# Asset Pricing

Prof. Lutz Hendricks

Econ520

April 12, 2016

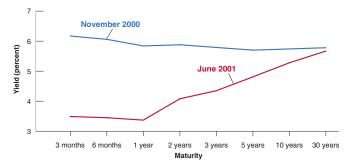
# **Objectives**

#### In this section you will learn:

- 1. how asset prices are determined as present discounted values of "dividends."
- 2. how asset prices are affected by policy.
- 3. how the yield curve can be used to predict future interest rates.

# Bond Yields The Yield Curve

#### The Yield Curve



The yield curve plots interest rates (yields) against bond maturities. Here: treasury bonds

#### **Bond Prices**

A discount bond pays \$100 in T years.

The price of a bond is the discounted expected present value of its payments

complication: risk

1 year discount bond:  $P_{1t} = \$100/(1+i_{1t})$ 

▶ this actually defines  $i_{1t}$ , the 1 year yield from t to t+1

$$1 + i_{1t} = \frac{\$100}{p_{1t}} \tag{1}$$

#### 2 year bond

#### 2 year discount bond:

- ightharpoonup price  $P_{2t}$
- ▶ payoff tomorrow:  $P_{1,t+1}$  (it's now a 1 year bond)
- without risk: it's 1 year return must be i<sub>1t</sub>

$$P_{2t} = \frac{P_{1,t+1}}{1 + i_{1,t}} = \frac{\$100}{(1 + i_{1,t})(1 + i_{1,t+1})}$$
(2)

Of course,  $i_{1,t+1}$  is not known at t – we must use its expected value

#### **Bond Prices**

Yield on 2 year bond:

the constant interest rate that produces the bond price as present value:

$$P_{2t} = \frac{\$100}{(1+i_{2t})^2} \tag{3}$$

Therefore:

$$(1+i_{2t})^2 = (1+i_{1,t})(1+i_{1,t+1})$$
(4)

Or approximately

$$i_{2,t} = \frac{1}{2}(i_{1,t} + i_{1,t+1}) \tag{5}$$

#### The Yield Curve

The yield curve plots yields against maturities If the yield curve is upward sloping:  $i_{1,t+1} > i_{1,t}$ 

agents expect rising short term interest rates

We can interpret the yield on a T year bond as the average short term interest rate agents expect over the next T years

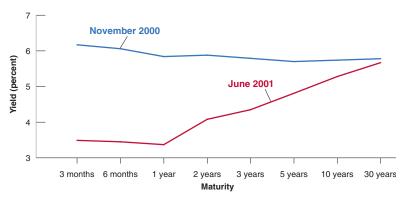
#### The Yield Curve

Long bond yields reveal investor expectations about future interest rates.

#### Qualifications:

- risk
- liquidity

# Example: The 2001 Recession



Nov-2000: the tail end of the tech bubble expansion

#### 2001 Recession

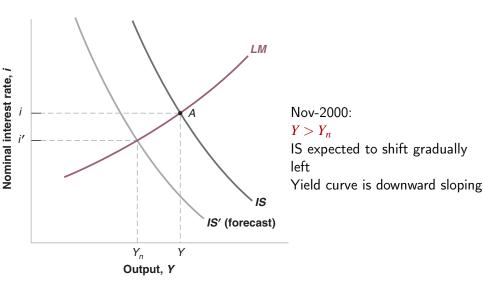
#### Nov-2000

- ► the Fed tries to slow growth with unemployment below the natural rate
- high short term interest rates
- ▶ expected slowdown of activity → lower long term interest rates

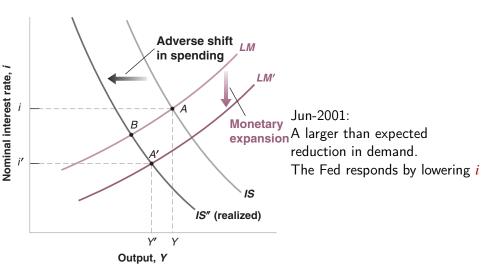
#### Jun-2001

- ▶ the tech bubble burst → recession
- the Fed lowers short term interest rates
- investors expect a recovery, but not soon
- the yield curve slopes upwards

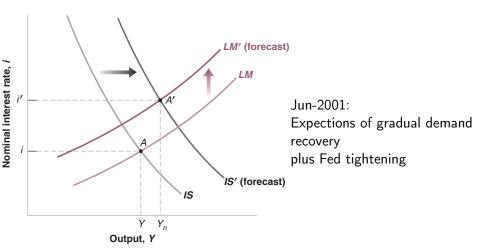
#### The 2001 Recession in the Model



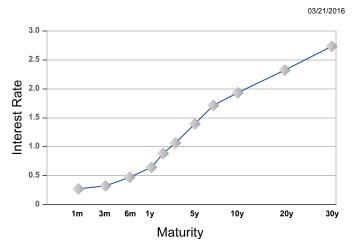
#### The 2001 Recession



# The 2001 Recession



#### The Current Yield Curve



Source: treasury.gov

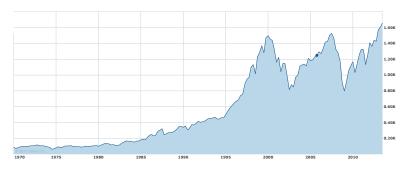
#### The Current Yield Curve

#### Key features:

- Liquidity trap short rates are essentially 0
- 2. Rates are below 2% up to maturities of 10 years investors expect low interest rates for a long time
- 3. Long yields are quite low (2.7% nominal) investors expect low inflation (or low real returns)

# The Stock Market

# The S&P 500



Source: yahoo.com

- Abstract from risk premia for now and assume
  - ▶ the return on stocks = the return on bonds
- ▶ Return on bonds:  $i_{1,t}$
- Return on stocks:
  - ightharpoonup t: invest  $Q_t$
  - ▶ t+1: earn dividend  $D_{t+1}$  and sell stock for  $Q_{t+1}$
  - rate of return:  $(D_{t+1} + Q_{t+1})/Q_t$

Equal rates of return

$$1 + i_{1,t} = \frac{D_{t+1} + Q_{t+1}}{Q_t} \tag{6}$$

Solve

$$Q_t = \frac{D_{t+1} + Q_{t+1}}{1 + i_{1,t}} \tag{7}$$

Now apply the same equation for  $Q_{t+1}$ 

$$Q_{t} = \frac{D_{t+1}}{1 + i_{1,t}} + \frac{D_{t+2} + Q_{t+2}}{(1 + i_{1,t})(1 + i_{1,t+1})}$$
(8)

Now apply the same for  $Q_{t+2}$ , then for  $Q_{t+3}$ , etc...

We end up with

$$Q_{t} = \frac{D_{t+1}}{Z_{t,1}} + \frac{D_{t+2}}{Z_{t,2}} + \frac{D_{t+3}}{Z_{t,3}} + \dots + \frac{D_{t+n}}{Z_{t,n}} + \frac{Q_{t+n}}{Z_{t,n}}$$
(9)

where

$$Z_{t,n} = (1 + i_{1,t})(1 + i_{1,t+1})...(1 + i_{1,t+n})$$
(10)

discounts payoffs in t+n to t.

How does this change with inflation?

#### Result

Stock prices equal the present discounted value of future dividends. This is called the fundamental value.

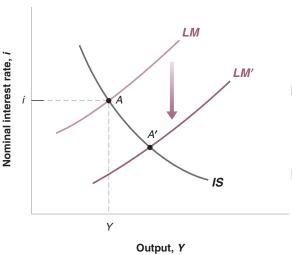
#### Implications:

- 1. High interest rates (now or in the future) depress stock prices.
- 2. Low dividends (now or in the future) depress stock prices.
- 3. Stock returns are generally unpredictable
  - 3.1 really: the difference between stock and bond returns is unpredictable
  - 3.2 this is called the **equity premium**

#### Caveats

- 1. Stocks are risky, so they generally earn higher returns than bonds
  - 1.1 We should discount by  $r_{1,t}$  plus a **risk premium**.
- 2. Stock prices often deviate from fundamental values for reasons that are not well understood
  - 2.1 The deviations are called **bubbles**

# Shocking the Stock Market

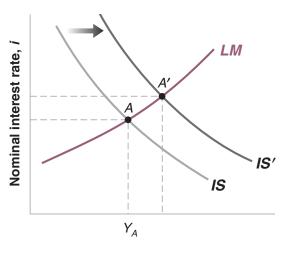


Monetary expansion:

- 1. Low interest rates
- 2. High future output and dividends

Both raise stock prices

# Rise in Consumption

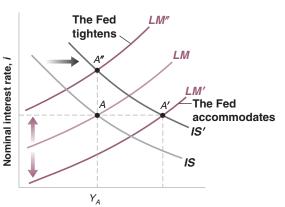


Two offsetting effects

- 1. higher Y
- 2. higher i

Change in stock prices is ambiguous

# Rise in Consumption



Possible Fed reactions:

- 1. Accomodate
- 2. Stabilize

One implication: No stable relationship between output and stock prices

#### Stocks Are Too Volatile

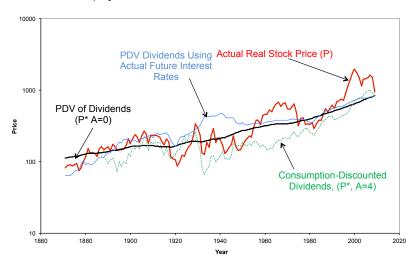
How volatile should stocks be?

A rough approximation:

- go to a period t (before today)
- collect data on future interest rates and dividends
- compute the present value of dividends
- compare with actual stock prices

#### Stocks Are Too Volatile

Comparing Actual Real Stock Price with Three Alternative PDVs of Future Real Dividends



Source: Robert Shiller (http://www.econ.yale.edu/~shiller/data.htm)

#### Stocks Are Too Volatile

#### Notes on the Shiller graph:

- Actual real price is the raw stock price, deflated with a price index
- 2. P\*, A=0: present value of dividends, assuming a constant interest rate
- 3. P\*, actual future interest rates: present value of dividends, discounted by realized future long-term interest rates
- 4. P\*, A=4: uses the Consumption Asset Pricing Model with risk aversion of 4

#### Each line is scaled such that

- 1. the terminal value equals that last observed stock price
- 2. the geometric mean of the growth rates is the same

The values are actually computed backwards as  $P_t = \frac{P_{t+1} + D_{t+1}}{1 + r_{t+1}}$ .

# Why Might Stocks Be so Volatile?

- 1. Tail risk:
  - stock prices include the risk of rare (bad) events e.g. major depressions; financial crises
- 2. Long-term risk: the long-run growth rate of dividends (or productivity) could fluctuate
- Bubbles: fluctuations are random; not related to fundamentals

# Asset Pricing With Risk

### What Is Risk?

Possible answers (with counter-examples):

# A Simple Model of Risk

A household lives for 2 periods. In period 1, he receives income y and eats  $c_1$ . In period 2, there are 2 possible states:

- 1. good state: income  $y_H$  with probability  $\pi_H$
- 2. bad state: income  $y_L$  with probability  $\pi_L$

Prefences:

$$u(c_1) + \underbrace{\pi_L u(c_L) + \pi_H u(c_H)}_{\text{expected utility in pd.}} 2$$
 (11)

# A Simple Model of Risk

#### There are 2 assets:

- 1. asset *L* pays 1 unit of consumption in state *L*
- 2. asset H pays 1 unit of consumption in state H

#### Budget constraints:

$$c_1 = y - p_L s_L - p_H s_H \tag{12}$$

$$c_L = y_L + s_L \tag{13}$$

$$c_H = y_H + s_H \tag{14}$$

#### Household Problem

$$\max_{s_L, s_H} u(y - p_L s_L - p_H s_H) + \underbrace{\sum_{j=L, H} \pi_j u(y_j + s_j)}_{\text{expected utility in pd 2}}$$
(15)

First-order conditions:

$$u'(c_1)p_j = \pi_j u'(y_j + s_j); j = L, H$$
 (16)

This solves for the household's willingness to pay for the assets:

$$p_j = \pi_j \frac{u'(c_j)}{u'(c_1)}, j = L, H$$
 (17)

#### Asset Prices

$$\frac{p_L}{p_H} = \frac{\pi_L}{\pi_H} \frac{u'(c_L)}{u'(c_H)} > 1 \tag{18}$$

Simplify by assuming that  $\pi_j = 1/2$ 

#### Result

An asset is valuable, if it pays in a state with low consumption (high marginal utility).

#### What Is Risk in the Model?

Safe asset: pays 1/2 in each state of the world.

$$p_{safe} = 0.5 (p_L + p_H) (19)$$

It follows that the "risky" asset  $p_L$  is more valuable (pays a lower expected return) than the safe asset:

$$p_H < p_{safe} < p_L \tag{20}$$

What then is risk?

#### **CAPM**

Consumption Asset Pricing Model.

Generalizes the logic of our simple model to many assets, many periods, and many states of the world.

#### Main result

An asset pays a high return, if its dividends are positively correlated with consumption (it pays out in good states of the world).

## **CAPM Asset Pricing Equation**

The price of an asset is the present value of dividends, discounted at the marginal rate of substitution:

$$p_{t} = \mathbb{E} \sum_{j=1}^{\infty} d_{t+j} \frac{u'(c_{t+j})}{u'(c_{t})}$$
 (21)

This is the basis for computing the  $\beta$  risk measure commonly used in finance.

Our 2 period model is a special case:

$$p_L = \pi_L \times 1 \times \frac{u'(c_L)}{u'(c_1)} + (1 - \pi_L) \times 0 \times \frac{u'(c_H)}{u'(c_1)}$$
 (22)

# Excess Volatility Puzzle

In the data, consumption is very smooth.

Therefore, u'(c) is very smooth.

The price of a stock should then equal the present value of smooth dividends, discounted at a roughly constant rate.

Stock prices should be smooth.

They are not.

## Equity Premium Puzzle

The same asset pricing equation should hold for a riskless bond. If consumption is very smooth, a riskless bond with a dividend of 100 should cost about the same as a a stock with a dividend of 100. The expected return on stocks and bonds should be very similar. They are not similar in the data.

# How severe is the puzzle?

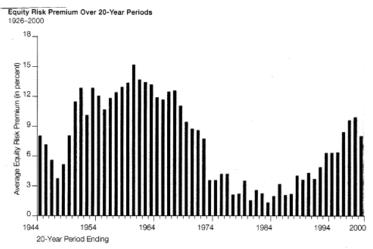
#### Investors forego very large returns.

Table 3  Terminal value of \$1 invested in Stocks and Bonds				
Investment Period	Stocks		T-bills	
	Real	Nominal	Real	Nominal
1802-1997	\$558,945	\$7,470,000	\$276	\$3,679
1926-2000	\$266.47	\$2,586.52	\$1.71	\$16.56

Source: Mehra and Prescott (2003)

# Long holding periods

Over 20 year holding periods: stocks dominate bonds.



Source: Mehra and Prescott (2003)

# Possible Explanations

What could explain the equity premium puzzle?

# Reading

▶ Blanchard and Johnson (2013), ch 15

#### Advanced Reading:

- ▶ Mehra and Prescott (1985): the paper that discovered the equity premium puzzle
- Mehra and Prescott (2003): later perspective on the equity premium puzzle

#### References I

- Blanchard, O. and D. Johnson (2013): *Macroeconomics*, Boston: Pearson, 6th ed.
- Mehra, R. and E. C. Prescott (1985): "The equity premium: A puzzle," *Journal of monetary Economics*, 15, 145–161.
- ——— (2003): "The equity premium in retrospect," *Handbook of the Economics of Finance*, 1, 889–938.