# Process Sequences



#### Recurrent Neural Networks

Jonathon Hare

Vision, Learning and Control University of Southampton

A lot of the ideas in this lecture come from Andrej Karpathy's blog post on the Unreasonable Effectiveness of RNNs (http://karpathy.github.io/2015/05/21/rnn-effectiveness/). Many of the images and animations and were made by Adam Prügel-Bennett.

# Recurrent Neural Networks - Motivation

$$x$$
: Jon and Ethan gave deep learning lectures  $y$ : 1 0 1 0 0 0 0

Jonathon Hare RNNs 3 / 21

#### Recurrent Neural Networks - Motivation

$$x: x^{(1)} \dots x^{(t)} \dots x^{(T_x)}$$
 $x: Jon \dots Ethan \dots lectures$ 
 $y: y^{(1)} \dots y^{(t)} \dots y^{(T_y)}$ 
 $y: 1 \dots 1 \dots 0$ 

In this example,  $T_x = T_y = 7$  but  $T_x$  and  $T_y$  can be different.

#### Recurrent Neural Networks

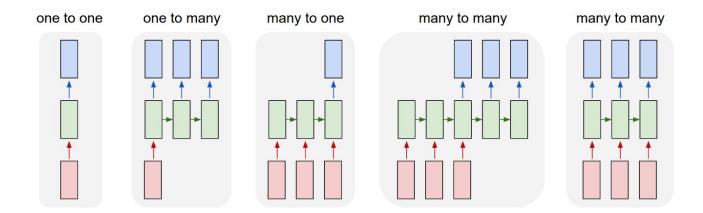


Image from http://karpathy.github.io/2015/05/21/rnn-effectiveness/

Jonathon Hare RNNs 5 / 21

# Aside: One Hot Encoding

How can we represent individual words (or other discrete tokens)?

"a" "abbreviations"

0

0

0 1 0 . . . 0

"zoology"

0

0 1 0 . . . . 0 0

1

"zoom"

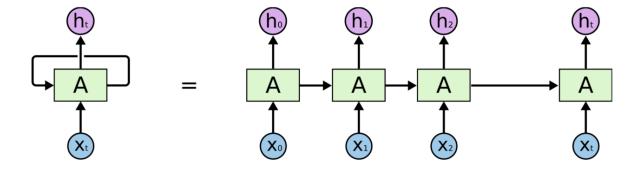
Image from https://ayearofai.com

# Why Not a Standard Feed Forward Network?

- For a task such as "Named Entity Recognition" a MLP would have several disadvantages
  - The inputs and outputs may have varying lengths
  - The features wouldn't be shared across different temporal positions in the network
    - Note that 1-D convolutions can be (and are) used to address this, in addition to RNNs more on this in a later lecture
- To interpret a sentence, or to predict tomorrows weather it is necessary to remember what happened in the past
- To facilitate this we would like to add a feedback loop delayed in time

Jonathon Hare RNNs 7 / 21

#### Recurrent Neural Networks



1

- RNNs are a family of ANNs for processing sequential data
- RNNs have directed cycles in their computational graphs

<sup>&</sup>lt;sup>1</sup>Image taken from https://towardsdatascience.com

#### Recurrent Neural Networks

RNNs combine two properties which make them very powerful.

- ① Distributed hidden state that allows them to store a lot of information about the past efficiently. This is because several different units can be active at once, allowing them to remember several things at once.
- Non-linear dynamics that allows them to update their hidden state in complicated ways<sup>2</sup>.

Jonathon Hare RNNs 9 / 21

#### Recurrent Neural Networks

RNNs are Turing complete in the sense they can simulate arbitrary programs<sup>3</sup>.

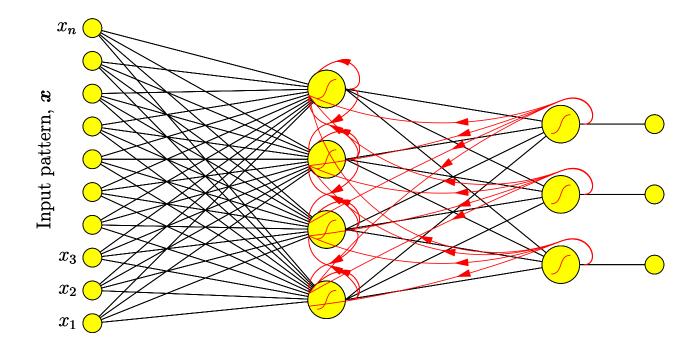
If training vanilla neural nets is optimisation over functions, training recurrent nets is optimisation over programs.

Jonathon Hare RNNs 10 / 21

<sup>&</sup>lt;sup>2</sup>Often said to be difficult to train, but this is not necessarily true - dropout can help with overfitting for example

<sup>&</sup>lt;sup>3</sup>Don't read too much into this - like universal approximation theory, just because they can doesn't mean its necessarily learnable!

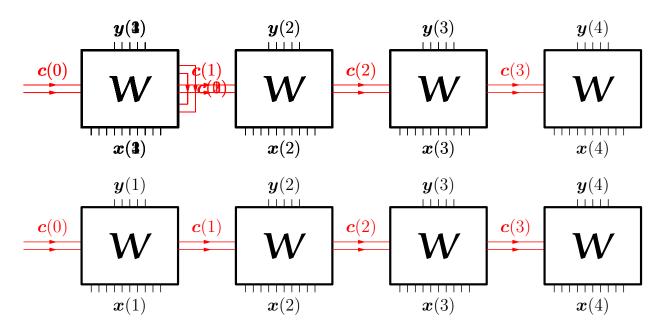
#### Recurrent Network



Jonathon Hare RNNs 11 / 21

# Training Recurrent Networks

ullet Given a set of inputs  $\mathcal{D} = ig( (m{x}(t), m{y}(t)) ig| t = 1, \, 2, \, \ldots, \, T ig)$ 



RNNs

• Minimise an error (here MSE, but your choice):

Jonathon Hare

#### An RNN is just a recursive function invocation

- y(t) = f(x(t), c(t-1)|W)
- ullet and the state  $oldsymbol{c}(t) = oldsymbol{g}(oldsymbol{x}(t-1), oldsymbol{c}(t-1)|oldsymbol{W})$
- If the output y(t) depends on the input x(t-3), then prediction will be

$$f(x(t), g(x(t-1), g(x(t-2), g(x(t-3)|W), W), W), W)$$

 it should be clear that the gradients of this with respect to the weights can be found with the chain rule

Jonathon Hare RNNs 13 / 21

# What is the state update g()?

- It depends on the variant of the RNN!
  - Elman
  - Jordan
  - LSTM
  - GRU

### Elman Networks ("Vanilla RNNs")

$$egin{aligned} m{h}_t &= \sigma_h (m{W}_{ih}m{x}_t + m{b}_{ih} + m{W}_{hh}m{h}_{t-1} + m{b}_{hh}) \ m{y}_t &= \sigma_y (m{W}_ym{h}_t + m{b}_y) \end{aligned}$$

- $\sigma_h$  is usually tanh
- $\sigma_h$  is usually identity (linear) the y's could be regressed values or logits
- the state  $h_t$  is referred to as the "hidden state"
- the output at time t is a projection of the hidden state at that time
- the hidden state at time t is a summation of a projection of the input and a projection of the previous hidden state

Jonathon Hare RNNs 15 / 21

#### Going deep: Stacking RNNs

- RNNs can be trivially stacked into deeper networks
- It's just function composition:

$$y(t) = f_2(f_1(x(t), c_2(t-1)|W_1), c_2(t-1)|W_2)$$

- The output of the inner RNN at time t is fed into the input of the outer RNN which produces the prediction y
- Also note: RNNs are most often not used in isolation it's quite common to process the inputs and outputs with MLPs (or even convolutions)

Jonathon Hare RNNs 16 / 2

# Example: Character-level language modelling

- We'll end with an example: an RNN that learns to 'generate' English text by learning to predict the next character in a sequence
- This is "Character-level Language Modelling"

Jonathon Hare RNNs 17 / 21

## Example: Character-level language modelling

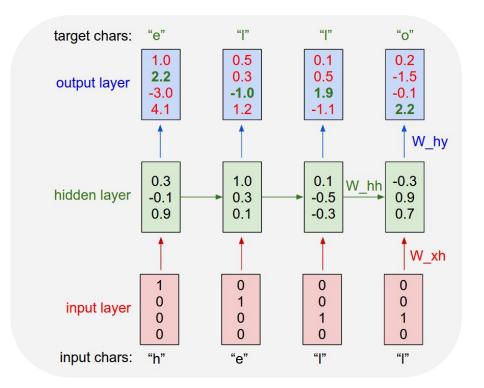


Image from http://karpathy.github.io/2015/05/21/rnn-effectiveness/

#### Training a Char-RNN

- The training data is just text data (e.g. sequences of characters)
- The task is unsupervised (or rather self-supervised): given the previous characters predict the next one
  - All you need to do is train on a reasonable sized corpus of text
  - Overfitting could be a problem: dropout is very useful here

Jonathon Hare RNNs 19 / 21

#### Sampling the Language Model

- Once the model is trained what can you do with it?
- if you feed it an initial character it will output the logits of the next character
- you can use the logits to select the next character and feed that in as the input character for the next timestep
- how do you 'sample' a character from the logits?
  - you could pick the most likely (maximum-likelihood solution), but this might lead to generated text with very low variance (it might be boring and repetitive)
  - you could treat the softmax probabilities defined by the logits as a categorical distribution and sample from them
    - you might increase the 'temperature', T, of the softmax to make the distribution more diverse (less 'peaky'):  $q_i = \frac{\exp(z_i/T)}{\sum_j \exp(z_j/T)}$

A lot of the ideas in this lectu on the input c(t-1), g(x) is (x(t-2), g(t-1)). (x(t-2), g(t-1)) lged snllhomitpon" ares Mnt Net) the pl

Onaafed a tre the sidisicters of to prediction couponet on the logits its venvows usts sevouvd be this in as useuled at on in the pan Lerate'atectsrray to paet inputs D = Pxxpraition the rople, the next vog the state atite

- Sampled from a single layer RNN<sup>4</sup>.

Jonathon Hare RNNs 21 / 21

<sup>&</sup>lt;sup>4</sup>LSTM, 128 dim hidden size, with linear input projection to 8-dimensions and output to the number of characters (84). Trained on the text of these slides for 50 epochs.