## CS231n Convolutional Neural Networks for Visual Recognition

Course Website

## Python Numpy Tutorial (with Jupyter and Colab)



This tutorial was originally contributed by Justin Johnson.

We will use the Python programming language for all assignments in this course. Python is a great general-purpose programming language on its own, but with the help of a few popular libraries (numpy, scipy, matplotlib) it becomes a powerful environment for scientific computing.

We expect that many of you will have some experience with Python and numpy; for the rest of you, this section will serve as a quick crash course on both the Python programming language and its use for scientific computing. We'll also introduce notebooks, which are a very convenient way of tinkering with Python code. Some of you may have previous knowledge in a different language, in which case we also recommend referencing: NumPy for Matlab users, Python for R users, and/or Python for SAS users.

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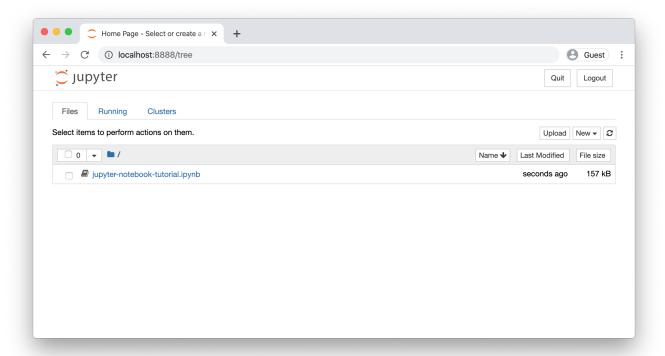
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## Jupyter and Colab Notebooks

Before we dive into Python, we'd like to briefly talk about *notebooks*. A Jupyter notebook lets you write and execute Python code *locally* in your web browser. Jupyter notebooks make it very easy to tinker with code and execute it in bits and pieces; for this reason they are widely used in scientific computing. Colab on the other hand is Google's flavor of Jupyter notebooks that is particularly suited for machine learning and data analysis and that runs entirely in the *cloud*. Colab is basically Jupyter notebook on steroids: it's free, requires no setup, comes preinstalled with many packages, is easy to share with the world, and benefits from free access to hardware accelerators like GPUs and TPUs (with some caveats).

**Run Tutorial in Colab (recommended)**. If you wish to run this tutorial entirely in Colab, click the **Open in Colab** badge at the very top of this page.

Run Tutorial in Jupyter Notebook. If you wish to run the notebook locally with Jupyter, make sure your virtual environment is installed correctly (as per the setup instructions), activate it, then run pip install notebook to install Jupyter notebook. Next, open the notebook and download it to a directory of your choice by right-clicking on the page and selecting Save Page As. Then cd to that directory and run jupyter notebook.



This should automatically launch a notebook server at <a href="http://localhost:8888">http://localhost:8888</a>. If everything worked correctly, you should see a screen like this, showing all available notebooks in the current directory. Click <a href="jupyter-notebook-tutorial.ipynb">jupyter-notebook-tutorial.ipynb</a> and follow the instructions in the notebook. Otherwise, you can continue reading the tutorial with code snippets below.

# Python

Python is a high-level, dynamically typed multiparadigm programming language. Python code is often said to be almost like pseudocode, since it allows you to express very powerful ideas in very few lines of code while being very readable. As an example, here is an implementation of the classic guicksort algorithm in Python:

```
def quicksort(arr):
    if len(arr) <= 1:
        return arr
    pivot = arr[len(arr) // 2]
    left = [x for x in arr if x < pivot]
    middle = [x for x in arr if x == pivot]
    right = [x for x in arr if x > pivot]
    return quicksort(left) + middle + quicksort(right)

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```

```
print(quicksort([3,6,8,10,1,2,1]))
# Prints "[1, 1, 2, 3, 6, 8, 10]"
```

## Python versions

As of January 1, 2020, Python has officially dropped support for python2. For this class all code will use Python 3.7. Ensure you have gone through the setup instructions and correctly installed a python3 virtual environment before proceeding with this tutorial. You can double-check your Python version at the command line after activating your environment by running python --version.

#### Basic data types

Like most languages, Python has a number of basic types including integers, floats, booleans, and strings. These data types behave in ways that are familiar from other programming languages.

**Numbers:** Integers and floats work as you would expect from other languages:

```
x = 3
print(type(x)) # Prints "<class 'int'>"
print(x) # Prints "3"
print(x + 1) # Addition; prints "4"
print(x - 1) # Subtraction; prints "2"
print(x * 2) # Multiplication; prints "6"
print(x ** 2) # Exponentiation; prints "9"
x += 1
print(x) # Prints "4"
x *= 2
print(x) # Prints "8"
y = 2.5
print(type(y)) # Prints "<class 'float'>"
print(y, y + 1, y * 2, y ** 2) # Prints "2.5 3.5 5.0 6.25"
```

Note that unlike many languages, Python does not have unary increment (x++) or decrement (x--) operators.

Python also has built-in types for complex numbers; you can find all of the details in the documentation.

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**Booleans:** Python implements all of the usual operators for Boolean logic, but uses English words rather than symbols (&&, | | |, etc.):

```
t = True
f = False
print(type(t)) # Prints "<class 'bool'>"
print(t and f) # Logical AND; prints "False"
print(t or f) # Logical OR; prints "True"
print(not t) # Logical NOT; prints "False"
print(t != f) # Logical XOR; prints "True"
```

**Strings:** Python has great support for strings:

```
hello = 'hello'  # String literals can use single quotes
world = "world"  # or double quotes; it does not matter.
print(hello)  # Prints "hello"
print(len(hello))  # String length; prints "5"
hw = hello + ' ' + world  # String concatenation
print(hw)  # prints "hello world"
hw12 = '%s %s %d' % (hello, world, 12)  # sprintf style string formatting
print(hw12)  # prints "hello world 12"
```

String objects have a bunch of useful methods; for example:

You can find a list of all string methods in the documentation.

#### Containers

Python includes several built-in container types: lists, dictionaries, sets, and tuples.

Lists

A list is the Python equivalent of an array, but is resizeable and can contain elements of different types:

```
xs = [3, 1, 2]  # Create a list
print(xs, xs[2])  # Prints "[3, 1, 2] 2"
print(xs[-1])  # Negative indices count from the end of the list; print(xs[2] = 'foo'  # Lists can contain elements of different types
print(xs)  # Prints "[3, 1, 'foo']"
xs.append('bar')  # Add a new element to the end of the list
print(xs)  # Prints "[3, 1, 'foo', 'bar']"
x = xs.pop()  # Remove and return the last element of the list
print(x, xs)  # Prints "bar [3, 1, 'foo']"
```

As usual, you can find all the gory details about lists in the documentation.

**Slicing:** In addition to accessing list elements one at a time, Python provides concise syntax to access sublists; this is known as *slicing*:

```
nums = list(range(5))
                         # range is a built-in function that creates a l
print(nums)
                         # Prints "[0, 1, 2, 3, 4]"
print(nums[2:4])
                         # Get a slice from index 2 to 4 (exclusive); pr
print(nums[2:])
                  # Get a slice from index 2 to the end; prints '
print(nums[:2])
                         # Get a slice from the start to index 2 (exclusion)
                         # Get a slice of the whole list; prints "[0, 1]
print(nums[:])
print(nums[:-1])
                         # Slice indices can be negative; prints "[0, 1,
nums[2:4] = [8, 9]
                         # Assign a new sublist to a slice
print(nums)
                         # Prints "[0, 1, 8, 9, 4]"
```

We will see slicing again in the context of numpy arrays.

**Loops:** You can loop over the elements of a list like this:

```
animals = ['cat', 'dog', 'monkey']
for animal in animals:
    print(animal)
# Prints "cat", "dog", "monkey", each on its own line.
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```

If you want access to the index of each element within the body of a loop, use the built-in **enumerate** function:

```
animals = ['cat', 'dog', 'monkey']
for idx, animal in enumerate(animals):
    print('#%d: %s' % (idx + 1, animal))
# Prints "#1: cat", "#2: dog", "#3: monkey", each on its own line
```

**List comprehensions:** When programming, frequently we want to transform one type of data into another. As a simple example, consider the following code that computes square numbers:

```
nums = [0, 1, 2, 3, 4]
squares = []
for x in nums:
    squares.append(x ** 2)
print(squares) # Prints [0, 1, 4, 9, 16]
```

You can make this code simpler using a **list comprehension**:

```
nums = [0, 1, 2, 3, 4]
squares = [x ** 2 for x in nums]
print(squares) # Prints [0, 1, 4, 9, 16]
```

List comprehensions can also contain conditions:

```
nums = [0, 1, 2, 3, 4]
even_squares = [x ** 2 for x in nums if x % 2 == 0]
print(even_squares) # Prints "[0, 4, 16]"
```

#### **Dictionaries**

A dictionary stores (key, value) pairs, similar to a Map in Java or an object in Javascript. You can use it like this:

```
d = {'cat': 'cute', 'dog': 'furry'} # Create a new dictionary with some
print(d['cat']) # Get an entry from a dictionary; prints "Back to Top
print('cat' in d) # Check if a dictionary has a given key; prints "II
```

```
d['fish'] = 'wet'  # Set an entry in a dictionary
print(d['fish'])  # Prints "wet"

# print(d['monkey'])  # KeyError: 'monkey' not a key of d
print(d.get('monkey', 'N/A'))  # Get an element with a default; prints "I
print(d.get('fish', 'N/A'))  # Get an element with a default; prints "I
del d['fish']  # Remove an element from a dictionary
print(d.get('fish', 'N/A'))  # "fish" is no longer a key; prints "N/A"
```

You can find all you need to know about dictionaries in the documentation.

**Loops:** It is easy to iterate over the keys in a dictionary:

```
d = {'person': 2, 'cat': 4, 'spider': 8}
for animal in d:
    legs = d[animal]
    print('A %s has %d legs' % (animal, legs))
# Prints "A person has 2 legs", "A cat has 4 legs", "A spider has 8 legs'
```

If you want access to keys and their corresponding values, use the items method:

```
d = {'person': 2, 'cat': 4, 'spider': 8}
for animal, legs in d.items():
    print('A %s has %d legs' % (animal, legs))
# Prints "A person has 2 legs", "A cat has 4 legs", "A spider has 8 legs'
```

**Dictionary comprehensions:** These are similar to list comprehensions, but allow you to easily construct dictionaries. For example:

```
nums = [0, 1, 2, 3, 4]
even_num_to_square = {x: x ** 2 for x in nums if x % 2 == 0}
print(even_num_to_square) # Prints "{0: 0, 2: 4, 4: 16}"
```

#### Sets

A set is an unordered collection of distinct elements. As a simple example, consider the following:

```
animals = {'cat', 'dog'}
print('cat' in animals)
                         # Check if an element is in a set; prints "True"
print('fish' in animals) # prints "False"
animals.add('fish')
                        # Add an element to a set
print('fish' in animals) # Prints "True"
print(len(animals))
                        # Number of elements in a set; prints "3"
animals.add('cat')
                        # Adding an element that is already in the set
print(len(animals)) # Prints "3"
animals.remove('cat')
                        # Remove an element from a set
print(len(animals))
                        # Prints "2"
```

As usual, everything you want to know about sets can be found in the documentation.

**Loops:** Iterating over a set has the same syntax as iterating over a list; however since sets are unordered, you cannot make assumptions about the order in which you visit the elements of the set:

```
animals = {'cat', 'dog', 'fish'}
for idx, animal in enumerate(animals):
    print('#%d: %s' % (idx + 1, animal))
# Prints "#1: fish", "#2: dog", "#3: cat"
```

**Set comprehensions:** Like lists and dictionaries, we can easily construct sets using set comprehensions:

```
from math import sqrt
nums = {int(sqrt(x)) for x in range(30)}
print(nums) # Prints "{0, 1, 2, 3, 4, 5}"
```

#### **Tuples**

A tuple is an (immutable) ordered list of values. A tuple is in many ways similar to a list; one of the most important differences is that tuples can be used as keys in dictionaries and as elements of sets, while lists cannot. Here is a trivial example:

```
d = {(x, x + 1): x for x in range(10)} # Create a dictionary with tuple
t = (5, 6) # Create a tuple
print(type(t)) # Prints "<class 'tuple'>"
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```

```
print(d[t])  # Prints "5"
print(d[(1, 2)]) # Prints "1"
```

The documentation has more information about tuples.

#### **Functions**

Python functions are defined using the def keyword. For example:

```
def sign(x):
    if x > 0:
        return 'positive'
    elif x < 0:
        return 'negative'
    else:
        return 'zero'

for x in [-1, 0, 1]:
    print(sign(x))
# Prints "negative", "zero", "positive"</pre>
```

We will often define functions to take optional keyword arguments, like this:

```
def hello(name, loud=False):
    if loud:
        print('HELLO, %s!' % name.upper())
    else:
        print('Hello, %s' % name)

hello('Bob') # Prints "Hello, Bob"
hello('Fred', loud=True) # Prints "HELLO, FRED!"
```

There is a lot more information about Python functions in the documentation.

#### Classes

The syntax for defining classes in Python is straightforward:

```
class Greeter(object):

# Constructor

def __init__(self, name):
        self.name = name # Create an instance variable

# Instance method

def greet(self, loud=False):
        if loud:
            print('HELLO, %s!' % self.name.upper())
        else:
            print('Hello, %s' % self.name)

g = Greeter('Fred') # Construct an instance of the Greeter class
g.greet() # Call an instance method; prints "Hello, Fred"
g.greet(loud=True) # Call an instance method; prints "HELLO, FRED!"
```

You can read a lot more about Python classes in the documentation.

# Numpy

Numpy is the core library for scientific computing in Python. It provides a high-performance multidimensional array object, and tools for working with these arrays. If you are already familiar with MATLAB, you might find this tutorial useful to get started with Numpy.

#### Arrays

A numpy array is a grid of values, all of the same type, and is indexed by a tuple of nonnegative integers. The number of dimensions is the *rank* of the array; the *shape* of an array is a tuple of integers giving the size of the array along each dimension.

We can initialize numpy arrays from nested Python lists, and access elements using square brackets:

```
import numpy as np

a = np.array([1, 2, 3])  # Create a rank 1 array
print(type(a))  # Prints "<class 'numpy.ndarray'>"
print(a.shape)  # Prints "(3,)"

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```

Numpy also provides many functions to create arrays:

```
import numpy as np
a = np.zeros((2,2)) # Create an array of all zeros
                    # Prints "[[ 0. 0.]
print(a)
                               [ 0. 0.11"
b = np.ones((1,2)) # Create an array of all ones
print(b)
                    # Prints "[[ 1. 1.]]"
c = np.full((2,2), 7) # Create a constant array
                      # Prints "[[ 7. 7.]
print(c)
                                [7. 7.11"
d = np.eye(2)
                    # Create a 2x2 identity matrix
print(d)
                     # Prints "[[ 1. 0.]
                     #
                               [ 0. 1.]]"
e = np.random.random((2,2)) # Create an array filled with random values
                            # Might print "[[ 0.91940167  0.08143941]
print(e)
                            #
                                            [ 0.68744134  0.87236687]]"
```

You can read about other methods of array creation in the documentation.

#### Array indexing

Numpy offers several ways to index into arrays.

**Slicing:** Similar to Python lists, numpy arrays can be sliced. Since arrays may be multidimensional, you must specify a slice for each dimension of the array:

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```
import numpy as np
# Create the following rank 2 array with shape (3, 4)
# [[ 1 2 3 4]
# [5 6 7 8]
# [ 9 10 11 12]]
a = np.array([[1,2,3,4], [5,6,7,8], [9,10,11,12]])
# Use slicing to pull out the subarray consisting of the first 2 rows
# and columns 1 and 2; b is the following array of shape (2, 2):
# [[2 3]
# [6 7]]
b = a[:2, 1:3]
# A slice of an array is a view into the same data, so modifying it
# will modify the original array.
print(a[0, 1]) # Prints "2"
b[0, 0] = 77 # b[0, 0] is the same piece of data as a[0, 1]
print(a[0, 1]) # Prints "77"
```

You can also mix integer indexing with slice indexing. However, doing so will yield an array of lower rank than the original array. Note that this is quite different from the way that MATLAB handles array slicing:

```
import numpy as np
# Create the following rank 2 array with shape (3, 4)
# [[ 1 2 3 4]
# [5 6 7 8]
# [ 9 10 11 12]]
a = np.array([[1,2,3,4], [5,6,7,8], [9,10,11,12]])
# Two ways of accessing the data in the middle row of the array.
# Mixing integer indexing with slices yields an array of lower rank,
# while using only slices yields an array of the same rank as the
# original array:
row r1 = a[1, :] # Rank 1 view of the second row of a
row_r2 = a[1:2, :] # Rank 2 view of the second row of a
print(row_r1, row_r1.shape) # Prints "[5 6 7 8] (4,)"
print(row_r2, row_r2.shape) # Prints "[[5 6 7 8]] (1, 4)"
                                                                 Back to Top
```

**Integer array indexing:** When you index into numpy arrays using slicing, the resulting array view will always be a subarray of the original array. In contrast, integer array indexing allows you to construct arbitrary arrays using the data from another array. Here is an example:

```
import numpy as np

a = np.array([[1,2], [3, 4], [5, 6]])

# An example of integer array indexing.
# The returned array will have shape (3,) and
print(a[[0, 1, 2], [0, 1, 0]]) # Prints "[1 4 5]"

# The above example of integer array indexing is equivalent to this:
print(np.array([a[0, 0], a[1, 1], a[2, 0]])) # Prints "[1 4 5]"

# When using integer array indexing, you can reuse the same
# element from the source array:
print(a[[0, 0], [1, 1]]) # Prints "[2 2]"

# Equivalent to the previous integer array indexing example
print(np.array([a[0, 1], a[0, 1]])) # Prints "[2 2]"
```

One useful trick with integer array indexing is selecting or mutating one element from each row of a matrix:

**Boolean array indexing:** Boolean array indexing lets you pick out arbitrary elements of an array. Frequently this type of indexing is used to select the elements of an array that satisfy some condition. Here is an example:

```
import numpy as np
a = np.array([[1,2], [3, 4], [5, 6]])
bool idx = (a > 2) # Find the elements of a that are bigger than 2;
                     # this returns a numpy array of Booleans of the same
                     # shape as a, where each slot of bool idx tells
                     # whether that element of a is > 2.
print(bool_idx)
                    # Prints "[[False False]
                                [ True True]
                                [ True True]]"
                     #
# We use boolean array indexing to construct a rank 1 array
# consisting of the elements of a corresponding to the True values
# of bool idx
print(a[bool idx]) # Prints "[3 4 5 6]"
# We can do all of the above in a single concise statement:
print(a[a > 2])  # Prints "[3 4 5 6]"
                                                                  Back to Top
```

For brevity we have left out a lot of details about numpy array indexing; if you want to know more you should read the documentation.

#### **Datatypes**

Every numpy array is a grid of elements of the same type. Numpy provides a large set of numeric datatypes that you can use to construct arrays. Numpy tries to guess a datatype when you create an array, but functions that construct arrays usually also include an optional argument to explicitly specify the datatype. Here is an example:

```
import numpy as np

x = np.array([1, 2])  # Let numpy choose the datatype
print(x.dtype)  # Prints "int64"

x = np.array([1.0, 2.0])  # Let numpy choose the datatype
print(x.dtype)  # Prints "float64"

x = np.array([1, 2], dtype=np.int64)  # Force a particular datatype
print(x.dtype)  # Prints "int64"
```

You can read all about numpy datatypes in the documentation.

## Array math

Basic mathematical functions operate elementwise on arrays, and are available both as operator overloads and as functions in the numpy module:

```
import numpy as np

x = np.array([[1,2],[3,4]], dtype=np.float64)

y = np.array([[5,6],[7,8]], dtype=np.float64)

# Elementwise sum; both produce the array

# [[ 6.0 8.0]

# [10.0 12.0]]

print(x + y)

print(np.add(x, y))
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```

```
# Elementwise difference; both produce the array
# [[-4.0 -4.0]
# [-4.0 -4.0]]
print(x - y)
print(np.subtract(x, y))
# Elementwise product; both produce the array
# [[ 5.0 12.0]
# [21.0 32.0]]
print(x * y)
print(np.multiply(x, y))
# Elementwise division; both produce the array
# [[ 0.2
                 0.333333331
# [ 0.42857143
                 0.5
                           11
print(x / y)
print(np.divide(x, y))
# Elementwise square root; produces the array
# [[ 1.
                 1.414213561
# [ 1.73205081 2.
                           11
print(np.sqrt(x))
```

Note that unlike MATLAB, \* is elementwise multiplication, not matrix multiplication. We instead use the dot function to compute inner products of vectors, to multiply a vector by a matrix, and to multiply matrices. dot is available both as a function in the numpy module and as an instance method of array objects:

```
import numpy as np

x = np.array([[1,2],[3,4]])
y = np.array([[5,6],[7,8]])

v = np.array([9,10])
w = np.array([11, 12])

# Inner product of vectors; both produce 219
print(v.dot(w))
print(np.dot(v, w))

# Matrix / vector product; both produce the rank 1 array [29 67] Back to Top
print(x.dot(v))
```

```
print(np.dot(x, v))

# Matrix / matrix product; both produce the rank 2 array
# [[19 22]
# [43 50]]
print(x.dot(y))
print(np.dot(x, y))
```

Numpy provides many useful functions for performing computations on arrays; one of the most useful is sum:

```
import numpy as np

x = np.array([[1,2],[3,4]])

print(np.sum(x)) # Compute sum of all elements; prints "10"
print(np.sum(x, axis=0)) # Compute sum of each column; prints "[4 6]"
print(np.sum(x, axis=1)) # Compute sum of each row; prints "[3 7]"
```

You can find the full list of mathematical functions provided by numpy in the documentation.

Apart from computing mathematical functions using arrays, we frequently need to reshape or otherwise manipulate data in arrays. The simplest example of this type of operation is transposing a matrix; to transpose a matrix, simply use the T attribute of an array object:

Numpy provides many more functions for manipulating arrays; you can see the full list in the documentation.

### Broadcasting

Broadcasting is a powerful mechanism that allows numpy to work with arrays of different shapes when performing arithmetic operations. Frequently we have a smaller array and a larger array, and we want to use the smaller array multiple times to perform some operation on the larger array.

For example, suppose that we want to add a constant vector to each row of a matrix. We could do it like this:

```
import numpy as np
# We will add the vector v to each row of the matrix x,
# storing the result in the matrix y
x = np.array([[1,2,3], [4,5,6], [7,8,9], [10, 11, 12]])
v = np.array([1, 0, 1])
                      # Create an empty matrix with the same shape as x
y = np.empty_like(x)
# Add the vector v to each row of the matrix x with an explicit loop
for i in range(4):
   y[i, :] = x[i, :] + v
# Now y is the following
# [[ 2 2 4]
# [5 5 7]
 [8 8 10]
 [11 11 13]]
print(y)
```

This works; however when the matrix x is very large, computing an explicit loop in Python could be slow. Note that adding the vector v to each row of the matrix x is equivalent to forming a matrix vv by stacking multiple copies of v vertically, then performing elementwise summation of x and vv. We could implement this approach like this:

```
import numpy as np

# We will add the vector v to each row of the matrix x,
# storing the result in the matrix y
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```

```
x = np.array([[1,2,3], [4,5,6], [7,8,9], [10, 11, 12]])
v = np.array([1, 0, 1])
vv = np.tile(v, (4, 1)) # Stack 4 copies of v on top of each other
                          # Prints "[[1 0 1]
print(vv)
                          #
                                     [1 0 1]
                          #
                                     [1 0 1]
                                     [1 0 1]]"
y = x + vv # Add x and vv elementwise
print(y) # Prints "[[ 2  2  4
         #
                     [ 5 5 71
         #
                     [8 8 10]
                     [11 11 13]]"
```

Numpy broadcasting allows us to perform this computation without actually creating multiple copies of v. Consider this version, using broadcasting:

The line y = x + v works even though x has shape (4, 3) and v has shape (3, ) due to broadcasting; this line works as if v actually had shape (4, 3), where each row was a copy of v, and the sum was performed elementwise.

Broadcasting two arrays together follows these rules:

- 1. If the arrays do not have the same rank, prepend the shape of the lower rank array with 1s until both shapes have the same length.
- 2. The two arrays are said to be *compatible* in a dimension if they have the same size in the dimension, or if one of the arrays has size 1 in that dimension.
- 3. The arrays can be broadcast together if they are compatible in all dimensions.

- 4. After broadcasting, each array behaves as if it had shape equal to the elementwise maximum of shapes of the two input arrays.
- 5. In any dimension where one array had size 1 and the other array had size greater than 1, the first array behaves as if it were copied along that dimension

If this explanation does not make sense, try reading the explanation from the documentation or this explanation.

Functions that support broadcasting are known as *universal functions*. You can find the list of all universal functions in the documentation.

Here are some applications of broadcasting:

```
import numpy as np
# Compute outer product of vectors
v = np.array([1,2,3]) # v has shape (3,)
w = np.array([4,5]) # w has shape (2,)
# To compute an outer product, we first reshape v to be a column
# vector of shape (3, 1); we can then broadcast it against w to yield
# an output of shape (3, 2), which is the outer product of v and w:
# [[ 4 5]
# [8 10]
# [12 15]]
print(np.reshape(v, (3, 1)) * w)
# Add a vector to each row of a matrix
x = np.array([[1,2,3], [4,5,6]])
\# x has shape (2, 3) and v has shape (3,) so they broadcast to (2, 3),
# giving the following matrix:
# [[2 4 6]
# [5 7 911
print(x + v)
# Add a vector to each column of a matrix
\# x has shape (2, 3) and w has shape (2,).
# If we transpose x then it has shape (3, 2) and can be broadcast
# against w to yield a result of shape (3, 2); transposing this result
\# yields the final result of shape (2, 3) which is the matrix x with
# the vector w added to each column. Gives the following matrix:
# [[ 5 6 7]
# [ 9 10 11]]
                                                                  Back to Top
print((x.T + w).T)
```

```
# Another solution is to reshape w to be a column vector of shape (2, 1);
# we can then broadcast it directly against x to produce the same
# output.
print(x + np.reshape(w, (2, 1)))

# Multiply a matrix by a constant:
# x has shape (2, 3). Numpy treats scalars as arrays of shape ();
# these can be broadcast together to shape (2, 3), producing the
# following array:
# [[ 2  4  6]
# [ 8 10 12]]
print(x * 2)
```

Broadcasting typically makes your code more concise and faster, so you should strive to use it where possible.

#### Numpy Documentation

This brief overview has touched on many of the important things that you need to know about numpy, but is far from complete. Check out the numpy reference to find out much more about numpy.

## SciPy

Numpy provides a high-performance multidimensional array and basic tools to compute with and manipulate these arrays. SciPy builds on this, and provides a large number of functions that operate on numpy arrays and are useful for different types of scientific and engineering applications.

The best way to get familiar with SciPy is to browse the documentation. We will highlight some parts of SciPy that you might find useful for this class.

#### Image operations

SciPy provides some basic functions to work with images. For example, it has functions to read images from disk into numpy arrays, to write numpy arrays to disk as images, and to resize images. Here is a simple example that showcases these functions:

```
# Read an JPEG image into a numpy array
img = imread('assets/cat.jpg')
print(img.dtype, img.shape) # Prints "uint8 (400, 248, 3)"

# We can tint the image by scaling each of the color channels
# by a different scalar constant. The image has shape (400, 248, 3);
# we multiply it by the array [1, 0.95, 0.9] of shape (3,);
# numpy broadcasting means that this leaves the red channel unchanged,
# and multiplies the green and blue channels by 0.95 and 0.9
# respectively.
img_tinted = img * [1, 0.95, 0.9]

# Resize the tinted image to be 300 by 300 pixels.
img_tinted = imresize(img_tinted, (300, 300))

# Write the tinted image back to disk
imsave('assets/cat_tinted.jpg', img_tinted)
```



Left: The original image. Right: The tinted and resized image.

#### MATLAB files

The functions **scipy.io.loadmat** and **scipy.io.savemat** allow you to read and write MATLAB files. You can read about them in the documentation.

#### Distance between points

SciPy defines some useful functions for computing distances between sets of points.

The function scipy.spatial.distance.pdist computes the distance between all pairs of points in a given set:

```
import numpy as np
from scipy spatial distance import pdist, squareform
# Create the following array where each row is a point in 2D space:
# [[0 1]
# [1 0]
# [2 0]]
x = np.array([[0, 1], [1, 0], [2, 0]])
print(x)
# Compute the Euclidean distance between all rows of x.
# d[i, j] is the Euclidean distance between x[i, :] and x[j, :],
# and d is the following array:
# [[ 0.
                 1.41421356 2.236067981
# [ 1.41421356 0.
                             1.
# [ 2.23606798 1.
                                       ]]
d = squareform(pdist(x, 'euclidean'))
print(d)
```

You can read all the details about this function in the documentation.

A similar function (scipy.spatial.distance.cdist) computes the distance between all pairs across two sets of points; you can read about it in the documentation.

## Matplotlib

Matplotlib is a plotting library. In this section give a brief introduct Back to Top matplotlib.pyplot module, which provides a plotting system similar to that of MATLAB.

### **Plotting**

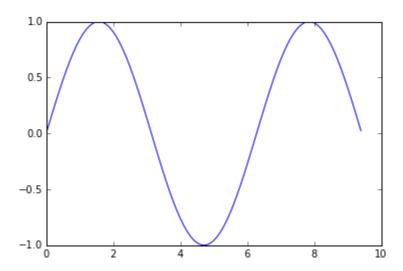
The most important function in matplotlib is **plot**, which allows you to plot 2D data. Here is a simple example:

```
import numpy as np
import matplotlib.pyplot as plt

# Compute the x and y coordinates for points on a sine curve
x = np.arange(0, 3 * np.pi, 0.1)
y = np.sin(x)

# Plot the points using matplotlib
plt.plot(x, y)
plt.show() # You must call plt.show() to make graphics appear.
```

Running this code produces the following plot:



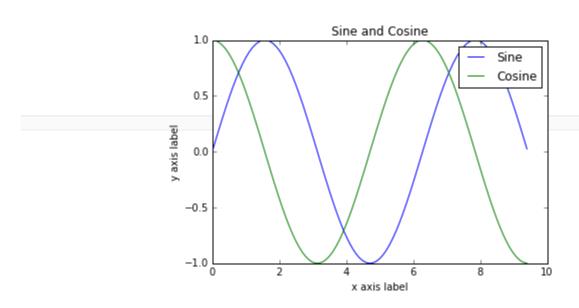
With just a little bit of extra work we can easily plot multiple lines at once, and add a title, legend, and axis labels:

```
import numpy as np
import matplotlib.pyplot as plt

# Compute the x and y coordinates for points on sine and cosine curves
x = np.arange(0, 3 * np.pi, 0.1)
y_sin = np.sin(x)
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```

```
y_cos = np.cos(x)

# Plot the points using matplotlib
plt.plot(x, y_sin)
plt.plot(x, y_cos)
plt.xlabel('x axis label')
plt.ylabel('y axis label')
plt.title('Sine and Cosine')
plt.legend(['Sine', 'Cosine'])
plt.show()
```



You can read much more about the **plot** function in the documentation.

## Subplots

You can plot different things in the same figure using the **subplot** function. Here is an example:

```
import numpy as np
import matplotlib.pyplot as plt

# Compute the x and y coordinates for points on sine and cosine curves
x = np.arange(0, 3 * np.pi, 0.1)
y_sin = np.sin(x)
y_cos = np.cos(x)

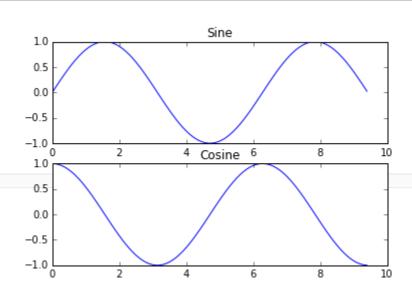
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```

```
# Set up a subplot grid that has height 2 and width 1,
# and set the first such subplot as active.
plt.subplot(2, 1, 1)

# Make the first plot
plt.plot(x, y_sin)
plt.title('Sine')

# Set the second subplot as active, and make the second plot.
plt.subplot(2, 1, 2)
plt.plot(x, y_cos)
plt.title('Cosine')

# Show the figure.
plt.show()
```



You can read much more about the subplot function in the documentation.

### **Images**

You can use the **imshow** function to show images. Here is an example:

```
import numpy as np
from scipy.misc import imread, imresize
import matplotlib.pyplot as plt
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```

```
img = imread('assets/cat.jpg')
img_tinted = img * [1, 0.95, 0.9]

# Show the original image
plt.subplot(1, 2, 1)
plt.imshow(img)

# Show the tinted image
plt.subplot(1, 2, 2)

# A slight gotcha with imshow is that it might give strange results
# if presented with data that is not uint8. To work around this, we
# explicitly cast the image to uint8 before displaying it.
plt.imshow(np.uint8(img_tinted))
plt.show()
```



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