcache-load-misses # 22.82% of all L1-dcache hits [24.74%]

<not supported> LLC-loads

<not supported> LLC-load-misses

6.774342229 seconds time elapsed

pi@raspberrypi:~/QH\_directory/Parallel-programming/PI/scipy $ sudo perf\_3.16 stat -d ./scipy\_fftpack.py 4194304

The jobsize for the scipy-FFT is: 4194304

Time elapsed: 10.2858328819

Performance counter stats for './scipy\_fftpack.py 4194304':

11499.008000 task-clock (msec) # 0.951 CPUs utilized

294 context-switches # 0.026 K/sec

0 cpu-migrations # 0.000 K/sec

43,179 page-faults # 0.004 M/sec

7,991,923,690 cycles # 0.695 GHz [37.69%]

658,981,249 stalled-cycles-frontend # 8.25% frontend cycles idle [37.64%]

80,212,208 stalled-cycles-backend # 1.00% backend cycles idle [37.48%]

1,231,541,106 instructions # 0.15 insns per cycle

# 0.54 stalled cycles per insn [24.95%]

117,857,245 branches # 10.249 M/sec [24.76%]

7,131,390 branch-misses # 6.05% of all branches [25.05%]

68,264,384 L1-dcache-loads # 5.937 M/sec [25.16%]

16,363,636 L1-dcache-load-misses # 23.97% of all L1-dcache hits [25.28%]

<not supported> LLC-loads

<not supported> LLC-load-misses

12.086282828 seconds time elapsed

pi@raspberrypi:~/QH\_directory/Parallel-programming/PI/scipy $ sudo perf\_3.16 stat -d ./scipy\_fftpack.py 8388608

The jobsize for the scipy-FFT is: 8388608

Time elapsed: 25.9255290031

Performance counter stats for './scipy\_fftpack.py 8388608':

22221.711000 task-clock (msec) # 0.766 CPUs utilized

3,542 context-switches # 0.159 K/sec

0 cpu-migrations # 0.000 K/sec

102,108 page-faults # 0.005 M/sec

15,433,014,722 cycles # 0.695 GHz [37.41%]

1,172,943,066 stalled-cycles-frontend # 7.60% frontend cycles idle [37.66%]

157,561,860 stalled-cycles-backend # 1.02% backend cycles idle [37.88%]

2,303,830,512 instructions # 0.15 insns per cycle

# 0.51 stalled cycles per insn [25.08%]

204,140,715 branches # 9.187 M/sec [24.81%]

11,259,901 branch-misses # 5.52% of all branches [24.87%]

154,236,787 L1-dcache-loads # 6.941 M/sec [24.90%]

32,169,107 L1-dcache-load-misses # 20.86% of all L1-dcache hits [24.89%]

<not supported> LLC-loads

<not supported> LLC-load-misses

29.012408584 seconds time elapsed

Also test on the lab desktop MS-7320 machine:

qihao@qihao-MS-7320:~/QH\_directory/Parallel-programming/PI/scipy$ sudo perf stat -d ./scipy\_fftpack.py 1048576

[sudo] password for qihao:

This is the name of the script: ./scipy\_fftpack.py

The jobsize for the FFT is: 1048576

double float array 'a' datatype: float64

single float array 'b' datatype: float32

output of FFT single float complex array 'c' datatype: complex64

Time elapsed (Without user input): 0.107489109039

Performance counter stats for './scipy\_fftpack.py 1048576':

539.494506 task-clock (msec) # 2.622 CPUs utilized

33 context-switches # 0.061 K/sec

0 cpu-migrations # 0.000 K/sec

10,718 page-faults # 0.020 M/sec

1,267,711,227 cycles # 2.350 GHz (27.49%)

1,044,718,678 instructions # 0.82 insn per cycle (39.23%)

181,226,423 branches # 335.919 M/sec (37.41%)

3,111,866 branch-misses # 1.72% of all branches (35.13%)

314,736,823 L1-dcache-loads # 583.392 M/sec (25.06%)

9,866,794 L1-dcache-load-misses # 3.13% of all L1-dcache hits (26.48%)

4,025,299 LLC-loads # 7.461 M/sec (28.61%)

200,776 LLC-load-misses # 4.99% of all LL-cache hits (27.76%)

0.205796079 seconds time elapsed

qihao@qihao-MS-7320:~/QH\_directory/Parallel-programming/PI/scipy$ sudo perf stat -d ./scipy\_fftpack.py 2097152

[sudo] password for qihao:

This is the name of the script: ./scipy\_fftpack.py

The jobsize for the FFT is: 2097152

double float array 'a' datatype: float64

single float array 'b' datatype: float32

output of FFT single float complex array 'c' datatype: complex64

Time elapsed (Without user input): 0.232925891876

Performance counter stats for './scipy\_fftpack.py 2097152':

666.672749 task-clock (msec) # 2.001 CPUs utilized

39 context-switches # 0.058 K/sec

0 cpu-migrations # 0.000 K/sec

17,878 page-faults # 0.027 M/sec

1,573,377,223 cycles # 2.360 GHz (26.39%)

1,285,034,397 instructions # 0.82 insn per cycle (38.30%)

196,959,357 branches # 295.436 M/sec (37.44%)

2,827,981 branch-misses # 1.44% of all branches (36.89%)

368,622,142 L1-dcache-loads # 552.928 M/sec (24.80%)

19,379,087 L1-dcache-load-misses # 5.26% of all L1-dcache hits (26.03%)

7,869,690 LLC-loads # 11.804 M/sec (27.80%)

497,838 LLC-load-misses # 6.33% of all LL-cache hits (27.07%)

0.333103302 seconds time elapsed

qihao@qihao-MS-7320:~/QH\_directory/Parallel-programming/PI/scipy$ sudo perf stat -d ./scipy\_fftpack.py 4194304

This is the name of the script: ./scipy\_fftpack.py

The jobsize for the FFT is: 4194304

double float array 'a' datatype: float64

single float array 'b' datatype: float32

output of FFT single float complex array 'c' datatype: complex64

Time elapsed (Without user input): 0.49596786499

Performance counter stats for './scipy\_fftpack.py 4194304':

924.591713 task-clock (msec) # 1.532 CPUs utilized

43 context-switches # 0.047 K/sec

4 cpu-migrations # 0.004 K/sec

32,214 page-faults # 0.035 M/sec

2,165,588,361 cycles # 2.342 GHz (25.05%)

1,525,607,316 instructions # 0.70 insn per cycle (38.93%)

201,220,785 branches # 217.632 M/sec (38.39%)

2,749,902 branch-misses # 1.37% of all branches (37.83%)

485,940,520 L1-dcache-loads # 525.573 M/sec (26.00%)

26,339,892 L1-dcache-load-misses # 5.42% of all L1-dcache hits (26.45%)

13,511,637 LLC-loads # 14.614 M/sec (26.46%)

669,069 LLC-load-misses # 4.95% of all LL-cache hits (25.30%)

0.603490330 seconds time elapsed

qihao@qihao-MS-7320:~/QH\_directory/Parallel-programming/PI/scipy$ sudo perf stat -d ./scipy\_fftpack.py 8388608

This is the name of the script: ./scipy\_fftpack.py

The jobsize for the FFT is: 8388608

double float array 'a' datatype: float64

single float array 'b' datatype: float32

output of FFT single float complex array 'c' datatype: complex64

Time elapsed (Without user input): 1.05380797386

Performance counter stats for './scipy\_fftpack.py 8388608':

1498.391588 task-clock (msec) # 1.288 CPUs utilized

47 context-switches # 0.031 K/sec

1 cpu-migrations # 0.001 K/sec

60,890 page-faults # 0.041 M/sec

3,570,224,470 cycles # 2.383 GHz (25.92%)

2,619,521,662 instructions # 0.73 insn per cycle (38.15%)

270,457,050 branches # 180.498 M/sec (37.46%)

2,929,406 branch-misses # 1.08% of all branches (36.50%)

660,090,865 L1-dcache-loads # 440.533 M/sec (24.97%)

50,783,363 L1-dcache-load-misses # 7.69% of all L1-dcache hits (25.85%)

26,119,184 LLC-loads # 17.431 M/sec (26.27%)

1,833,397 LLC-load-misses # 7.02% of all LL-cache hits (25.99%)

1.163739455 seconds time elapsed

qihao@qihao-MS-7320:~/QH\_directory/Parallel-programming/PI/scipy$ sudo perf stat -d ./scipy\_fftpack.py 16777216

This is the name of the script: ./scipy\_fftpack.py

The jobsize for the FFT is: 16777216

double float array 'a' datatype: float64

single float array 'b' datatype: float32

output of FFT single float complex array 'c' datatype: complex64

Time elapsed (Without user input): 2.11045312881

Performance counter stats for './scipy\_fftpack.py 16777216':

2568.300348 task-clock (msec) # 1.150 CPUs utilized

42 context-switches # 0.016 K/sec

3 cpu-migrations # 0.001 K/sec

118,236 page-faults # 0.046 M/sec

6,143,194,965 cycles # 2.392 GHz (25.34%)

4,316,160,476 instructions # 0.70 insn per cycle (37.88%)

363,200,054 branches # 141.417 M/sec (37.51%)

2,788,883 branch-misses # 0.77% of all branches (37.05%)

1,109,261,526 L1-dcache-loads # 431.905 M/sec (25.18%)

109,433,866 L1-dcache-load-misses # 9.87% of all L1-dcache hits (25.48%)

56,473,676 LLC-loads # 21.989 M/sec (25.62%)

3,590,643 LLC-load-misses # 6.36% of all LL-cache hits (25.36%)

2.233689157 seconds time elapsed