

$$\sum_{f \in \mathcal{F}} P_f = \sum_{h \in \mathcal{H}} D_h$$

Ground Route

Datas :

All the costs(variables and fixed costs).

P_f : production of factory f wich belings to $F=\{f_1... f_n\}$

D_h : demands of hubs h belonging to $H=\{h_1...h_m\}$

Objective : Minimize costs of transportation of the electric plugs from Factories to hubs.

Variables :

X_{od} : number of pallets sent from o to d .

T_{od} : number of trucks sent from o to d .

Ground Route

Objective function :

Min $\sum (o \text{ in } F) \sum (d \text{ in } H) [X_{od}.CT_{Pod} + T_{od}.CT_{od}]$

Constraints :

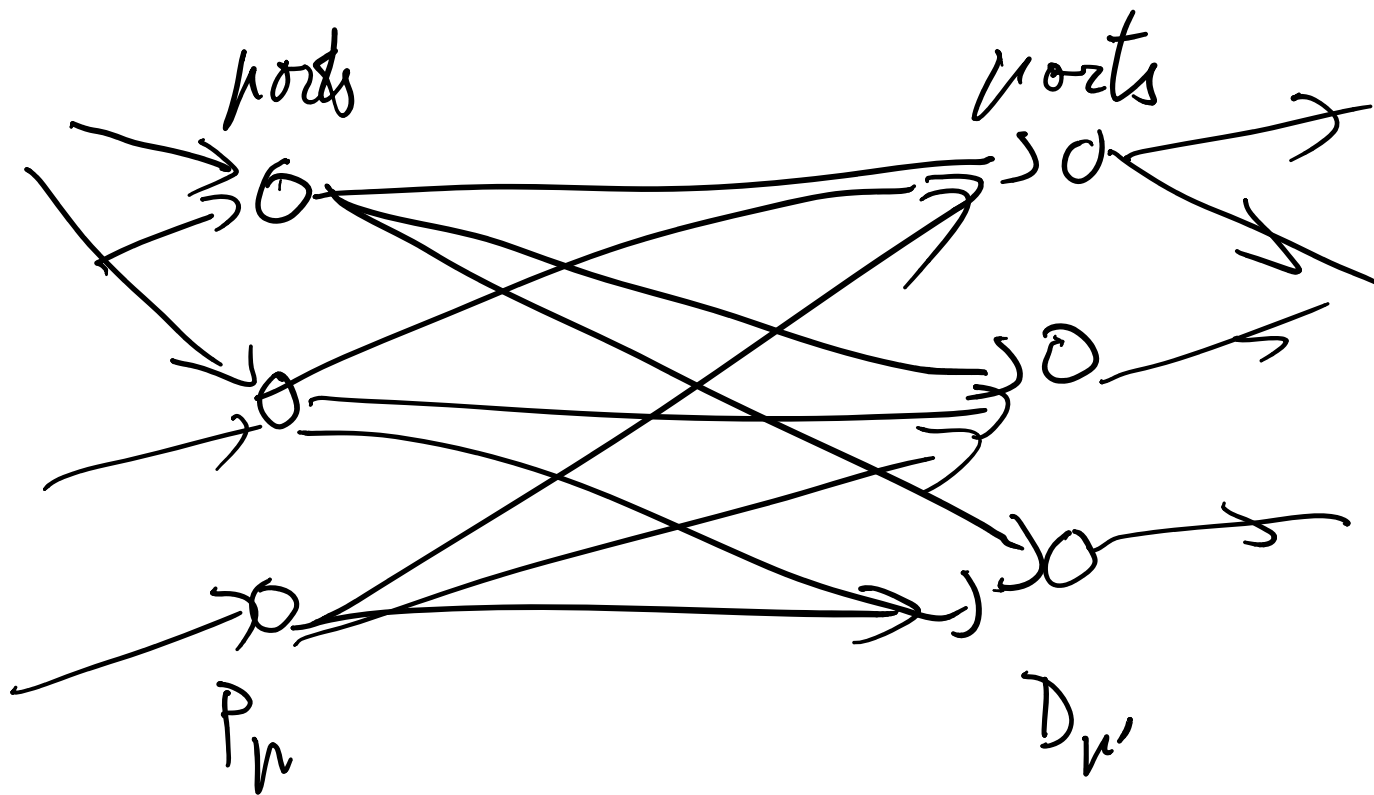
$X_{od} \leq N9.T_{od}$; For all $o \text{ in } F$ and $d \text{ in } H$ (Capacity constraint)

Flow constraints :

$0 - \sum (o \text{ in } F) X_{od} = -D_d$ (for all $d \text{ in } H$)

$\sum (d \text{ in } H) X_{od} - 0 = P_o$ (for all $o \text{ in } F$)

X_{od}, T_{od} belongs to N



$$\sum_{n \in \text{ports}} P_n = \sum_{n' \in \text{ports}} D_{n'}$$

Maritime Route

Data :

Assumption : $\sum (o \text{ in } P) P_o = \sum (d \text{ in } P) D_d$

Costs for maritime route. P_o : production at the departure ports.

D_d : Demand at the arrival ports.

P is a set of ports. o are departure ports, d are destination ports.

Variables :

X_{lod} : nb of individual pallets sent by boats from o ($o \text{ in } P$) to d ($d \text{ in } P$) $P = \{p_1 \dots p_j\}$ related to CBPod

Z_{11od} : Nb of containers N11 sent from o to d related to CBN11od

X_{11od} : Nb of pallets transfered into N11 containers

Z_{22od} : nb of containers N22 sent from o to d related to CBN22od

X_{22od} : Nb of pallets transfered into N22 containers.

Y_{od} : binary, 1 if a pallet or more is sent from o to d , else 0. related to CBFCod

X_{od} : nb of pallet sent from o to d . related to CBPCod

Maritime Route

Objective function :

Min $\sum (o \in P) \sum (d \in P) [X_{lod}.CB_{Pod} + Z_{11od}.CB_{N11od} + Z_{22od}.CB_{N22od} + Y_{od}.CB_{FCod} + X_{od}.CB_{PCod}]$

Constraints :

$\sum (d \in P) X_{od} - O = P_o$ for all $o \in P$ (Departure ports)

$O - \sum (o \in P) X_{od} = -D_d$ for all $d \in P$ (Arrival ports)

$X_{od} \leq M.Y_{od}$ for all $o \in P$ and $d \in P$

$X_{11od} \leq N_{11}.Z_{11od}$ for all $o \in P$ and $d \in P$

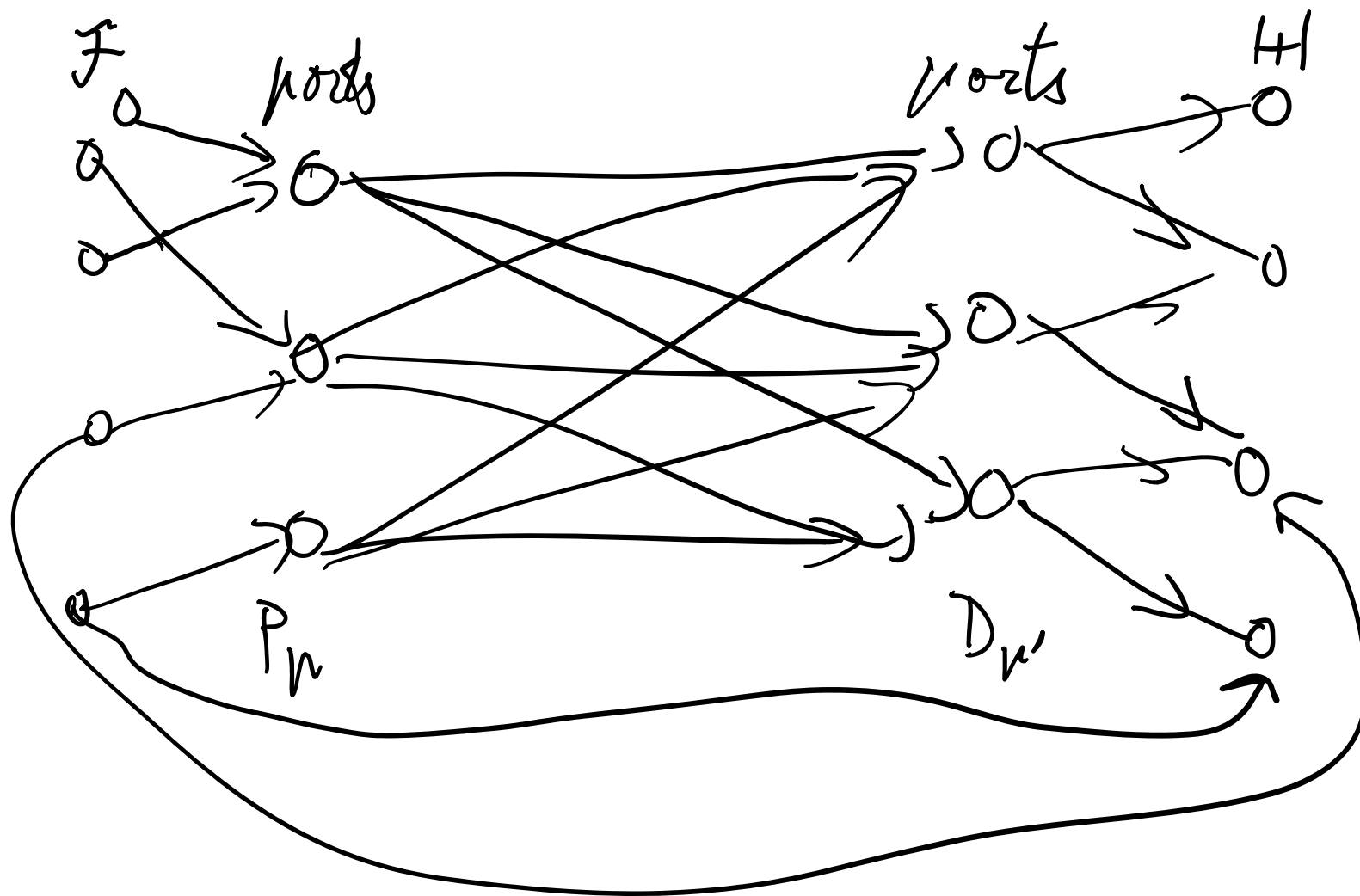
$X_{22od} \leq N_{22}.Z_{22od}$ for all $o \in P$ and $d \in P$

$X_{lod} + X_{11od} + X_{22od} = X_{od}$ for all $o \in P$ and $d \in P$ (*the total number of pallets sent in N11 containers or N22 containers or individually from o to d equals Sum of all the pallets sent by boat from o to d*) => Conservation constraint.

Domain definition :

$X_{lod}, X_{11od}, X_{22od}, X_{od}, Z_{11od}, Z_{22od}$ belongs to N^+ (positive integers)

Y_{od} belongs to $\{0;1\}$ (binary)



$$\sum_{f \in F} P_f$$

=

$$\sum_{h \in H} D_h$$

Merging the maritime and ground route

Constraints :

$X_{od} \leq N9.T_{od}$; For all o in FUP and d in HUP \- (od in P.P) (*Capacity constraint, applies only to transfer from factories to ports or hubs, or from ports to hubs*)

$\sum_{d \in PUH} X_{od} - O = P_o$ for all o in F

$O - \sum_{o \in PUF} X_{od} = -D_d$ for all d in H

$\sum_{o \in P+} X_{od} - \sum_{d \in P-} X_{do} = 0$ for all o in P (*what goes inside the ports goes out*).

Constraints for maritime Route :

$X_{od} \leq M.Y_{od}$ for all o in P and d in P

$X_{11od} \leq N11.Z_{11od}$ for all o in P and d in P

$X_{22od} \leq N22.Z_{22od}$ for all o in P and d in P

$X_{lod} + X_{11od} + X_{22od} = X_{od}$ for all o in P and d in P (*the total number of pallets sent in N11 containers or N22 containers or individually from o to d equals Sum of all the pallets sent by boat from o to d) => Conservation constraint.*

Merging the maritime and ground route

Objective Function :

Min (sum (o in FUP) sum (d in HUP) [Xod.CTPod + Tod.CTod]) + (sum (o in P) sum (d in P) [Xlod.CBPod + Z11od.CBN11od + Z22.CBN22od + Yod.CBFCod + Xod.CBPCod])

Ground route

Maritime Route