

Statistics:

- Covariance between two variables in a population: $cov(x, y) = \frac{1}{n} \sum_i (x_i - \bar{x})(y_i - \bar{y})$
- $cov(a_1x + b_1, a_2y + b_2) = a_1a_2cov(x, y)$
- $var(ax + by) = a^2var(x) + b^2var(y) + 2abcov(x, y)$
- When y is a binary variable then: $var(y) = p(1 - p)$

OLS:

Simple linear regression:

- $\hat{\beta}_1 = \frac{cov(x, y)}{var(x)}$
- $var(\hat{\beta}_1) = \frac{\hat{\sigma}_u^2}{SST_x}$ where $\hat{\sigma}_u^2 = \frac{\sum_i \hat{u}_i^2}{n-k-1}$ (k represents the number of regressors)

Multiple linear regression:

- $var(\hat{\beta}_j) = \frac{\hat{\sigma}_u^2}{SST_x(1-R_j^2)}$

Linear Probability Model:

- $P(y = 1|\mathbf{x}) = E[y|x]$

Other:

- $SST = \sum_{i=1}^n (y_i - \bar{y})^2$
- $SSE = \sum_{i=1}^n (\hat{y}_i - \bar{y})^2$
- $SSR = \sum_{i=1}^n \hat{u}_i^2$
- $R^2 = SSE/SST = 1 - SSR/SST$
- Adjusted $R^2 = 1 - \frac{SSR/(n-k-1)}{SST/(n-1)}$

Inference:

- General test statistic for population parameter θ : $\frac{\hat{\theta} - \theta_0}{se(\hat{\theta})}$
- General confidence interval for population parameter θ : $[\hat{\theta} - c \cdot se(\hat{\theta}), \hat{\theta} + c \cdot se(\hat{\theta})]$
- F statistic for q restrictions in a regression done with n observations and k exogenous variables:

$$F = \frac{(R_{UR}^2 - R_R^2)/q}{(1 - R_{UR}^2)/(n - k - 1)} \sim F(q, n - k - 1)$$

$$F = \frac{(SSR_R - SSR_{UR})/q}{SSR_{UR}/(n - k - 1)} \sim F(q, n - k - 1)$$

- F statistic for Chow Test with $q = k + 1$ in a regression done with n observations and k exogenous variables:

$$F = \frac{(SSR_{pooled} - (SSR_1 + SSR_2))/q}{(SSR_1 + SSR_2)/(n - 2k - 1)} \sim F(q, n - 2k - 1)$$