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# Summary



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  3. Transform Y Variable
  4. Model Selection
  5. Model Diagnostic & Remedial measures :
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    - b. Non Normality
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# Raw Data

- Company Name
  - Product Name
  - Laptop Type
  - Screen Inches
  - Screen Resolution
  - CPU Model
- Random Access Memory (RAM)
  - Memory
  - Gpu Characteristic
  - Operating System
  - Laptop's Weight
  - Laptop's Price (Response variable)

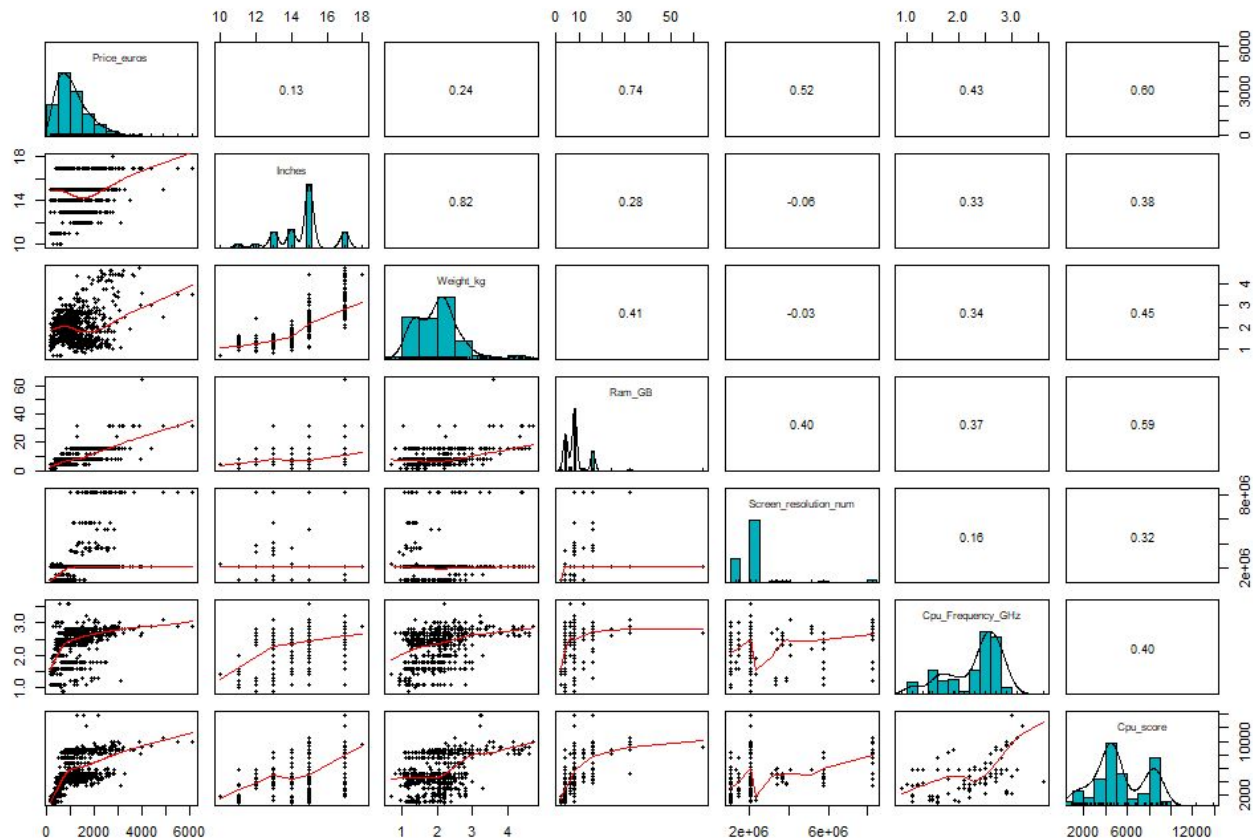
Company <chr>	Product <chr>	TypeName <chr>	Inches <dbl>	ScreenResolution <chr>	Cpu <chr>	Ram <chr>	Memory <chr>	
Apple	MacBook Pro	Ultrabook	13.3	IPS Panel Retina Display 2560x1600	Intel Core i5 2.3GHz	8GB	128GB SSD	
Apple	Macbook Air	Ultrabook	13.3	1440x900	Intel Core i5 1.8GHz	8GB	128GB Flash Storage	
HP	250 G6	Notebook	15.6	Full HD 1920x1080	Intel Core i5 7200U 2.5GHz	8GB	256GB SSD	
Apple	MacBook Pro	Ultrabook	15.4	IPS Panel Retina Display 2880x1800	Intel Core i7 2.7GHz	16GB	512GB SSD	
Apple	MacBook Pro	Ultrabook	13.3	IPS Panel Retina Display 2560x1600	Intel Core i5 3.1GHz	8GB	256GB SSD	
Cpu <chr>		Ram <chr>	Memory <chr>	Gpu <chr>		OpSys <chr>	Weight <chr>	Price_euros <dbl>
Intel Core i5 2.3GHz		8GB	128GB SSD	Intel Iris Plus Graphics 640		macOS	1.37kg	1339.69
Intel Core i5 1.8GHz		8GB	128GB Flash Storage	Intel HD Graphics 6000		macOS	1.34kg	898.94
Intel Core i5 7200U 2.5GHz		8GB	256GB SSD	Intel HD Graphics 620		No OS	1.86kg	575.00
Intel Core i7 2.7GHz		16GB	512GB SSD	AMD Radeon Pro 455		macOS	1.83kg	2537.45
Intel Core i5 3.1GHz		8GB	256GB SSD	Intel Iris Plus Graphics 650		macOS	1.37kg	1803.60

# Clean Data

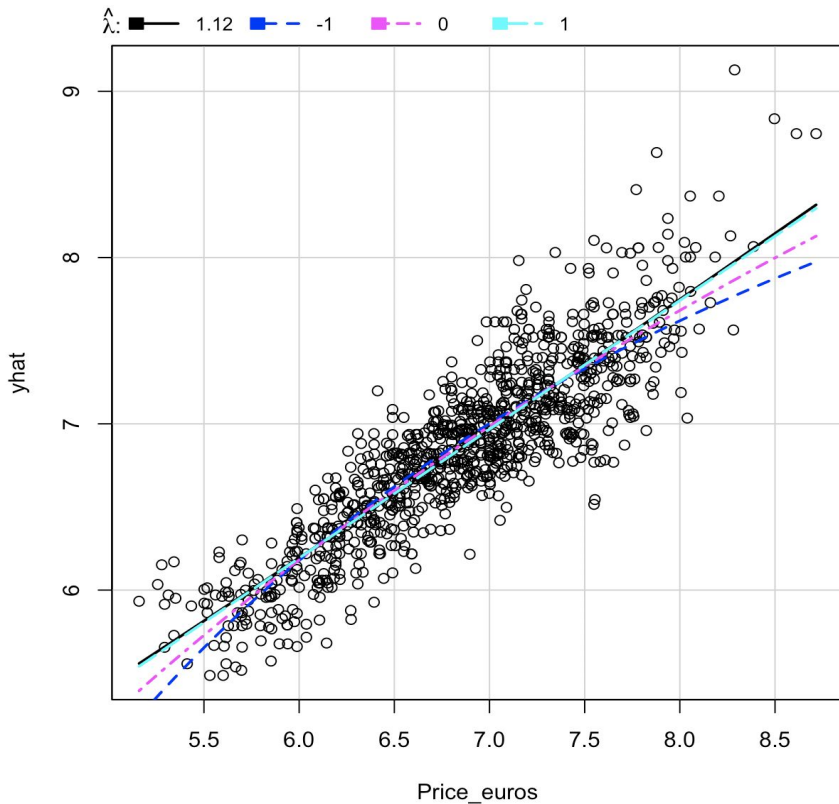
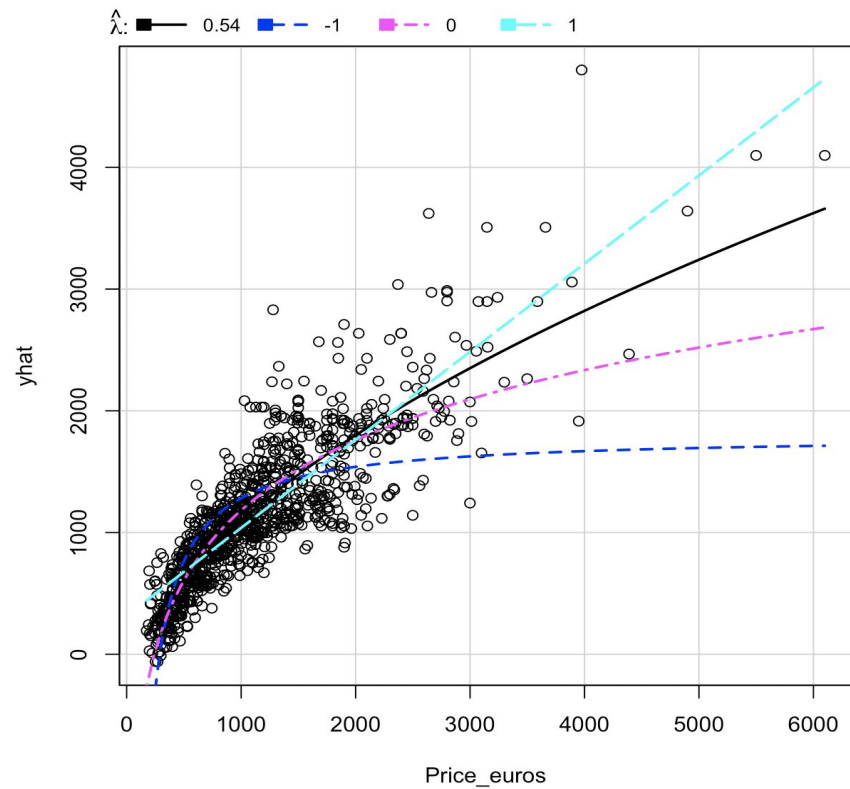
- **Product and Type Name:**
  - Dropped
- **Screen Resolution:**
  - Separated into screen resolution and touchscreen (0, 1)
- **CPU and GPU:**
  - Replaced numerically by CPU/GPU benchmarks
- **Memory:**
  - Separated into four categories (Flash, HDD, Hybrid, SSD)
- **Company/Operational Systems:**
  - changed to 10/ 8 qualitative predictor variable
- **Inches:**
  - Change the size of screen (inches) to integer
- **Weight :**
  - Change Weight(char) variable into Weight\_kg(dbl)
- **Ram:**
  - Keep only the size of ram with unit GB.

[illegible]

# The Scatter Plot on Training Data



# Transform Y to log(Y)



# Model selection

Min\_model: regress response variable on constant,  
no predictor variable

Full\_model: regress response variable on all  
predictor variables

Use stepwise regression with forward and backward  
direction to find our final selected model, which  
contains:

Cpu\_score, Ram\_GB, Weight\_kg,  
Cpu\_Frequency\_GHz, Windows 7,  
Screen\_resolution\_num, No OS, Acer, Toshiba,  
Touchscreen, Linux, Asus, macOS, Mac OS X, HP,  
Inches, SSD and Android.

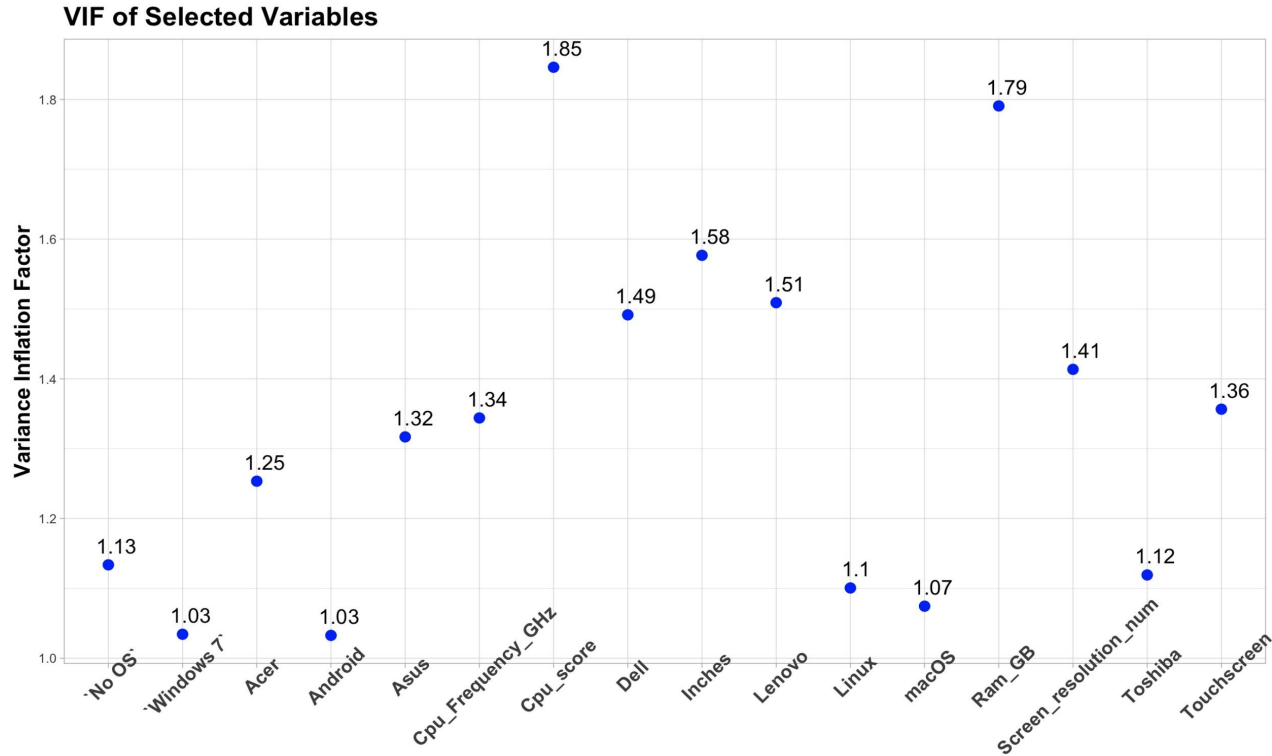
After fitting test data, we find out that the predicted  
R-square improved from 0.7317687 to 0.7786004.

```
Residuals:
    Min       1Q   Median       3Q      Max
-0.97248 -0.18896 -0.01379  0.17560  1.02487

Coefficients:
              Estimate Std. Error t value Pr(>|t|)
(Intercept)  5.744e+00  1.472e-01  39.026 < 2e-16 ***
Cpu_score    1.146e-04  5.146e-06  22.267 < 2e-16 ***
Ram_GB       3.893e-02  2.433e-03  15.999 < 2e-16 ***
Weight_kg    -1.042e-01  2.638e-02  -3.952 8.30e-05 ***
Cpu_Frequency_GHz 2.815e-01  2.099e-02  13.411 < 2e-16 ***
`Windows 7`   4.856e-01  5.006e-02   9.700 < 2e-16 ***
Screen_resolution_num 6.125e-08  7.937e-09   7.716 2.87e-14 ***
`No OS`      -2.702e-01  4.271e-02  -6.326 3.76e-10 ***
Acer         -1.836e-01  3.585e-02  -5.121 3.63e-07 ***
Toshiba       2.812e-01  5.078e-02   5.537 3.93e-08 ***
Touchscreen   1.365e-01  3.083e-02   4.428 1.06e-05 ***
Linux        -1.655e-01  4.701e-02  -3.520 0.00045 ***
Asus         -6.896e-02  3.041e-02  -2.268 0.02354 *
macOS         2.711e-01  8.780e-02   3.087 0.00207 **
`Mac OS X`    2.820e-01  1.240e-01   2.273 0.02322 *
HP            5.300e-02  2.427e-02   2.184 0.02922 *
Inches       -2.740e-02  1.234e-02  -2.220 0.02665 *
SSD          -9.571e-05  4.800e-05  -1.994 0.04643 *
Android      -3.984e-01  2.110e-01  -1.888 0.05926 .
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.2932 on 1010 degrees of freedom
Multiple R-squared:  0.78,    Adjusted R-squared:  0.7761
F-statistic: 199 on 18 and 1010 DF,  p-value: < 2.2e-16
```

# Model Diagnostic & Remedial measures - Multicollinearity



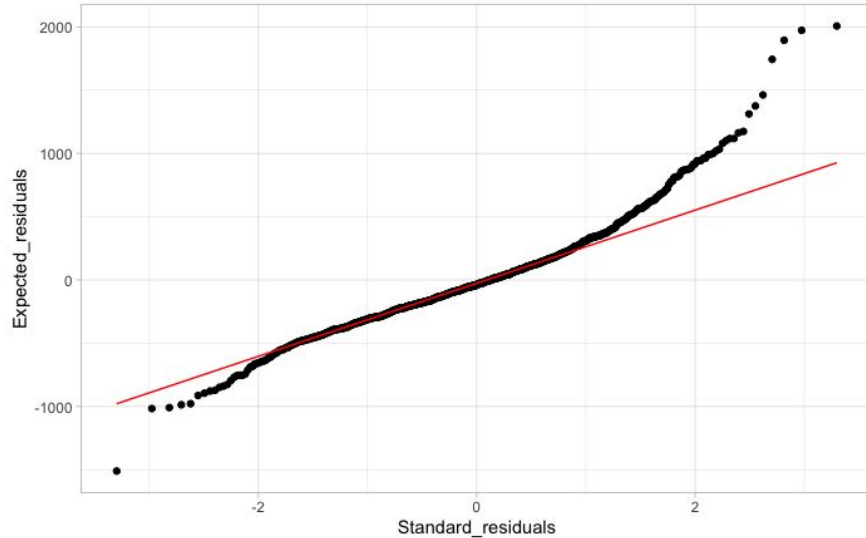
According to the graph, we don't have multicollinearity issue here.



# Model Diagnostic & Remedial measures - Non Normality

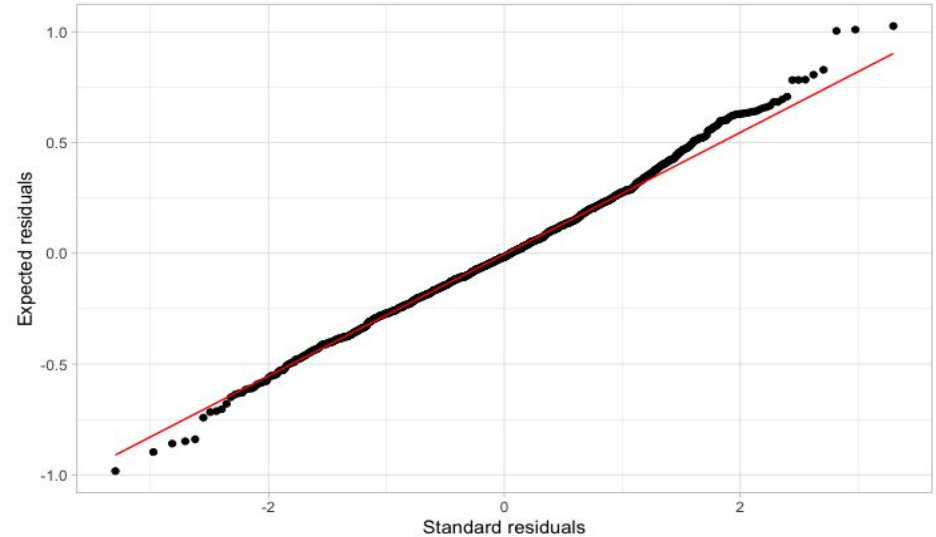
## Full Model

Normal Probability plot of full model



## Transform Y

Normal Probability plot after transform y to  $\log(y)$



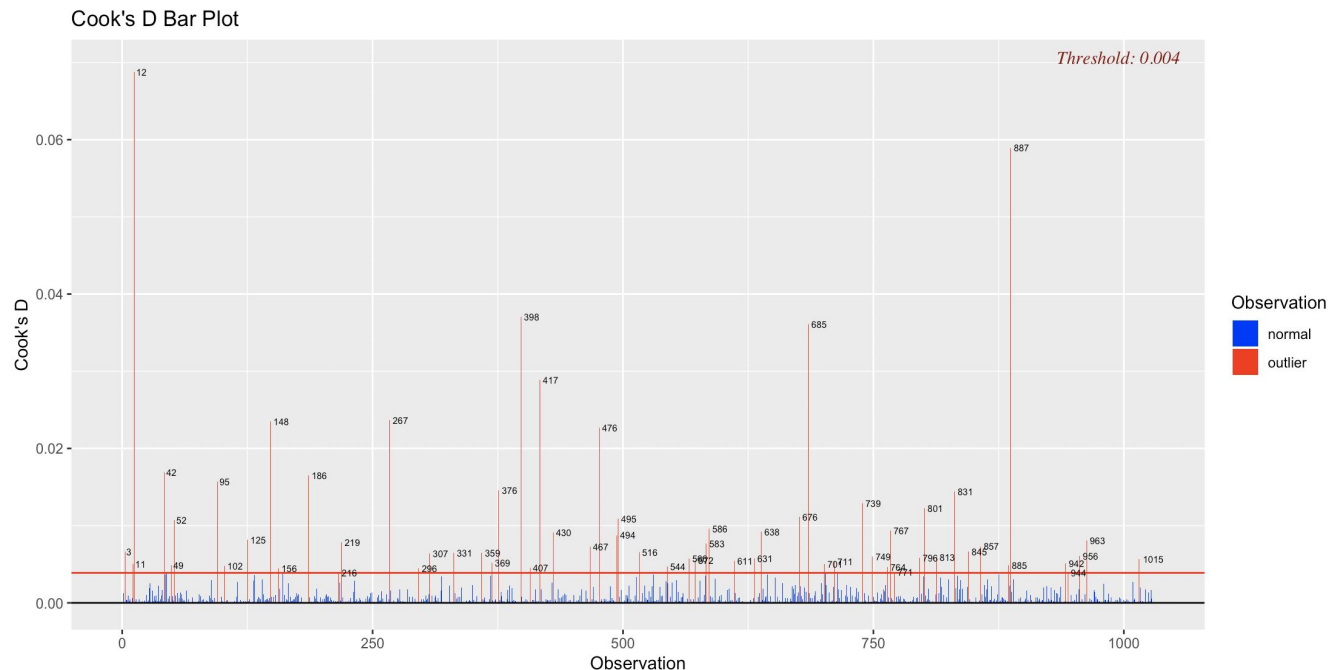
From the above Q-Q plot, we fixed the non-normality by transforming Y to  $\log(Y)$ .

# Model Diagnostic & Remedial measures - Non Constant Variance



From the above plot, we can see that full model's residuals variance is not constant, so we decide to use weighted least square model. We calculate weight by using absolute residuals versus selected predictors. The right hand side graph shows we have almost constant variance now. The predicted R square of the weighted model: 0.778793

# Model Diagnostic & Remedial measures - Outliers



The Cook's Distance Bar Plot suggests that we have outliers in our data, so we use robust regression model to fix this problem. We use the same weight as the WLS model. The result shows the predicted R square is 0.7790693

# Conclusion

Our final model formula:

- $\text{Price\_euros} = \exp\{5.51 + 1.11e-04 * \text{Cpu\_score} + 0.045 * \text{Ram\_GB} - 0.155 * \text{Weight\_kg} + 0.253 * \text{Cpu\_Frequency\_GHz} + 0.461 * \text{Windows\_7} + 6.35e-08 * \text{Screen\_resolution\_num} - 0.261 * \text{No\_OS} - 0.182 * \text{Acer} + 0.295 * \text{Toshiba} + 0.118 * \text{Touchscreen} - 0.156 * \text{Linux} - 0.0715 * \text{Asus} + 0.265 * \text{macOS} + 0.26 * \text{Mac\_OS\_X} + 0.033 * \text{HP} - 2.69e-03 * \text{Inches} - 4.055e-05 * \text{SSD} - 0.331 * \text{Android}\}$

Example:

Inches <int>	Price_euros <dbl>	Weight_kg <dbl>	Ram_... <dbl>	Touchscreen <dbl>	Screen_resolution_num <dbl>	Cpu_Frequency_GHz <dbl>	Cpu_score <dbl>
13	1803.6	1.37	8	0	4096000	3.1	5815.869

- $Y = \exp(5.502 + 1.11e-04 * 5815.869 + 0.045 * 8 - 0.155 * 1.37 + 0.253 * 3.1 + 6.354e-08 * 4096000 + 0.265 * 1 - 2.687e-03 * 13 - 4.055e-05 * 256) = 1918.8$

Study Limitation:

- few data, dealing with outliers, variable selection...

Future Enhancement:

- Study on the coefficients that are not significant, include all/no categorical
- Try to get more data, filter out data to have less outliers, non linear model...

Predictors	Price_euros		
	Estimates	CI	p
(Intercept)	5.50	5.22 – 5.79	<0.001
Cpu_score	0.00	0.00 – 0.00	<0.001
Ram_GB	0.05	0.04 – 0.05	<0.001
Weight_kg	-0.15	-0.21 – -0.10	<0.001
Cpu_Frequency_GHz	0.25	0.22 – 0.29	<0.001
Windows_7	0.46	0.38 – 0.54	<0.001
Screen_resolution_num	0.00	0.00 – 0.00	<0.001
No_OS	-0.26	-0.32 – -0.20	<0.001
Acer	-0.18	-0.24 – -0.13	<0.001
Toshiba	0.30	0.22 – 0.37	<0.001
Touchscreen	0.12	0.05 – 0.19	0.001
Linux	-0.16	-0.21 – -0.10	<0.001
Asus	-0.07	-0.13 – -0.01	0.015
macOS	0.26	0.18 – 0.35	<0.001
Mac_OS_X	0.27	0.18 – 0.35	<0.001
HP	0.03	-0.02 – 0.08	0.197
Inches	-0.00	-0.03 – 0.02	0.828
SSD	-0.00	-0.00 – 0.00	0.295
Android	-0.33	-0.85 – 0.18	0.208
Observations	1029		

# References

- <https://www.kaggle.com/ionaskel/laptop-prices>
- [https://www.cpubenchmark.net/high\\_end\\_cpus.html](https://www.cpubenchmark.net/high_end_cpus.html)
- [https://www.cpubenchmark.net/low\\_end\\_cpus.html](https://www.cpubenchmark.net/low_end_cpus.html)
- [https://www.cpubenchmark.net/midlow\\_range\\_cpus.html](https://www.cpubenchmark.net/midlow_range_cpus.html)
- [https://www.cpubenchmark.net/mid\\_range\\_cpus.html](https://www.cpubenchmark.net/mid_range_cpus.html)
- <https://gpu.userbenchmark.com/>

спасибо  
danke 謝謝  
ngiyabonga  
teşekkür ederim  
tapadh leat  
gracias  
mochchakkeram  
go raibh maith agat  
arigatō  
takk  
dakujem  
merci  
ευχαριστώ  
감사합니다  
terima kasih  
sukriya  
kop khun krap  
grazie  
sagolun  
dziękuję  
hvala  
mauruuru  
bedankt  
obrigado