

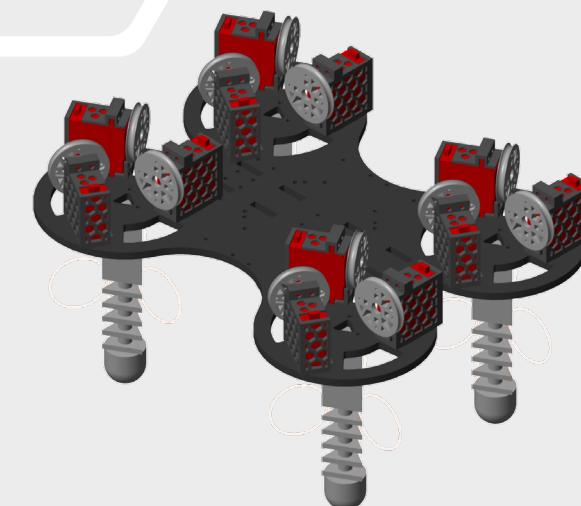
# Modeling, Simulation, and Control of a Soft Quadruped Robot

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**Qinglei Ji (PhD)**

Solution Engineer – Controls & AI

Volvo Cars Cooperation, Gothenburg

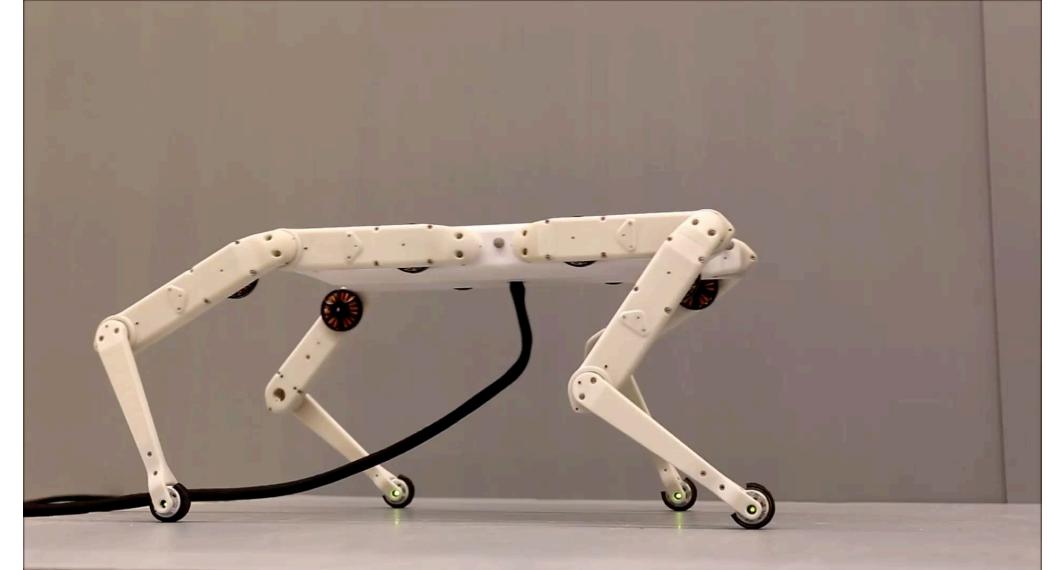


# Quadruped Robots

Enhanced mobility and adaptability to complex environment



Spot, Boston Dynamics



3D printed Robot

<https://www.youtube.com/watch?v=wlkCQXHEgjA>

<https://3dprint.com/270090/open-source-quadruped-robot-with-3d-printed-components/>

# Soft Quadruped Robots

Systems built from highly compliant materials to provide flexibility and adaptability to the workspace.

- Continuous movements
- Smooth motions
- Safe interactions
- Need for fast, precise and light-weight actuators



Multi-gait robot



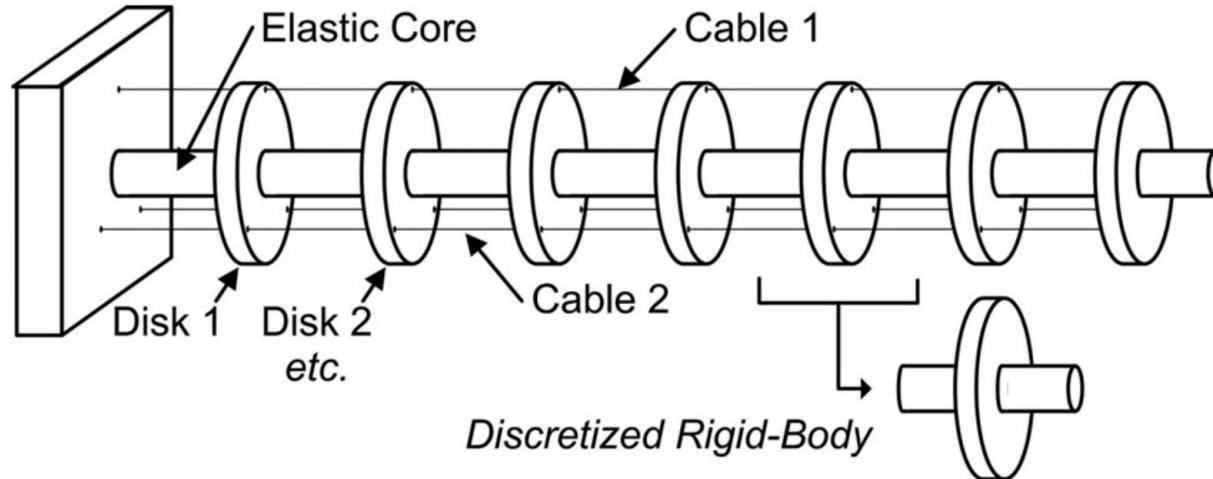
3D printed Soft Robot

*Shepherd et al., "Multigait soft robot." Proceedings of the national academy of sciences 108, no. 51 (2011): 20400-20403.*

*Ishida et al., "Morphing structure for changing hydrodynamic characteristics of a soft underwater walking robot." IEEE Robotics and Automation Letters 4, no. 4 (2019): 4163-4169.*

# Tendon-driven Continuum Actuator

Combines fast response and compliance

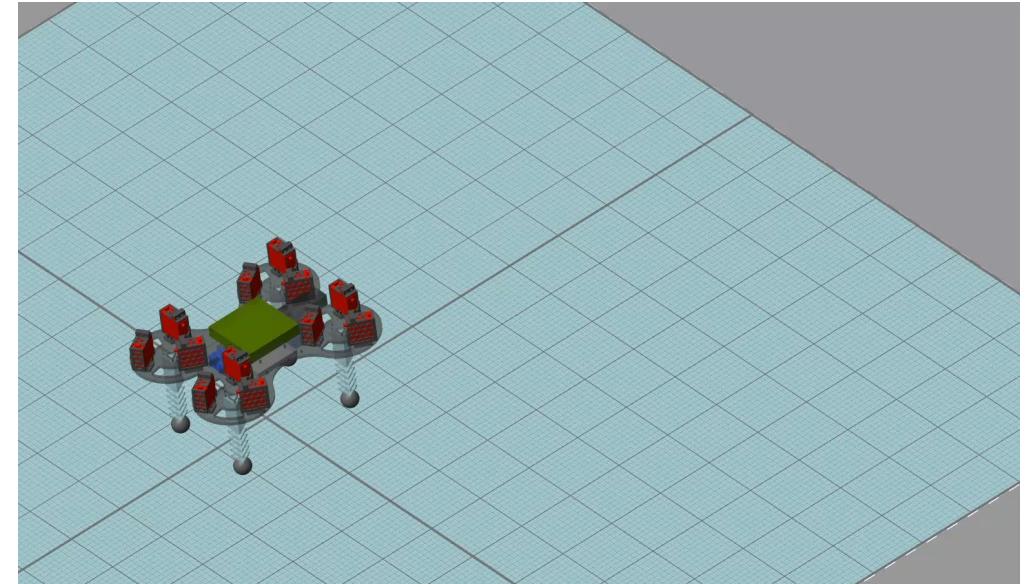
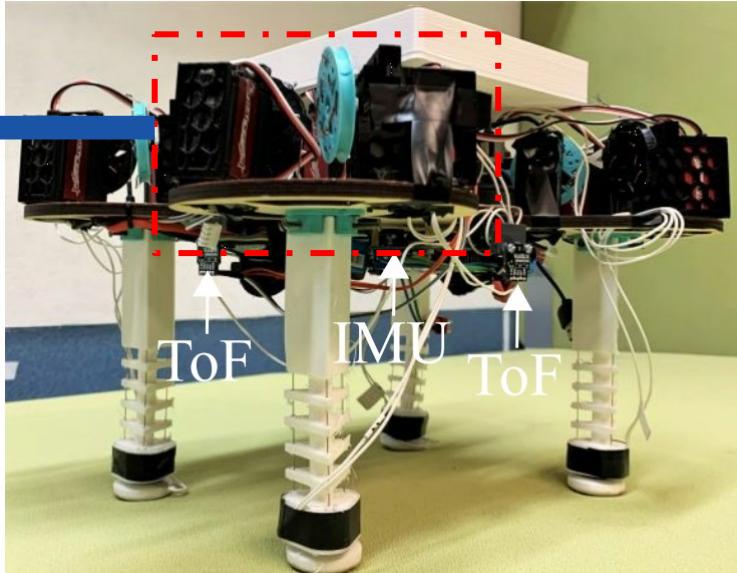


# Soft Quadruped Robot at KTH

Quadruped robot enabled by tendon-driven soft actuators

- Complex to model and control
- Slow simulation

Each leg actuated  
by three pulley-  
driven actuators  
with cables

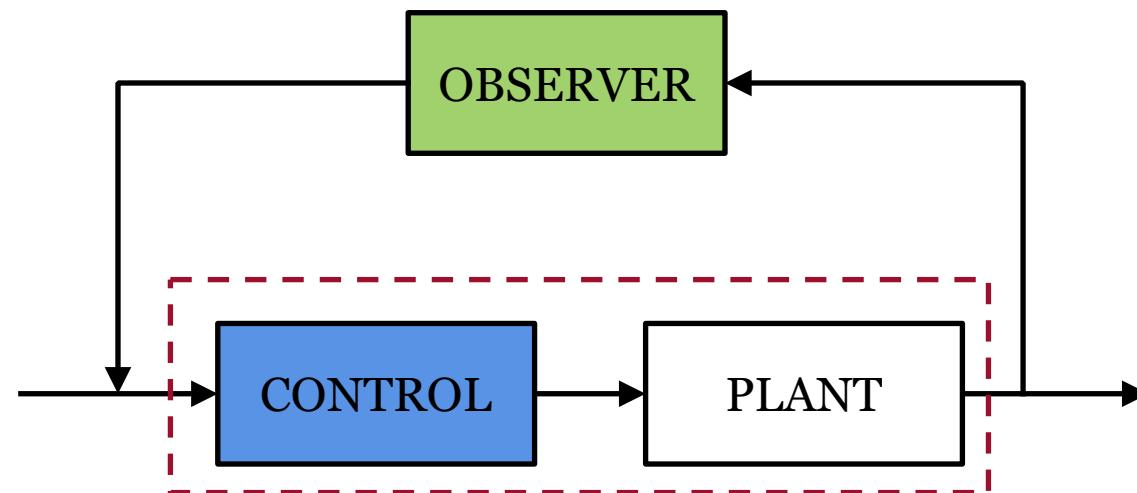


Muralidharan ST, Zhu R, Ji Q, Feng L, Wang XV, Wang L. A soft quadruped robot enabled by continuum actuators. In 2021 IEEE 17th International Conference on Automation Science and Engineering (CASE) 2021 Aug 23 (pp. 834-840). IEEE.



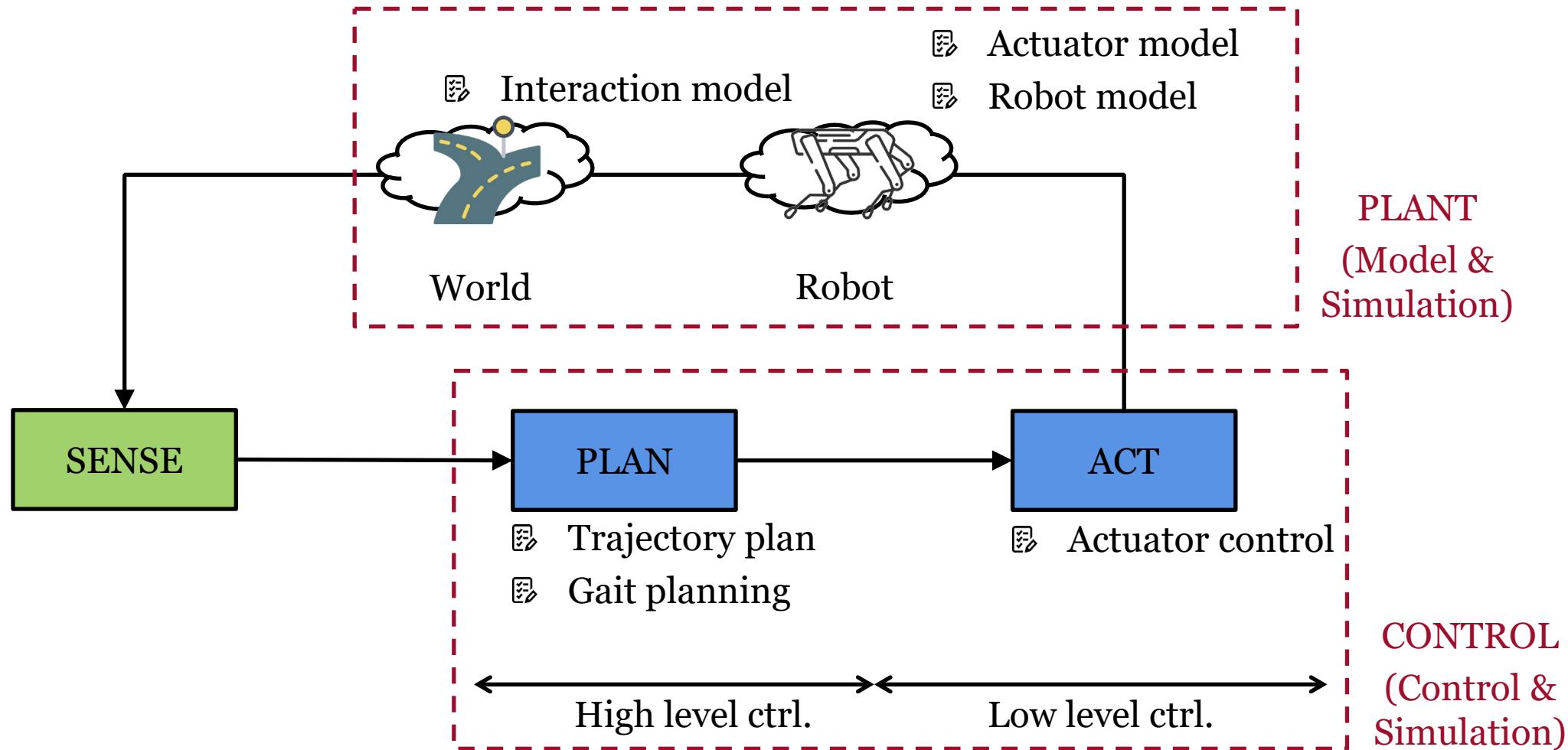
# Control Architecture

- Control: Mechanism or algorithm for ensuring the system behaves in a desired manner.
- Plant: System or process being controlled (mechanical, electrical, biological or economic systems, etc.).
- Observer: Measure or estimate the internal state of the plant.



Typical feedback architecture in controls engineering.

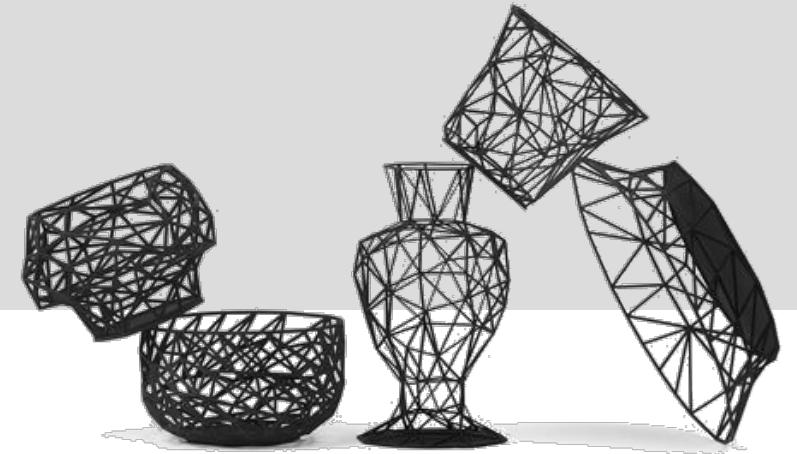
# Control Architecture



Sense-Plan-Act architecture in robotic and autonomous driving systems.

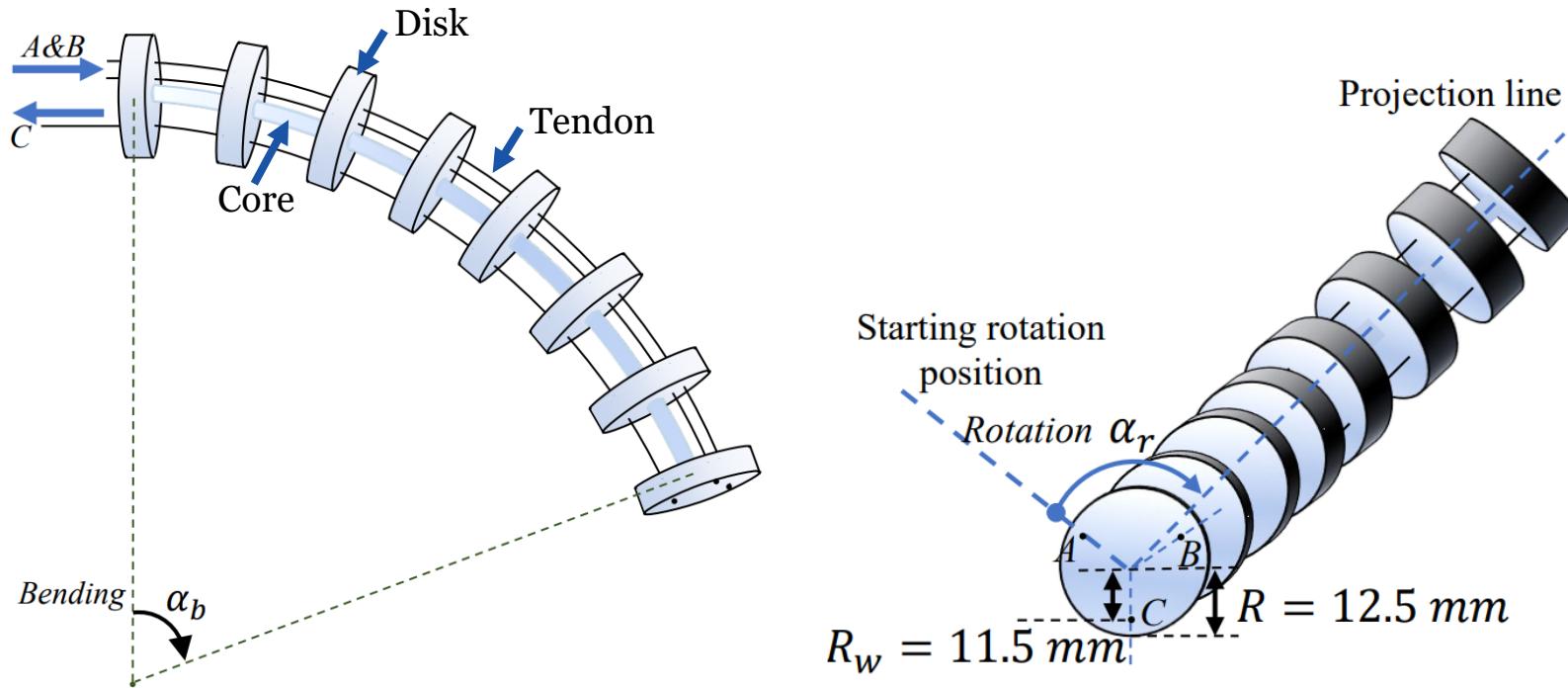
# Outline

- ✓ Background
- ✓ Modeling
- ✓ Simulation
- ✓ Control
- ✓ Conclusion



# Inverse Kinematics Model

Inverse kinematics model for an **incompressible** tendon-driven soft actuator



$$x_A = R_w \alpha_b \cdot \cos(\alpha_r)$$

$$x_B = R_w \alpha_b \cdot \cos(\alpha_r + \frac{2}{3}\pi)$$

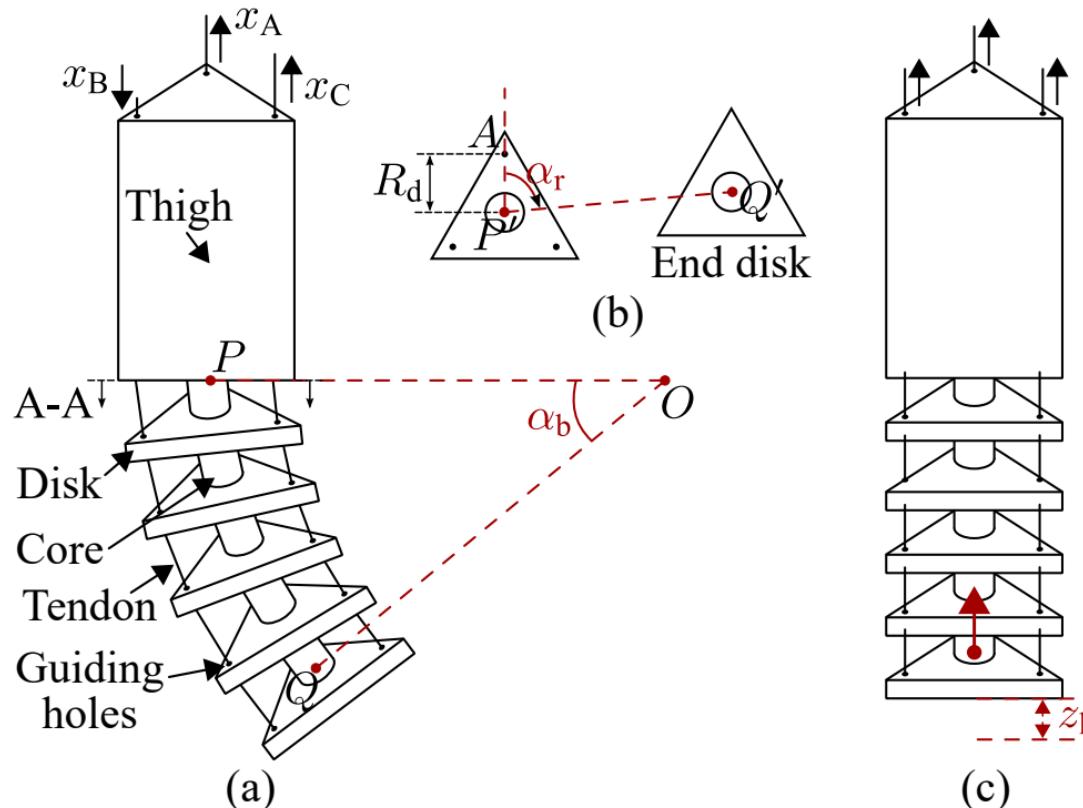
$$x_C = R_w \alpha_b \cdot \cos(\alpha_r + \frac{4}{3}\pi)$$

Hsiao K, Mochiyama H. A wire-driven continuum manipulator model without assuming shape curvature constancy. In 2017 IEEE/RSJ International Conference on Intelligent Robots and Systems (IROS) 2017 Sep 24 (pp. 436-443). IEEE.

Muralidharan ST, Zhu R, Ji Q, Feng L, Wang XV, Wang L. A soft quadruped robot enabled by continuum actuators. In 2021 IEEE 17th International Conference on Automation Science and Engineering (CASE) 2021 Aug 23 (pp. 834-840). IEEE.

# Inverse Kinematics Model

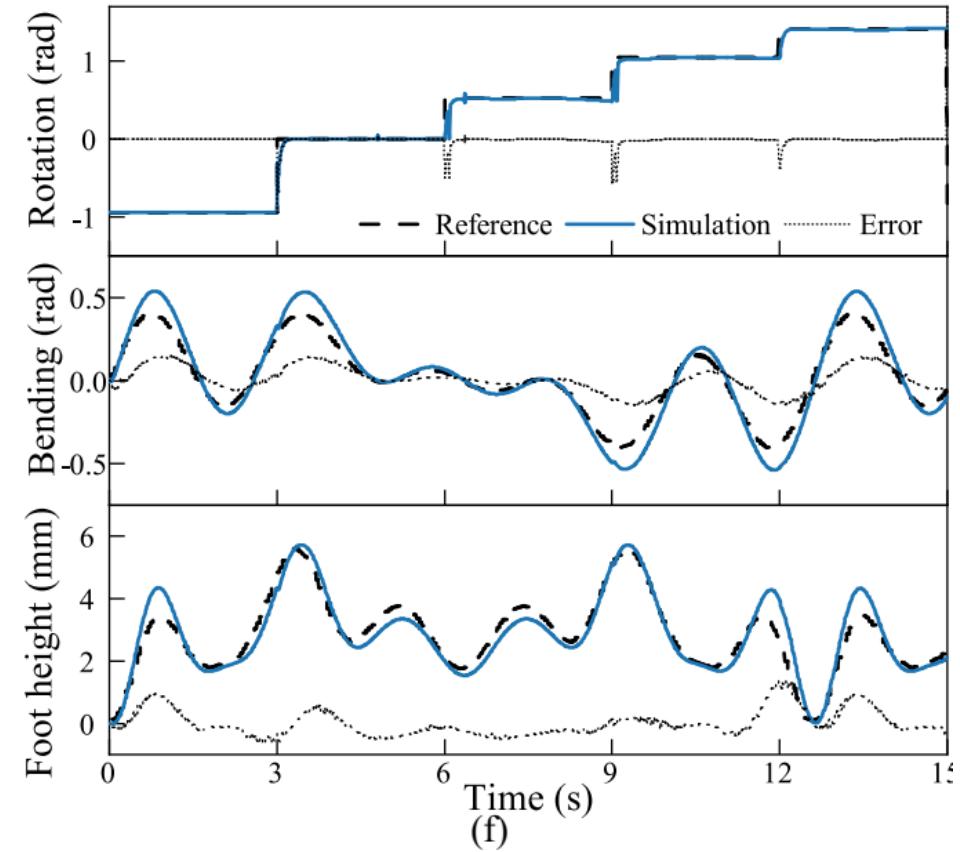
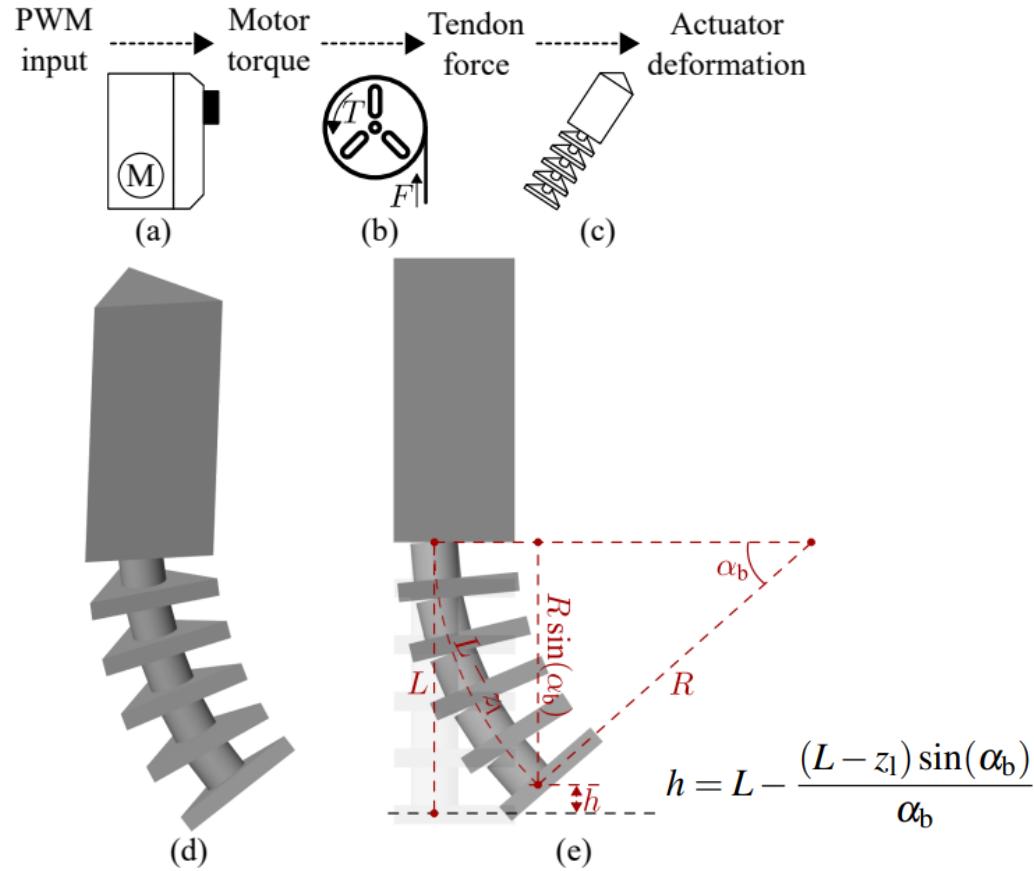
Proposed model for a **compressible** tendon-driven soft actuator



$$[x_A, x_B, x_C]^T = g\left(\begin{bmatrix} \alpha_b \\ \alpha_r \\ z_1 \end{bmatrix}\right) = f\left(\begin{bmatrix} \alpha_b \\ \alpha_r \end{bmatrix}\right) + z_1 \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix}$$

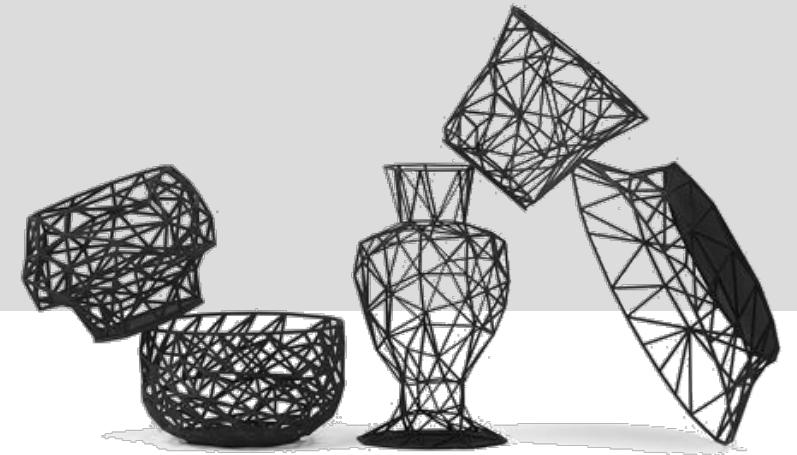
# Inverse Kinematics Model

## Model validation



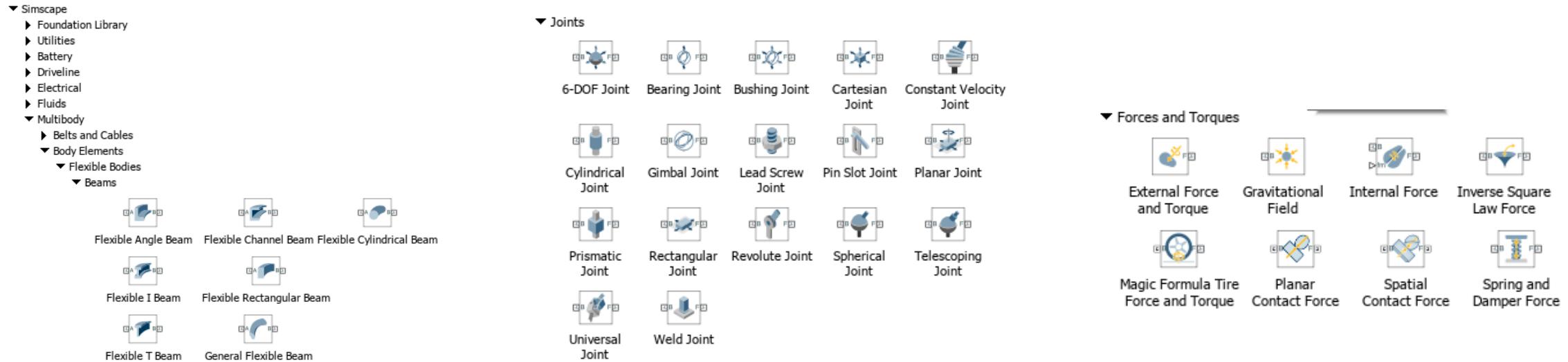
# Outline

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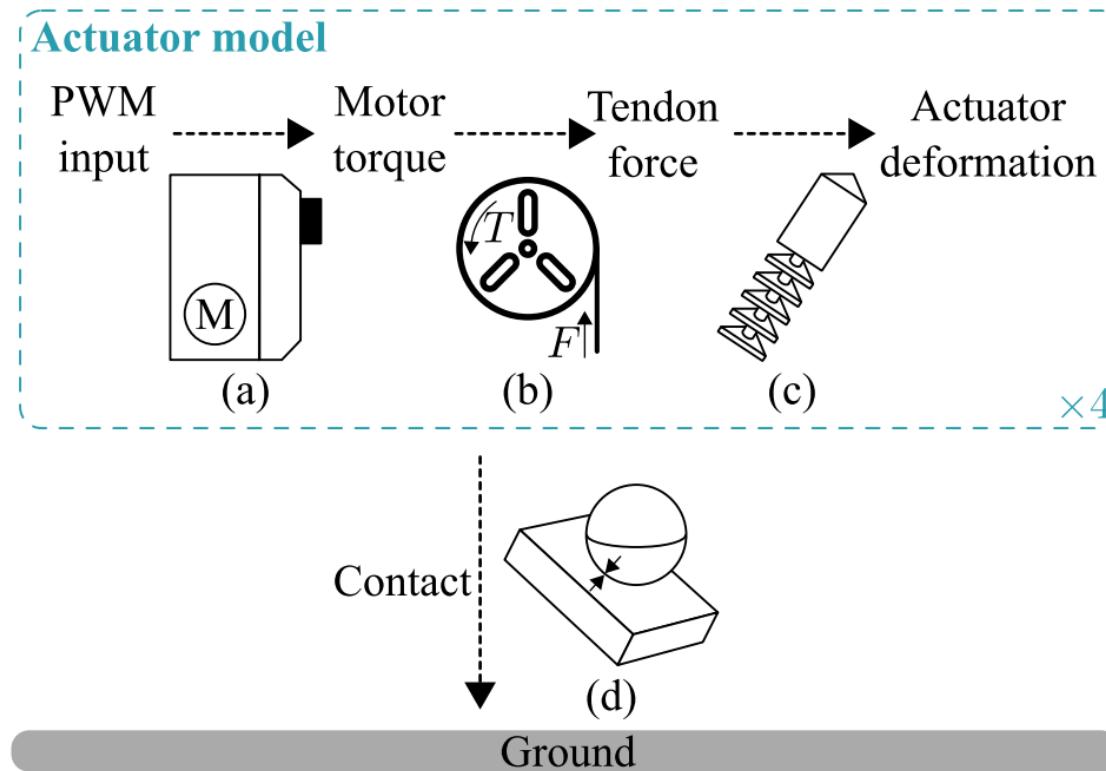
# Simulation Environment

- Simscape Multibody toolbox in MATLAB Simulink (support for flexible/soft materials)
- Integrated modeling and simulation for machine learning, controller, and physical plant



Complete body, joint, and force types for modeling soft robots.

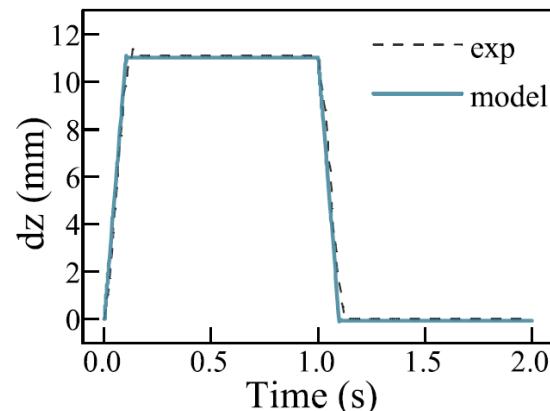
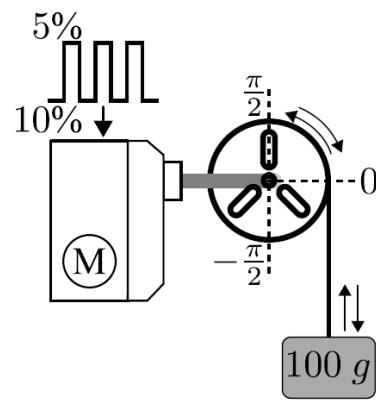
# System Architecture



Overview of the quadruped robot's main subsystems.

Ji, Qinglei, et al. "Synthesizing the optimal gait of a quadruped robot with soft actuators using deep reinforcement learning." *Robotics and Computer-Integrated Manufacturing* 78 (2022): 102382.

# Motor Parameter Characterization

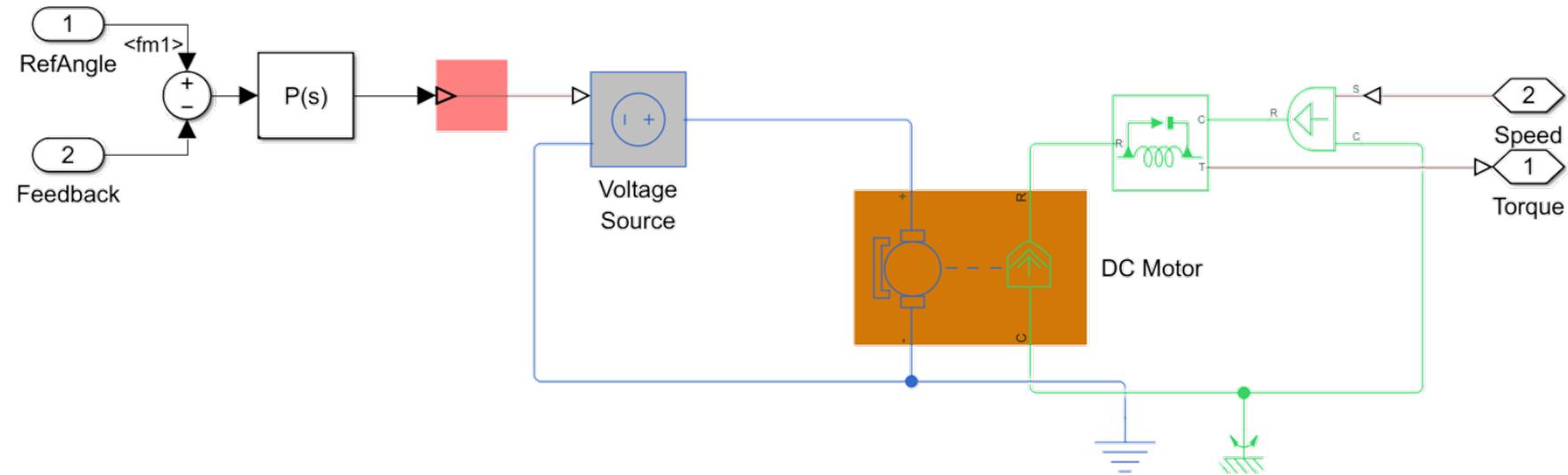


**Table 1**  
Identified servo motor parameters.

Parameters	Value
Stall torque (cm * kg)	11.2
Time traveling $60^\circ$ (s)	0.2
Nominal voltage (V)	6
Rotational range (rad)	$[-\pi/2, \pi/2]$

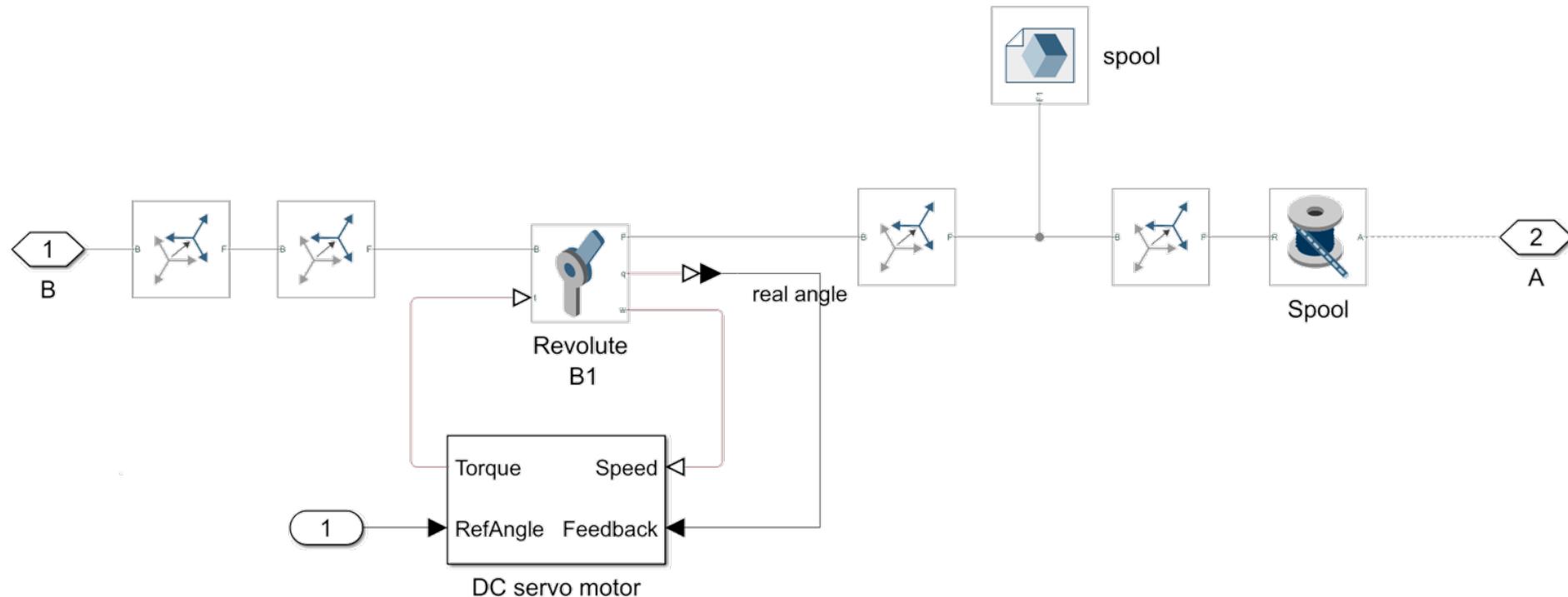
Identifying motor parameters with known load.

# Motor Model



Servo motor with angle control.

# Motor Model

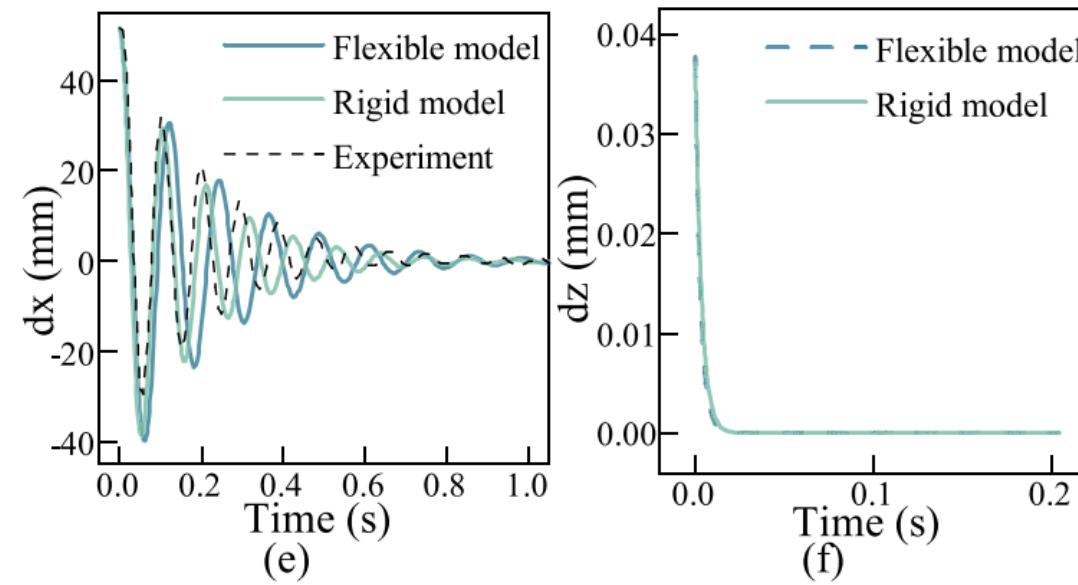
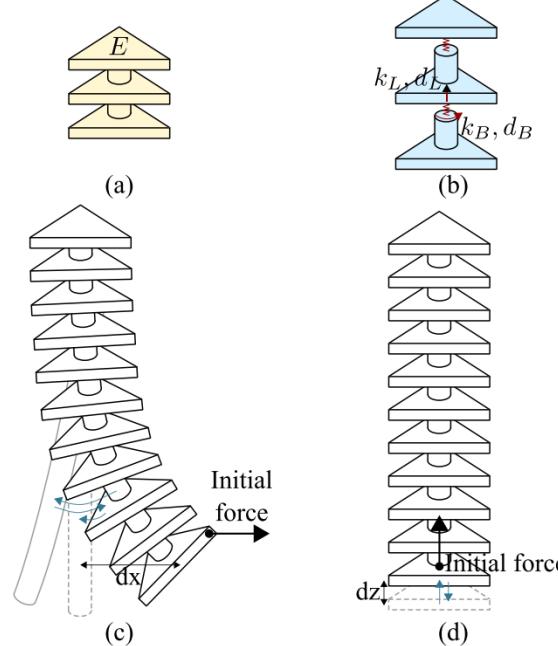


Connect to spool with force feedback.

# Soft Material Model

Choices for modeling soft material

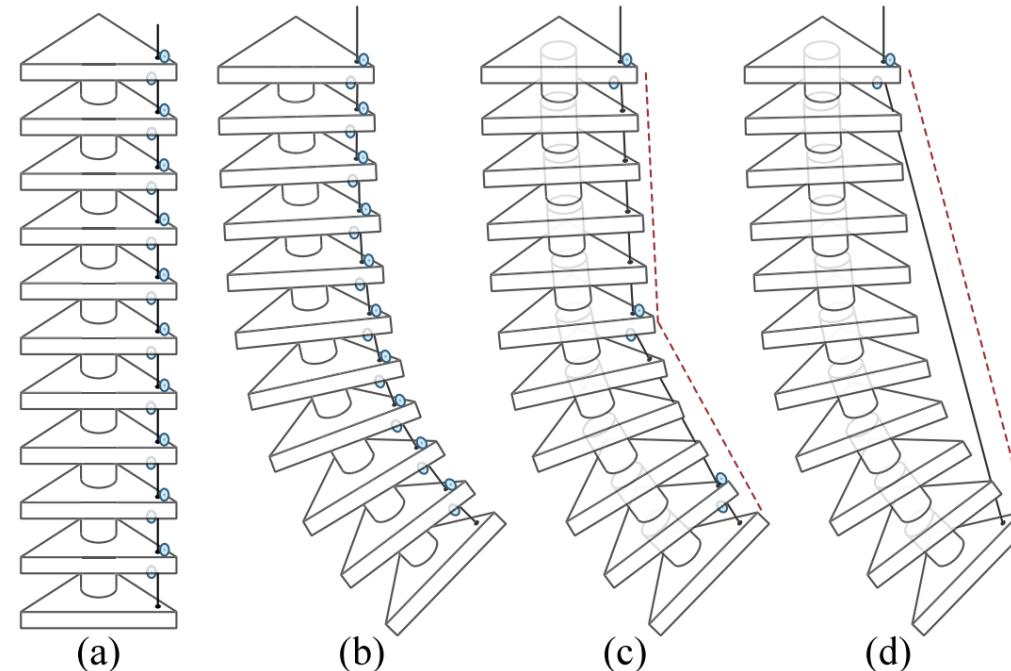
- Elastic material modelling
- Lumped parameter method with hard material



# Tendon Modeling

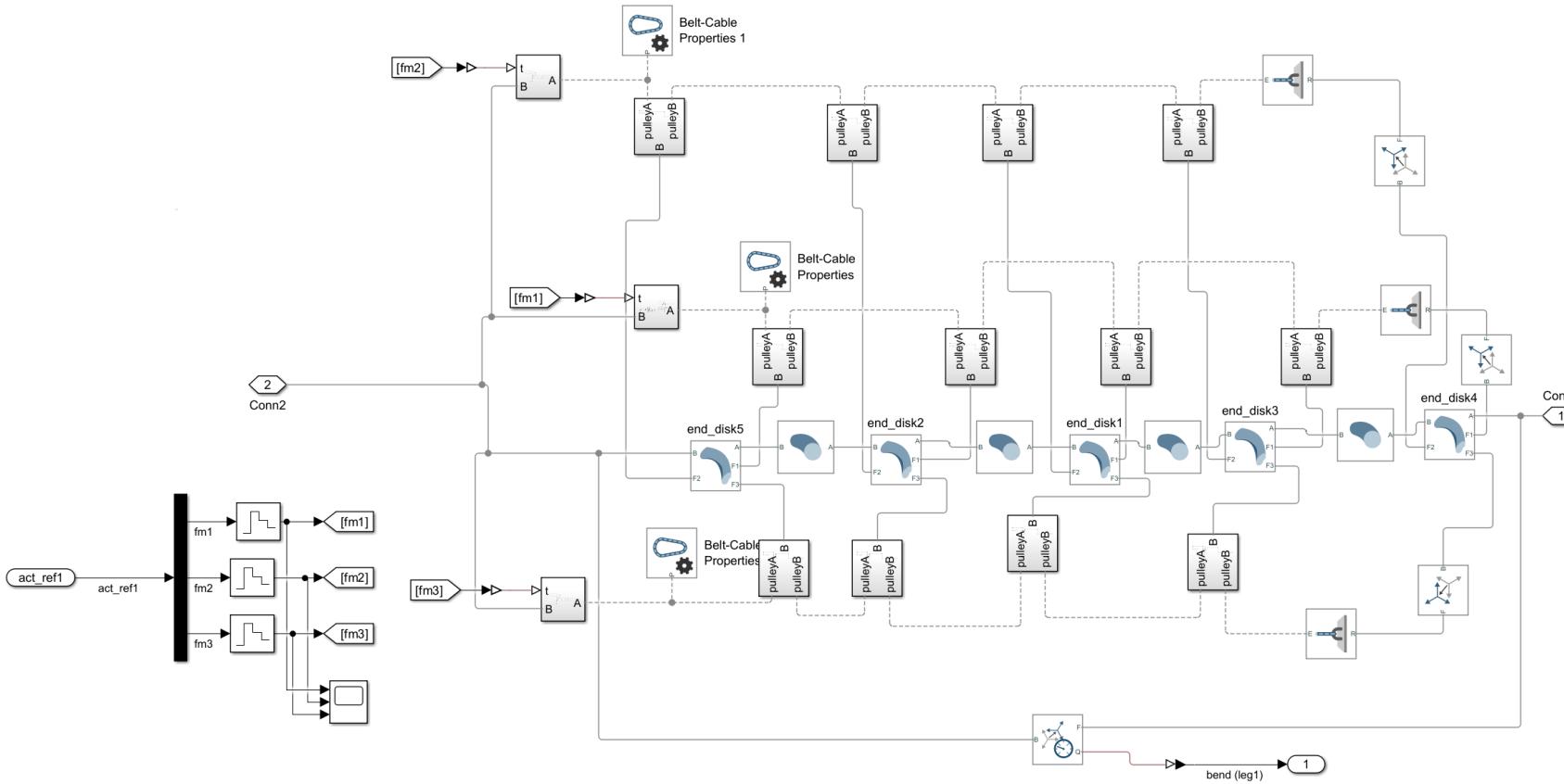
Choices for modelling tendon mechanism

- Equally distributed force pairs
- Confined cable by pully pairs
- Varying numbers of pulleys



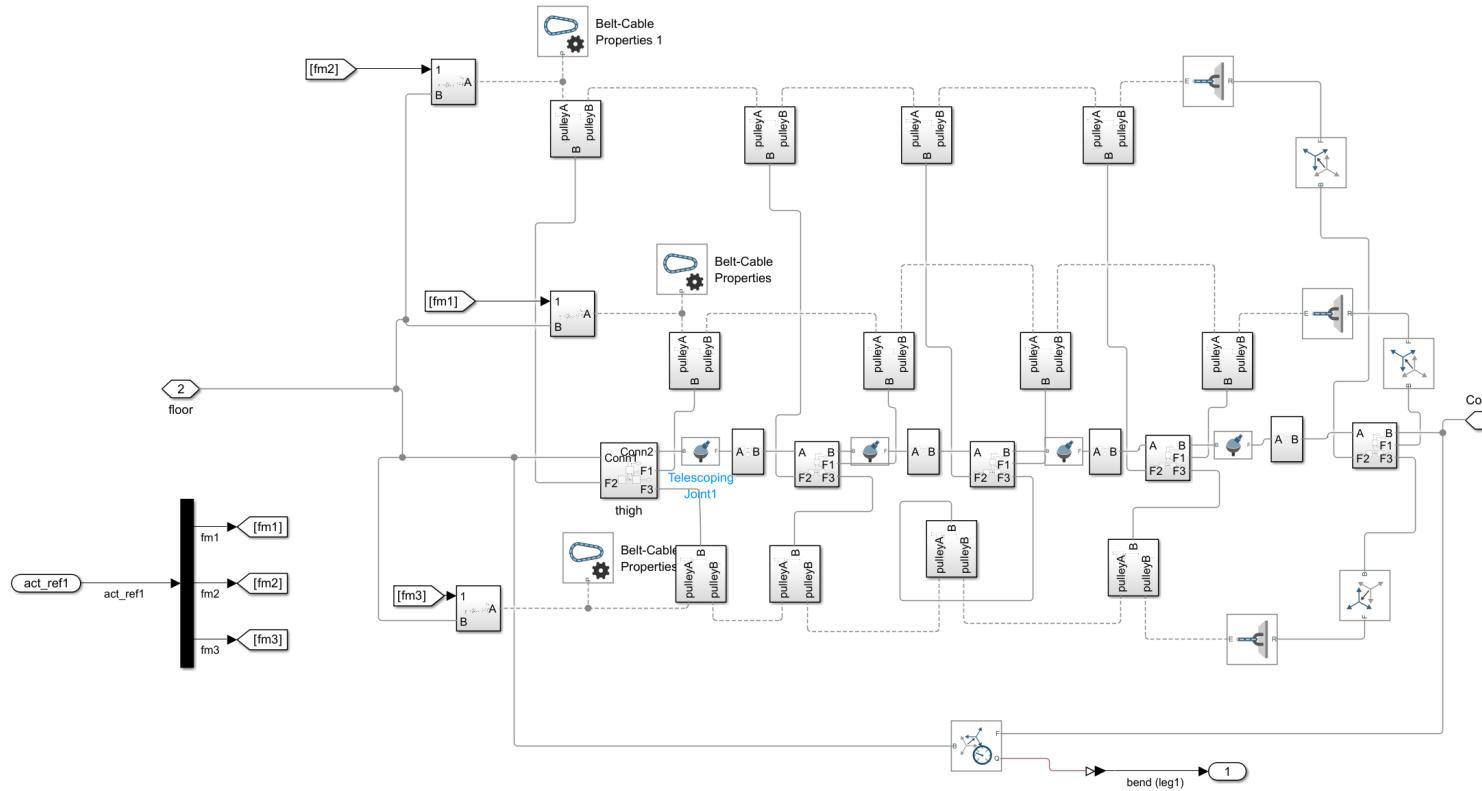
Varying numbers of pulleys for trade-off between accuracy and simulation efficiency.

# Soft Actuator Model in Simulink

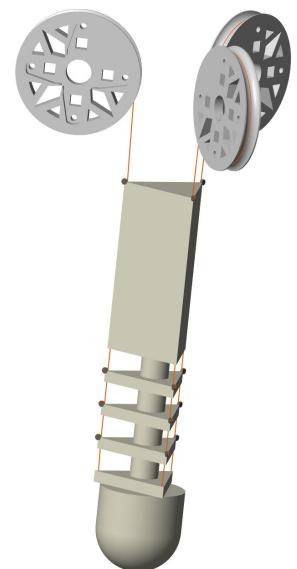


Soft material sections.

# Soft Actuator Model in Simulink

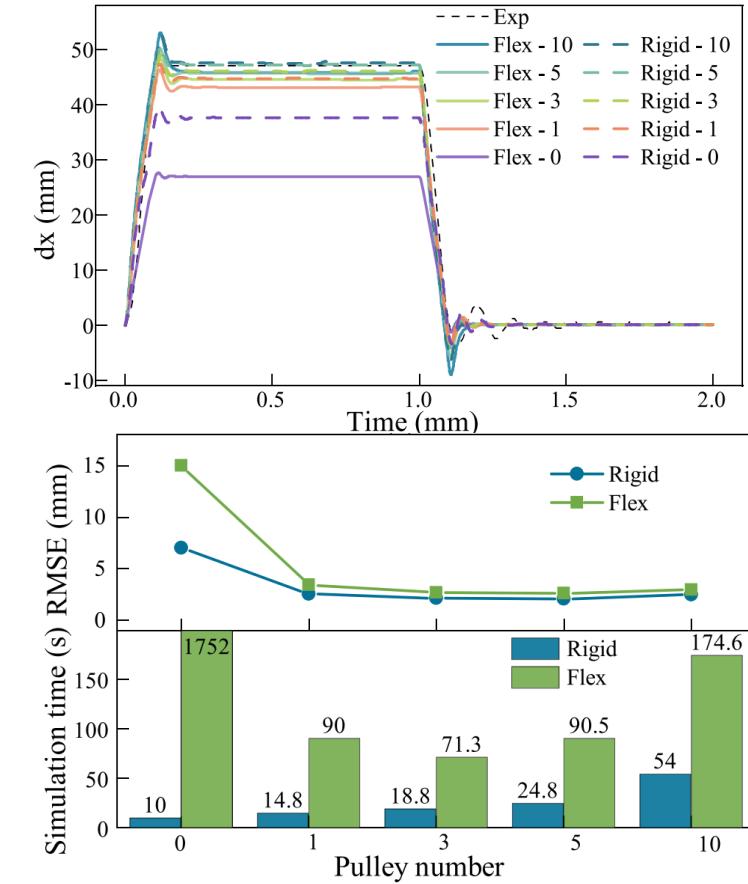
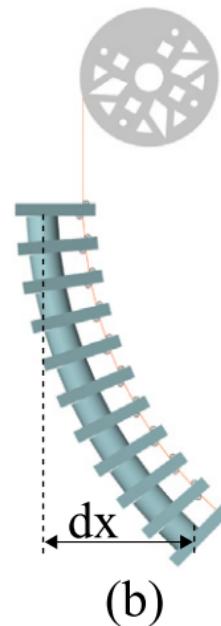
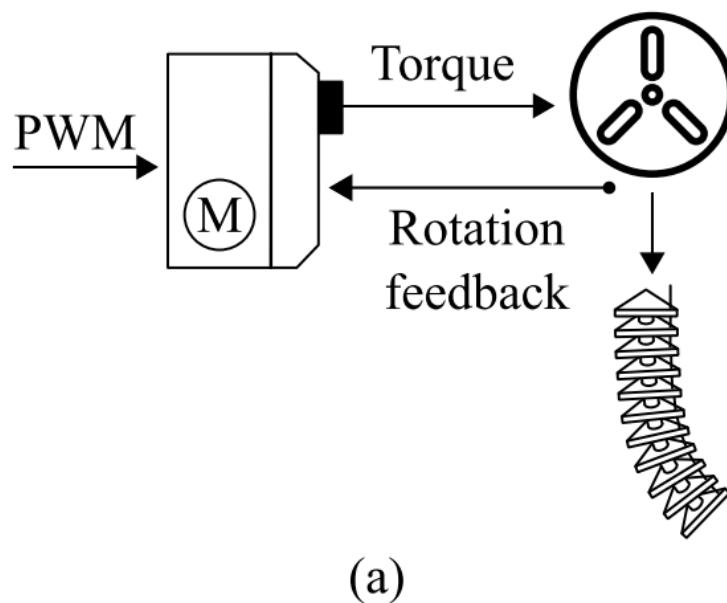


Rigid material connected by lumped joints.



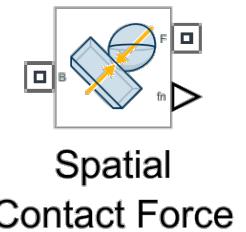
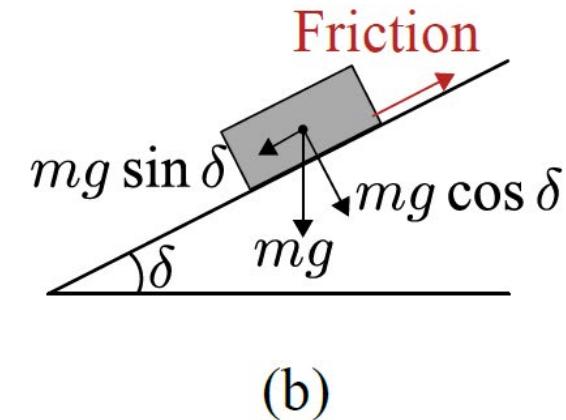
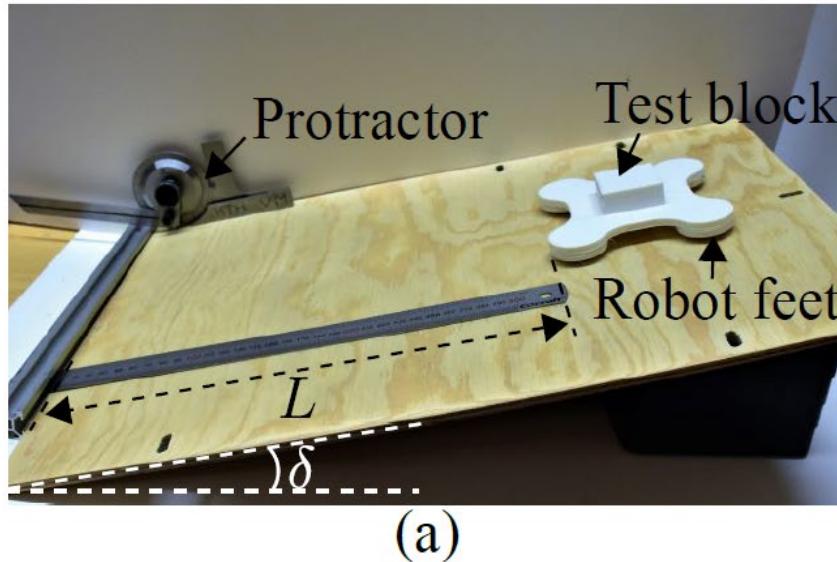
# Result

## Precision *vs* simulation time



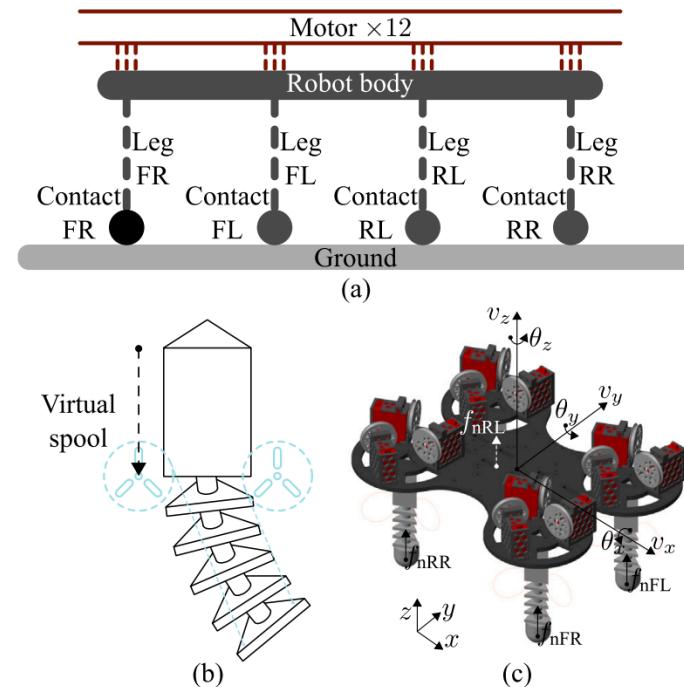
# Foot-ground Contact Model

Spatial contact force block in Simscape to model the friction between foot and ground.

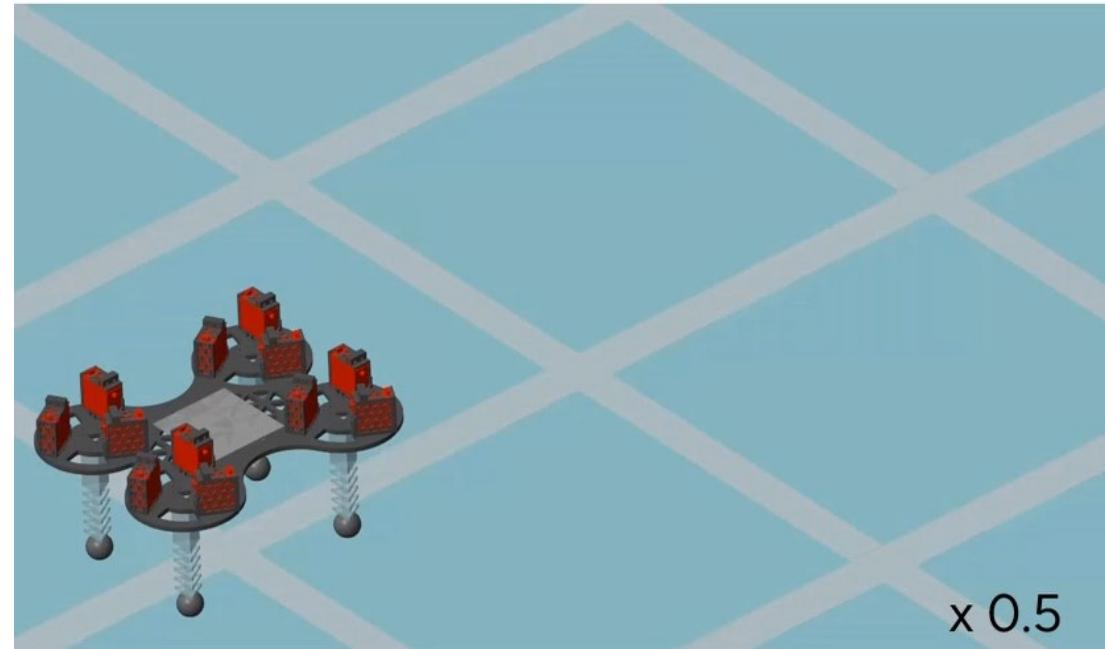


Inclined plan experiment to acquire the friction coefficient.

# Simulation Demonstration

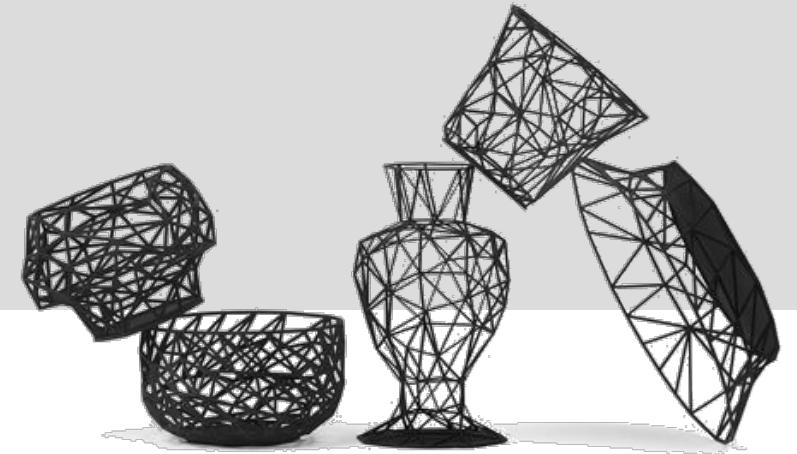


Complete robot model  
architecture.



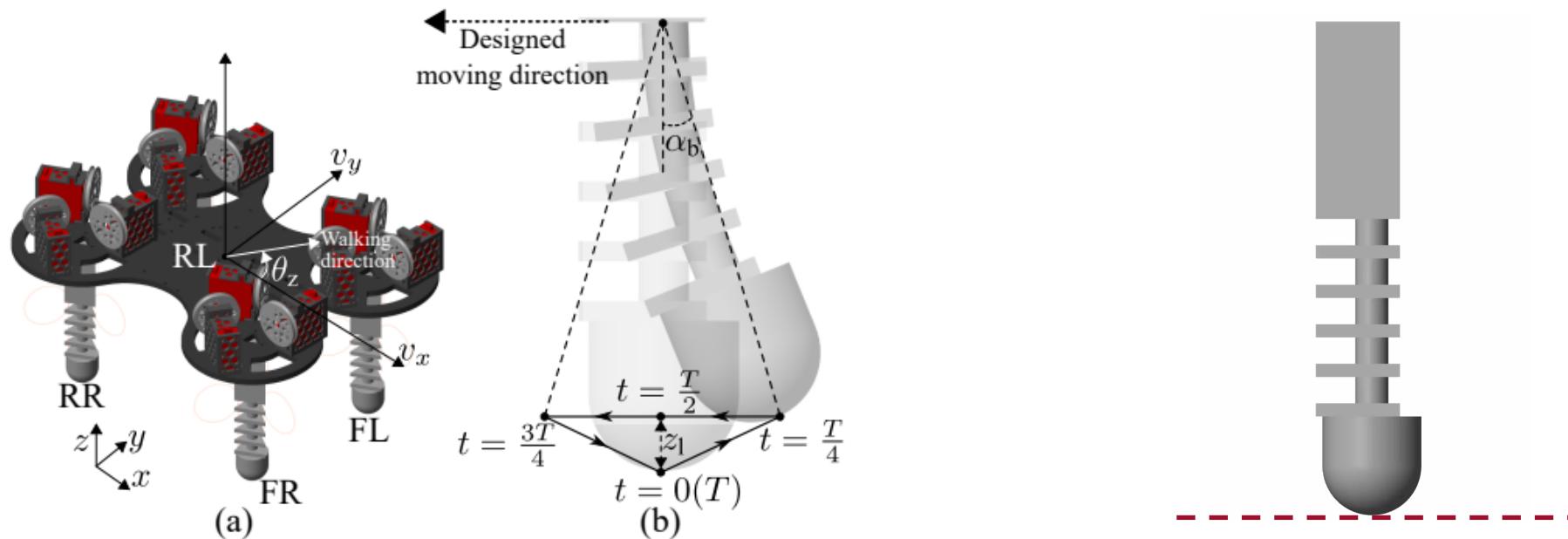
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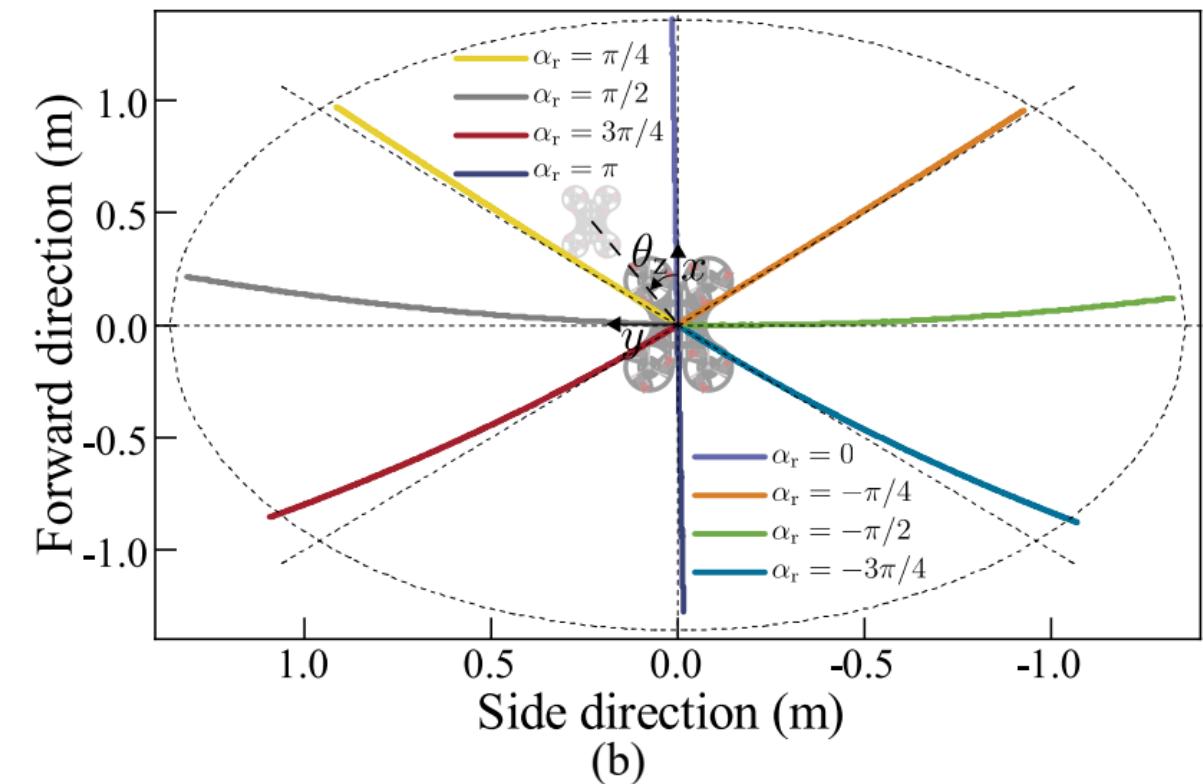
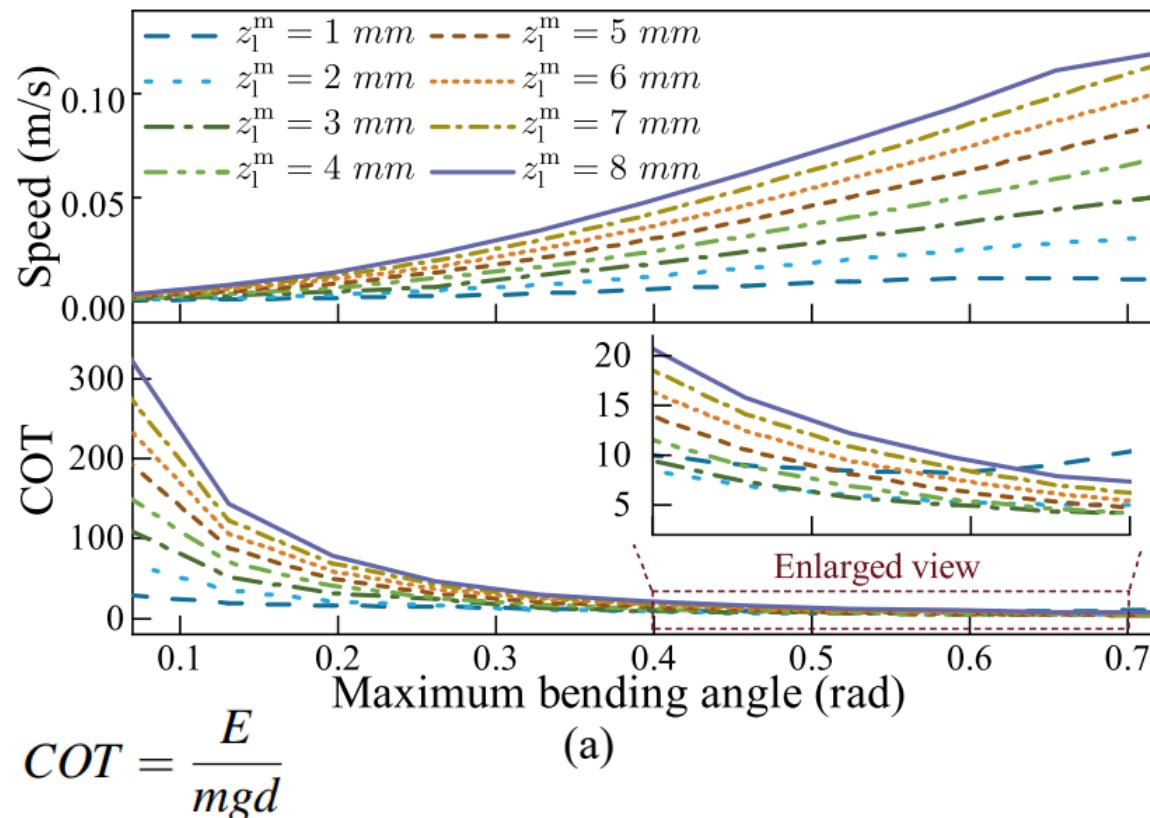


# Robot Gait Development - Trot Gait

Assumption: Actuator rotational directional refers to the walking direction

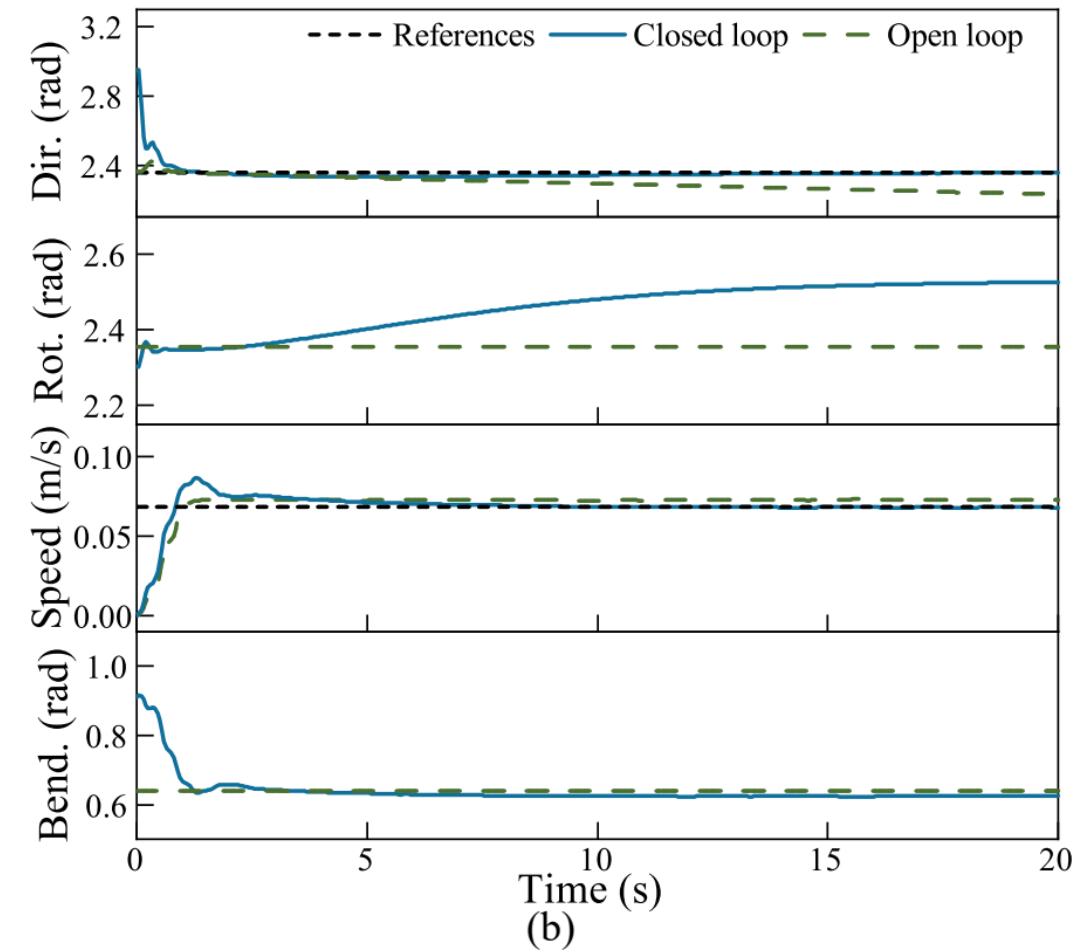
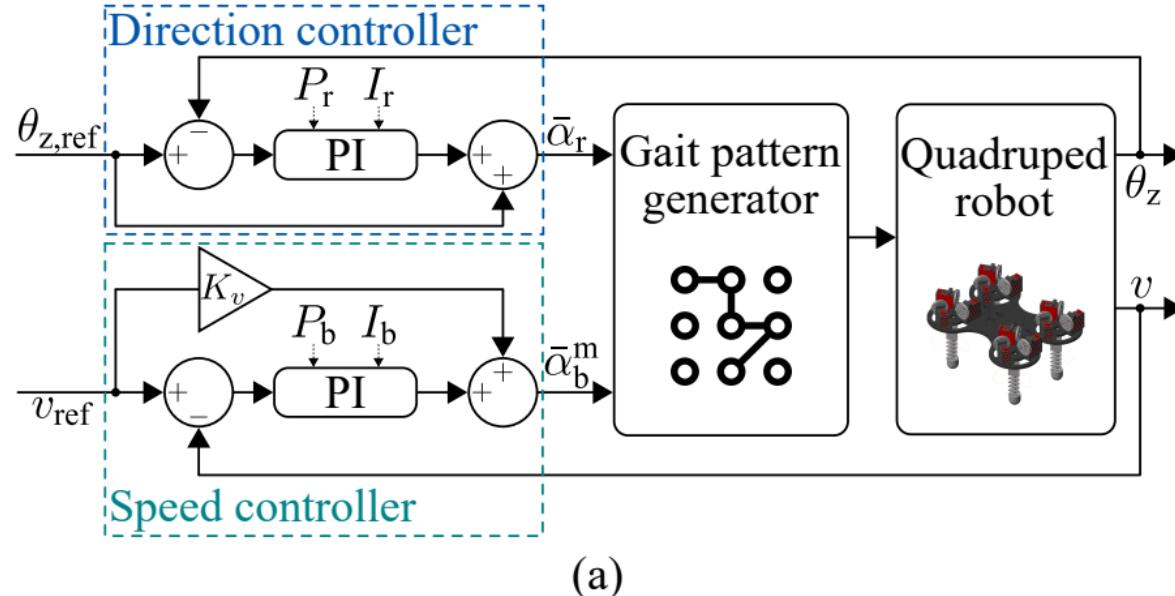


# Influences of Input Parameters

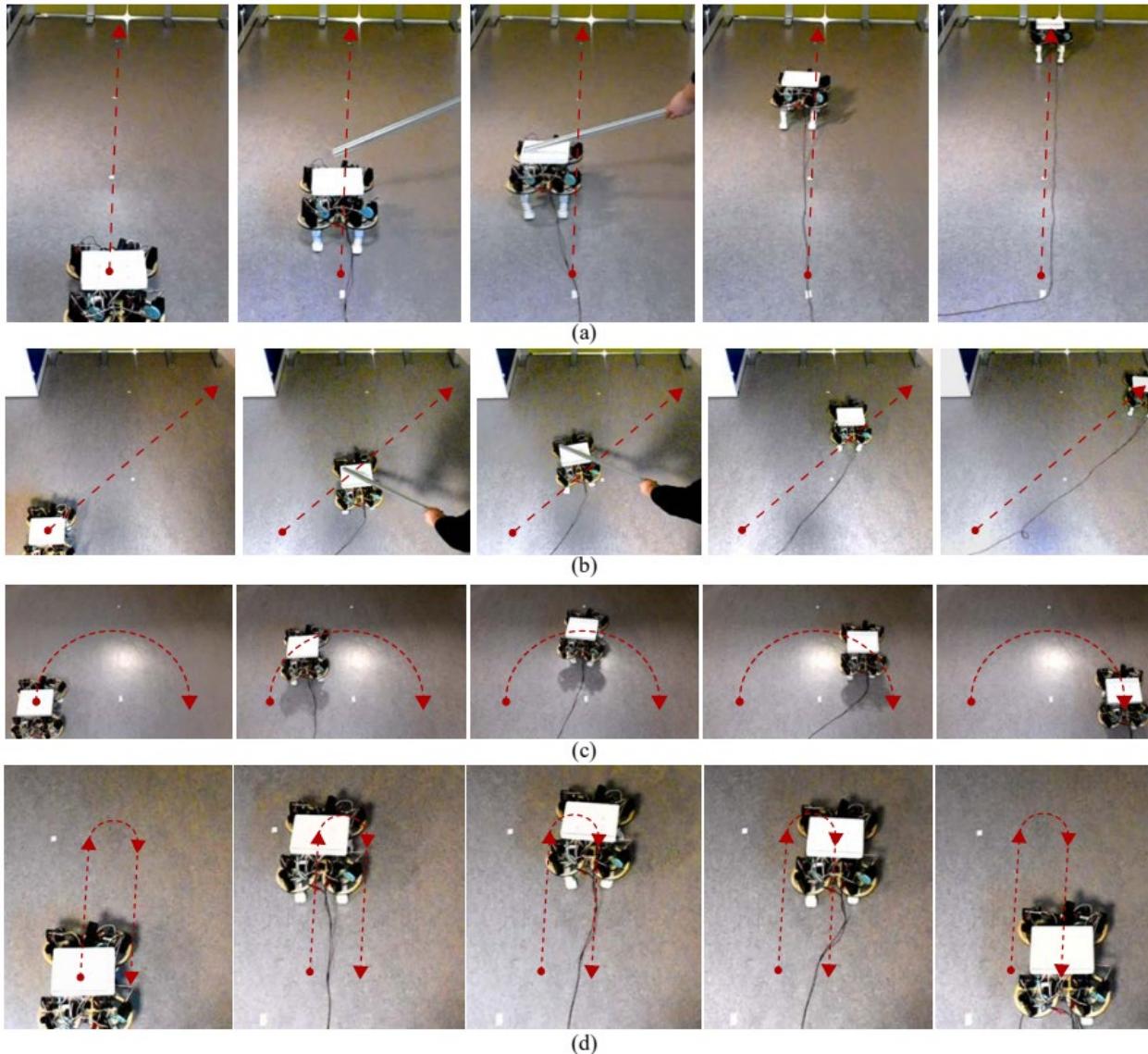


# Closed-loop Direction and Speed Control

Fixed compressed length



# Implementation



$$R = \frac{v}{\dot{\alpha}_r}$$



# Omnidirectional walking of a quadruped robot enabled by compressible tendon-driven soft actuators

Qinglei Ji<sup>1,2</sup>, Shuo Fu<sup>2</sup>, Lei Feng<sup>2</sup>, Georgios Andrikopoulos<sup>2</sup>,  
Xi Vincent Wang<sup>1</sup> and Lihui Wang<sup>1</sup>

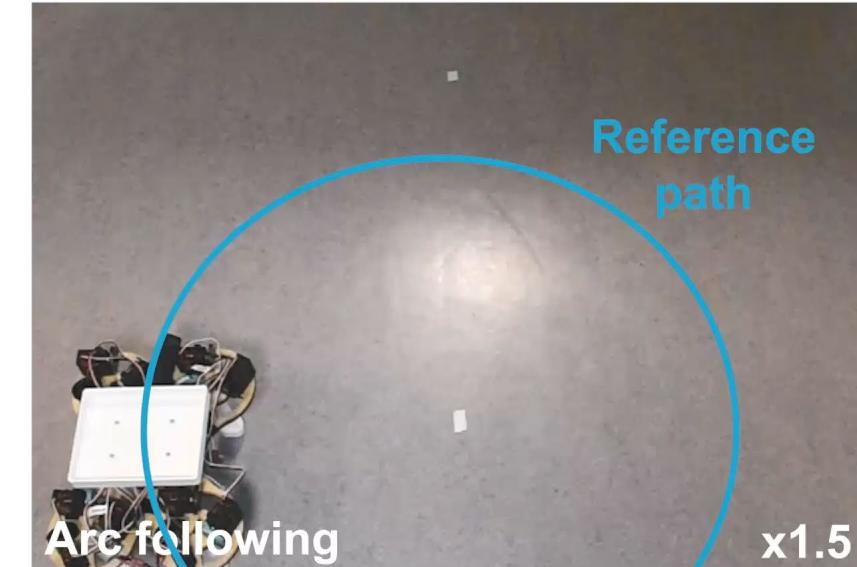
<sup>1</sup> Department of Production Engineering, KTH Royal Institute of Technology, Stockholm 10044, Sweden

<sup>2</sup> Department of Machine Design, KTH Royal Institute of Technology, Stockholm 10044, Sweden



Swedish  
Research  
Council

**xPres**  
Excellence in Production Research

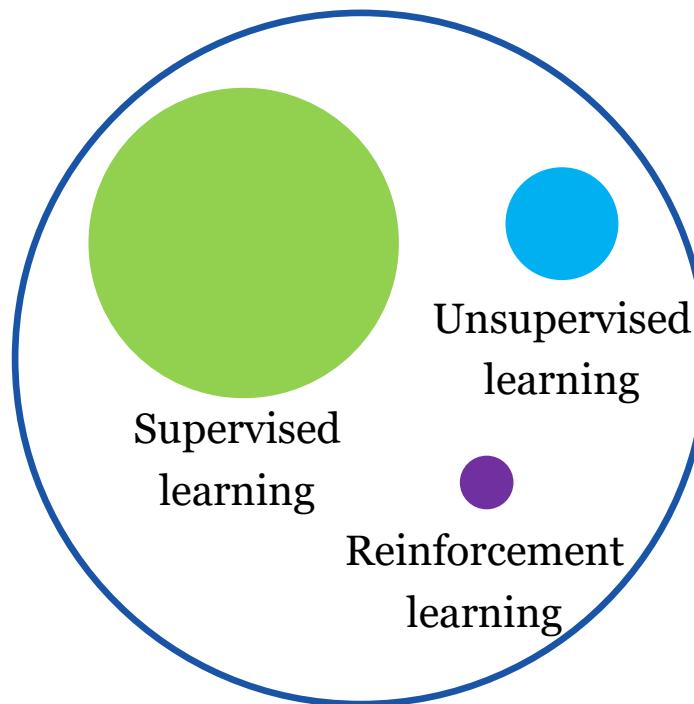


# Reinforcement Learning

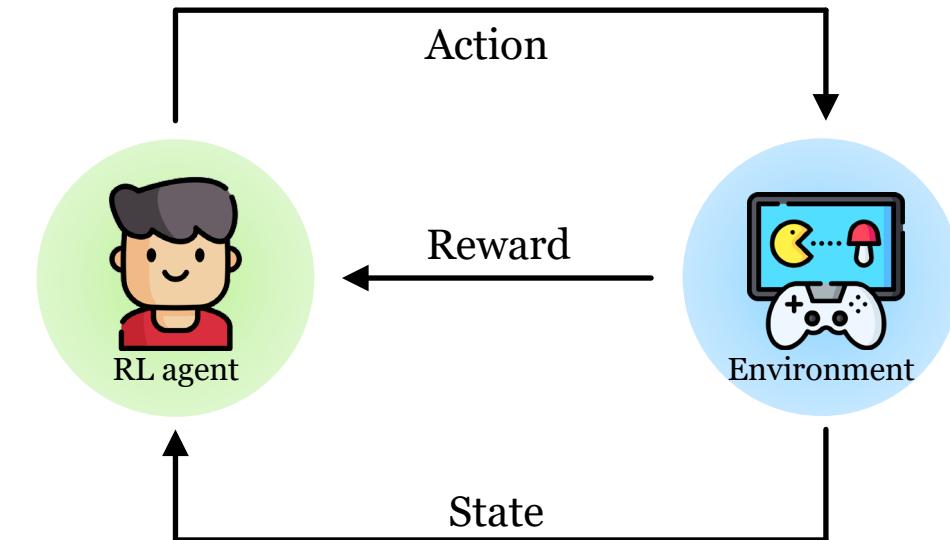
Learn with reward or penalty feedback.

Difference in design philosophy of reward in RL vs cost in optimal control:

- RL: Reward shaping is an art, often requiring intuition
- Optimal Control: Cost functions often derived from physical principles



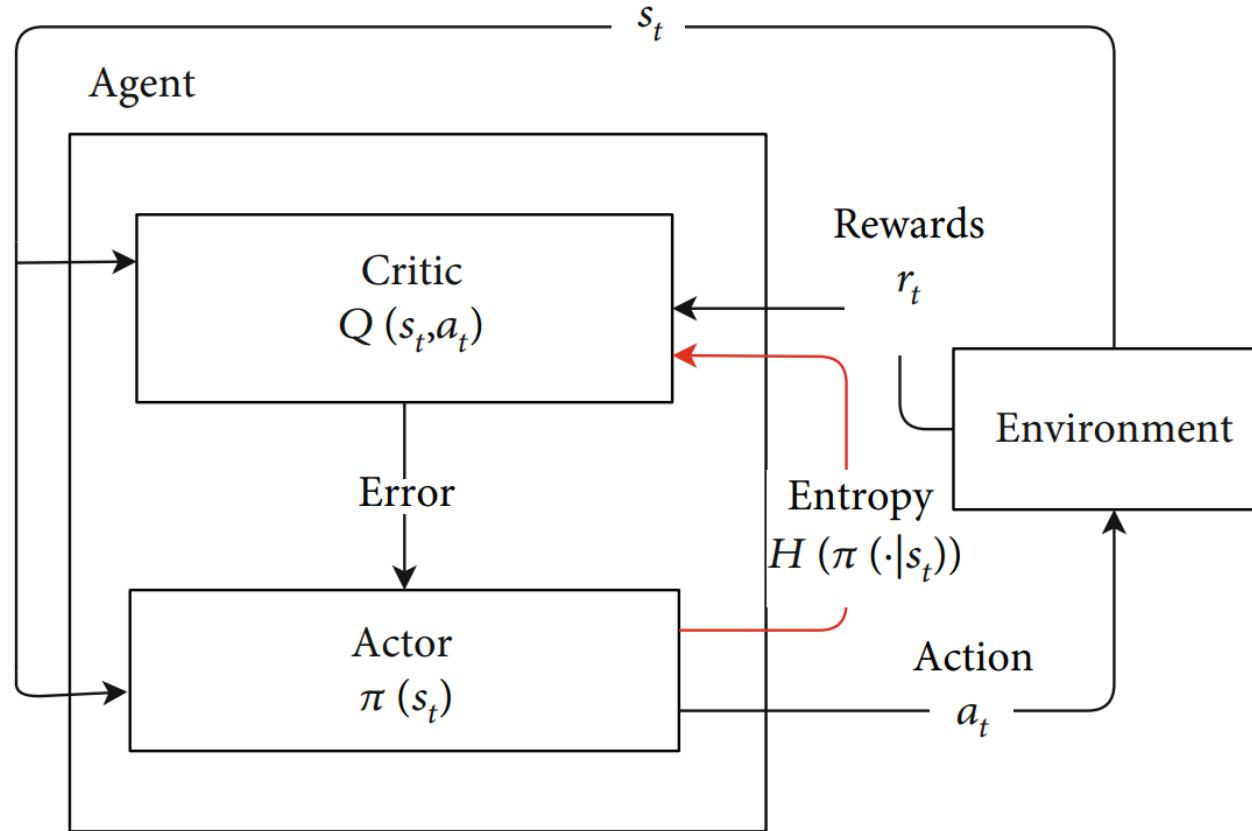
Classifications of AI techniques



Reinforcement learning

# Gait Learning for Soft Quadruped Robot

Soft Actor Critic (SAC) method

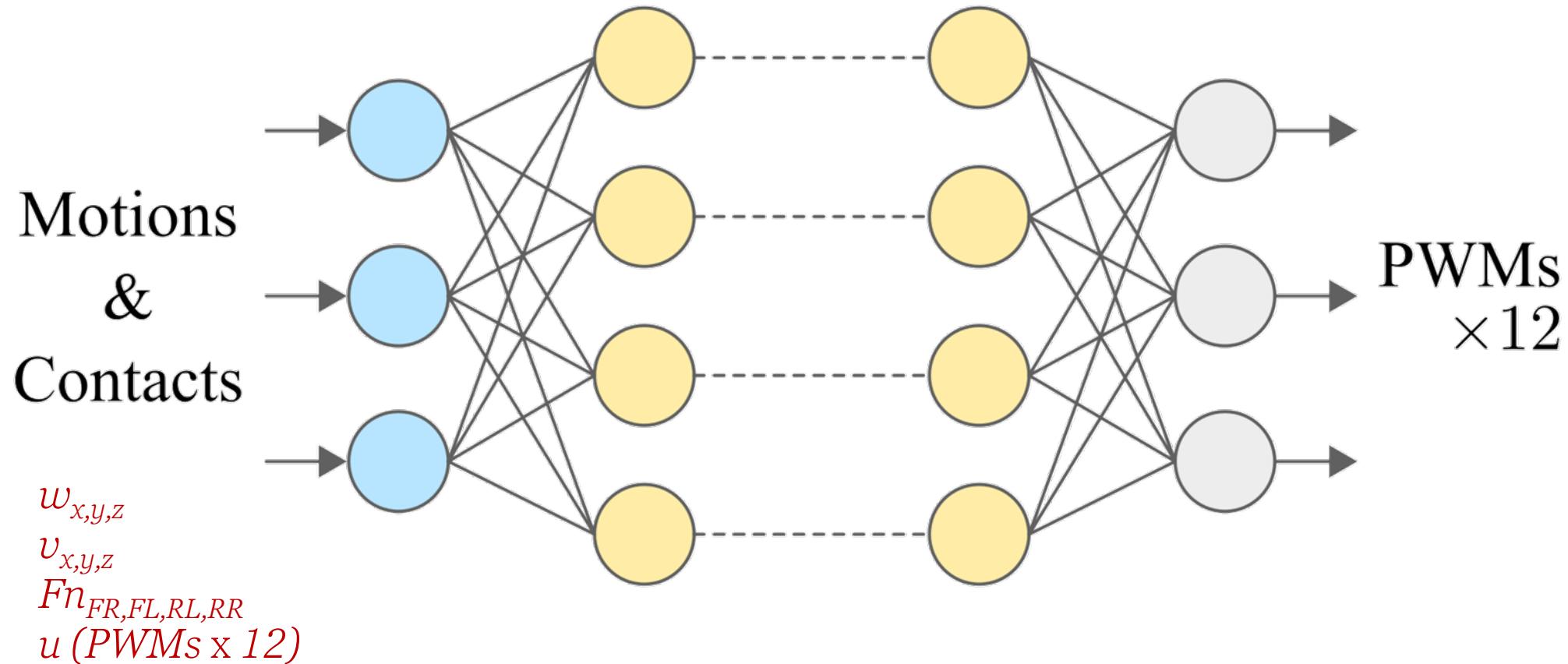


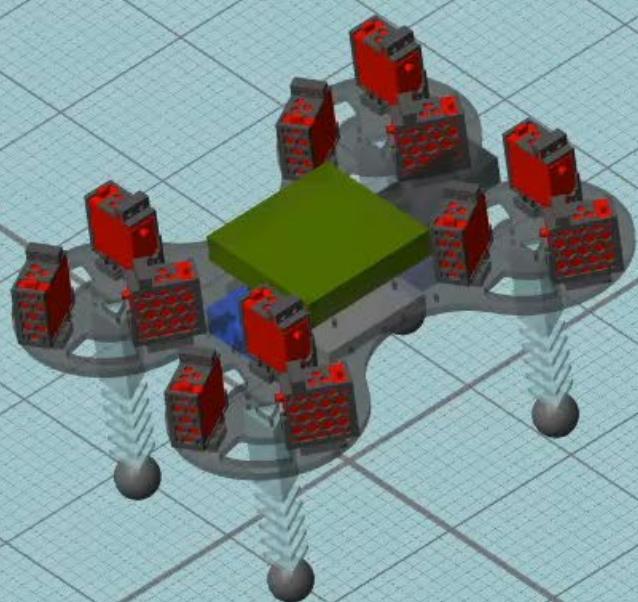
$$\pi^* = \arg \max_{\pi} \sum_t \mathbb{E}_{(s_t, a_t) \sim \rho_{\pi}} [r(s_t, a_t) + \alpha \mathcal{H}(\pi(\cdot | s_t))]$$

Haarnoja T, Zhou A, Hartikainen K, Tucker G, Ha S, Tan J, Kumar V, Zhu H, Gupta A, Abbeel P, Levine S. Soft actor-critic algorithms and applications. arXiv preprint arXiv:1812.05905. 2018 Dec 13.

# Gait Learning for Soft Quadruped Robot

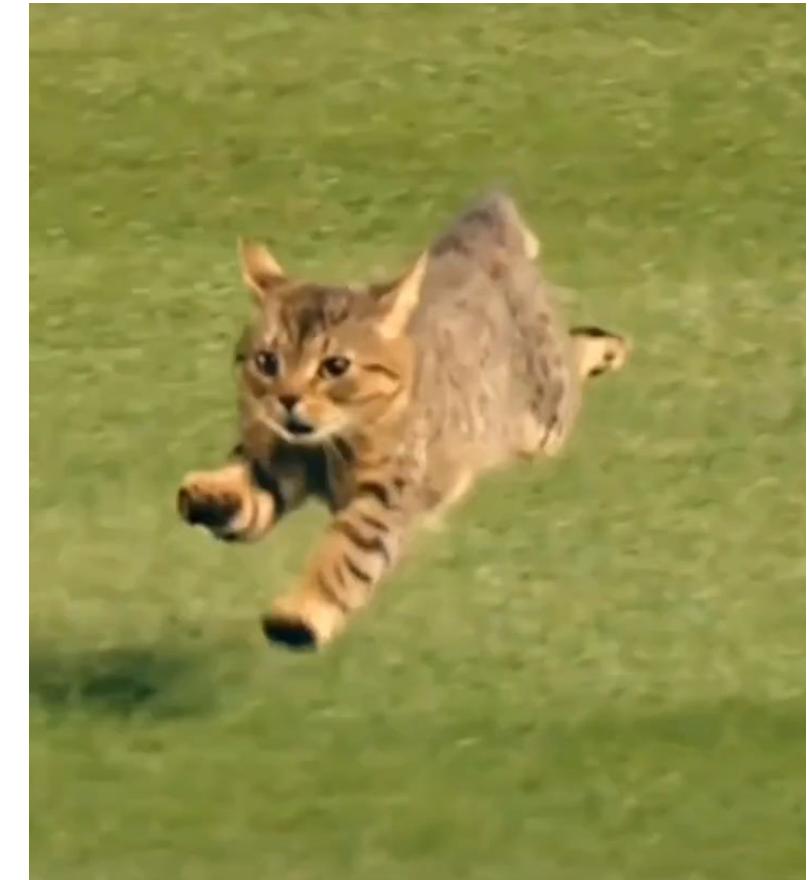
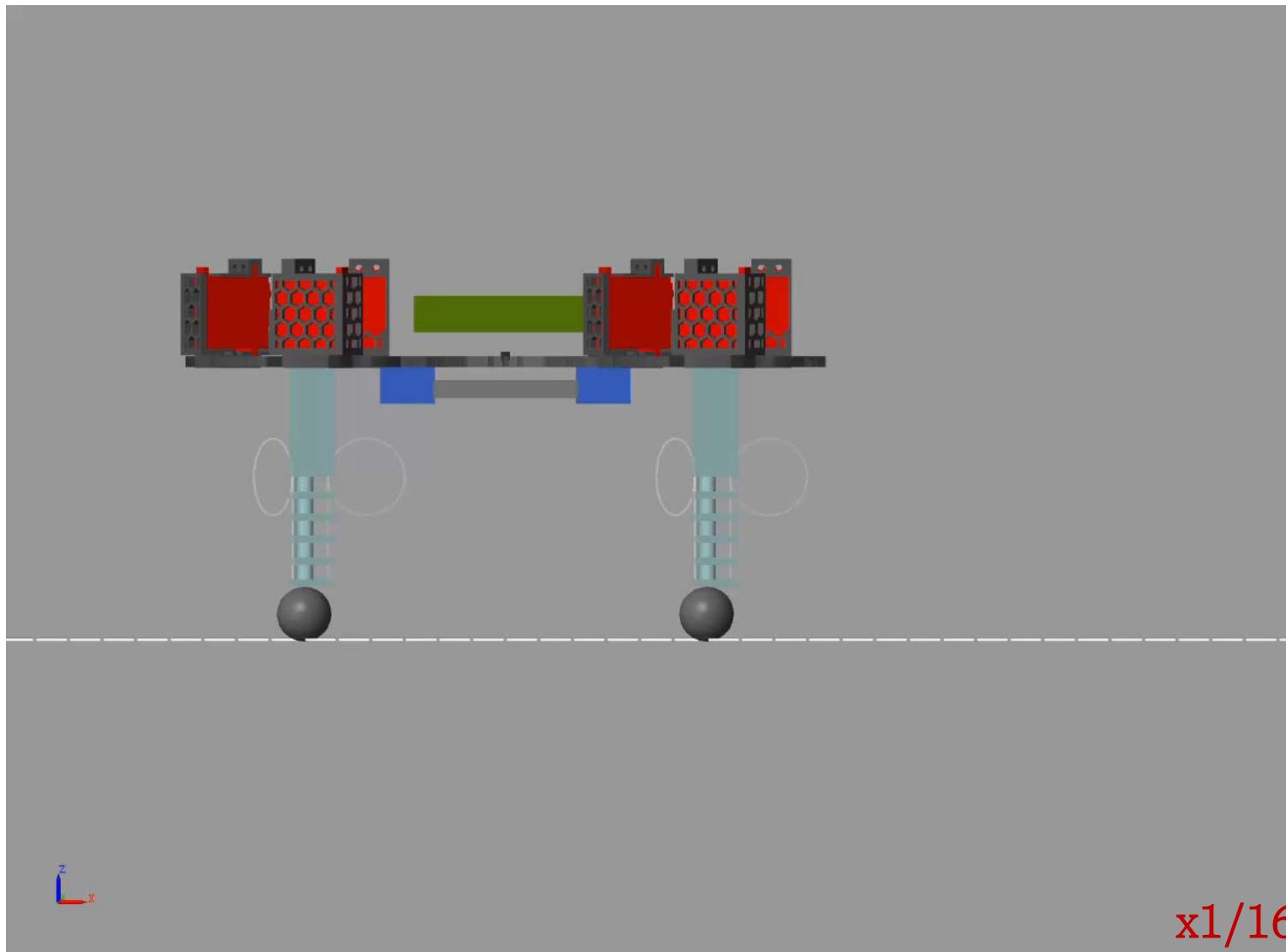
Actor network





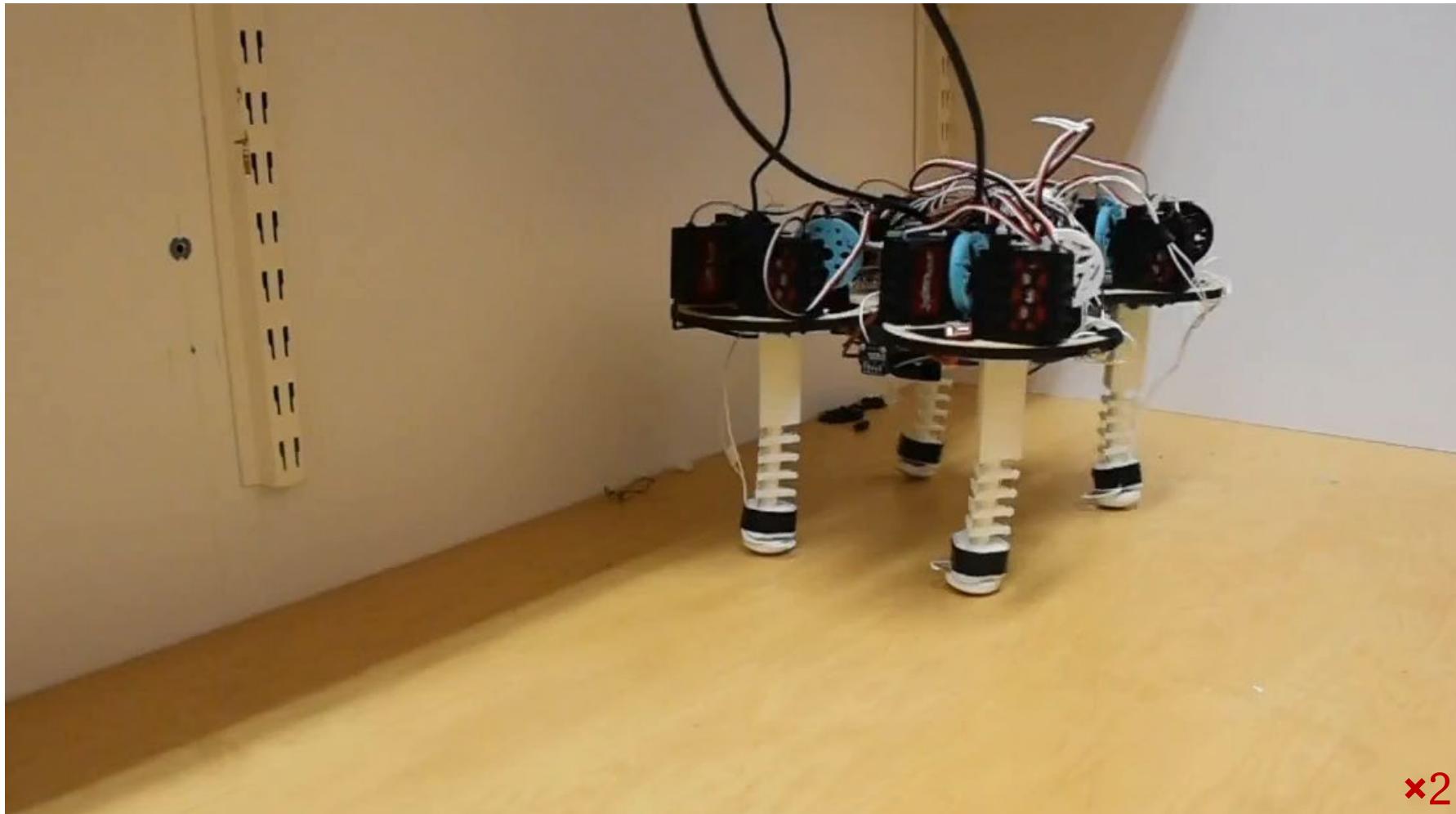
x1/4

# Gait Learning for Soft Quadruped Robot



# Implementation

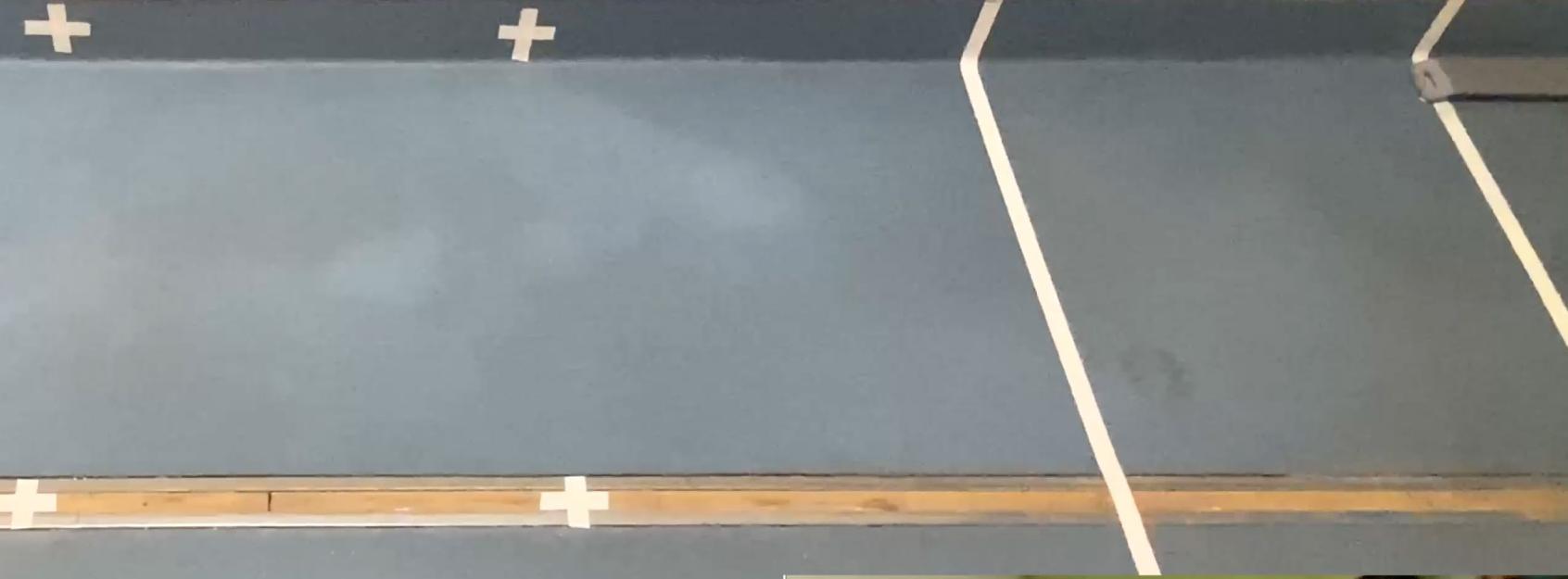
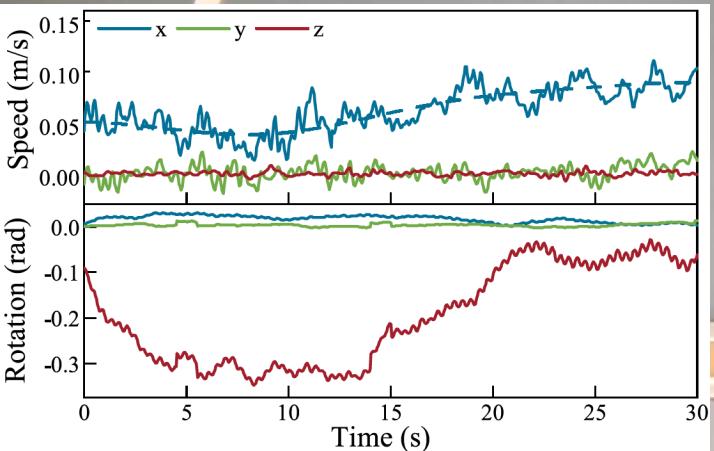
Sim2Real gap



## Solutions

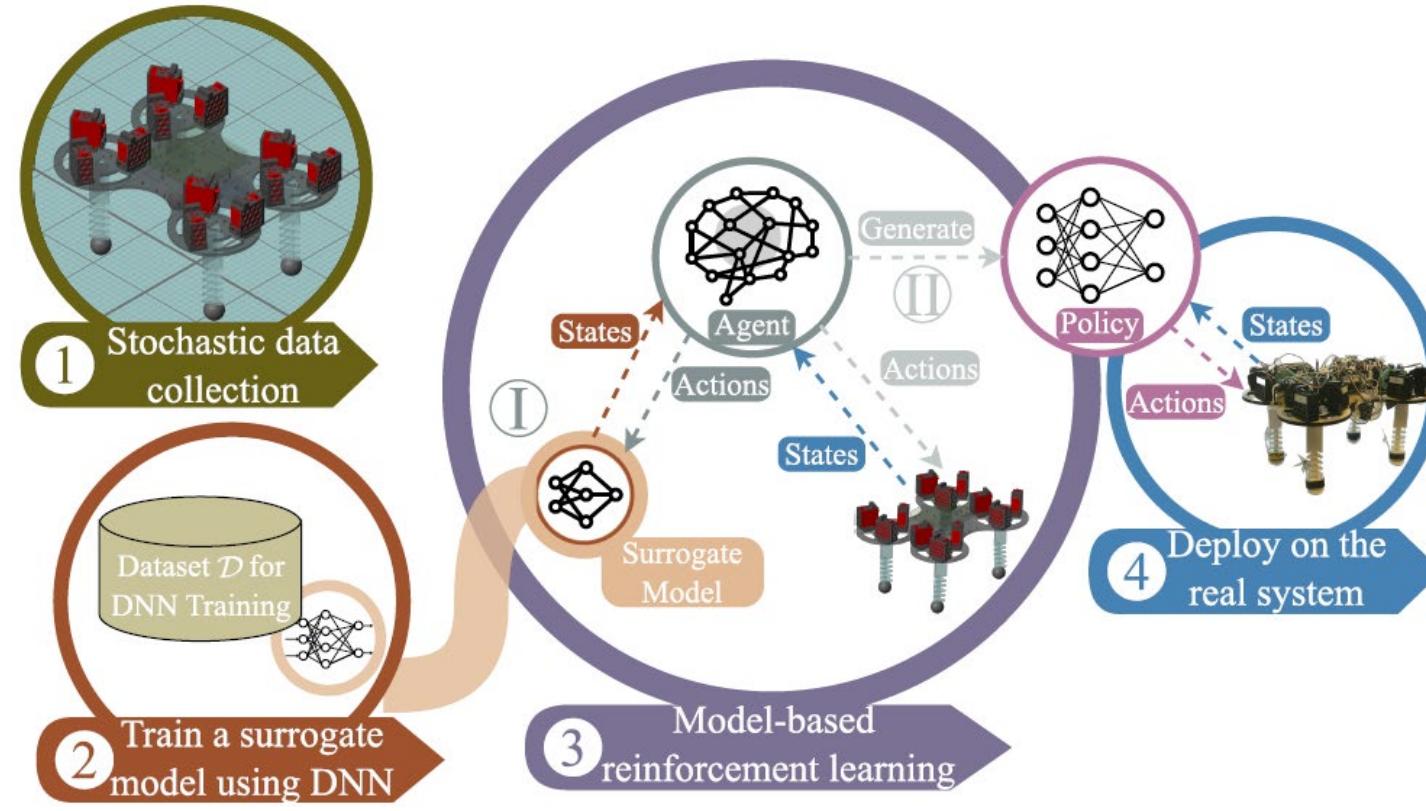
- ☒ Add random noises
- ☒ Change env. params.

×2



# Model-Based Reinforcement Learning

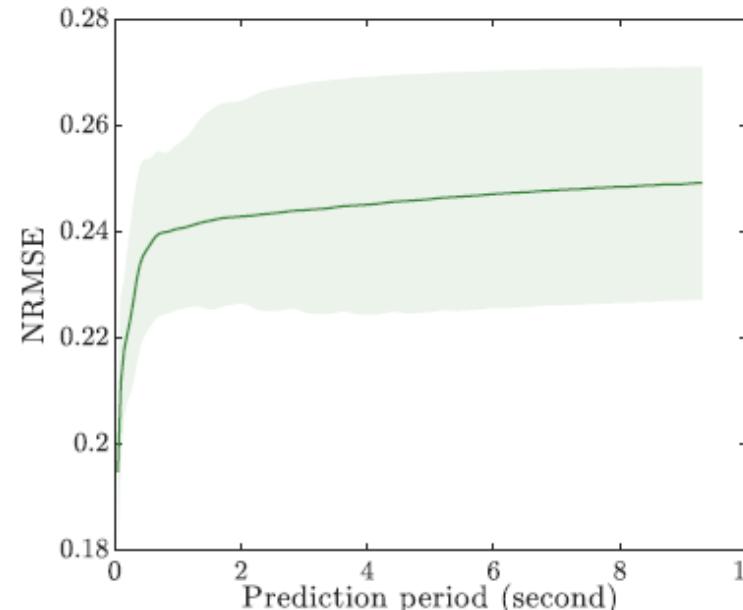
Training via simulation or real world is expensive



Niu, Xuezhi, Kaige Tan, and Lei Feng. "Optimal Gait Control for a Tendon-driven Soft Quadruped Robot by Model-based Reinforcement Learning." arXiv preprint arXiv:2406.07069 (2024).

# Surrogate Model

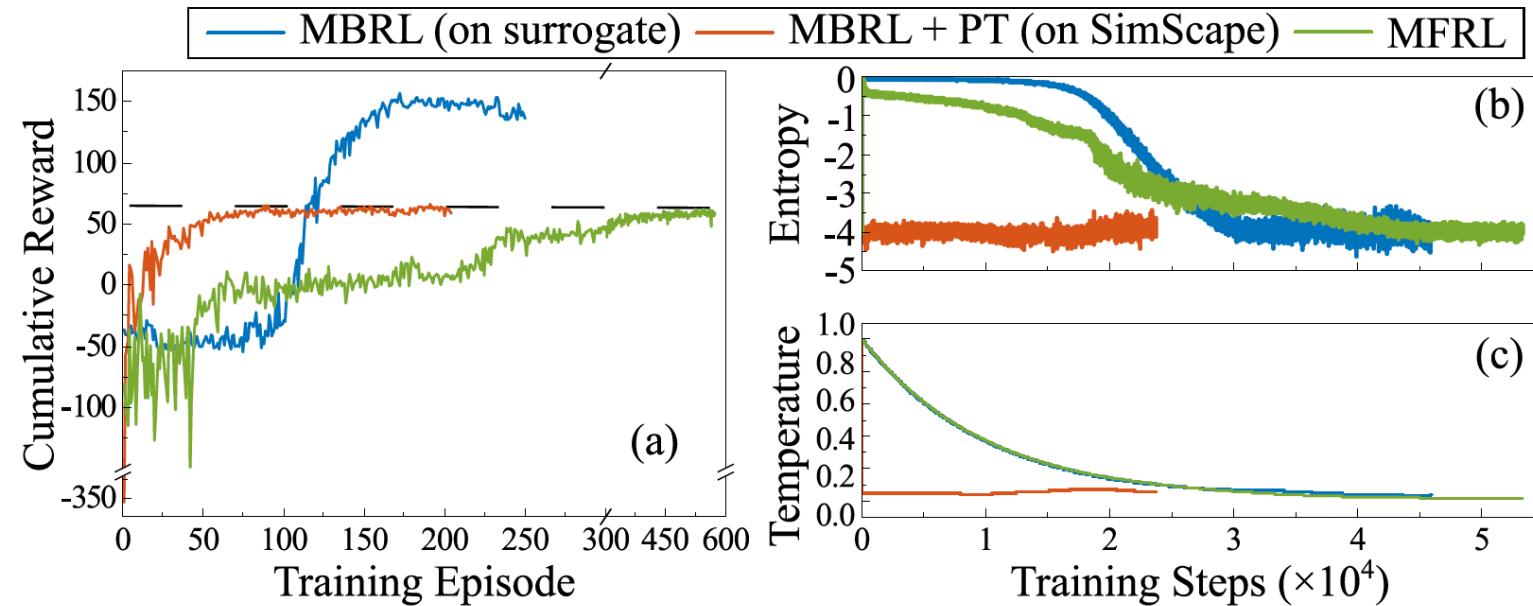
- Predict next state with current state and actions
- Precision is decreased when prediction is iterated for long term prediction
- DNN with three hidden layers (64, 128, 64)
- Supervised learning
- Long-term prediction



Prediction accuracy decreases for long term.

# MBRL + Post-training

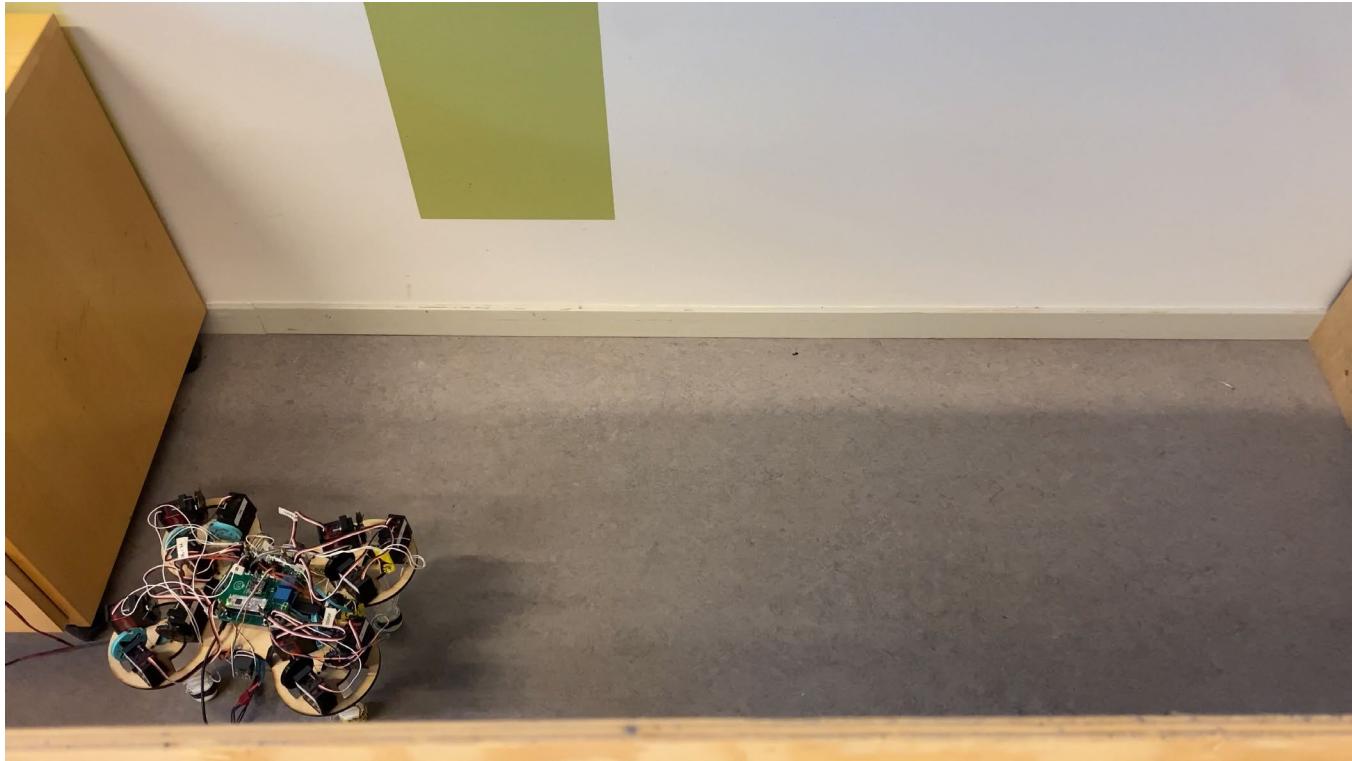
## Post-Training for Improving Control Quality



The training results in 0.2 m/s reference speed. (a) Cumulative reward with training episodes. Variations in (b) entropy and (c) temperature during the training process.

# Implementation

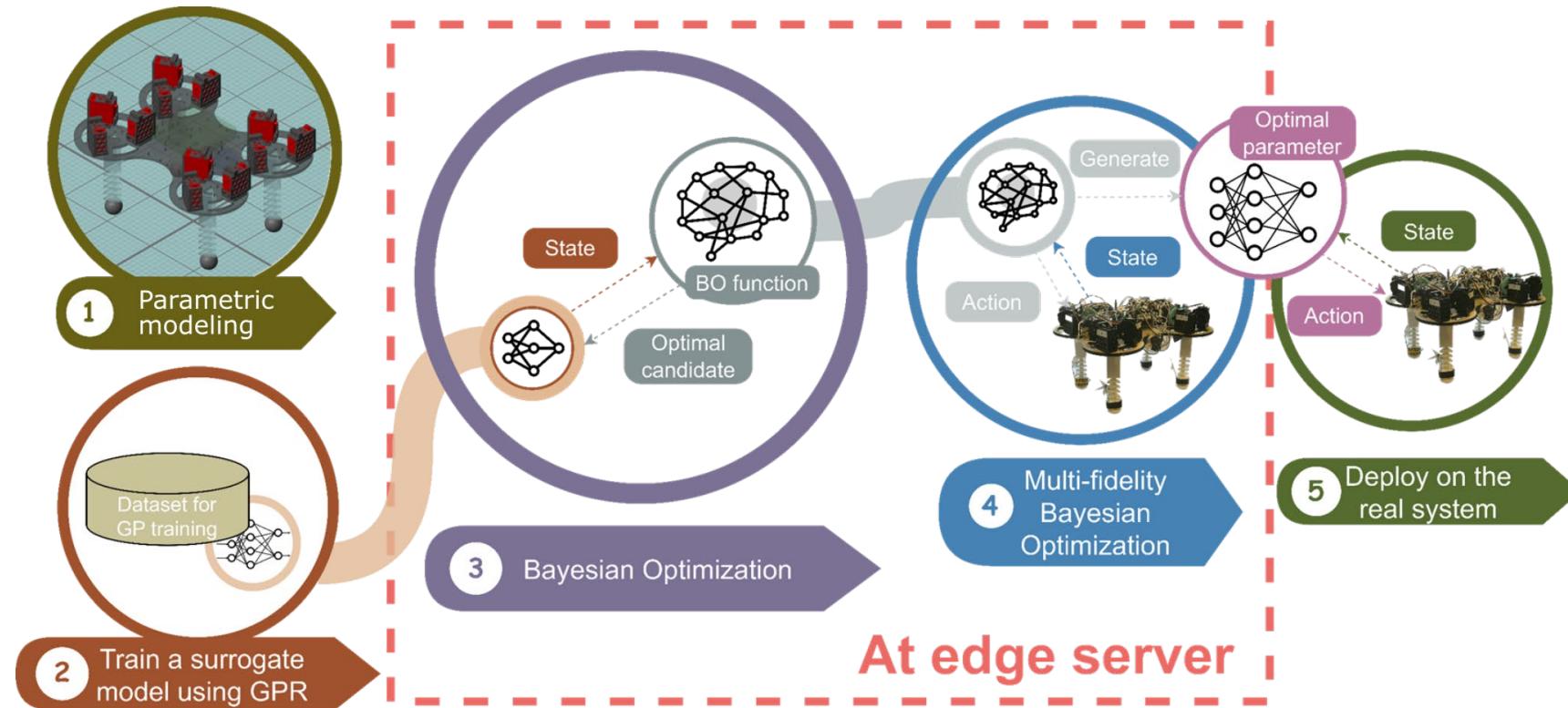
Great improvement on the training speed: 11 vs 48 hours



Similar stable walking speed with the identical environment

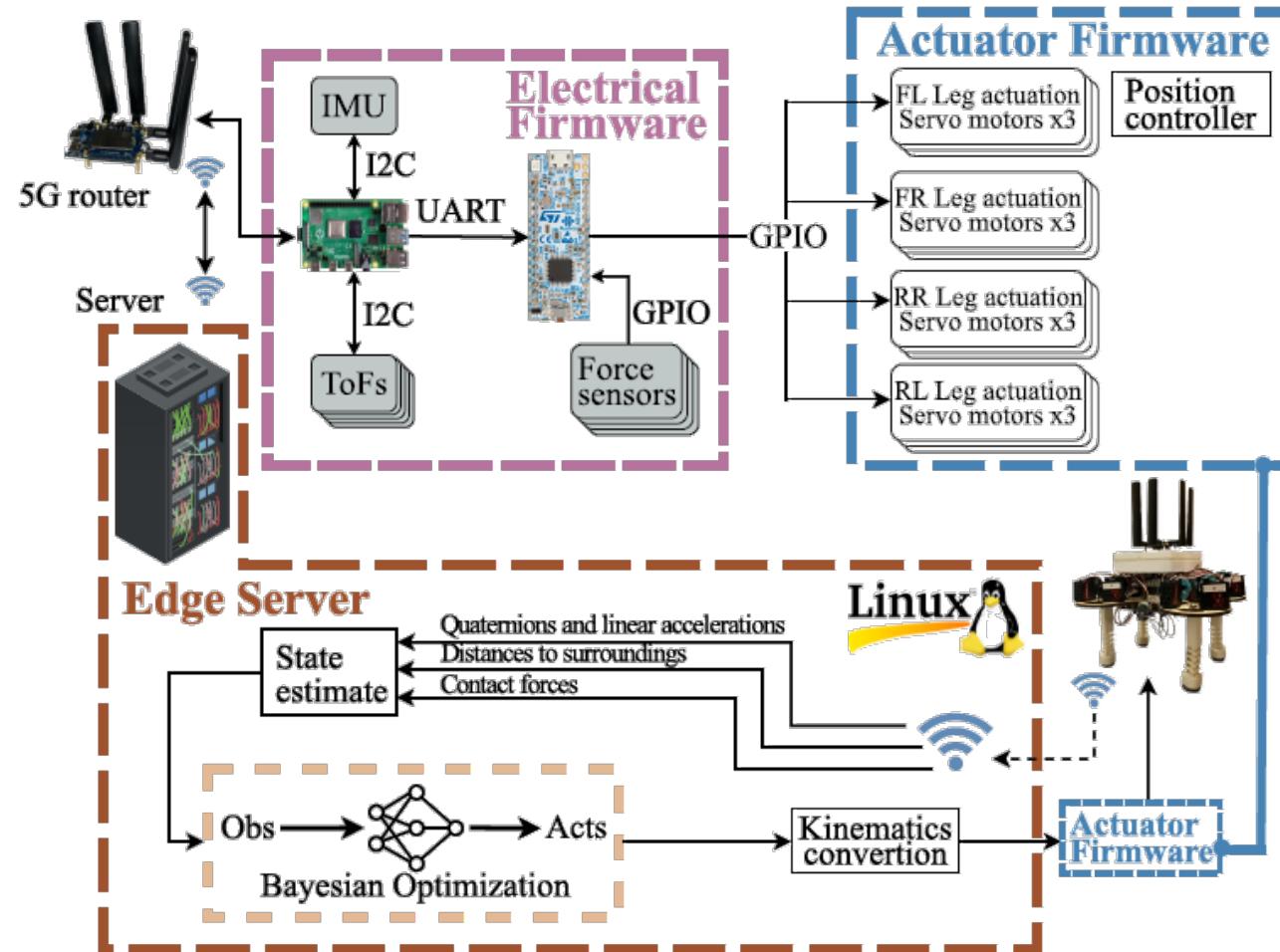
# Bayesian optimization with parametric model

Parametric model (CPG) from expert knowledge



# Edge Computing for Online Learning and Control

Offload computing to cloud



# Training iteration demos



Initial gait  
(0.046m/s)



Intermidiate gait during training  
(0.143m/s)



Optimal converged gait  
(0.215m/s)

# Final Remarks

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- Unified simulation, control, and learning environment.
- Trade-off between model accuracy *vs* simplified simulation for time-efficient learning.
- Learn from simulation and real world to overcome Sim2Real gap.
- Offload computing to cloud for intensive online learning tasks.

