

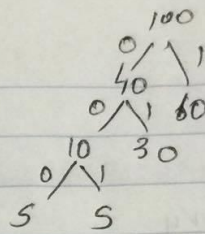
# CS323- LECTURE NOTES

4/7/2016 - aishwarya

4/6/16.

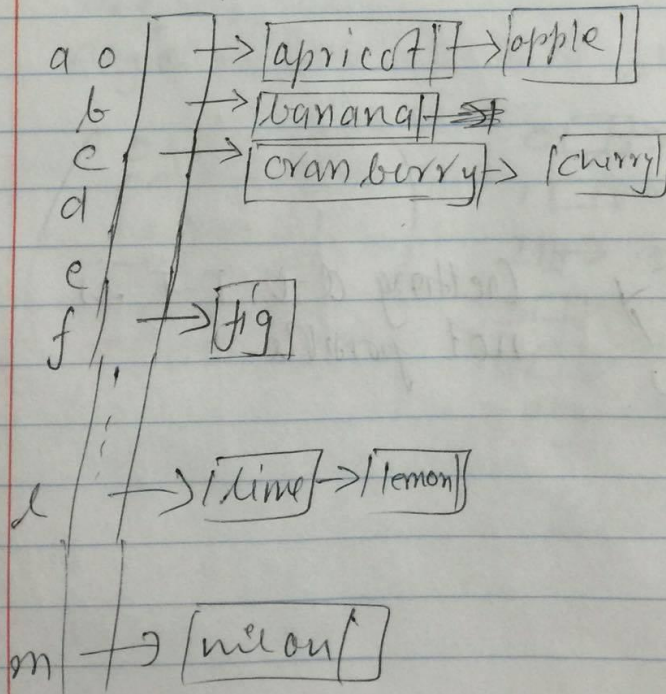
## Homework 2

	freq
a	60 $\times 2 \rightarrow 120$
b	5 $\rightarrow 10$
c	30 $\rightarrow 60$
d	5 $\rightarrow 10$
	<u>100</u> <u>200</u>



b=

prefix  
 (length 1) 60  
 (length 3) 19  
 (length 2) 60  
 (length 3) 19  
150



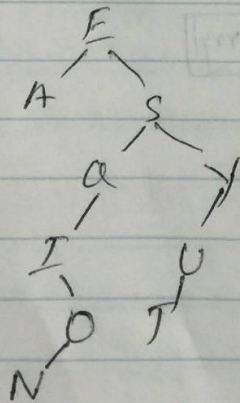
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- 0 apricot
- 1 banana
- 2 cranberry
- 3 apple
- 4 cherry
- 5 fig
- 6 date
- 7
- 8
- 9
- 10
- 11 lime
- 12 melon
- 13 lemon

probing  
from given  
data

Q3 →



Creating a-U-I-T is  
not possible.



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advantages to trie

- finding characters are easier and is quick.

disadvantage

- takes more space.

Q5 1) Directed Graph  $V = \{0, 1, 2, 3, 4, 5\}$

$E = \{(0, 1), (1, 2), (2, 1), (2, 0), (3, 2), (4, 5), (5, 4), (0, 4)\}$

- Does NOT have any loops

- Cycles  $\rightarrow 0 \rightarrow 1 \rightarrow 2 \rightarrow 0$   $1 \rightarrow 2 \rightarrow 1$   $4 \rightarrow 5 \rightarrow 4$

$$\deg^-(V_2) = 2$$

$$\deg^+(V_2) = 2$$

$$\begin{pmatrix} 0 & 1 & 0 & 0 & 1 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 1 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 & 1 & 0 \end{pmatrix}$$

chaining

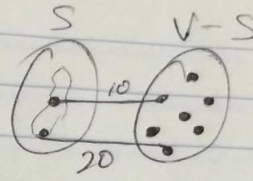
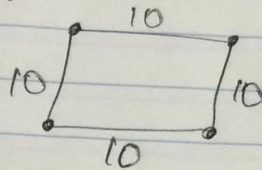
$0 \rightarrow 1 \rightarrow 2 \rightarrow 0$   
 $1 \rightarrow 2$   
 $2 \rightarrow 0 \rightarrow 1$   
 $3 \rightarrow 2$   
 $4 \rightarrow 5$   
 $5 \rightarrow 4$

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Prim's Algorithm  
Kruskal's Algorithm

min cost



its a graph  
80 vertices  
are connected.

do proof by contradiction

min cost  $\rightarrow$  cost of edge  
closest

for  $i = 1$  to  $n$

$\text{minCost}[i] = C[s, i]$

$\text{closest}[i] = s$

for  $i = 2$  to  $n$

(remaining vertices  
in  $V-S$ )

$j =$  Find closest minimum of minCost

for vertices still in  $V-S$ .

for each  
neighbour<sup>K</sup> of  $j$  in  $V-S$

~~for~~

if  $\text{minCost}[K] > C[j, K]$

$\text{minCost}[K] = C[j, K]$

$\text{closest}[K] = j$

Time  
Complexity

$O(|V|^2 + |V|^2) \rightarrow \text{improve}$

$\downarrow$  finding loop  $\downarrow$  heap  $\rightarrow |V| \log |V| + |E| \log |V|$



class workDijkstra's SSSP Algorithm

$distance[w]$  = shortest path known  
between source  $s$  and  $w$

$pred[w]$  = the vertex immediately  
before  $w$  on the path from  $s$  to  $w$

for vertices  $w \in V$   
 $distance[w] = \infty$   
 $pred[w] = s$   
end for

while  $q$  (priority min-heap queue) is not empty  
 $u = \text{getMin}(q)$   
for each neighbour  $v$  of  $u$   
if  $distance[u] + c[u, v] < distance[v]$   
 $distance[v] = distance[u] + c[u, v]$   
 $pred[v] = u$   
update  $q$  - priority of  $v$

time complexity  $\rightarrow O(|E| \log |V| + |V|)$

Amortized  
Analysis.

delete max  $V$  times.  
 $O(|E| + |V| \log |V|)$

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\$50  $\longrightarrow$  \$100  
10 years.

#5 APSP = all pairs shortest path  
(Single Source shortest Path can be applied)

for  $v \in V$

run Dijkstra's Algorithm with source  $v$

Dynamic Programming |  $f(0) = 0$   $f(1) = 1$   
 $f(n) = f(n-1) + f(n-2)$

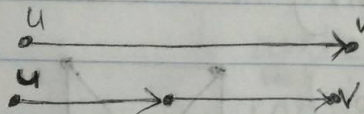
$f[0] = 0$

$f[1] = 1$

for  $i = 2$  to  $100$

$f[i] = f[i-1] + f[i-2]$

hybrid  $\rightarrow$  memoization



introduce intermediate  
nodes

optimal substructure

wrong way  $\rightarrow$  for  $i = 1$  to  $n$

for  $j = 1$  to  $n$

for  $k = 1$  to  $n$



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right

for  $k=1$  to  $n$

for  $i=1$  to  $n$

for  $j=1$  to  $n$

$c[i,j]$  cost of edge

distance is cost of path  $(k-1)$

if  $c[i,k] + d[k,j] < d[i,j]$

$d[i,j] = c[i,k] + d[k,j]$

$p[i,j] = p[k,j]$

Floyd's  
APSP Algo.

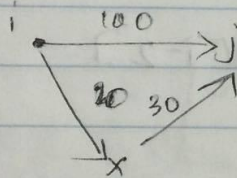
initialization

for  $i=1$  to  $n$

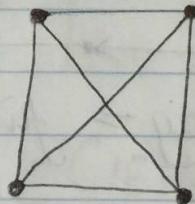
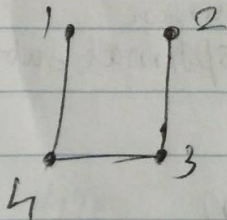
for  $j=1$  to  $n$

$d[i,j] = c[i,j]$

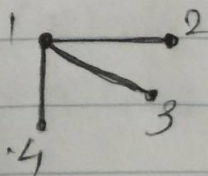
$p[i,j] = i$



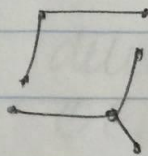
Minimum Spanning Tree (MST)



it is a tree  
but not  
a spanning  
tree.  
have to  
reach all  
vertices



if



this one  
is no spanning  
tree