

Lecture #9

Topics:

Lamport's Bakery Algorithm

Two assertions necessary for the Mutual Exclusion proof

Readings: Lecture on the web
Class notes

Bibliography: [SH] 3.5.2.
[GA] 3.3.3., 3.6.1

Software Implementation – Lamport's Bakery Algorithm

CPU_i

Shared variables: **choosing**, **number** (integer arrays[1..N]);
Initialized to false and 0.

While(true) {

```
L1:  choosing[i] = 1;
      number[i] = 1 + max(number[1], ..., number[N]);
      choosing[i] = 0;
      for (int j = 1; j <= N; j++) {
L2:    while (choosing[j] = 1) {}
L3:    while(number[j] <> 0 and (number[j],j) < (number[i], i)) {}
      }
```

Critical Section

```
      number[i] = 0;
    }
```

Note: $(a, b) > (c, d)$ iff $(a > c)$ OR $[(a == c) \text{ AND } (b > d)]$

Assertions that are used in proving **Mutual Exclusion** for the Bakery Algorithm

Assertion 1: if processes i and k are in the bakery, and i entered the bakery before k entered the doorway, then $\text{number}[i] < \text{number}[k]$ (1)

Assertion 2: if process i executes its Critical Section, and process k is in the bakery ($k \neq i$) then $(\text{number}[i], i) < (\text{number}[k], k)$ (2)