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# Introduction to Genetic Algorithms (GAs)

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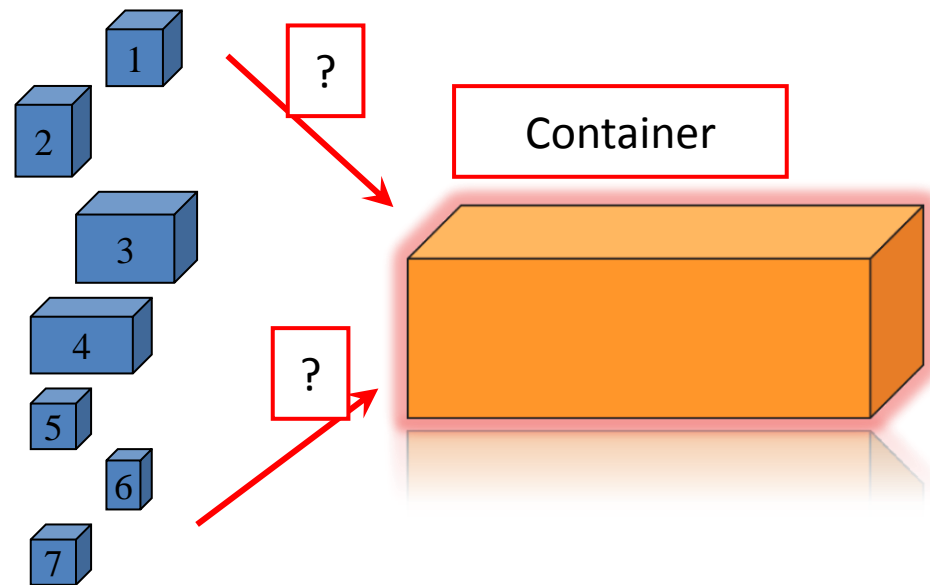
2012-07

## **Example:** **Allocation of Boxes into container**

**Objective:** Maximum Profit

**Constraints:** Weight - 2100 lbs  
capacity - 12 m<sup>3</sup>

Cargo	Volume (m <sup>3</sup> )	Weight (lb)	Value (\$1000)
1	3	400	3
2	4	500	6
3	6	200	4
4	5	600	9
5	2	250	4
6	1	300	2
7	2	350	5







## Excel Solver

<b>Objective</b>											
<b>MAX</b>	<b>Profit</b>										
<b>Variable</b>	<b>x1</b>	<b>x2</b>	<b>x3</b>	<b>x4</b>	<b>x5</b>	<b>x6</b>	<b>x7</b>		<b>Results</b>		
	0	1	0	1	0	1	1	=	22		
<b>Coefficient</b>	3	6	4	9	4	2	5				
<b>Subject to</b>											
	<b>x1</b>	<b>x2</b>	<b>x3</b>	<b>x4</b>	<b>x5</b>	<b>x6</b>	<b>x7</b>	<b>Summation</b>			
	3	4	6	5	2	1	2	12	<=	12	
	400	500	200	600	250	300	350	1750	<=	2100	

**Solver Parameters**

Set Target Cell:  

Equal To: ☒ Max ☐ Min ☐ Value of:

By Changing Cells:  

Subject to the Constraints:

\$C\$5:\$I\$5 = binary

\$J\$10:\$J\$11 <= \$L\$10:\$L\$11



## Genetic Evolution Example: 1 Gene

Initial	1	0	0	1	0	0	0	=	Profit 12
Evolution									
1	1	0	0	1	1	0	0	=	16
2	1	0	0	1	1	0	1	=	21
3	0	0	0	1	1	0	1	=	18
4	0	0	0	1	1	1	1	=	20
5	0	0	0	1	0	1	1	=	16
6	0	1	0	1	0	1	1	=	22



## Genetic Evolution

Example: **More** genes (certain part)

Initial 

1	0	0	1	0	0	0
---	---	---	---	---	---	---

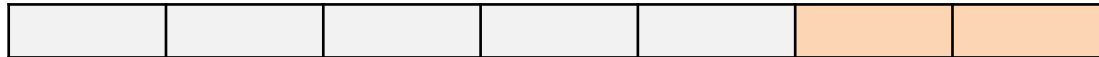
 = Profit 12

Evolution

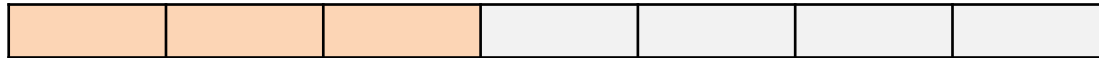
1



2



3



4



5



6





- (I) Design Chromosome**
- (II) Fitness Value**
- (III) Evolution Process**
  - **Mating Pool**
  - **Crossover**
  - **Mutation**
- (IV) Stopping Condition**



GAs was proposed by Holland in 1975

## Idea of GAs

- To mimic a biological evolutionary process.

## Two main Parts:

- Chromosome Design
- Genetic Operators Design



## Encoding of chromosome

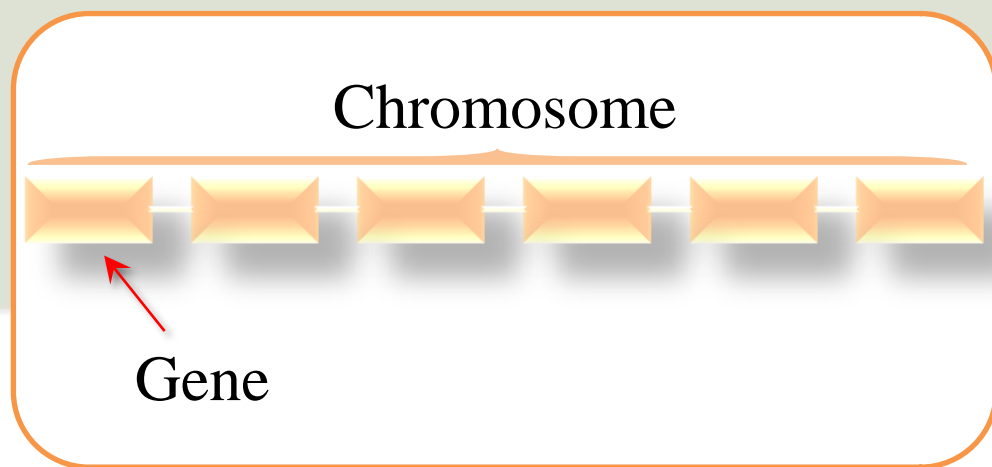
- The first step in GAs is to design and encode a chromosome.

## Chromosome function

- Represents a feasible solution of the problem.
- Consists of a number of Genes
- The length of a chromosome depends on the problem and the designer of the GAs.

## Gene

- Binary integer: 0 or 1.
- Real number.

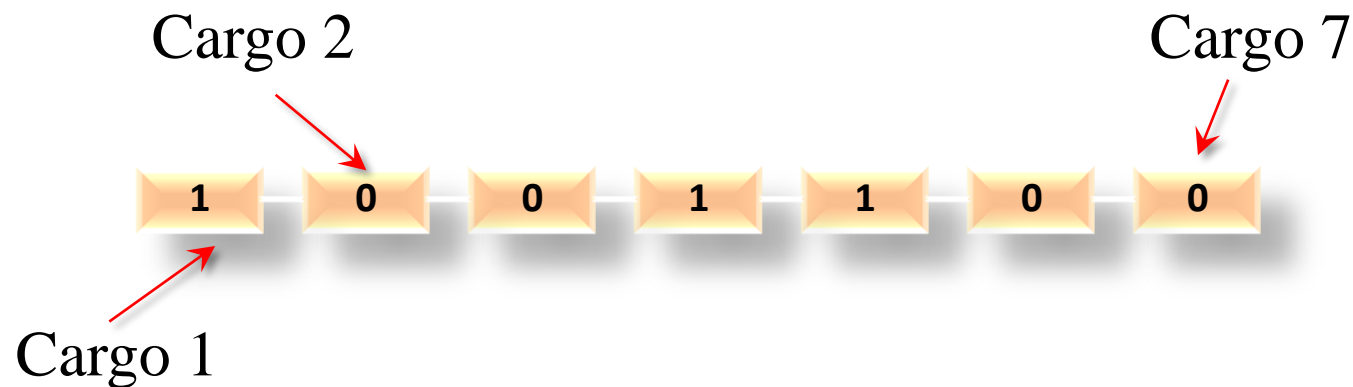






## Allocation Example

- Each gene represents 1 cargo.
- The chromosome consists of 7 genes
- If the cargo is in, then represents by 1 otherwise 0.

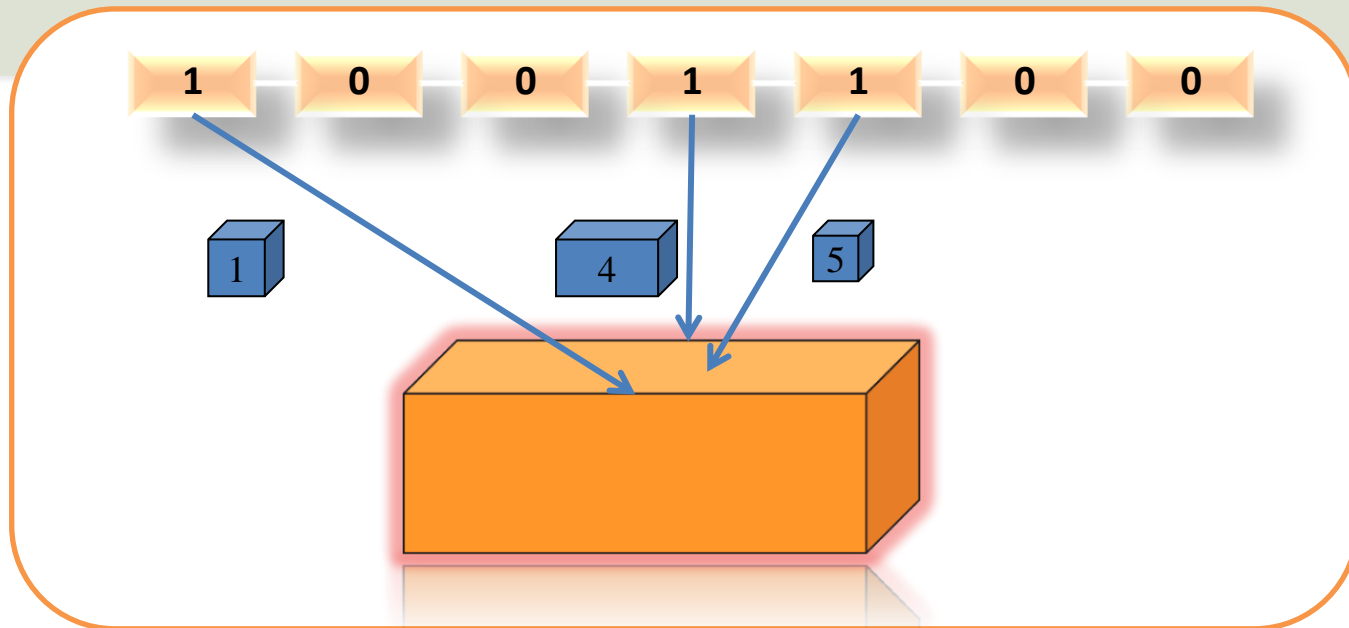




## Decoding of Chromosome

- It means how to interpret the chromosome.
- Explain how to convert the chromosome into a solution.

## Allocation Example





## Validation

- Check the chromosome validity.
- A chromosome is valid if it does not violate the constraints.

## Allocation Example



Cargo	Volume (m <sup>3</sup> )	Weight (lb)
1	3	400
2	4	500
3	6	200
4	5	600
5	2	250
6	1	300
7	2	350

Cargo	Volume	Weight
1	3	400
4	5	600
5	2	250
<b>Total</b>	10	1250

Constraints	12	2100
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Valid



## Question

Can we design the chromosome by using  
**Real Value?**



## Encoding with Real Value

- Cargo's sequence to put in the container.
- Count until the constraints violated.

Cargo	Volume (m <sup>3</sup> )	Weight (lb)
1	3	400
2	4	500
3	6	200
4	5	600
5	2	250
6	1	300
7	2	350

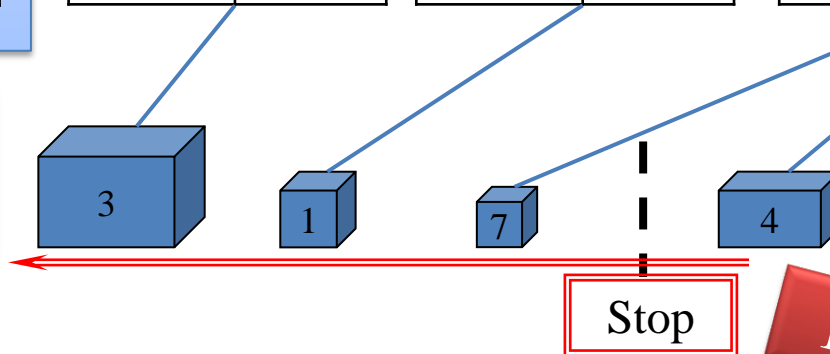


Cargo	3
Volume	6
Weight	200
Value	4

Cargo	3,1
Volume	9
Weight	600
Value	7

Cargo	3,1,7
Volume	11
Weight	950
Value	12

Cargo	3,1,7,4
Volume	16
Weight	1550
Value	21



**Invalid**

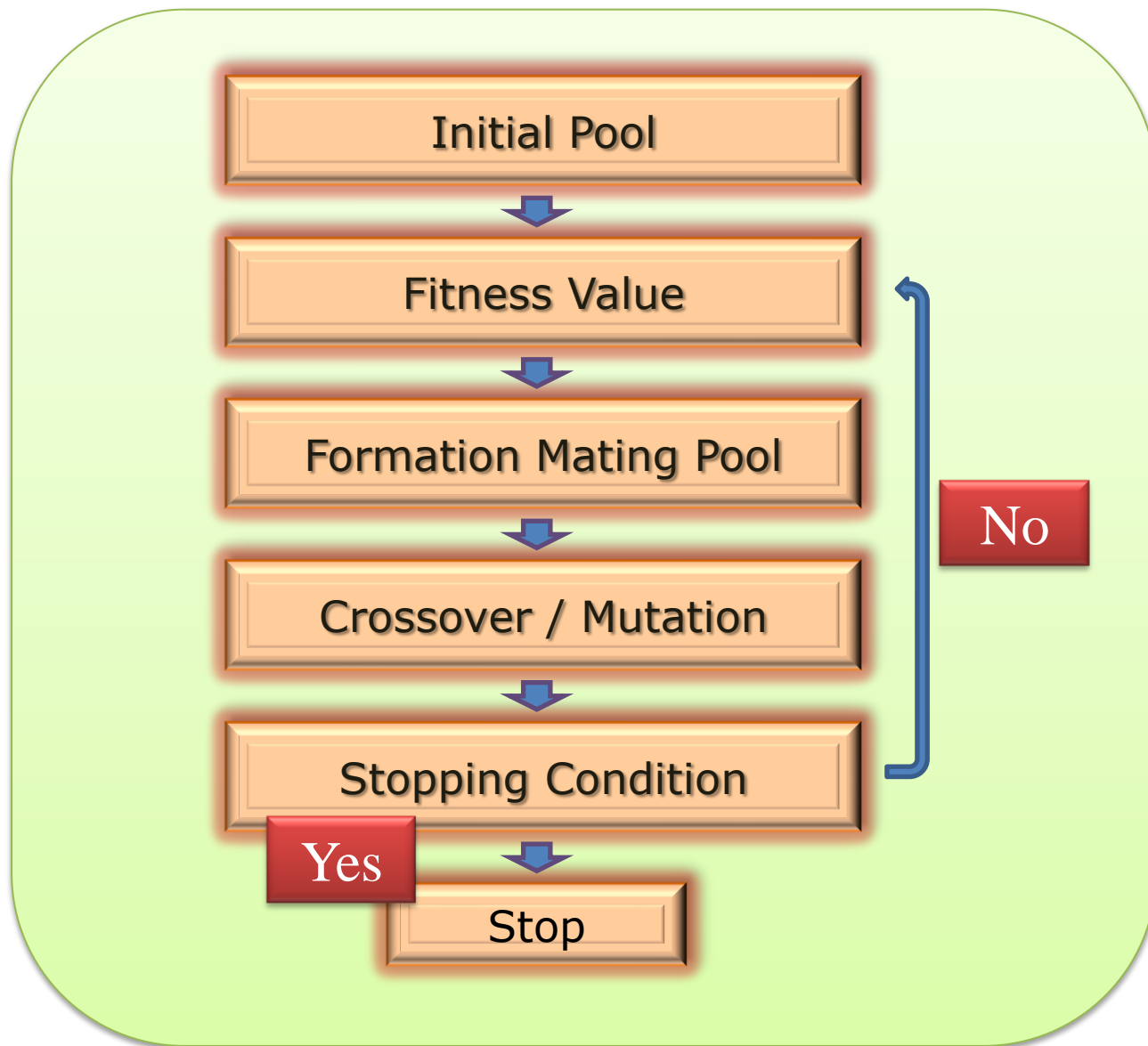


## Summary : Encoding of Chromosome

**Skills:**

Real/Binary Value  
Sequence/Position

**Avoid:** Lengthy chromosome



## Formation of Initial Pool

- Evolution started based on the initial pool.
- A Pool of chromosomes

## Ways of Forming:

- Totally Random.
- Rules

## Allocation Example

- Highest Profit
- Smallest Size
- Lightest Weight

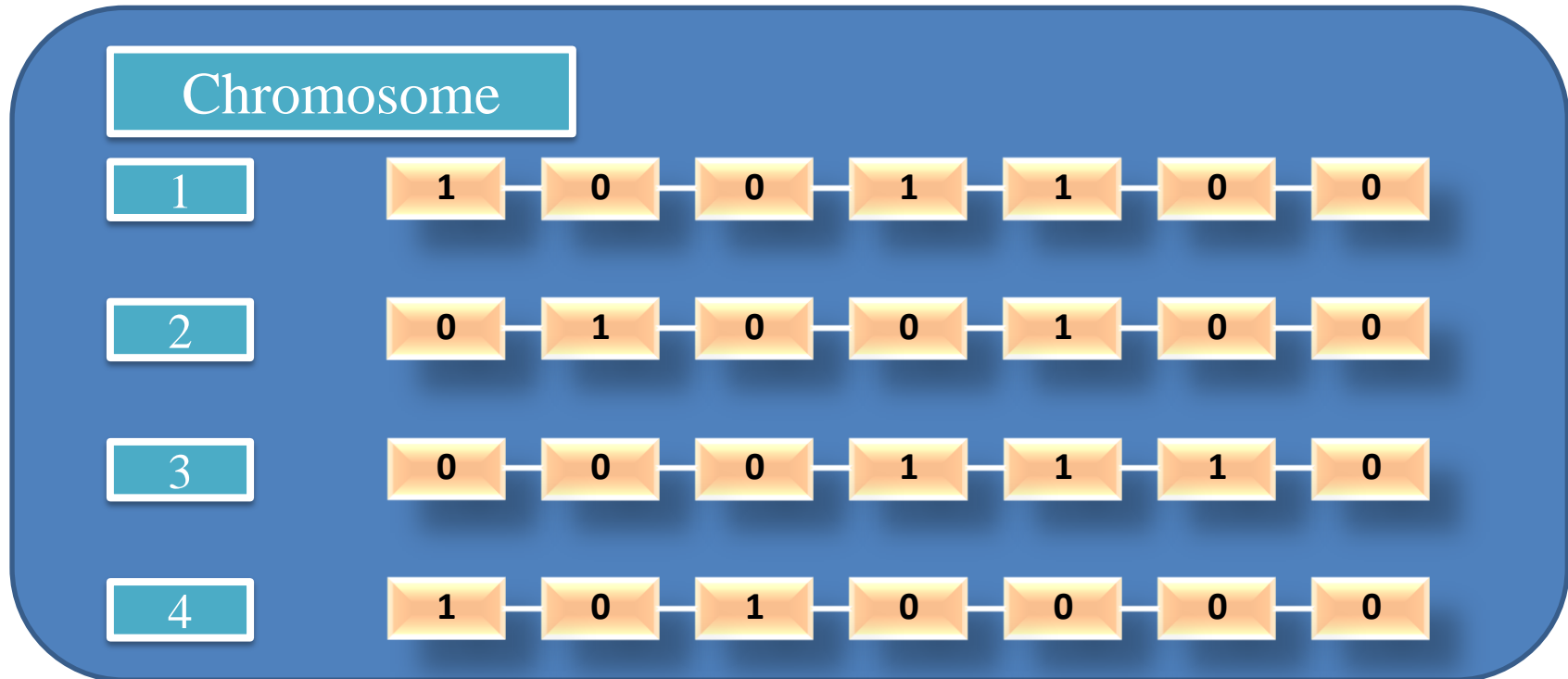
Cargo	Volume (m <sup>3</sup> )	Weight (lb)
1	3	400
2	4	500
3	6	200
4	5	600
5	2	250
6	1	300
7	2	350





## Allocation Example

- Initial Pool Size: 4



## Pool Size

- Commonly around 10 to 100



## Fitness value

- Represents the strength/goodness of the chromosome.
- It means how good this solution is.
- A **large** fitness value, meaning a **good** chromosome

## Allocation Example

$$\text{Fitness Value} = 3k + 9k + 4k = 16k$$



Cargo	Value (\$1000)
1	3
2	6
3	4
4	9
5	4
6	2
7	5



## Allocation Example

Chromosome								Fitness Value
1	1	0	0	1	1	0	0	16
2	0	1	0	0	1	0	0	10
3	0	0	0	1	1	1	0	15
4	1	0	1	0	0	0	0	7



## Purpose of Mating Pool

- Crossover and Mutation

## Remark

- Number of chromosomes in Mating Pool = Number of chromosomes in Initial Pool.

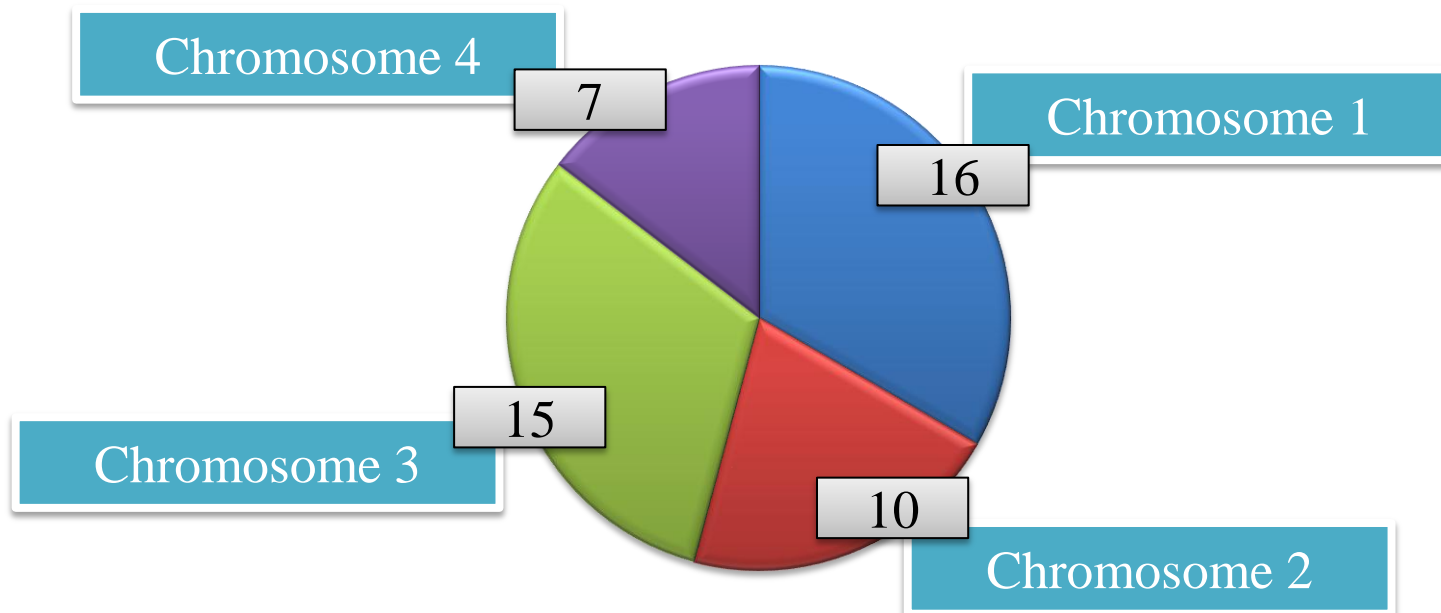
## Forming Method

- Roulette Wheel Selection.



## Roulette Wheel Selection

- Mimic the idea of survive of the best





## Allocation Example

### Initial Pool

1	1	0	0	1	1	0	0	16
2	0	1	0	0	1	0	0	10
3	0	0	0	1	1	1	0	15
4	1	0	1	0	0	0	0	7

### Mating Pool

1	1	0	0	1	1	0	0	16
2	0	0	0	1	1	1	0	15
3	1	0	1	0	0	0	0	7
4	0	0	0	1	1	1	0	15



## Question: Design for Production Scheduling

- Chromosome
- Fitness Value

### Problem

10 Jobs and 3 Machines

Minimize Makespan

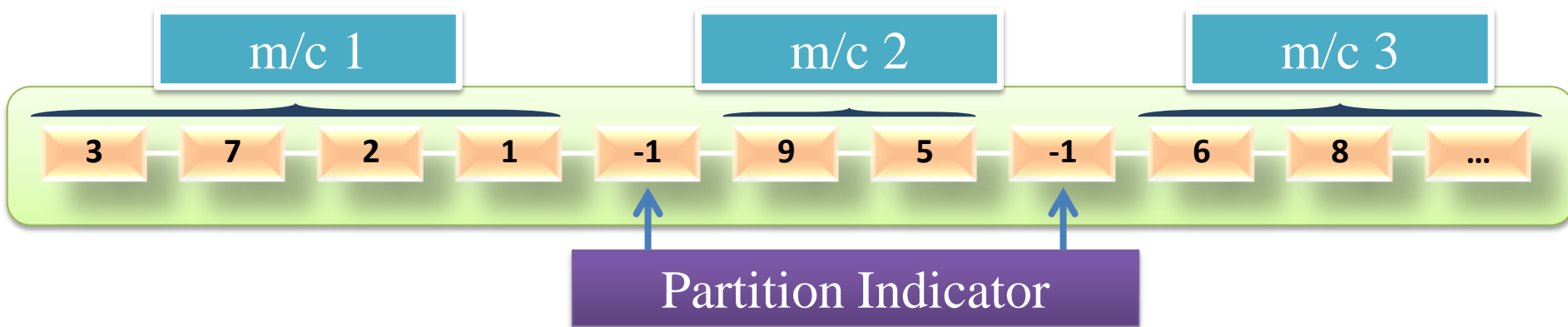
Job	PT	Job	PT
1	12	6	5
2	15	7	12
3	16	8	17
4	11	9	21
5	17	10	15

Setup Time	1	2	3	4	5	6	7	8	9	10
1	-	12	4	2	5	6	4	12	5	3
2	5	-	3	6	7	3	2	4	6	4
3	3	1	-	1	3	4	6	7	8	8
4	7	4	2	-	12	3	3	1	3	5
5	12	3	6	3	-	12	3	3	12	6
6	4	1	8	3	4	-	6	7	2	8
7	6	9	5	3	2	1	-	9	4	3
8	12	4	7	3	9	4	10	-	2	6
9	1	2	7	4	9	3	12	15	-	4
10	9	6	2	6	8	11	3	8	6	-





## Chromosome Encoding



Fitness Value of Chromosome  $i = 1 - 1/\text{makespan of } i$



## Skills

MIN		<b>=1-f/max</b>	<b>=1-f/Sum</b>
Chromo.		FV	FV
1	12	0.760	0.934
2	14	0.720	0.923
3	16	0.680	0.912
4	20	0.600	0.890
5	8	0.840	0.956
6	4	0.920	0.978
7	32	0.360	0.823
8	50	0.000	0.724
9	7	0.860	0.961
10	18	0.640	0.901