

# MemToolbox tutorial

(This tutorial uses a beta version of the toolbox and was last updated on 8/15/2012.)

The MemToolbox is a collection of MATLAB functions for modeling visual working memory. In support of its goal to provide a full suite of data analysis tools, the toolbox includes implementations of popular models of visual working memory, real and simulated data sets, Bayesian and maximum likelihood estimation procedures for fitting models to data, visualizations of data and fit, validation tools, model comparison metrics, and experiment scripts.

Through a series of demonstrations, code for which can be found in the MemDemos folder, the following tutorial covers most of the toolbox's core functionality.

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## Demo 1: Mixture modeling in just two lines of code

While the MemToolbox can fit models to 2AFC and change detection data (Demo 9), to start the tutorial we will assume that you have collected data (or wish to collect data) using a continuous partial report task with colors. In such a task, observers see the stimulus display, and then after a delay are asked to report the exact color of a single item. Error is quantified as the distance between the responses and the correct answer in degrees on the color wheel.

continuous partial report



The simplest way to use the MemToolbox with such data is through `MemFit`, a function that houses much of the toolbox's functionality under one roof. To use `MemFit` with continuous report data, first specify your data as a vector of errors, one for each trial, in units of degrees on the color wheel. These errors should fall between  $-180$  and  $180$ .

```
>> errors = [-89, 29, -2, 6, -16, 65, 43, -12, 10, 0, 178, -42, 52, 1, -2];
```

Next, call `MemFit` on the error vector.

```
>> MemFit(errors);
```

The toolbox will now run through its analysis of your data, showing you a histogram of the errors, the name and parameterization of the model it is fitting to the data, and the maximum a posteriori and credible intervals of the model parameter values inferred from the data. By default, the MemToolbox fits the standard mixture model of Zhang and Luck (2008) to the data.

```
Error histogram:  -180 _____.'_'_____ +180
                  Model:  Standard mixture model
                  Parameters:  g, sd
```

```
Just a moment while MTB fits a model to your data...
```

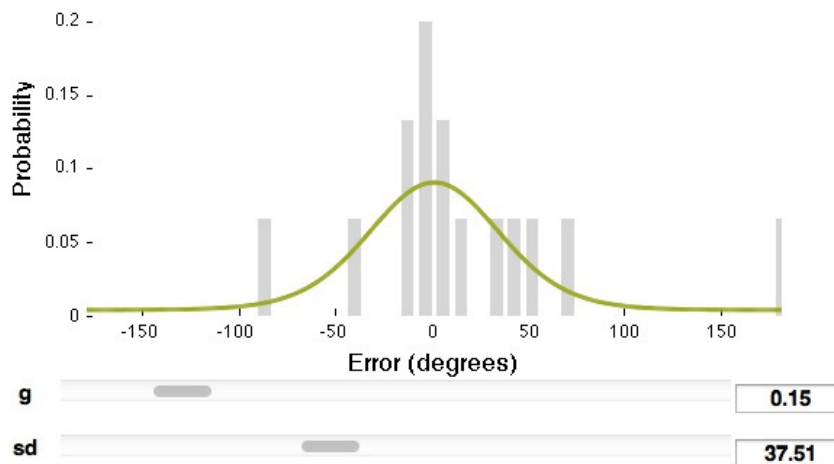
```
...finished. Now let's view the results:
```

parameter	MAP estimate	lower CI	upper CI
g	0.151	0.027	0.623
sd	37.507	13.831	65.613

Then it will ask whether you'd like to see the fit:

```
Would you like to see the fit? (y/n):
```

If you respond in the affirmative (by entering the letter `y` and hitting the return key), you'll find an interactive visualization that lets you manipulate the values of the model parameters and see the impact on the predicted distribution of data. As you change the values, notice that the prediction line changes color – it gets less saturated and more gray as you choose values that make the data less likely.



Hooray! In just two lines of code, you've performed mixture modeling using the MemToolbox. For now, say no ('n') to the next question the toolbox asks you about seeing more detailed model fit information. We'll get to those in some of the later demos.

## Demo 2: Choosing a different model

In the previous example, the toolbox picked a model on your behalf, but you can choose a different model if you would like. A full listing of available models can be found by entering `help MemModels` at the command line. One of the available models extends the standard mixture by allowing a bias term, such that the central tendency of the data isn't fixed at zero. You can access this model by using `WithBias()` together with the `StandardMixtureModel`:

```
>> model = WithBias(StandardMixtureModel);
```

To use this model, first specify your data:

```
>> errors = [-89, 29, -2, 6, -16, 65, 43, -12, 10, 0, 178, -42, 52, 1, -2];
```

Then call `MemFit`:

```
>> MemFit(errors, model);
```

The toolbox will then walk through the same analysis as before using the model that you picked.

## Demo 3: Specifying your data as a structure

The two models we have seen cared only about the errors made by the participant on the task. Other models require auxiliary data to make their predictions. For example, the

swap model advocated by Bays, Catalao and Husain (2009), which holds that participants sometimes mistakenly report the value of the other items in the display instead of the target item. This model requires not only the errors made on each trial but also the distances of the non-target items from the target value. (The swap model is available in the toolbox under the name `SwapModel`). Thus, to use this model, you need to tell the model the colors of the distractor items. These data, the errors and the non-target values, should be bundled together into a structure:

```
>> data.errors = [-89, 29, -2, 6, -16 ...
>> data.distractors = [-10, 2, -100, 163, 42 ...
```

The help file for each model lists its required fields:

```
>> help SwapModel

SWAPMODEL returns a structure for a three-component model with guesses and
swaps. Based on Bays, Catalao, & Husain (2009) model. This is an extension
of the StandardMixtureModel that allows for observers' misreporting
incorrect items.

In addition to data.errors, the data struct should include:
    data.distractors, Row 1: distance of distractor 1 from target
    ...
    data.distractors, Row N: distance of distractor N from target
    ...
```

Let's test the model. Rather than making you type out a long vector of errors and a full matrix of distractor values, we'll use one of the datasets that comes loaded with the toolbox. These can be accessed through the function `MemDataset`, which returns a structure array with fields containing different aspects of the data. For example, data set #3 includes a vector of errors and distractor values for each trial (in addition to the set size, `n`, and the delay duration, `time`). This is precisely what you need to use the swap model:

```
>> data = MemDataset(3)

data =

    errors: [1x4000 double]
  distractors: [2x4000 double]
           n: [1x4000 double]
          time: [1x4000 double]
```

Now, instead of feeding `MemFit` the error vector, you can give it the entire data structure at once:

```
>> MemFit(data, SwapModel);
```

The toolbox will now run through the usual analysis. You may notice some new things in the output of `MemFit`. We'll explain these in demo #4.

## Demo 4: Digging deeper into MemFit()

Let's peek under the hood at the functions that underlie `MemFit`. By default, the `MemToolbox` uses Markov Chain Monte Carlo (MCMC) to do model fitting. MCMC

samples parameter values in proportion to how well they describe the data and how well they match the prior. The distribution of these parameter values is used to estimate the true underlying model and to express our confidence in that estimate. In this demo, we'll show you how to read the various plots produced by `MemFit` that relate to MCMC. Once you've mastered the basics from demos 1–3, we recommend the following as a standard workflow when using the toolbox.

Start by loading in a dataset, either yours or one from the toolbox:

```
>> data = MemDataset(1);
```

Now run `MemFit` using the `StandardMixtureModel`. This time, assign the output of `MemFit` to a variable and don't suppress printing with a semicolon.

```
>> fit = MemFit(data, StandardMixtureModel)
```

First, we see the usual histogram, model name, and parameterization:

```
Error histogram:  -180 _____.'.'_____ +180
                  Model:  Standard mixture model
                  Parameters:  g, sd
```

There should be no surprises here. In the off chance that you have specified your data in an incorrect format (e.g., by using radians instead of degrees or by coding errors in the range  $[0,360]$ ), the toolbox will try its best to massage your data into the correct format, always throwing a warning letting you know what it has done. Then the toolbox announces:

```
Just a moment while MTB fits a model to your data...
Running 3 chains...
```

This refers to the “chains” of Markov Chain Monte Carlo, which you can read about on Wikipedia ([http://en.wikipedia.org/wiki/Markov\\_chain\\_Monte\\_Carlo](http://en.wikipedia.org/wiki/Markov_chain_Monte_Carlo)). The default MCMC algorithm used by MemToolbox uses multiple chains whose starting values are specified in the model file (and modifiable), and it continues running them until they have converged to a similar range of parameters. Every 200 steps, the toolbox will update you on its progress:

```
... not yet converged (200)
```

and then at some point, depending on the model, the chains will converge:

```
... chains converged after 400 samples!
```

The final estimate is based on samples taken after convergence:

```
... collecting 3000 samples from converged distribution
```

The toolbox then analyzes these samples, returning the MAP (maximum a posteriori) estimate and credible intervals:

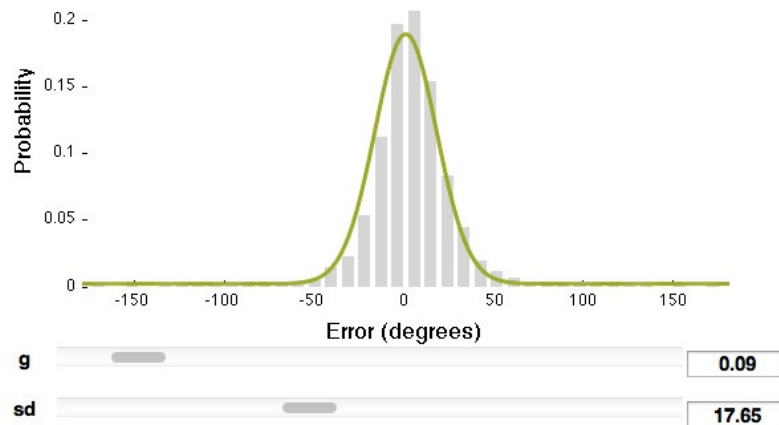
```
...finished. Now let's view the results:

parameter  MAP estimate  lower CI  upper CI
```

g	0.093	0.078	0.106
sd	17.638	16.940	18.377

Would you like to see the fit? (y/n): y

Depending on your interests, the maximum a posteriori (MAP) estimates and credible intervals might constitute an answer to your question. Even so, the next step is to visualize the model fit:

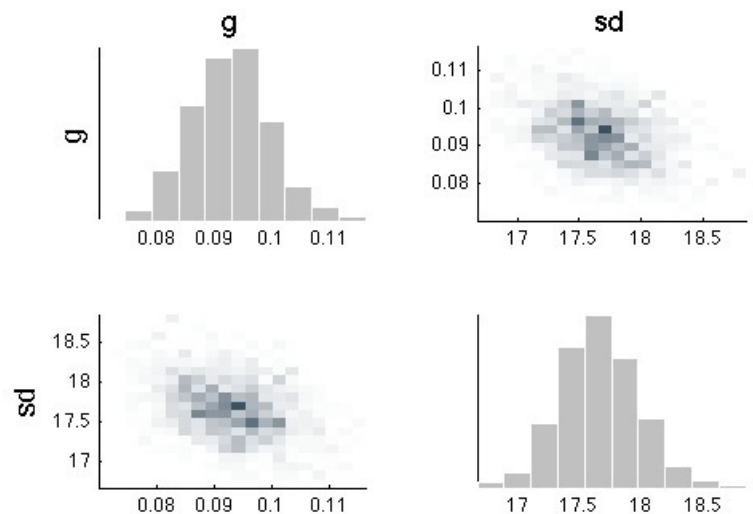


This is mostly useful for familiarizing yourself with the behavior of the model and for recognizing gross inconsistencies between the model and data. At first pass, this one looks okay.

Next, the toolbox will ask:

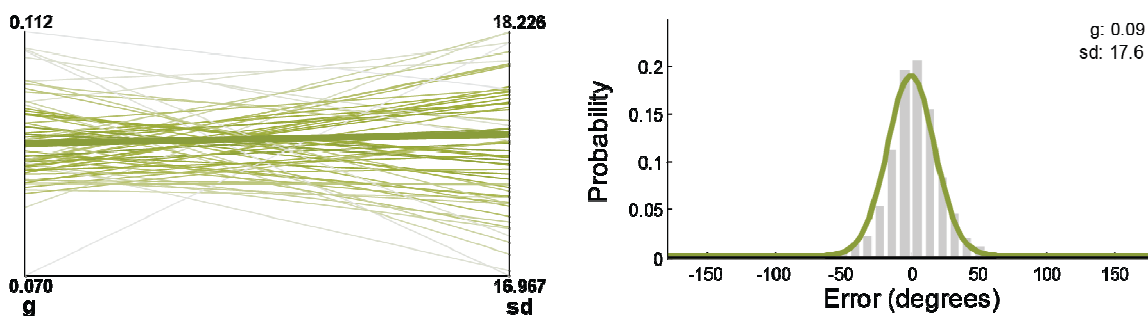
Would you like to see the tradeoffs between parameters, samples from the posterior distribution and a posterior predictive check? (y/n): y

Answering in the affirmative will bring up three plots:



The first shows the full posterior distribution for each parameter and a heat map for each pair of them. This can be useful for diagnosing correlations between parameters and for understanding how much the data constrain the parameters:

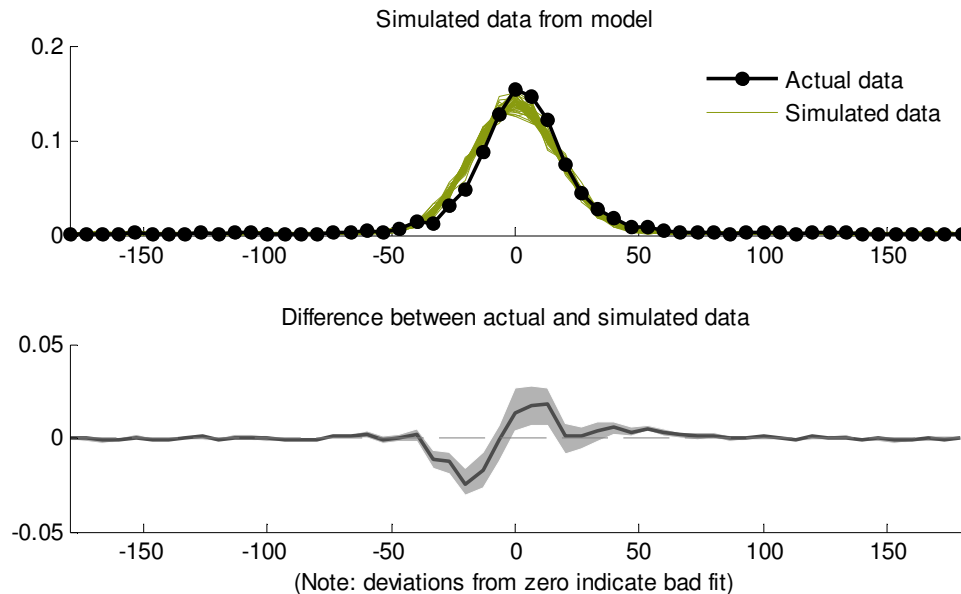
For example, in the standard Zhang & Luck (2008) mixture model, there is a correlation between the guess rate parameter ( $g$ ) and the standard deviation parameter ( $sd$ ). The data is equally consistent with a slightly higher guess rate and slightly lower standard deviation, or with a slightly lower guess rate and slightly higher standard deviation. This is apparent in the negative slope of the heat map plots in the bottom left and upper right quadrant.



The second plot produced by `MemFit` shows the parameters of the model in a parallel coordinates plot ([http://en.wikipedia.org/wiki/Parallel\\_coordinates](http://en.wikipedia.org/wiki/Parallel_coordinates)), along with a visualization of their fit to the data. Each line on the parallel coordinates plot corresponds to a reasonable set of parameters for fitting the data (e.g., a sample from the posterior on the parameters given the data). The lines are colored such that more likely parameter combinations get darker colors, and less likely parameter values appear more gray. The negative correlation between the parameters of this particular model is indicated by the fact that the lines tend to have slopes that differ from zero (e.g., high values on one parameter give low values on the other, and vice versa). A positive correlation would be shown by the lines being mostly parallel between the left and right sides, meaning high values of one parameter give high values of the other.

With only two parameters, the parallel coordinates plot does not provide as much information as the scatter plots and heat maps in the first figure. However, when more parameters are present, parallel coordinates plots allow you to simultaneously understand how all of the parameters relate to each other, rather than just how pairs of parameters relate; we will explore this later in the tutorial.

This plot is also interactive. Try clicking one of the lines with a high value of guess rate ( $g$ ). The plot of the data on the right will redraw with the new parameter values you chose. Now try clicking on one of the lines with a low value of guess rate ( $g$ ). Can you see why both provide equally good fits?



The third plot shows the *posterior predictive distribution*—the model’s residual. The first two plots provide ways of examining which parameter values of the model provide the best fits. This figure instead shows whether or not the model—with its best parameter values—provides a good fit to the data. In particular, we simulate ‘fake’ data from the posterior of the model and ask whether it looks like the real data. If the model provides a good fit, then the data that is simulated using the best fit parameters (the posterior) will closely resemble the actual data. If the model is systematically wrong in some way, this should be (visually) evident as a mismatch between the simulated and actual data. The top of the plot shows the data in black, and the simulated data in green. They should be on top of each other if the model provides a good fit. The bottom of the plot shows the difference between the two, both on average (line) and with 95% confidence intervals (gray shading). Any regions where the gray shading does not include zero are regions where the model is systematically incorrect in its predictions.

The current data shows an example of a poor fit – this observer’s data is clearly shifted to the right of the model data. We’ll explore this next in the section on model comparison.

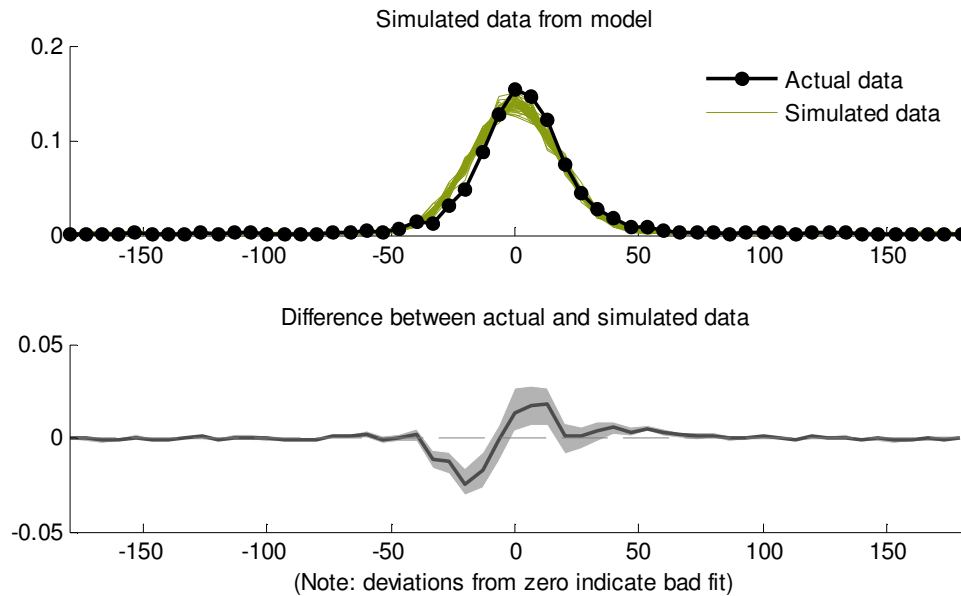
### Demo 5: Model comparison

In this demo we’ll cover model comparison. Let’s start by using the standard mixture model on the first built-in dataset, as in Demo 4:

```
>> data = MemDataset(1);
>> model1 = StandardMixtureModel();
>> MemFit(data,model1)
```

We can see that the residuals for this model show that it does not fit well:

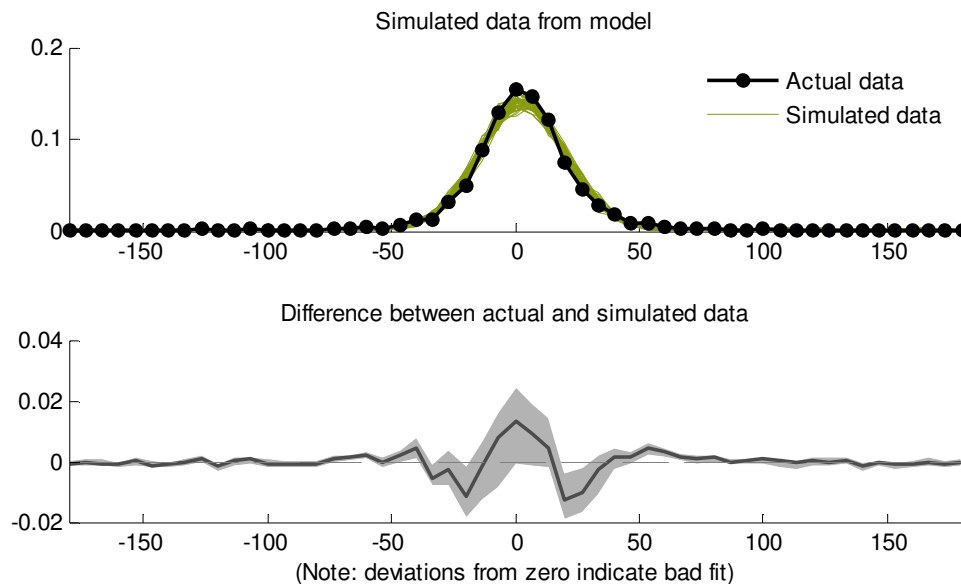




In particular, it looks like the model overestimates counterclockwise error and underestimates clockwise errors. This particular subject had a clockwise-bias in their responses, and the `StandardMixtureModel` is always centered around zero. To fix this, we can use a different model. In particular, we can use the `StandardMixtureModel` model, but allow a bias parameter to shift the model's center point:

```
>> model2 = WithBias(StandardMixtureModel);
>> MemFit(data,model2)
```

This model fits much better than the one with no bias:



However, we can see that this model also seems to be systematically incorrect. In particular, the data appear to be ‘peakier’ than this model suggests they should be. Even so, this model still appears to be an improvement on the model that assumes no bias. How can we quantify this? MemToolbox has built-in model comparison metrics. In particular, simply calling `MemFit` with more than one model automatically compares them:

```
>> MemFit(data, {model1, model2})
```

MemToolbox compares the models using six different metrics, including the log likelihood, AIC, AICc, BIC, Bayes factor (and posterior odds of the models) and DIC. It also provides (brief) ideas of what direction is preferable for each metric.

The `MemFit` command should give the following output:

```
You've chosen to compare the following models:
```

```
Model 1:    Standard mixture model
Parameters:  g, sd

Model 2:    Standard mixture model with bias
Parameters:  mu, g, sd
```

```
Just a moment while MTB fits these models to your data...
```

Initially the toolbox will show you the log-likelihood, AIC, AICc and BIC:

```
Computing log likelihood, AIC, AICc and BIC...
```

```
The log likelihood of the parameters given the data.
```

```
model  Log likelihood
-----
1      -14429.61
2      -14396.70
1:2    -32.91
Preferred model: 2 (Standard mixture model with bias)
```

The Akaike Information Criterion is a measure of goodness of fit that includes a penalty term for each additional model parameter. Lower AIC denotes a better fit. To compare models A:B, look at the difference  $AIC(A) - AIC(B)$ . Positive values provide evidence in favor of model B, negative in favor of model A.

```
model  AIC
-----
1      28863.23
2      28799.41
1:2    63.82
Preferred model: 2 (Standard mixture model with bias)
```

The corrected Akaike Information is the same as the AIC, but it includes a correction for finite data. It can be interpreted in the same way.

```
model  AICc
-----
1      28863.23
2      28799.42
1:2    63.81
Preferred model: 2 (Standard mixture model with bias)
```

The Bayesian Information Criterion is similar to AIC, with different assumptions about the prior of models, and thus a more stringent penalty for more complex models.

```
model      BIC
-----
1          28875.32
2          28817.55
1:2        57.77
Preferred model: 2 (Standard mixture model with bias)
```

**You will then be asked if you wish to compare the models using DIC. Answer 'y'.**

Would you like to compute the DIC (note that this can be slow, since it requires running MCMC on each model)? (y/n): y

Computing DIC...

Comparing 2 models by DIC:  
- Sampling from model 1: Standard mixture model  
- Sampling from model 2: Standard mixture model with bias

The Deviance Information Criterion is a generalization of the AIC and BIC that includes a penalty for the effective number of parameters, estimated from the dispersion in the posterior of the models.

```
model      DIC
-----
1          28869.51
2          28805.39
1:2        64.12
Preferred model: 2 (Standard mixture model with bias)
```

**You will then be asked if you wish to compare the models using Bayes factors ('y').**

Would you like to compute an approximate Bayes Factor? Note that the Bayes Factor is heavily dependent on the prior in order to understand how flexible each model is; it is thus important that before examining Bayes factors you carefully consider the priors for your models. If you wish to specify a more concentrated prior to be used for Bayes factor calculation but not for inference, you can specify a `model.priorForMC` in addition to a `model.prior`. Also note that Bayes Factor calculations are slow. (y/n): y

Computing Bayes Factors...  
Calculating posterior samples for model 1: Standard mixture model  
Calculating posterior samples for model 2: Standard mixture model with bias  
Calculating likelihoods for model 1: Standard mixture model  
Calculating likelihoods for model 2: Standard mixture model with bias

When comparing models A:B, the log Bayes factor for model A is the change in log odds in favor of that model after seeing the data, with positive values ruling in favor of model A. Typically, a log Bayes factor between 0 and 0.5 is not worth more than a mention, one between 0.5 and 1 is substantial support, one between 1 and 2 is strong support, and one above 2 is decisive.

```
model      Log Bayes factor
-----
1:2        -13.29
```

Computed from the Bayes factor, this gives the posterior odds of each model, a measure of degree-of-belief in each after having seen the data.

```

model      Posterior odds
-----
1          0.00
2          1.00
Preferred model: 2 (Standard mixture model with bias)

```

Note the warning you are given that you should consider the priors on your parameters (or specify new ones in the form of the `.priorForMC` function) in order to usefully compute Bayes factors. This is because the Bayes factor heavily penalizes flexibility, and uses the prior to understand how flexible a model is. So, for example, the model with a bias could have predicted just about any graph of errors — as specified, a bias of 80 or 130 degrees is equally likely as a bias of only 5 degrees — means it is penalized heavily for its complexity. This is probably not a reasonable prior for a bias parameter, since in reality the bias parameter might be expected to vary only within a small range near zero. Thus, with the current priors the Bayes factor is overpenalizing the model with a bias.

Specifying more reasonable priors for parameters is up to the user of the toolbox, since it depends heavily on your particular paradigm. For example, if you were running a standard color working memory experiment with set size 3, it might be reasonable to specify a prior like so:

```

model = StandardMixtureModel();
model.priorForMC = @(p) (betapdf(p(1), 1.25, 2.5) * ... % for g
                        lognpdf(deg2k(p(2)), 2.5, 0.5)); % for sd

```

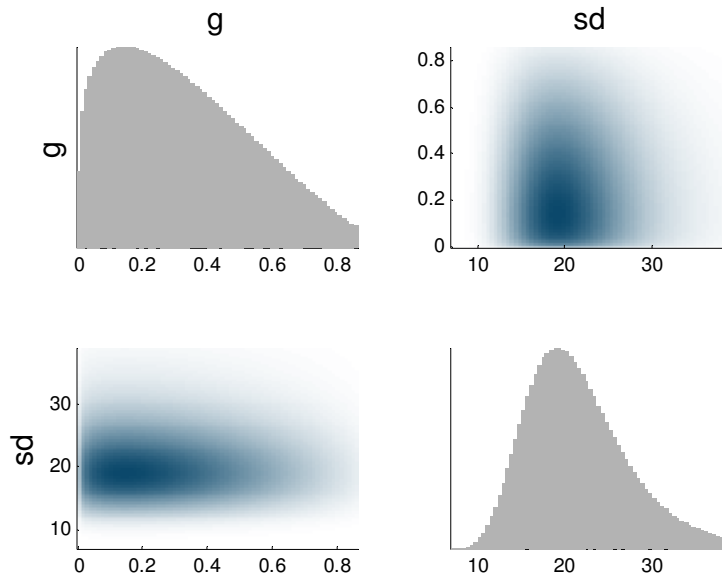
which says something like: in advance of the data, it is reasonable to expect a guess rate around 0.20 (and it would be surprising if it was less than 0.05 or more than 0.80), and a standard deviation of ~10 - ~30 degrees would be reasonable as well. To visualize what the priors you are using are, you can use the `PlotPrior` function. For example, to see the default prior for the `StandardMixtureModel()`:

```
>> PlotPrior(model)
```

or, to visualize the `priorForMC` we specified above:

```
>> PlotPrior(model, 'UseModelComparisonPrior', true)
```

which would show you the prior we just specified:



You may also find the `PlotPriorPredictive` function useful; it shows you what kinds of data you would expect from the current prior.

Bayes factors can, of course, be computed with very diffuse priors like those used by default in the toolbox. However, this almost certainly overpenalizes models with more parameters and should be interpreted with this in mind.

## Demo 6: Using the parallel toolbox to speed up the analysis

The MemToolbox is compatible with the Parallel Computing toolbox. Using it can achieve a big speedup. To use it, run the command `matlabpool open`. You can automate this within your program by opening the pool if it isn't already open:

```
if(~(matlabpool('size') > 0))
    matlabpool open;
end
```

If your machine has multiple processors or multiple cores, then all of the fitting functions — `MCMC`, `MLE`, etc. — will work many times faster once you run `matlabpool`.

## Demo 7: Cleaner plots of the posterior

Using MCMC means that we are sampling from the posterior rather than evaluating it directly. Thus, even though the true posterior is almost always a smooth function of the parameters, the plots obtained from the standard `MemFit` call will not always be smooth. We can fix this by using `GridSearch` rather than MCMC to refine our graph. In particular, given the results of a standard call to `MemFit`:

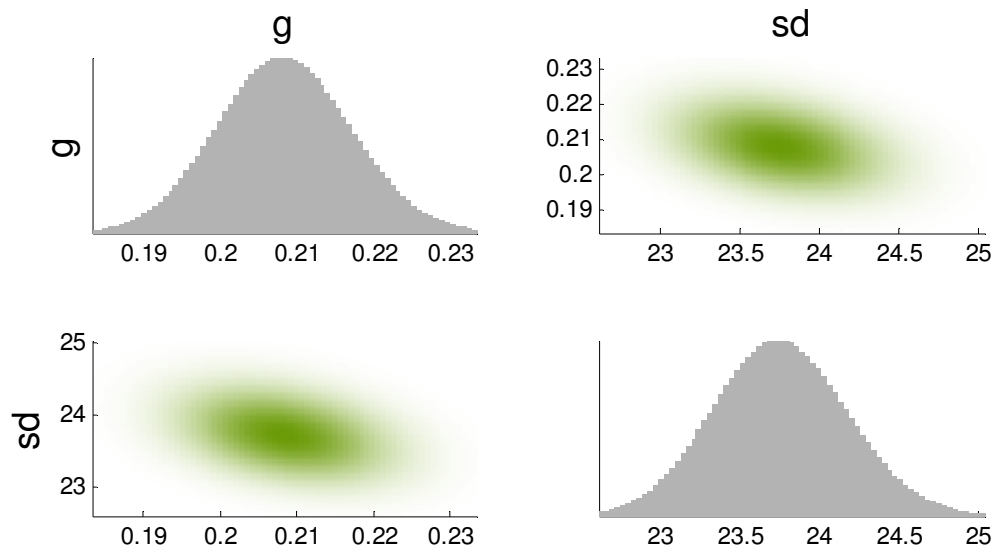
```
>> data = MemDataset(3);
```

```
>> model = StandardMixtureModel();
>> fit = MemFit(data, model);
```

We can make a more refined version of the first figure from Demo 4:

```
>> fullPosterior = GridSearch(data, model, ...
    'PosteriorSamples', fit.posteriorSamples)
>> PlotPosterior(fullPosterior, model.paramNames)
```

Then, rather than the noisy sampling-based-plot, we can get a full posterior :



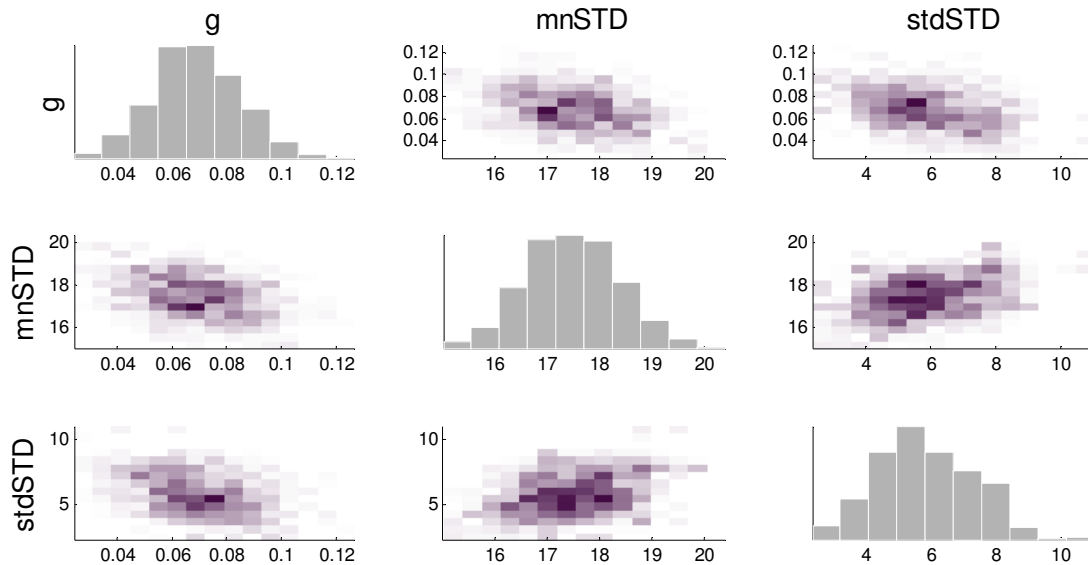
This example also gives you a little bit of a peek under the hood of `MemFit` – in particular, the separate fitting functions (try `help MemFitting`) and plotting functions (`help MemPlots`) of `MemToolbox`.

We first fit the data using `GridSearch` and obtain the posterior. We call this `fullPosterior`, since it came from `GridSearch` (although in reality it is only proportional to the posterior, it is not the true posterior distribution); the results from MCMC we generally call `posteriorSamples`. Then we call the plot function `PlotPosterior`, which takes either a `fullPosterior` or `posteriorSamples` as the first parameter, and the names of the model's parameters as the second parameter. More advanced uses of the `MemToolbox` will generally require separate calls to the `MemFitting` and `MemPlots` functions.

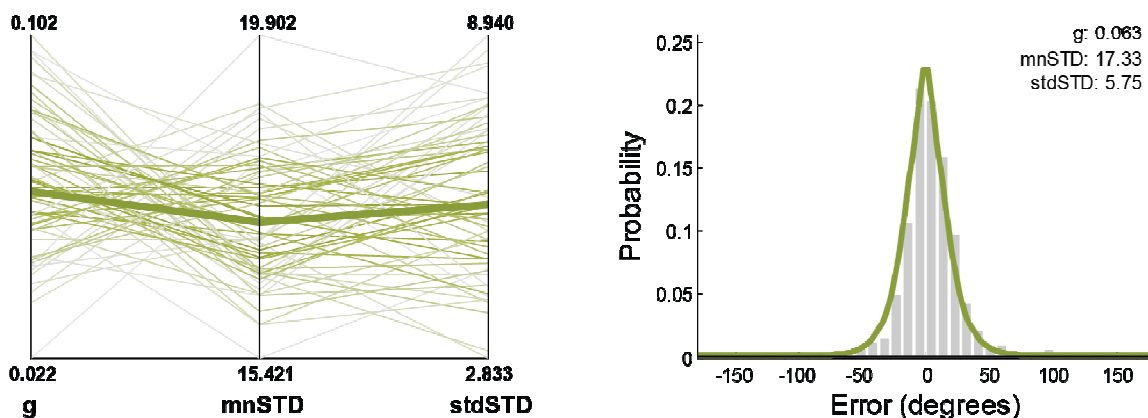
## Demo 8: Understanding models with more parameters

So far we have focused on understanding the posterior of models with only 2 parameters, like that of the standard mixture model. In such models, a heatmap of the two parameters values provides a full understanding of the posterior distribution. For more complex models, understanding the distribution from just the 2-dimensional heatmaps can be more challenging. For example, the default `VariablePrecisionModel` has three parameters, controlling the guess rate ( $g$ ), the mean of the precision ( $mnSTD$ ) and the

standard deviation of the precision (`stdSTD`). All of these parameters are slightly correlated with each other:

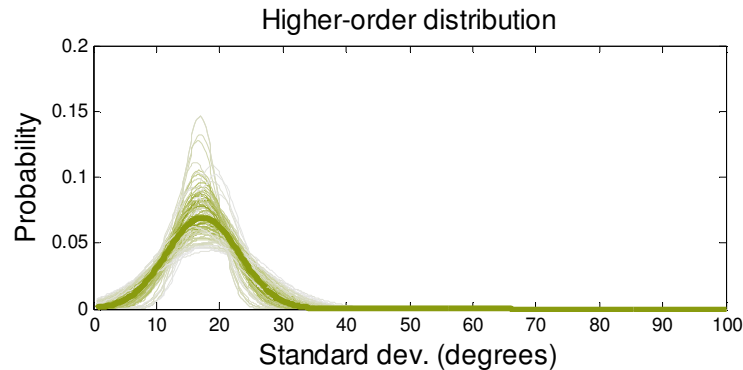


For example, you can see that high values of guess rate give rise to low values of the mean precision and low standard deviations of the precision. Sometimes understanding the full posterior distribution in this format can be complex. In these cases, the parallel coordinates plot is often helpful, as it shows the correlations between all parameters and the predicted distribution for particular parameter settings.



This example also gives you a peak at another feature of the MemToolbox – custom model plots. When you call `MemFit` with the `VariablePrecisionModel`, it not only creates the graphs you are used to seeing -- the posterior plot, the parallel coordinates plot, and the posterior predictive – it also creates another, fourth plot. This is because the `VariablePrecisionModel` includes a function called `.modelPlot`, which is automatically

called by `MemFit`. In this case, the custom model plot shows the higher-order distribution on precision, with the MAP parameters displayed in solid green and other samples from the posterior shown with their color indicating their likelihood:



This helps visualize the meaning of the higher-order parameters. Other models include different custom model plots; for example, the swap model shows a distractor-centered error plot (as in Bays et al. 2009 Figure 2), to allow visualization of whether observers are frequently choosing distractor items.

## Demo 9: Fitting 2AFC or change detection data

Throughout the tutorial we have assumed that you are making use of a continuous report task. However, the `MemToolbox` also fully supports change detection and two-alternative forced-choice tasks for all models.

For example, in a change detection task observers see the stimulus display, then after a delay are asked to report whether the test display is the same or different, with a cue to which item may have changed. In a two-alternative forced-choice, observers might be cued to a particular item (for example, with an arrow pointing to the relevant item) and then asked to pick which of two colors the item at that location was.

### two-alternative forced-choice



### change detection



These two tasks are formally identical, since in both cases observers are effectively being asked whether their memory representation more closely matches the original item or a new, different item. To make use of such data, we can specify `data.changeSize` and `data.afcCorrect` rather than `data.errors`. `data.changeSize` indicates the difference between the study and test item, in degrees; `data.afcCorrect` indicates whether the observer got the trial correct (1) or incorrect (0).



For example, lets make a fake dataset where we sometimes test observers with a very distant color (exactly the opposite side of the color wheel), and observers get 100% of these trials correct; and we sometimes test observers with a relatively close color (20 degrees away on the color wheel), and observers get exactly 50% of those trials correct:

```
>> data.changeSize = [180 180 180 180 180 180 20 20 20 20 20 20];
>> data.afcCorrect = [1 1 1 1 1 1 0 0 0 1 1 1];
>> MemFit(data)
```

When we run this code, `MemFit` will recognize that we passed in 2AFC data and will automatically adjust the default model to make use of 2AFC data:

```
Warning: It looks like you passed in 2AFC data. Trying to fit with
TwoAFC(StandardMixtureModel()).
```

```
Mean percent correct: 0.75
      Model:      2AFC Standard mixture model
Parameters:      g, sd
```

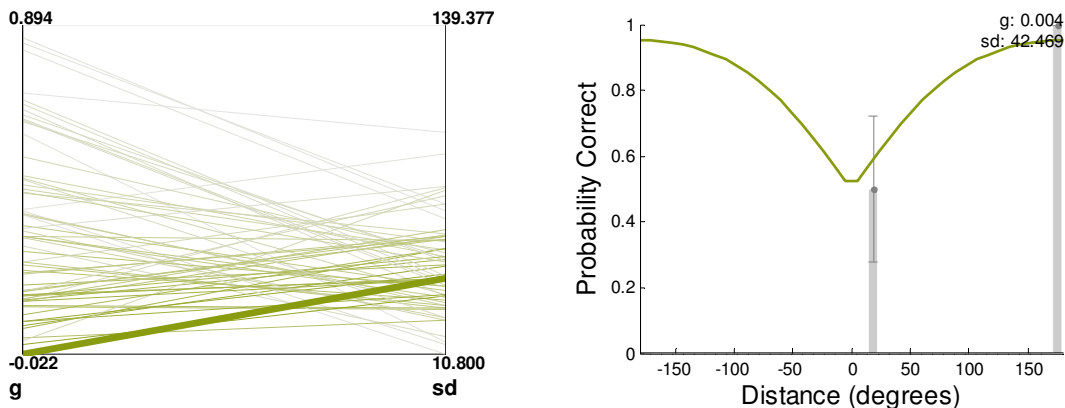
```
Just a moment while MTB fits a model to your data...
```

```
...finished. Now let's view the results:
```

parameter	MAP estimate	lower CI	upper CI
g	0.001	0.010	0.817
sd	42.207	19.006	90.096

The MAP estimates should look intuitively reasonable – since we got all the trials with 180 degree differences correct, we probably aren't guessing much; and since we got half of the trials at 20 degrees correct, our standard deviation is probably around 40 degrees. However, having only 6 trials of each type, our credible intervals are very large: it's still reasonable to believe our guess rate might be as high as 0.80, and our SD could be anywhere from 19 to 90 degrees.

The data from this model can also be visualized; the default is to show a bar plot with error bars, along with the model fit:



The MemToolbox supports converting any model to a 2AFC/change detection model using the `TwoAFC()` wrapper function. Thus, to make a model for a change detection task with a `SwapModel`, you could use `TwoAFC(SwapModel)` as your model. However, for models

that depend on information about particular displays (like the swap model), the 2AFC wrapper is somewhat slow, since it must compute the likelihood for each display separately.

## Demo 10: Fitting orientation data

Sometimes you may wish to use continuous report data on dimensions that span only 180 degrees. For example, oriented lines that do not have a preferred direction.

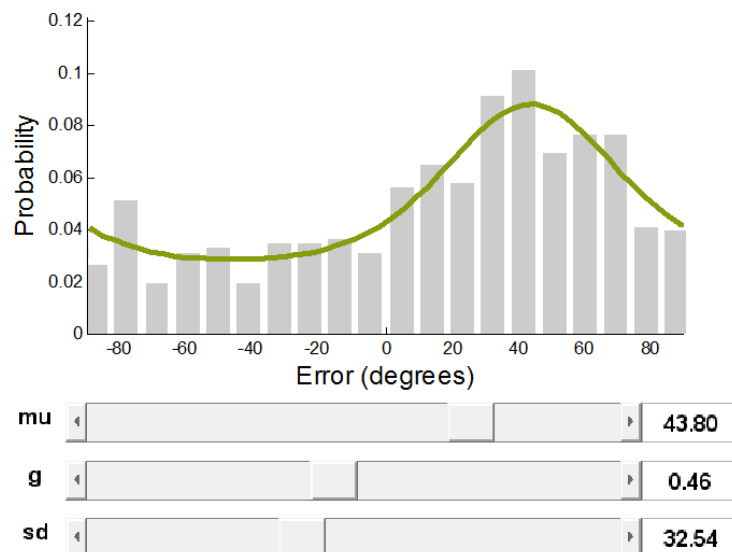
MemToolbox supports this via the `Orientation()` wrapper function. In particular, for such data you should specify your `.errors` as ranging from -90 to 90, rather than -180 to 180, and then wrap your chosen model in `Orientation()` before calling any of the fitting functions:

```
>> data.errors = [-12 3 38 27 -29 21 -22 52 -2 -19 21 17 38 6 34 25 44 ...];
>> MemFit(data, Orientation(WithBias(StandardMixtureModel)))
```

This will fit a model that wraps from -90 to 90 degrees. The model will have “(with orientation)” added to the end of its name.

```
Model: Standard mixture model with bias (for orientation)
```

The graphs of the model will also be adjusted to range from -90 to 90 degrees:



If you specify data that appears to be orientation data, but the model you include is not wrapped with the `Orientation()` wrapper function, `MemFit` will raise a warning but will proceed anyway.

## Demo 11: Analyzing multiple subjects

Typically, the question of interest in working memory research is not about a single observer, but a population: Do those who napped have higher working memory capacities? Is guess rate greater at set size 6 than at set size 3?

When aggregating results from multiple subjects we typically fit a model separately to the data from each subject. To do so in MemToolbox, there is a provided helper function, `FitMultipleSubjects_MAP`, that returns the maximum a posteriori parameters for each subject:

```
>> datasets{1} = MemDataset(1);
>> datasets{2} = MemDataset(2);
>> model = StandardMixtureModel();
>> fit = FitMultipleSubjects_MAP(datasets, model)
```

This is equivalent to simply looping over each subject and calling `MAP`:

```
for i=1:length(datasets)
    params(i,:) = MAP(datasets{i}, model);
end
```

although the `FitMultipleSubjects_MAP` function also calculate means and standard errors for each parameter for you. There is a similar `FitMultipleSubject_MLE` function that calculates maximum likelihood parameters rather than maximum a posterior parameters.

In addition to fitting separate models for individual subject, the MemToolbox also supports a better technique, although one that is more computationally intensive: fitting a single hierarchical model of all the subjects together. This treats each of the subjects' parameters as samples from a normally-distributed population and uses the data to infer the population mean and SD of each parameter.

Hierarchical modeling is the toolbox's default and can be performed by passing multiple data sets, one per subject, to the `MemFit` function:

```
>> data1 = MemDataset(1);
>> data2 = MemDataset(2);
>> model = StandardMixtureModel();
>> fit = MemFit({data1,data2}, model)
```

It is also possible to use the `FitMultipleSubjects_Hierarchical` function directly – its format mirrors the format of the `FitMultipleSubjects_MLE` and `FitMultipleSubjects_MAP` functions.

## Demo 12: Comparing data across conditions

`SplitDataByCondition()` / `PlotPosteriorComparison()`, and `PlotShift()`

## Demo 13: Fitting a model with one set of data and evaluating it with another

GetDataByField() / RemoveDataByField(), Model Comparison, PlotPosteriorPredictive

## Demo 14: Customizing plots and figures

'NewFigure', true in plots; subfigure(), 'PdfColor'

## Demo 15: Advanced MCMC use

PlotConvergence(), changing the convergence detection options and the number of samples to take

## Demo 16: Creating your own model

Creating your own model in MemToolbox is relatively straightforward. The main requirements are to (1) specify the parameters and their ranges, and (2) implement a likelihood function that says how likely the data is given a particular parameter setting. These requirements are nearly the same as those to use the built-in Matlab `mle()` or `fminsearch()` functions.

Thus, a model struct requires the following (standard) fields:

- `.name` – the name of the model
- `.paramNames` – a list of parameters
- `.lowerbound` – the lowest possible value for each parameter
- `.upperbound` – the highest possible value for each parameter
- `.start` – some reasonable initial values for the parameters
- `.pdf` – the likelihood function for the data, given the parameters

In addition, the model requires one field that is unique to MemToolbox:

- `.movestd` – the amount the search technique should move for each parameter

Finally, it is possible to specify a number of optional fields:

- `.prior` – a prior for the parameter settings
- `.priorForMC` – a prior used only in computing Bayes Factors
- `.generator` – to produce samples from the model, given some parameters

For a more thorough discussion of each of these fields and for examples of possible settings for them, please see the example `TemplateModel` included in the `MemTutorials` folder:

```
>> edit TemplateModel.m
```

## Demo 17: Checking a model

The MemToolbox includes a number of tools to check models and ensure they are being properly fit and to ensure that the correct models are being recovered by the model comparison metrics. Many of these functions are located in the `MemTests` folder. For example, the function `TestSamplingAndFitting` takes as input a model and the parameter values for that model, plus a list of how many trials to simulate data from. It will then return the best fit parameters and credible intervals for fitting the model on simulated data. You could use this to calculate, for example, whether the model's credible intervals are well calibrated; or whether the model seems to properly recover its parameters:

```
>>model = WithBias(StandardMixtureModel);
>>paramsIn = {0, 0.1, 10}; % mu, g , K
>>numTrials = [10 100 1000];
>>numItems = [3 5]; % simulate half trials at set size 3 and half at 5
>>[paramsOut, lowerCI, upperCI] = ...
    TestSamplingAndFitting(model, paramsIn, numTrials, numItems);
```

The function `TestAllModels` runs code much like this on each of the included models to ensure the parameters of these models are being properly recovered. Similarly, `TestModelComparison` allows you to see under what circumstances the correct model can be reliably recovered from data.

These functions make use of a number of built-in functions that can be helpful to your own model simulations. For example, `SampleFromModel()` takes as input a model and the parameters of that model, and generates data from this model. Thus, to generate 500 samples from the `StandardMixtureModel` with parameters `g=0.1` and `sd=20`, you could run:

```
>>fakeData.errors = SampleFromModel(StandardMixtureModel, [0.1 20], [1 500])
```

Some models require extra information in order to make it possible to sample from them – for example, you cannot sample from a `SwapModel` without saying what the distractors should be for the data you wish to generate. To help create display information, the toolbox provides a `GenerateDisplays` function that takes as input the number of trials to generate and the number of items per trial (as either a scalar or vector whose length is equal to `numTrials`). This information can then be passed to `SampleFromModel` to generate data:

```
>>numTrials = 100;
>>itemsPerTrial = [3 3 3... 4 4 4... 5 5 5];
>>fakeData = GenerateDisplays(numTrials, itemsPerTrial);
>>params = [0.1, 0.1, 20];
>>errors = SampleFromModel(SwapModel, params, [1 numTrials], fakeData)
>>fakeData.errors = errors;
```

We now know this data contains 100 trials sampled from a `SwapModel` with a swap rate of 0.10 and a guess rate of 0.10; we could thus use this as ground truth for checking that parameters are properly recovered or that the `SwapModel` is preferred to the `StandardMixtureModel` when doing model comparison with this data.

