

# Lecture 14: Robot Learning

# So far: Supervised Learning

## Supervised Learning

**Data:**  $(x, y)$

$x$  is data,  $y$  is label

**Goal:** Learn a *function* to map  $x \rightarrow y$

**Examples:** Classification, regression,  
object detection, semantic  
segmentation, image captioning, etc.

Classification



Cat

[This image is CC0 public domain](#)

# So far: Self-Supervised Learning

## Self-Supervised Learning

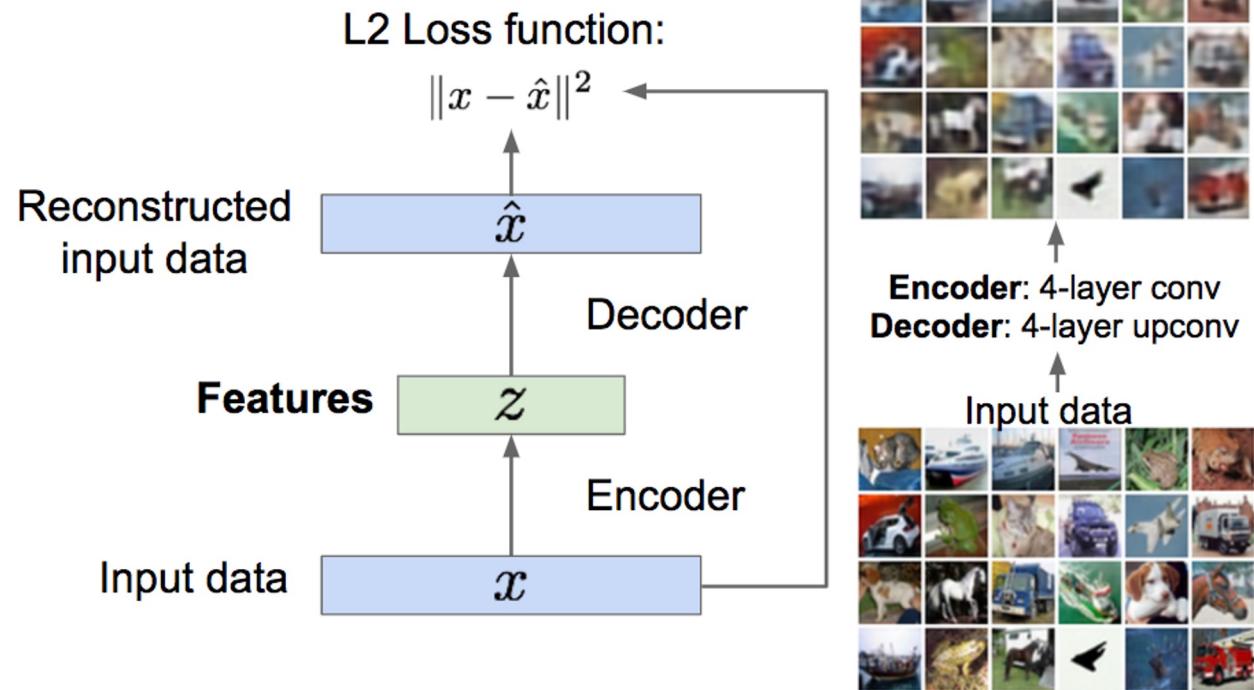
Data:  $x$

Just data, no labels!

**Goal:** Learn some underlying hidden *structure* of the data

**Examples:** Clustering, dimensionality reduction, feature learning, density estimation, etc.

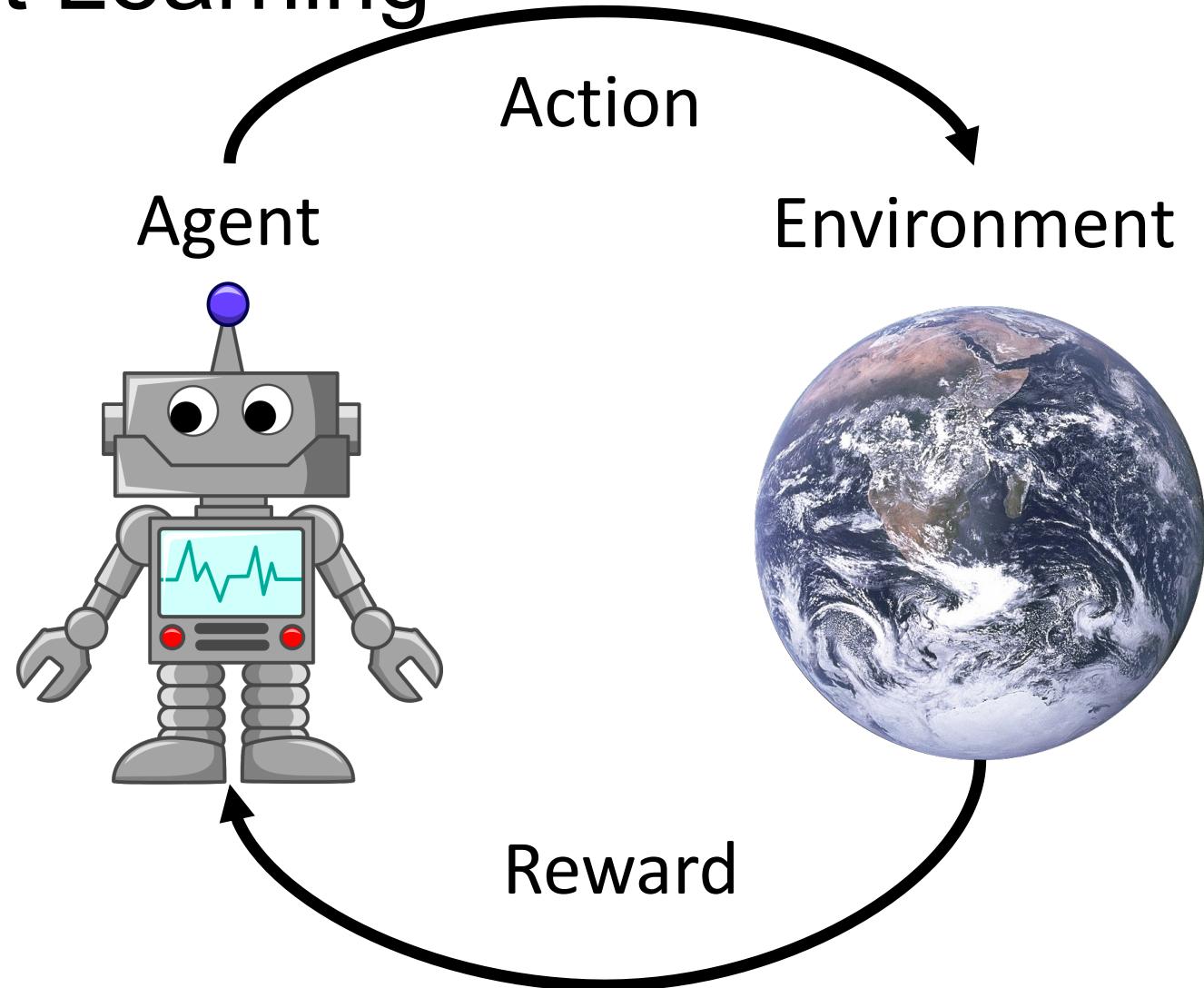
Feature Learning  
(e.g. autoencoders)



# Today: Reinforcement Learning

Problems where an **agent** performs **actions** in **environment**, and receives **rewards**

**Goal:** Learn how to take actions that maximize reward



[Earth photo](#) is in the public domain  
[Robot image](#) is in the public domain

# Overview

- What is reinforcement learning?
- Algorithms for reinforcement learning
  - Q-Learning
  - Policy Gradients
  - Model-based RL and planning

# Reinforcement Learning

Environment

Agent

# Reinforcement Learning

Environment

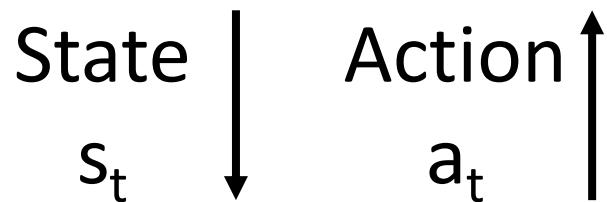
State  
 $s_t$

The agent sees a **state**; may be noisy or incomplete

Agent

# Reinforcement Learning

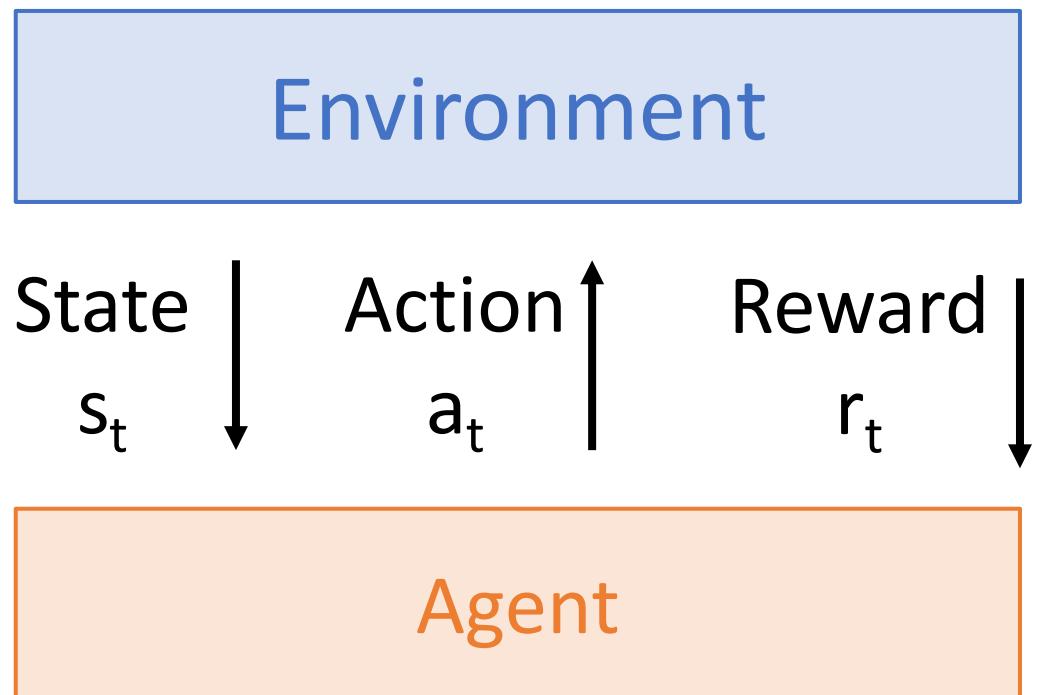
Environment



Agent

The makes an **action** based on what it sees

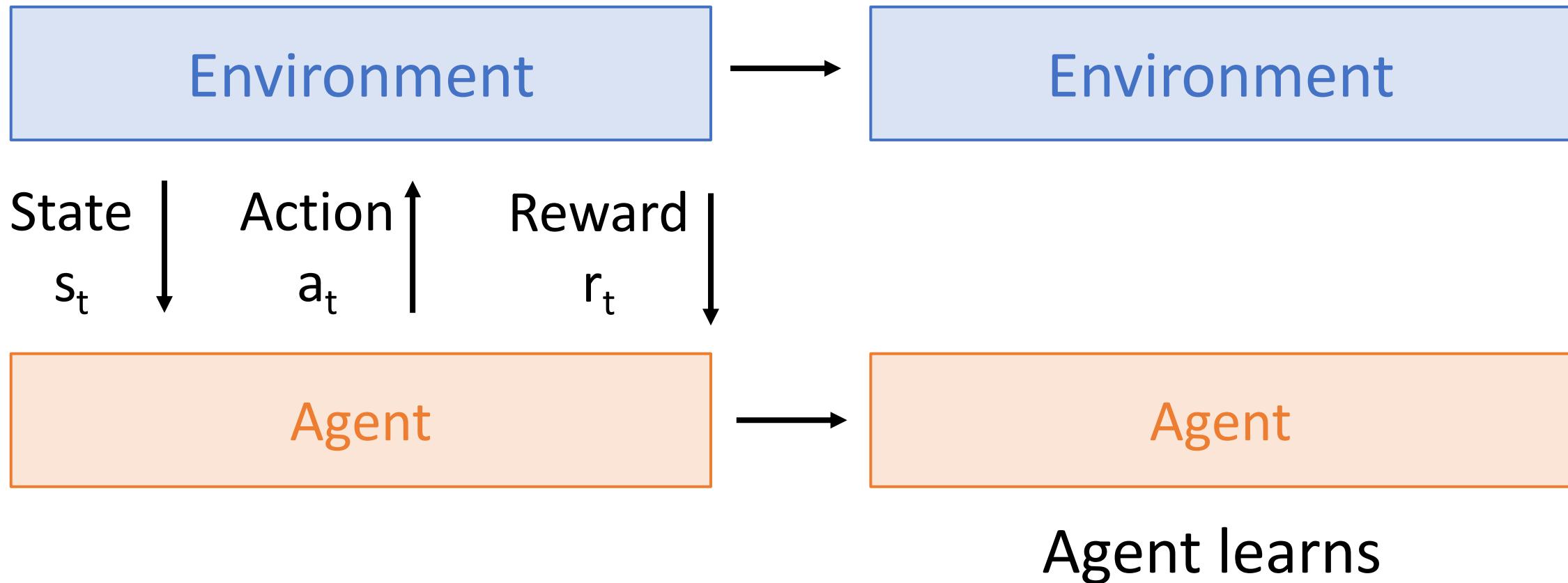
# Reinforcement Learning



**Reward** tells the agent  
how well it is doing

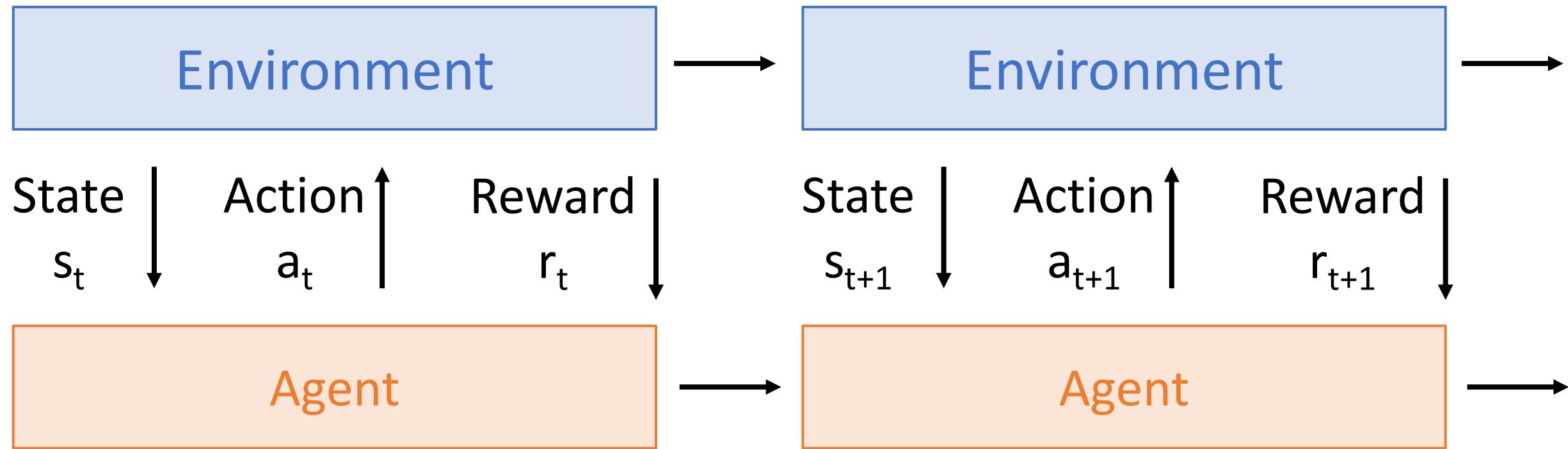
# Reinforcement Learning

Action causes change  
to environment

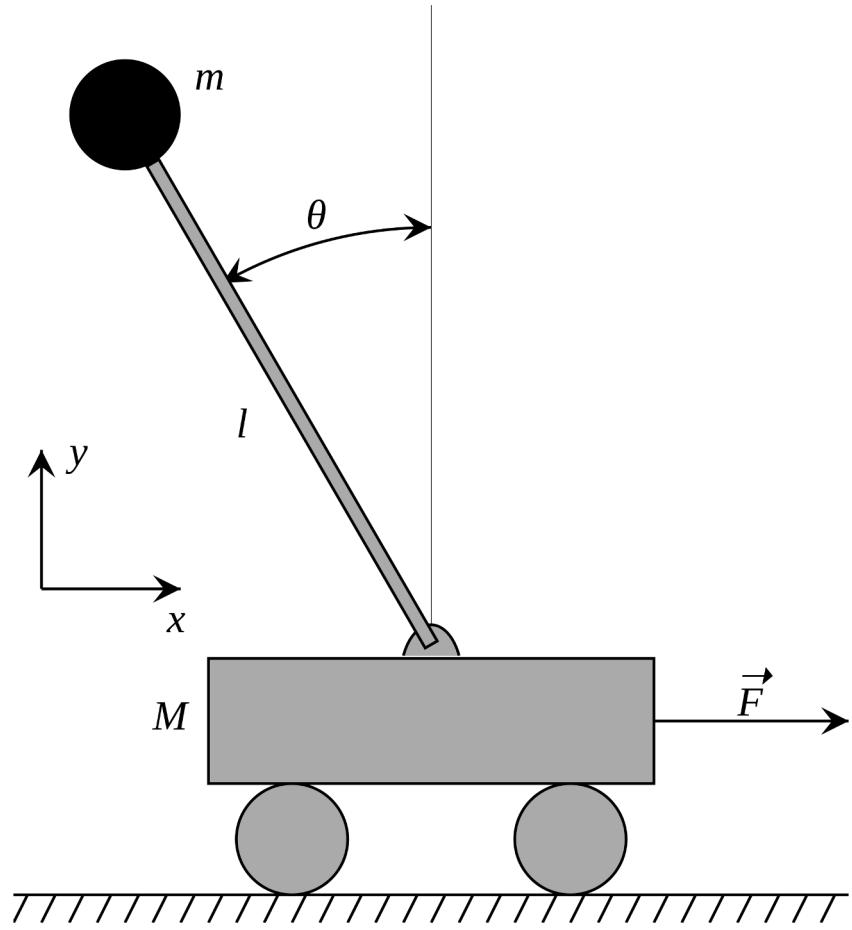


# Reinforcement Learning

Process repeats



# Example: Cart-Pole Problem



**Objective:** Balance a pole on top of a movable cart

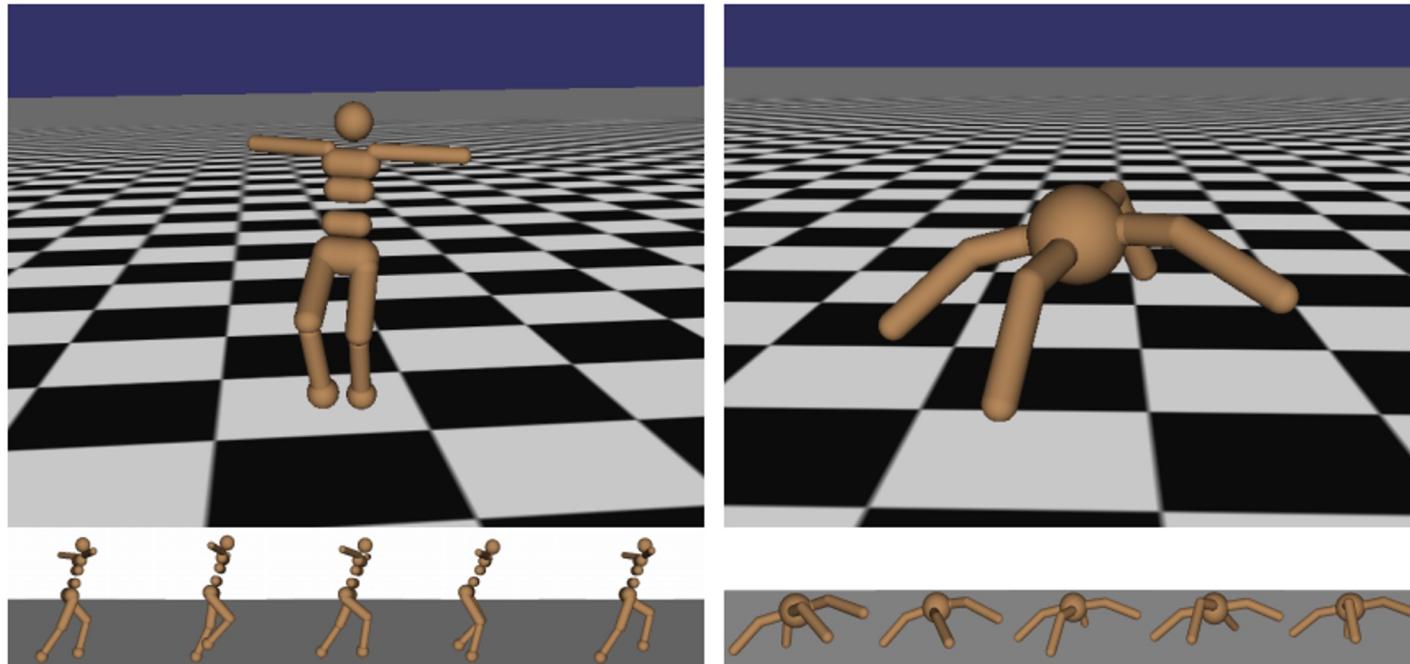
**State:** angle, angular speed, position, horizontal velocity

**Action:** horizontal force applied on the cart

**Reward:** 1 at each time step if the pole is upright

This image is [CC0 public domain](#)

# Example: Robot Locomotion



**Objective:** Make the robot move forward

**State:** Angle, position, velocity of all joints

**Action:** Torques applied on joints

**Reward:** 1 at each time step upright + forward movement

Figure from: Schulman et al, "High-Dimensional Continuous Control Using Generalized Advantage Estimation", ICLR 2016

# Example: Atari Games



**Objective:** Complete the game with the highest score

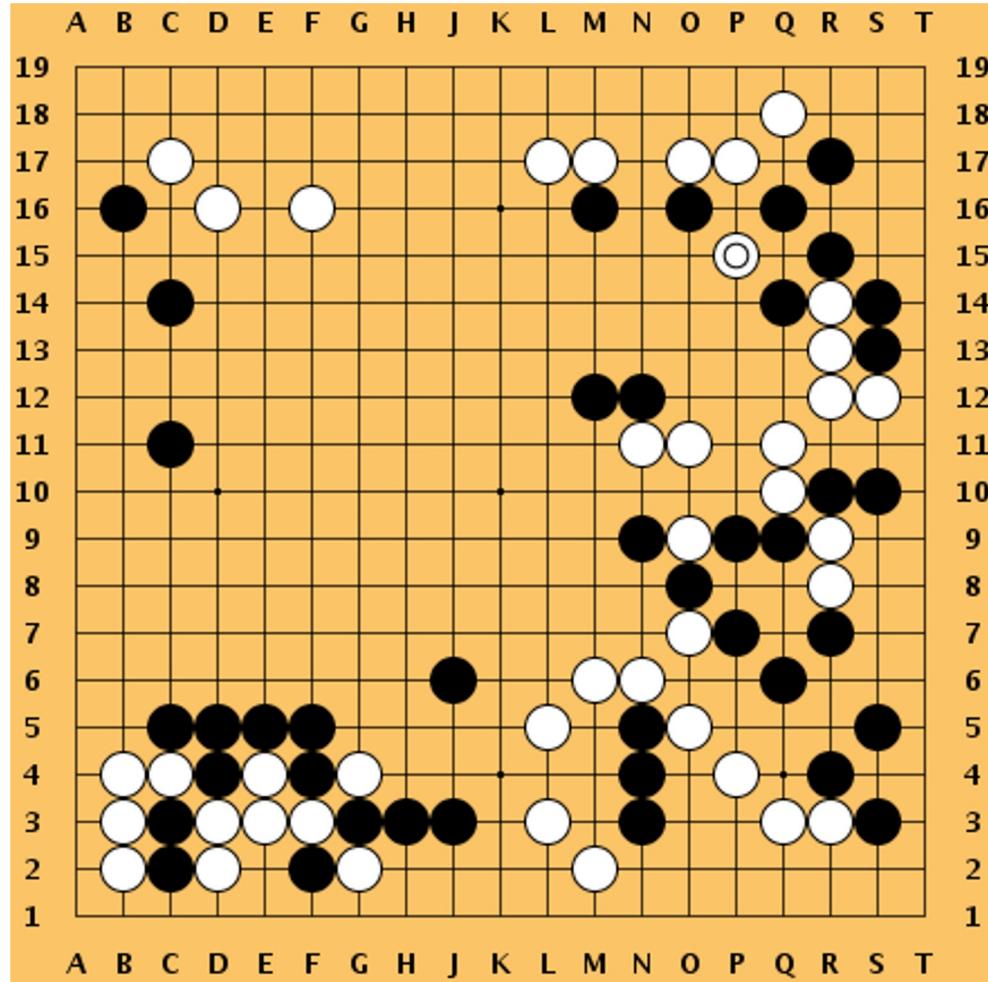
**State:** Raw pixel inputs of the game screen

**Action:** Game controls e.g. Left, Right, Up, Down

**Reward:** Score increase/decrease at each time step

Mnih et al, "Playing Atari with Deep Reinforcement Learning", NeurIPS Deep Learning Workshop, 2013

# Example: Go



**Objective:** Win the game!

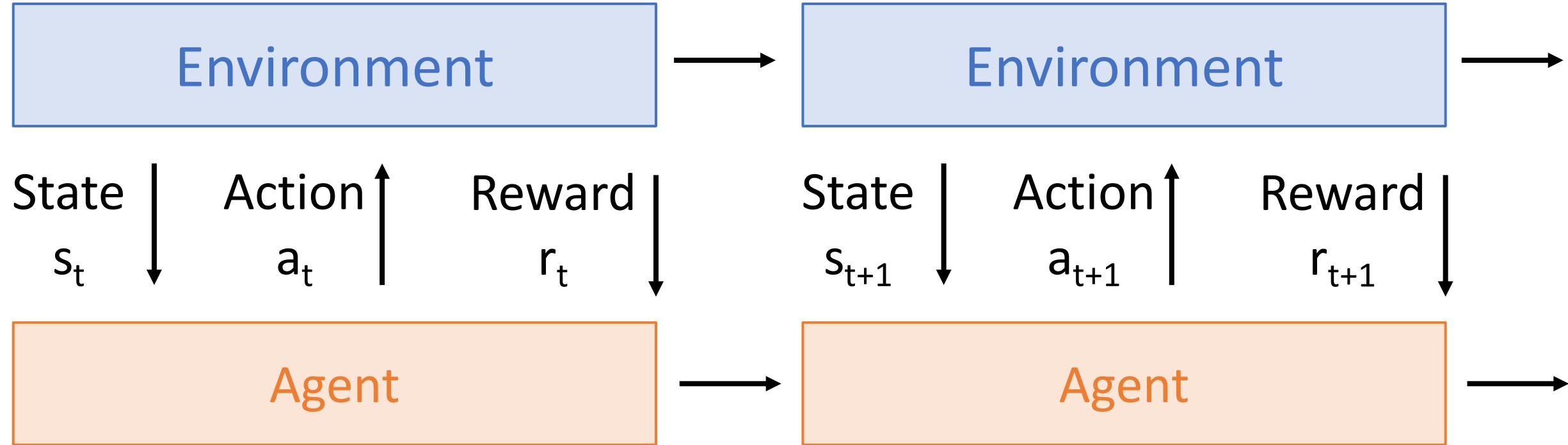
**State:** Position of all pieces

**Action:** Where to put the next piece down

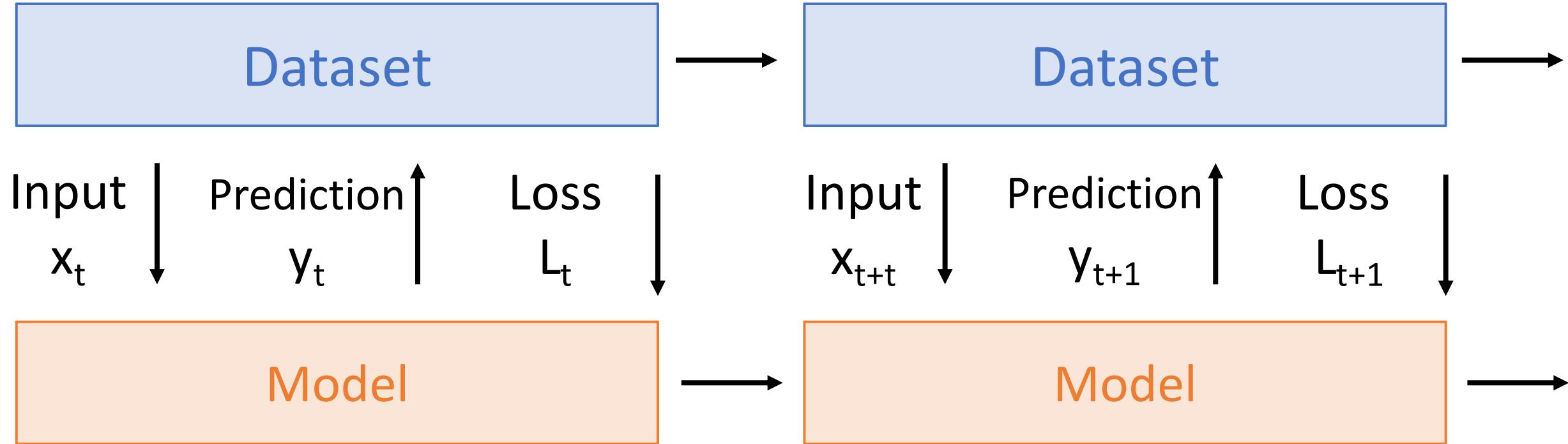
**Reward:** On last turn: 1 if you won, 0 if you lost

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# Reinforcement Learning vs Supervised Learning

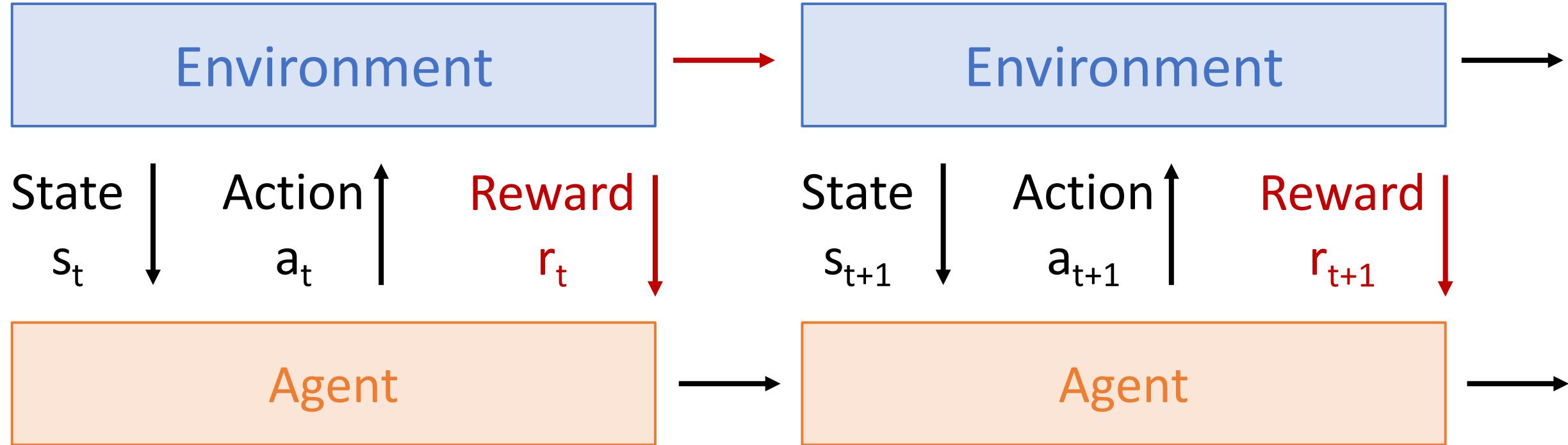


# Reinforcement Learning vs Supervised Learning



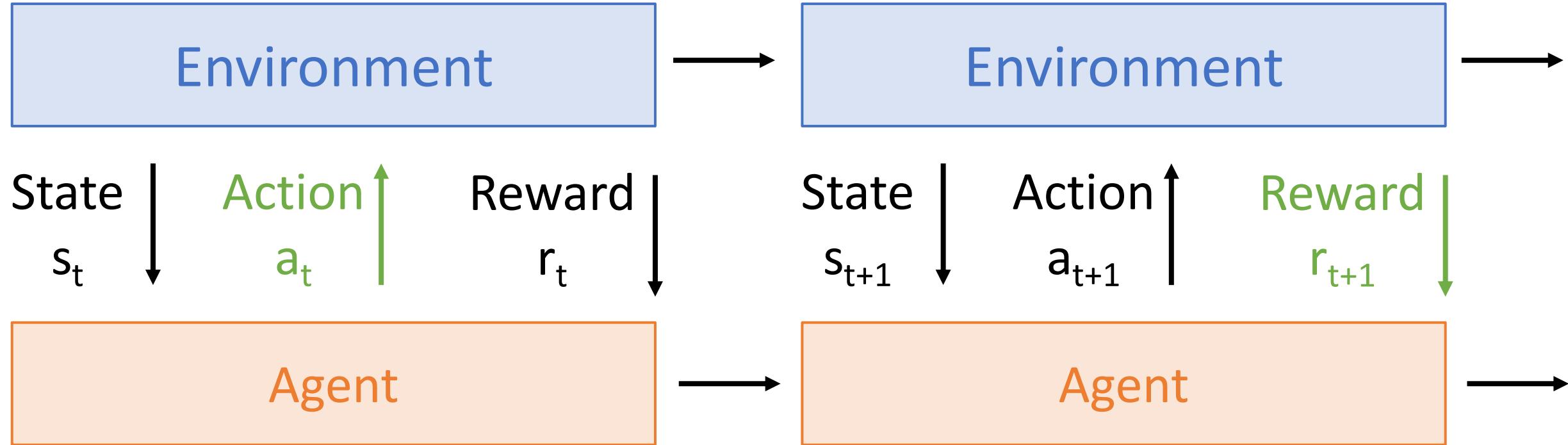
Why is RL different from normal supervised learning?

# Reinforcement Learning vs Supervised Learning



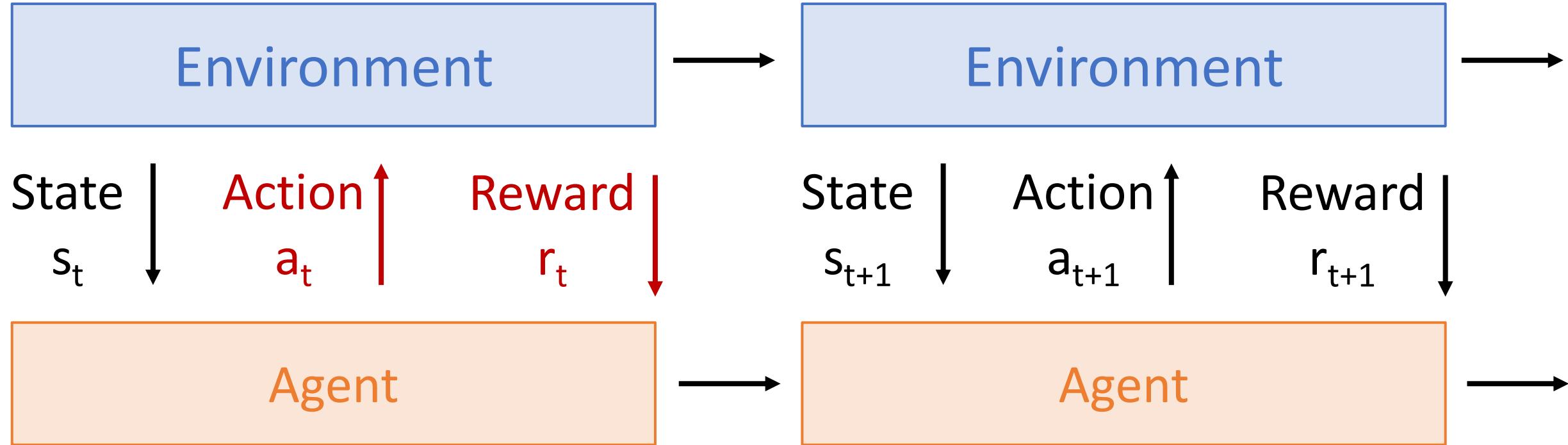
**Stochasticity:** Rewards and state transitions may be random

# Reinforcement Learning vs Supervised Learning



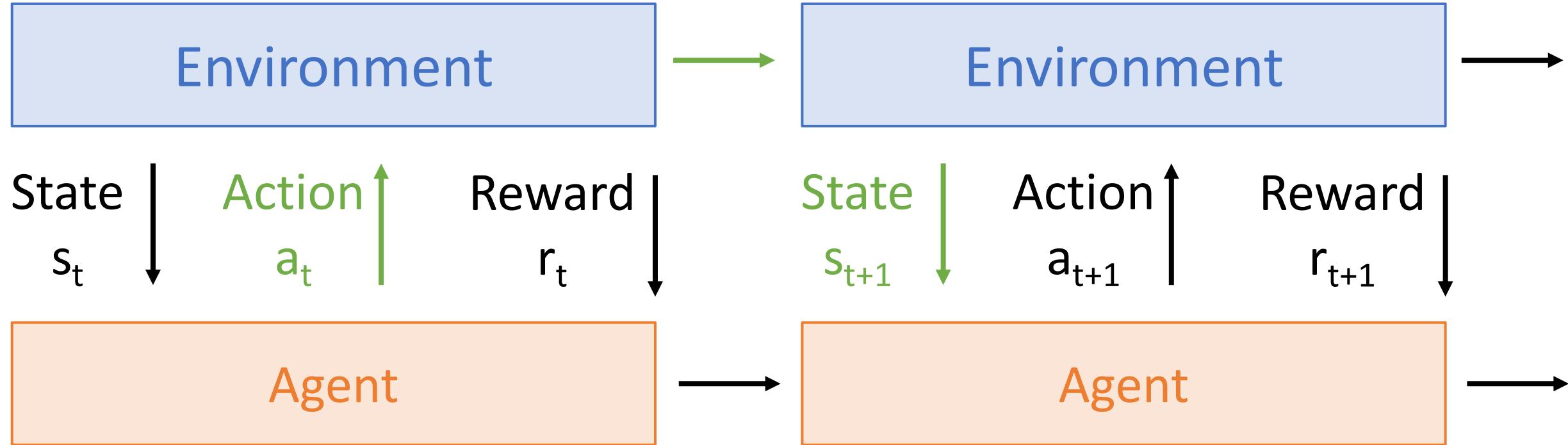
**Credit assignment:** Reward  $r_t$  may not directly depend on action  $a_t$

# Reinforcement Learning vs Supervised Learning



**Nondifferentiable:** Can't backprop through world; can't compute  $dr_t/da_t$

# Reinforcement Learning vs Supervised Learning



**Nonstationary:** What the agent experiences depends on how it acts

# Markov Decision Process (MDP)

Mathematical formalization of the RL problem: A tuple  $(S, A, R, P, \gamma)$

S: Set of possible states

A: Set of possible actions

R: Distribution of reward given (state, action) pair

P: Transition probability: distribution over next state given (state, action)

$\gamma$ : Discount factor (tradeoff between future and present rewards)

**Markov Property:** The current state completely characterizes the state of the world. Rewards and next states depend only on current state, not history.

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**Goal:** Find policy  $\pi^*$  that maximizes cumulative discounted reward:  $\sum_t \gamma^t r_t$

# Markov Decision Process (MDP)

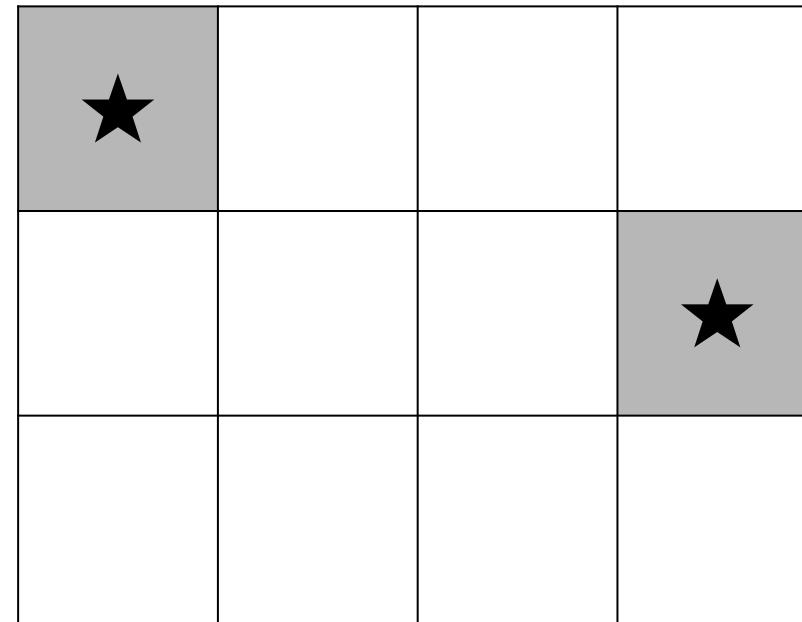
- At time step  $t=0$ , environment samples initial state  $s_0 \sim p(s_0)$
- Then, for  $t=0$  until done:
  - Agent selects action  $a_t \sim \pi(a | s_t)$
  - Environment samples reward  $r_t \sim R(r | s_t, a_t)$
  - Environment samples next state  $s_{t+1} \sim P(s | s_t, a_t)$
  - Agent receives reward  $r_t$  and next state  $s_{t+1}$

# A simple MDP: Grid World

## Actions:

1. Right
2. Left
3. Up
4. Down

## States



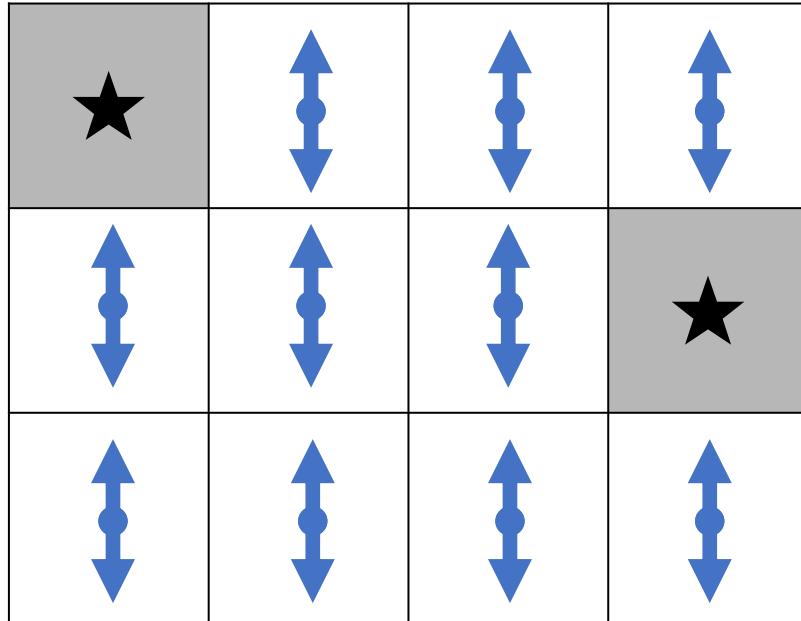
## Reward

Set a negative “reward” for each transition  
(e.g.  $r = -1$ )

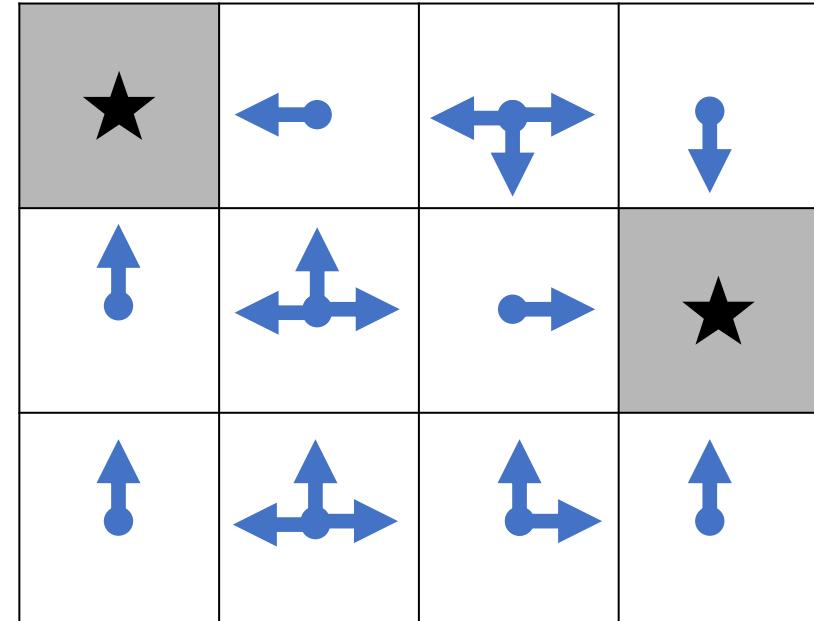
**Objective:** Reach one of the terminal states in as few moves as possible

# A simple MDP: Grid World

**Bad policy**



**Optimal Policy**



# Finding Optimal Policies

**Goal:** Find the optimal policy  $\pi^*$  that maximizes (discounted) sum of rewards.

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**Solution:** Maximize the expected sum of rewards

$$\pi^* = \arg \max_{\pi} \mathbb{E} \left[ \sum_{t \geq 0} \gamma^t r_t \mid \pi \right]$$

$$\begin{aligned} s_0 &\sim p(s_0) \\ a_t &\sim \pi(a \mid s_t) \\ s_{t+1} &\sim P(s \mid s_t, a_t) \end{aligned}$$

# Value Function and Q Function

Following a policy  $\pi$  produces **sample trajectories** (or paths)  $s_0, a_0, r_0, s_1, a_1, r_1, \dots$

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How good is a state? The **value function** at state  $s$ , is the expected cumulative reward from following the policy from state  $s$ :

$$V^\pi(s) = \mathbb{E} \left[ \sum_{t \geq 0} \gamma^t r_t \mid s_0 = s, \pi \right]$$

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**How good is a state-action pair?** The **Q function** at state  $s$  and action  $a$ , is the expected cumulative reward from taking action  $a$  in state  $s$  and then following the policy:

$$Q^\pi(s, a) = \mathbb{E} \left[ \sum_{t \geq 0} \gamma^t r_t \mid s_0 = s, a_0 = a, \pi \right]$$

# Bellman Equation

**Optimal Q-function:**  $Q^*(s, a)$  is the Q-function for the optimal policy  $\pi^*$   
It gives the max possible future reward when taking action  $a$  in state  $s$ :

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**Intuition:** After taking action  $a$  in state  $s$ , we get reward  $r$  and move to a new state  $s'$ . After that, the max possible reward we can get is  $\max_{a'} Q^*(s', a')$

# Solving for the optimal policy: Value Iteration

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$$Q_{i+1}(s, a) = \mathbb{E}_{r, s'} \left[ r + \gamma \max_{a'} Q_i(s', a') \right]$$

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**Solution:** Approximate  $Q(s, a)$  with a neural network, use Bellman Equation as loss!

# Solving for the optimal policy: Deep Q-Learning

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Use the Bellman Equation to tell what  $Q$  should output for a given state and action:

$$y_{s,a,\theta} = \mathbb{E}_{r,s'} \left[ r + \gamma \max_{a'} Q(s', a'; \theta) \right]$$

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**Problem:** How to sample batches of data for training?

# Case Study: Playing Atari Games



**Objective:** Complete the game with the highest score

**State:** Raw pixel inputs of the game screen

**Action:** Game controls e.g. Left, Right, Up, Down

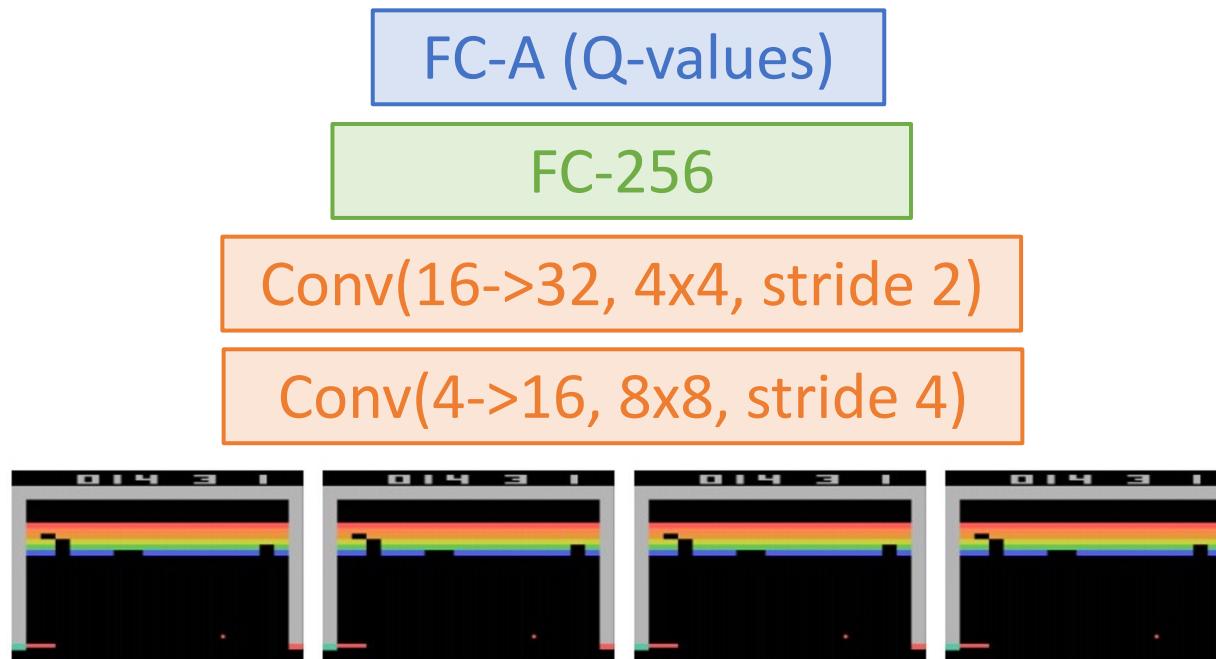
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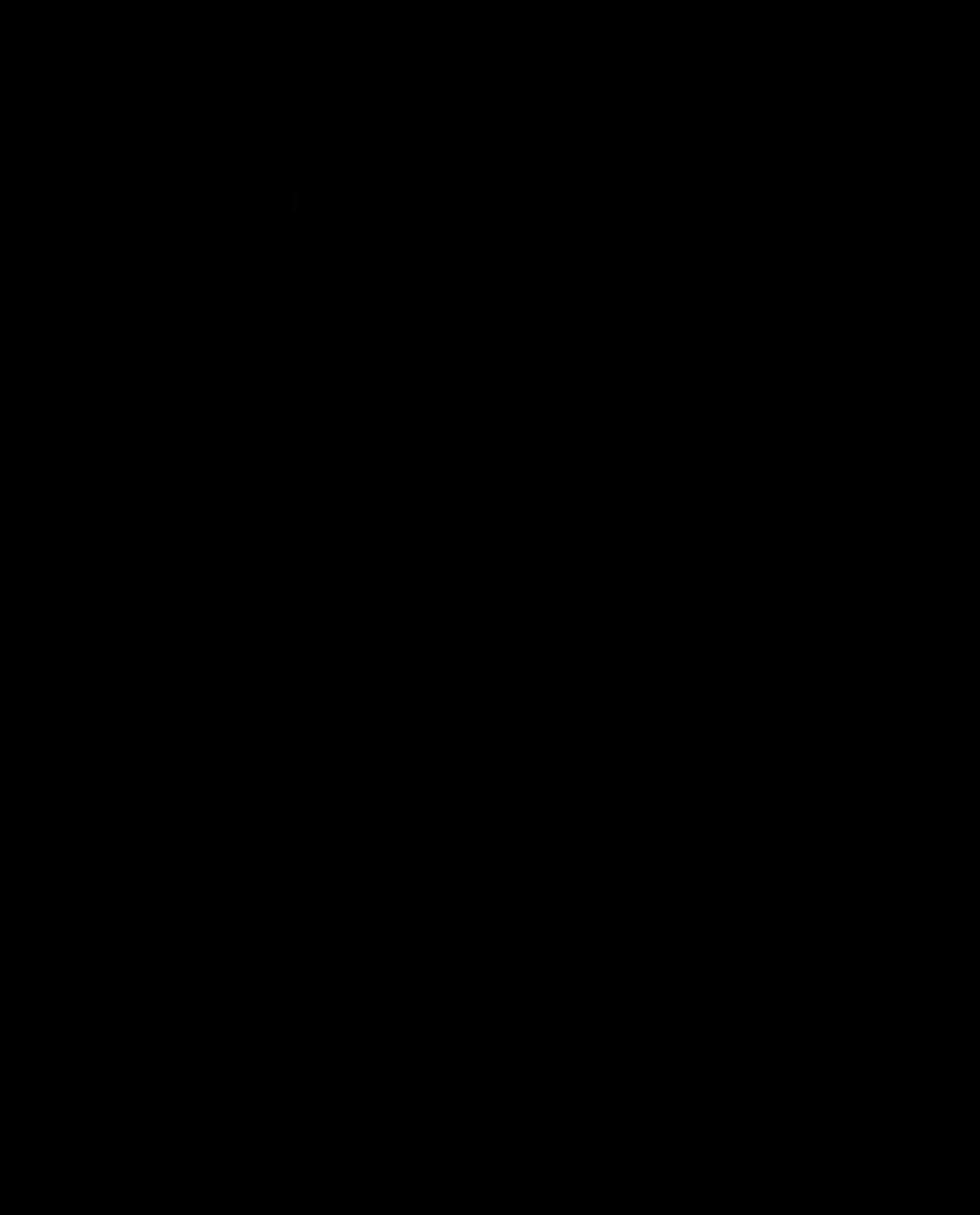
$Q(s, a; \theta)$   
Neural network  
with weights  $\theta$

**Network output:**  
Q-values for all actions



With 4 actions: last  
layer gives values  
 $Q(s_t, a_1), Q(s_t, a_2),$   
 $Q(s_t, a_3), Q(s_t, a_4)$

**Network input: state  $s_t$ : 4x84x84 stack of last 4 frames**  
(after RGB->grayscale conversion, downsampling, and cropping)



<https://www.youtube.com/watch?v=V1eYniJ0Rnk>

# Q-Learning

**Q-Learning:** Train network  $Q_\theta(s, a)$  to estimate future rewards for every (state, action) pair

**Problem:** For some problems this can be a hard function to learn.

For some problems it is easier to learn a mapping from states to actions

# Q-Learning vs Policy Gradients

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**Objective function:** Expected future rewards when following policy  $\pi_\theta$ :

$$J(\theta) = \mathbb{E}_{r \sim p_\theta} \left[ \sum_{t \geq 0} \gamma^t r_t \right]$$

Find the optimal policy by maximizing:  $\theta^* = \arg \max_{\theta} J(\theta)$  **(Use gradient ascent!)**

# Policy Gradients

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**Problem:** Nondifferentiability! Don't know how to compute  $\frac{\partial J}{\partial \theta}$

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**Objective function:** Expected future rewards when following policy  $\pi_\theta$ :

$$J(\theta) = \mathbb{E}_{r \sim p_\theta} \left[ \sum_{t \geq 0} \gamma^t r_t \right]$$

Find the optimal policy by maximizing:  $\theta^* = \arg \max_{\theta} J(\theta)$  **(Use gradient ascent!)**

**Problem:** Nondifferentiability! Don't know how to compute  $\frac{\partial J}{\partial \theta}$

**General formulation:**  $J(\theta) = \mathbb{E}_{x \sim p_\theta}[f(x)]$  Want to compute  $\frac{\partial J}{\partial \theta}$

# Policy Gradients: REINFORCE Algorithm

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$$\frac{\partial}{\partial \theta} \log p_\theta(x)$$

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Approximate the expectation via sampling!

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Sequence of states  
and actions when  
following policy  $\pi_\theta$

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Reward we get from  
state sequence x

$$\frac{\partial J}{\partial \theta} = \mathbb{E}_{x \sim p_\theta} \left[ f(x) \sum_{t \geq 0} \frac{\partial}{\partial \theta} \log \pi_\theta(a_t | s_t) \right]$$

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Gradient of predicted action scores with respect to model weights. Backprop through model  $\pi_\theta$ !

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1. Initialize random weights  $\theta$

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1. Initialize random weights  $\theta$
2. Collect trajectories  $x$  and rewards  $f(x)$  using policy  $\pi_\theta$
3. Compute  $dJ/d\theta$

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1. Initialize random weights  $\theta$
2. Collect trajectories  $x$  and rewards  $f(x)$  using policy  $\pi_\theta$
3. Compute  $dJ/d\theta$
4. Gradient ascent step on  $\theta$
5. GOTO 2

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**Intuition:**

When  $f(x)$  is high: Increase the probability of the actions we took.

When  $f(x)$  is low: Decrease the probability of the actions we took.

# So far: Q-Learning and Policy Gradients

**Q-Learning:** Train network  $Q_\theta(s, a)$  to estimate future rewards for every (state, action) pair

Use Bellman Equation to define loss function for training Q:

$$y_{s,a,\theta} = \mathbb{E}_{r,s'} \left[ r + \gamma \max_{a'} Q(s', a'; \theta) \right] \quad \text{Where } r \sim R(s, a), s' \sim P(s, a)$$
$$L(s, a) = (Q(s, a; \theta) - y_{s,a,\theta})^2$$

**Policy Gradients:** Train a network  $\pi_\theta(a | s)$  that takes state as input, gives distribution over which action to take in that state. Use REINFORCE Rule for computing gradients:

$$J(\theta) = \mathbb{E}_{x \sim p_\theta}[f(x)] \quad \frac{\partial J}{\partial \theta} = \mathbb{E}_{x \sim p_\theta} \left[ f(x) \sum_{t \geq 0} \frac{\partial}{\partial \theta} \log \pi_\theta(a_t | s_t) \right]$$

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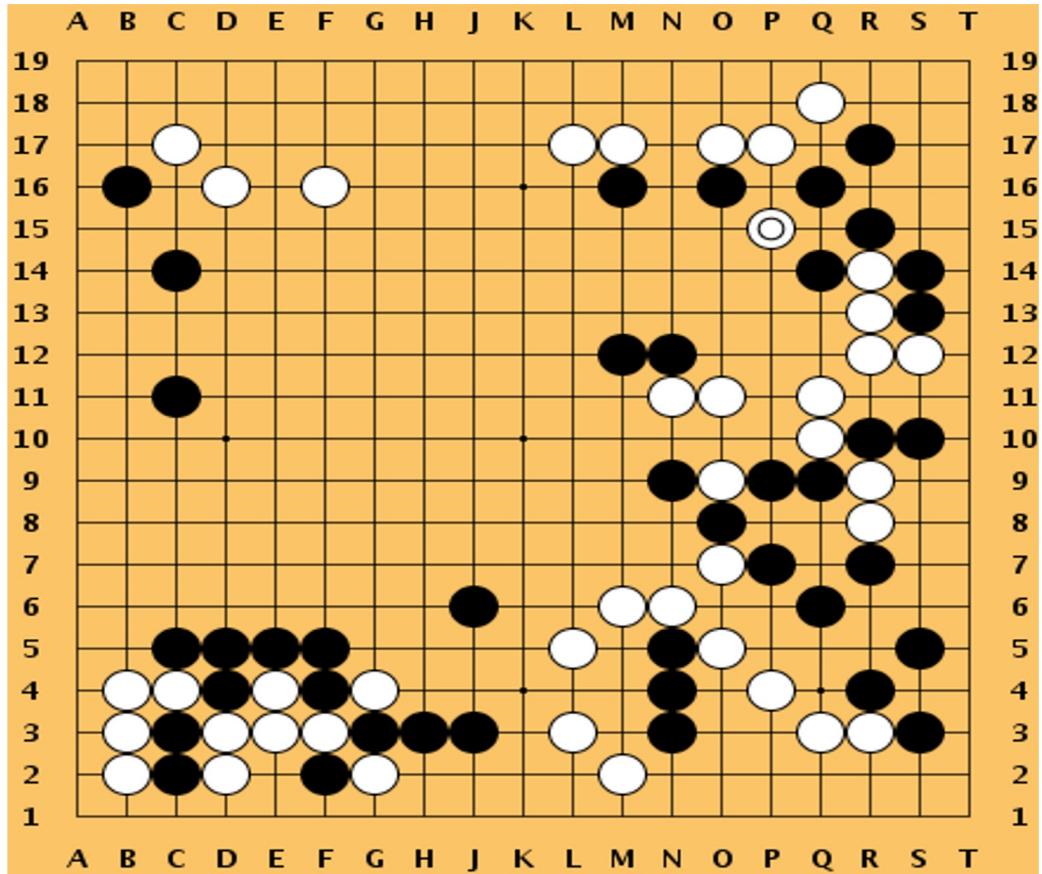
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Improving policy gradients: Add **baseline** to reduce variance of gradient estimator

# Case Study: Playing Games

## AlphaGo: (January 2016)

- Used imitation learning + tree search + RL
- Beat 18-time world champion Lee Sedol



Silver et al, "Mastering the game of Go with deep neural networks and tree search", Nature 2016

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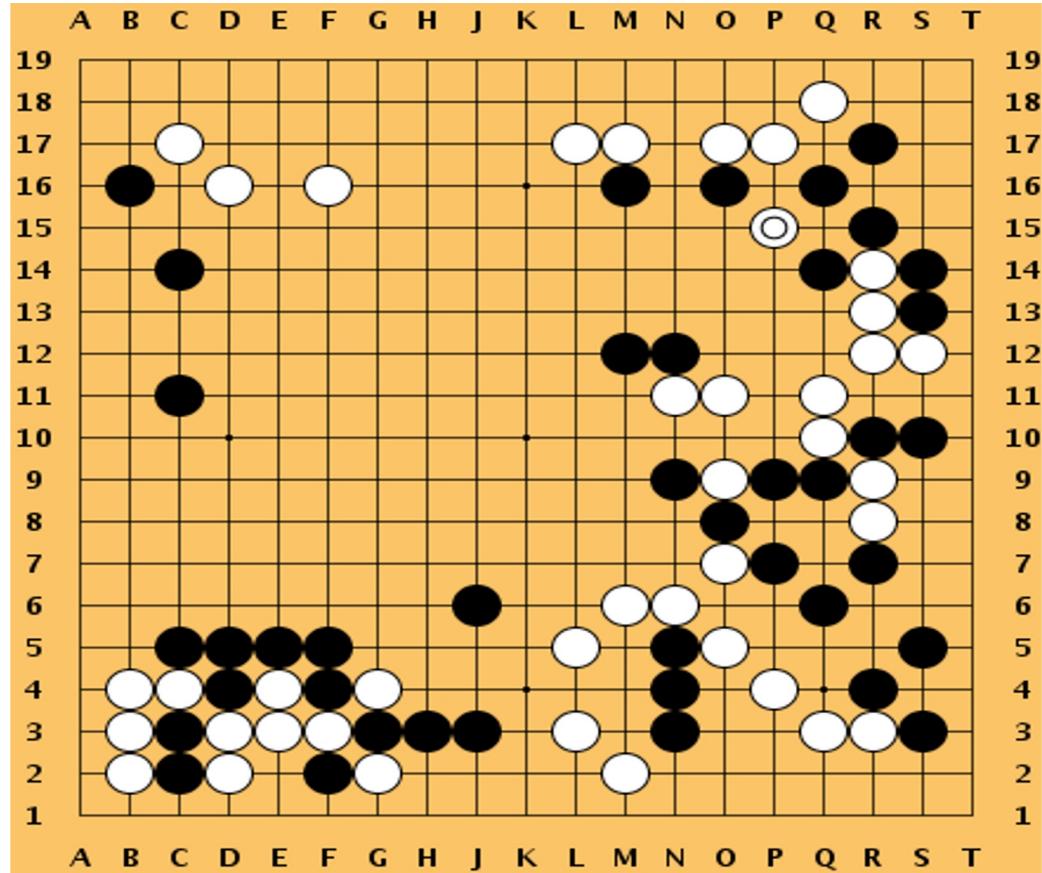
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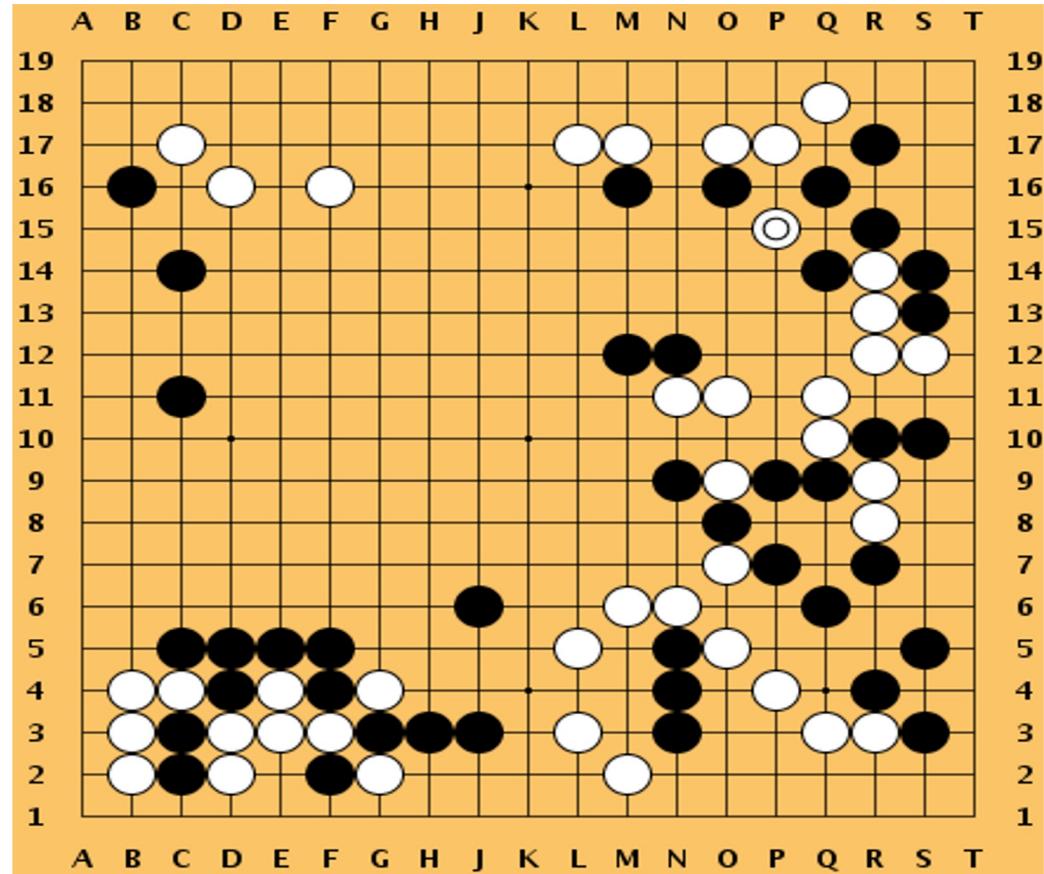
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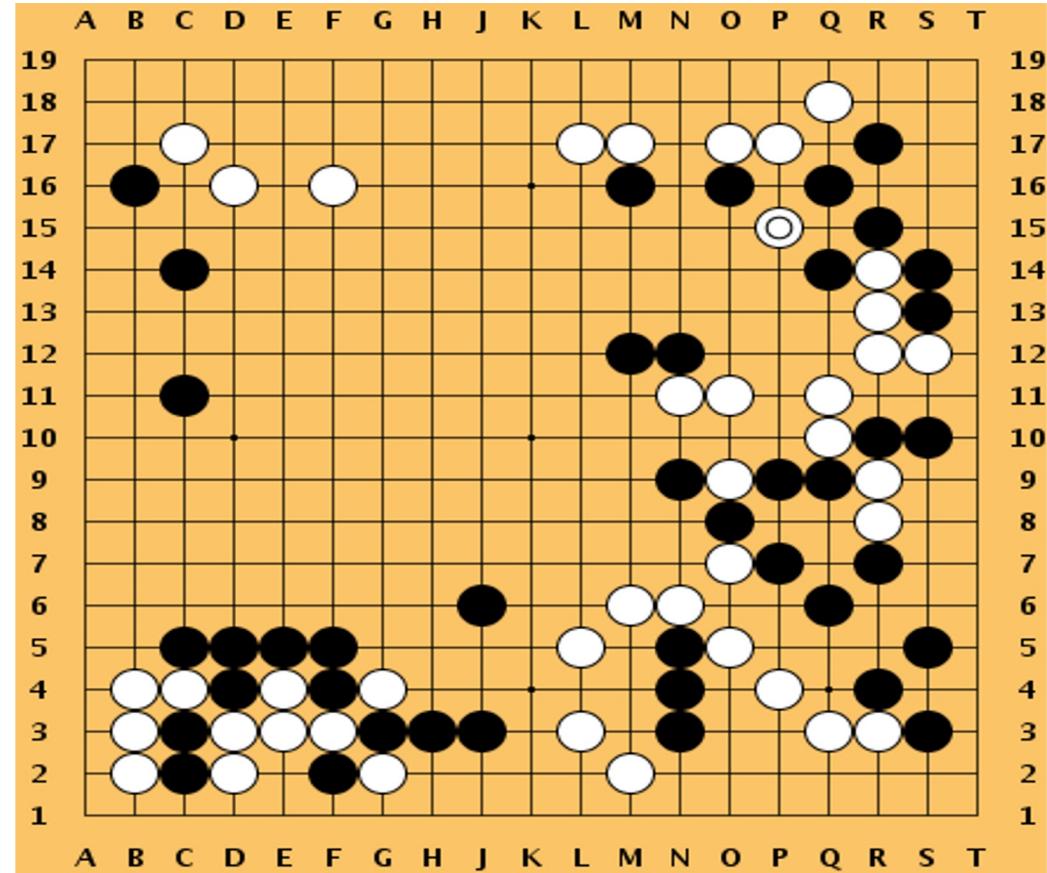
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November 2019: Lee Sedol announces retirement

"With the debut of AI in Go games, I've realized that I'm not at the top even if I become the number one through frantic efforts"

"Even if I become the number one, there is an entity that cannot be defeated"

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Quotes from: <https://en.yna.co.kr/view/AEN20191127004800315>  
[Image of Lee Sedol](#) is licensed under [CC BY 2.0](#)

# More Complex Games

**StarCraft II: AlphaStar**

(October 2019)

Vinyals et al, “Grandmaster level in StarCraft II using multi-agent reinforcement learning”, Science 2018

**Dota 2: OpenAI Five (April 2019)**

No paper, only a blog post:

<https://openai.com/five/#how-openai-five-works>

# Problems of Model-Free RL

- Learns from trials and error
- Require extensive interactions

**AlphaGo Zero: Google DeepMind  
supercomputer learns 3,000 years of human  
knowledge in 40 days**

# Problems of Model-Free RL

- Learns from trials and error
- Require extensive interactions
- Safety concerns
- Limited interpretability
  - What if things go wrong?



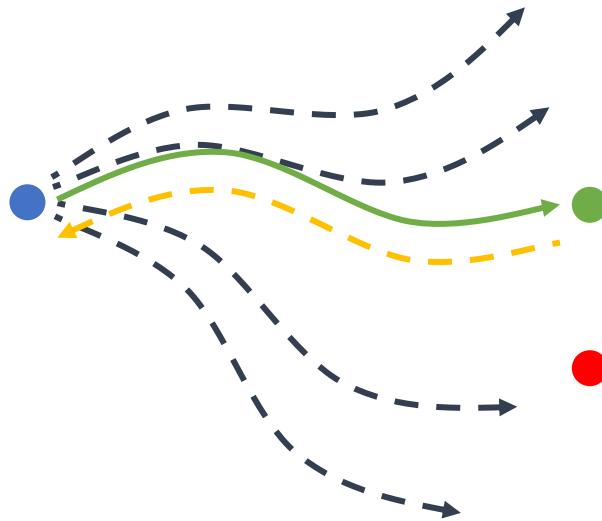
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- Safety concerns
- Limited interpretability
  - What if things go wrong?
- Humans maintain an intuitive model of the world
  - Widely applicable
  - Sample efficient



# Model-Based RL

**Model-Based:** Learn a model of the world's state transition function  $P(s_{t+1}|s_t, a_t)$  and then use planning through the model to make decisions



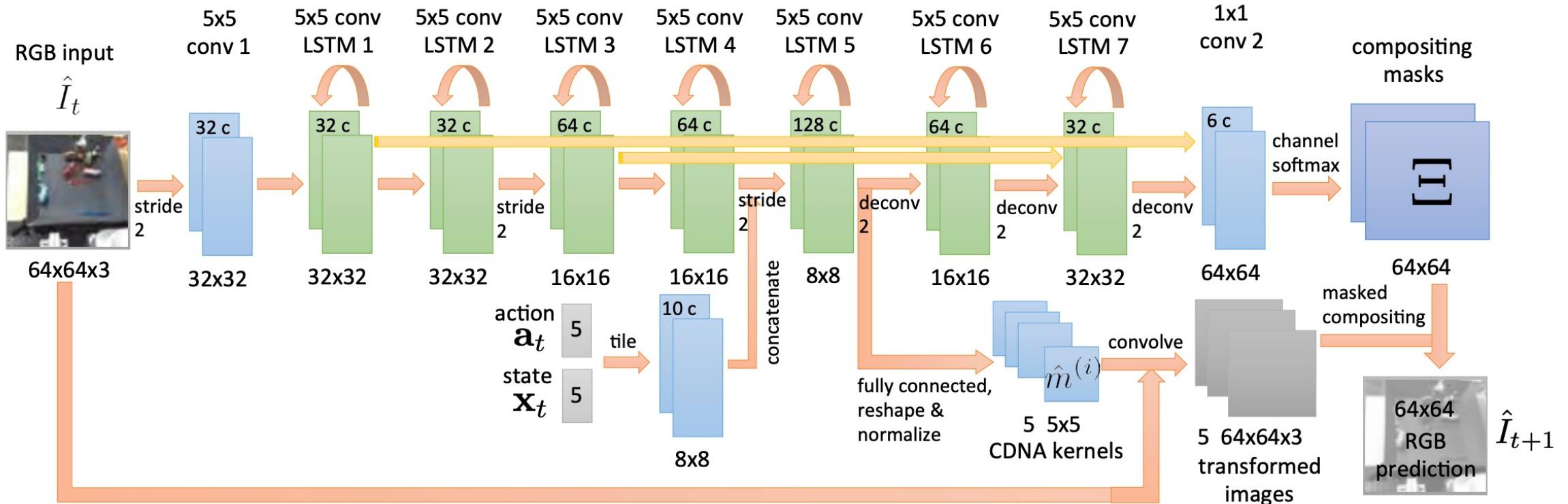
Model might not be accurate enough.

1. Execute the first action
2. Obtain new state
3. Re-optimize the action sequence using gradient descent

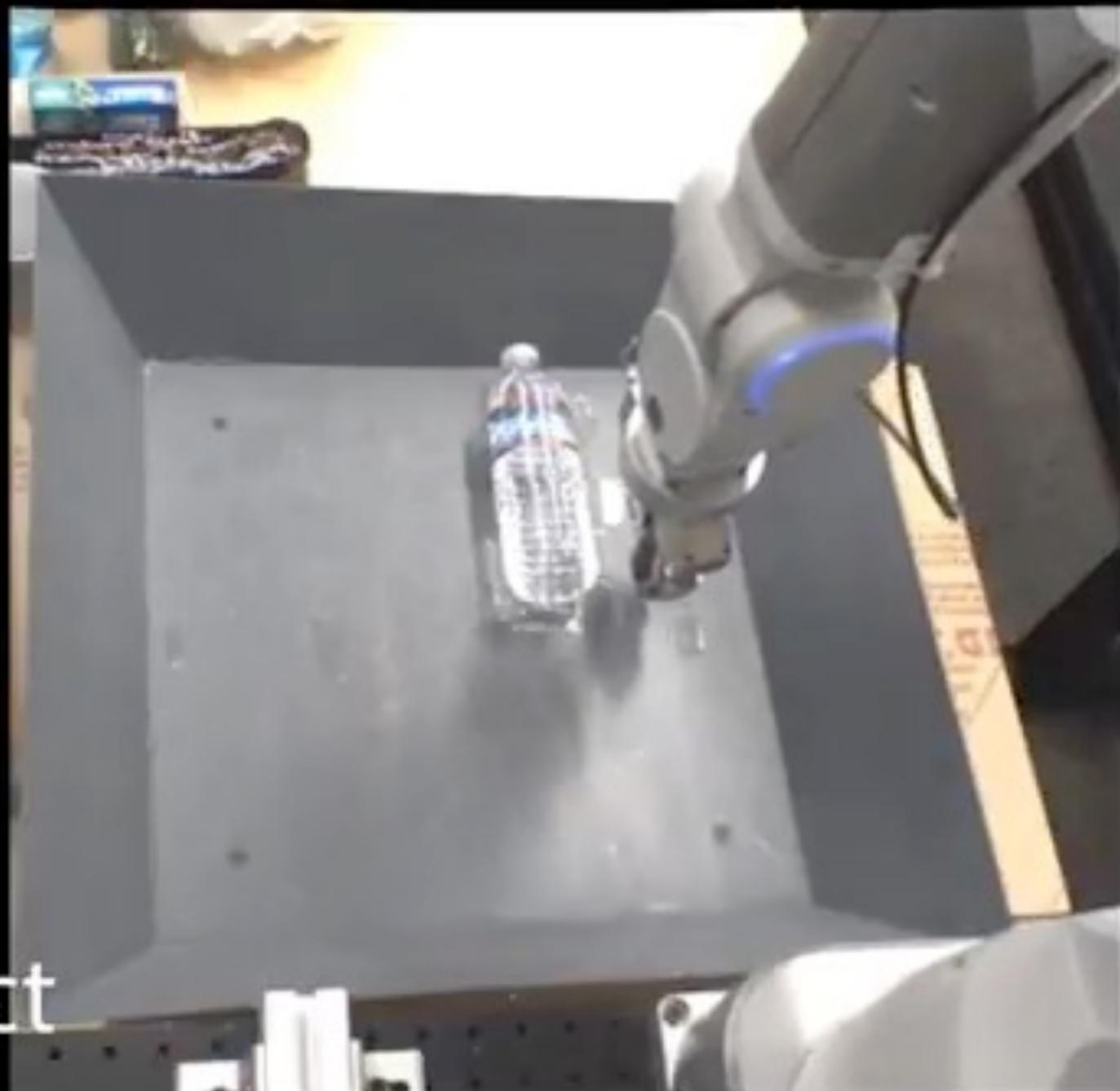
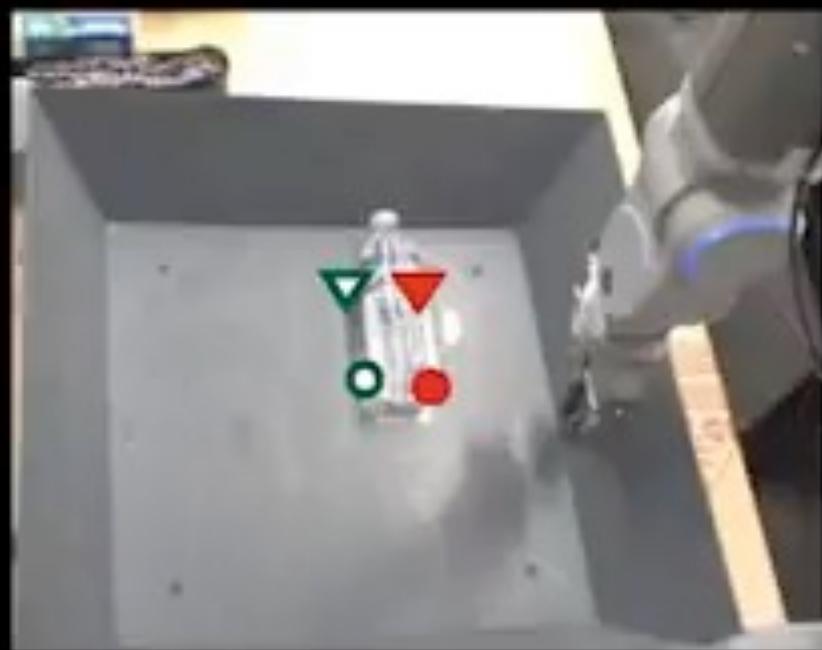
**Key:** GPU for parallel sampling / gradient descent

**Key question:** what should be the form of  $s_t$ ?

# Pixel Dynamics - Deep Visual Foresight

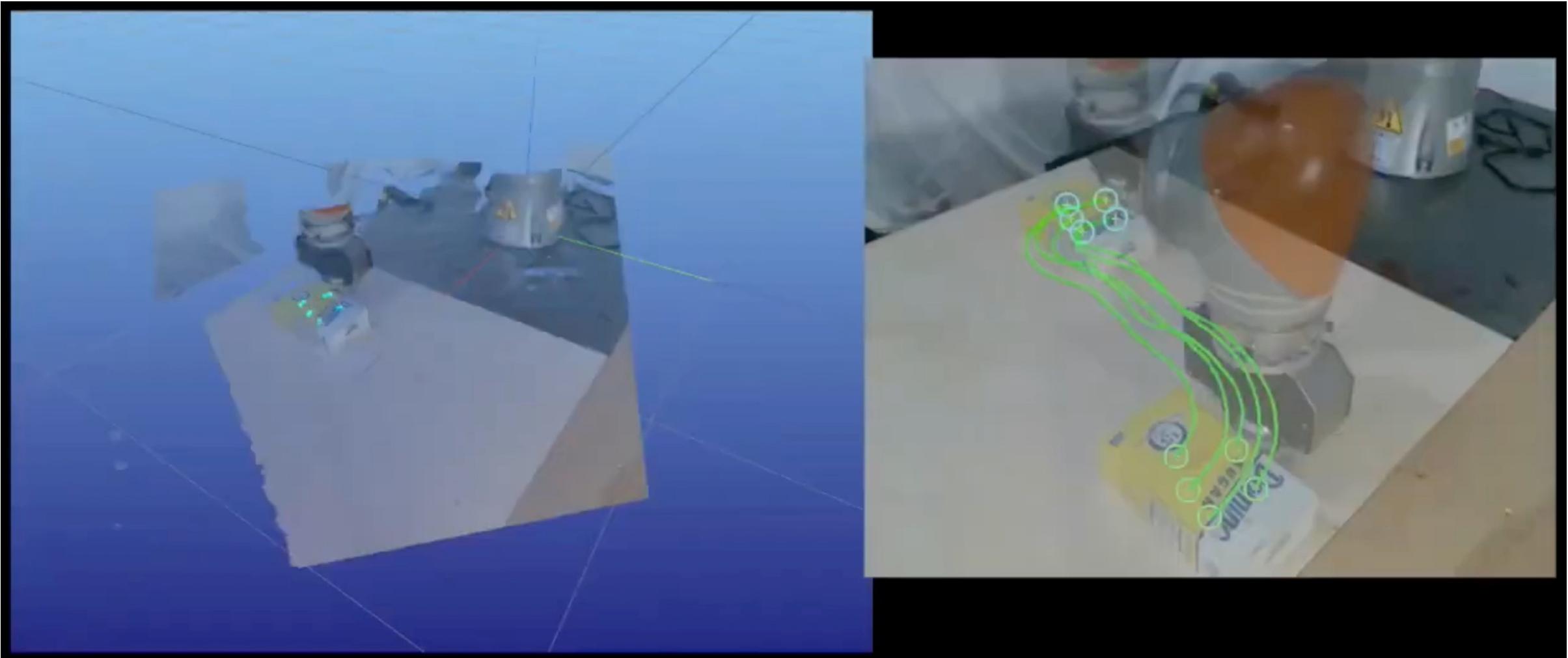


Finn and Levine, "Deep Visual Foresight for Planning Robot Motion", ICRA 2017



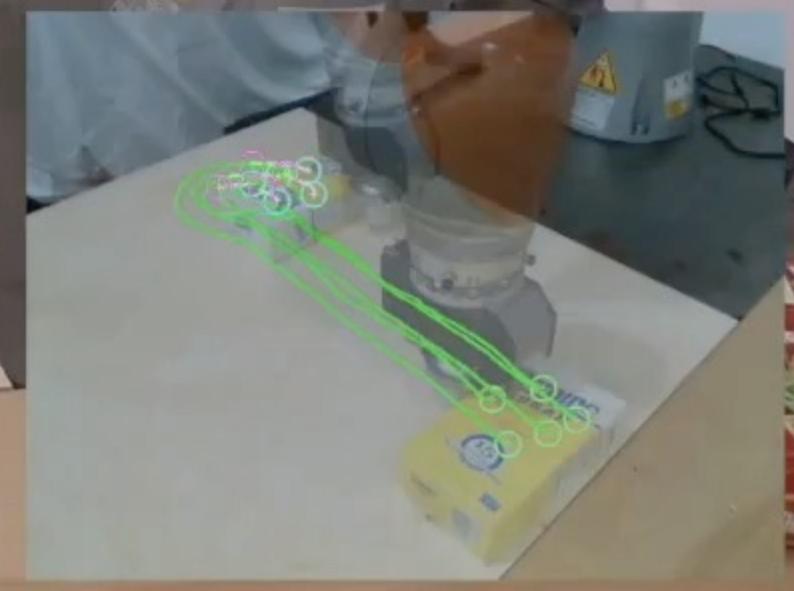
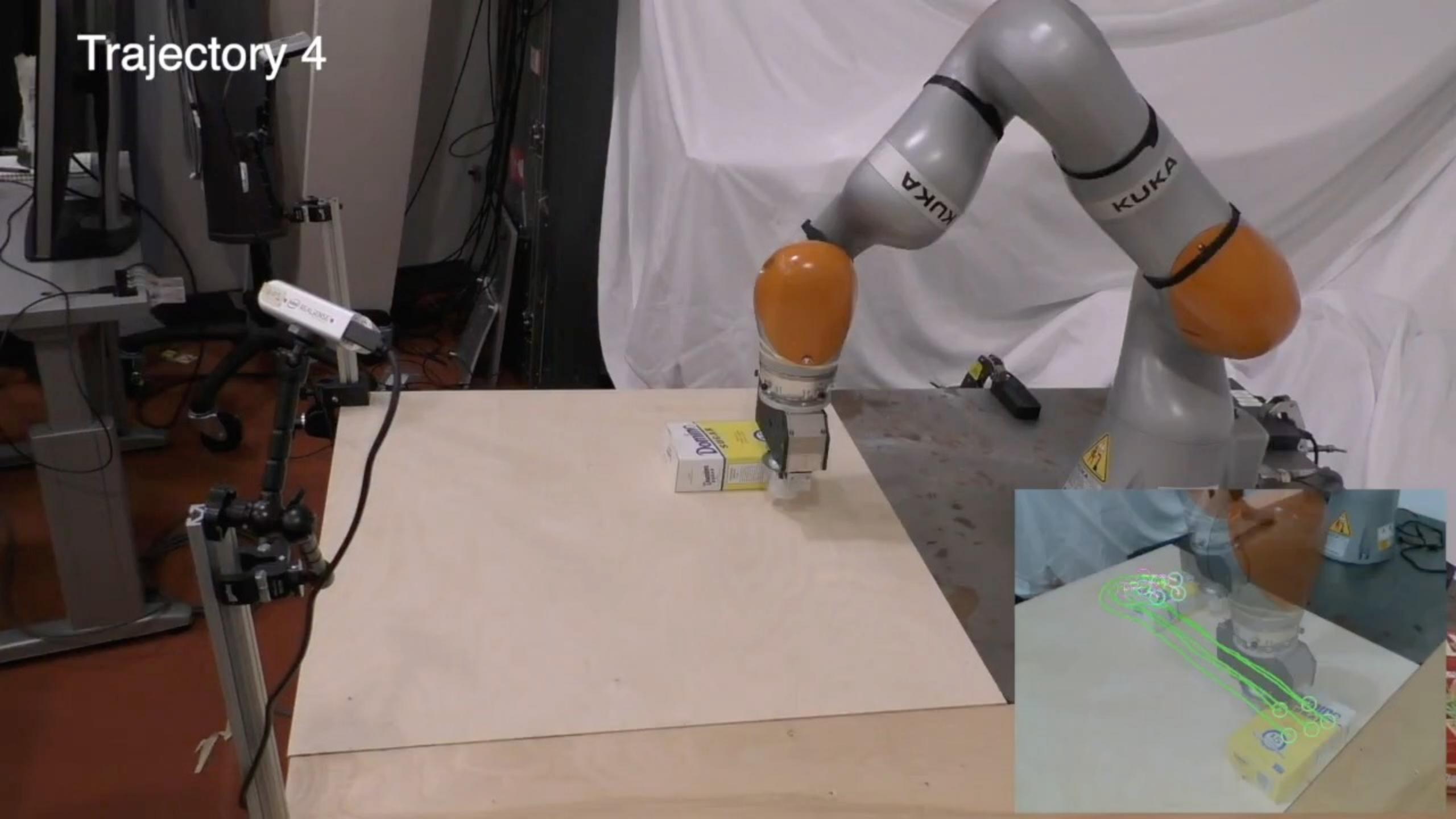
transparent object

# Keypoint Dynamics

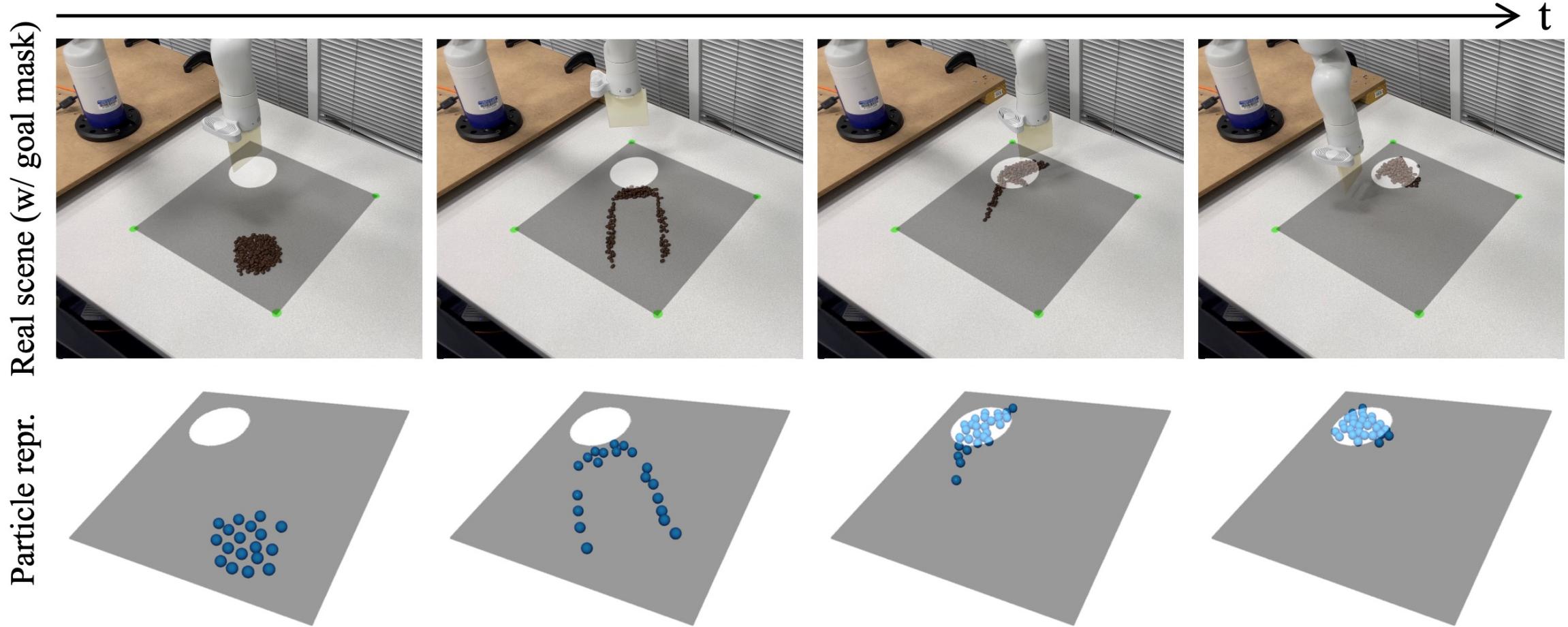


Manuelli, Li, Florence, Tedrake, "Keypoints into the Future: Self-Supervised Correspondence in Model-Based Reinforcement Learning", CoRL 2020

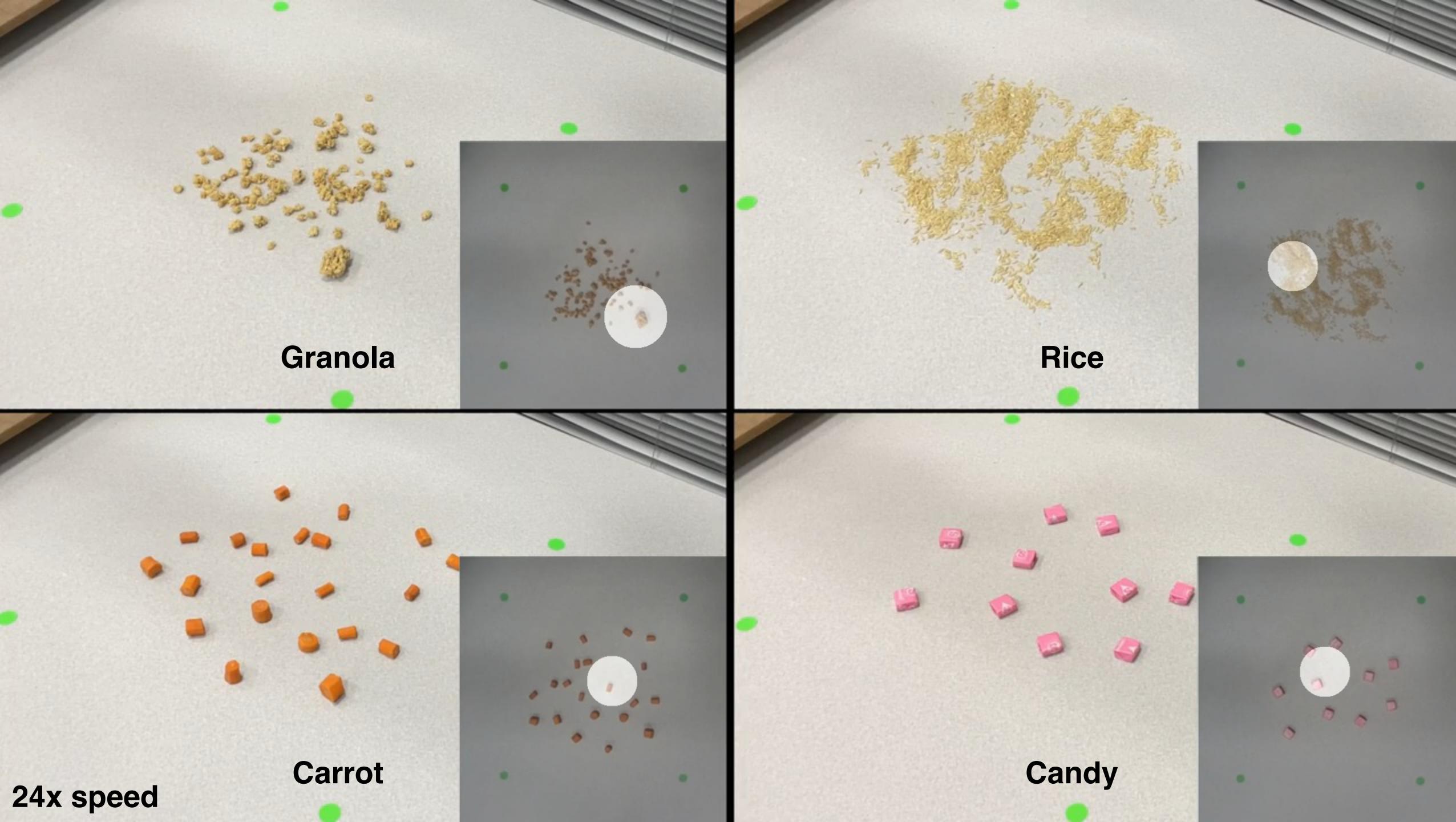
# Trajectory 4

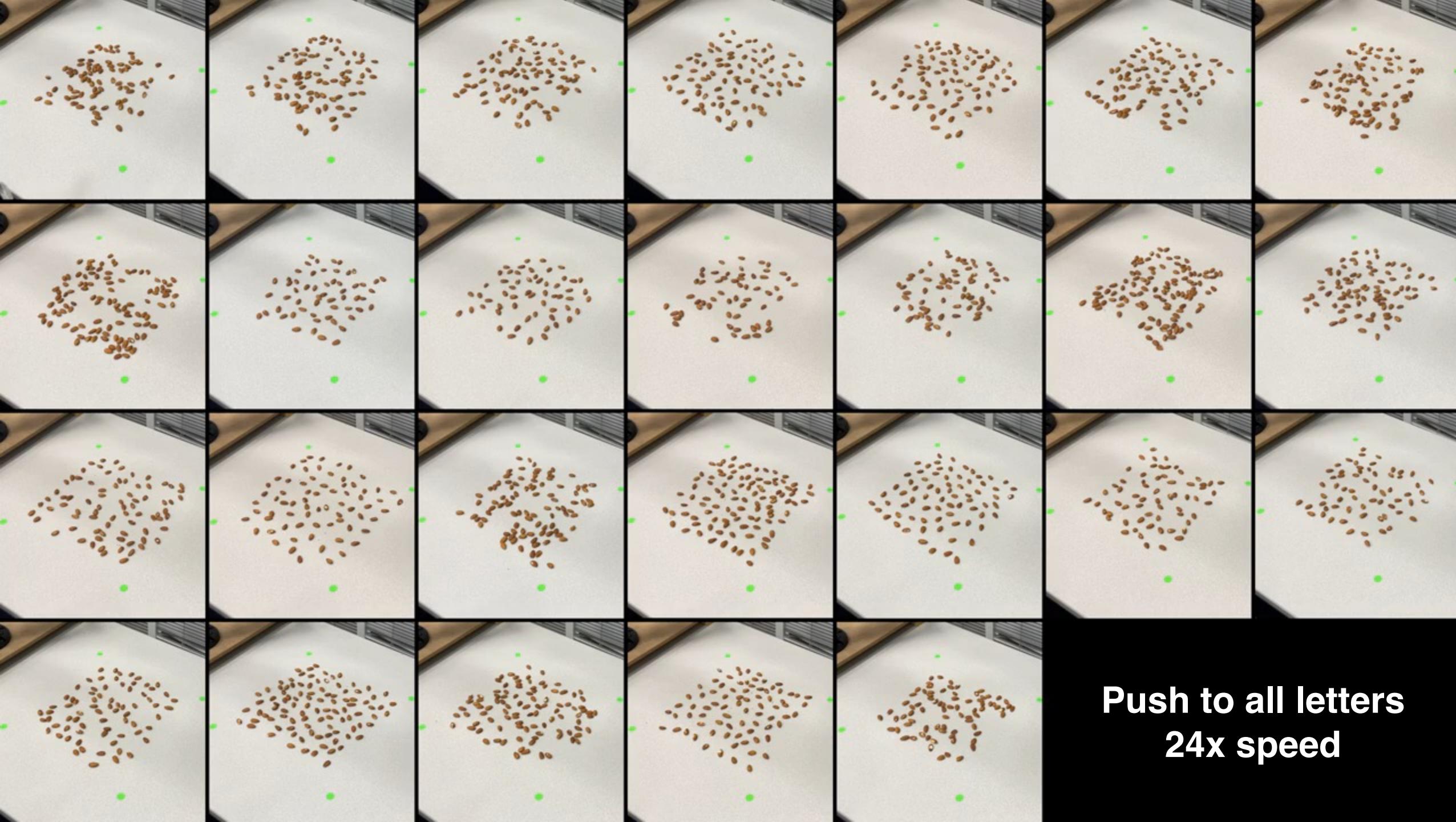


# Particle Dynamics



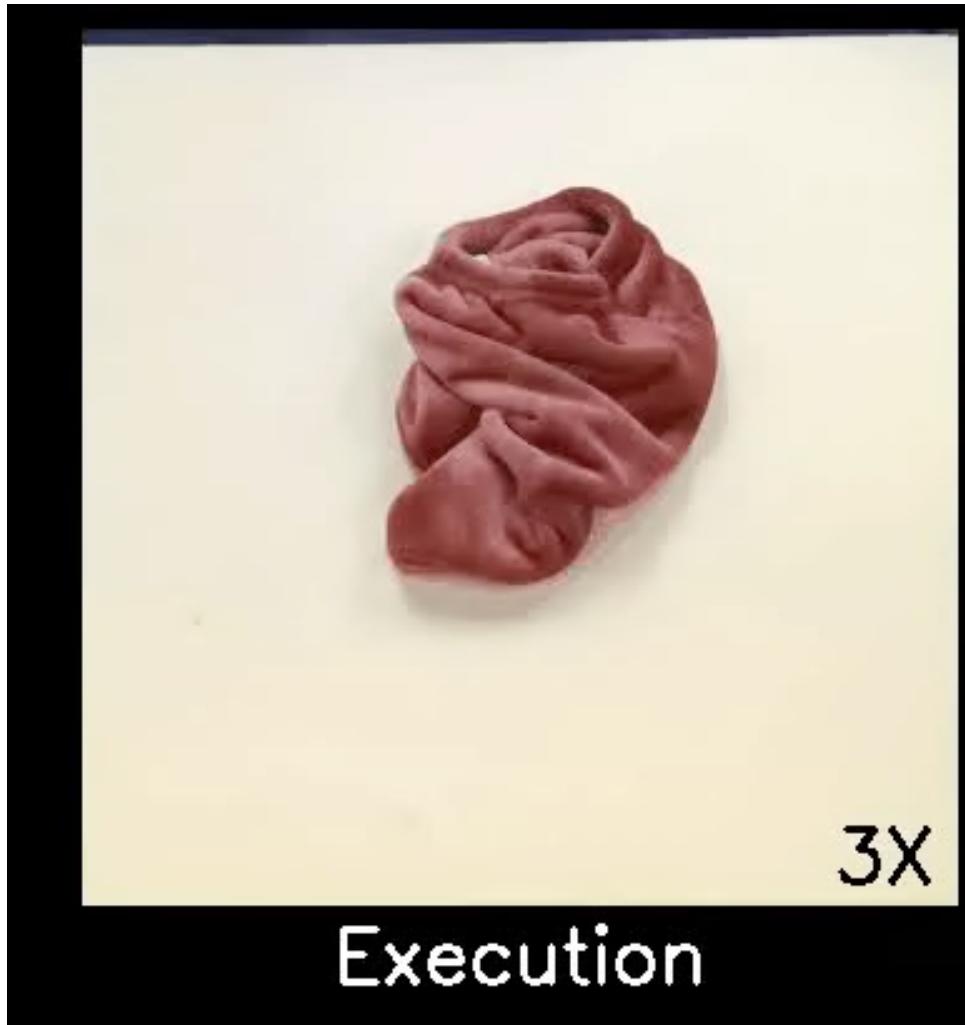
Wang, Li, Driggs-Campbell, Fei-Fei, Wu, "Dynamic-Resolution Model Learning for Object Pile Manipulation", RSS 2023



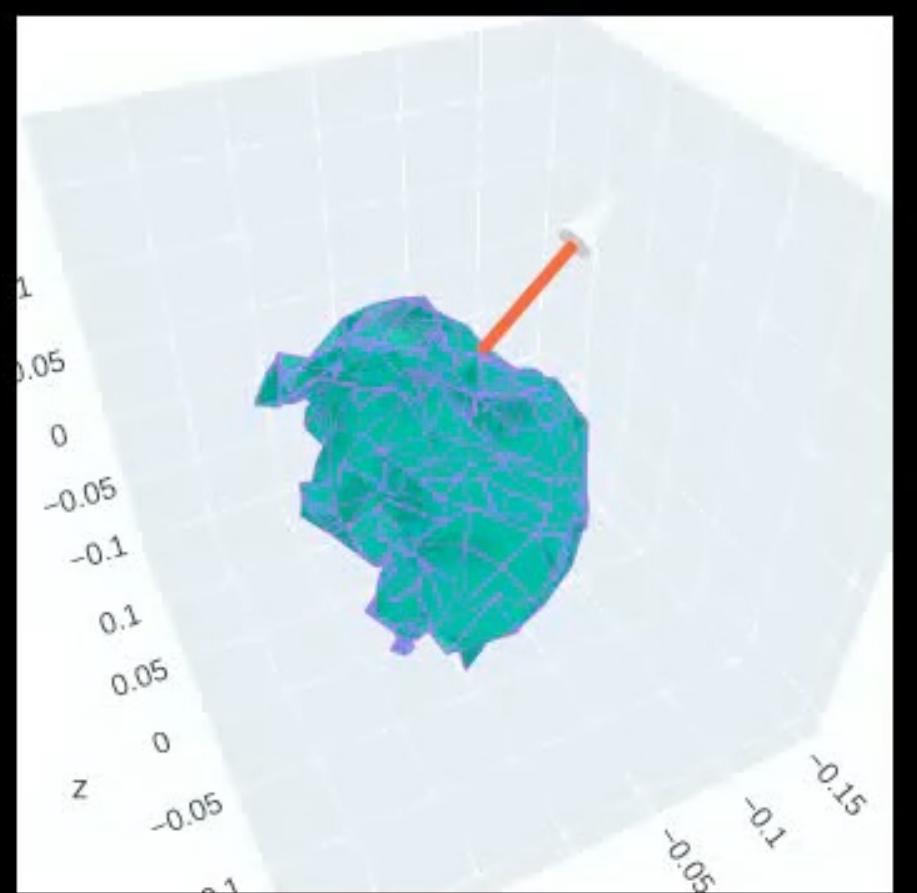


**Push to all letters  
24x speed**

# Mesh-Based Dynamics



Execution



Model rollout

Huang, Lin, Held, "Mesh-based Dynamics with Occlusion Reasoning for Cloth Manipulation", RSS 2022

# Other approaches

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Sutton and Barto, "Reinforcement Learning: An Introduction", 1998; Degris et al, "Model-free reinforcement learning with continuous action in practice", 2012; Mnih et al, "Asynchronous Methods for Deep Reinforcement Learning", ICML 2016

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Ng et al, "Algorithms for Inverse Reinforcement Learning", ICML 2000

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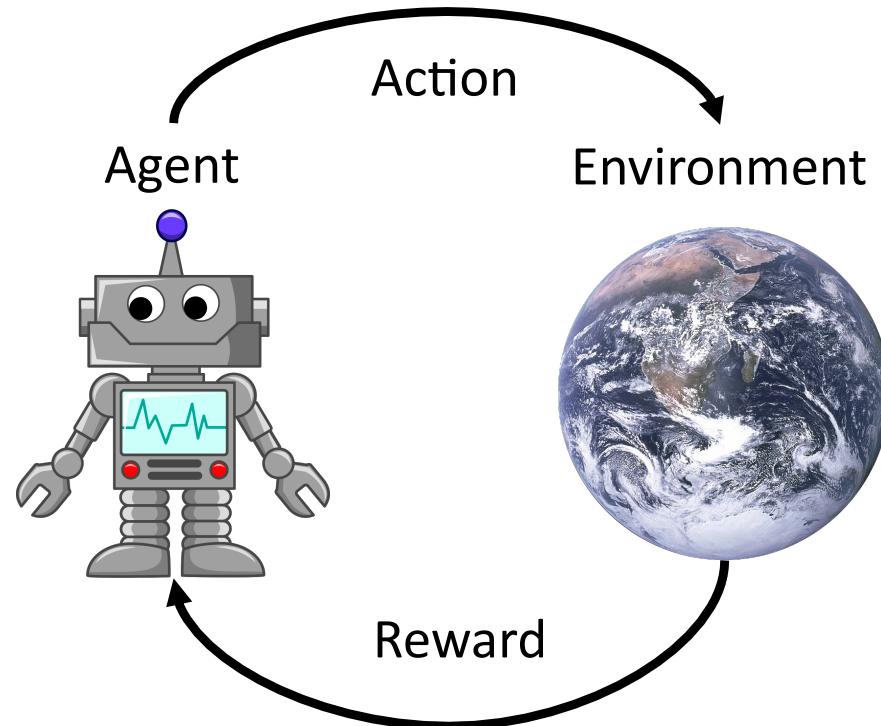
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Ng et al, "Algorithms for Inverse Reinforcement Learning", ICML 2000

**Adversarial Learning:** Learn to fool a discriminator that classifies actions as real/fake

Ho and Ermon, "Generative Adversarial Imitation Learning", NeurIPS 2016

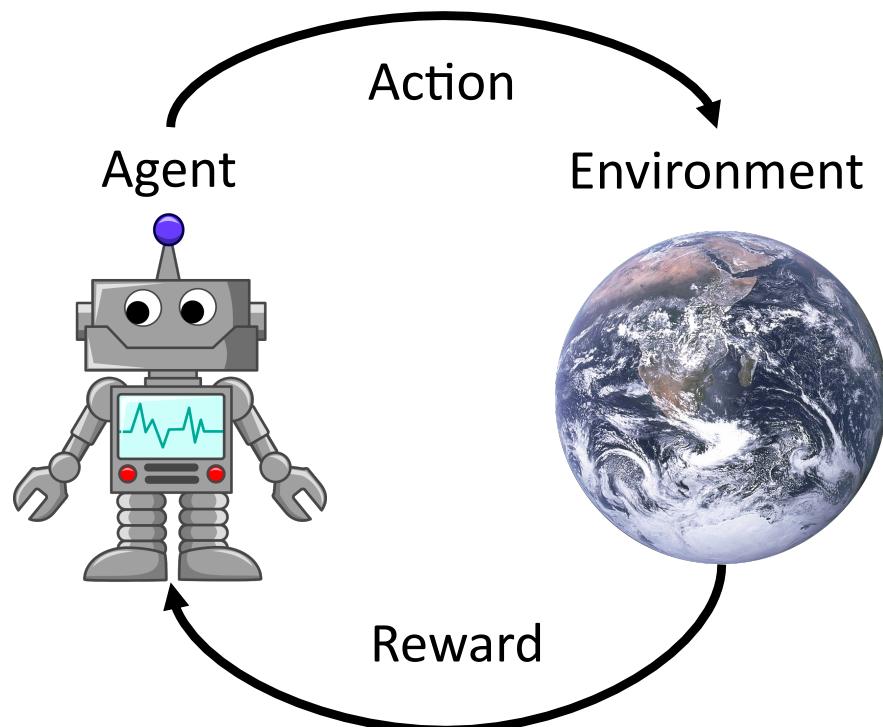
# Reinforcement Learning: Interacting With World



Normally we use RL to train  
**agents** that interact with a (noisy,  
nondifferentiable) **environment**

# Summary: Reinforcement Learning

RL trains **agents** that interact with an **environment** and learn to maximize **reward**



**Q-Learning:** Train network  $Q_\theta(s, a)$  to estimate future rewards for every (state, action) pair. Use Bellman Equation to define loss function for training Q

**Policy Gradients:** Train a network  $\pi_\theta(a | s)$  that takes state as input, gives distribution over which action to take in that state. Use REINFORCE Rule for computing gradients

Next time: Generative Models  
Guest Lecture by Dr. Ruiqi Gao from Google Brain