Supplementary Materials for: An Effective Biclustering-based Framework for Identifying Cell Subpopulations from scRNA-seq Data*

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^{*}Availability and Implementation: DivBiclust, including source codes, preprocessed data, experiment results, and a supplementary document, is freely available at https://www.github.com/Qiong-Fang/DivBiclust.

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1 Data Preparation

Nine real scRNA-seq datasets are used in our experiments. Three datasets with smaller cell sets were generated by low-throughput plate-based scRNA-Seq methods. They respectively contain the transcriptomes of human cancer/somatic cells [9], the transcriptomes of human embryonic cells [14], and the transcriptomes of human pancreatic islet cells [7]. Thus we call them the HCC, HEC, and HPIC datasets, respectively. Six datasets were generated by the high-throughput InDrop [6] method, which respectively contain the transcriptomes of pancreatic cells from four human donors and two mouse strains [1]. We denote these six datasets as the HUM1, HUM2, HUM3, HUM4, MOU1, and MOU2 datasets, respectively. In this section, we introduce the preprocessing steps of these scRNA-Seq datasets.

1.1 HCC Dataset

The HCC dataset contains the transcriptomes of circulating tumor cells. It was downloaded from the Gene Expression Ominbus (GEO) database (GSE38495). We follow the preprocessing steps in [13] and only keep the genes with RPKM ≥ 20 to avoid the influence of low-expressed genes. Then, a log transformation is performed to reduce the effect of extreme values. The resulting gene expression matrix contains 86 cells and 4501 genes with 8.1% missing values. The 86 cells respectively belong to 11 classes with the transcriptomes shown in Table 1.

Table 1: Transcriptomes of Human Cancer/Somatic Cells

Cell type	#Samples
Brain	16
Bladder cancer cell line (T24)	4
Embryonic stem cells	8
Melanoma cancer (SKMEL5)	4
Melanoma cancer (UACC)	3
Melanoma-derived circulating tumor cells (CTC)	6
Melanocytes	2
Prostate cancer cell line (PC3)	4
Prostate cancer cell (picked from Petri dish)	8
Prostate cancer cell (isolated by EPCAM marker)	11
Universal human reference RNA	20

The abbreviations for the names of 11 cell types are respectively "Brain", "Bladder(T24)", "ESC", "Melanoma(SKMEL5)", "Melanoma(UACC)", "Melanoma (CTC)", "Melanocytes", "Prostate(PC3)", "Prostate", "Prostate(EPCAM)", and "refRNA". They are used in the experiment section for simplicity in presentation.

1.2 HEC Dataset

The HEC dataset includes the transcriptomes of human oocytes and early embryos at seven developmental stages plus the primary outgrowth during hESC derivation. It was downloaded from the GEO database with the accession number GSE36552. We also follow the preprocessing steps in [13] and filter out those genes whose log-transformed RPKM under all the cell samples are smaller than 0.1. A gene expression matrix with 124 cells, 20 018 genes and 36.9% missing values is produced. The cells are divided into 9 classes and the transcriptome details are presented in Table 2.

Table 2: Transcriptomes of Human Embryonic Cells

Cell type	#Samples
Oocyte	3
Zygote	3
2-cell	6
4-cell	12
8-cell	20
Morulae	16
Late-blastocyst	30
hESC passage 0	8
hESC passage 10	26

1.3 HPIC Dataset

The HPIC dataset includes the expression profiles of endocrine and exocrine cells in human pancreatic islets. We obtained a preprocessd HPIC expression matrix from Lin et al. [8], in which undefined cells and bulk RNA-seq samples were excluded. It consists of 60 cells and 180 253 transcripts, and contains 77.8% missing values. The 60 cells are divided into 6 classes with the transcriptome details shown in Table 3.

Table 3: Transcriptomes of Human Pancreatic Islet Cells

Cell type	Biological hormone	#Samples
Acinar	NA	11
Alpha	Glucagon	18
Beta	Insulin	12
Delta	Somatostatin	2
Duct	NA	8
PP	Pancreatic Polypeptide	9

1.4 HUM and MOU Datasets

The four HUM datasets and two MOU datasets respectively contain the transcriptomes of the pancreas islets cells from four human donors and two mouse strains [1]. They were downloaded from the GEO database with the accession number GSE84133. The cells in each HUM dataset belong to 14 classes and the cells in each MOU dataset belong to 13 classes. The transcriptome details of the six datasets are listed in Tables 4 and 5, respectively.

We first take a simple preprocessing strategy by filtering out the genes with zero expression values under all the cell samples, and generate four datasets with large gene sets and higher dropout rates. On the other hand, gene selection has become an indispensable preprocessing step in many cell subpopulation identification methods, which filters out those low-variance or low-abundance genes before the cell clustering analysis is performed. Therefore, we adopt the gene selection strategy in [10] and keep top 10% of the genes which have the maximum count across all the cells. Accordingly, four datasets with smaller gene sets and lower dropout rates are generated. We call the datasets generated by the first preprocessing strategy as the HUM1_NZ, HUM2_NZ, HUM3_NZ, and HUM4_NZ datasets, respectively, and use HUM1, HUM2, HUM3, and HUM4 to refer to the datasets generated by the second preprocessing strategy. The statistics of the datasets generated by two different preprocessing strategies are listed in Table 6. Because some of the related methods we compare with cannot deal with the datasets with larger gene sets, the experiment results presented in the paper are conducted on the datasets generated by the second preprocessing strategy. We show the experiment results on the NZ datasets in Section 2 in the supplementary materials.

Table 4: Transcriptomes of four HUM datasets

Cell type	# Samples				
Cen type	HUM1	HUM2	HUM3	HUM4	
Alpha	236	676	1130	284	
Beta	872	371	787	495	
Gamma	70	86	36	63	
Delta	214	125	161	101	
Acinar	110	3	843	2	
Ductal	120	301	376	280	
$Activated_stellate$	51	81	100	52	
$Quiescent_stellate$	92	22	54	5	
Schwann	5	6	1	1	
Endothelial	130	23	92	7	
Macrophage	14	17	14	10	
Mast	8	9	7	1	
T_{cell}	2	2	2	1	
Epsilon	13	2	2	1	

Table 5: Transcriptomes of two MOU datasets

Cell type	# Samples		
Cen type	MOU1	MOU2	
Alpha	9	182	
Beta	343	551	
Gamma	14	27	
Delta	85	133	
Ductal	236	39	
$Activated_stellate$	4	10	
$Quiescent_stellate$	29	18	
Schwann	3	3	
Endothelial	72	67	
Macrophage	17	19	
$B_{-}cell$	2	8	
T_{cell}	4	3	
Immune_other	4	4	

1.5 Analysis of Data Noise

We conduct an analysis over the datasets to study their noise levels and the results are used to help determine a proper setting for the similarity threshold α used in the pattern mining phase. The analysis consists of three steps as follows.

- For each cell c in the dataset, a set T of 100 genes are selected whose expression levels under c are maximal. The vector of the expression values of genes in T under the cell c is called the expression profile of c over T.
- \bullet Then, the distance between the cell c and every other cell is computed, and the distance function is defined as follows.

$$D(c, c_i) = \frac{1}{|T|} \sum_{t_i \in T} \frac{|M(c, t_j) - M(c_i, t_j)|}{M(c, t_j)}.$$
 (1)

• In the dataset with high dropout rate, it is possible that the expression values of genes in T under a certain cell c_i are all zeros. Such cells never have the chance to be covered by the

Table 6:	Statistics	of the HUM	and MOU	Datasets
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Dataset	# Cells #Classes		nonzero data (NZ)		Top 10% data		
Dataset	# Cens	#Classes	# Genes	Dropout rate	# Genes	Dropout Rate	
HUM1	1,937	14	16,016	88.0%	2,012	63.7%	
HUM2	1,724	14	16,310	88.4%	2,012	64.1%	
HUM3	3,605	14	16,678	89.5%	2,012	63.6%	
HUM4	1,303	14	15,720	86.0%	2,012	59.0%	
MOU1	822	13	14,359	90.1%	1,487	67.9%	
MOU2	1,064	13	14,646	87.6%	1,487	67.9%	

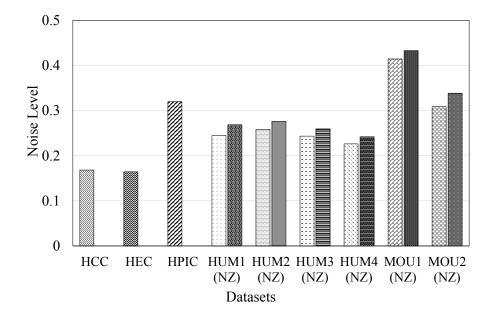


Figure 1: Noise Levels of Fifteen scRNA-seq Datasets

bicluster with cell c as the seed. Thus, we only take into accounts the cells whose expression profiles over T contain at least 50% valid entries. The noise level of a cell c is the average of the distance between c and every other cell, and the noise level of a dataset is the average of the noise levels of all the cells in the data.

The distance function is formulated based on the definition of the sc-bicluster and is similar with the computation of α . Thus, the noise level of a dataset can be a reference for setting the similar threshold α .

Figure 1 shows the noise levels of all the fifteen datasets, including the nonzero versions of the four HUM and two MOU datasets.

2 Experiment Results on MOU Data

2.1 Impact of α and $|T_s|$

According to the data noise analysis shown in Figure 1, the noise level of the MOU1 dataset is the highest which exceeds 0.4. The noise level of the MOU2 dataset is 0.31 and is similar with that of the HPIC dataset. Therefore, we refer to the setting for the HPIC dataset and set the dropout threshold γ to 0.1 for the two MOU datasets as well. The similarity threshold β for pattern merging is fixed to 0.5.

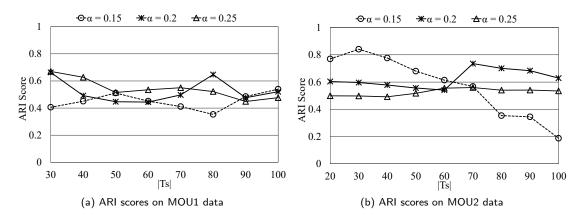


Figure 2: ARI w.r.t. similarity threshold α and the size of initial gene set $|T_s|$ ($\beta = 0.5$).

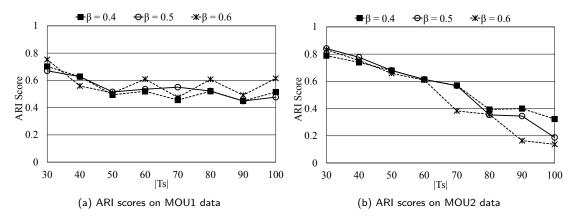


Figure 3: ARI w.r.t. the threshold β for pattern merging and the size of initial gene set $|T_s|$

The ARI scores of *DivBiclust* on the two MOU datasets with respect to the similarity threshold α and the size of initial gene set $|T_s|$ are presented in Figure 2. Due to the higher noise level of the MOU1 dataset, the ARI scores on this dataset is generally lower than the ARI scores on the MOU2 dataset under most of the settings. In addition, as listed in Table 7, the best ARI score on the MOU1 dataset is 0.670 which is achieved when $\alpha=0.25$ and $|T_s|=30$, and the best ARI score on the MOU2 dataset is 0.841 and it is achieved when $\alpha=0.15$ and $|T_s|=30$. For the more noisy MOU1 dataset, a more relaxed similarity threshold is needed.

Table 7: The Highest ARI Scores on the MOU1 and MOU2 Data

Dataget	ARI Score	Parameter Settings		
Dataset		α	$ T_s $	γ
MOU1	0.670	0.25	30	0.1
MOU2	0.841	0.15	30	0.1

2.2 Impact of β

Next, we study how the setting of the similarity threshold β affects the clustering accuracy using the MOU datasets. The threshold α and γ are respectively fixed to the optimal settings for individual dataset as listed in Table 7. Then, the threshold β varies in $\{0.4, 0.5, 0.6\}$ and $|T_s|$ increases from 30 to 100. The experiment results are shown in Figure 3. Similar to the results on

Table 0. Comparisons of Clustering Accuracy	Table 8:	Comparisons	of Clustering	Accuracy
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Methods	Data	asets
	MOU1	MOU2
DivBiclust	0.670	0.841
SNN-Cliq	0.063	0.065
BackSPIN	0.006	0.003
CIDR	0.322	0.272
SC3	0.439	0.262
pcaReduce	0.317	0.221
TSCAN	0.404	0.412
Seurat v3	0.472	0.298
GiniClust2	0.383	0.282
SOUP	0.332	<u>0.478</u>

^{*} The largest ARI score over each dataset is highlighted using bolded font, and the second largest one is underlined

the four HUM datasets, the impact of β on the clustering accuracy is limited over the two MOU datasets as well. On both datasets, as β increases from 0.4 to 0.6, the ARI scores under all the $|T_s|$ values simply show a small change. In addition, the highest ARI scores under different β settings all occur with $|T_s|$ equal to 30. Thus, the setting of β does not affect the the optimal settings of other parameters. Therefore, β is fixed to 0.5 as we declared in the paper.

2.3 Comparison with Related Methods

The optimal ARI scores achieved by *DivBiclust* and nine state-of-the-art methods on the two MOU datasets are listed in Table 8. The results again effectively demonstrate the superiority of our *DivBiclust* method in identifying the cell subpopulations. The ARI scores achieved by *DivBiclust* on the MOU1 and MOU2 datasets are 0.670 and 0.841, which are respectively 0.198 and 0.363 higher than the best results achieved by the counterpart methods.

The heatmaps that demonstrate the correlations between the cell clusters generated by DivBiclust and the ground-truth cell classes of the datasets are shown in Figure 4. The clustering result of a related method that achieves the second highest ARI score is also presented for comparison. Because both Seurat and SOUP involve a parameter that can be used to control the final number of cell clusters, these two methods perform better at identifying the final number of cell subpopulations. However, the clustering result generated by DivBiclust still achieves much higher ARI score. The reason is that, DivBiclust successfully identifies several largest cell classes with high accuracy from both MOU1 and MOU2 data. For example, the three largest cell classes in the MOU1 data are respectively "beta cells", "ductal cells", and "Endothelial". DivBiclust manages to cluster together 72.0% beta cells, 94.9% ductal cells, and 93.1% endothelial cells, individually. In contrast, the clustering result generated by Seurat v3 only successfully clusters 44.0% beta cells, 53.8% ductal cells, and 97.2% endothelial cells. Similar advantage is observed from the results on the MOU2 dataset. DivBiclust successfully clusters 481 beta cells, 171 alpha cells, and 115 delta cells, which respectively account for 87.3% of the beta cells, 94.0% of the alpha cells, and 86.5% of the delta cells in the dataset.

3 Experiments on HUM_NZ and MOU_NZ Datasets

As discussed in Section 1.4, two preprocessing methods are adopted to handle the data of human and mouse pancreatic cells. The first preprocessing method simply removes those genes which have zero expression values under all cell samples, and the resultant nonzero datasets are denoted as the HUM1_NZ, HUM2_NZ, HUM3_NZ, HUM4_NZ, MOU1_NZ, and MOU2_NZ datasets. Compared

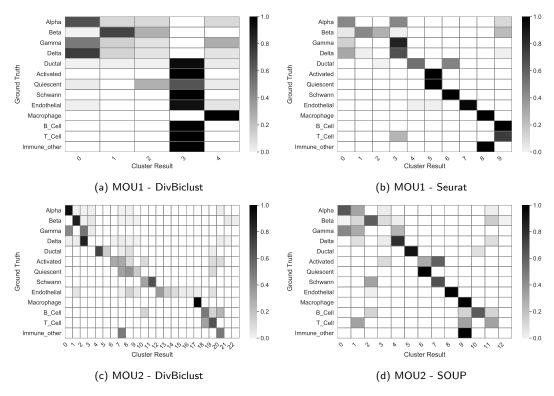


Figure 4: Comparisons with the ground-truth clustering of the MOU1 and MOU2 datasets

to the datasets generated by the second preprocessing method, these nonzero datasets have much larger gene sets and much higher dropout rates. In this set of experiments, we study whether or not the adoption of different preprocessing steps for the datasets would affect the performance of DivBiclust in identifying cell subpopulations.

3.1 Clustering Accuracy

Although the dropout rates of the datasets generated by two different preprocessing steps are quite different, according to the data noise analysis performed in Section 1.5, we find that the noise level of each nonzero dataset is only slightly higher than the noise level of the corresponding dataset generated by the second preprocessing strategy. Thus, we take the parameter settings for the HUM and MOU datasets when running *DivBiclust* over the corresponding HUM_NZ and MOU_NZ datasets.

Specifically, we fix the similarity threshold α to 0.2 and fix the dropout threshold γ to 0 for the four HUM_NZ datasets. Then, we respectively set α to 0.25 and 0.15 and fix γ to 0.1 for MOU1_NZ and MOU2_NZ datasets. The ARI scores with respect to the size of initial gene set $|T_s|$ are shown in Figures 5 and 6. The ARI scores on the nonzero datasets are generally smaller than the ARI scores on the preprocessed datasets with gene selection. The reason is that, the gene selection strategy filters out those low-abundance and low-variance genes and thus reduces the noise level in the datasets. However, the varying trend of the ARI scores on two types of datasets are similar, and the difference between the scores under the same $|T_S|$ value is small . For example, on the HUM1_NZ, HUM2_NZ, and HUM4_NZ datasets, the ARI scores with $|T_s|$ equal to 30 or 40 remain high and are at least 0.88. The highest ARI score over the HUM3_NZ dataset is achieved when $|T_s|$ is equal to 60, and the highest ARI scores on both MOU1_NZ and MOU2_NZ datasets are achieved when $|T_s|$ equals to 30. These results are accordant with what we observed from the experiments over the HUM1, HUM2, HUM3, and HUM4 datasets. Therefore, we are still able to effectively identify the cell subpopulations using the nonzero datasets.

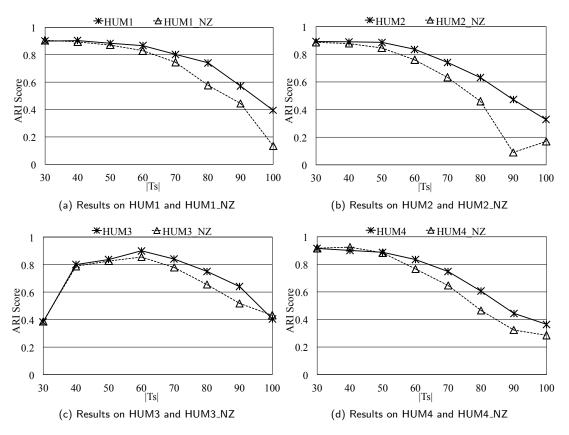


Figure 5: Comparison of ARI scores on HUM and HUM_NZ Datasets

3.2 Running time

Figures 7 and 8 show the running time of DivBiclust on two different types of datasets. Because the HUM and MOU datasets have much smaller gene sets compared to the corresponding HUM_NZ and MOU_NZ datasets, the total running time is generally shorter. The only exception is that the running time on the HUM3 and HUM3_NZ datasets are roughly the same. The reason is that, when dealing with these two datasets with large cell sets, the main time consumption is for pattern merging. Because the number of cells in these two datasets are the same, the number of mined sc-biclusters for merging are very close and thus the time cost is similar with each other. On the other hand, even when $|T_s|$ is set to 30, the running time of DivBiclust on the HUM3_NZ dataset with more than 3000 cells is around 130 seconds. The running time on all the other datasets is no longer than 30 seconds. Thus, DivBiclust is efficient in dealing with both types of datasets.

3.3 Comparison with Related Methods

We list the ARI scores achieved by DivBiclust and nine state-of-the-art methods on the six nonzero datasets in Table 9. For each dataset, DivBiclust takes exactly the same parameter settings for the corresponding HUM or MOU datasets. The ARI scores achieved by DivBiclust are much higher than the scores achieved by the counterpart methods over all the datasets. The experiment results again well demonstrate the effectiveness of DivBiclust in identifying cell subpopulations from the scRNA-seq datasets.

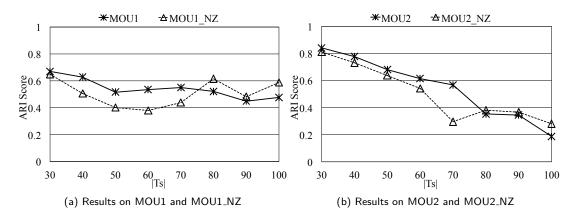


Figure 6: Comparison of ARI scores on MOU and MOU_NZ Datasets

Table 9: Comparisons of Clustering Accuracy*

M-41 1-	Datasets					
Methods	HUM1_NZ	$HUM2_NZ$	$HUM3_NZ$	$HUM4_NZ$	$MOU1_NZ$	MOU2_NZ
DivBiclust	0.894	0.887	0.854	0.925	0.649	0.810
SNN-Cliq	0.052	0.085	_†	0.334	-0.005	0.056
BackSPIN	0.016	0.001	0.038	0.004	0.007	0.007
CIDR	0.188	0.238	0.295	0.449	0.112	0.025
SC3	0.529	0.573	0.559	0.510	0.394	0.276
pcaReduce	0.307	0.351	0.392	0.339	0.327	0.214
TSCAN	0.407	0.570	0.614	0.532	0.456	0.325
Seurat v3	0.383	0.403	0.513	0.493	0.481	0.315
GiniClust2	0.396	0.470	0.423	0.299	0.551	0.305
SOUP	0.621	0.764	0.486	0.556	0.527	0.467

^{*} The largest ARI score over each dataset is highlighted using bolded font, and the second largest one is underlined.

4 Parameter Settings of Related Methods

In the paper, we compare *DivBiclust* with nine state-of-the-art method in terms of the accuracy for identifying cell subpopulations. These nine related methods are SNN-Cliq [13], BackSPIN [16], CIDR [8], SC3 [5], pcaReduce [18], TSCAN [4], Seurat v3 [2,11], GiniClust2 [12], and SOUP [17]. The source codes of all these methods are publicly downloaded, and their parameter settings are as follows.

- The SNN-Cliq method utilized an SNN-based graph and the SNN threshold is set to 3 as suggested in [13]. The similarity threshold for merging the quasi-cliques is fixed to 0.5, and this threshold plays the same role as the threshold β for pattern merging in our *DivBiclust* method.
- In the BackSPIN method, two parameters need to be specified. The number of selected genes determines the size of the matrix taken for partition-based biclustering. We either take 5000 genes as suggested in [16] or use the complete gene set. The depth of clustering controls the number of matrix splits, which is also tuned with the best ARI score being reported for every dataset.
- The CIDR method combines PCA with hierarchical clustering. We set the cluster number to be the same as the number of ground-truth cell clusters. The principal coordinates that are used in clustering are automatically estimated by a variation of the scree [3] method.

[†] SNN-Cliq cannot handle the HUM3_NZ dataset and generate the cell clustering.

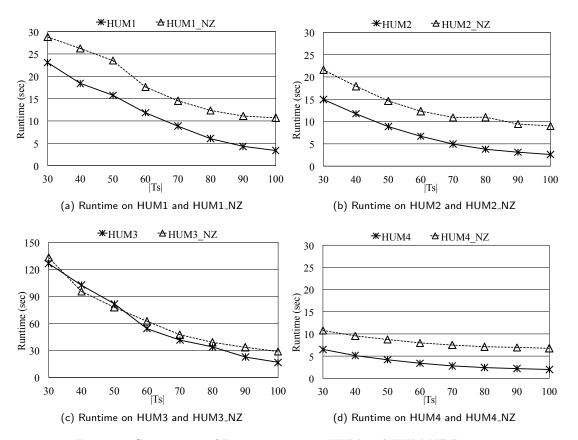


Figure 7: Comparison of Running Time on HUM and HUM_NZ Datasets

- The SC3 method involves a parameter K for K-means clustering. We studied the performance by either estimating K automatically or setting it to the number of cell clusters in the ground truth, and take the better result for each dataset.
- The pcaReduce method cannot determine the number of final cell clusters, and thus we set it to be the same as the number of clusters in the ground truth. Moreover, pcaReduce is a randomized algorithm, and so we run it for 10 times and report the highest ARI score for each dataset.
- The TSCAN method adopts a two-way clustering, where the number of gene clusters is fixed to 5% of the total number of genes. The optimal cell cluster number is selected by Bayesian Information Criterion (BIC) from a range of possible cluster numbers defined by user. We set the range to be [1, 15], which covers the number of ground-truth cell clusters in all the datasets.
- The Seurat v3 method involves a parameter to tune the granularity of the clustering result. The larger the value is, the more number of clusters is generated by the graph-based clustering algorithm Louvain. As suggested in [15], we set the parameter to 0.9.
- GiniClust2 is the integration of two clustering methods, GiniClust and K-means, where K is set to the number of cell clusters in the ground-truth.
- The SOUP method first performs K-means over a set of "pure cells", where K is set to the number of cell clusters in the ground-truth. The proportion of pure cells is set to 50% of the total number of cells in the dataset as suggested by the author.

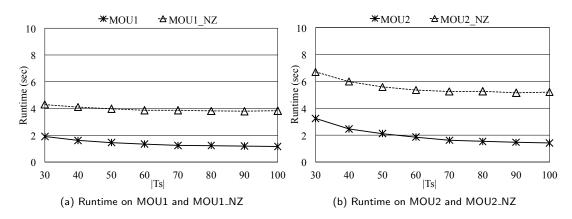


Figure 8: Comparison of Running Time on MOU and MOU_NZ Datasets

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