Grade: 100/100 **Excellent!**

Assignment 1 - (Zinren Zhou

10/10.
$$(-\infty, +\infty) = x^2$$
 domain: $(-\infty, +\infty)$

: this function is convex in its domain

$$f'(x) = \frac{1}{x^2} < 0$$

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$$f''(x) = -\frac{1}{x^2} < 0$$

this function is concave in its domain

C.
$$f(x) = \frac{1}{1+e^{-x}}$$
 domain: $(-(n, +\infty))$

$$f'(x) = -\frac{1}{(+e^{-x})^2} \cdot (-e^{-x})$$

$$= \frac{e^{-x}}{(+e^{-x})^2}$$

$$f''(x) = \left(\frac{1}{e^{x} + e^{-x} + 2}\right)^{1}$$

$$= \frac{1}{(e^{1} + e^{-1})^{2}} \cdot (e^{1} - e^{-1})$$

$$= \frac{e^{-1} - e^{1}}{(e^{1} + e^{-1} + 1)^{2}}$$

: if
$$x < 0$$
, then $f''(x) > 0$
if $x > 0$, then $f''(x) < 0$

: this function is convex when ac (-0,0)

10/102.

$$a. \quad \text{as } V(0,\theta)$$

$$f(x) = \frac{1}{\theta - 0}$$

$$=\int_{0}^{\theta}\frac{x}{\theta^{-0}}dx$$

$$= \int_0^\theta \frac{x}{\theta} dx$$

$$=\frac{\chi^2}{2\theta} \quad \begin{bmatrix} \theta \\ 0 \end{bmatrix}$$

$$= \left[\left(x^{2} \right) - \left[\left(x \right)^{2} \right]$$

$$= \int_{-\infty}^{\infty} x^2 f(u) dx - E(x)^2$$

$$=\frac{1}{6-0}\int_{0}^{6}x^{2}dx-\frac{6^{2}}{4}$$

$$=\frac{x^{3}}{3\theta}\Big|_{0}^{\theta}-\frac{6^{2}}{4}$$

$$=\frac{9^{2}}{3}-\frac{9^{2}}{4}$$

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$$C. \quad H(x) = -\int f(x) \cdot \ln f(x) dx \qquad f(x) = \dot{b}$$

$$= -\int_{0}^{b} \dot{b} \cdot \ln (\dot{b}) dx$$

$$= -\dot{b} \cdot \ln (\dot{b}) \int_{0}^{b} 1 \cdot dx$$

$$= -\dot{b} \cdot \ln (\dot{b}) \cdot \theta$$

$$= \left[n\left(\frac{1}{\theta}\right) \right]$$

 $= \ln \theta$ $= \ln \theta$ $= (x_1, x_2, ..., x_n) = \prod_{i=1}^{n} p(x_i) = \begin{cases} \frac{1}{\theta^n}, x_1, x_2 ..., x_n \in (0, \theta) \\ 0, \text{ others} \end{cases}$

when b is smaller, I is larger : 0 > max (X1, X2, -, Xn)

:
$$\hat{\theta} = \max_{\{X_1, X_2, \dots, X_n\}}$$

20/204.

Let M be the event: the \$1M is behind the door I choose initially

Let W be the event: I win the \$1 m by switching the door

$$\int_{C} CM[W_c] = 0$$

: $p(w) = p(w|m) \cdot p(m) + p(w|m^c) \cdot p(m^c)$ = $0 \times \frac{1}{3} + 1 \times \frac{2}{3}$

: the probabity of wining by switching the

So I choose to switch the door.

20/205. If Σ is PSD, then $\forall y = \Gamma y_1, y_2, \dots y_n J^T, y^T \Sigma y > 0$

 $TE[(X_1-M_1)(X_1-M_1)] \sim [E[(X_1-M_1)(X_1-M_1)]$

$$y^{T} \Sigma = \left[\begin{bmatrix} y_{1} & y_{1} & y_{2} & y_{3} & y_{4} & y_{4} \\ \vdots & y_{1} & y_{2} & y_{3} & y_{4} & y_{4} \\ \vdots & y_{1} & y_{2} & y_{3} & y_{4} & y_{4} \\ \vdots & y_{1} & y_{2} & y_{3} & y_{4} & y_{4} \\ \vdots & y_{1} & y_{2} & y_{3} & y_{4} & y_{4} \\ \vdots & y_{1} & y_{2} & y_{3} & y_{4} & y_{4} \\ \vdots & y_{1} & y_{2} & y_{4} & y_{4} & y_{4} \\ \vdots & y_{1} & y_{2} & y_{4} & y_{4} & y_{4} \\ \vdots & y_{1} & y_{2} & y_{4} & y_{4} & y_{4} \\ \vdots & y_{1} & y_{2} & y_{4} & y_{4} \\ \vdots & y_{1} & y_{4} & y_{4} & y_{4} & y_{4} \\ \vdots & y_{1} & y_{4} & y_{4} & y_{4} & y_{4} \\ \vdots & y_{1} & y_{2} & y_{4} & y_{4} & y_{4} \\ \vdots & y_{1} & y_{2} & y_{4} & y_{4} & y_{4} \\ \vdots & y_{1} & y_{2} & y_{4} & y_{4} & y_{4} \\ \vdots & y_{1} & y_{2} & y_{4} & y_{4} & y_{4} \\ \vdots & y_{1} & y_{2} & y_{4} & y_{4} & y_{4} \\ \vdots & y_{1} & y_{2} & y_{4} & y_{4} & y_{4} \\ \vdots & y_{1} & y_{2} & y_{4} & y_{4} & y_{4} \\ \vdots & y_{1} & y_{2} & y_{4} & y_{4} & y_{4} \\ \vdots & y_{1} & y_{2} & y_{4} & y_{4} & y_{4} & y_{4} \\ \vdots & y_{1} & y_{2} & y_{4} & y_{4} & y_{4} & y_{4} \\ \vdots & y_{1} & y_{2} & y_{4} & y_{4} & y_{4} & y_{4} \\ \vdots & y_{1} & y_{2} & y_{4} & y_{4} & y_{4} & y_{4} \\ \vdots & y_{1} & y_{2} & y_{4} & y_{4} & y_{4} & y$$

: yTZy=E (Z2) 70

is Z is	PSD.		