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Bloomberg School of Public Health

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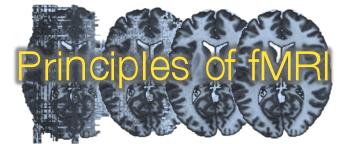
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Neuroscience and the  
Institute for Cognitive Science  
University of Colorado, Boulder

# Basis Sets II



@fMRIstats

# Temporal Basis Functions

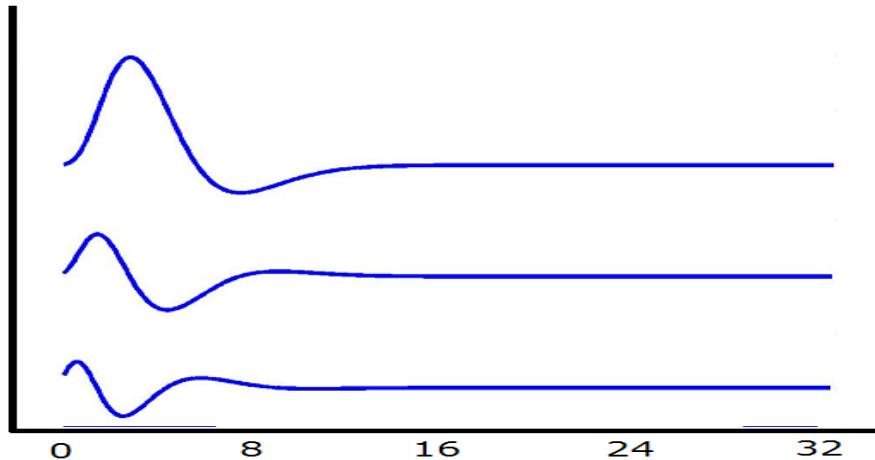


- Recall that when performing the GLM we often use **temporal basis functions** to allow for different types of HRFs in different brain regions.
- These consist of a linear combination of pre-specified temporal functions:
  - The stimulus function is convolved with each of the basis functions to give a set of predictors.
  - The parameter estimates are weights on the basis functions, so that the weighted average provides a model for the hemodynamic response.
  - Usually fit for each trial type in each voxel for each subject.



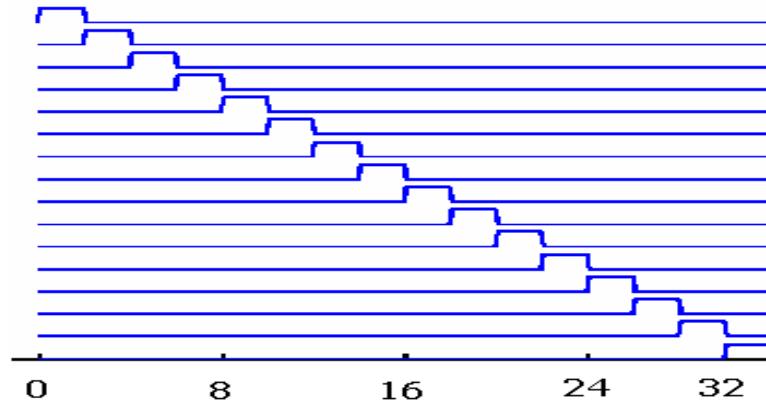
# Basis Sets

## Canonical HRF + Derivatives



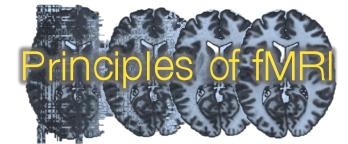
Including the derivatives allows for a shift in delay and dispersion.

## Finite Impulse Response

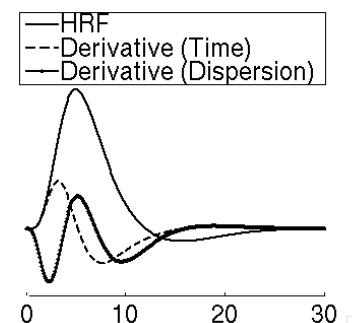
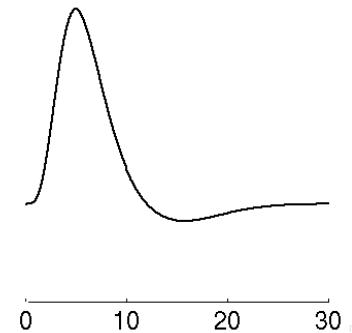


Estimates an HRF of arbitrary shape for each event type in each voxel of the brain

# Basis Sets

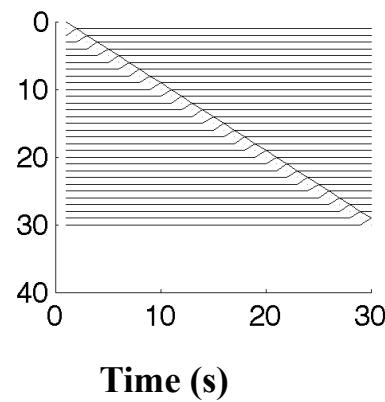


Single HRF



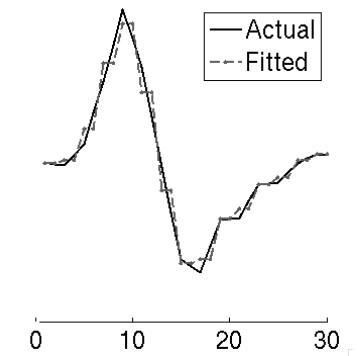
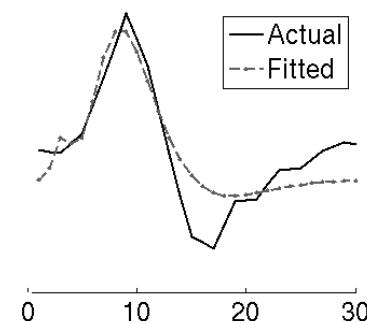
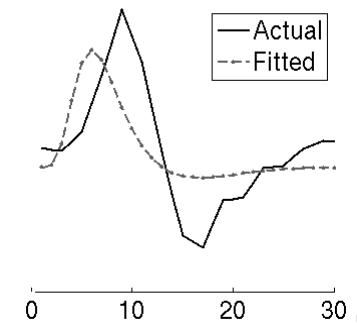
HRF +  
derivatives

Finite Impulse  
Response  
(FIR)



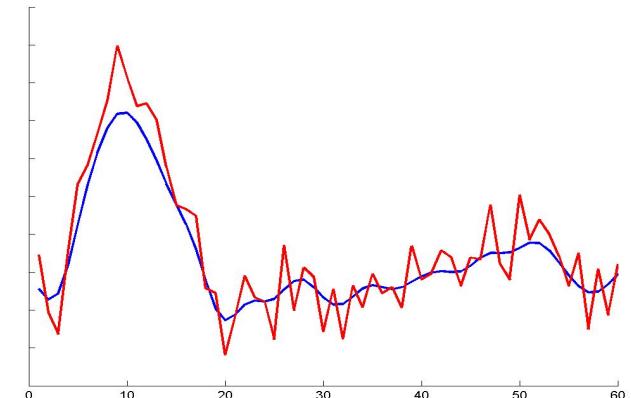
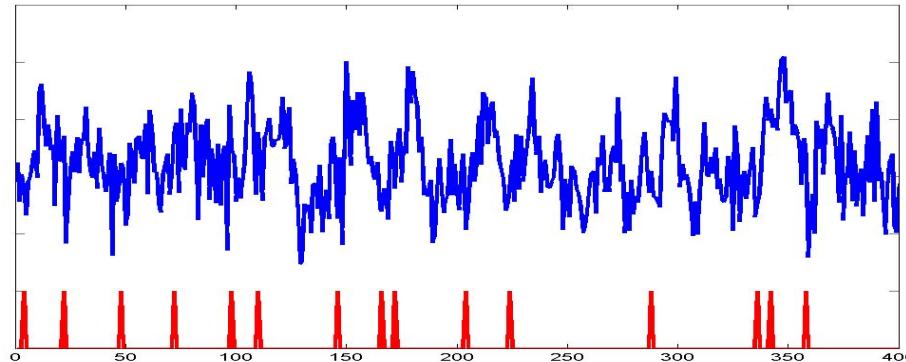
Basis functions

Data & Fitted



# Smooth FIR

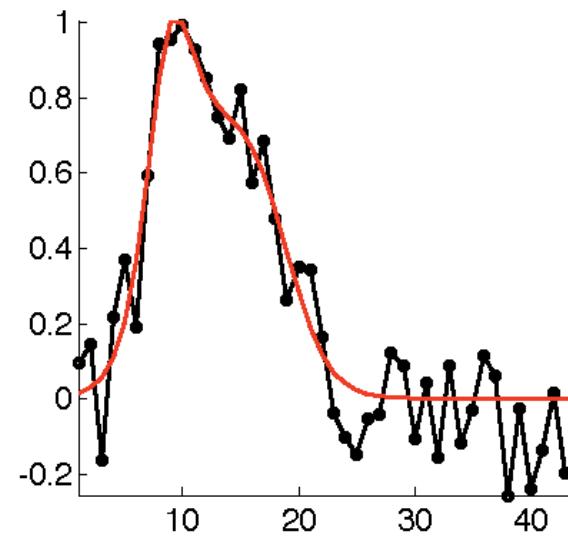
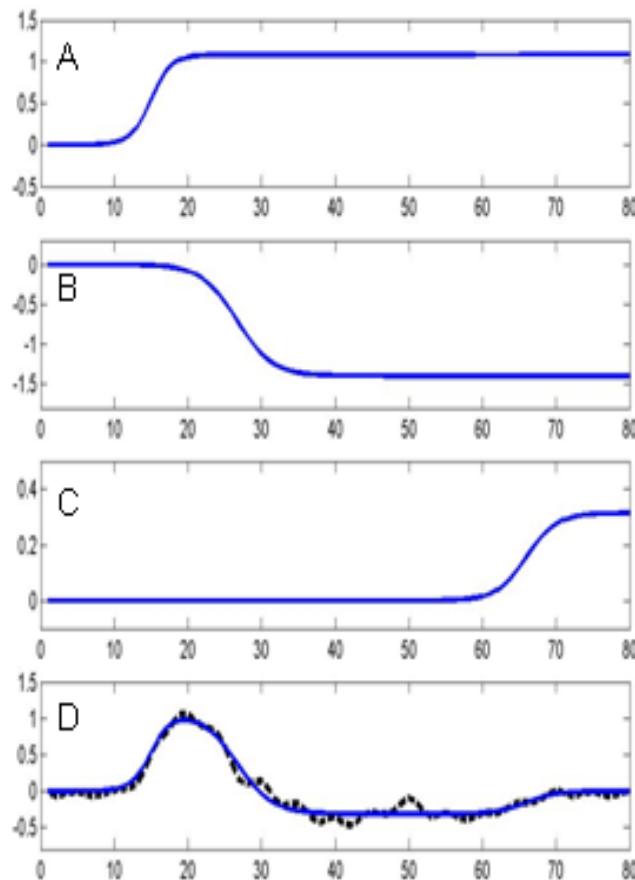
- The standard FIR method can give rise to noisy estimates of the HRF.
  - One can impose smoothness constraints by specifying a Gaussian prior on the filter parameters.
  - The maximum a posteriori estimate gives a smoothed version of the FIR fit (Goutte et al., 2000).



Red – FIR  
Blue – Smooth FIR

# Inverse Logit Model

- Alternatively one can use a superposition of three inverse logit (sigmoid) functions.



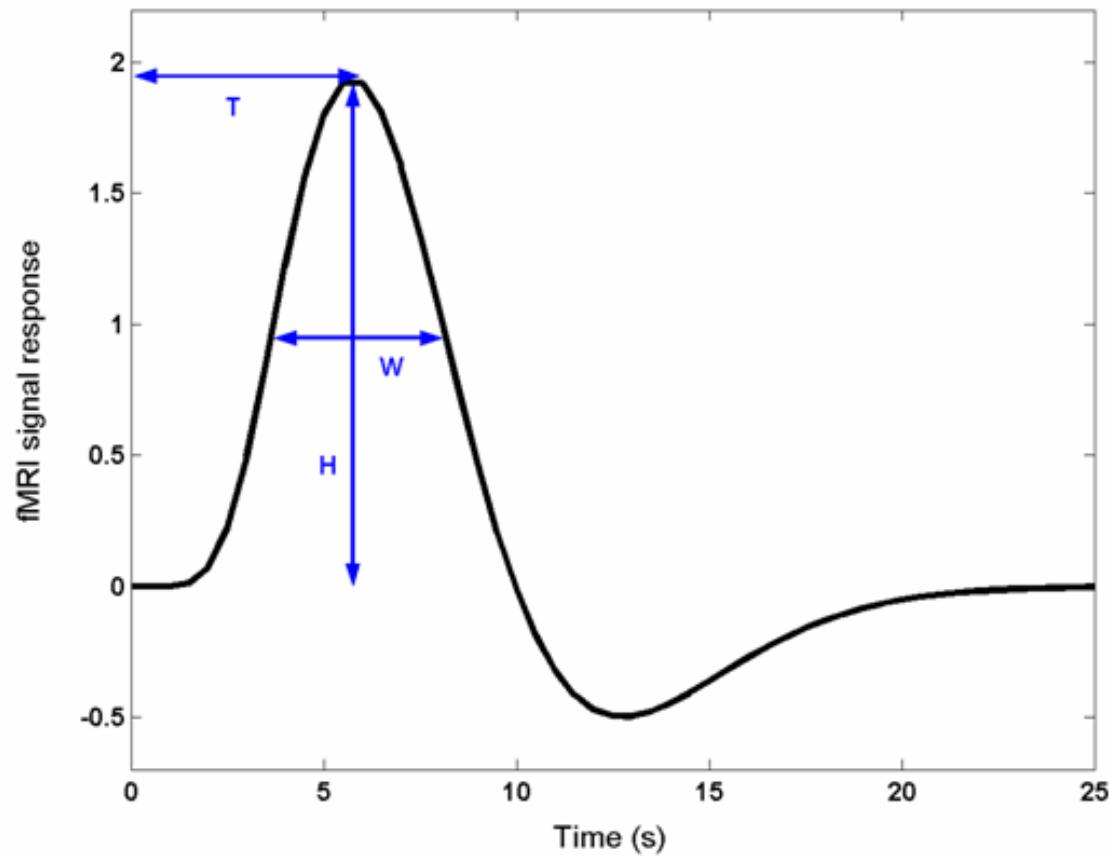
Black – Data  
Red – Fitted response

Lindquist & Wager (2007; 2008)

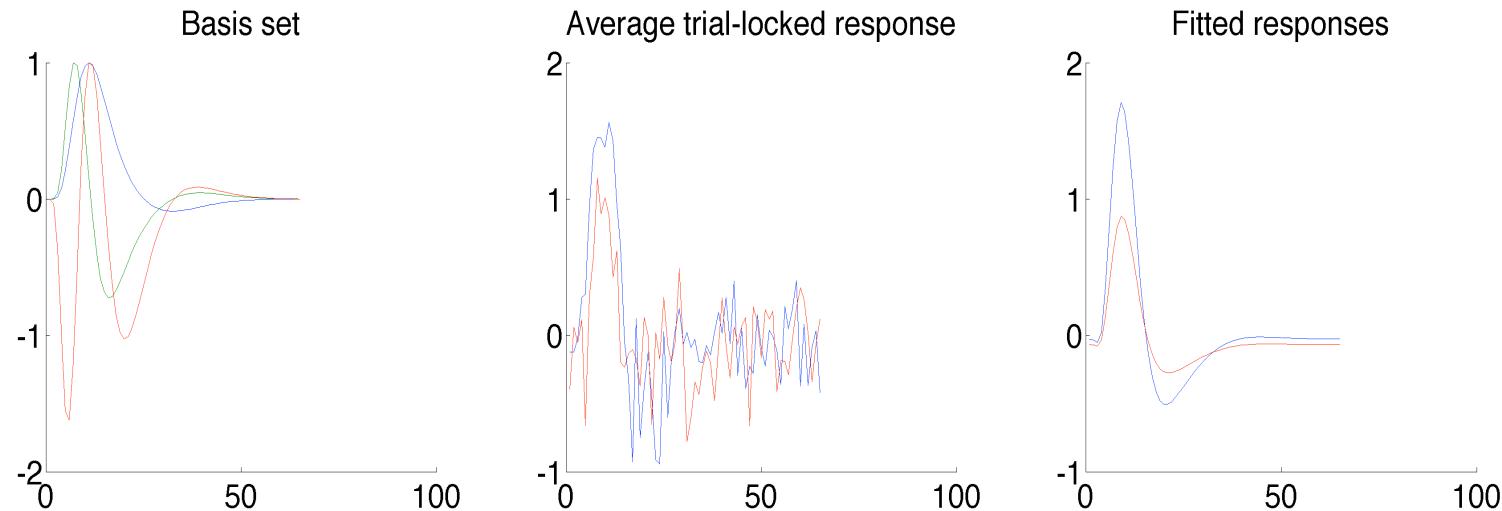
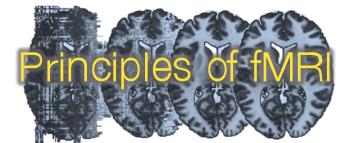
# Summarizing the HRF

- One problem with using basis sets is that it is difficult to summarize the response magnitude using a single number.
  - Problematic for second-level analysis.
- One can get around this by using
  - the “main” basis function,
  - all basis functions, or
  - re-parameterized fitted responses (Calhoun et al. (2004); Lindquist et al. (2009)).
    - Recreate the HRF and estimate the magnitude.
    - Use this information at the second level.

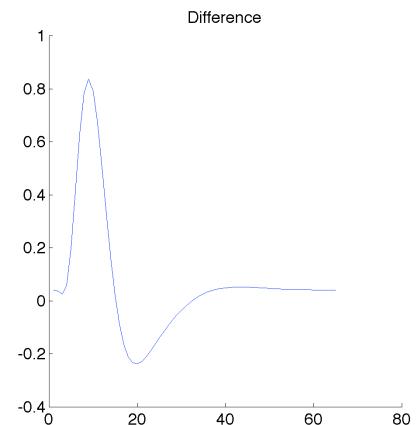
# Summarizing the HRF



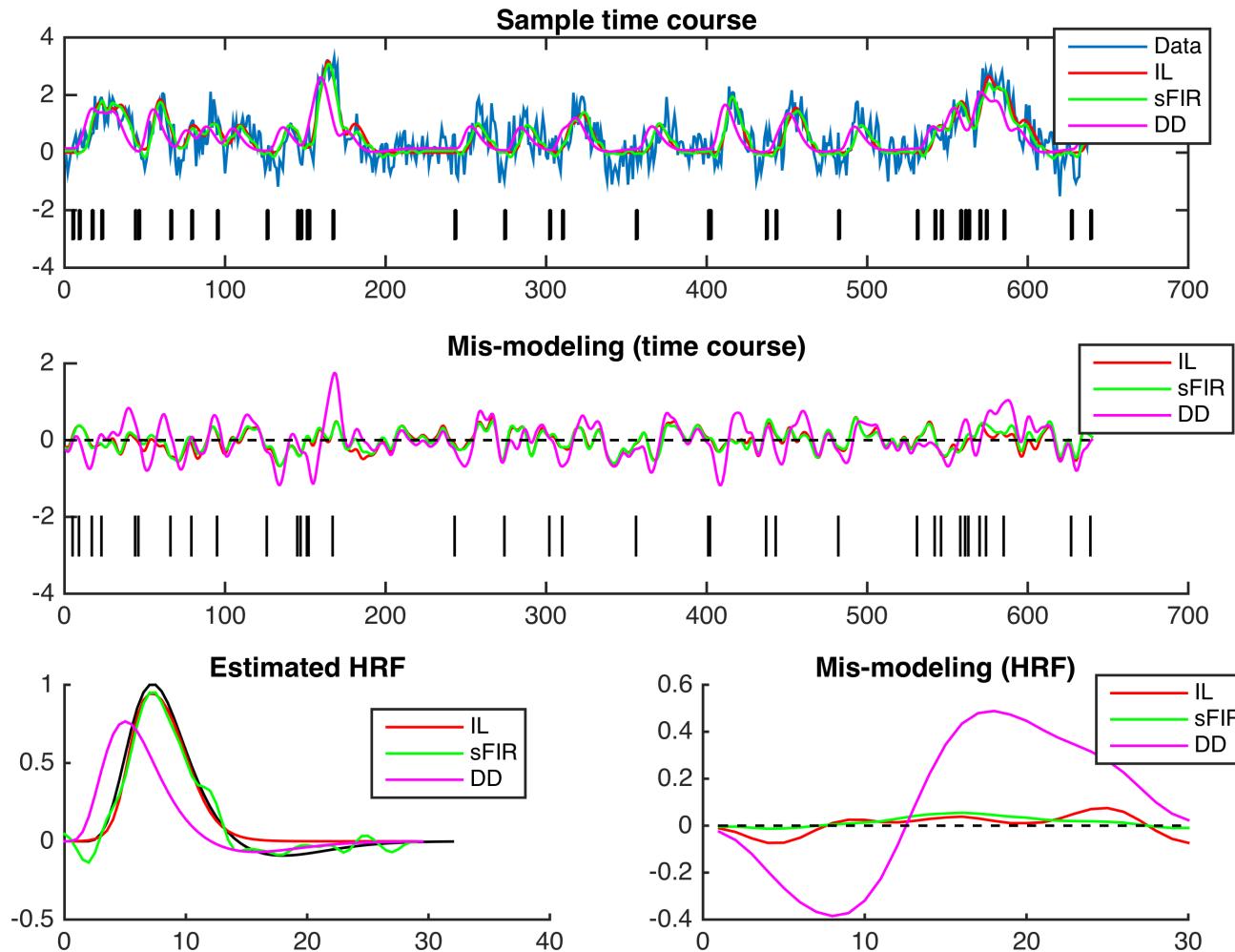
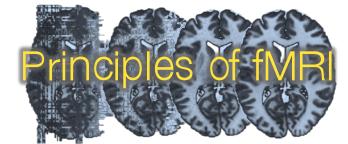
# Problems



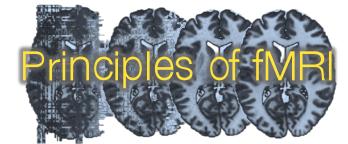
- All three parameters contribute to response magnitude!
  - Difference between amplitudes of fitted responses: 0.84
  - Difference between canonical HRF betas: 0.43
  - Amplitude of the difference does NOT equal difference between 'canonical' parameter estimates.



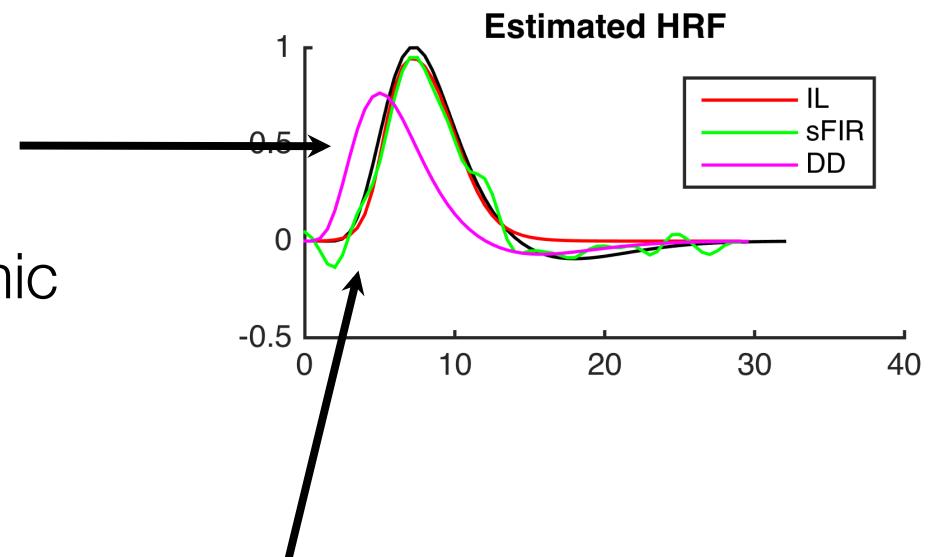
# Comparing Hemodynamic Models



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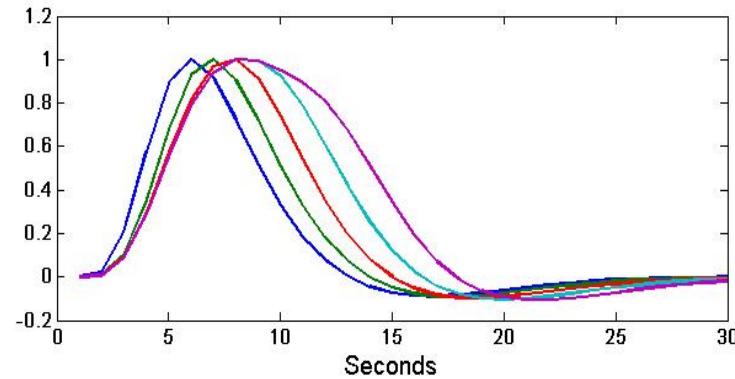
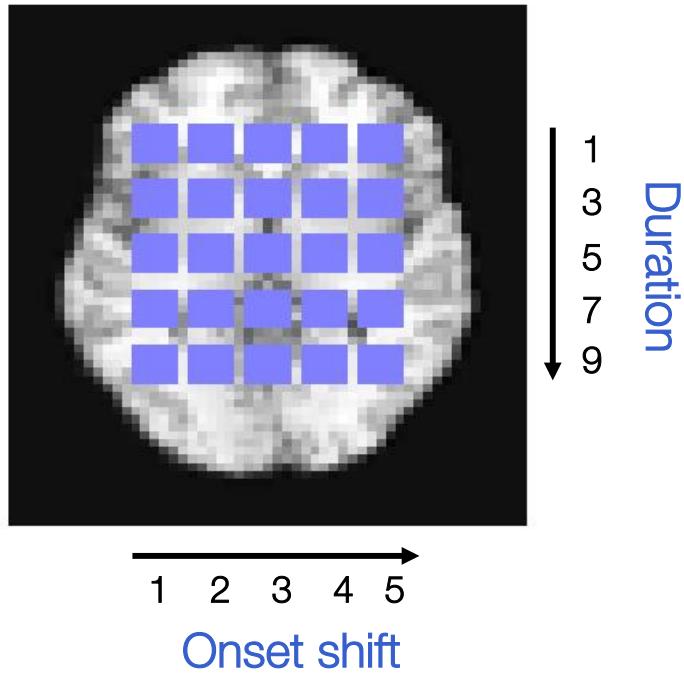


'Traditional' derivative model:  
Robust to noise, reliable  
...but not robust to hemodynamic  
variability



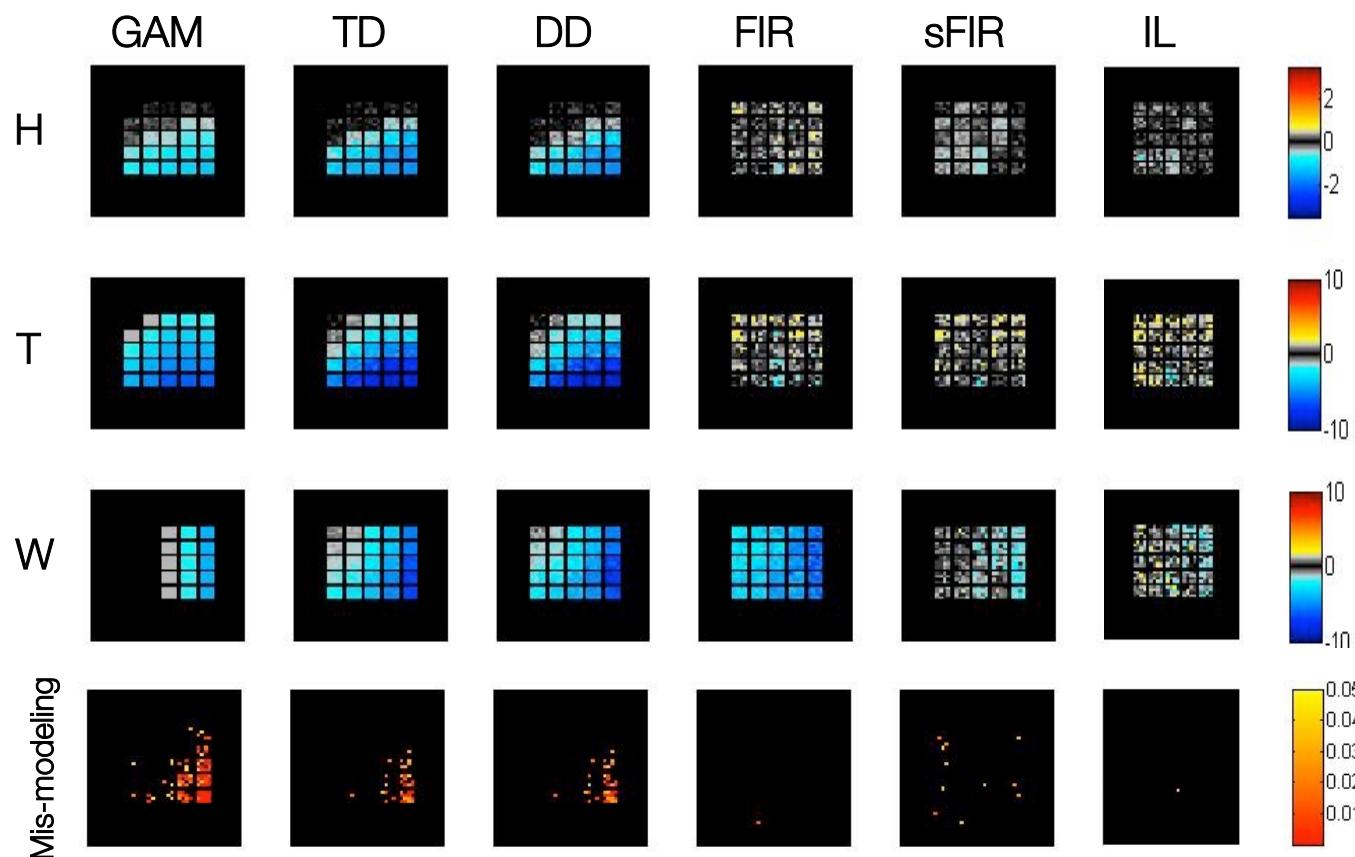
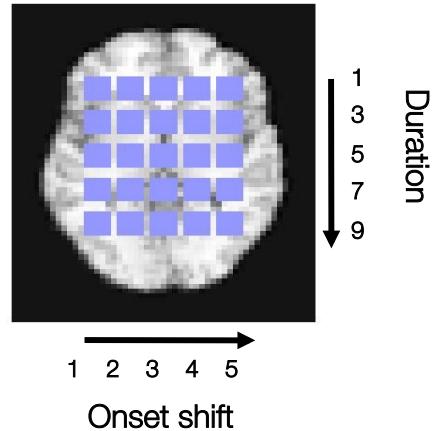
Flexible models:  
Robust to hemodynamic variability  
Less robust to noise (but still pretty good)

# Simulation



25 unique activations

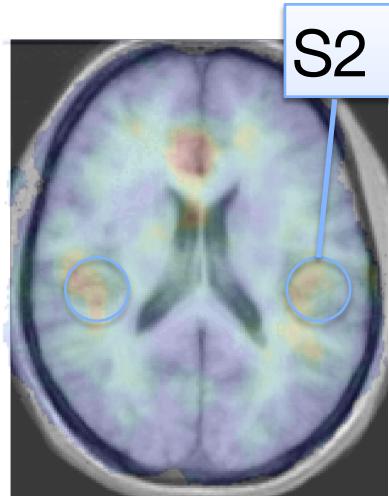
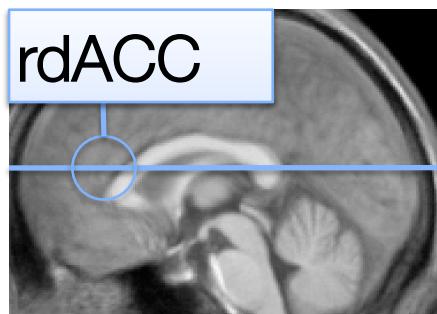
- TR=1, ISI = 30, 10 epochs, 15 “subjects”, Cohen’ s d = 0.5
- Estimates of amplitude were obtained and averaged across the 15 subjects.



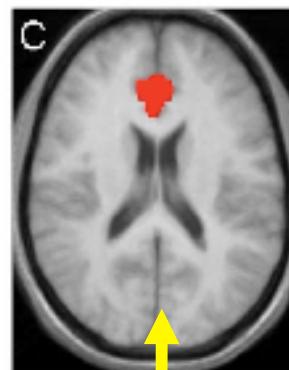
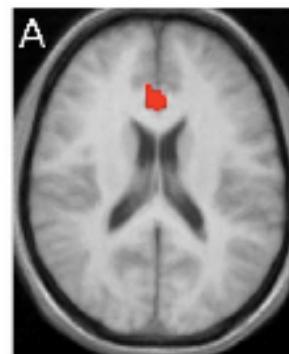
Lindquist & Wager, 2008; Loh, Lindquist, & Wager 2008

# Example

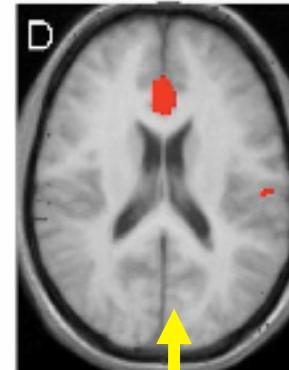
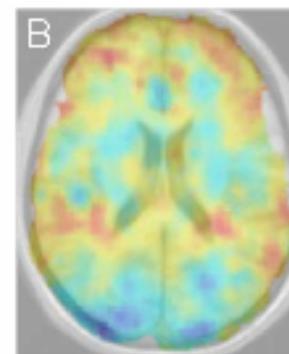
## Pain study Regions of interest



## SPM HRF+ Derivatives



Smooth FIR  
Goutte et al.

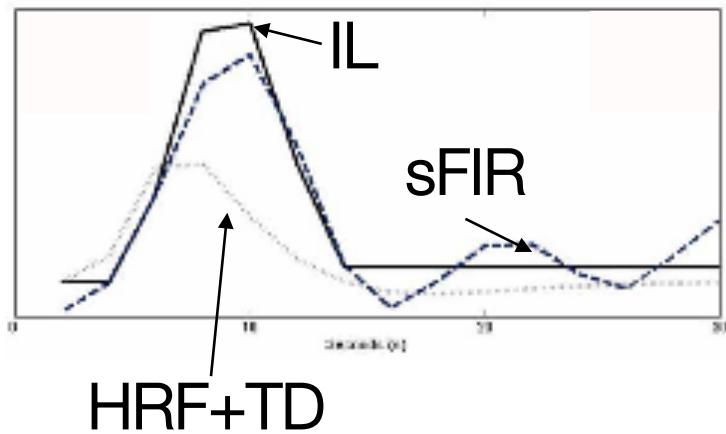


Inverse Logit  
Lindquist, & Wager 2007

Loh, Lindquist, &  
Wager 2008  
(yellow/red =  
mis-modeled)

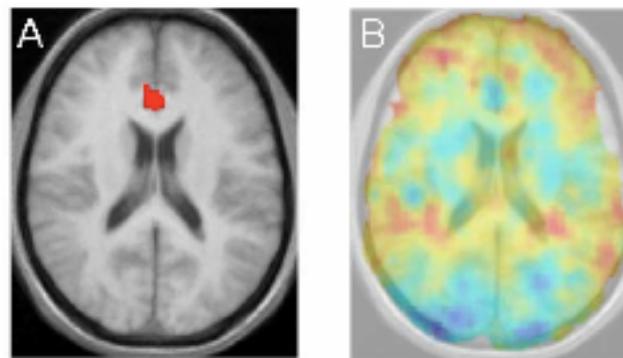
# Example

## Evoked HRF estimates



SPM HRF+  
Derivatives

Mis-modeling  
Map



Loh, Lindquist, &  
Wager 2008  
(yellow/red =  
mis-modeled)

Smooth FIR  
Goutte et al.

Inverse Logit  
Lindquist, & Wager 2007

# End of Module



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